

# Crab Crossing design and Simulations

Salvador Sosa

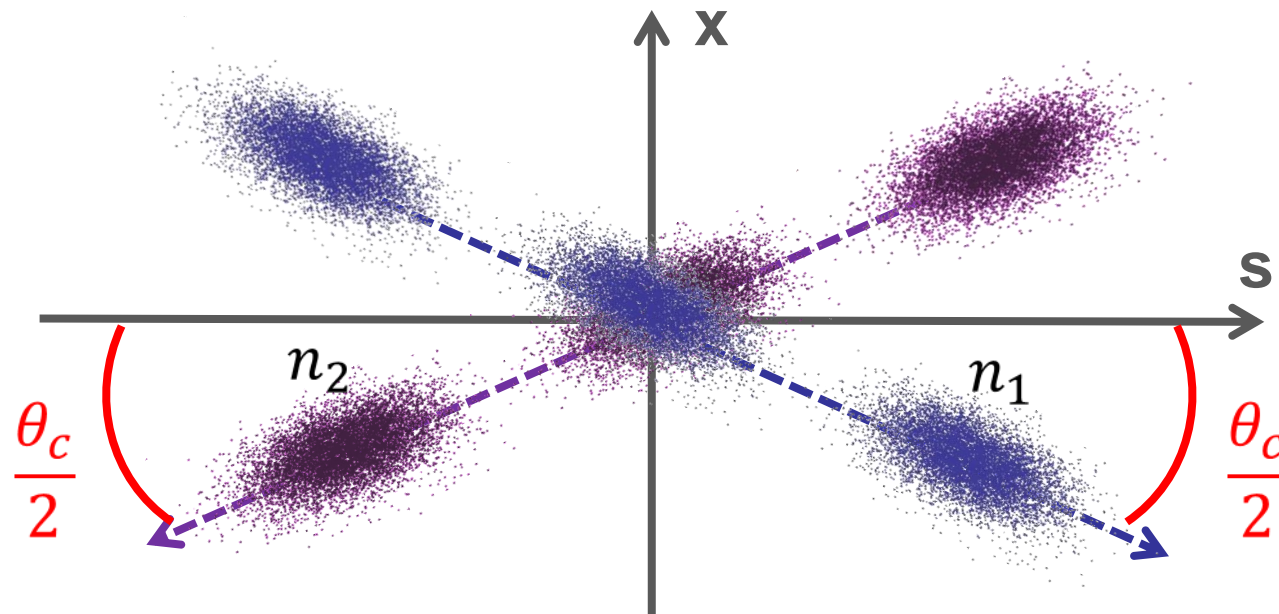
*Old Dominion University*

[ssosa006@odu.edu](mailto:ssosa006@odu.edu)

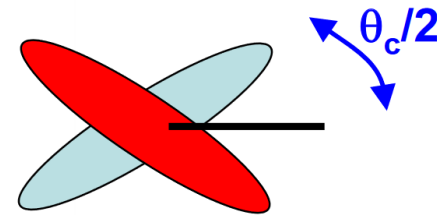
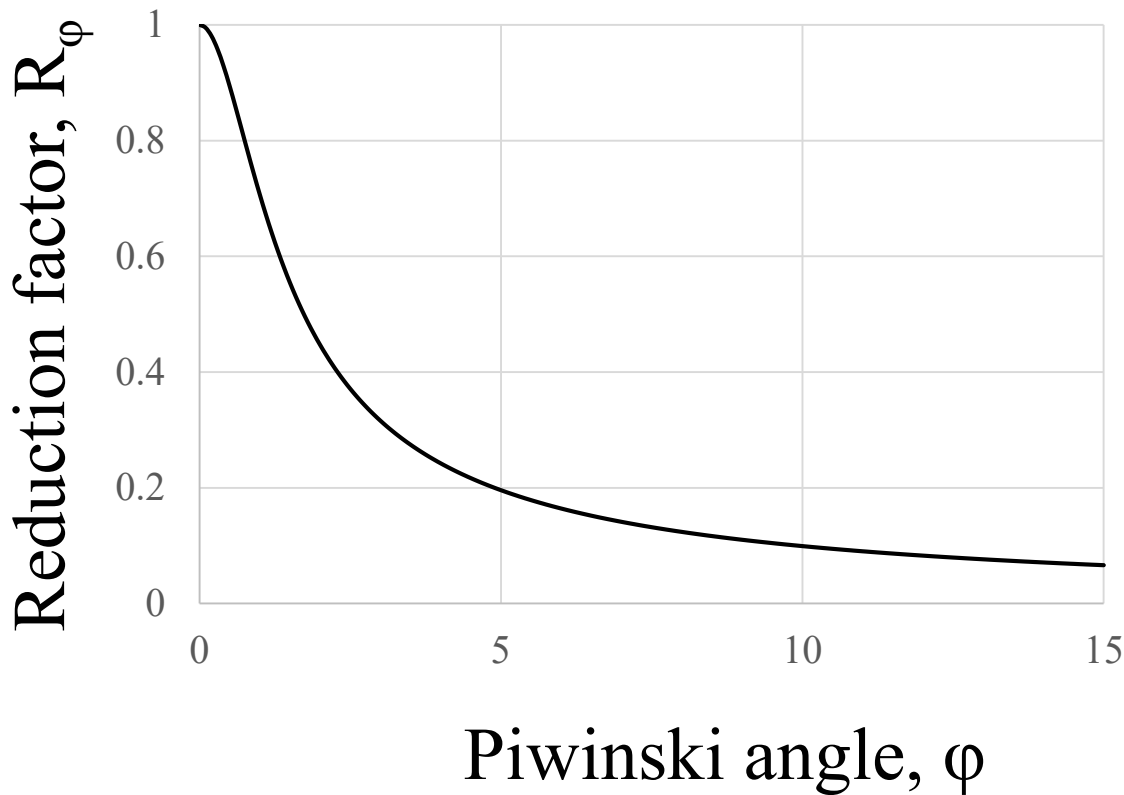
- Crab Crossing concepts and considerations for JLEIC
- Preliminary self-consistent set of crab crossing parameters
- Crab Crossing simulations
- Future Plans

# Beam Crossing Angle

- Reduce parasitic collisions
- Reduce long range beam-beam effects

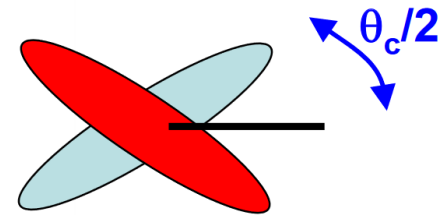


$$R_\phi = \frac{1}{\sqrt{1 + \phi^2}}; \quad \phi \equiv \frac{\theta_c \sigma_z}{2\sigma_x} \text{ "Piwinski angle"}$$



# Luminosity Reduction @ JLEIC

$$R_\phi = \frac{1}{\sqrt{1 + \phi^2}}; \quad \phi \equiv \frac{\theta_c \sigma_z}{2\sigma_x} \text{ "Piwinski angle"}$$



$$R_\phi \approx 0.0797$$

Crossing beam parameters		
$\theta_c$	50	mrad
$\sigma_z$	9.08	mm
$\sigma_x$	$18.04 \times 10^{-3}$	mm
$\phi$	12.5	rad

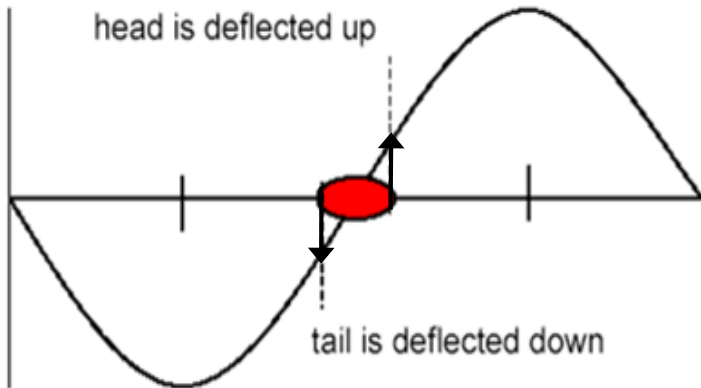
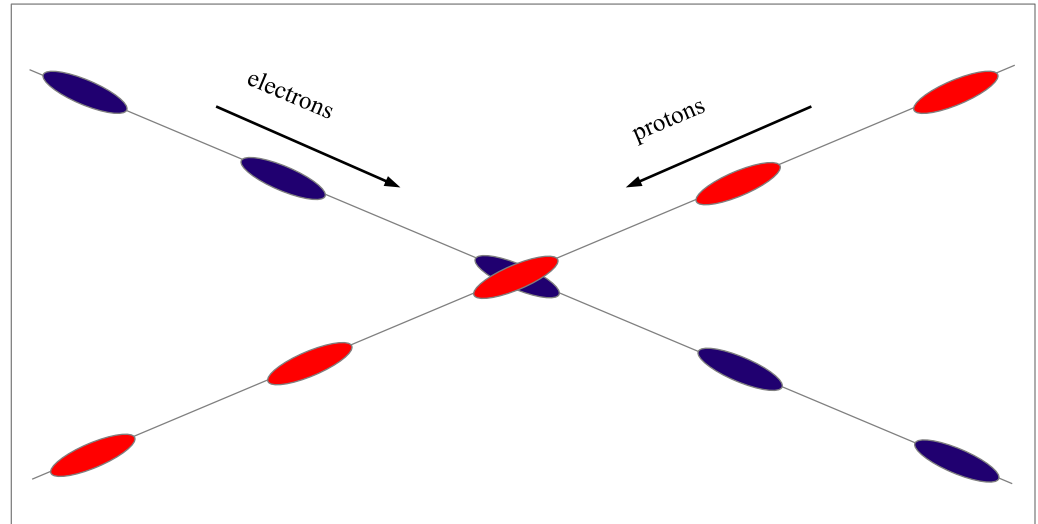
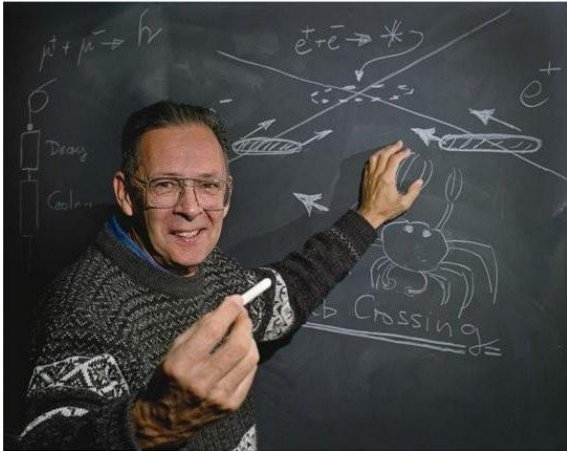
**Roughly 8% of Luminosity**

# JLEIC Luminosity Approach

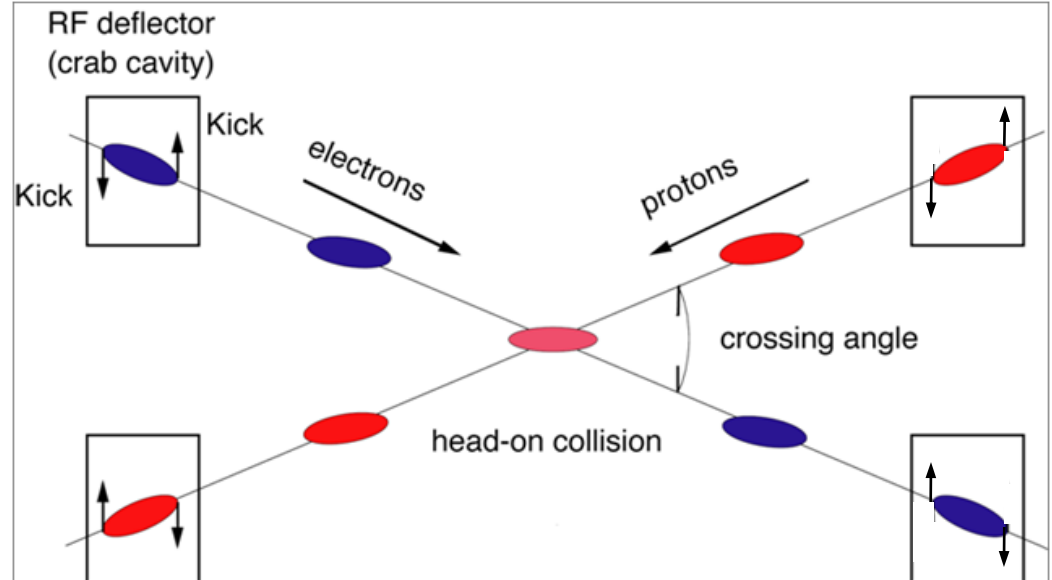
- Short bunches for both ion and electron beams
- Small transverse emittance
- Ultrahigh collision frequency
- Staged electron cooling
- Small final focusing  $\beta^*$
- Large beam-beam tune shift
- **Crab crossing of colliding beams**

$$\mathcal{L} = \frac{N_1 N_2 f n_b}{4\pi\epsilon \sqrt{\beta_x^* \beta_y^*}} \cdot \frac{1}{\sqrt{1 + \left(\frac{\sigma_z}{\sigma_x} \tan \frac{\theta_{cross}}{2}\right)^2}}$$

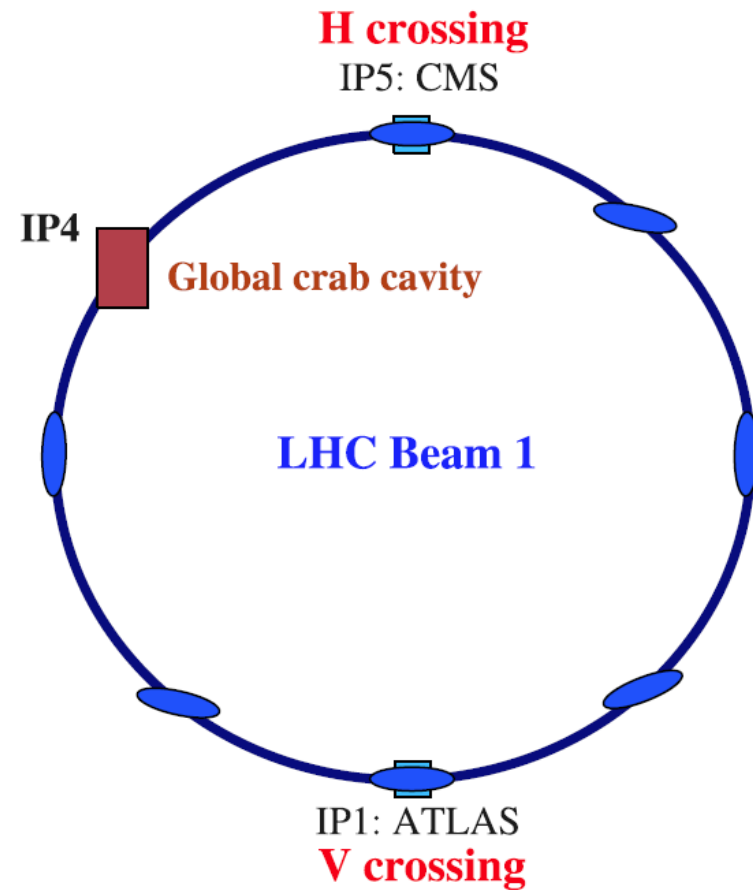
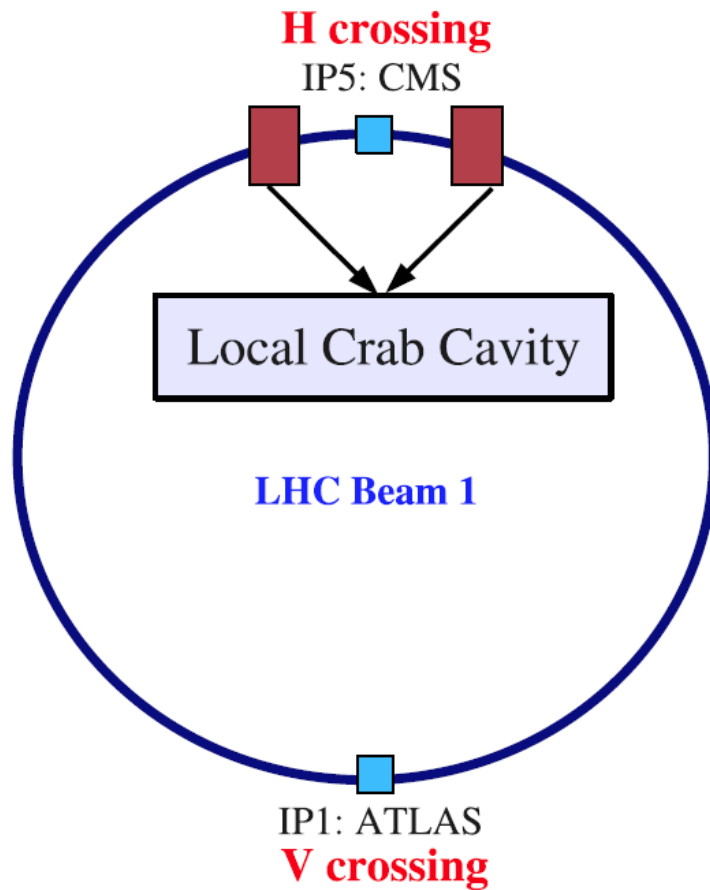
# The Crabbing Concept



\*R. Palmer, SLAC-PUB-4707 (1988).



# Crabbing Schemes: Local & Global



Y.-P. Sun et. Al, Phys. Rev. ST. Accel. Beams, 12, 101002

- Local crabbing:
- $(2n+1)\pi/2$  phase advance between crab cavities



# Crabbing by deflecting cavity

- Use of a transverse electric field to impart a “kick” on the bunch

$$V_{da} = \frac{cE_b \tan \frac{\varphi_{cross}}{2}}{e2\pi f \sqrt{\beta_{crab}\beta^*}}$$

$E_b$  = beam energy

$f$  = RF frequency

$\beta_{crab}$  = beta function at CC location

$\beta^*$  = beta function at IP

$\varphi_{cross}$  = beam crossing angle

S. Ahmed, et al. in Proceedings of IPAC2011, WEPC047

# Crabbing by dispersive cavity

- Conventional accelerating/bunching cavity located in a region of dispersion  $D(s)$

$$V_a = \frac{c E_b \varphi_{crab}}{e 2\pi f \sqrt{\beta_{crab} \beta^* D'}}$$

$E_b$  = beam energy

$f$  = RF frequency

$\beta_{crab}$  = beta function at CC location

$\beta^*$  = beta function at IP

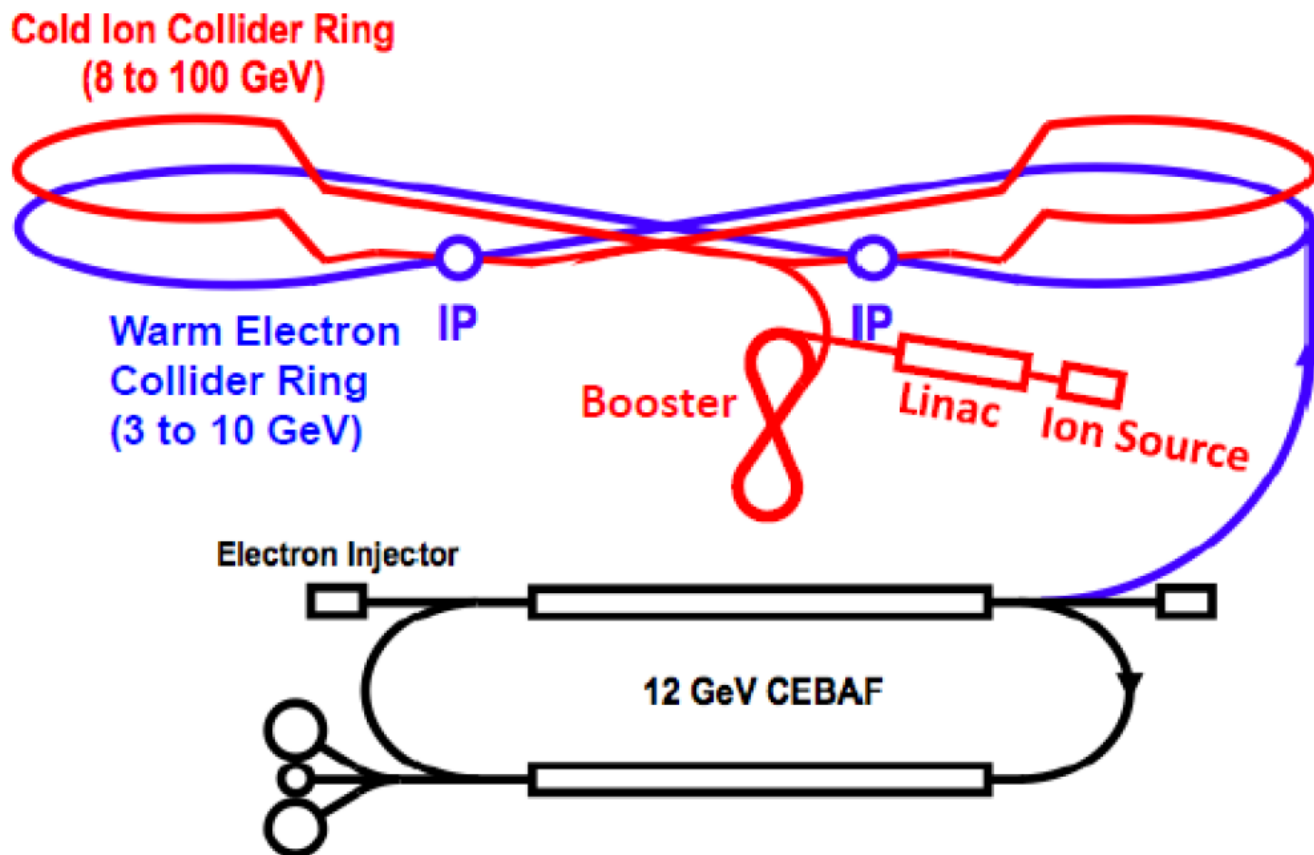
$\varphi_{crab}$  = crab angle

$D'$   $\leq 0.3$  (from ion ring lattice simulation)

**Dispersive crab voltage larger than deflecting crab voltage.**

S. Ahmed, et al. in Proceedings of IPAC2011, WEPC047

# JLEIC layout

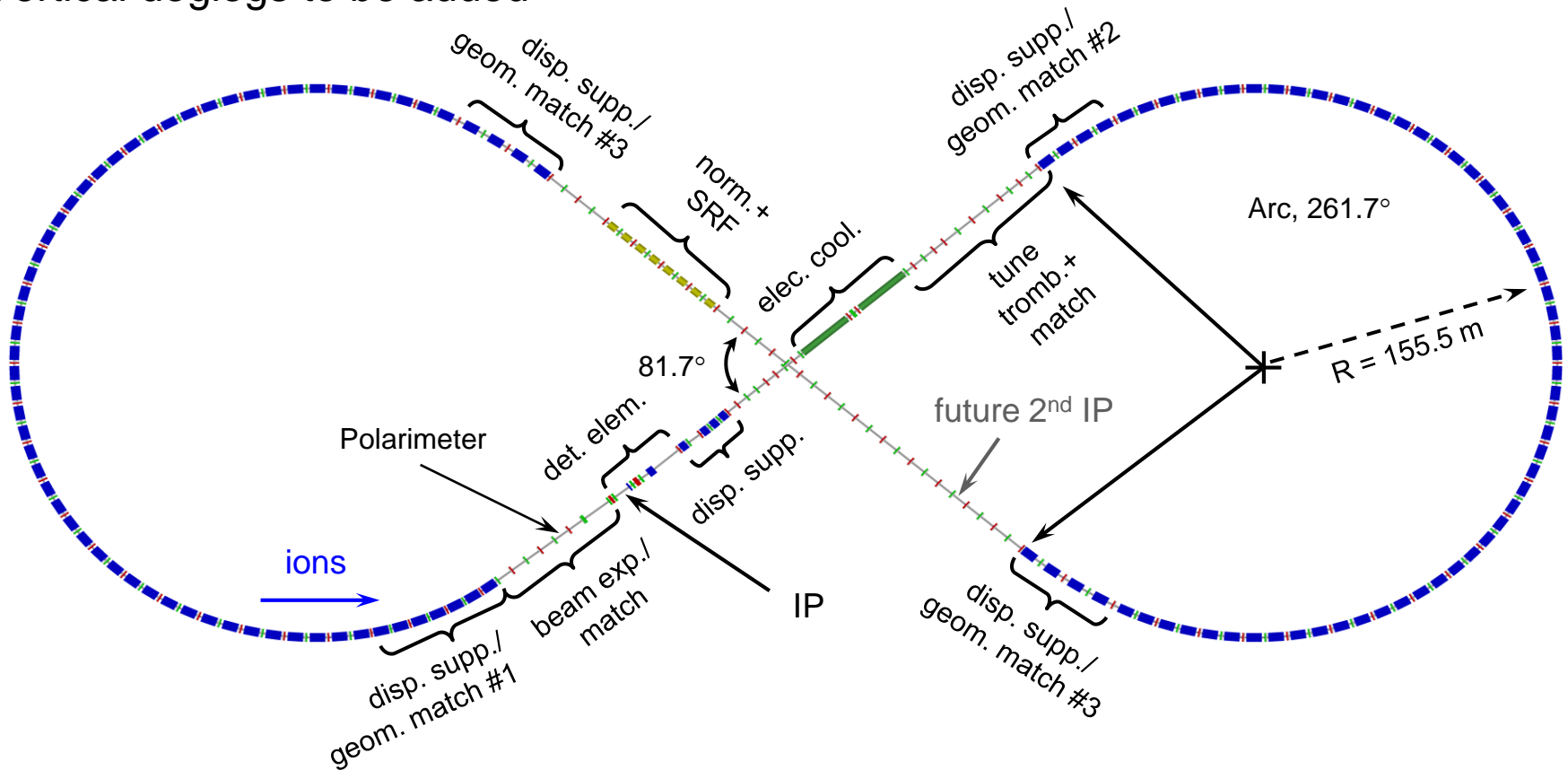


C.M. energy -  $\sqrt{s} = 15 - 65 \text{ GeV}$

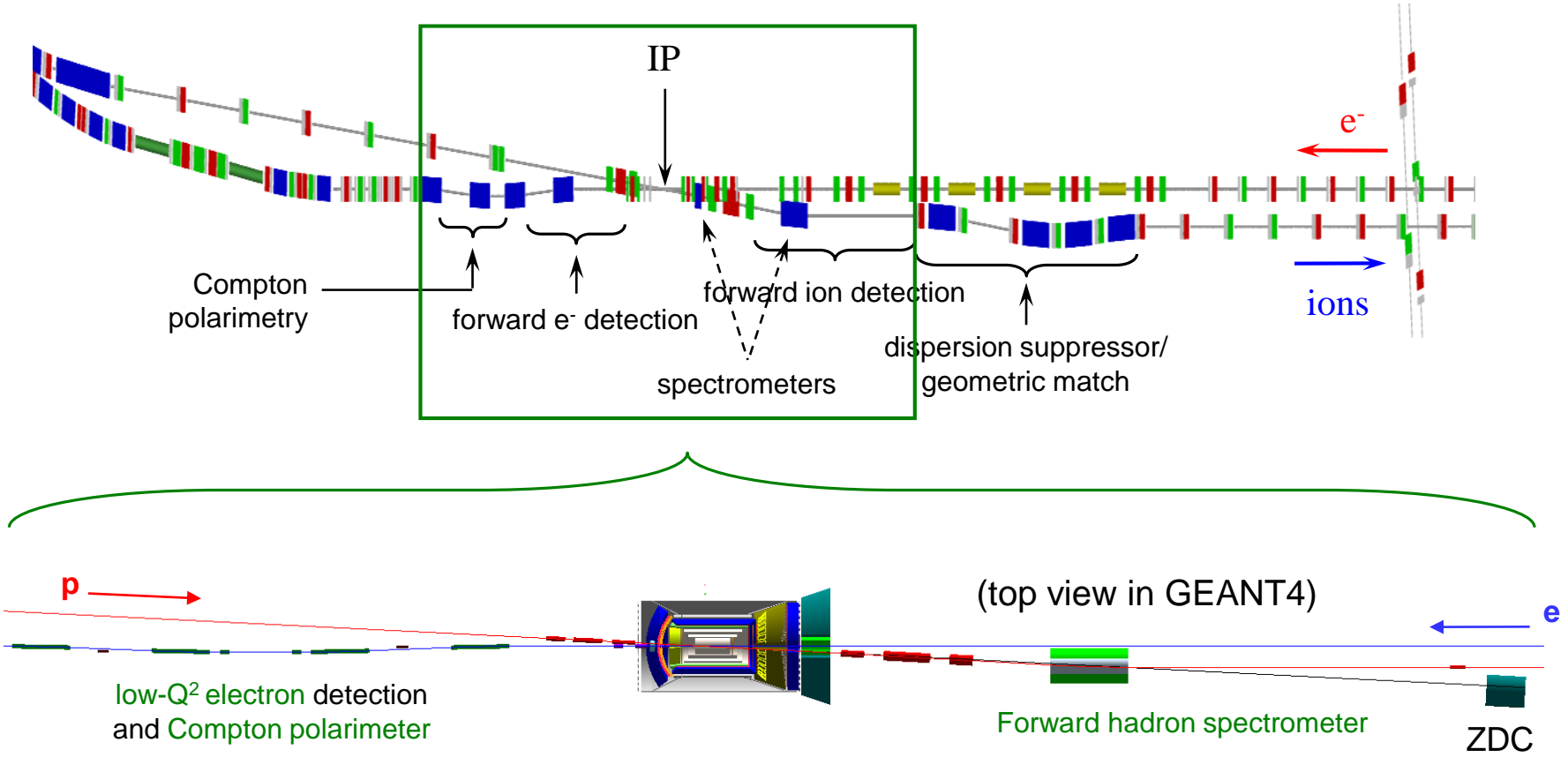
$L \approx 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ , optimized around 45-50 GeV

# Ion Collider Ring

- Figure-8 ring with a circumference of 2153.9 m
- Two 261.7° arcs connected by two straights crossing at 81.7°
- Vertical doglegs to be added

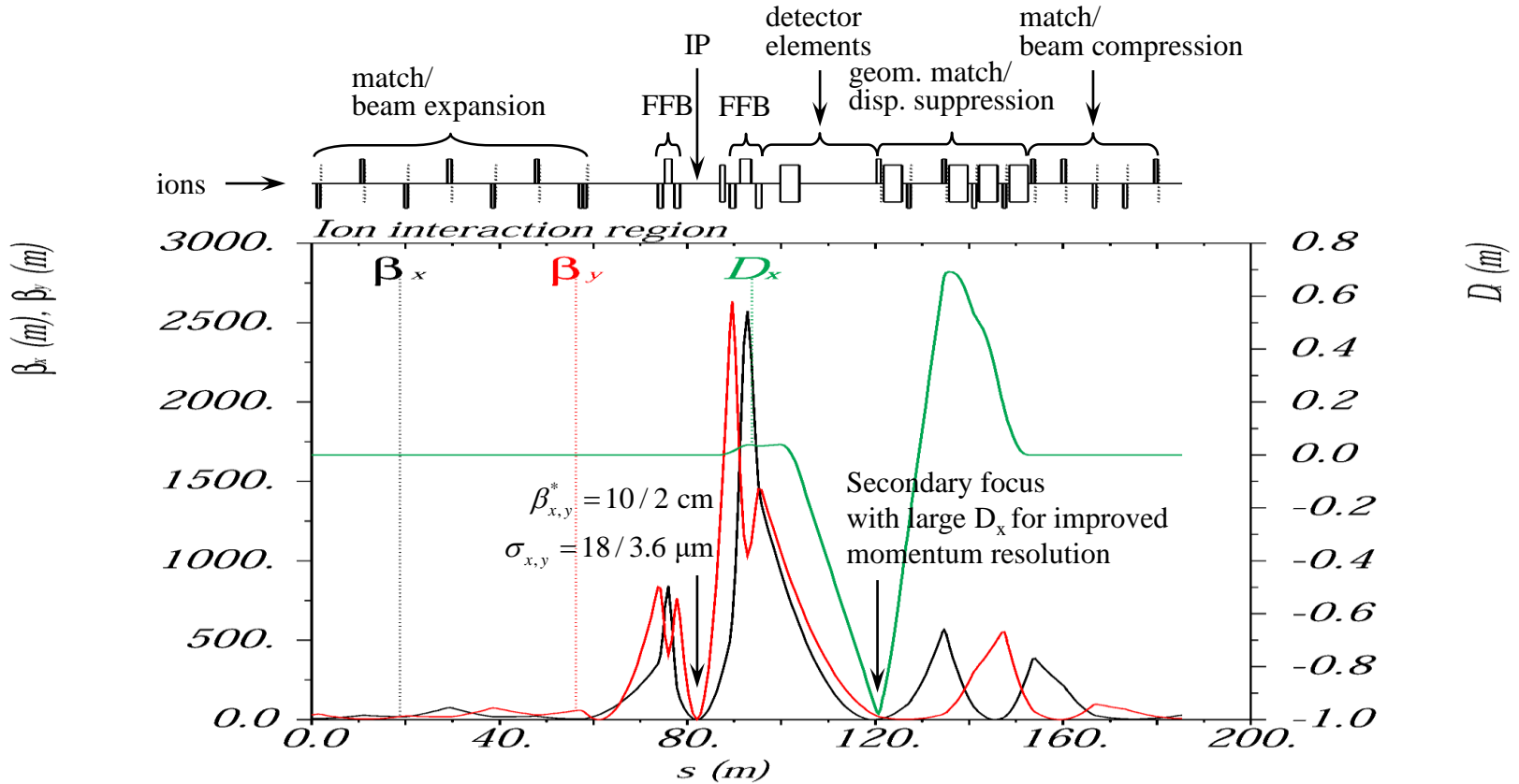


# Detector Region Layout

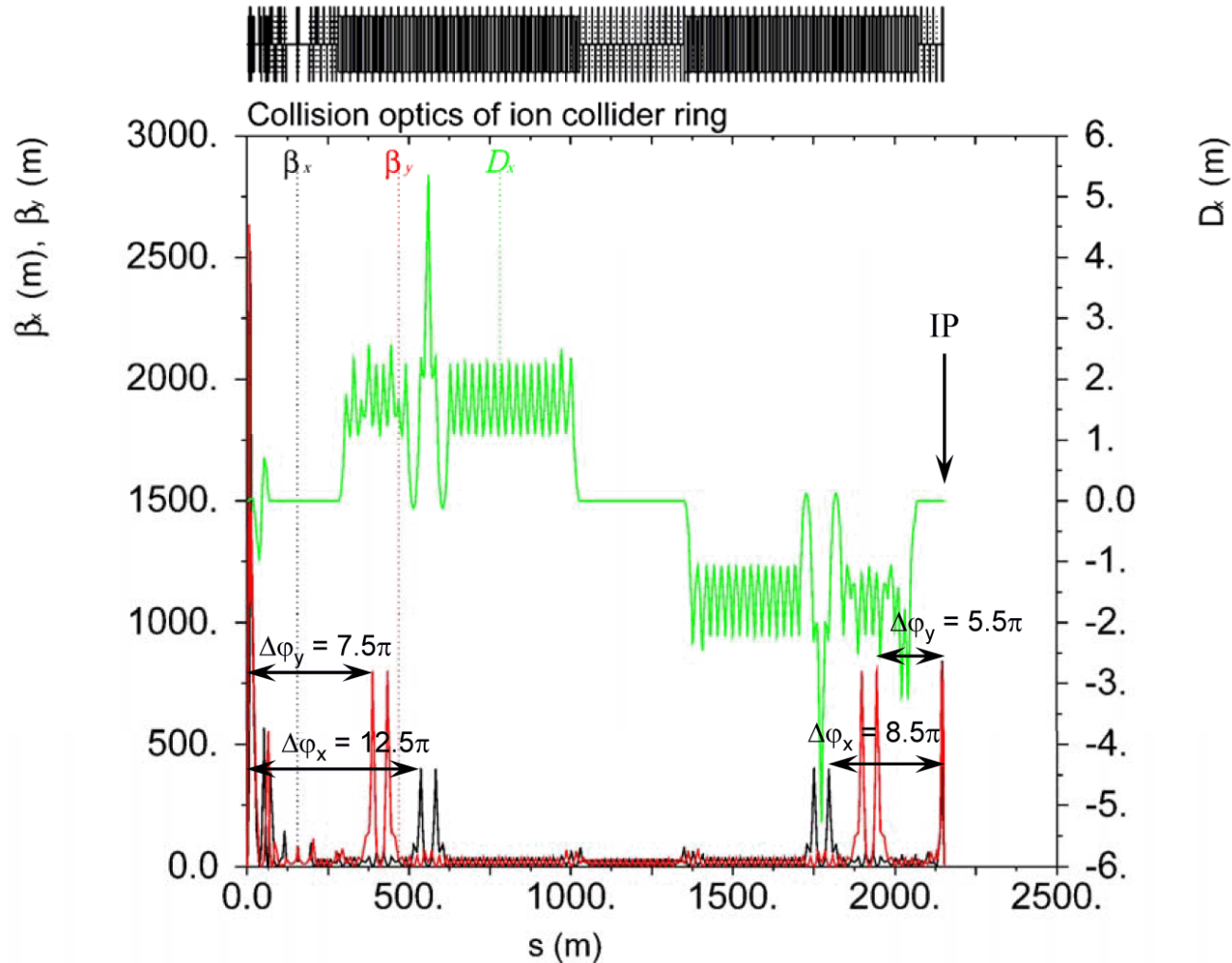


# Baseline Ion IR Optics

- IR design features
  - Modular design
  - Based on triplet Final Focusing Blocks (FFB)
  - Asymmetric design to satisfy detector requirements and reduce chromaticity
  - Spectrometer dipoles before and after downstream FFB, second focus downstream of IP
  - No dispersion at IP, achromatic optics downstream of IP



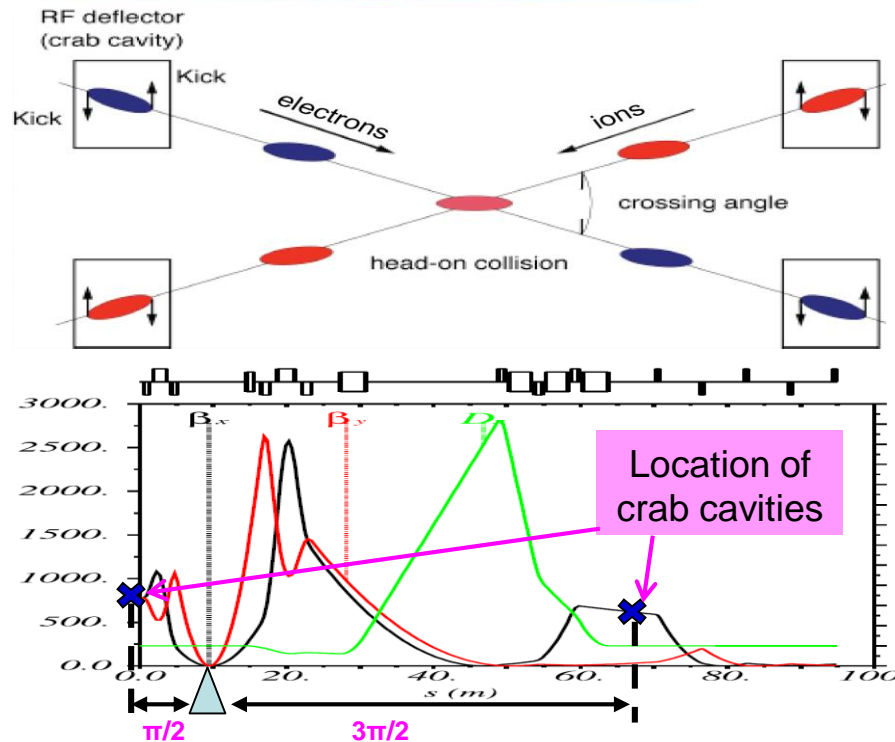
# Collision optics of JLEIC ion collider ring



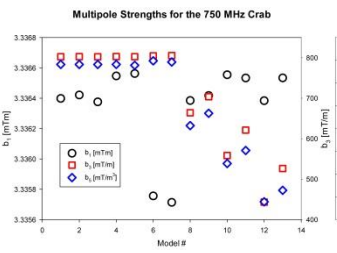
$\beta_x$  peaks from CCB sextupoles adequate for crab cavity locations.

# Crab Crossing at JLEIC

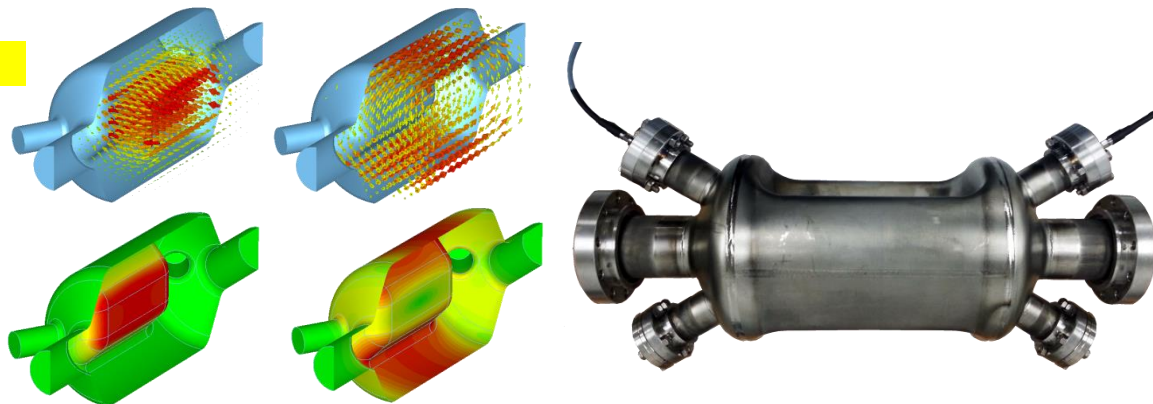
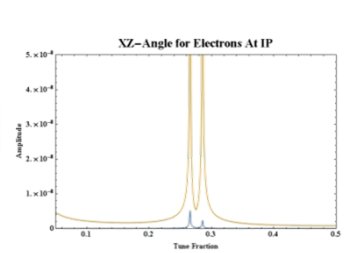
- Effective head-on bunch collisions restored with 50 mrad crossing angle
- Local crab scheme
- Two cavities are placed at  $(2n+1)\pi/2$  phase advance relative to IP
- Optimal  $\beta_x$  at locations of crab cavities for minimizing the required kicking voltage
- Deflective crabbing using transverse electric field of SRF cavities (as at KEK-B)
  - Design and analysis completed
  - Prototype fabricated and characterized
  - Final testing with promising results



## Multipole Tailoring



## Beam Dynamics Studies





# Crab crossing Design Parameters

Parameter	Unit	Electron	Proton
Energy	GeV	10	100
Frequency	MHz	952.6	
Crossing angle	mrad	50	
$\beta^*$	cm	10	
$\beta_x$ @ crab cavity location	m	200	400
Integrated kicking voltage	MV	2.8	19.81

Deflecting voltage:

$$V_{da} = \frac{cE_b \tan \frac{\varphi_{cross}}{2}}{e2\pi f \sqrt{\beta_{crab}\beta^*}}$$

S. Abeyratne et al, MEIC Design Summary, 2015

# Bunch at IP with and w/o crabbing

## Bunched Beam parameters

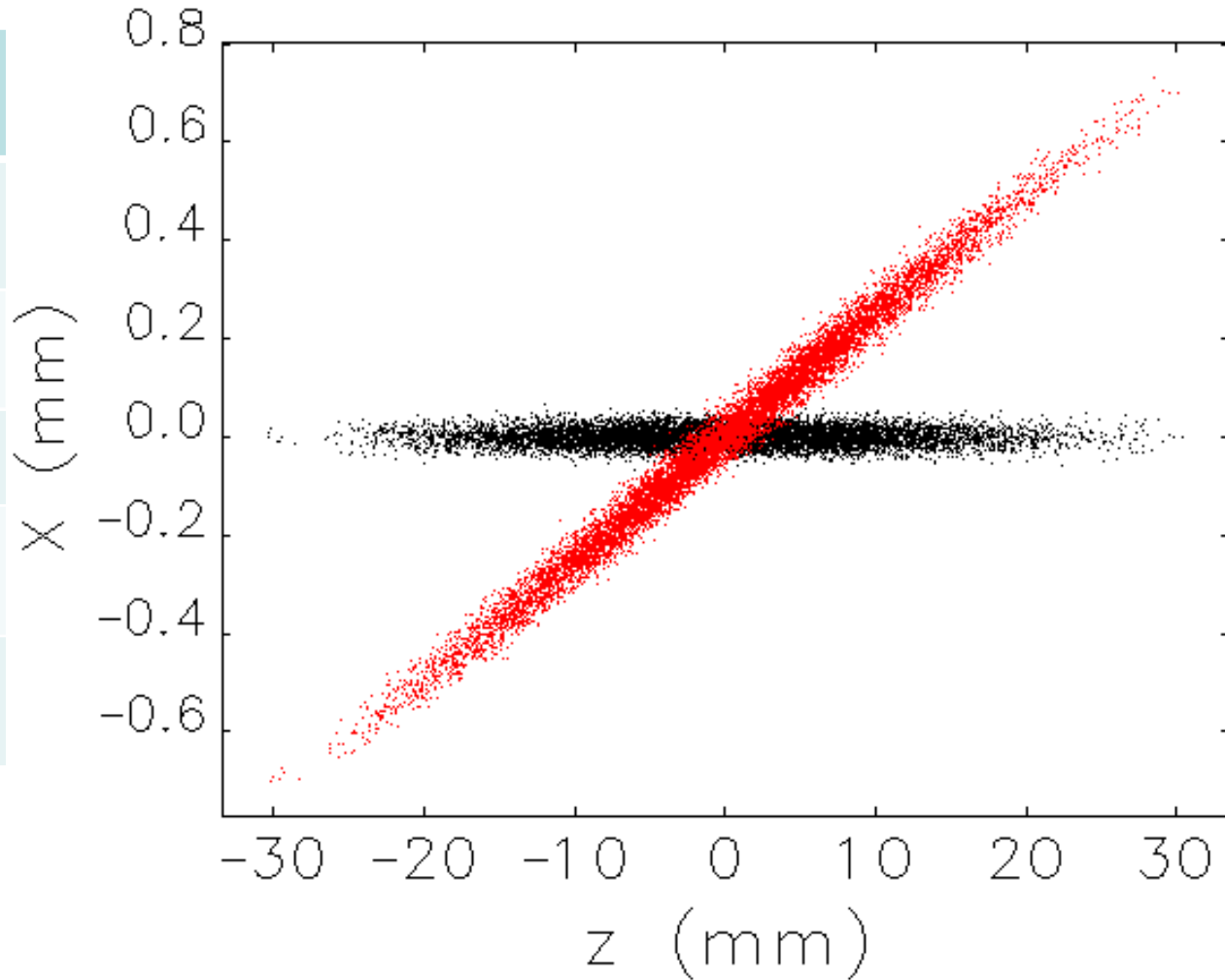
N particles 10,000

$\epsilon_{nx}$  0.35  $\mu\text{m}$

dp/p  $3e^{-4}$

$\sigma_s$  1 cm

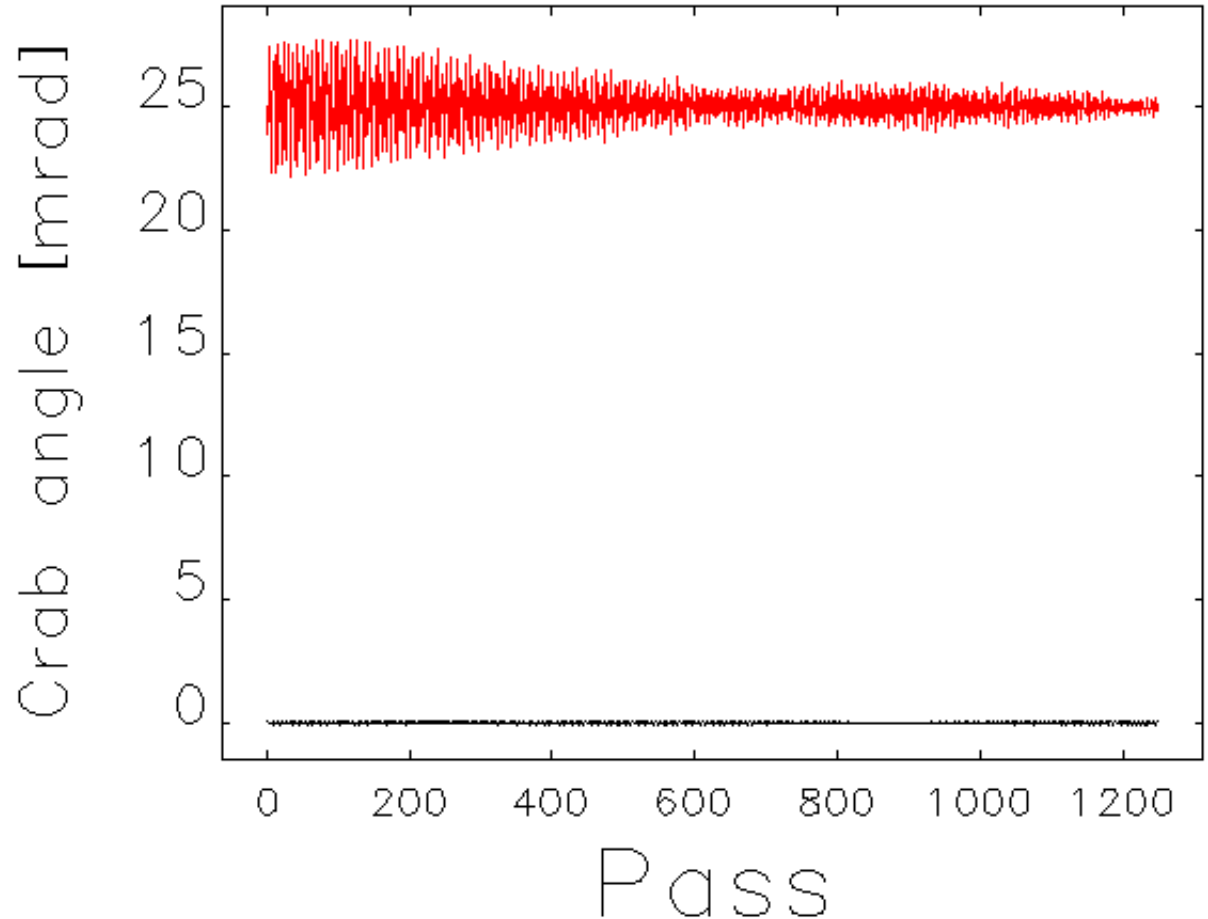
Gaussian distribution  
3 - sigma



Crab angle  $\approx 25$  mrad

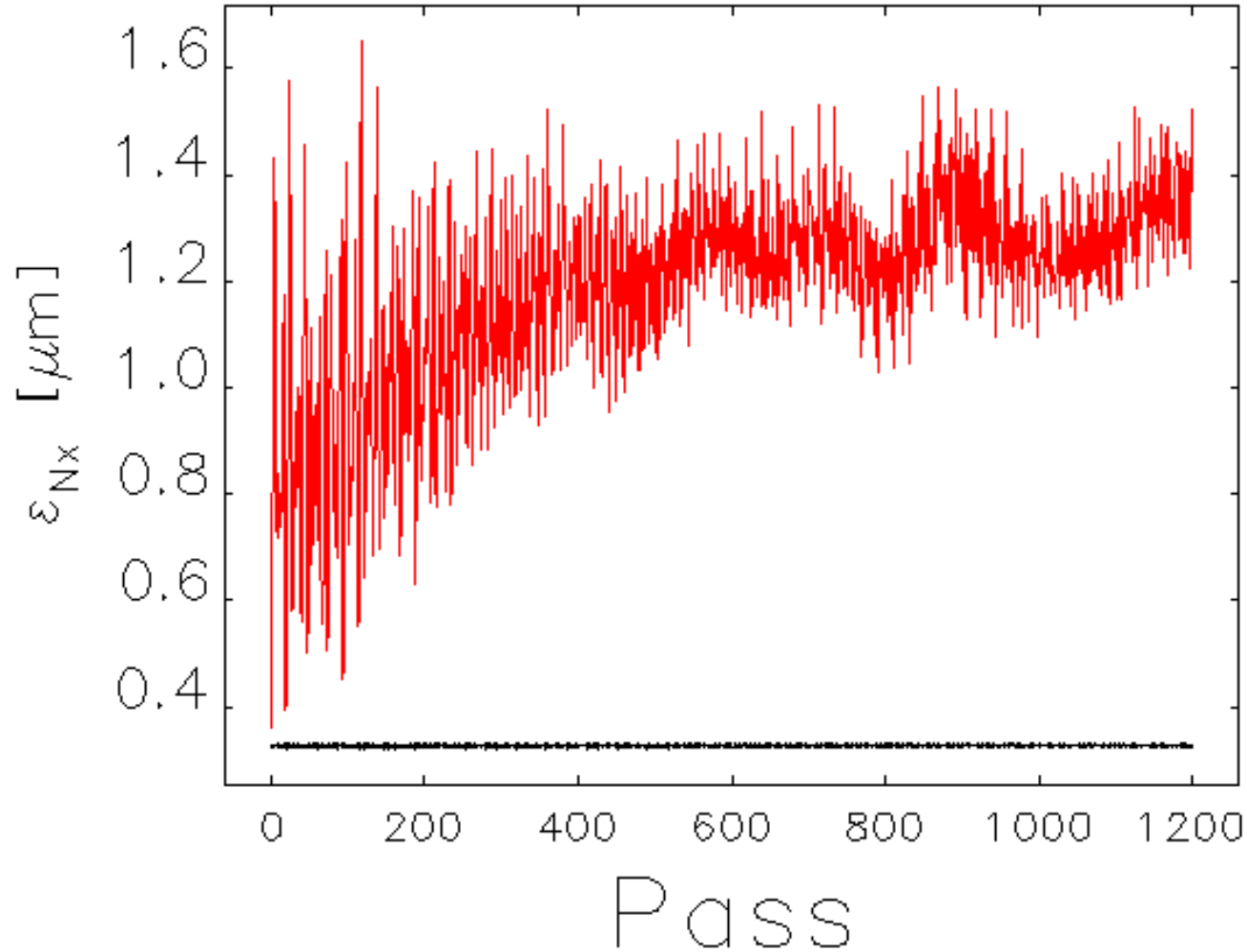
# Crab stability with time

- Calculated as
 
$$\varphi_{crab} = \frac{\langle xz \rangle}{\langle zz \rangle}$$
- $x = x_{rc} + z \tan \varphi$

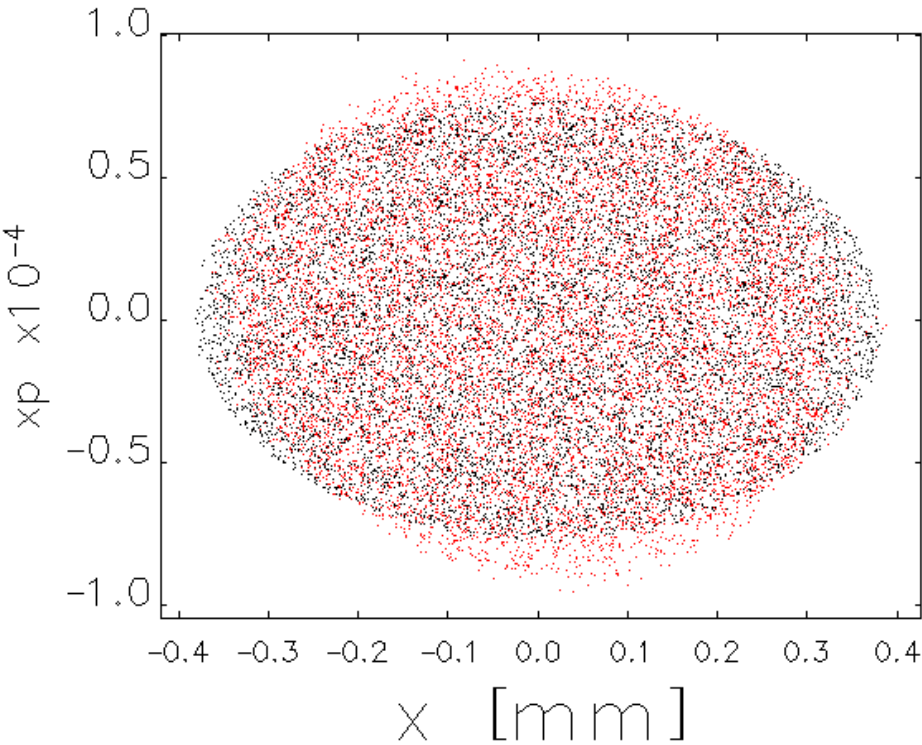


Crab angle jitter suppression, required for beam stability and minimum emittance impact.

# Emittance growth with crabbing

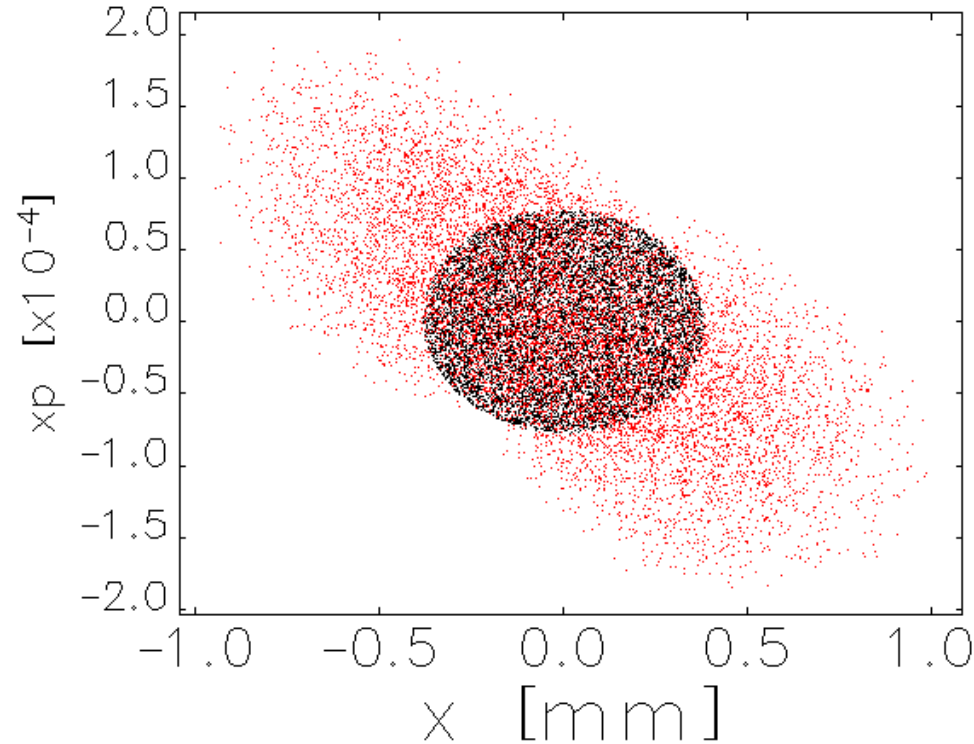


# Bunch matching in ion ring lattice



## Crabbing OFF:

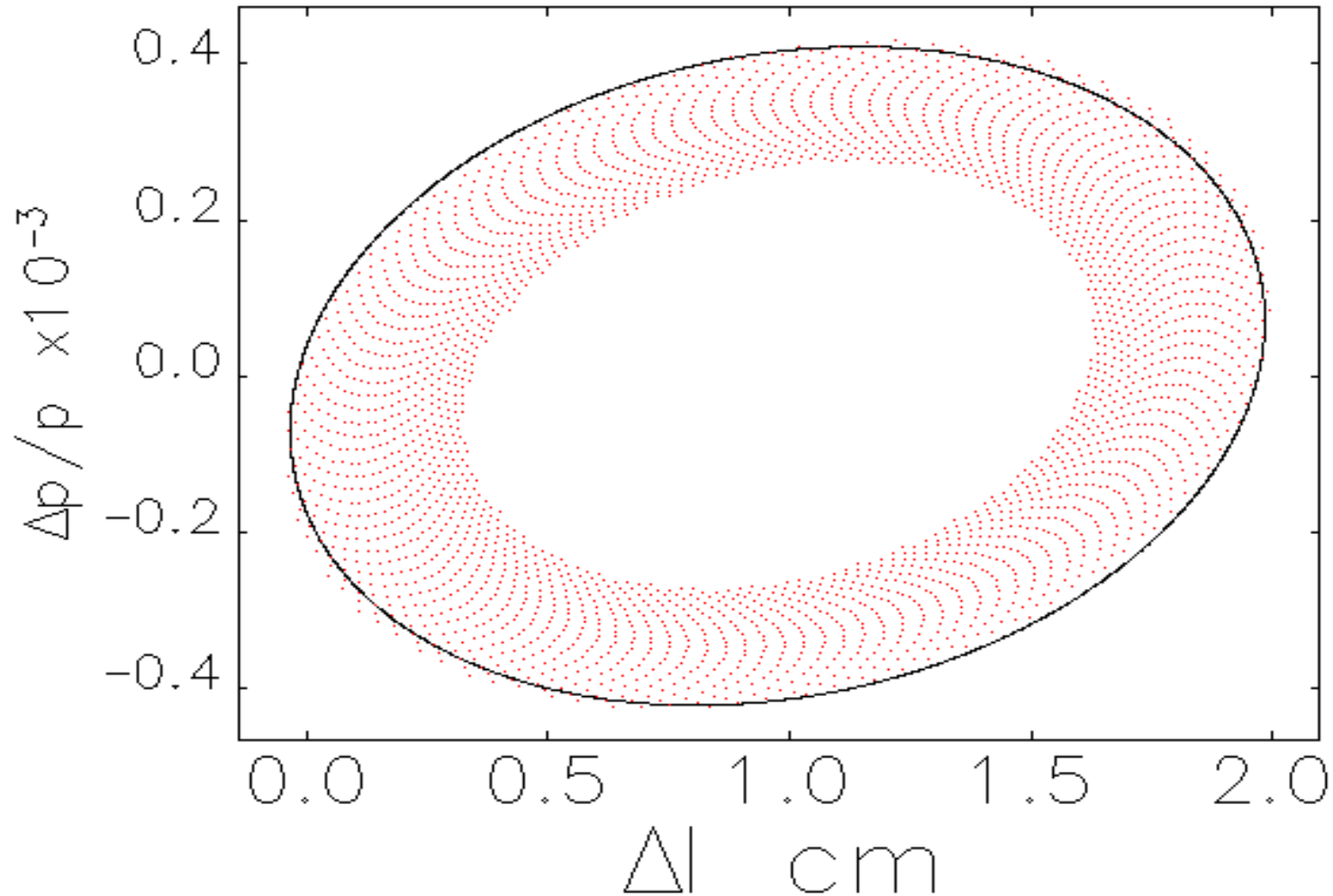
Particle distributions are  
matched after 1 turn.



## Crabbing ON:

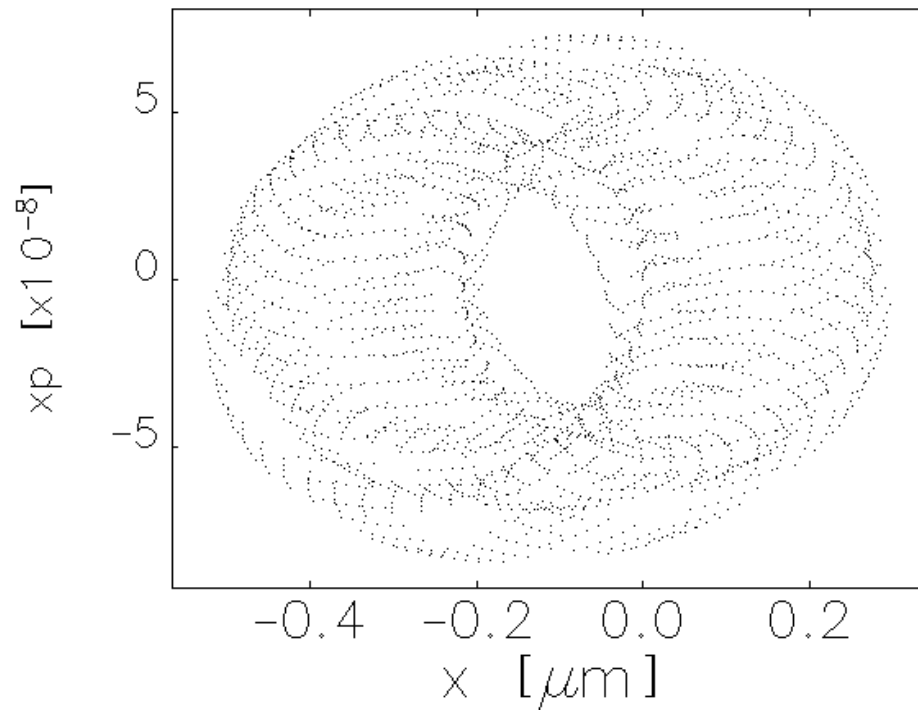
Particle distribution is not  
matched after 1 turn.

# Momentum spread in Phase Space

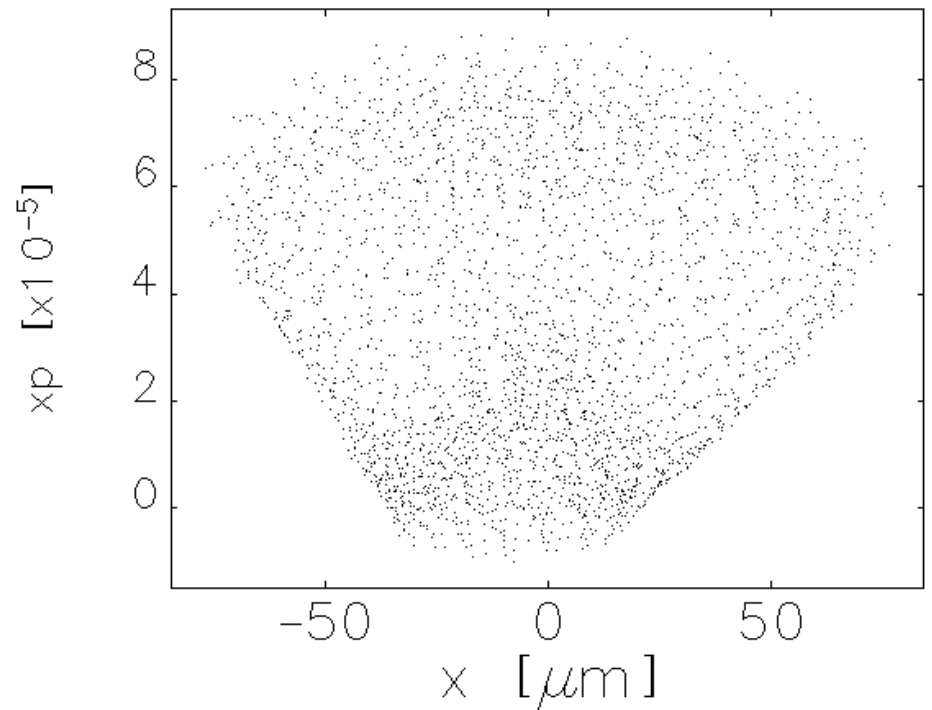


# Phase space

Of 1 particle over 3000 turns, crabbing off and on



Crabbing OFF



Crabbing ON

# Crab crossing plan

- Avoid sextupoles in crabbed beam region by switching optics sections
- Optimize the crabbing system for best beam stability and minimum emittance impact
- Study effects of and specify tolerances on crab cavity errors such as misalignment, amplitude and phase instability
- Study and specify tolerances on cavity multipole components by estimating impact on the ring's dynamic aperture
- Specify high-order mode requirements
- Specify requirement on the beam parameters such as maximum bunch length
- Evaluate and optimize impedance of the crab cavities
- Complete beam dynamics simulation using an optimized field map satisfying the determined requirements



# Acknowledgements

- Vasiliy Morozov
- Jean Delayen, ODU
- Jlab CASA members
- JLEIC Collaboration