

Possibility: $\partial_{\perp} \omega \neq 0$