

$$\left(-\frac{d^2}{d\zeta^2}+\lambda_M^2\zeta^2+2\lambda_M(J-1)+\frac{4L_M^2-1}{4\zeta^2}\right)\phi_J=M^2\phi_j$$