# Supersymmetric Meson-Baryon Properties of QCD from Light-Front Holography and Superconformal Algebra







Invariant under boosts! Independent of  $P^{\mu}$ 

Causal, Frame-independent. Creation Operators on Simple Vacuum, Current Matrix Elements are Overlaps of LFWFS



#### **Bound States in Relativistic Quantum Field Theory:**

Light-Front Wavefunctions Dirac's Front Form: Fixed  $\tau = t + z/c$ 

Fixed 
$$\tau = t + z/c$$
  
 $\psi(x_i, \vec{k}_{\perp i}, \lambda_i)$   
 $x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$ 

Invariant under boosts. Independent of  $P^{\mu}$ 

$$\mathbf{H}_{LF}^{QCD}|\psi\rangle = M^2|\psi\rangle$$

**Direct connection to QCD Lagrangian** 

# **Off-shell in invariant mass**

Remarkable new insights from AdS/CFT, the duality between conformal field theory and Anti-de Sitter Space

Light-Front QCD

### Physical gauge: $A^+ = 0$

(c)

mma

Exact frame-independent formulation of nonperturbative QCD!

$$\begin{split} L^{QCD} &\to H_{LF}^{QCD} \\ H_{LF}^{QCD} &= \sum_{i} [\frac{m^{2} + k_{\perp}^{2}}{x}]_{i} + H_{LF}^{int} \\ H_{LF}^{int}: \text{ Matrix in Fock Space} \\ H_{LF}^{QCD} |\Psi_{h} \rangle &= \mathcal{M}_{h}^{2} |\Psi_{h} \rangle \\ |p, J_{z} \rangle &= \sum_{n=3}^{\infty} \psi_{n}(x_{i}, \vec{k}_{\perp i}, \lambda_{i}) |n; x_{i}, \vec{k}_{\perp i}, \lambda_{i} \rangle \end{split}$$

Eigenvalues and Eigensolutions give Hadronic Spectrum and Light-Front wavefunctions

## LFWFs: Off-shell in P- and invariant mass



Yukawa Híggs coupling of confined quark to Híggs zero mode gives

$$\bar{u}u \ g_q < h > = \frac{m_q}{x_q} m_q = \frac{m_q^2}{x_q}$$

$$H_{LF} = \sum_{q} \frac{k_{\perp q}^2 + m_q^2}{x_q}$$

$$|p, S_z\rangle = \sum_{n=3}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$

sum over states with n=3, 4, ... constituents

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

are boost invariant; they are independent of the hadron's energy and momentum  $P^{\mu}$ .

The light-cone momentum fractions

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_{i}^{n} k_{i}^{+} = P^{+}, \ \sum_{i}^{n} x_{i} = 1, \ \sum_{i}^{n} \vec{k}_{i}^{\perp} = \vec{0}^{\perp}.$$

Intrinsic heavy quarks s(x), c(x), b(x) at high x !

$$\overline{\bar{s}(x) \neq s(x)}$$
$$\overline{\bar{u}(x) \neq \bar{d}(x)}$$



Fixed LF time



 $= 2p^+F(q^2)$ 

# Front Form



Drell, sjb

Exact LF Formula for Paulí Form Factor

$$\frac{F_{2}(q^{2})}{2M} = \sum_{a} \int [dx][d^{2}\mathbf{k}_{\perp}] \sum_{j} e_{j} \frac{1}{2} \times Drell, sjb$$

$$\begin{bmatrix} -\frac{1}{q^{L}}\psi_{a}^{\uparrow *}(x_{i}, \mathbf{k}'_{\perp i}, \lambda_{i}) \psi_{a}^{\downarrow}(x_{i}, \mathbf{k}_{\perp i}, \lambda_{i}) + \frac{1}{q^{R}}\psi_{a}^{\downarrow *}(x_{i}, \mathbf{k}'_{\perp i}, \lambda_{i}) \psi_{a}^{\uparrow}(x_{i}, \mathbf{k}_{\perp i}, \lambda_{i}) \end{bmatrix}$$

$$\mathbf{k}'_{\perp i} = \mathbf{k}_{\perp i} - x_{i}\mathbf{q}_{\perp} \qquad \mathbf{k}'_{\perp j} = \mathbf{k}_{\perp j} + (1 - x_{j})\mathbf{q}_{\perp}$$

$$\mathbf{q}_{R,L} = q^{x} \pm iq^{y}$$

$$\mathbf{p}, \mathbf{S}_{z} = \frac{1}{2} - \frac{1}{2} \qquad \mathbf{p} + \mathbf{q}, \mathbf{S}_{z} = \frac{1}{2} - \frac{1}{2}$$

### Must have $\Delta \ell_z = \pm 1$ to have nonzero $F_2(q^2)$

Nonzero Proton Anomalous Moment --> Nonzero orbítal quark angular momentum



Sign reversal in DY!

## Advantages of the Dirac's Front Form for Hadron Physics Poincare' Invariant

## Physics Independent of Observer's Motion

- Measurements are made at fixed τ
- Causality is automatic
- Structure Functions are squares of LFWFs
- Form Factors are overlap of LFWFs
- LFWFs are frame-independent: no boosts, no pancakes!
- Same structure function measured at an e p collider and the proton rest frame
- No dependence of hadron structure on observer's frame
- LF Holography: Dual to AdS space
- LF Vacuum trivial -- no vacuum condensates!
- Profound implications for Cosmological Constant



## Terrell, Penrose

• Light Front Wavefunctions:  $\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$ off-shell in  $P^-$  and invariant mass  $\mathcal{M}^2_{q\bar{q}}$ 



**Boost-invariant LFWF connects confined quarks and gluons to hadrons** 

Need a First Approximation to QCD

Comparable in simplicity to Schrödinger Theory in Atomic Physics

**Relativistic, Frame-Independent, Color-Confining** 

**Origin of hadronic mass scale** 

AdS/QCD Líght-Front Holography Superconformal Algebra

QCD Lagrangian

$$\mathcal{L}_{QCD} = -\frac{1}{4} Tr(G^{\mu\nu}G_{\mu\nu}) + \sum_{f=1}^{n_f} i\bar{\Psi}_f D_{\mu}\gamma^{\mu}\Psi_f + \sum_{f=1}^{n_f} i_f \bar{\Psi}_f \Psi_f$$

$$iD^{\mu} = i\partial^{\mu} - gA^{\mu} \qquad G^{\mu\nu} = \partial^{\mu}A^{\mu} - \partial^{\nu}A^{\mu} - g[A^{\mu}, A^{\nu}]$$

### **Classical Chiral Lagrangian is Conformally Invariant**

## Where does the QCD Mass Scale come from?

QCD does not know what MeV units mean! Only Ratios of Masses Determined

ode Alfaro, Fubini, Furlan:

Scale can appear in Hamiltonian and EQM without affecting conformal invariance of action!

## Unique confinement potential!



$$Light-Front QCD$$

$$\mathcal{L}_{QCD} \longrightarrow H_{QCD}^{LF}$$

$$(H_{LF}^{0} + H_{LF}^{I})|\Psi \rangle = M^{2}|\Psi \rangle$$

$$[\frac{\vec{k}_{\perp}^{2} + m^{2}}{x(1-x)} + V_{\text{eff}}^{LF}]\psi_{LF}(x, \vec{k}_{\perp}) = M^{2}\psi_{LF}(x, \vec{k}_{\perp})$$

$$[-\frac{d^{2}}{d\zeta^{2}} + \frac{1-4L^{2}}{4\zeta^{2}} + U(\zeta)]\psi(\zeta) = \mathcal{M}^{2}\alpha$$

$$AdS/QCD:$$

$$U(\zeta) = \kappa^{4}\zeta^{2} + 2\kappa^{2}(L+S-1)$$

Semiclassical first approximation to QCD

Fixed  $\tau = t + z/c$ 



Coupled Fock states

Elímínate hígher Fock states and retarded interactions

Effective two-particle equation

 $\psi(\zeta)$ 

Azimuthal Basis  $\zeta, \phi$ 

$$m_q = 0$$

Confining AdS/QCD potential!

Sums an infinite # diagrams

de Tèramond, Dosch, sjb

AdS/QCD Soft-Wall Model

 $e^{\varphi(z)} = e^{+\kappa^2 z^2}$  $\zeta^2 = x(1-x)\mathbf{b}_{\perp}^2$ .





$$\left[-\frac{d^2}{d\zeta^2} + \frac{1-4L^2}{4\zeta^2} + U(\zeta)\right]\psi(\zeta) = \mathcal{M}^2\psi(\zeta)$$



Light-Front Schrödinger Equation  $U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2 (L + S - 1)$ 

Unique Confinement Potential!

Conformal Symmetry of the action

Confinement scale:

 $\kappa \simeq 0.5 \ GeV$ 

de Alfaro, Fubini, Furlan:
Fubini, Rabinovici

Scale can appear in Hamiltonian and EQM without affecting conformal invariance of action!

#### • de Alfaro, Fubini, Furlan



Retains conformal invariance of action despite mass scale!  $4uw-v^2=\kappa^4=[M]^4$ 

Identical to LF Hamiltonian with unique potential and dilaton!

Dosch, de Teramond, sjb

$$\left[-\frac{d^2}{d\zeta^2} + \frac{1-4L^2}{4\zeta^2} + U(\zeta)\right]\psi(\zeta) = \mathcal{M}^2\psi(\zeta)$$
$$U(\zeta) = \kappa^4\zeta^2 + 2\kappa^2(L+S-1)$$

#### Meson Spectrum in Soft Wall Model

$$m_{\pi} = 0$$
 if  $m_q = 0$ 

Pion: Negative term for J=0 cancels positive terms from LFKE and potential

Massless pion!

• Effective potential:  $U(\zeta^2) = \kappa^4 \zeta^2 + 2\kappa^2 (J-1)$ 

LF WE

$$\left(-rac{d^2}{d\zeta^2}-rac{1-4L^2}{4\zeta^2}+\kappa^4\zeta^2+2\kappa^2(J-1)
ight)\phi_J(\zeta)=M^2\phi_J(\zeta)$$

• Normalized eigenfunctions  $\;\langle \phi | \phi 
angle = \int d\zeta \, \phi^2(z)^2 = 1\;$ 

$$\phi_{n,L}(\zeta) = \kappa^{1+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{1/2+L} e^{-\kappa^2 \zeta^2/2} L_n^L(\kappa^2 \zeta^2)$$
$$\mathcal{M}_{n,J,L}^2 = 4\kappa^2 \left(n + \frac{J+L}{2}\right)$$

G. de Teramond, H. G. Dosch, sjb

Eigenvalues

$$m_u = m_d = 0$$

#### de Tèramond, Dosch, sjb



$$M^2(n, L, S) = 4\kappa^2(n + L + S/2)$$

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## Prediction from AdS/QCD: Meson LFWF



week ending 24 AUGUST 2012



#### AdS/QCD Holographic Wave Function for the $\rho$ Meson and Diffractive $\rho$ Meson Electroproduction



Changes in physical length scale mapped to evolution in the 5th dimension z

AdS<sub>5</sub>

- Truncated AdS/CFT (Hard-Wall) model: cut-off at  $z_0 = 1/\Lambda_{QCD}$  breaks conformal invariance and allows the introduction of the QCD scale (Hard-Wall Model) Polchinski and Strassler (2001).
- Smooth cutoff: introduction of a background dilaton field  $\varphi(z)$  usual linear Regge dependence can be obtained (Soft-Wall Model) Karch, Katz, Son and Stephanov (2006).

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• Isomorphism of SO(4,2) of conformal QCD with the group of isometries of AdS space

$$ds^{2} = \frac{R^{2}}{r^{2}} (\eta_{\mu\nu} dx^{\mu} dx^{\nu} - dz^{2}),$$
 invariant measure

 $x^{\mu} \rightarrow \lambda x^{\mu}, \ z \rightarrow \lambda z$ , maps scale transformations into the holographic coordinate z.

- AdS mode in z is the extension of the hadron wf into the fifth dimension.
- Different values of z correspond to different scales at which the hadron is examined.

$$x^2 \to \lambda^2 x^2, \quad z \to \lambda z.$$

 $x^2 = x_\mu x^\mu$ : invariant separation between quarks

- The AdS boundary at  $z \to 0$  correspond to the  $Q \to \infty,$  UV zero separation limit.

# AdS/CFT

# Dílaton-Modífied AdS/QCD

$$ds^{2} = e^{\varphi(z)} \frac{R^{2}}{z^{2}} (\eta_{\mu\nu} x^{\mu} x^{\nu} - dz^{2})$$



- Soft-wall dilaton profile breaks conformal invariance  $e^{\varphi(z)} = e^{+\kappa^2 z^2}$
- Color Confinement
- ullet Introduces confinement scale  $\kappa$
- Uses AdS<sub>5</sub> as template for conformal theory

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 $e^{\varphi(z)} = e^{+\kappa^2 z^2}$ 

Ads Soft-Wall Schrödinger Equation for bound state of two scalar constituents:

$$\left[ -\frac{d^2}{dz^2} - \frac{1 - 4L^2}{4z^2} + U(z) \right] \Phi(z) = \mathcal{M}^2 \Phi(z)$$

$$U(z) = \kappa^4 z^2 + 2\kappa^2 (L + S - 1)$$

Derived from variation of Action for Dilaton-Modified AdS\_5

Identical to Light-Front Bound State Equation!



**Light-Front Holography**: Unique mapping derived from equality of LF and AdS formula for EM and gravitational current matrix elements and identical equations of motion

# Uniqueness of Dilaton

$$\varphi_p(z) = \kappa^p z^p$$



Dosch, de Tèramond, sjb

Haag, Lopuszanski, Sohnius (1974)

Superconformal Quantum Mechanics  $\{\psi,\psi^+\} = 1$   $B = \frac{1}{2}[\psi^+,\psi] = \frac{1}{2}\sigma_3$  $\psi = \frac{1}{2}(\sigma_1 - i\sigma_2), \quad \psi^+ = \frac{1}{2}(\sigma_1 + i\sigma_2)$  $Q = \psi^{+}[-\partial_{x} + \frac{f}{x}], \quad Q^{+} = \psi[\partial_{x} + \frac{f}{x}], \quad S = \psi^{+}x, \quad S^{+} = \psi x$  $\{Q, Q^+\} = 2H, \{S, S^+\} = 2K$  $\{Q, S^+\} = f - B + 2iD, \ \{Q^+, S\} = f - B - 2iD$ generates conformal algebra [H,D] = i H, [H, K] = 2 i D, [K, D] = - i K $Q \simeq \sqrt{H}, \quad S \simeq \sqrt{K}$ 

## Superconformal Quantum Mechanics

# **Baryon Equation** $Q \simeq \sqrt{H}, S \simeq \sqrt{K}$

Consider  $R_w = Q + wS;$ 

w: dimensions of mass squared

$$G = \{R_w, R_w^+\} = 2H + 2w^2K + 2wfI - 2wB \qquad 2B = \sigma_3$$

**Retains Conformal Invariance of Action** 

Fubini and Rabinovici

New Extended Hamíltonían G ís díagonal:

$$G_{11} = \left(-\partial_x^2 + w^2 x^2 + 2wf - w + \frac{4(f + \frac{1}{2})^2 - 1}{4x^2}\right)$$

$$G_{22} = \left(-\partial_x^2 + w^2 x^2 + 2wf + w + \frac{4(f - \frac{1}{2})^2 - 1}{4x^2}\right)$$
  
Identify  $f - \frac{1}{2} = L_B$ ,  $w = \kappa^2$ 

Eigenvalue of G:  $M^2(n, L) = 4\kappa^2(n + L_B + 1)$ 

# LF Holography

**Baryon Equation** 

Superconformal Quantum Mechanics

$$\left(-\partial_{\zeta}^{2} + \kappa^{4}\zeta^{2} + 2\kappa^{2}(L_{B}+1) + \frac{4L_{B}^{2}-1}{4\zeta^{2}}\right)\psi_{J}^{+} = M^{2}\psi_{J}^{+}$$

$$\left(-\partial_{\zeta}^{2} + \kappa^{4}\zeta^{2} + 2\kappa^{2}L_{B} + \frac{4(L_{B}+1)^{2} - 1}{4\zeta^{2}}\right)\psi_{J}^{-} = M^{2}\psi_{J}^{-}$$

$$M^{2}(n, L_{B}) = 4\kappa^{2}(n + L_{B} + 1)$$
 S=1/2, P=+

both chiralities

## **Meson Equation**

$$\left(-\partial_{\zeta}^{2} + \kappa^{4}\zeta^{2} + 2\kappa^{2}(J-1) + \frac{4L_{M}^{2} - 1}{4\zeta^{2}}\right)\phi_{J} = M^{2}\phi_{J}$$

$$M^2(n, L_M) = 4\kappa^2(n + L_M) \qquad Same_{\varkappa}!$$

## S=0, I=1 Meson is superpartner of S=1/2, I=1 Baryon Meson-Baryon Degeneracy for L<sub>M</sub>=L<sub>B</sub>+1

#### **Fermionic Modes and Baryon Spectrum**

[Hard wall model: GdT and S. J. Brodsky, PRL **94**, 201601 (2005)] [Soft wall model: GdT and S. J. Brodsky, (2005), arXiv:1001.5193]



From Nick Evans

• Nucleon LF modes

$$\psi_{+}(\zeta)_{n,L} = \kappa^{2+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{3/2+L} e^{-\kappa^{2}\zeta^{2}/2} L_{n}^{L+1} \left(\kappa^{2}\zeta^{2}\right)$$
$$\psi_{-}(\zeta)_{n,L} = \kappa^{3+L} \frac{1}{\sqrt{n+L+2}} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{5/2+L} e^{-\kappa^{2}\zeta^{2}/2} L_{n}^{L+2} \left(\kappa^{2}\zeta^{2}\right)$$

• Normalization

$$\int d\zeta \,\psi_+^2(\zeta) = \int d\zeta \,\psi_-^2(\zeta) = 1$$

Quark Chíral Symmetry of Eígenstate!

• Eigenvalues

$$\mathcal{M}_{n,L,S=1/2}^2 = 4\kappa^2 \,(n+L+1)$$

• "Chiral partners"

$$\frac{\mathcal{M}_{N(1535)}}{\mathcal{M}_{N(940)}} = \sqrt{2}$$

## Nucleon: Equal Probability for L=0, I



#### Dosch, de Teramond, Lorce, sjb

$$m_u = m_d = 46 \text{ MeV}, m_s = 357 \text{ MeV}$$



Fit to the slope of Regge trajectories, including radial excitations

Same Regge Slope for Meson, Baryons: Supersymmetric feature of hadron physics


de Tèramond, Dosch, sjb



### Solid line: $\chi = 0.53$ GeV



Superconformal meson-nucleon partners

de Tèramond, Dosch, sjb

# Superconformal Algebra

## 2X2 Hadronic Multiplets

Bosons, Fermions with Equal Mass!



Proton: quark + scalar diquark |q(qq) >(Equal weight: L = 0, L = 1)

## Features of Supersymmetric Equations

 J =L+S baryon simultaneously satisfies both equations of G with L, L+1 with same mass eigenvalue

• 
$$J^z = L^z + 1/2 = (L^z + 1) - 1/2$$
  $S^z = \pm 1/2$ 

- Proton spin carried by quark L<sup>z</sup>  $< J^z >= \frac{1}{2}(S_q^z = \frac{1}{2}, L^z = 0) + \frac{1}{2}(S_q^z = -\frac{1}{2}, L^z = 1) = < L^z >= \frac{1}{2}$ 
  - Mass-degenerate meson "superpartner" with L<sub>M</sub>=L<sub>B</sub>+1. "Shifted meson-baryon Duality"

## Mesons and baryons have same $\kappa$ !

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### Solid line: $\chi = 0.53$ GeV



Superconformal meson-nucleon partners

de Tèramond, Dosch, sjb

E. Klempt and B. Ch. Metsch



The leading Regge trajectory:  $\Delta$  resonances with maximal J in a given mass range. Also shown is the Regge trajectory for mesons with J = L+S.



 $\chi(mesons) = -1$   $\chi(baryons, tetraquarks) = +1$ 

**New World of Tetraquarks** 

$$3_C \times 3_C = \overline{3}_C + 6_C$$
  
Bound!

- Diquark: Color-Confined Constituents: Color  $3_C$
- Diquark-Antidiquark bound states  $\overline{3}_C \times 3_C = 1_C$

$$\sigma(TN) \simeq 2\sigma(pN) - \sigma(\pi N)$$

 $2\big[\sigma([\{qq\}N) + \sigma(qN)\big] - [\sigma(qN) + \sigma(\bar{q}N)] = [\sigma(\{qq\}N) + \sigma(\{qq\}N)]$ 

Candidates  $f_0(980)I = 0, J^P = 0^+$ , partner of proton

 $a_1(1260)I = 0, J^P = 1^+$ , partner of  $\Delta(1233)$ 

### Dosch, de Teramond, sjb

Supersymmetry across the light and heavy-light spectrum



Heavy charm quark mass does not break supersymmetry

### Dosch, de Teramond, sjb

Supersymmetry across the light and heavy-light spectrum



Heavy bottom quark mass does not break supersymmetry

# Foundations of Light-Front Holography

- The QCD Lagrangian for  $m_q = 0$  has no mass scale.
- What determines the hadron mass scale?
- DAFF principle: add terms linear in D and K to Conformal Hamiltonian: Mass scale K appears, but action remains scale invariant —> unique harmonic oscillator potential
- Apply DAFF to the Poincare' invariant LF Hamiltonian: Unique color-confining potential
- Fixes AdS<sub>5</sub> dilaton: predicts Spin and Spin-Orbit Interactions
- Apply DAFF to Superconformal representation of the Lorentz group
- Predicts Meson, Baryon, Tetraquark spectroscopy, dynamics
- Supersymmetric Features of Spectrum

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# Chíral Features of Soft-Wall AdS/QCD Model

- Boost Invariant
- Trivial LF vacuum! No condensate, but consistent with GMOR
- Massless Pion
- Hadron Eigenstates (even the pion) have LF Fock components of different L<sup>z</sup>

• Proton: equal probability  $S^z=+1/2, L^z=0; S^z=-1/2, L^z=+1$ 

$$J^z = +1/2 :< L^z >= 1/2, < S^z_q >= 0$$

- Self-Dual Massive Eigenstates: Proton is its own chiral partner.
- Label State by minimum L as in Atomic Physics
- Minimum L dominates at short distances
- AdS/QCD Dictionary: Match to Interpolating Operator Twist at z=0.
   No mass -degenerate parity partners!

## Running Coupling from Modified Ads/QCD

#### Deur, de Teramond, sjb

• Consider five-dim gauge fields propagating in AdS $_5$  space in dilaton background  $arphi(z)=\kappa^2 z^2$ 

$$S = -\frac{1}{4} \int d^4x \, dz \, \sqrt{g} \, e^{\varphi(z)} \, \frac{1}{g_5^2} \, G^2$$

• Flow equation

$$\frac{1}{g_5^2(z)} = e^{\varphi(z)} \frac{1}{g_5^2(0)} \quad \text{or} \quad g_5^2(z) = e^{-\kappa^2 z^2} g_5^2(0)$$

where the coupling  $g_5(z)$  incorporates the non-conformal dynamics of confinement

- YM coupling  $\alpha_s(\zeta) = g_{YM}^2(\zeta)/4\pi$  is the five dim coupling up to a factor:  $g_5(z) \to g_{YM}(\zeta)$
- $\bullet\,$  Coupling measured at momentum scale Q

$$\alpha_s^{AdS}(Q) \sim \int_0^\infty \zeta d\zeta J_0(\zeta Q) \,\alpha_s^{AdS}(\zeta)$$

 $\alpha_s^{AdS}(Q^2) = \alpha_s^{AdS}(0) e^{-Q^2/4\kappa^2}$  from dilaton  $e^{\kappa^2 z^2}$ 

Solution

where the coupling  $\alpha_s^{AdS}$  incorporates the non-conformal dynamics of confinement

Bjorken sum rule defines effective charge 
$$\alpha_{g1}(Q^2)$$
$$\int_0^1 dx [g_1^{ep}(x,Q^2) - g_1^{en}(x,Q^2)] \equiv \frac{g_a}{6} [1 - \frac{\alpha_{g1}(Q^2)}{\pi}]$$

- Can be used as standard QCD coupling
- Well measured
- Asymptotic freedom at large Q<sup>2</sup>
- Computable at large Q<sup>2</sup> in any pQCD scheme
- Universal  $\beta_0$ ,  $\beta_1$

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$$\frac{1}{g_5^2(z)} = e^{\varphi(z)} \frac{1}{g_5^2(0)} \quad \text{or} \quad g_5^2(z) = e^{-\kappa^2 z^2} g_5^2(0)$$

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$$\alpha_s^{AdS}(Q) \sim \int_0^\infty \zeta d\zeta J_0(\zeta Q) \, \alpha_s^{AdS}(\zeta)$$

Solution

 $\alpha_s^{AdS}(Q^2)=\alpha_s^{AdS}(0)\,e^{-Q^2/4\kappa^2}.$  where the coupling  $\alpha_s^{AdS}$  incorporates the non-conformal dynamics of confinement



### Analytic, defined at all scales, IR Fixed Point

AdS/QCD dilaton captures the higher twist corrections to effective charges for Q < 1 GeV

$$e^{\varphi} = e^{+\kappa^2 z}$$

 $\mathbf{2}$ 

Deur, de Teramond, sjb







#### **Process-independent strong running coupling**

Daniele Binosi,<sup>1</sup> Cédric Mezrag,<sup>2</sup> Joannis Papavassiliou,<sup>3</sup> Craig D. Roberts,<sup>2</sup> and Jose Rodríguez-Quintero<sup>4</sup>

# Features of LF Holographic QCD

- Regge spectroscopy—same slope in n,L for mesons, baryons
- Chiral features for  $m_q=0$ :  $m_{\pi}=0$ , chiral-invariant proton
- Hadronic LFWFs
- Counting Rules
- Connection between hadron masses and  $\Lambda_{\overline{MS}}$

Superconformal AdS Light-Front Holographic QCD (LFHQCD)

Meson-Baryon Mass Degeneracy for L<sub>M</sub>=L<sub>B</sub>+1

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# **Tony Zee**

# "Quantum Field Theory in a Nutshell"

# Dreams of Exact Solvability

"In other words, if you manage to calculate  $m_P$  it better come out proportional to  $\Lambda_{QCD}$  since  $\Lambda_{QCD}$  is the only quantity with dimension of mass around.

Light-Front Holography:

Similarly for  $m_{\rho}$ .

$$m_p \simeq 3.21 \ \Lambda_{\overline{MS}}$$

$$m_{\rho} \simeq 2.2 \ \Lambda_{\overline{MS}}$$

Put in precise terms, if you publish a paper with a formula giving  $m_{\rho}/m_{P}$  in terms of pure numbers such as 2 and  $\pi$ , the field theory community will hail you as a conquering hero who has solved QCD exactly."

$$\frac{\Lambda_{\overline{MS}}}{m_{\rho}} = 0.455 \pm 0.031$$

## Fundamental Hadronic Features of Hadrons

Virial Theorem Partition of the Proton's Mass: Potential vs. Kinetic Contributions Color Confinement  $U(\zeta^2) = \kappa^4 \zeta^2$   $\begin{aligned} \Delta \mathcal{M}^2_{LFKE} &= \kappa^2 (1 + 2n + L) \\ \Delta \mathcal{M}^2_{LFPE} &= \kappa^2 (1 + 2n + L) \end{aligned}$ Role of Quark Orbital Angular Momentum in the Proton Equal L=0, I Quark-Diquark Structure Quark Mass Contribution  $\Delta M^2 = < rac{m_q^2}{r} > from the Yukawa coupling to the Higgs zero mode$ Baryonic Regge Trajectory  $M_{\rm p}^2(n, L_B) = 4\kappa^2(n + L_B + 1)$ Mesonic Supersymmetric Partners  $L_M = L_R + 1$ Proton Light-Front Wavefunctions and Dynamical Observables  $\psi_M(x,k_{\perp}) = \frac{4\pi}{\kappa_{\perp}/x(1-x)}e^{-\frac{k_{\perp}^2}{2\kappa^2x(1-x)}}$ Form Factors, Distribution Amplitudes, Structure Functions Non-Perturbative - Perturbative OCD Transition  $Q_0 = 0.87 \pm 0.08~GeV~\overline{MS}~scheme$  $m_p \simeq 3.21 \ \Lambda_{\overline{MS}}$  $m_{
ho} \simeq 2.2 \ \Lambda_{\overline{MS}}$ Dimensional Transmutation: **Stan Brodsky** 

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## Connection to the Linear Instant-Form Potential



### A.P.Trawinski, S.D. Glazek, H. D. Dosch, G. de Teramond, sjb

#### **Space-Like Dirac Proton Form Factor**

• Consider the spin non-flip form factors

$$F_{+}(Q^{2}) = g_{+} \int d\zeta J(Q,\zeta) |\psi_{+}(\zeta)|^{2},$$
  
$$F_{-}(Q^{2}) = g_{-} \int d\zeta J(Q,\zeta) |\psi_{-}(\zeta)|^{2},$$

where the effective charges  $g_+$  and  $g_-$  are determined from the spin-flavor structure of the theory.

- Choose the struck quark to have  $S^z = +1/2$ . The two AdS solutions  $\psi_+(\zeta)$  and  $\psi_-(\zeta)$  correspond to nucleons with  $J^z = +1/2$  and -1/2.
- For SU(6) spin-flavor symmetry

$$F_1^p(Q^2) = \int d\zeta J(Q,\zeta) |\psi_+(\zeta)|^2,$$
  

$$F_1^n(Q^2) = -\frac{1}{3} \int d\zeta J(Q,\zeta) \left[ |\psi_+(\zeta)|^2 - |\psi_-(\zeta)|^2 \right],$$

where  $F_1^p(0) = 1$ ,  $F_1^n(0) = 0$ .

• Compute Dirac proton form factor using SU(6) flavor symmetry

$$F_1^p(Q^2) = R^4 \int \frac{dz}{z^4} V(Q, z) \Psi_+^2(z)$$

Nucleon AdS wave function

$$\Psi_{+}(z) = \frac{\kappa^{2+L}}{R^2} \sqrt{\frac{2n!}{(n+L)!}} z^{7/2+L} L_n^{L+1} \left(\kappa^2 z^2\right) e^{-\kappa^2 z^2/2}$$

• Normalization  $(F_1^p(0) = 1, V(Q = 0, z) = 1)$ 

$$R^4 \int \frac{dz}{z^4} \, \Psi_+^2(z) = 1$$

• Bulk-to-boundary propagator [Grigoryan and Radyushkin (2007)]

$$V(Q,z) = \kappa^2 z^2 \int_0^1 \frac{dx}{(1-x)^2} x^{\frac{Q^2}{4\kappa^2}} e^{-\kappa^2 z^2 x/(1-x)}$$

• Find

$$F_1^p(Q^2) = \frac{1}{\left(1 + \frac{Q^2}{\mathcal{M}_{\rho}^2}\right)\left(1 + \frac{Q^2}{\mathcal{M}_{\rho'}^2}\right)}$$

with  $\mathcal{M}_{\rho_n}^2 \to 4\kappa^2(n+1/2)$ 



Using SU(6) flavor symmetry and normalization to static quantities





#### **Nucleon Transition Form Factors**

- Compute spin non-flip EM transition  $N(940) \rightarrow N^*(1440)$ :  $\Psi^{n=0,L=0}_+ \rightarrow \Psi^{n=1,L=0}_+$
- Transition form factor

$$F_{1N \to N^*}^{p}(Q^2) = R^4 \int \frac{dz}{z^4} \Psi_+^{n=1,L=0}(z) V(Q,z) \Psi_+^{n=0,L=0}(z)$$

• Orthonormality of Laguerre functions  $(F_1^p_{N \to N^*}(0) = 0, V(Q = 0, z) = 1)$ 

$$R^4 \int \frac{dz}{z^4} \Psi_+^{n',L}(z) \Psi_+^{n,L}(z) = \delta_{n,n'}$$

• Find

with  $\mathcal{M}_{\rho_n}^2$ 

$$F_{1N\to N^{*}}(Q^{2}) = \frac{2\sqrt{2}}{3} \frac{\frac{Q^{2}}{M_{P}^{2}}}{\left(1 + \frac{Q^{2}}{M_{\rho}^{2}}\right)\left(1 + \frac{Q^{2}}{M_{\rho'}^{2}}\right)\left(1 + \frac{Q^{2}}{M_{\rho''}^{2}}\right)} \to 4\kappa^{2}(n+1/2)$$

de Teramond, sjb

### Consistent with counting rule, twist 3

Predict hadron spectroscopy and dynamics







## Flavor Dependence of $Q^6 F_2(Q^2)$

Sufian, de Teramond, Deur, Dosch, sjb

Dressed soft-wall current brings in higher Fock states and more vector meson poles



#### **Current Matrix Elements in AdS Space (SW)**

• Propagation of external current inside AdS space described by the AdS wave equation

$$\left[z^2\partial_z^2 - z\left(1 + 2\kappa^2 z^2\right)\partial_z - Q^2 z^2\right]J_{\kappa}(Q, z) = 0.$$

• Solution bulk-to-boundary propagator

$$J_{\kappa}(Q,z) = \Gamma\left(1 + \frac{Q^2}{4\kappa^2}\right) U\left(\frac{Q^2}{4\kappa^2}, 0, \kappa^2 z^2\right),$$

where U(a, b, c) is the confluent hypergeometric function

$$\Gamma(a)U(a,b,z) = \int_0^\infty e^{-zt} t^{a-1} (1+t)^{b-a-1} dt.$$

• Form factor in presence of the dilaton background  $\varphi = \kappa^2 z^2$ 

$$F(Q^2) = R^3 \int \frac{dz}{z^3} e^{-\kappa^2 z^2} \Phi(z) J_{\kappa}(Q, z) \Phi(z).$$

• For large  $Q^2 \gg 4\kappa^2$ 

$$J_{\kappa}(Q,z) \to zQK_1(zQ) = J(Q,z),$$

the external current decouples from the dilaton field.

de Tèramond & sjb Grigoryan and Radyushkin

Dressed Current ín Soft-Wall Model

$$e^{\varphi(z)} = e^{+\kappa^2 z}$$

## Timelike Pion Form Factor from AdS/QCD and Light-Front Holography





# Future Directions

- Hadronization at the Amplitude Level: LFWFs
- Running Coupling at all Q<sup>2</sup>
- Factorization Scale for ERBL, DGLAP evolution: Qo
- Calculate Sivers Effect including FSI and ISI
- Eliminate renormalizations scale ambiguity: PMC
- Compute Tetraquark Spectroscopy: Sequential Clusters
- Update SU(6) spin-flavor symmetry
- Heavy Quark States: Supersymmetry, not conformal
- Compute higher Fock states; e.g. Intrinsic Heavy Quarks
- Nuclear States Hidden Color
- Basis LF Quantization

de Tèramond, Dosch, Wu, Vary, sjb

Remarkable símílarítíes wíth DSE approach of Roberts et al.


- Flavor-Dependent Anti-Shadowing
- LFVacuum and Cosmological Constant: No QCD condensates
- Principle of Maximum Conformality (PMC): Eliminate renormalization anomaly; scheme independent
- Match Perturbative and Non-Perturbative Domains
- Hadronization at Amplitude Level
- Intrinsic Heavy Quarks from AdS/QCD: Higgs at high x<sub>F</sub>
- Ridge from flux tube collisions
- Baryon-to-meson anomaly at high p<sub>T</sub>

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# Supersymmetric Meson-Baryon Properties of QCD from Light-Front Holography and Superconformal Algebra





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"One of the gravest puzzles of theoretical physics"

DARK ENERGY AND THE COSMOLOGICAL CONSTANT PARADOX

A. ZEE

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$$(\Omega_{\Lambda})_{QCD} \sim 10^{45}$$
  

$$(\Omega_{\Lambda})_{EW} \sim 10^{56}$$
  

$$\Omega_{\Lambda} = 0.76(expt)$$

**Extraordinary conflict between the conventional definition of the vacuum in** quantum field theory and cosmology

Elements of the solution: (A) Light-Front Quantization: causal, frame-independent vacuum (B) New understanding of QCD "Condensates" (C) Higgs Light-Front Zero Mode

### Light-Front vacuum can símulate empty universe

### Shrock, Tandy, Roberts, sjb

- Independent of observer frame
- Causal
- Lowest invariant mass state M= o.
- Trivial up to k+=0 zero modes-- already normal-ordering
- Higgs theory consistent with trivial LF vacuum (Srivastava, sjb)
- QCD and AdS/QCD: "In-hadron"condensates (Maris, Tandy Roberts) -- GMOR satisfied.
- QED vacuum; no loops
- Zero cosmological constant from QED, QCD, EW

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#### S

#### Systematic All-Orders Method to Eliminate Renormalization-Scale and Scheme Ambiguities in Perturbative QCD

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We introduce a generalization of the conventional renormalization schemes used in dimensional regularization, which illuminates the renormalization scheme and scale ambiguities of perturbative QCD predictions, exposes the general pattern of nonconformal  $\{\beta_i\}$  terms, and reveals a special degeneracy of the terms in the perturbative coefficients. It allows us to systematically determine the argument of the running coupling order by order in perturbative QCD in a form which can be readily automatized. The new method satisfies all of the principles of the renormalization group and eliminates an unnecessary source of systematic error.

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## Elímination of QCD Scale Ambiguíties

The Principle of Maximum Conformality (PMC)

Applications of PMC renormalization-scale-setting for top, Higgs production, and other processes at the LHC



S-Q Wang, X-G Wu, sjb



 $\sigma_{
m fid}(p$ 

20

10

0



Comparison of the PMC predictions for the fiducial cross section  $\sigma_{\rm fid}(pp \rightarrow H \rightarrow \gamma \gamma)$  with the ATLAS measurements at various collision energies. The LHC-XS predictions are presented as a comparison.

$\sigma_{\rm fid}(pp \to H \to \gamma\gamma)$	$7 { m TeV}$	$8 { m TeV}$	$13 { m TeV}$
ATLAS data [48]	$49\pm18$	$42.5^{+10.3}_{-10.2}$	$52^{+40}_{-37}$
LHC-XS $[3]$	$24.7\pm2.6$	$31.0\pm3.2$	$66.1_{-6.6}^{+6.8}$
PMC prediction	$30.1^{+2.3}_{-2.2}$	$38.4^{+2.9}_{-2.8}$	$85.8^{+5.7}_{-5.3}$



Collins, Ellis, Gunion, Mueller, sjb Polyakov, et al. Hoyer, Vogt, et al



Two Components (separate evolution):

 $c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$ 

week ending 15 MAY 2009



Consistent with EMC measurement of charm structure function at high x

Goldhaber, Kopeliovich, Schmidt, Soffer sjb

Intrínsic Charm Mechanism for Inclusive High-X<sub>F</sub> Higgs Production



Also: intrinsic strangeness, bottom, top

**Higgs can have > 80% of Proton Momentum!** New production mechanism for Higgs