

# Heavy-quarkonium theory in the LHC era

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In collaboration with Mathias Butenschön and Zhiguo He

PRL **104** (2010) 072001

PRL **106** (2011) 022003

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PRL **107** (2011) 232001

PRL **108** (2012) 172002

MPLA **28** (2013) 1350027 (Brief Reviews)

PRL **114** (2015) 092004

PRL **115** (2015) 022002

# CERN Courier, Volume 52, Issues 1 and 2



# Outline

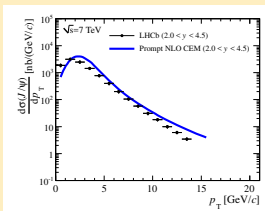
- 1 **Introduction:** CEM, CSM, NRQCD factorization
- 2 **NLO NRQCD:** General concept, singularities
- 3 **Global fit:** Unpolarized  $J/\psi$  yield
- 4 **Further tests:** ATLAS, FTPS, ZEUS
- 5 **Polarization:** HERA, Tevatron, LHC
- 6  **$\eta_c$  yield:** LHC
- 7 **Summary:** NRQCD at the crossroads

# Introduction: CEM, CSM, NRQCD factorization

## Color evaporation model [Fritzsch 77; Halzen 77; Glück Owens Reya 78]

$$\sigma_{J/\psi} \approx \frac{1}{9} \rho_{J/\psi} \int_{2m_c}^{2m_D} ds_{c\bar{c}} \frac{d\sigma_{c\bar{c}}}{ds_{c\bar{c}}}$$

- $1/9$ : statistical probability that  $3 \times \bar{3}$   $c\bar{c}$  pair is asymptotically in color-single state
- $\rho_{J/\psi}$ : fraction of charmonia that materialize as  $J/\psi$
- Based **local parton-hadron duality**
- Assumes soft-gluon exchange with underlying event
- $2S+1 L_J^{[c]}$  quantum numbers do not enter
- Useful qualitative picture, rather than rigorous theory



[Schuler Vogt 96; Vogt 99; Frawley Ullrich Vogt 08]

→ Talk by Vincent Cheung.

# Color-singlet model vs. NRQCD factorization

## Color-singlet model [Berger Jones 81; Baier Rückl 81]

- $c\bar{c}$  pair in physical **color-singlet** state, e.g.  $c\bar{c}[{}^3S_1^{[1]}]$  for  $J/\psi$ .
- Nonperturbative information in  $J/\psi$  wave function at origin.
- Leftover IR divergences for P-wave quarkonia  $\leadsto$  **inconsistent!**
- Predicted cross section factor  $10^1$ – $10^2$  below Tevatron data.

## NRQCD factorization [Bodwin Braaten Lepage 95]

- Rigorous effective field theory.
- Based on **factorization of soft and hard scales**  
(Scale hierarchy:  $Mv^2 \lesssim \Lambda_{\text{QCD}} \ll Mv \ll M$ ).
- Theoretically consistent: no leftover singularities.
- Proof of factorization [Nayak Qiu Serman 05; Nayak 15].
- Can explain unpolarized yield at Tevatron and elsewhere.

# NRQCD factorization in a nutshell

**Factorization theorem**  $\sigma_{J/\psi} = \sum_n \sigma_{c\bar{c}[n]} \cdot \langle O^{J/\psi}[n] \rangle$

- $n$ : every possible Fock state, including **color-octet** states.
- $\sigma_{c\bar{c}[n]}$ : production rate of  $c\bar{c}[n]$ , calculated in perturbative QCD.
- $\langle O^{J/\psi}[n] \rangle$ : long-distance matrix elements (LDMEs), nonperturbative, extracted from experiment, universal?

**Scaling rules** [Lepage Magnea<sup>2</sup> Nakhleh Hornbostel 92]

LDMEs scale with relative velocity  $v$  ( $v^2 \approx 0.2$ ).

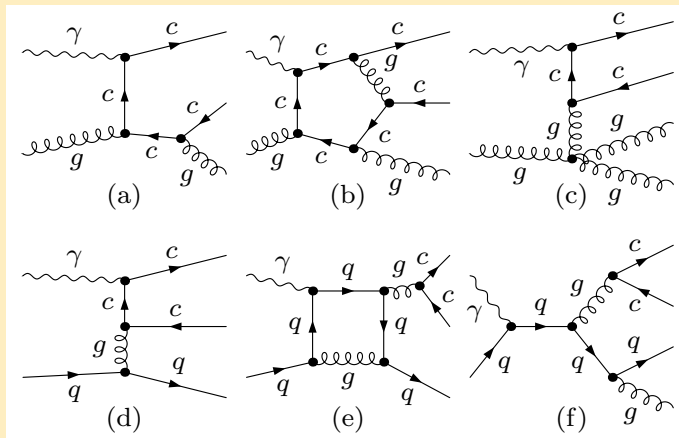
scaling	$v^3$ (CS state)	$v^7$ (CO states)	$v^{11}$
$n$	$^3S_1^{[1]}$	$^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_{0/1/2}^{[8]}$	...

- **Double expansion** in  $v$  and  $\alpha_s$ .
- Leading term in  $v$  ( $n = ^3S_1^{[1]}$ ) corresponds to **color-singlet model**.

# NLO NRQCD calculations

- **Petrelli Cacciari Greco Maltoni Mangano 98:**  
Photo- and hadroproduction (only  $2 \rightarrow 1$  processes)
- **Klasen BK Mihaila Steinhauser 05:**  
Two-photon scattering (w/o resolved photons)
- **Butenschön BK 09:**  
Photoproduction (w/o resolved photons)
- **Zhang Ma Wang Chao 10:**  
 $e^+e^-$  annihilation
- **Ma Wang Chao 10, Butenschön BK 10:**  
Hadroproduction
- **Butenschön BK 11:**  
 $\gamma p$  and  $\gamma\gamma$  (resolved photons)  $\leadsto$  global fit of CO LDMEs
- **Butenschön BK 11:**  
Polarization in photoproduction
- **Butenschön BK 12, Chao Ma K. Wang Y.-J. Zhang 12, Gong, Wan, J.-X. Wang, H.-F. Zhang 12, Shao, Ma, K. Wang, Chao 14:**  
Polarization in hadroproduction

# Sample diagrams for $J/\psi$ photoproduction in NRQCD





# Color and spin projection

## Amplitudes for $c\bar{c}[n]$ production by projector application:

$$A_{c\bar{c}[1S_0^{[8]}]} = \text{Tr} [C_8 \Pi_0 A_{c\bar{c}}] |_{q=0}$$

$$A_{c\bar{c}[3S_1^{[1/8]}]} = \epsilon_\alpha \text{Tr} [C_{1/8} \Pi^\alpha A_{c\bar{c}}] |_{q=0}$$

$$A_{c\bar{c}[3P_J^{[8]}]} = \epsilon_{\alpha\beta} \frac{d}{dq_\beta} \text{Tr} [C_8 \Pi^\alpha A_{c\bar{c}}] |_{q=0}$$

- $A_{c\bar{c}}$ : amputated pQCD amplitude for open  $c\bar{c}$  production.
- $q$ : relative momentum between  $c$  and  $\bar{c}$ .
- $C_{1/8}$ : color projectors
- $\Pi_{0/1}$ : spin projectors
- $\epsilon$ : polarization vectors and tensors

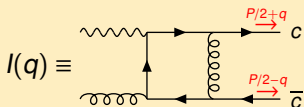
# Main Difference to Previous Calculations

## Virtual corrections: Two different approaches:

- First loop integration, then projectors: (Previous publications)
  - Loop integrals **Coulomb divergent**.
- First projectors, then loop integration: (Our method)
  - + **No Coulomb singularities**.
  - + One scale less in loop integration.
  - Loop integrals not standard form.

## Where do Coulomb divergences come from?

- Projectors: Relative momentum  $q \rightarrow 0$ .
- Scalar diagrams with gluon between external  $c$  and  $\bar{c}$ , e.g.:



$$\lim_{q \rightarrow 0} I(q) = \frac{A}{q^2} + \frac{B}{\epsilon} + C$$

**But:**  $I(0) = \frac{B}{\epsilon} + C$

- $\implies$  **No Coulomb singularities in dimensional regularization!**

# Cancellation of divergences

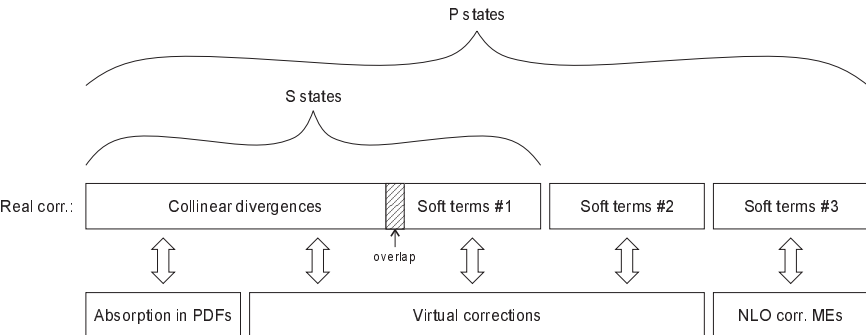
**UV divergences:** Cancellation within virtual corrections:

- Loop integrals
- Charm mass renormalization
- Strong coupling constant renormalization
- Wave function renormalization of external particles

**IR divergences:** Cancellation between:

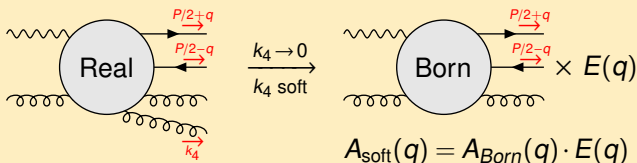
- **Virtual corrections** (loop integrals + wave function renormal.)
- Soft and collinear parts of **real corrections**
- Universal part absorbed into **proton** and **photon PDFs**
- Radiative corrections to **long distance matrix elements**

# Overview of IR singularity structure



# Structure of Soft Singularities

## Soft limits of the real corrections:



## S and P states: Soft #1 + Soft #2 + Soft #3 terms:

$$A_{\text{soft},s} = A_{\text{soft}}(0) = A_{\text{Born},s} \cdot E(0)$$

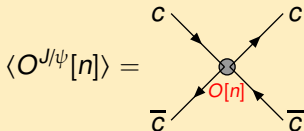
$$A_{\text{soft},p} = A'_{\text{soft}}(0) = A_{\text{Born},p} \cdot E(0) + A_{\text{Born},s} \cdot E'(0)$$

$$|A_{\text{soft},s}|^2 = |A_{\text{Born},s}|^2 \cdot E(0)^2$$

$$|A_{\text{soft},p}|^2 = |A_{\text{Born},p}|^2 \cdot E(0)^2 + 2 \operatorname{Re} A_{\text{Born},s}^* A_{\text{Born},p} \cdot E(0) E'(0) + |A_{\text{Born},s}|^2 \cdot E'(0)^2$$

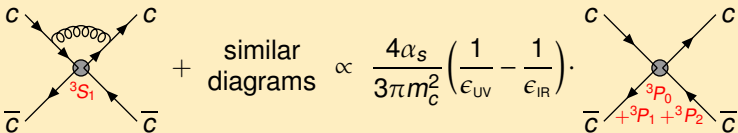
# Radiative Corrections to Long Distance MEs

**In NRQCD:** Long distance MEs =  $c\bar{c}$  scattering amplitudes:



$O[n]$  = 4-fermion operators  
 ( $n = {}^3S_1^{[1]}, {}^1S_0^{[8]}, {}^3S_1^{[8]}, {}^3P_{0/1/2}^{[8]}, \dots$ )

**Corrections to  $\langle O^{J/\psi} [{}^3S_1^{[1/8]}] \rangle$  with NRQCD Feynman rules:**



- **UV singularity** cancelled by renormalization of 4-fermion operat.
- **IR singularity** cancels soft #3 terms of  $P$  states!

# Global fit at NLO in NRQCD

Fit CO LDMEs to all available world data on  $J/\psi$  inclusive production:

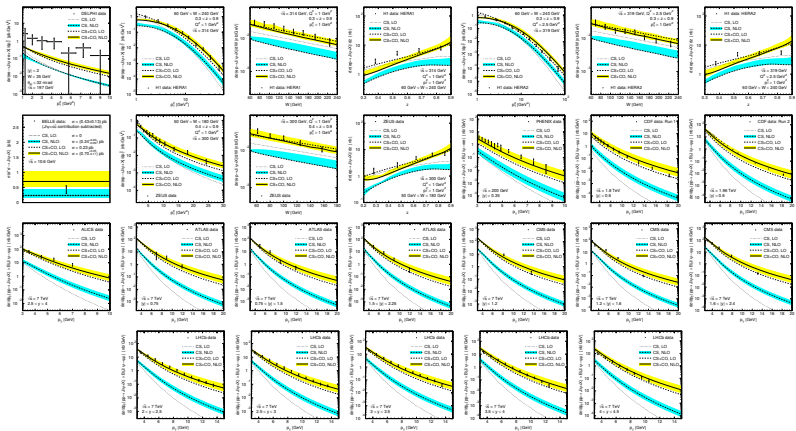
type	$\sqrt{s}$	collider	collaboration	reference
$pp$	200 GeV	RHIC	PHENIX	PRD82(2010)012001
$p\bar{p}$	1.8 TeV	Tevatron I	CDF	PRL97(1997)572; 578
$p\bar{p}$	1.96 TeV	Tevatron II	CDF	PRD71(2005)032001
$pp$	7 TeV	LHC	ALICE	NPB(PS)214(2011)56
			ATLAS	PoS(ICHEP 2010)013
			CMS	EPJC71(2011)1575
			LHCb	EPJC71(2011)1645
$\gamma p$	300 GeV	HERA I	H1, ZEUS	EPJ25(2002)25; 27(2003)173
$\gamma p$	319 GeV	HERA II	H1	EPJ68(2010)401
$\gamma\gamma$	197 GeV	LEP II	DELPHI	PLB565(2003)76
$e^+e^-$	10.6 GeV	KEKB	Belle	PRD79(2009)071101

Fit values for CO LDMEs:

$10^{-2} \text{ GeV}^{3+2L}$	feed-down included	feed-down subtracted
$\langle O[{}^1S_0^{[8]}] \rangle$	$4.97 \pm 0.44$	$3.04 \pm 0.35$
$\langle O[{}^3S_1^{[8]}] \rangle$	$0.224 \pm 0.059$	$0.168 \pm 0.046$
$\langle O[{}^3P_0^{[8]}] \rangle$	$-1.61 \pm 0.20$	$-0.908 \pm 0.161$
$\chi^2/\text{d.o.f.}$	$857/194 = 4.42$	$725/194 = 3.74$

Note: CO LDMEs  $\propto v^4 \times \langle O[{}^3S_1^{[1]}] \rangle \rightsquigarrow$  NRQCD velocity scaling rules  $\checkmark$

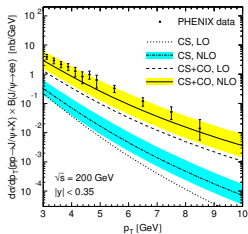
# Comparison with world data



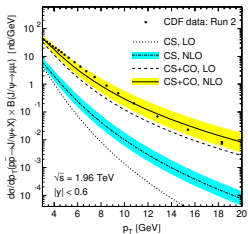


# Comparison with RHIC and Tevatron

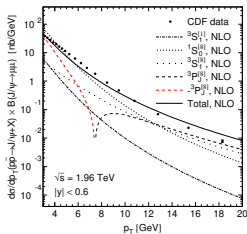
RHIC  
PHENIX



Tevatron II  
CDF

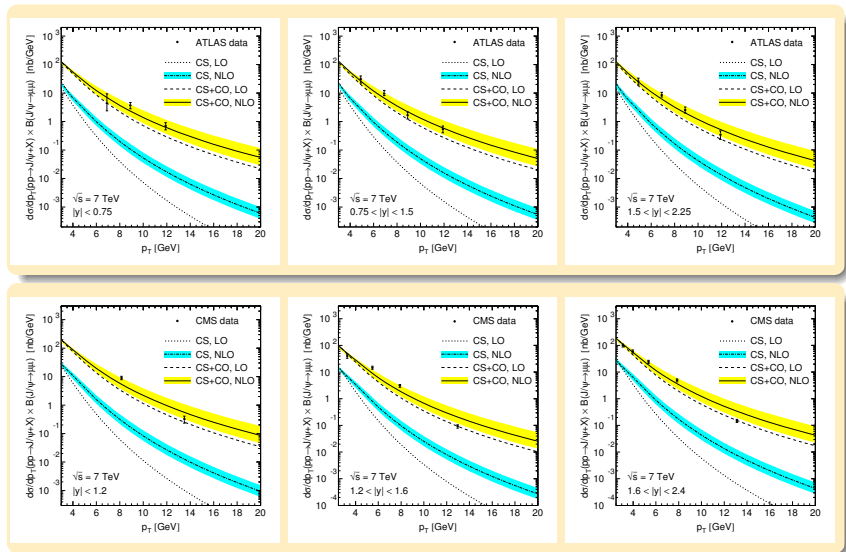


Decomposition of  
NLO NRQCD

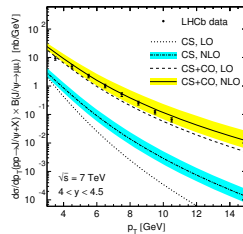
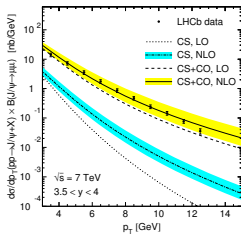
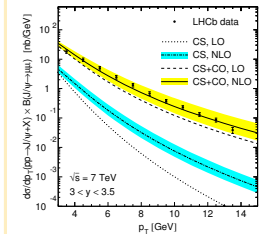
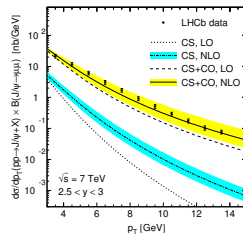
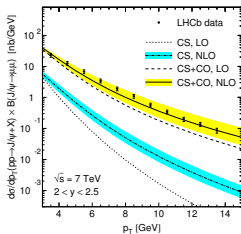
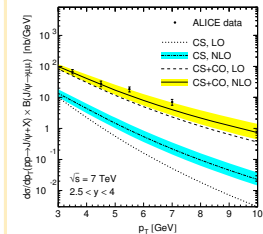


- Data **well described** by CS+CO at NLO.
- **CS** orders of magnitudes **below** data.
- **Sizeable NLO corrections**, especially in the  ${}^3P_J^{[8]}$  channels.

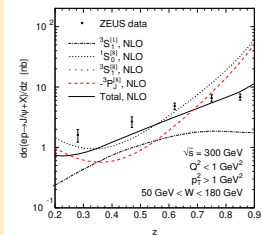
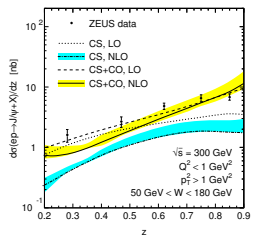
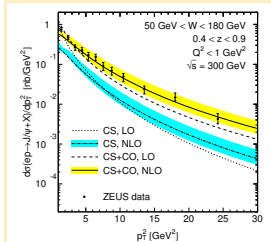
# Comparison with ATLAS and CMS at LHC



# Comparison with ALICE and LHCb at LHC

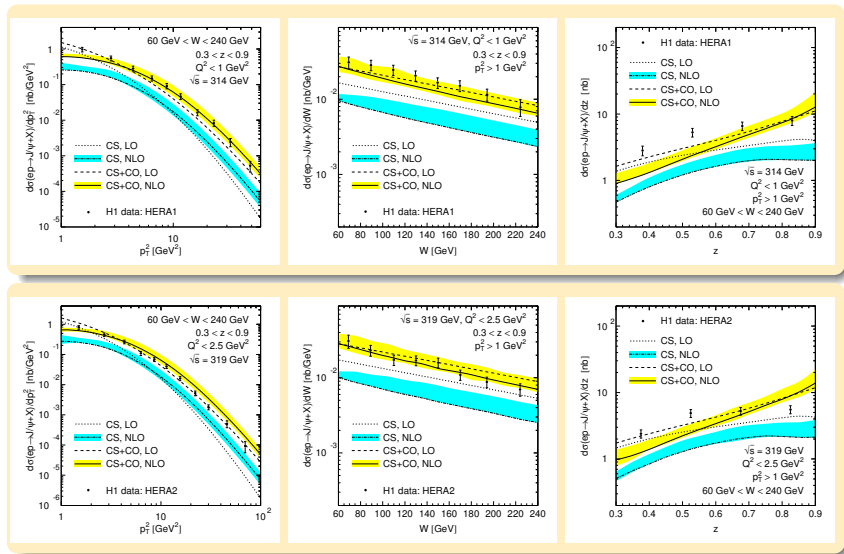


# Comparison with ZEUS at HERA I

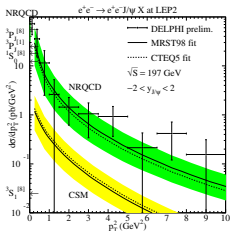


- $W = \gamma p$  CM energy.
- $z =$  fraction of  $\gamma$  energy going to  $J/\psi$  in  $p$  rest frame.
- Compensation of  $^1S_0^{[8]}$  vs.  $^3P_J^{[8]} \rightsquigarrow$  regular  $z \rightarrow 1$  behavior.
- Data **well described** by CS+CO at NLO.
- **CS** factor of 3–5 **below** the data.

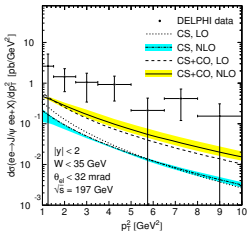
# Comparison with H1 at HERA I and II



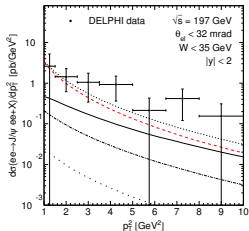
# Comparison with DELPHI at LEP II



[Klasen BK Mihaila Steinhauser 02]



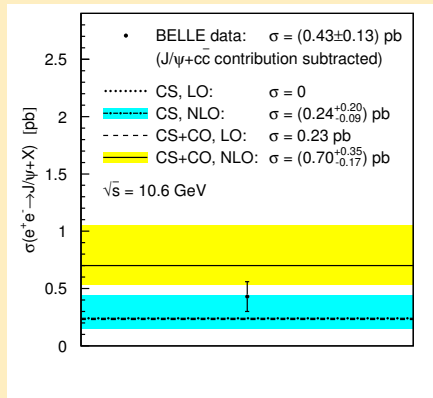
NLO NRQCD



Decomposition of NLO NRQCD

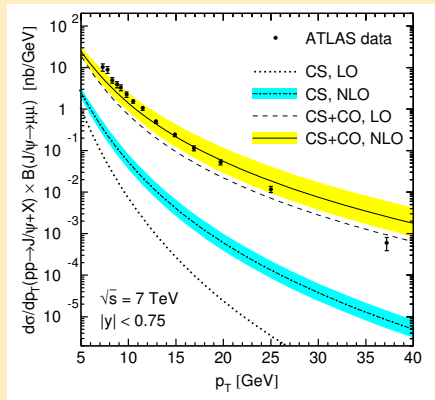
- Agreement with NRQCD at NLO worse than in 2002 at LO.
- Just 16 DELPHI events with  $p_T > 1$  GeV.
- No results from ALEPH, L3, OPAL.
- Data exhausted by single-resolved contribution.

# Comparison with Belle at KEKB



- At NLO, both CSM and NRQCD agree with data.
- # of charged tracks  $> 4$ , missing events **not corrected** for.  
 $\leadsto$  Belle point likely **higher**.

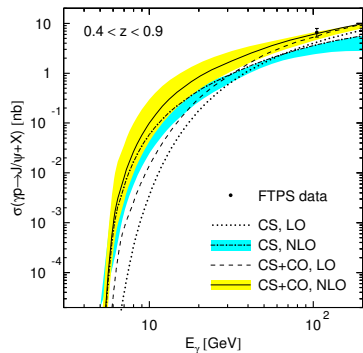
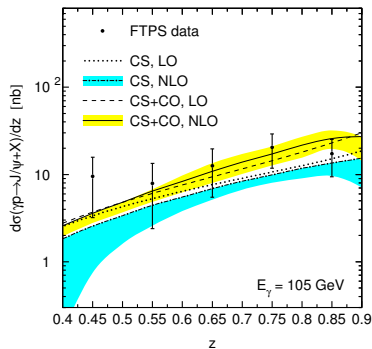
# Comparison with ATLAS (after fit) [NPB850(2011)387]



- Resummation of large logs  $\ln(p_T^2/M^2)$  necessary at large  $p_T$ .
- New formalism to include non-leading powers in  $p_T^2/M^2$  [Kang Qiu Sterman 2012].

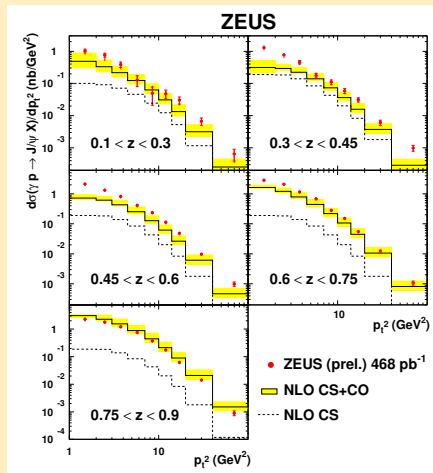


# Comparison with Fermilab Tagged-Photon Spectrometer data (excluded from fit) [PRL52(1984)795]



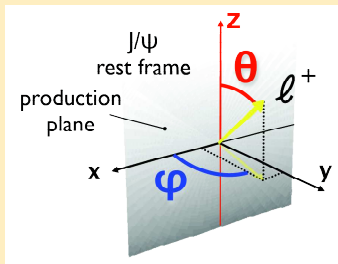
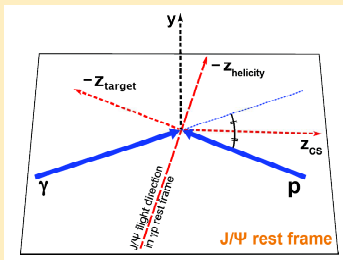
- Inelastic scattering of 105 GeV photons on hydrogen target.
- Data remarkably well described by CS+CO at NLO.

# Comparison with ZEUS (after fit) [JHEP1302(2013)071]



- Notorious NRQCD overshoot at **large z** overcome.

# Polarized $J/\psi$ photo- and hadroproduction



Decay angular distribution:

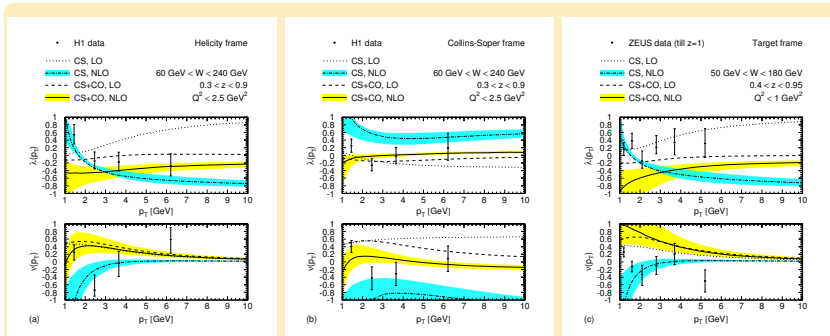
$$\frac{d\Gamma(J/\psi \rightarrow l^+l^-)}{d\cos\theta d\phi} \propto 1 + \lambda_\theta \cos^2\theta + \lambda_\phi \sin^2\theta \cos(2\phi) + \lambda_{\theta\phi} \sin(2\theta) \cos\phi$$

Polarization observables in spin density matrix formalism:

$$\lambda_\theta = \frac{d\sigma_{11} - d\sigma_{00}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_\phi = \frac{d\sigma_{1,-1}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_{\theta\phi} = \frac{\sqrt{2}\text{Re} d\sigma_{10}}{d\sigma_{11} + d\sigma_{00}}$$

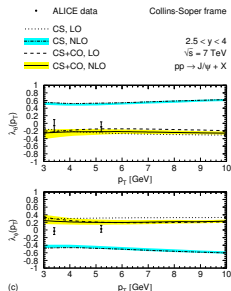
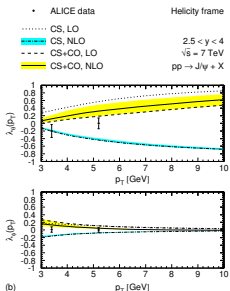
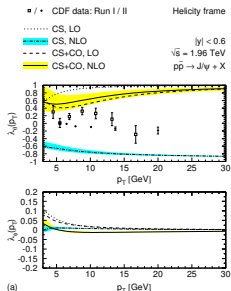
$\lambda = 0, +1, -1$ : unpolarized, transversely and longitudinally polarized.

# Comparison with H1 and ZEUS



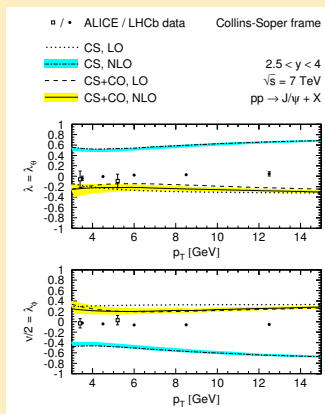
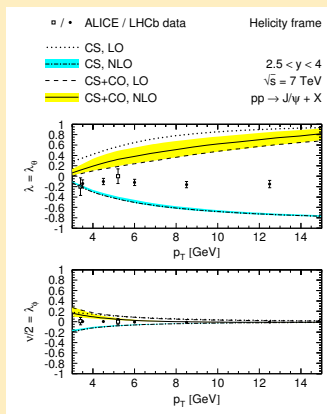
- No z cut on ZEUS data  $\leadsto$  diffractive production included.
- Perturbative stability in NRQCD higher than in CSM.
- $J/\psi$  preferably unpolarized at large  $p_T$ .

# Comparison with CDF and ALICE



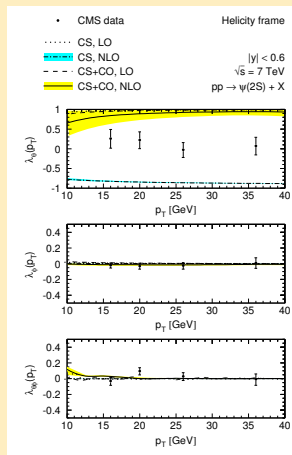
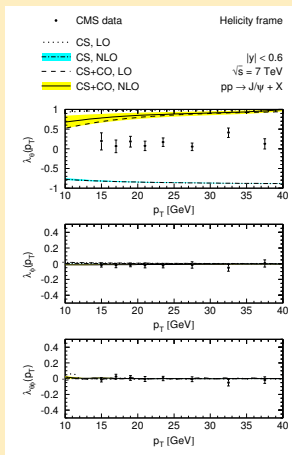
- CDF I [PRL85(2000)2886] and II [PRL99(2007)132001] data mutually inconsistent for  $p_T < 12$  GeV.
- CDF  $J/\psi$  polarization anomaly persists at NLO.
- 4/8 ALICE [PRL108 (2012) 082001] points agree w/ NLO NRQCD within errors, others  $< 2\sigma$  away.

# Comparison with ALICE [PRL108 (2012) 082001] and LHCb [EPJC73(2013)2631] data on prompt $J/\psi$ polarization



- ALICE and LHCb data mutually agree.
- NLO NRQCD predictions systematically disagree w/ data.

# Comparison with CMS data on prompt $J/\psi$ and $\psi'$ polarization [PLB727(2013)381]



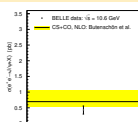
- NLO NRQCD predictions systematically disagree w/ data on  $\lambda_\theta$ .

# Comparison with Gong et al. and Chao et al.

BK, MB

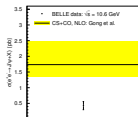
PRL108(2012)172002

$e^+e^-$  yield



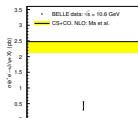
Gong et al.

PRL110(2013)042002

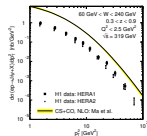
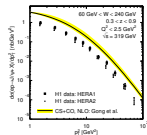
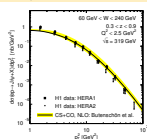


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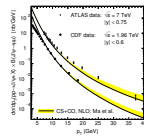
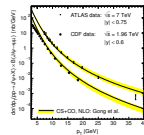
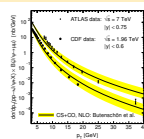
PRL108(2012)242004



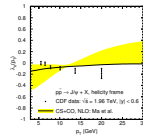
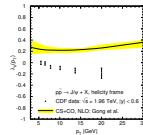
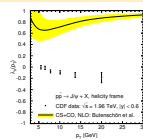
$\gamma p$  yield



$p\bar{p}/pp$  yield

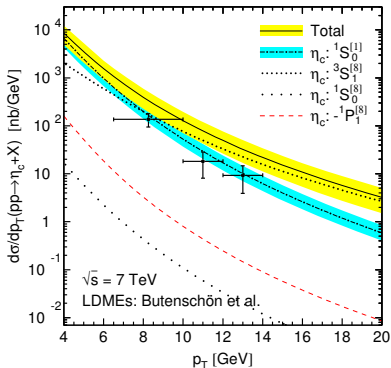


CDF polariz.

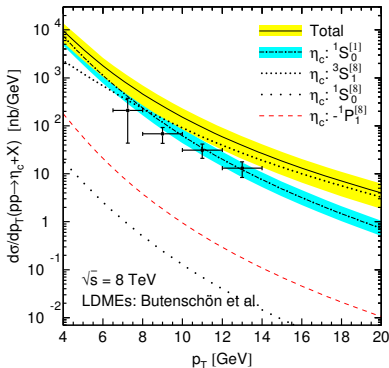




# LHCb data on $\eta_c$ yield [EPJC75(2015)311]



7 TeV



8 TeV

M. Butenschoen, Z. He, BK, PRL114(2015)092004

# Summary

- **NRQCD factorization** provides rigorous framework for production and decay of heavy quarkonia; predicts:
  - existence of CO states;
  - universality of LDMEs.
- NLO NRQCD nicely describes world data on unpolarized  $J/\psi$  yield.
- NLO CSM greatly undershoots data, except for  $e^+e^-$  annihilation.
- $\gamma\gamma$  scattering not conclusive yet.
- Hadroproduction data alone cannot reliably fix all 3 CO LDMEs.
- NLO NRQCD predictions for polarized  $J/\psi$  hadroproduction based on global analysis of  $J/\psi$  yield agrees with ALICE (low  $p_T$ ), but strongly disagrees with CDF, CMS, and LHCb.
- NLO NRQCD predictions for  $\eta_c$  yield based on heavy-quark spin symmetry greatly overshoot LHCb data.
- NRQCD factorization remains among the hottest topics of QCD @ LHC.