

$$v_j^z = -i \left(\kappa_j \frac{\partial}{\partial \kappa_j^2} - \kappa_j^2 \frac{\partial}{\partial \kappa_j} \right)$$