

Inclusive Jets and their substructure within SCET

Felix Ringer

Los Alamos National Laboratory

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Outline

- Inclusive jets
- The jet fragmentation function
- Conclusions

Kang, FR, Vitev '16

Kang, FR, Vitev '16

Chien, Kang, FR, Vitev, Xing '15

*Kang, Qiu, FR, Xing, Zhang
- in preparation*

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Kang, FR, Vitev `16

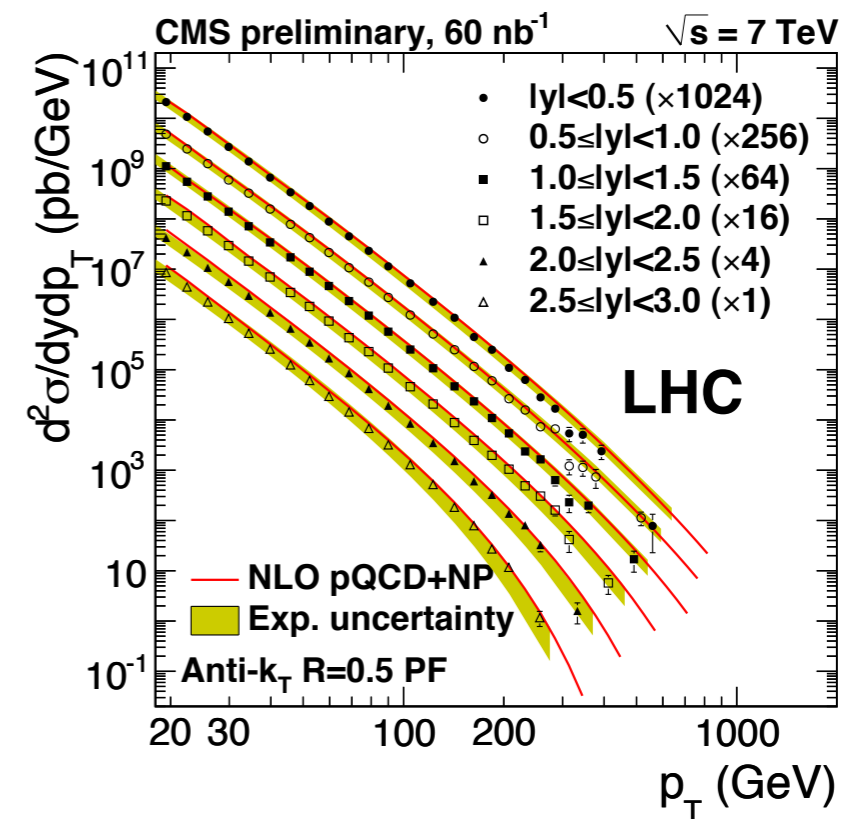
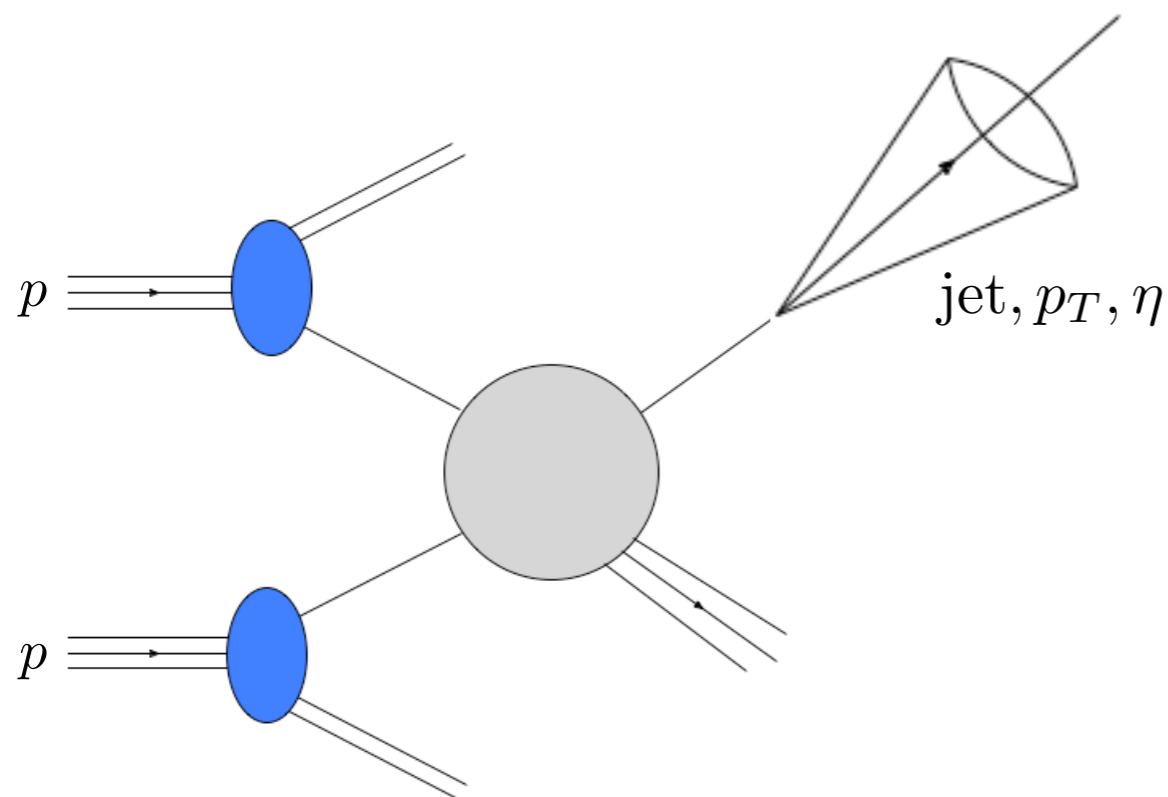
Kang, FR, Vitev `16

Chien, Kang, FR, Vitev, Xing `15

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Inclusive Jet Production $pp \rightarrow \text{jet} X$

- Large theoretical uncertainties especially at high p_T
- PDFs are constrained by collider jet data, especially $g(x), \Delta g(x)$
- Determination of α_s
- High p_T jets are a promising observable for the search of BSM physics at the LHC
- Jet quenching studies in heavy-ion collisions
- ...



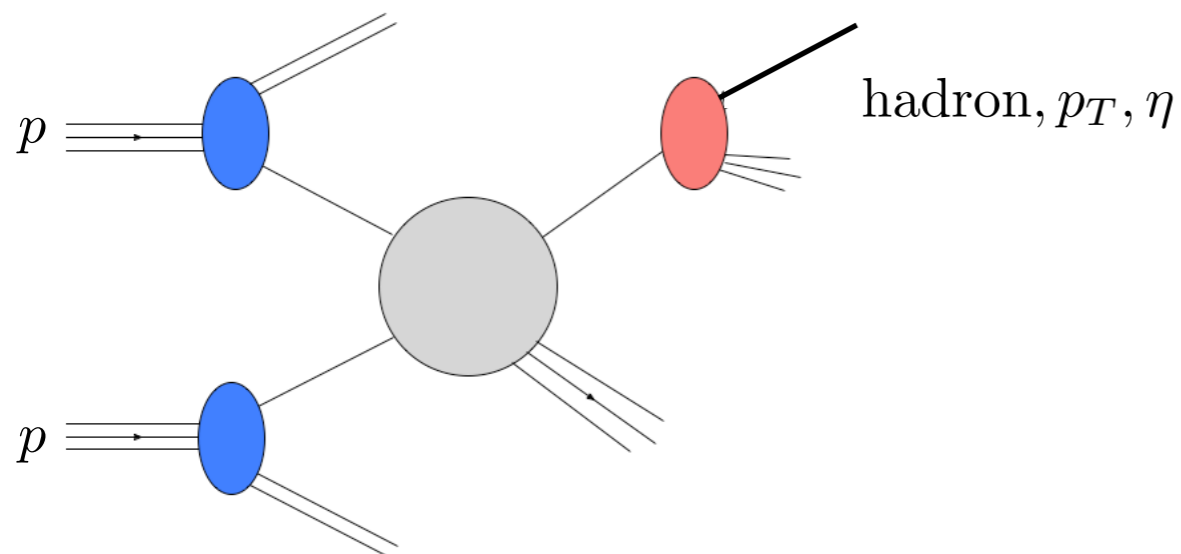
Recall Inclusive Hadron Production $pp \rightarrow hX$

Factorization

$$\frac{d\sigma^{pp \rightarrow hX}}{dp_T d\eta} = \frac{2p_T}{s} \sum_{a,b,c} \int_{x_a^{\min}}^1 \frac{dx_a}{x_a} f_a(x_a, \mu) \int_{x_b^{\min}}^1 \frac{dx_b}{x_b} f_b(x_b, \mu) \int_{z_c^{\min}}^1 \frac{dz_c}{z_c^2} \frac{d\hat{\sigma}_{ab}^c(\hat{s}, \hat{p}_T, \hat{\eta}, \mu)}{dvdz} D_c^h(z_c, \mu)$$

timelike DGLAP for FFs

$$\mu \frac{d}{d\mu} D_i^h(z, \mu) = \frac{\alpha_s(\mu)}{\pi} \sum_j \int_z^1 \frac{dz'}{z'} P_{ji} \left(\frac{z}{z'}, \mu \right) D_j^h(z', \mu)$$



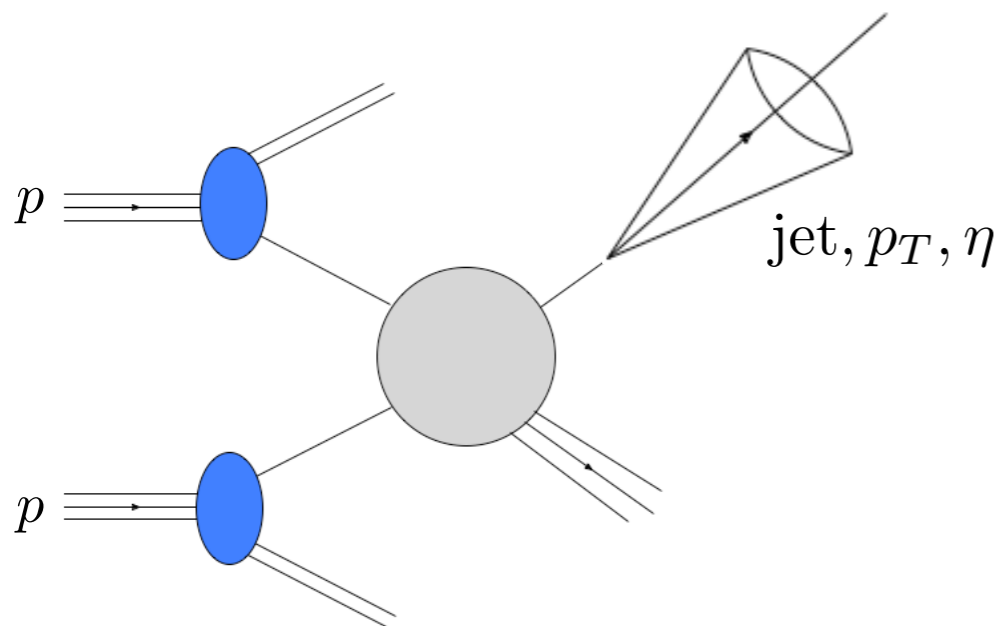
Aversa, Chiappetta, Greco, Guillet '89,
Jäger, Schäfer, Stratmann, Vogelsang '04

Inclusive Jet Production $pp \rightarrow \text{jet} X$

Factorization

Kang, FR, Vitev '16

$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \frac{2p_T}{s} \sum_{a,b,c} \int_{x_a^{\min}}^1 \frac{dx_a}{x_a} f_a(x_a, \mu) \int_{x_b^{\min}}^1 \frac{dx_b}{x_b} f_b(x_b, \mu) \int_{z_c^{\min}}^1 \frac{dz_c}{z_c^2} \frac{d\hat{\sigma}_{ab}^c(\hat{s}, \hat{p}_T, \hat{\eta}, \mu)}{dvdz} J_c(z_c, \omega_J, \mu)$$



Inclusive Jet Production $pp \rightarrow \text{jet} X$

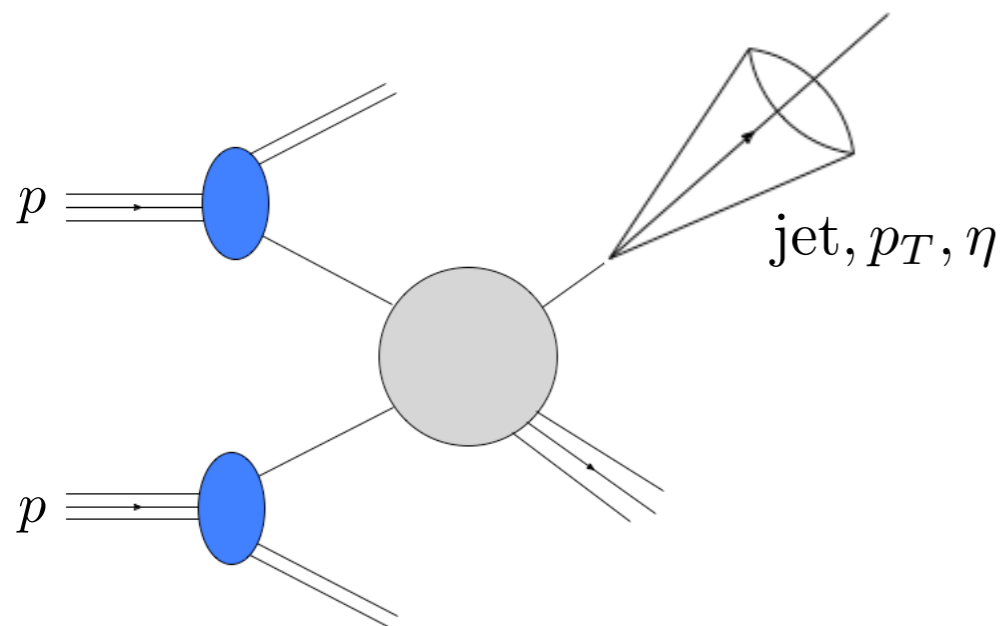
Factorization

Kang, FR, Vitev '16

$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \frac{2p_T}{s} \sum_{a,b,c} \int_{x_a^{\min}}^1 \frac{dx_a}{x_a} f_a(x_a, \mu) \int_{x_b^{\min}}^1 \frac{dx_b}{x_b} f_b(x_b, \mu) \int_{z_c^{\min}}^1 \frac{dz_c}{z_c^2} \frac{d\hat{\sigma}_{ab}^c(\hat{s}, \hat{p}_T, \hat{\eta}, \mu)}{dvdz} J_c(z_c, \omega_J, \mu)$$

timelike DGLAP for semi-inclusive jet function

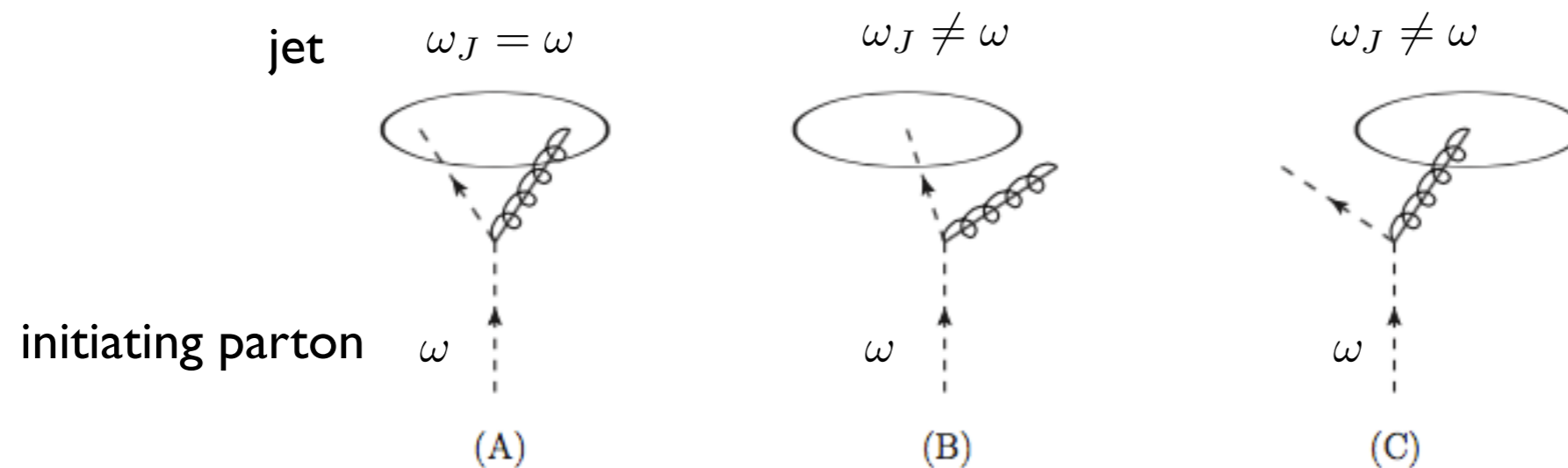
$$\mu \frac{d}{d\mu} J_i(z, \omega_J, \mu) = \frac{\alpha_s(\mu)}{\pi} \sum_j \int_z^1 \frac{dz'}{z'} P_{ji} \left(\frac{z}{z'}, \mu \right) J_j(z', \omega_J, \mu)$$



→ resummation of $\sim (\alpha_s \ln R)^n$
 NLO $\sim \mathcal{A} + \mathcal{B} \ln R + \mathcal{O}(R^2)$

Semi-inclusive jet function in SCET at NLO

- The siJF describes how a parton (q or g) is transformed into a jet with radius R and energy fraction z



where

$$z = \omega_J / \omega$$

momentum sum rule: $\int_0^1 dz z J_i(z, \omega R, \mu) = 1$

Semi-inclusive jet function in SCET at NLO

Leading order

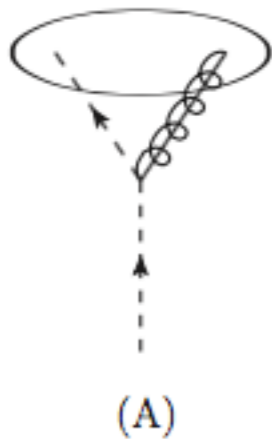
$$J_q^{(0)}(z, \omega_J) = \delta(1 - z)$$

Semi-inclusive jet function in SCET at NLO

Leading order

$$J_q^{(0)}(z, \omega_J) = \delta(1 - z)$$

Next-to-leading order



$$J_q(z, \omega_J) = \delta(1 - z) \frac{\alpha_s}{\pi} \left(\frac{\mu^2 e^{\gamma_E}}{4\pi} \right)^\epsilon \int_0^1 dx \hat{P}_{qq}(x, \epsilon) \int \frac{dq_\perp}{q_\perp^{1+2\epsilon}} \Theta_{\text{alg}}$$

where: anti- k_T : $\Theta_{\text{anti-}k_T} = \theta \left(x(1-x)\omega_J \tan \frac{R}{2} - q_\perp \right)$

$$\hat{P}_{qq}(x, \epsilon) = C_F \left[\frac{1+x^2}{1-x} - \epsilon(1-x) \right]$$

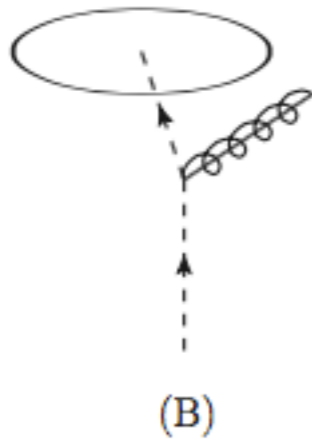
$$x = \frac{\ell^- - q^-}{\ell^-}$$

Semi-inclusive jet function in SCET at NLO

Leading order

$$J_q^{(0)}(z, \omega_J) = \delta(1 - z)$$

Next-to-leading order

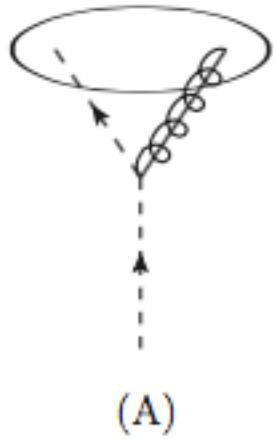


$$J_{q \rightarrow q(g)}(z, \omega_J) = \frac{\alpha_s}{\pi} \left(\frac{\mu^2 e^{\gamma_E}}{4\pi} \right)^\epsilon \hat{P}_{qq}(z, \epsilon) \int \frac{dq_\perp}{q_\perp^{1+2\epsilon}} \Theta_{\text{alg}}$$

where: $\Theta_{\text{anti-}k_T} = \theta \left(q_\perp - (1 - z)\omega_J \tan \frac{R}{2} \right)$

Semi-inclusive jet function

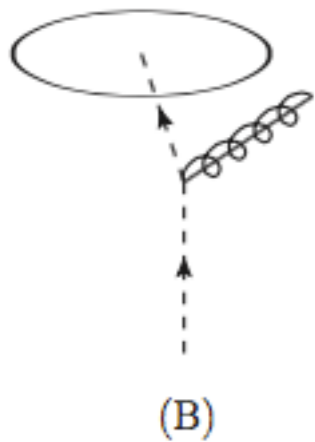
$\overline{\text{MS}}$ scheme, anti- k_T



$$J_q(z, \omega_J) = \delta(1 - z) \frac{\alpha_s}{2\pi} C_F \left[\frac{1}{\epsilon^2} + \frac{3}{2\epsilon} + \frac{1}{\epsilon} L + \frac{1}{2} L^2 + \frac{3}{2} L + \frac{13}{2} - \frac{3\pi^2}{4} \right]$$

Ellis, Vermilion, Walsh, Hornig, Lee '10

where $L = \ln \left(\frac{\mu^2}{\omega_J^2 \tan^2(R/2)} \right)$

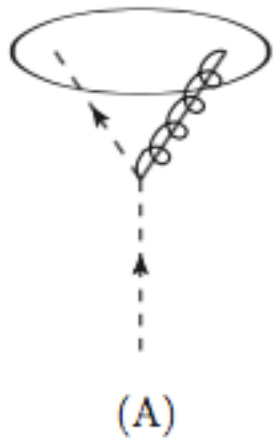


$$J_q(z, \omega_J) = \frac{\alpha_s}{2\pi} \delta(1 - z) \left[-\frac{1}{\epsilon^2} - \frac{1}{\epsilon} L - \frac{1}{2} L^2 + \frac{\pi^2}{12} \right] + \frac{\alpha_s}{2\pi} \left[\left(\frac{1}{\epsilon} + L \right) \frac{1 + z^2}{(1 - z)_+} - 2(1 + z^2) \left(\frac{\ln(1 - z)}{1 - z} \right)_+ - (1 - z) \right]$$

(C) ...

Semi-inclusive jet function

$\overline{\text{MS}}$ scheme, anti- k_T

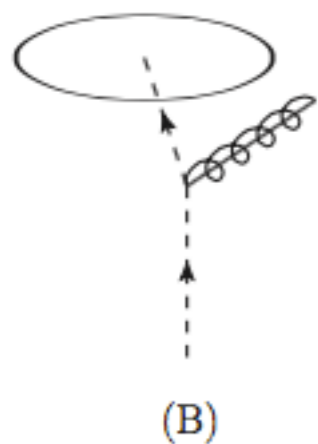


$$J_q(z, \omega_J) = \delta(1 - z) \frac{\alpha_s}{2\pi} C_F \left[\frac{1}{\epsilon^2} + \frac{3}{2\epsilon} + \frac{1}{\epsilon} L + \frac{1}{2} L^2 + \frac{3}{2} L + \frac{13}{2} - \frac{3\pi^2}{4} \right]$$

Essentially the same result as in the exclusive case

Ellis, Vermilion, Walsh, Hornig, Lee '10

where $L = \ln \left(\frac{\mu^2}{\omega_J^2 \tan^2(R/2)} \right)$



$$J_q(z, \omega_J) = \frac{\alpha_s}{2\pi} \delta(1 - z) \left[-\frac{1}{\epsilon^2} - \frac{1}{\epsilon} L - \frac{1}{2} L^2 + \frac{\pi^2}{12} \right] + \frac{\alpha_s}{2\pi} \left[\left(\frac{1}{\epsilon} + L \right) \frac{1 + z^2}{(1 - z)_+} - 2(1 + z^2) \left(\frac{\ln(1 - z)}{1 - z} \right)_+ - (1 - z) \right]$$

(C) ...

→ only a single logarithmic $\ln R$ remains

Renormalization and RG evolution

Bare - renormalized semi-inclusive jet function

$$J_{i,\text{bare}}(z, \omega_J) = \sum_j \int_z^1 \frac{dz'}{z'} Z_{ij} \left(\frac{z}{z'}, \mu \right) J_j(z', \omega_J, \mu)$$

RG equation

$$\mu \frac{d}{d\mu} J_i(z, \omega_J, \mu) = \sum_j \int_z^1 \frac{dz'}{z'} \gamma_{ij}^J \left(\frac{z}{z'}, \mu \right) J_j(z', \omega_J, \mu).$$

Anomalous dimension

$$\gamma_{ij}^J(z, \mu) = - \sum_k \int_z^1 \frac{dz'}{z'} (Z)_{ik}^{-1} \left(\frac{z}{z'}, \mu \right) \mu \frac{d}{d\mu} Z_{kj}(z', \mu)$$

Renormalization and RG evolution

We find

$$\gamma_{ij}^J(z, \mu) = \frac{\alpha_s(\mu)}{\pi} P_{ji}(z)$$

→

$$\mu \frac{d}{d\mu} J_i(z, \omega_J, \mu) = \frac{\alpha_s(\mu)}{\pi} \sum_j \int_z^1 \frac{dz'}{z'} P_{ji}\left(\frac{z}{z'}, \mu\right) J_j(z', \omega_J, \mu).$$

DGLAP evolution equation like for FFs. Resums single $\ln R$: LL_R , NLL_R

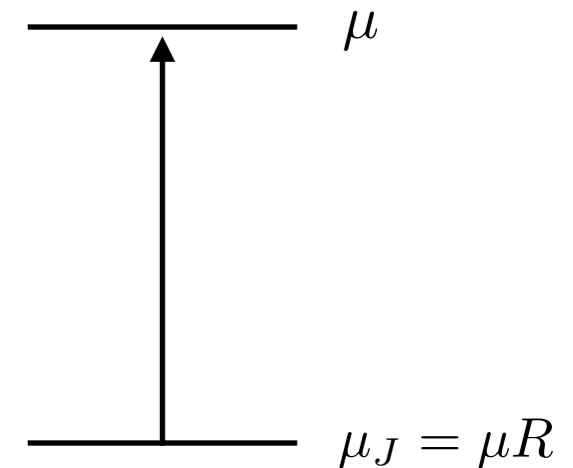
see also

Dasgupta, Dreyer, Salam, Soyez '15, '16

Jet function evolution

$$\frac{d}{d \log \mu^2} \begin{pmatrix} J_S(z, \omega_J, \mu) \\ J_g(z, \omega_J, \mu) \end{pmatrix} = \frac{\alpha_s(\mu)}{2\pi} \begin{pmatrix} P_{qq}(z) & 2N_f P_{gq}(z) \\ P_{qg}(z) & P_{gg}(z) \end{pmatrix} \otimes \begin{pmatrix} J_S(z, \omega_J, \mu) \\ J_g(z, \omega_J, \mu) \end{pmatrix}$$

initial condition contains distributions in $1 - z$



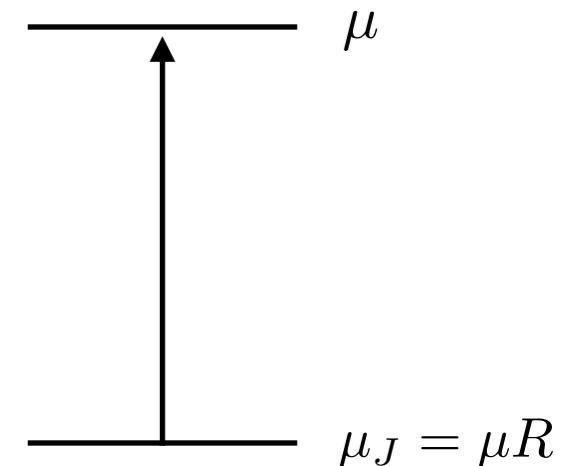
where

$$J_S(z, \omega_J, \mu) = \sum_{q, \bar{q}} J_q(z, \omega_J, \mu) = 2N_f J_q(z, \omega_J, \mu) \quad (\text{singlet jet function})$$

Jet function evolution

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where

$$J_S(z, \omega_J, \mu) = \sum_{q, \bar{q}} J_q(z, \omega_J, \mu) = 2N_f J_q(z, \omega_J, \mu)$$

(singlet jet function)

solve in Mellin space:

$$f(N) = \int_0^1 dz z^{N-1} f(z)$$

$$(f \otimes g)(N) = f(N) g(N)$$

Jet function evolution

solve in Mellin space to LL_R

$$\begin{pmatrix} J_S(N, \omega_J, \mu) \\ J_g(N, \omega_J, \mu) \end{pmatrix} = \left[e_+(N) \left(\frac{\alpha_s(\mu)}{\alpha_s(\mu_J)} \right)^{-r_-(N)} + e_-(N) \left(\frac{\alpha_s(\mu)}{\alpha_s(\mu_J)} \right)^{-r_+(N)} \right] \begin{pmatrix} J_S(N, \omega_J, \mu_J) \\ J_g(N, \omega_J, \mu_J) \end{pmatrix}$$

where
$$e_{\pm}(N) = \frac{1}{r_{\pm}(N) - r_{\mp}(N)} \begin{pmatrix} P_{qq}(N) - r_{\mp}(N) & 2N_f P_{gq}(N) \\ P_{qg}(N) & P_{gg}(N) - r_{\mp}(N) \end{pmatrix}$$

see

Vogt '04 (Pegasus),
Anderle, FR, Stratmann '15

$$r_{\pm}(N) = \frac{1}{2\beta_0} \left[P_{qq}(N) + P_{gg}(N) \pm \sqrt{(P_{qq}(N) - P_{gg}(N))^2 + 4P_{qg}(N)P_{gq}(N)} \right]$$

Jet function evolution

solve in Mellin space to LL_R

$$\begin{pmatrix} J_S(N, \omega_J, \mu) \\ J_g(N, \omega_J, \mu) \end{pmatrix} = \left[e_+(N) \left(\frac{\alpha_s(\mu)}{\alpha_s(\mu_J)} \right)^{-r_-(N)} + e_-(N) \left(\frac{\alpha_s(\mu)}{\alpha_s(\mu_J)} \right)^{-r_+(N)} \right] \begin{pmatrix} J_S(N, \omega_J, \mu_J) \\ J_g(N, \omega_J, \mu_J) \end{pmatrix}$$

where
$$e_{\pm}(N) = \frac{1}{r_{\pm}(N) - r_{\mp}(N)} \begin{pmatrix} P_{qq}(N) - r_{\mp}(N) & 2N_f P_{gq}(N) \\ P_{qg}(N) & P_{gg}(N) - r_{\mp}(N) \end{pmatrix}$$

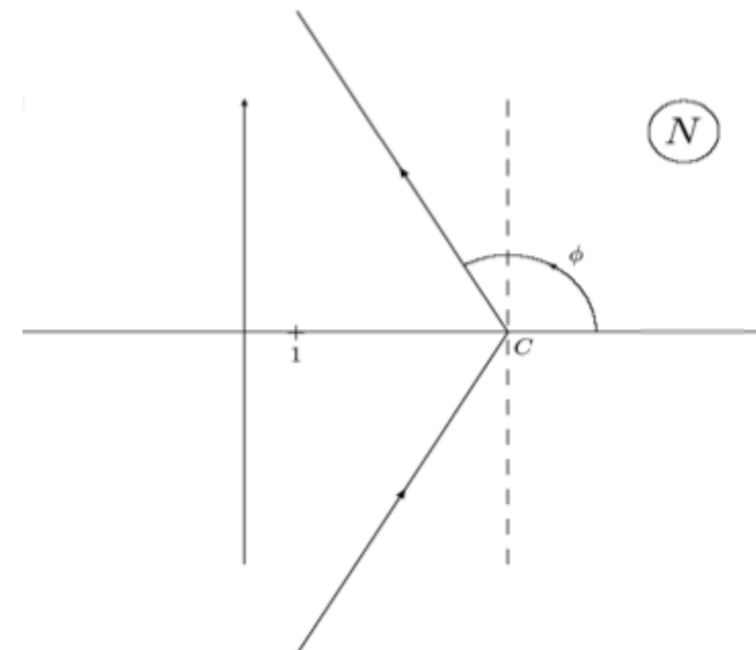
see

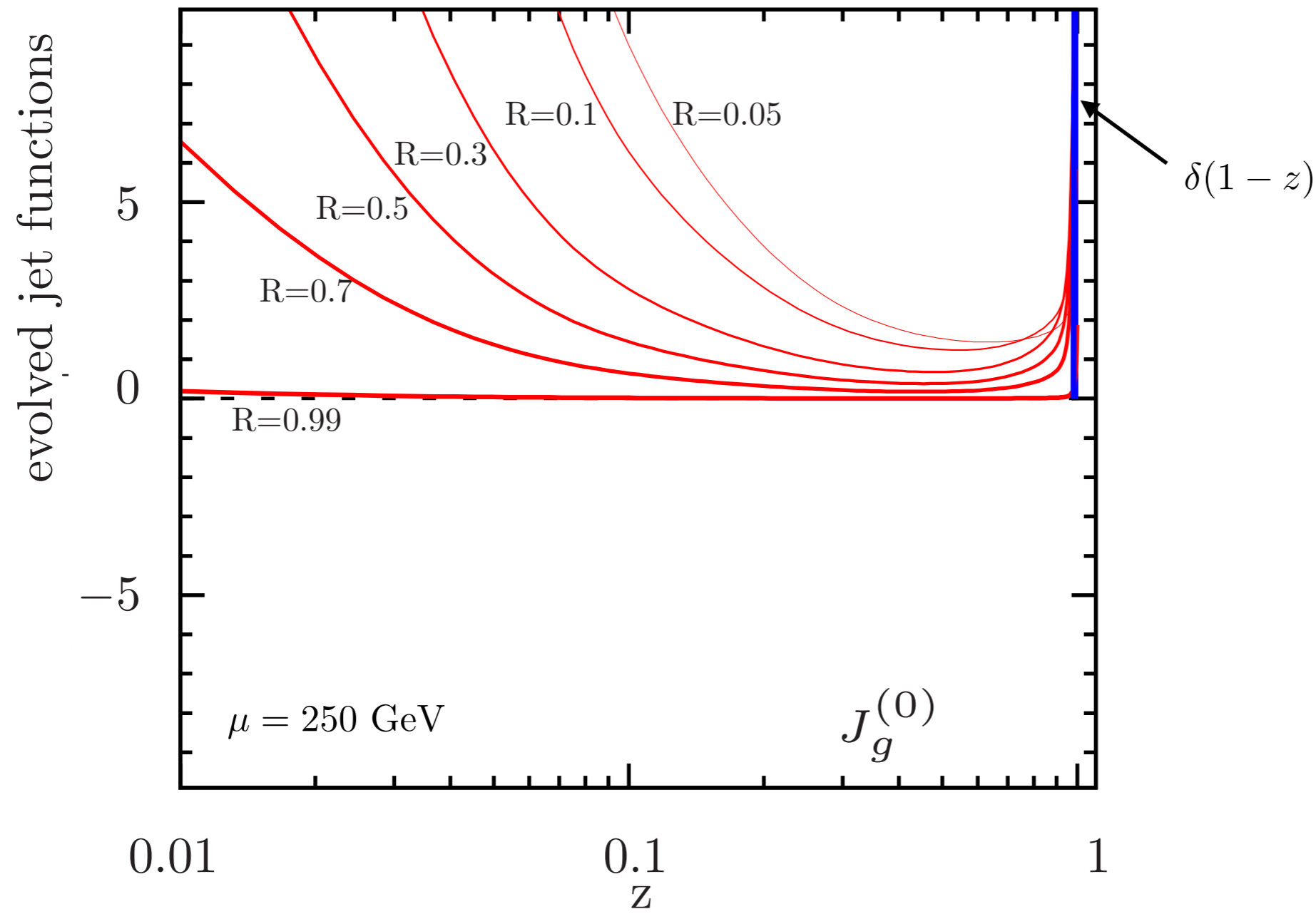
Vogt '04 (Pegasus),
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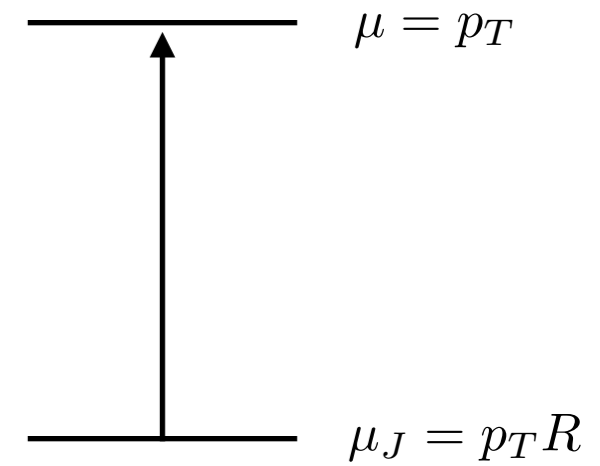
Mellin inverse

$$J_{S,g}(z, \omega_J, \mu) = \frac{1}{2\pi i} \int_{C_N} dN z^{-N} J_{S,g}(N, \omega_J, \mu)$$

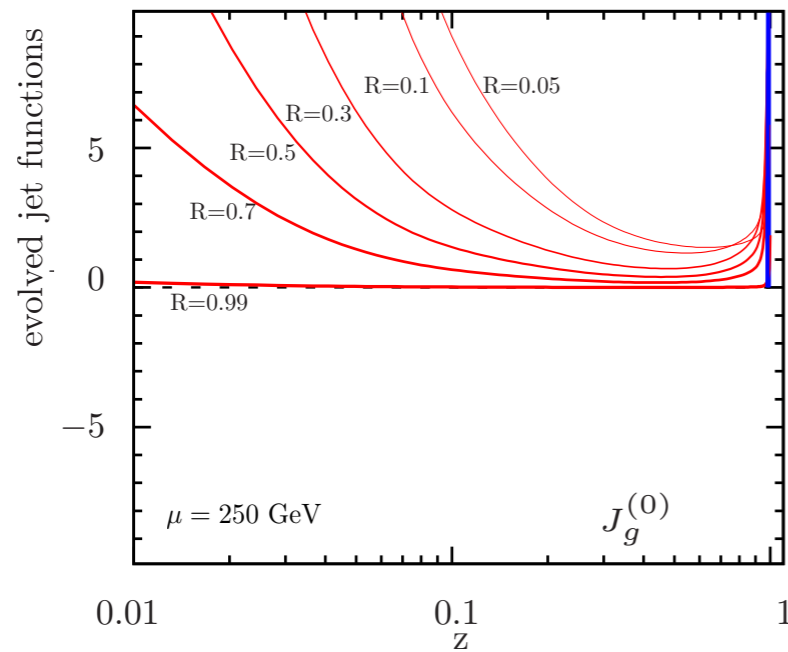




LL_R DGLAP evolution



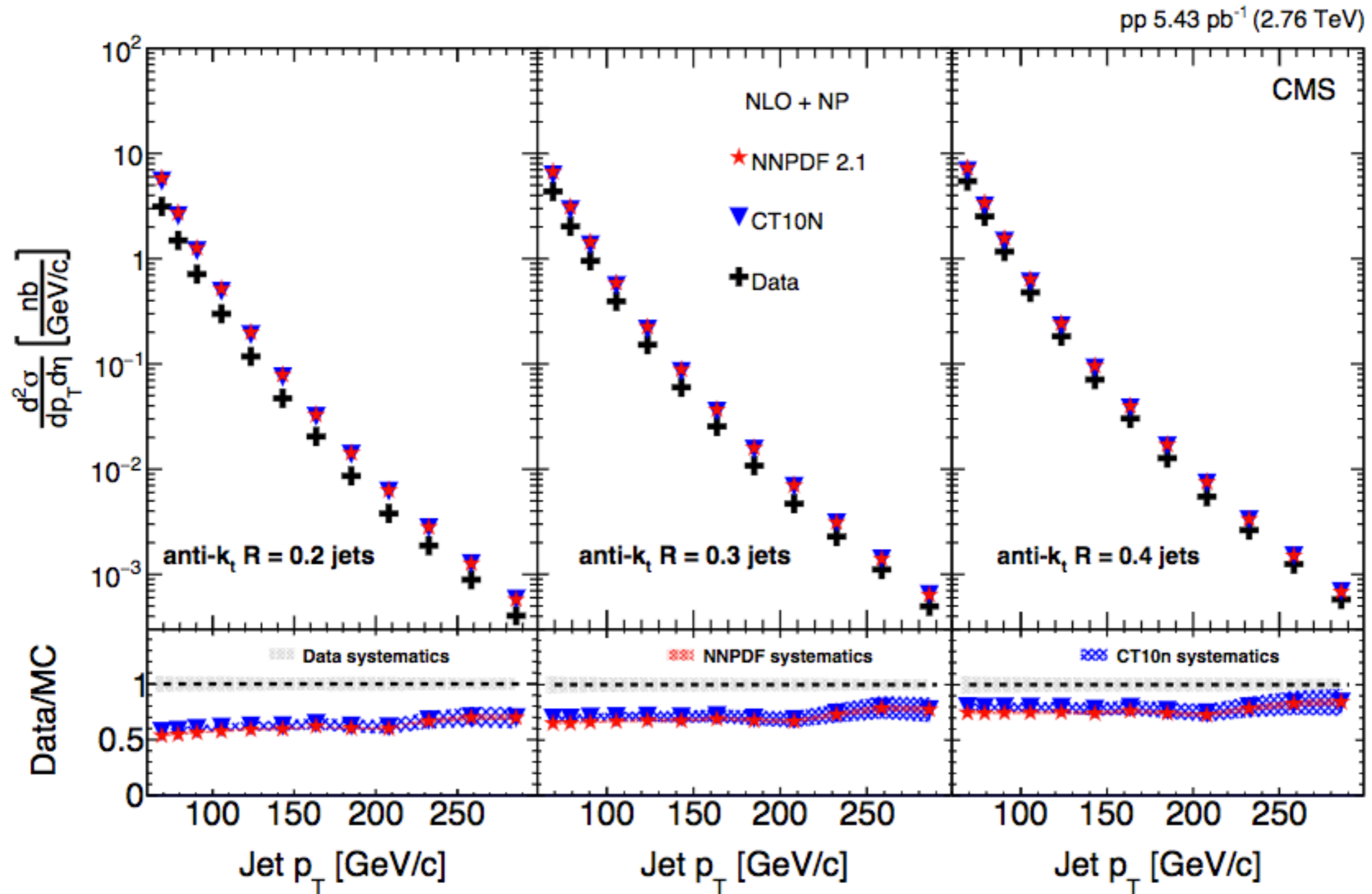
see
 Vogt '04 (Pegasus),
 Anderle, FR, Stratmann '15



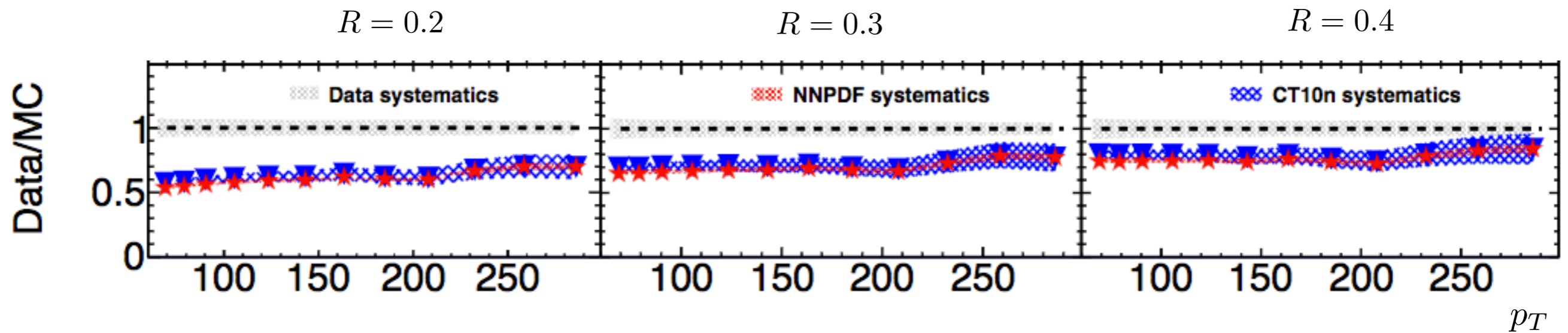
$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}^c \otimes J_c$$

- Resummation of $\alpha_s^n \ln^n R$
- Adopt a prescription used for quarkonium fragmentation functions
Bodwin, Chao, Chung, Kim, Lee, Ma '16

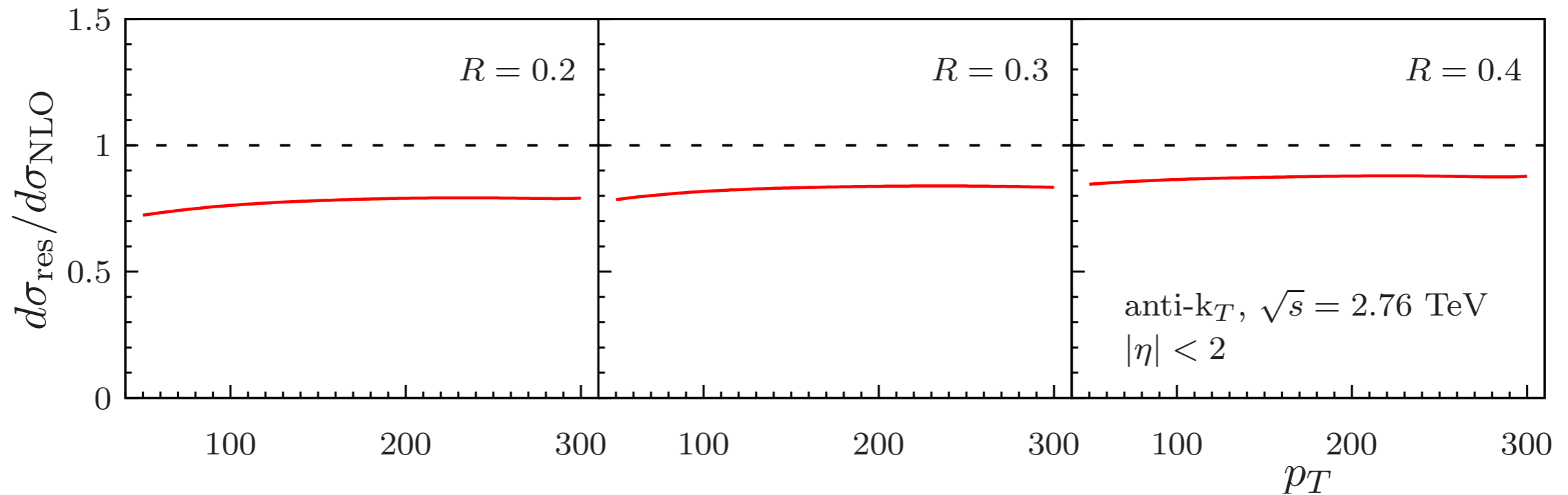
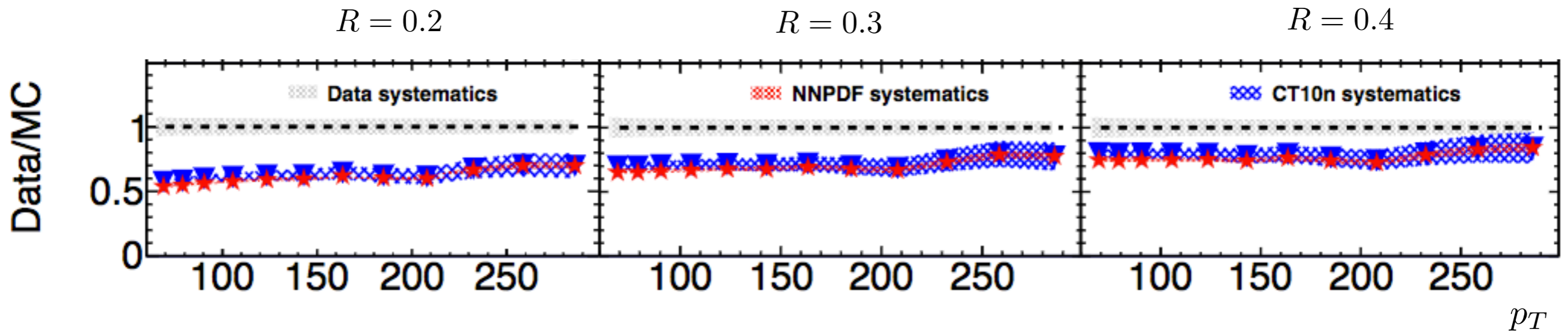
Inclusive Jet Production in SCET $pp \rightarrow \text{jet} X$



Inclusive Jet Production in SCET $pp \rightarrow \text{jet} X$



Inclusive Jet Production in SCET $pp \rightarrow \text{jet} X$



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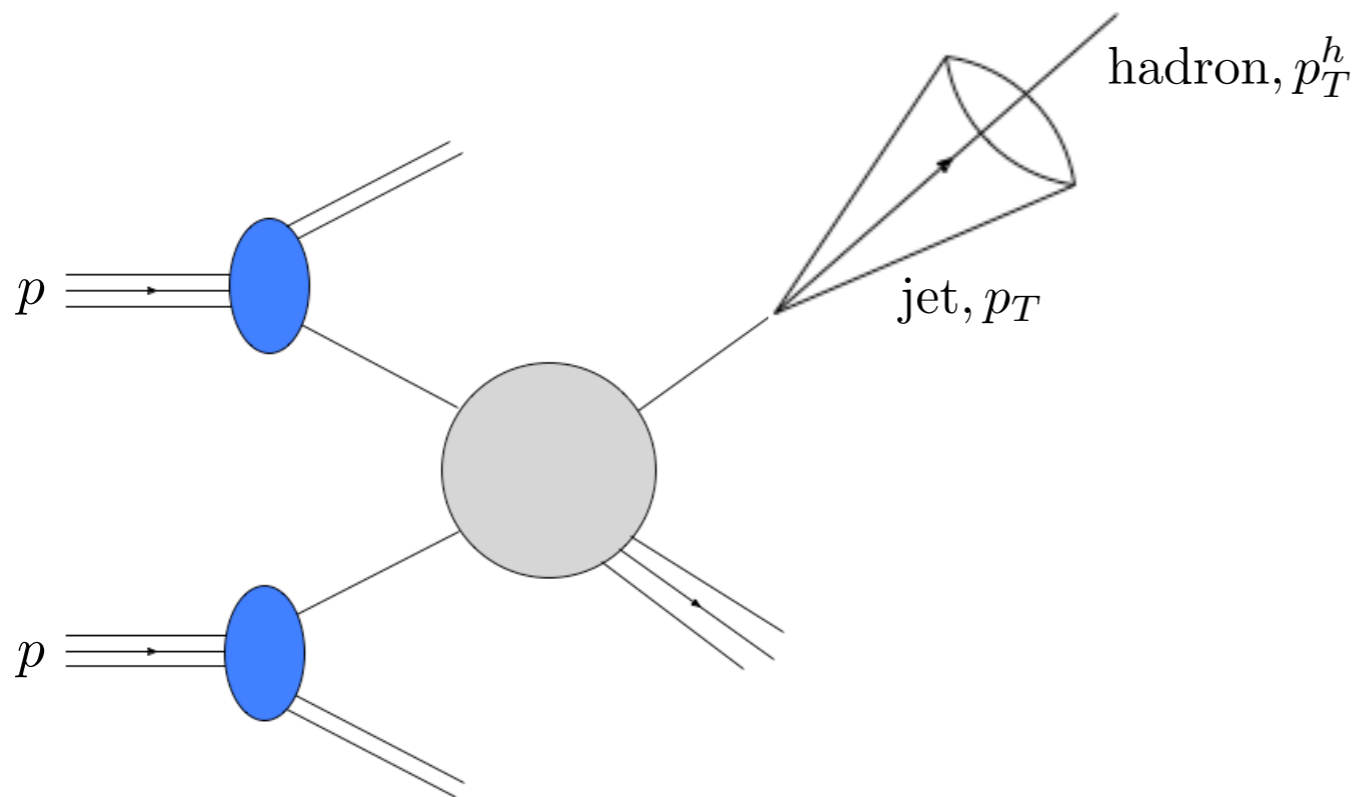
Kang, FR, Vitev '16

Chien, Kang, FR, Vitev, Xing '15

*Kang, Qiu, FR, Xing, Zhang
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Jet fragmentation function $pp \rightarrow (\text{jet}h)X$

- Jet substructure observable studying the distribution of hadrons inside a jet
- Provides further constraints for fits of fragmentation functions
- Possible studies include spin correlations and TMDs
- Differential probe for the modification of jets in AA and eA



Jet fragmentation function

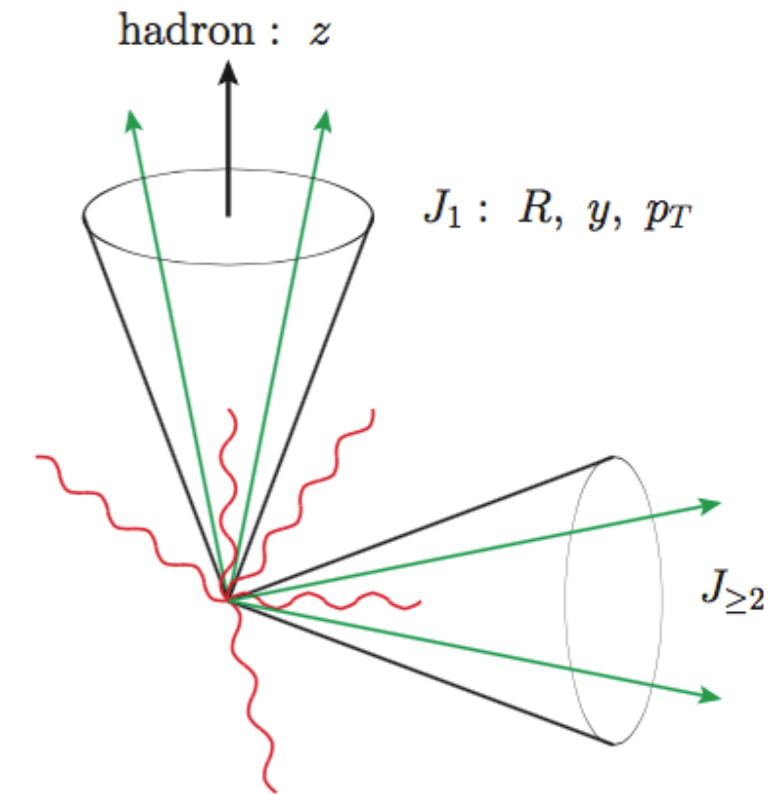
Definition:

$$F(z_h, p_T) = \frac{d\sigma^{pp \rightarrow (\text{jet}h)X}}{dp_T d\eta dz_h} / \frac{d\sigma^{pp \rightarrow \text{jet}X}}{dp_T d\eta}$$

where

$$z_h = p_T^h / p_T$$

The JFF describes the longitudinal momentum distribution of hadrons inside a reconstructed jet



Procura, Stewart `10; Liu `11; Jain, Procura, Waalewijn `11
 and `12; Procura, Waalewijn `12; Bauer, Mereghetti `14;
 Baumgart, Leibovich, Mehen, Rothstein `14,
 Chien, Kang, FR, Vitev, Xing `15,
 Bain, Dai, Hornig, Leibovich, Makris, Mehen `16,
 Bain, Makris, Mehen `16,
 Arleo, Fontannaz, Guillet, Nguyen `14,
 Kaufmann, Mukherjee, Vogelsang `15 ...

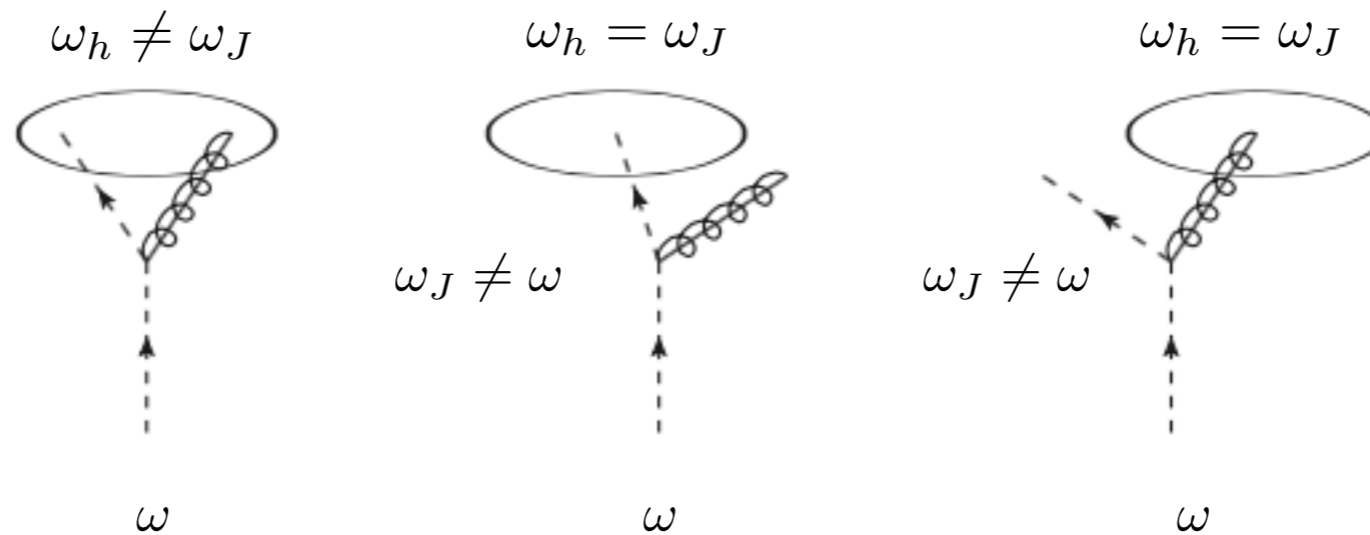
Semi-inclusive fragmenting jet function

Factorized cross section:
$$\frac{d\sigma^{pp \rightarrow (\text{jet}h)X}}{dp_T d\eta dz_h} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c^h$$

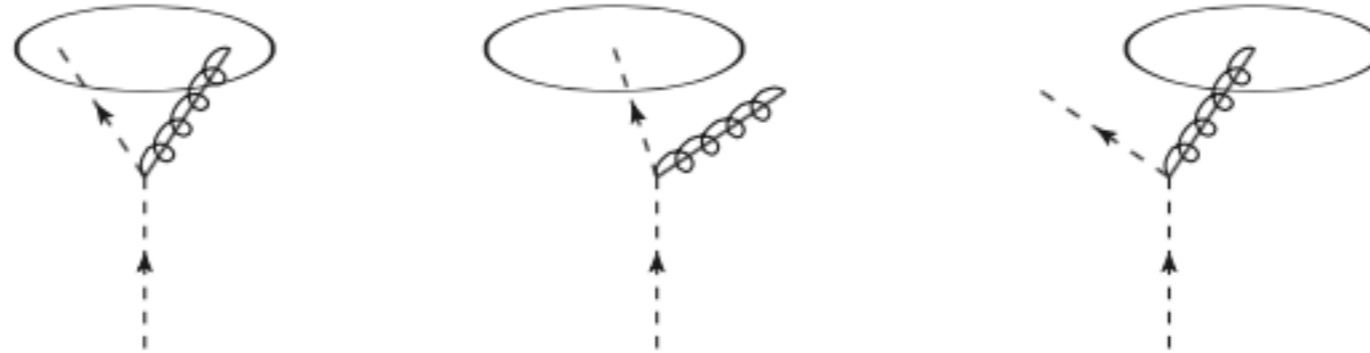
where
$$\mathcal{G}_i^h(z, z_h, \omega_J, \mu) = \sum_j \int_{z_h}^1 \frac{dz'_h}{z'_h} \mathcal{J}_{ij}(z, z'_h, \omega_J, \mu) D_j^h\left(\frac{z_h}{z'_h}, \mu\right)$$

NLO: $z = \omega_J/\omega$ $z_h = \omega_h/\omega_J$

- fragmenting parton
- jet $\omega_J = \omega$
- initiating parton ω



Semi-inclusive jet function

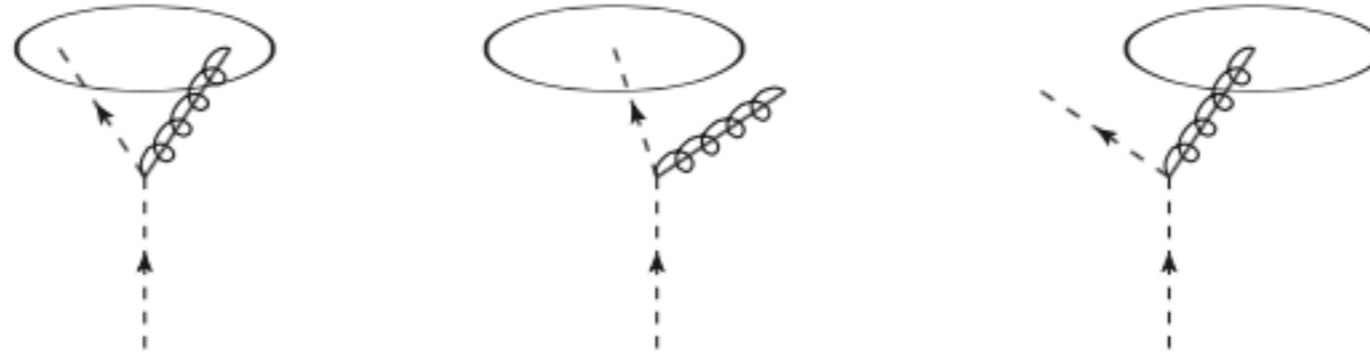


$\overline{\text{MS}}$ scheme, anti- k_T

Quark-quark:

$$\begin{aligned}
 \mathcal{G}_{q,\text{bare}}^q(z, z_h, \omega_J, \mu) = & \delta(1-z)\delta(1-z_h) + \frac{\alpha_s}{2\pi} \left(-\frac{1}{\epsilon} - L \right) P_{qq}(z_h)\delta(1-z) \\
 & + \frac{\alpha_s}{2\pi} \left(\frac{1}{\epsilon} + L \right) P_{qq}(z)\delta(1-z_h) \\
 & + \delta(1-z) \frac{\alpha_s}{2\pi} \left[2C_F(1+z_h^2) \left(\frac{\ln(1-z_h)}{1-z_h} \right)_+ + C_F(1-z_h) + 2P_{qq}(z_h) \ln z_h \right] \\
 & - \delta(1-z_h) \frac{\alpha_s}{2\pi} \left[2C_F(1+z^2) \left(\frac{\ln(1-z)}{1-z} \right)_+ + C_F(1-z) \right]
 \end{aligned}$$

Semi-inclusive jet function



$\overline{\text{MS}}$ scheme, anti- k_T

Quark-quark:

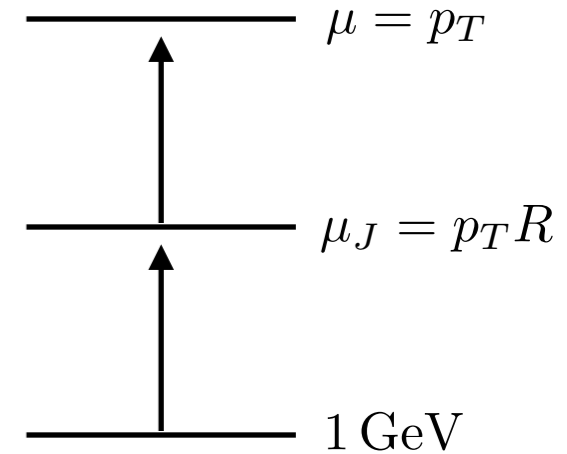
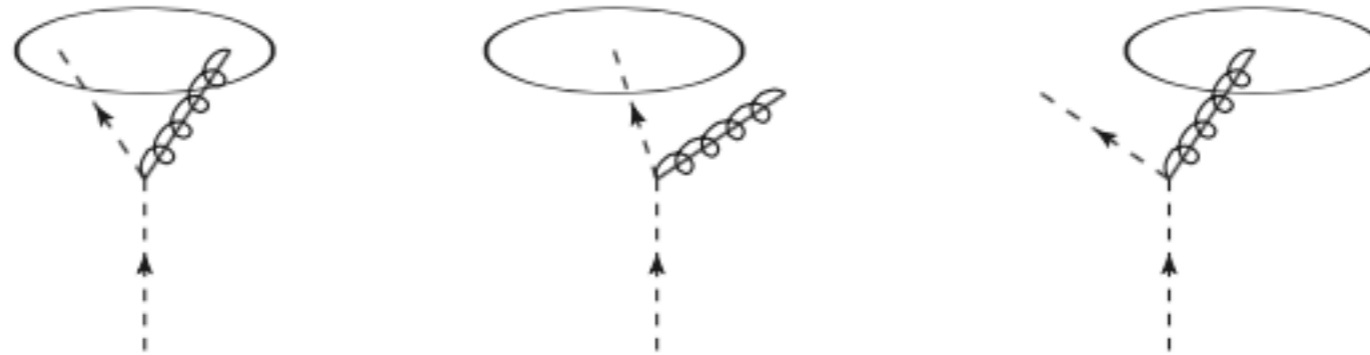
$$\begin{aligned}
 \mathcal{G}_{q,\text{bare}}^q(z, z_h, \omega_J, \mu) &= \delta(1-z)\delta(1-z_h) + \frac{\alpha_s}{2\pi} \left(-\frac{1}{\epsilon} - L \right) P_{qq}(z_h) \delta(1-z) \\
 &+ \frac{\alpha_s}{2\pi} \left(\frac{1}{\epsilon} + L \right) P_{qq}(z) \delta(1-z_h) \\
 &+ \delta(1-z) \frac{\alpha_s}{2\pi} \left[2C_F(1+z_h^2) \left(\frac{\ln(1-z_h)}{1-z_h} \right)_+ + C_F(1-z_h) + 2P_{qq}(z_h) \ln z_h \right] \\
 &- \delta(1-z_h) \frac{\alpha_s}{2\pi} \left[2C_F(1+z^2) \left(\frac{\ln(1-z)}{1-z} \right)_+ + C_F(1-z) \right]
 \end{aligned}$$

IR (circled around the first term) and UV (circled around the second term)

Matching:

$$\mathcal{G}_i^h(z, z_h, \omega_J, \mu) = \sum_j \int_{z_h}^1 \frac{dz'_h}{z'_h} \mathcal{J}_{ij}(z, z'_h, \omega_J, \mu) D_j^h\left(\frac{z_h}{z'_h}, \mu\right)$$

Semi-inclusive jet function



Quark-quark:

$$\begin{aligned}
 \mathcal{G}_{q,\text{bare}}^q(z, z_h, \omega_J, \mu) &= \delta(1-z)\delta(1-z_h) + \frac{\alpha_s}{2\pi} \left(-\frac{1}{\epsilon} - L \right) P_{qq}(z_h) \delta(1-z) \\
 &+ \frac{\alpha_s}{2\pi} \left(\frac{1}{\epsilon} + L \right) P_{qq}(z) \delta(1-z_h) \\
 &+ \delta(1-z) \frac{\alpha_s}{2\pi} \left[2C_F(1+z_h^2) \left(\frac{\ln(1-z_h)}{1-z_h} \right)_+ + C_F(1-z_h) + 2P_{qq}(z_h) \ln z_h \right] \\
 &- \delta(1-z_h) \frac{\alpha_s}{2\pi} \left[2C_F(1+z^2) \left(\frac{\ln(1-z)}{1-z} \right)_+ + C_F(1-z) \right]
 \end{aligned}$$

... 2 DGLAPs now

Matching:

$$\mathcal{G}_i^h(z, z_h, \omega_J, \mu) = \sum_j \int_{z_h}^1 \frac{dz'_h}{z'_h} \mathcal{J}_{ij}(z, z'_h, \omega_J, \mu) D_j^h\left(\frac{z_h}{z'_h}, \mu\right)$$

In-jet fragmentation

- Light charged hadrons

Arleo, Fontannaz, Guillet, Nguyen `14,

Kaufmann, Mukherjee, Vogelsang `15

Kang, FR, Vitev `15

- Photons

Kaufmann, Mukherjee, Vogelsang `16

- Heavy flavor mesons

Chien, Kang, FR, Vitev, Xing `15

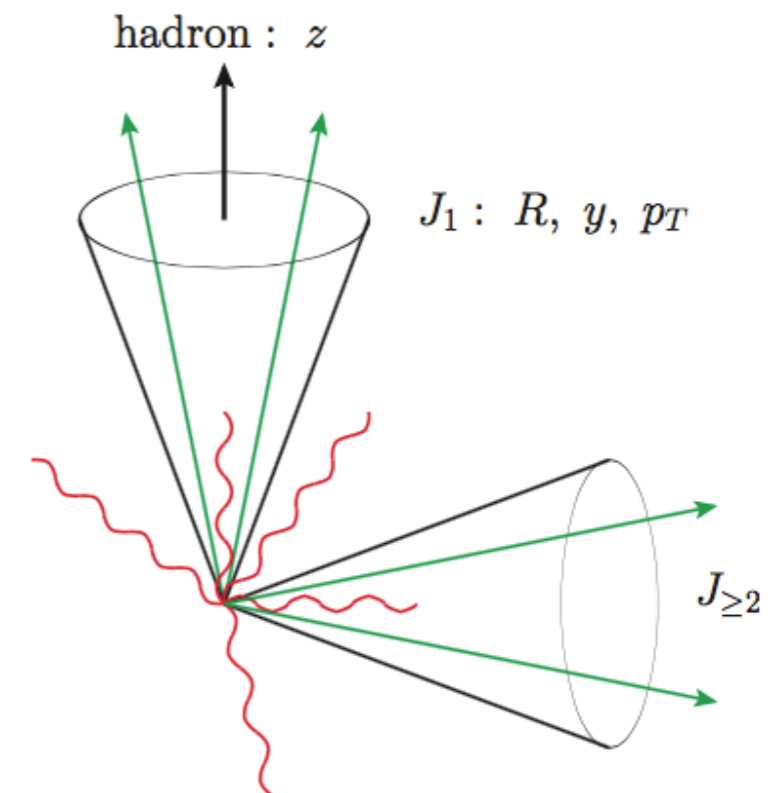
Bain, Dai, Hornig, Leibovich, Makris, Mehen `16

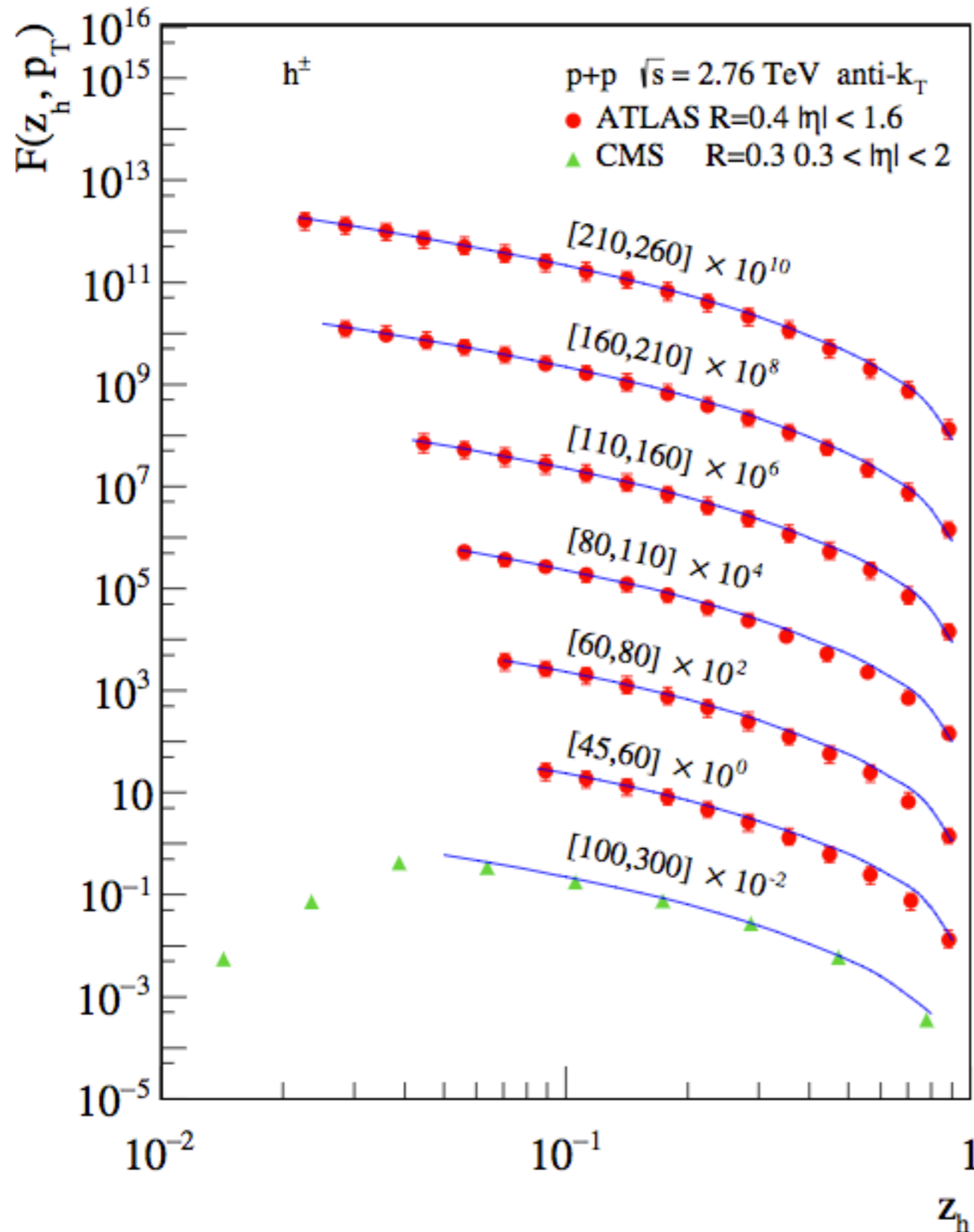
- Quarkonia

Baumgart, Leibovich, Mehen, Rothstein `14

Bain, Dai, Hornig, Leibovich, Makris, Mehen `16

Kang, Qiu, FR, Xing, Zhang - in preparation

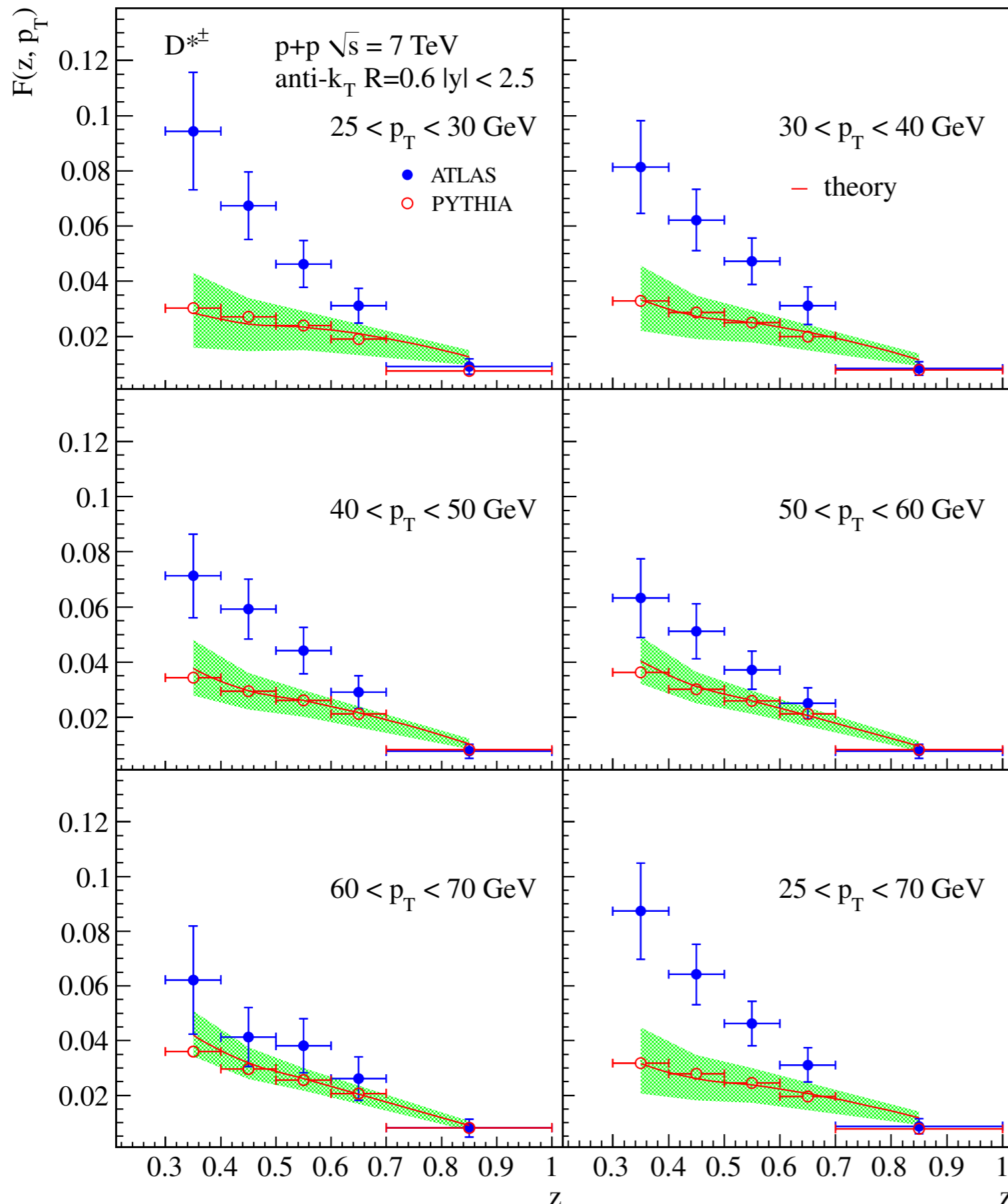




Comparison to ATLAS and CMS data at $\sqrt{s} = 2.76$ TeV

Light charged hadrons $h = \pi + K + p$

Using DSS FFs
de Florian, Sassot, Stratmann - '07

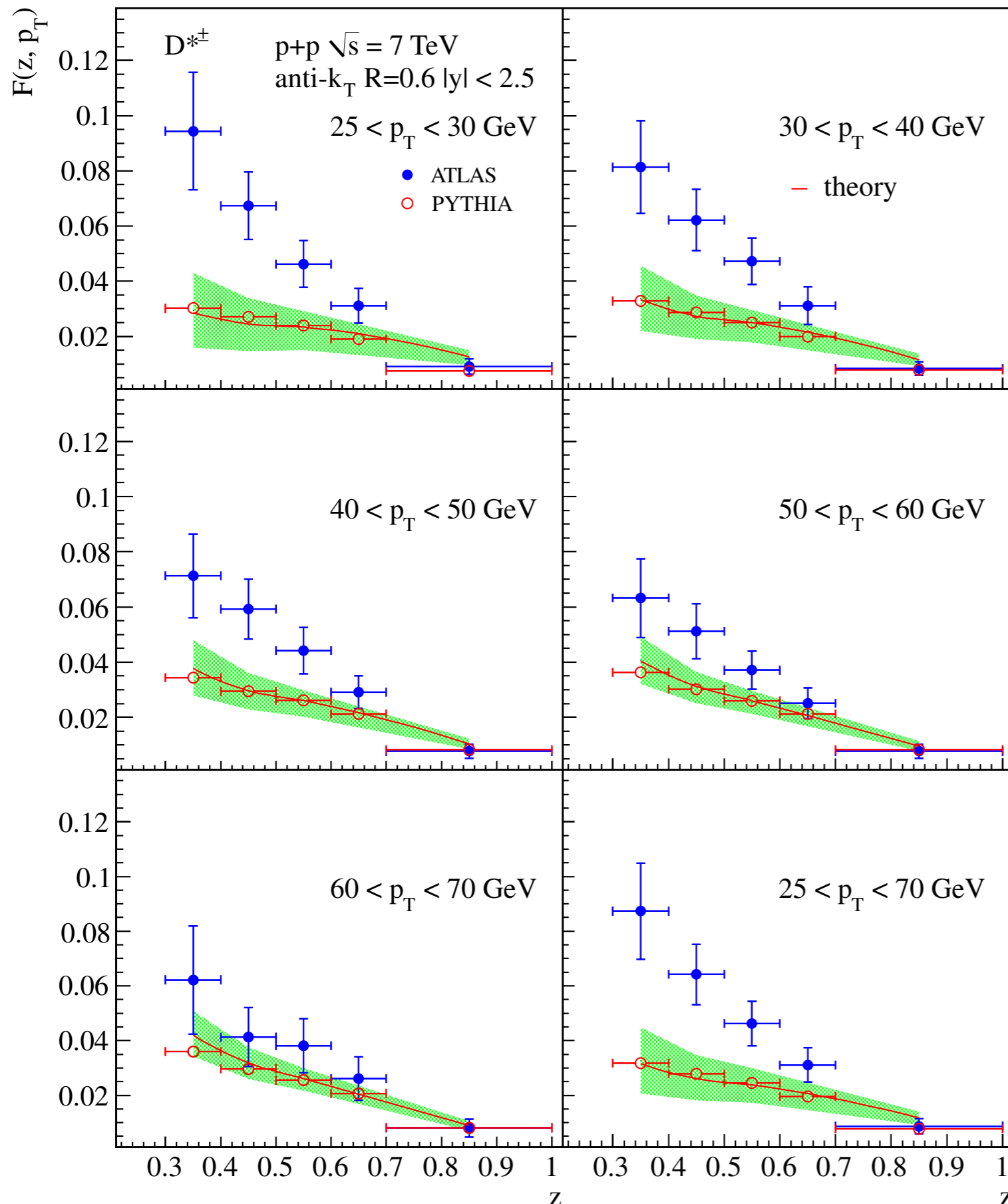


D-meson
jet fragmentation function

Comparison to ATLAS data
and PYTHIA simulations
at $\sqrt{s} = 7 \text{ TeV}$

Using FFs from
Kneesch, Kniehl, Kramer, Schienbein - '08

ZMVNFS, $e^+e^- \rightarrow DX$
 $\mu, \mu_J, \mu_g \gg m_Q$



D-meson
jet fragmentation function

Comparison to ATLAS data
and PYTHIA simulations
at $\sqrt{s} = 7 \text{ TeV}$

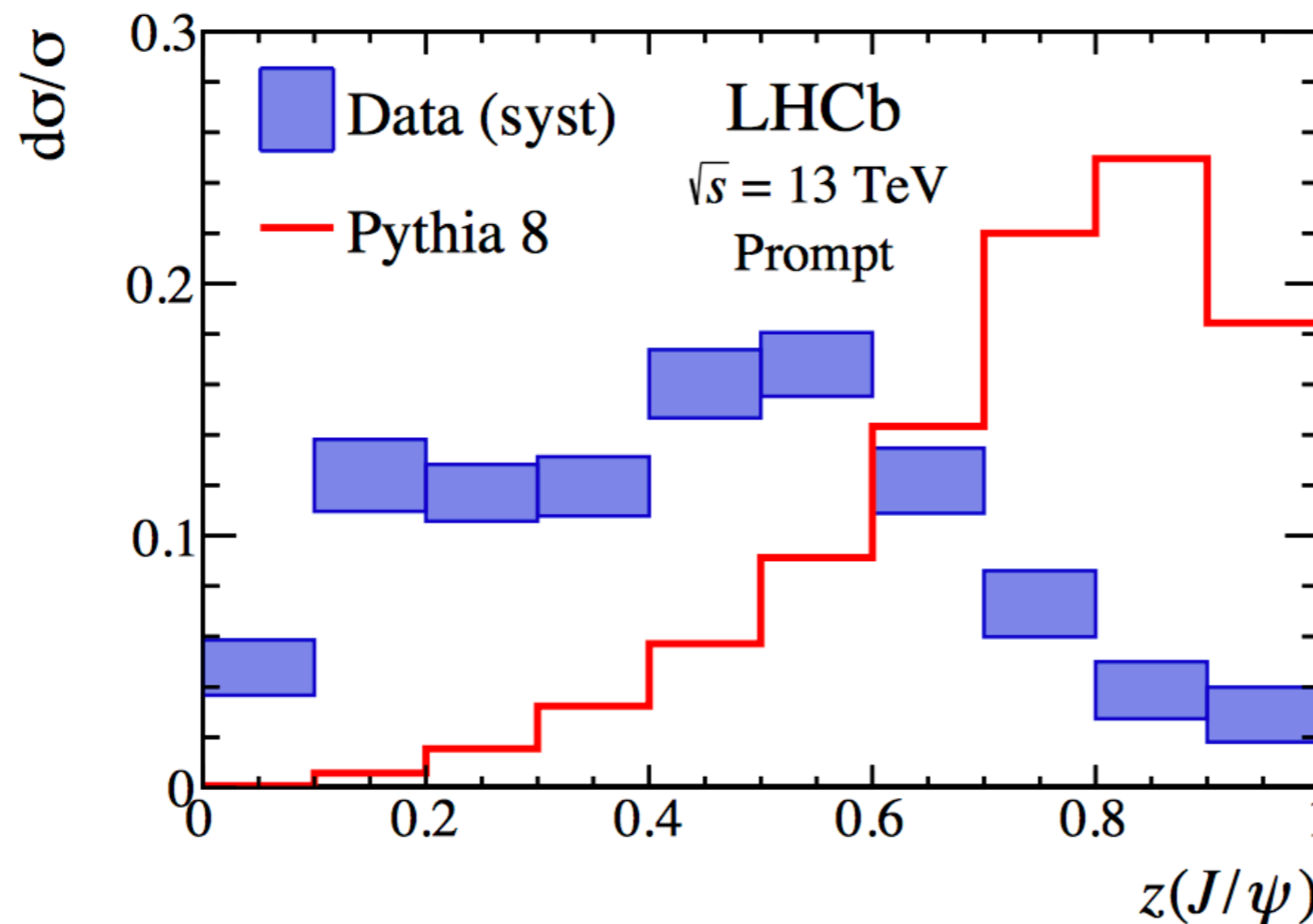
Using FFs from
Kneesch, Kniehl, Kramer, Schienbein - '08

ZMVNFS, $e^+e^- \rightarrow DX$
 $\mu, \mu_J, \mu_g \gg m_Q$

New global fit of D-meson FFs:
Anderle, Kaufmann, FR, Stratmann, Vitev
- in preparation

Quarkonium-in-jet fragmentation

- Quarkonium-in-jet fragmentation proposed in *Baumgart, Leibovich, Mehen, Rothstein '14*
Bain, Dai, Hornig, Leibovich, Makris, Mehen '16
- J/ψ -in-jet measurement from LHCb *arXiv: 1701.05111*



- Semi-inclusive in-jet fragmentation $pp \rightarrow (\text{jet } J/\psi) X$
Kang, Qiu, FR, Xing, Zhang - in preparation

J/psi fragmentation functions

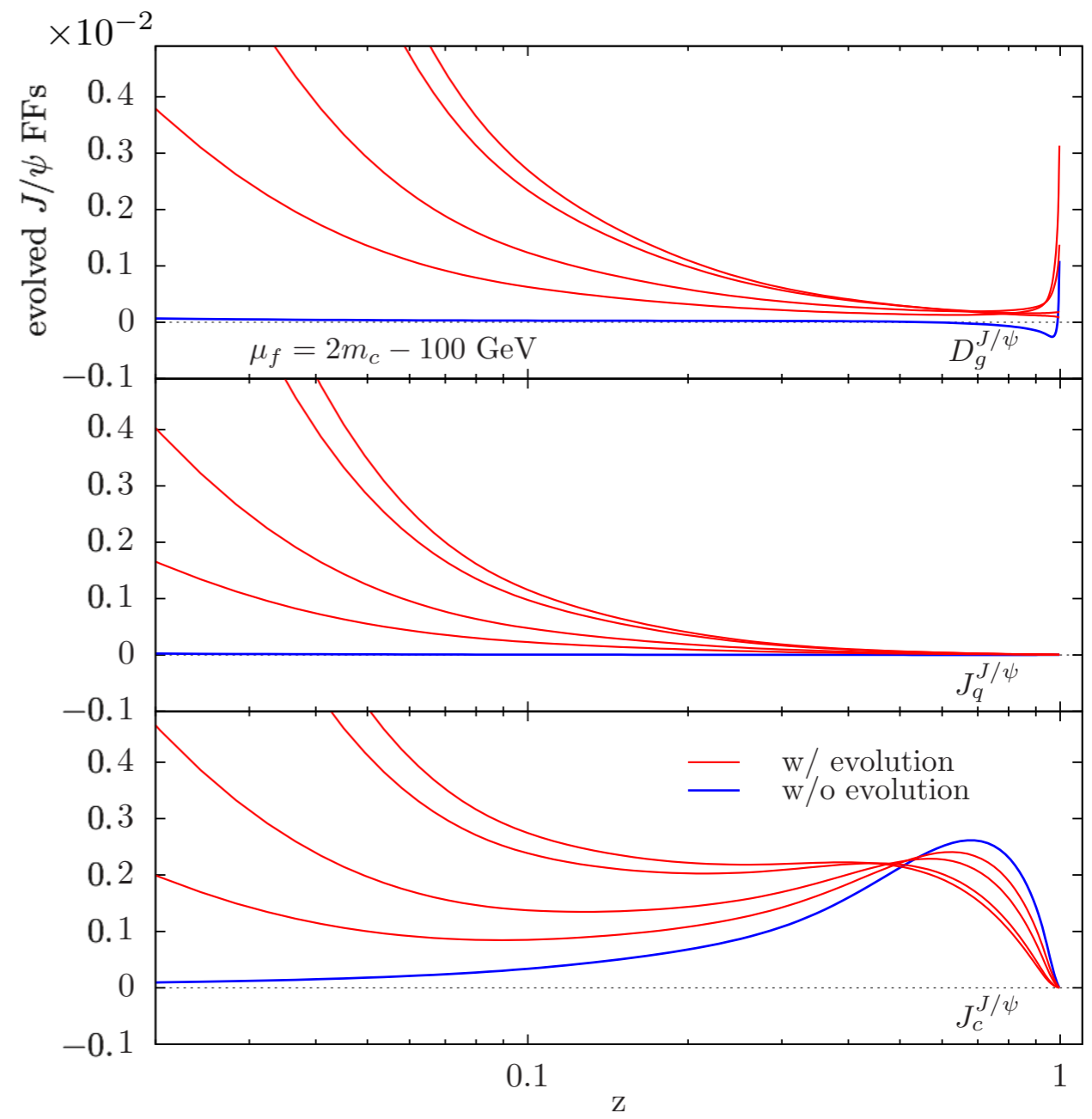
Single-parton FFs:

$$D_{i \rightarrow J/\psi}(z) = \sum_{n_\lambda} \pi \alpha_s \hat{d}_{i \rightarrow Q\bar{Q}(n_\lambda)}(z) \langle \mathcal{O}_{Q\bar{Q}(n_\lambda)}^{J/\psi} \rangle$$

NRQCD LDMEs

perturbatively calculable

... evolution again with DGLAP in Mellin moment space



LDMEs: Butenschoen, Kniehl '14

Braaten, Yuan '93, Kang, Qiu, Sterman '12, Ma, Qiu, Zhang '13 ...



J/psi siFJF

$$\frac{d\sigma^{pp \rightarrow (\text{jet} J/\psi) X}}{dp_T d\eta dz_h} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c^h$$

where $\mathcal{G}_i^h(z, z_h, \omega_J, \mu) = \sum_j \int_{z_h}^1 \frac{dz'_h}{z'_h} \mathcal{J}_{ij}(z, z'_h, \omega_J, \mu) D_j^h\left(\frac{z_h}{z'_h}, \mu\right)$

evolved FFs



J/psi siFJF

$$\frac{d\sigma^{pp \rightarrow (\text{jet} J/\psi) X}}{dp_T d\eta dz_h} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c^h$$

where $\mathcal{G}_i^h(z, z_h, \omega_J, \mu) = \sum_j \int_{z_h}^1 \frac{dz'_h}{z'_h} \mathcal{J}_{ij}(z, z'_h, \omega_J, \mu) D_j^h\left(\frac{z_h}{z'_h}, \mu\right)$

evolved FFs



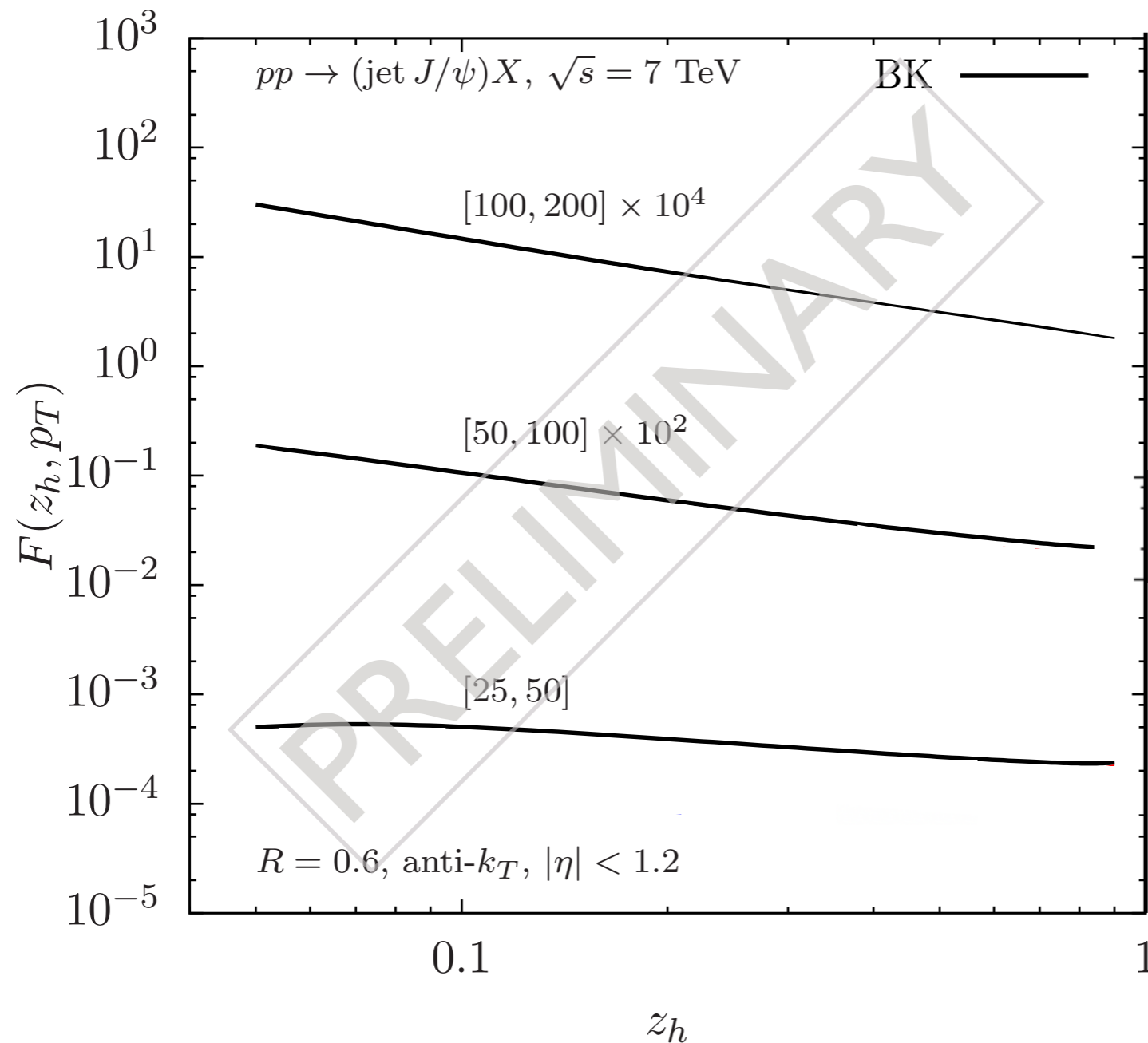
Take Mellin moments wrt z_h :

$$\int_0^1 dz_h z_h^{N-1} \mathcal{G}_i^h(z, z_h, \omega_J, \mu) = \sum_j \mathcal{J}_{ij}(z, N, \omega_J, \mu) D_j^h(N, \mu)$$

Quarkonium-in-jet fragmentation

- semi-inclusive in-jet fragmentation $pp \rightarrow (\text{jet } J/\psi) X$

Kang, Qiu, FR, Xing, Zhang - in preparation



LDMEs:

Butenschoen, Kniehl '14

Outline

- Inclusive jets
- The jet fragmentation function
- **Conclusions**

Kang, FR, Vitev `16

Kang, FR, Vitev `16

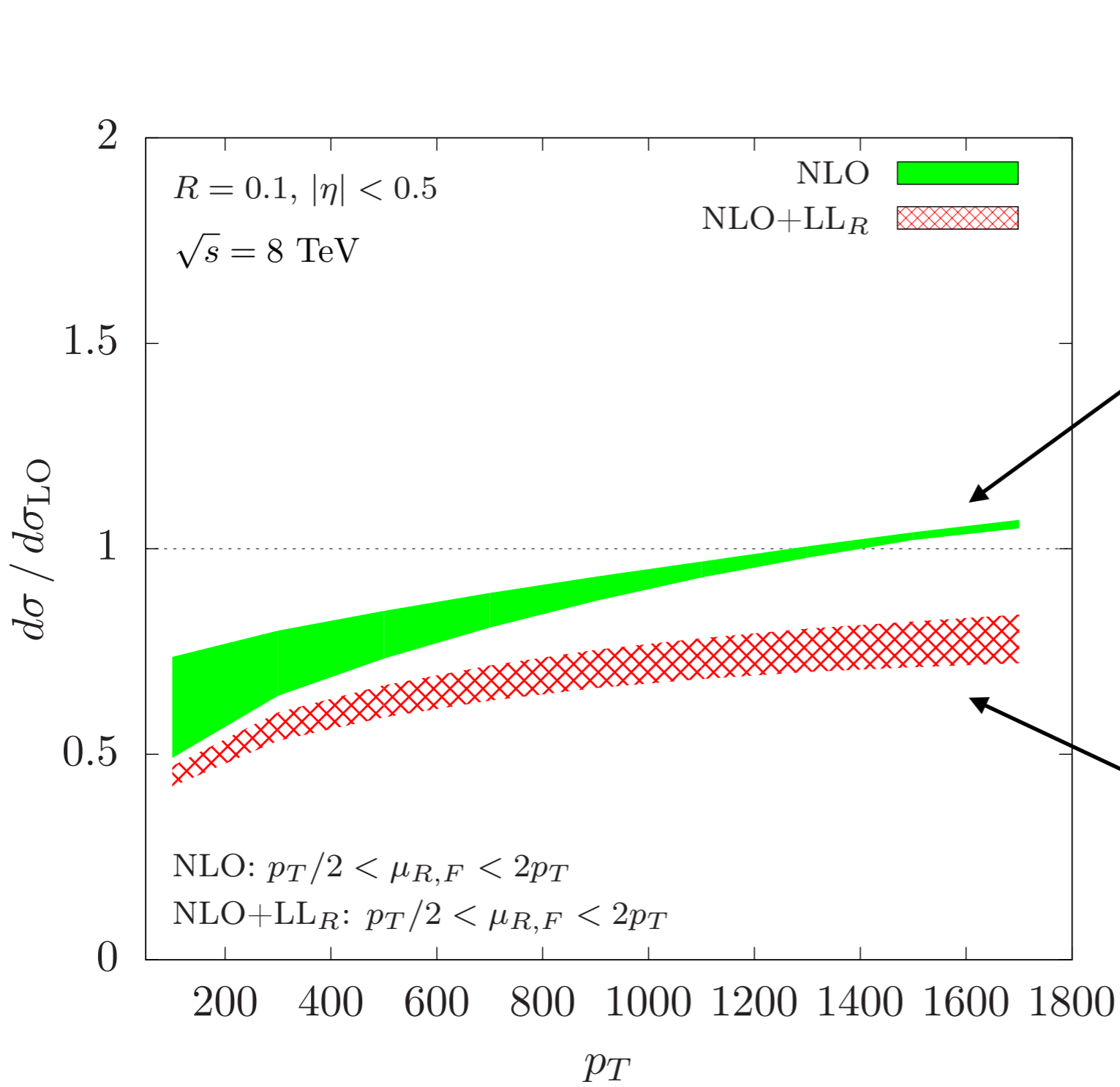
Chien, Kang, FR, Vitev, Xing `15

*Kang, Qiu, FR, Xing, Zhang
- in preparation*

Conclusions

- (Semi-) inclusive jet observables in SCET
- Longitudinal hadron-in-jet distribution
- New constraints for global fits of FFs/ LDMEs

- TMDs, spin-asymmetries inside jets ...



LL_R DGLAP evolution

Vanishing, unphysical scale dependence

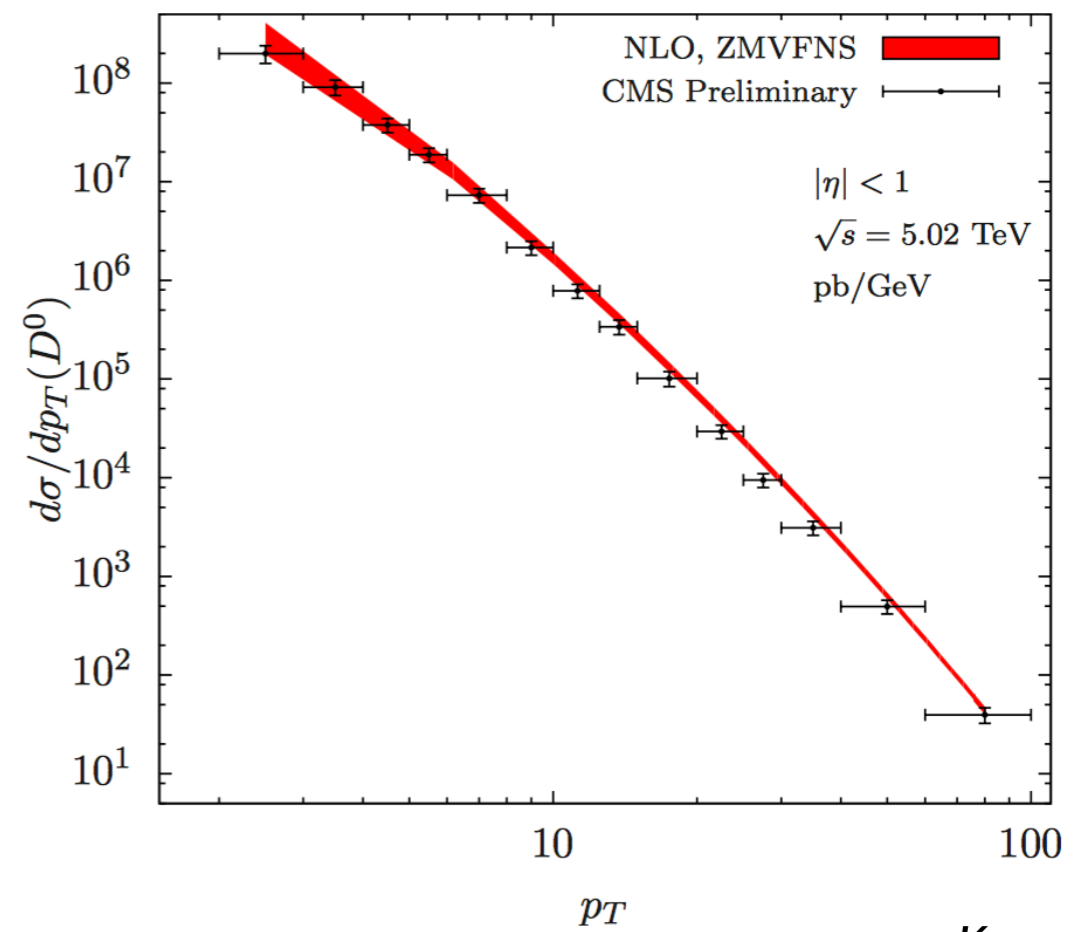
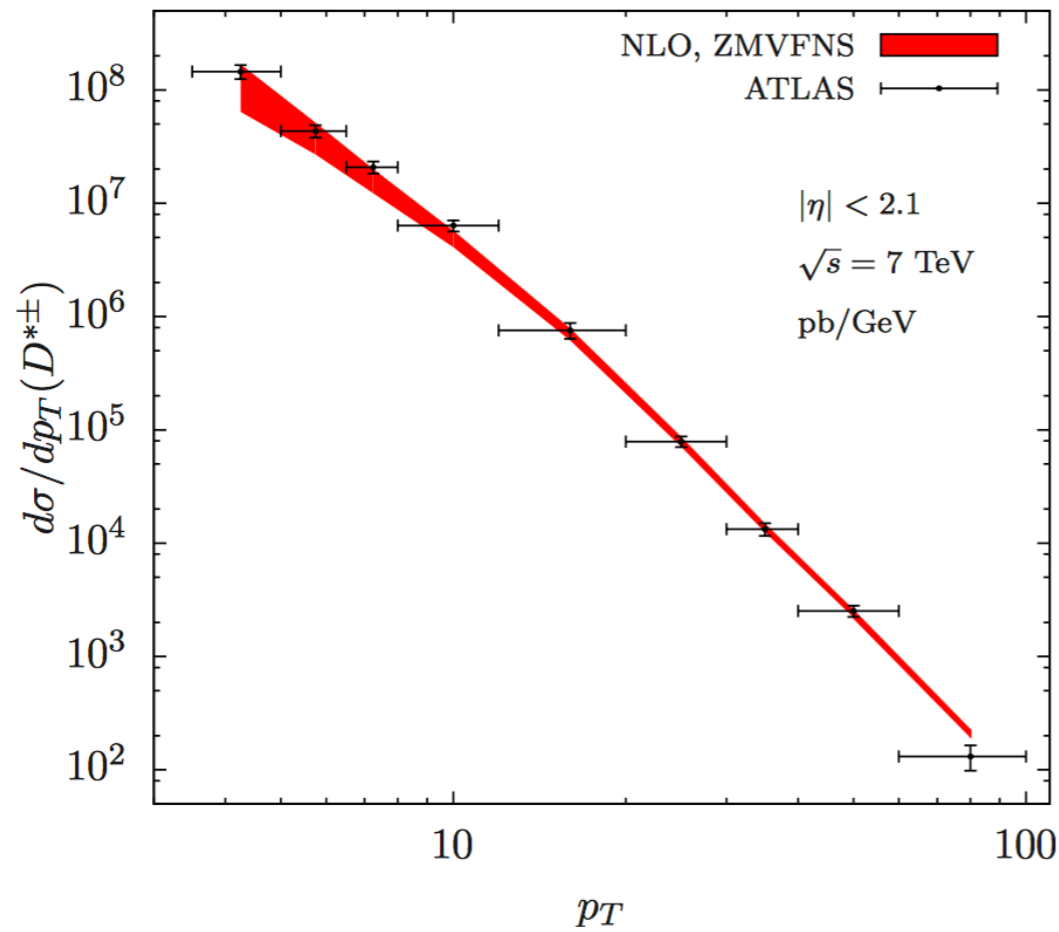
Note: same at NNLO (large- N_c)
Currie, Glover, Pires '16

Additional final state factorization

see also
Dasgupta, Dreyer, Salam, Soyez '15, '16

Inclusive D-meson production in pp

NLO + ZMVFNS FFs from
Knesch, Kniehl, Kramer, Schienbein - '08



Kang, FR, Vitev '16