

$$\left(-\frac{d^2}{d\zeta^2} + \lambda_M^2 \zeta^2 + 2\lambda_M (J-1) + \frac{4\nu^2-1}{4\zeta^2}\right) \phi_J = M^2 \phi_J,$$