Recent results on exclusive hadronic cross sections measurements with the *BABAR* detector



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# $a_{\ell} = \frac{1}{2}(g-2)_{\ell}$ precision test of QED

- OK for electrons
- long-standing  $\approx 3 \sigma$  discrepancy for muons



#### Low energy hadronic cross sections and $a_{\mu}$

The dominant correction and error from hadronic vacuum polarization

$a_{\mu} = (g-2)_{\mu} / 2$ Individual SM contributions × 10 <sup>-11</sup>				
a, QED	116584718.951 ± 0.080			
a_EW	153.6 ± 1.0			
a had,LO-VP	6923 ± 42			
$a_{\mu}^{had,HO-VP}$	-98.4 ± 0.7			
$a_{\mu}^{had,LbLs}$	105 ± 26			
Comparison with measurement				
$\mathbf{a}_{\mu}^{\text{total-SM}}$	116591802 ± 49			
$a_{\mu}^{\text{BNL-E821}}$	116592089 ± 63			
Data - SM	287 + 80			

M. Davier et al., EPJ C71, 1515 (2011)

at low energies total hadronic cross section determined from (finite) sum of exclusive modes





Many exclusive modes measured by BABAR

New preliminary measurements for

- $\pi^+\pi^-\pi^0\pi^0$
- $\pi^+\pi^-\eta$
- $K_s^0 K_L^0 \pi^0$ ;  $K_s^0 K_L^0 \eta$ ;  $K_s^0 K_L^0 \pi^0 \pi^0$
- $K_{s}^{0}K^{+}\pi^{+}\pi^{0}$ ;  $K_{s}^{0}K^{+}\pi^{+}\eta$



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#### The BABAR experiment



#### Data samples

As of 2008/04/11 00:00





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#### The ISR method at the $\Upsilon(4S)$

Initial State Radiation from  $e^+e^-$  allows to measure cross sections at all center-of-mass energies  $\sqrt{s'}$  below the nominal  $\sqrt{s}$  of the beams

$$\frac{\mathrm{d}\sigma(s;s';\theta_{\gamma})}{\mathrm{d}s'\mathrm{d}\theta_{\gamma}} = W(s;s';\theta_{\gamma}) \cdot \sigma_{x}(s')$$



tag photon to identify ISR events

- hadrons in fiducial detector region
- fully reconstruct the final state
- kinematic fit: energy resolution

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boost \implies harder momentum spectrum for daughter particles
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- cross sections down to threshold
- measure  $\sigma$  at all  $\sqrt{s}$  simultaneously
- large "effective" luminosity





#### $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$

One of the least known cross sections among those relevant to  $(g-2)_{\mu}$ 

- ISR photon: highest energy photon with  $E_{\gamma}^{CM}>3~{
  m GeV}$
- exacty two oppositely charged tracks of p > 100 MeV
- at least 4 additional photons E > 50 MeV
- kinematic fit  $e^+e^- \rightarrow \gamma_{ISR} 4\pi$ : require  $\chi^2_{4\pi\gamma} < 30$

Explicitly veto backgrounds based on particle ID (kaons) and kinematic fit to any competing mode

non-ISR  $q\bar{q}$  events where photons from  $\pi^0$  misidentified as  $\gamma_{\rm ISR}$  subtracted based on simulation and  $\pi^0$  yield in  $\gamma_{\rm ISR}\gamma$  combinations

poorly known  $\pi^+\pi^-3\pi^0$  cross section: use data





### $e^+e^- ightarrow \pi^+\pi^-\pi^0\pi^0$ cross section



$$e^+e^- \rightarrow \pi^+\pi^-\eta$$

Expected to proceed via  $\rho\eta$ : important to understand higher  $\rho$  excitations Reconstruct  $\gamma_{\scriptscriptstyle ISR}\pi^+\pi^-\gamma\gamma$ ; kinematic fit.

Background modelled on MC extrapolating yields from data



Extract signal yield in each energy bin fitting the  $\gamma\gamma$  inv. mass residual background from processes with  $\eta$  subtracted using MC



#### $e^+e^- ightarrow \pi^+\pi^-\eta$ cross section



BABAR measurement compatible with previous measurements, but more precise and on a broader energy range





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the  $\pi^+\pi^-$  mass spectrum is not well described by the  $\rho(770)\eta$  model (already noticed by SND)

interference with  $\rho(1450)\eta$ ?



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#### VDM fits to the $e^+e^- \rightarrow \pi^+\pi^-\eta$ cross section





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 $e^+e^- 
ightarrow K^0_c K^0_c \pi^0$ 

Reconstruct  $\gamma_{\rm {\it ISR}}$  ,  $K^0_{\rm S}\to\pi^+\pi^-$  and  $\pi^0\to\gamma\gamma$ 

 $K_{L}^{0}$  detected as isolated energy cluster in the calorimeter E > 0.2 GeVvalidated on  $e^{+}e^{-} \rightarrow \gamma \phi \rightarrow \gamma K_{S}^{0} K_{L}^{0}$ Inv. mass resolution of hadronic system (after kin.fit):  $\approx 25 \text{ MeV}$ 





First measurement of this cross section

syst. uncertainty  $\approx 10\%$  at peak,  $\approx 30\%$  at 3.0 GeV





NFW

### Resonant substructures in $K_s^0 K_L^0 \pi^0$



Fit the (background-subtracted)  $K_s^0 \pi^0$ and  $K_{L}^0 \pi^0$  invariant mass distributions with coherent resonant/non resonant



Dominant  $K^*(892)^0 \overline{K}^0$  with small  $K_2^*(1430)^0 \overline{K}^0$ 



The  $K^*(892)^0 \bar{K}^0$  nearly saturates the  $K^0_s K^0_L \pi^0$  cross section small  $K^*_2(1430)^0 \bar{K}^0$  and  $\phi \pi^0$ 



## Total $K\bar{K}\pi$ cross section

Summing the  $K_s^0 K_L^0 \pi^0$  cross section and the other two charge configurations measured previously by *BABAR* PRD 77, 092002 (2008)



The  $K\bar{K}\pi$  is  $\approx 12\%$  of the total cross section for  $E \approx 1.65$  GeV





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Cross sections to final states with K and  $\eta$ 

Both measured for the first time!









NEW

#### $KK\pi\pi$ cross sections

Of the 6 possible charge combinations, 4 were already measured by BABAR



#### $KK\pi\pi$ cross sections



First (preliminary) measurement of the missing charge combinations:



 $K_{S}K_{I}\pi^{0}\pi^{0}$ 

BABAR preliminary

The total  $KK\pi\pi$  cross section is  $\approx 25\%$  of the total at  $E \approx 2$  GeV

now measured without any model assumption



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NEW

## $K^0_{_S}K^0_{_L}\pi^0(\pi^0)$ in the charmonium region



$$\sigma(e^+e^- 
ightarrow (car{c}) 
ightarrow X) \propto \Gamma((car{c}) 
ightarrow e^+e^-) imes \mathcal{B}((car{c}) 
ightarrow X)$$

|--|

Measured	Measured	Calculated Branching Frac	tions $(10^{-3})$
Quantity	Value (eV)	This work	Previous
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \to K^0_S K^0_L \pi^0}$	$11.4 \pm 1.3 \pm 0.6$	$2.06\ \pm 0.24 \pm 0.10$	-
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \to K^0_S K^0_L \eta}$	$8.0 \pm 1.8 \pm 0.4$	$1.45\ \pm 0.32 \pm 0.08$	-
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \to K^0_S K^0_L \pi^0 \pi^0}$	$10.3 \pm 2.3 \pm 0.5$	$1.86\ \pm 0.43 \pm 0.10$	-
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \to K^*(892)^0 \overline{K}^0 + c.c.} \cdot \mathcal{B}_{K^*(892)^0 \to K^0 \pi^0}$	$6.7 \pm 0.9 \pm 0.4$	$1.20\ \pm 0.15 \pm 0.06$	-
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \to K_2^*(1430)^0 \overline{K}^0 + c.c.} \cdot \mathcal{B}_{K_2^*(1430) \to K^0 \pi^0}$	$2.4 \pm 0.7 \pm 0.1$	$0.43\ \pm 0.12 \pm 0.02$	$< 4 \ [26]$
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \to K^0_S K^0_L \pi^0}$	< 0.7	< 0.3	-
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \to K_S^0 K_L^0 \eta}$	$3.14\ \pm 1.08\ \pm 0.16$	$1.33\ \pm 0.46 \pm 0.07$	-
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \to K_S^0 K_L^0 \pi^0 \pi^0}$	$2.92\ \pm 1.27\ \pm 0.15$	$1.24\ \pm 0.54 \pm 0.06$	- 🥂
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NEW

#### Published cross sections measured by BABAR via ISR

 $e^+e^- \rightarrow \pi^+\pi^-$ 

 $e^+e^- \rightarrow K^+K^-$ 

 $\begin{array}{l} e^+e^- \rightarrow K_S K_L, \, K_S K_L \pi^+ \pi^-, \, K_S K_S \pi^+ \pi^-, \, K_S K_S K^+ K^- \\ e^+e^- \rightarrow p \text{ anti-}p \end{array}$ 

 $\begin{array}{l} \mathbf{e}^{\star}\mathbf{e}^{-} \rightarrow \Lambda \text{ anti-}\Lambda, \Sigma^{0} \text{ anti-}\Sigma^{0}, \Lambda \text{ anti-}\Sigma^{0}\\ \mathbf{e}^{\star}\mathbf{e}^{-} \rightarrow \pi^{\star}\pi\pi^{0}\\ \mathbf{e}^{\star}\mathbf{e}^{-} \rightarrow K^{\star}K^{\cdot}\eta, \mathbf{K}_{S}K^{\star}\pi^{-}K^{\star}K^{\cdot}\pi^{0}\\ \mathbf{e}^{\star}\mathbf{e}^{-} \rightarrow \pi^{\star}\pi^{\star}\pi^{\star}\pi^{\star}\end{array}$ 

 $e^+e^- \rightarrow K^+K^-\pi^+\pi^-, K^+K^-\pi^0\pi^0, K^+K^-K^+K^-$ 

 $e^+e^- \rightarrow 2(\pi^+\pi^-)\pi^0, 2(\pi^+\pi^-)\eta, K^+K^-\pi^+\pi^-\pi^0, K^+K^-\pi^+\pi^-\eta \\ e^+e^- \rightarrow 3(\pi^+\pi^-), 2(\pi^+\pi^-\pi^0), K^+K^-2(\pi^+\pi^-)$ 

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