

$$\left| \sum_{initial} S^z - \sum_{final} S_z \right| \leq n$$