



Jefferson Lab

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Impact of Jefferson Lab data on global (spin) PDF analysis

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<http://www.jlab.org/JAM>



*N. Sato et al., PRD 93, 074005 (2016)
PRD 94, 114004 (2016)*

Outline

- Wish to learn about quark & gluon (spin) distributions in nucleon, especially impact of recent 6 GeV (low- W , high- x) JLab data
- New Iterative Monte Carlo (IMC) methodology, with Bayesian determination of PDF errors
 - standard single-fit technology problematic for “new” PDFs
- Twist-2 and twist-3 helicity PDFs from inclusive DIS data (“JAM15”)
 - what about flavour decomposition... SIDIS?
- First MC analysis of fragmentation functions from e^+e^- annihilation data (“JAM16”)
- New analysis (“JAM17”) — combined DIS + SIDIS + e^+e^- for *simultaneous* extraction of PDFs and fragmentation functions

Methodology

- Analysis of data requires estimating expectation values and variances of observables \mathcal{O} (= PDFs, FFs)

$$E[\mathcal{O}] = \int d^n a \mathcal{P}(\vec{a}|\text{data}) \mathcal{O}(\vec{a})$$

$$V[\mathcal{O}] = \int d^n a \mathcal{P}(\vec{a}|\text{data}) [\mathcal{O}(\vec{a}) - E[\mathcal{O}]]^2$$

→ probability distribution

$$\mathcal{P}(\vec{a}|\text{data}) \propto \mathcal{L}(\text{data}|\vec{a}) \pi(\vec{a}) \quad \text{Bayes' theorem}$$

priors

→ likelihood function

$$\mathcal{L}(\text{data}|\vec{a}) \sim \exp \left[-\frac{1}{2} \chi^2(\vec{a}) \right]$$

$$\chi^2(\vec{a}) = \sum_i \left(\frac{\text{data}_i - \text{theory}_i(\vec{a})}{\delta(\text{data})} \right)^2$$

Methodology

- Standard method for evaluating E, V is “maximum likelihood”

→ maximize probability distribution

$$\mathcal{P}(\vec{a}|\text{data}) \rightarrow \vec{a}_0$$

→ if \mathcal{O} linear in parameters, and if probability is symmetric in all parameters

$$E[\mathcal{O}(\vec{a})] = \mathcal{O}(\vec{a}_0), \quad V[\mathcal{O}(\vec{a})] \rightarrow \text{Hessian}$$

- In practice, since in general $E[f(\vec{a})] \neq f(E[\vec{a}])$, maximum likelihood method will sometimes fail

→ need more versatile approach (*e.g.* Monte Carlo)

$$E[\mathcal{O}] \approx \frac{1}{N} \sum_k \mathcal{O}(\vec{a}_k), \quad V[\mathcal{O}] \approx \frac{1}{N} \sum_k [\mathcal{O}(\vec{a}_k) - E[\mathcal{O}]]^2$$

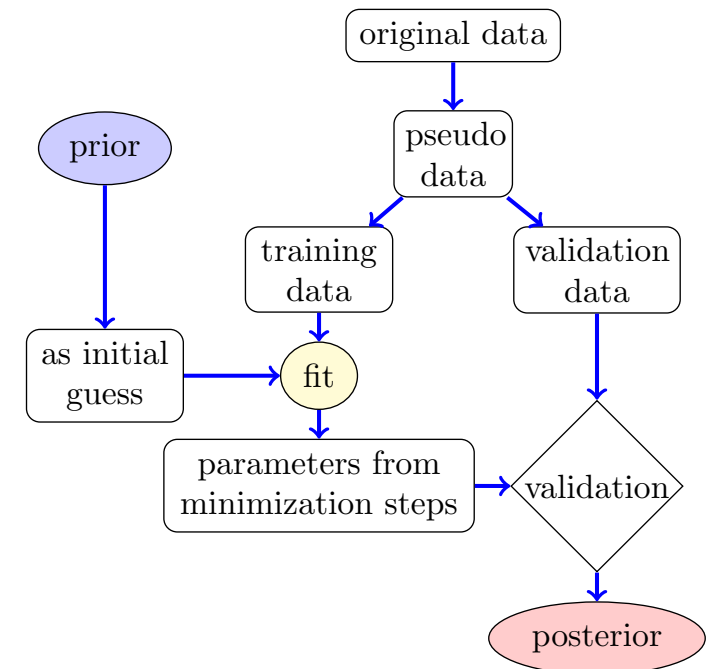
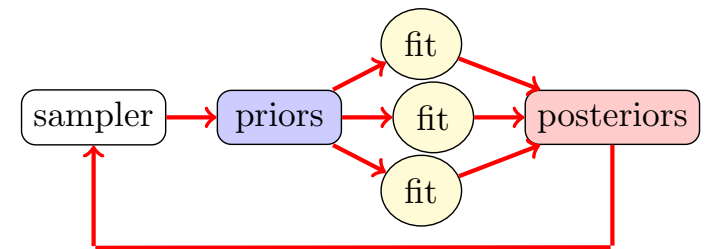
Iterative Monte Carlo

- Can use traditional functional form for input distribution shape

$$xf(x) = N x^a (1 - x)^b (1 + c \sqrt{x} + d x)$$

but sample significantly larger parameter space than possible in single-fit analyses

- no assumptions on exponents
- cross-validation to avoid overfitting
- iterate until convergence criteria satisfied
- unambiguous determination of PDF uncertainties



Inclusive DIS global analysis

- Maximally utilize high-precision, high-statistics spin data at lower (as well as higher) energies
 - ~15 experiments completed at JLab, with data straddling resonance & DIS regions
 - explore systematics of lowering kinematic cuts down to $Q^2 > 1 \text{ GeV}^2$, $W^2 > 3.5 \text{ GeV}^2$
 - control of nuclear and finite- Q^2 corrections
 - constrain (poorly-determined) PDFs at large x , and extract higher twist (twist-3) distributions

Inclusive DIS global analysis

- Fit experimental asymmetries (longitudinal & transverse) rather than derived structure functions

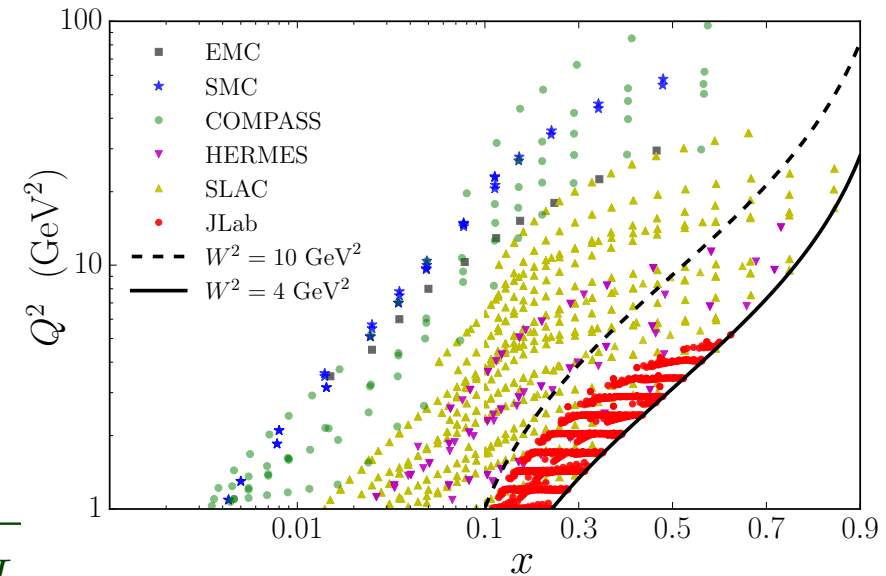
$$A_{\parallel} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = D(A_1 + \eta A_2)$$

$$A_{\perp} = \frac{\sigma^{\uparrow\Rightarrow} - \sigma^{\uparrow\Leftarrow}}{\sigma^{\uparrow\Rightarrow} + \sigma^{\uparrow\Leftarrow}} = d(A_2 - \xi A_1)$$

where $A_1 = (g_1 - \gamma^2 g_2) \frac{2x}{(1 + \gamma^2)F_2 - F_L}$

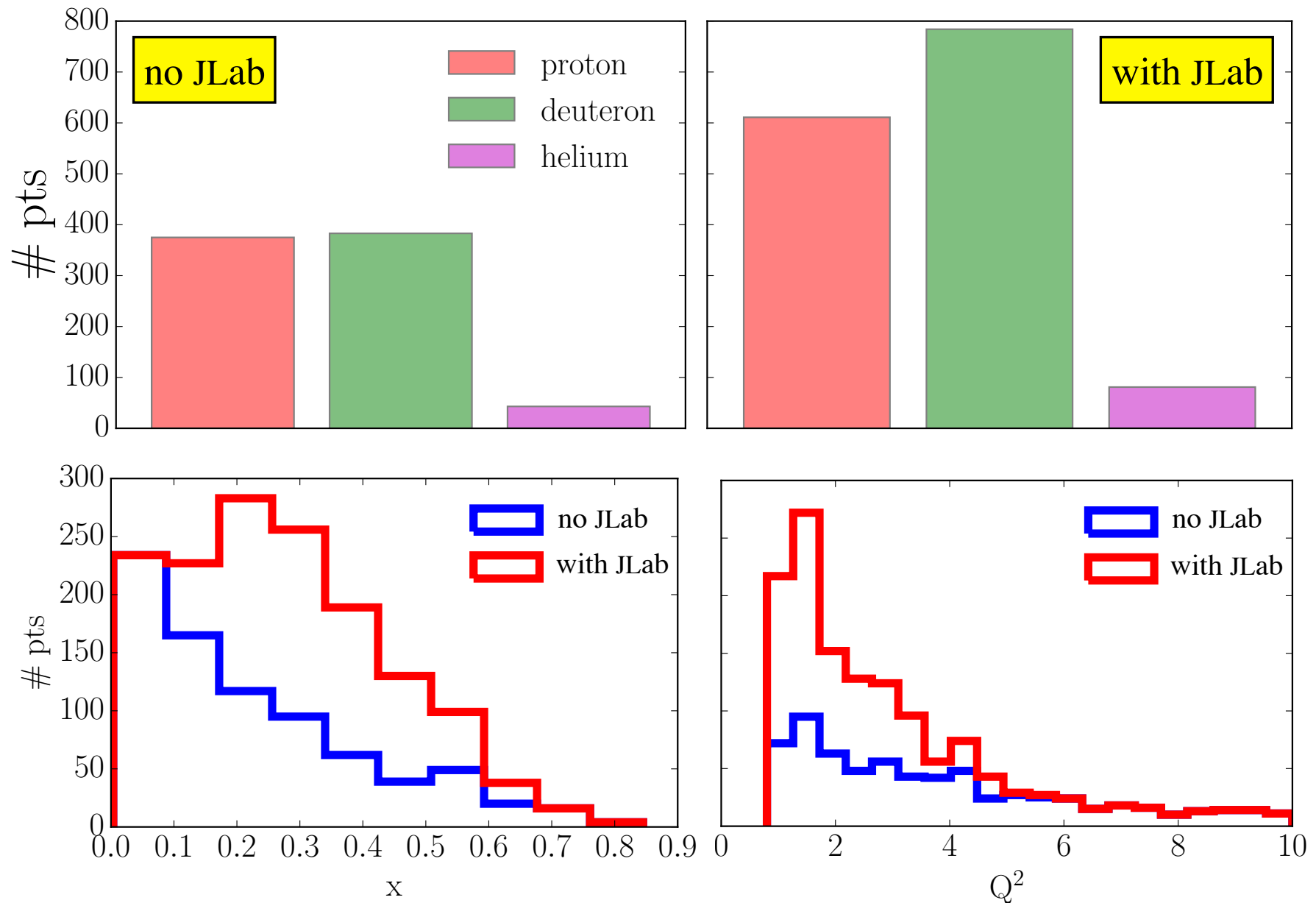
$$A_2 = \gamma(g_1 + g_2) \frac{2x}{(1 + \gamma^2)F_2 - F_L}$$

→ remove assumptions about $R = \sigma_L/\sigma_T$ ratio



Inclusive DIS global analysis

Significant contribution of JLab data to global database



Inclusive DIS global analysis

- Parametrization at scale $Q^2 = \mu_0^2 (= 1 \text{ GeV}^2)$

$$x\Delta q^+(x) = Nx^\alpha(1-b)^\beta(1+\gamma x)$$

$$\Delta q^+ \equiv \Delta q + \Delta \bar{q}$$

→ constraints from hadronic weak decays

$$\Delta u^{+(1)} - \Delta d^{+(1)} = 1.269(3), \quad \Delta u^{+(1)} + \Delta d^{+(1)} - 2\Delta s^{+(1)} = 0.586(31)$$

- Q^2 evolution performed in moment space

$$f^{(n)}(Q^2) = \int_0^1 dx x^{n-1} f(x, Q^2)$$

→ significant efficiencies compared with x -space evolution

Inclusive DIS global analysis

- Inclusive DIS data constrain Δu^+ & Δd^+ distributions
→ mostly insensitive to polarized strangeness and glue

- Assume g_1, g_2 can be described as sum of twist $\tau = 2$ and higher twist terms

$$g_1 = g_1^{\tau 2(\text{TMC})} + g_1^{\tau 3(\text{TMC})} + g_1^{\tau 4}$$

$$g_2 = g_2^{\tau 2(\text{TMC})} + g_2^{\tau 3(\text{TMC})}$$

includes OPE target mass corrections

- Structure function (moments) at leading twist τ (at NLO)

$$g_{1,\tau 2}^{(n)} = \frac{1}{2} \sum_q e_q^2 (\Delta C_{qq}^{(n)} \Delta q^{(n)} + \Delta C_g^{(n)} \Delta g^{(n)})$$

$$g_{2,\tau 2}^{(n)} = -\frac{n-1}{n} g_{1,\tau 2}^{(n)}$$

Wandzura-Wilczek relation

Inclusive DIS global analysis

■ Higher twist corrections

→ twist-3 part of g_1 related to twist-3 part of g_2

$$g_1^{\tau 3} = (\rho^2 - 1) \left[g_2^{\tau 3} - 2 \int_x^1 \frac{dy}{y} g_2^{\tau 3} \right]$$

→ twist-3 part of g_2 parametrized via twist-3 PDFs

$$D^{\tau 3}(x) = N x^a (1-x)^b (1+cx) \quad \text{NOT } Q^2 \text{ SUPPRESSED!}$$

– at parton level

→ similar functional form also for twist-4 part

$$g_1^{\tau 4} = \frac{h(x)}{Q^2} = N' x^{a'} (1-x)^{b'} (1+\gamma' x) \frac{1}{Q^2}$$

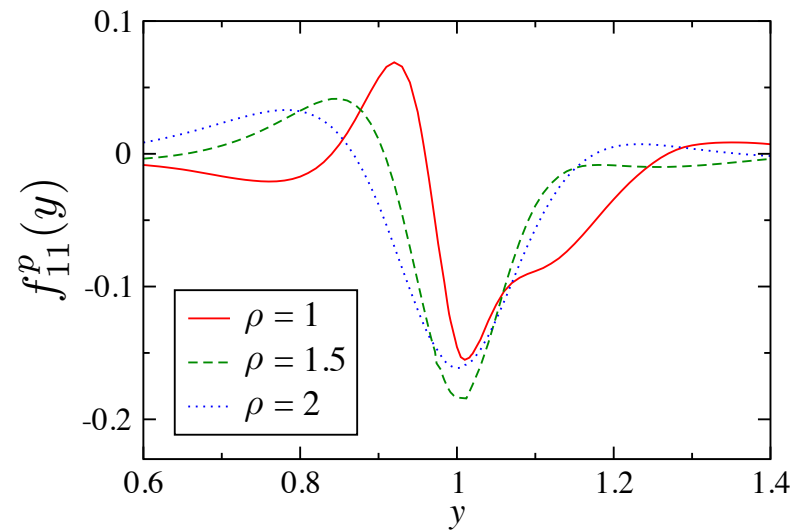
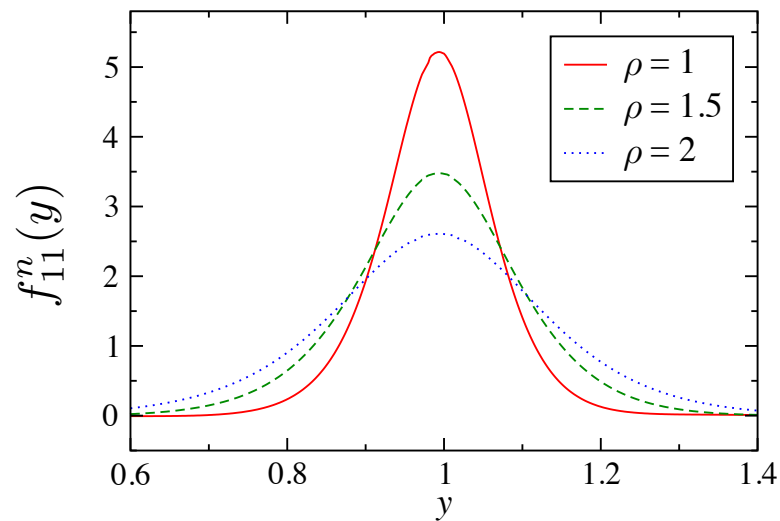
– at hadron level

Inclusive DIS global analysis

■ Nuclear corrections

→ nuclear binding and Fermi motion described by (spin-dependent) smearing functions

$$g_i^A(x) = \int \frac{dy}{y} f_{ij}^N(y) g_j^N(x/y)$$

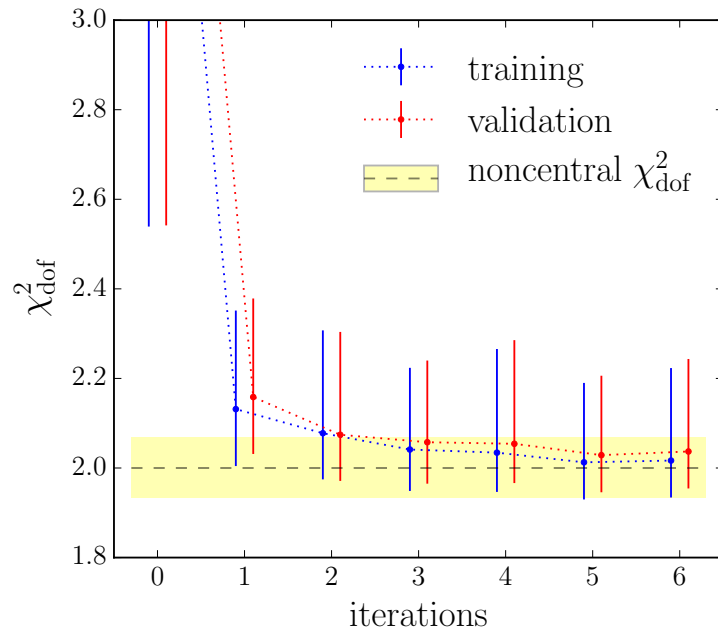


→ effective polarization approximation (EPA) often used...

$$f^N(y) \rightarrow \langle \sigma_z \rangle^N \delta(y - 1)$$

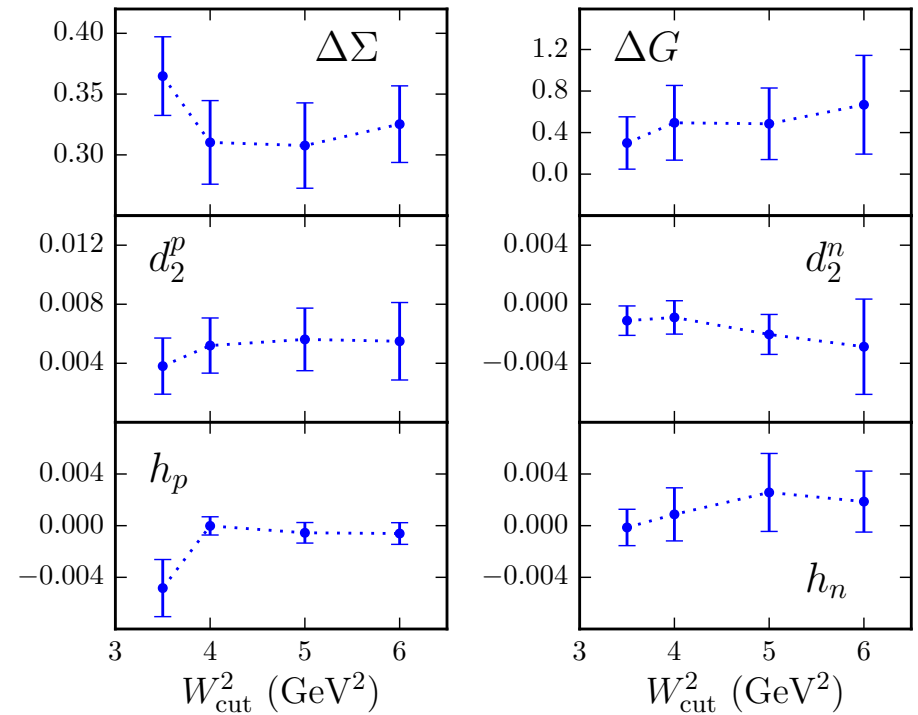
IMC analysis

Convergence criteria



→ convergence after
~ 5–6 iterations

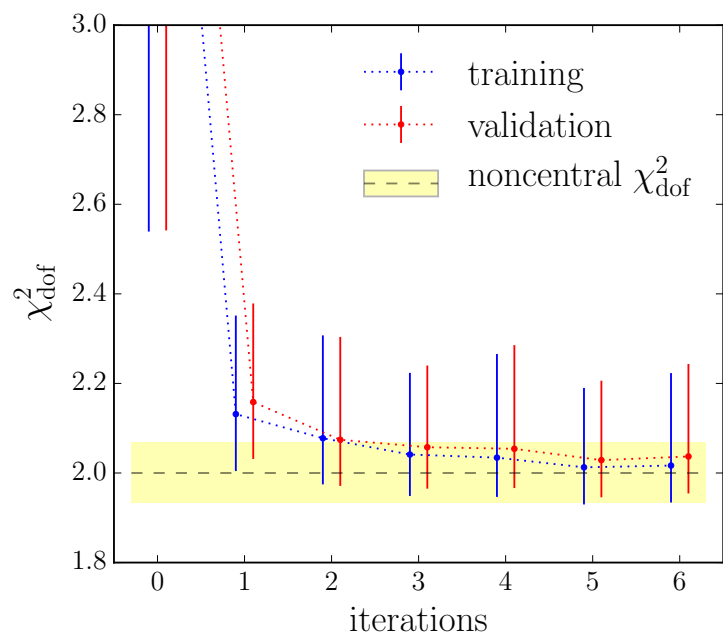
Sensitivity to kinematic cuts



→ stability for $W^2 > 4$ GeV²

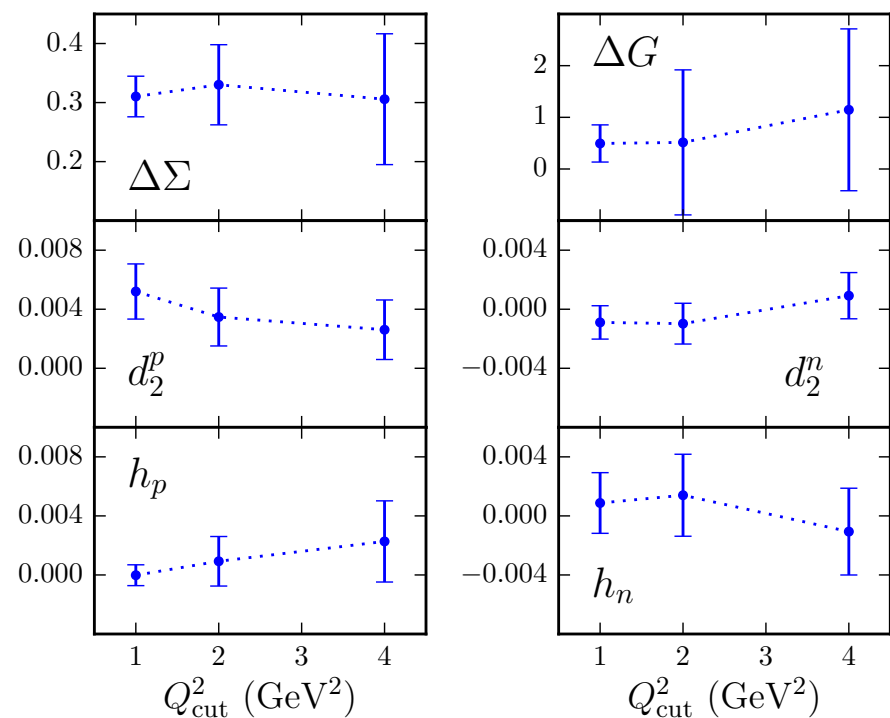
IMC analysis

Convergence criteria



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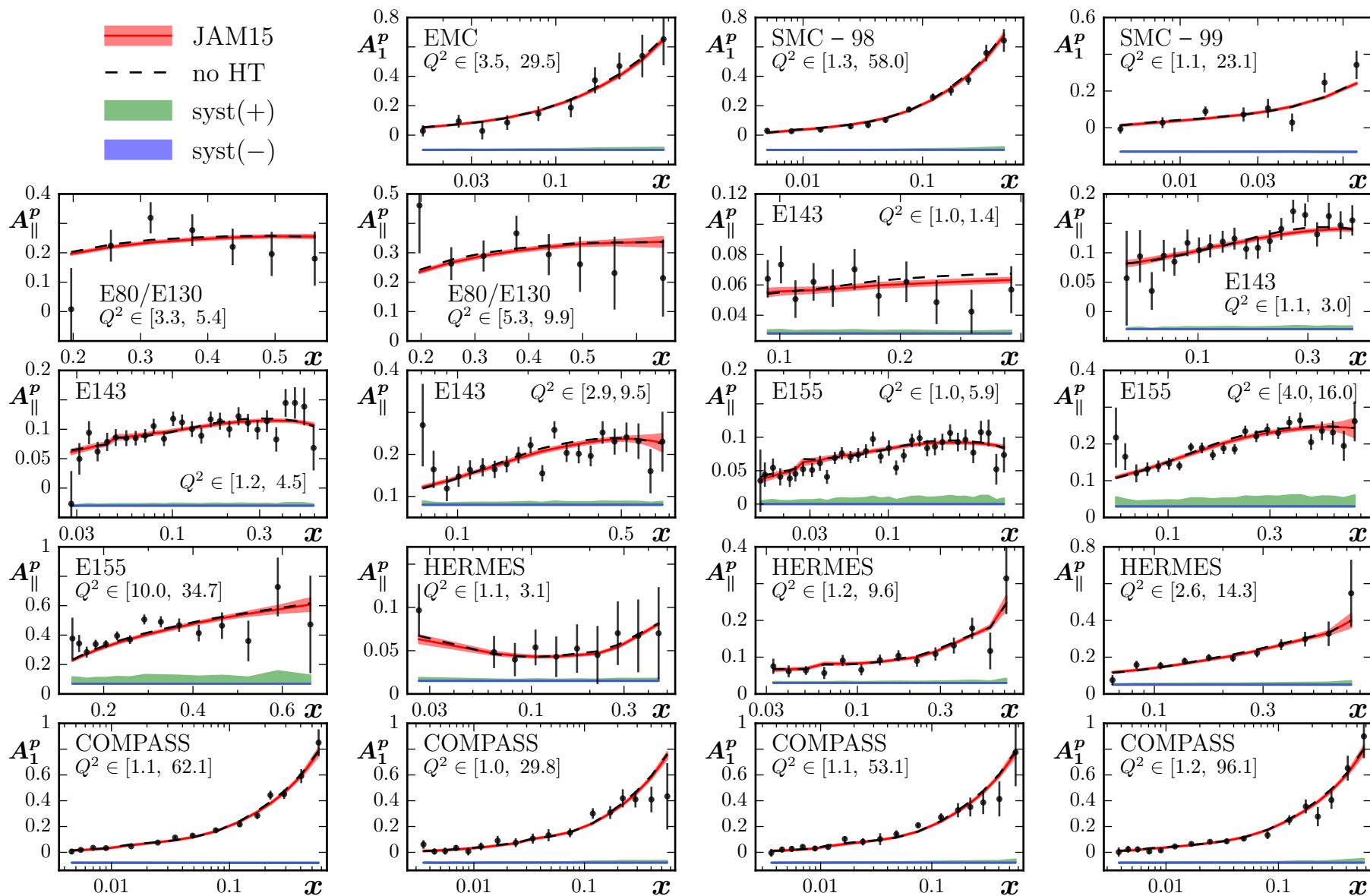
Sensitivity to kinematic cuts



→ stability for $W^2 > 4$ GeV²
and $Q^2 > 1$ GeV²

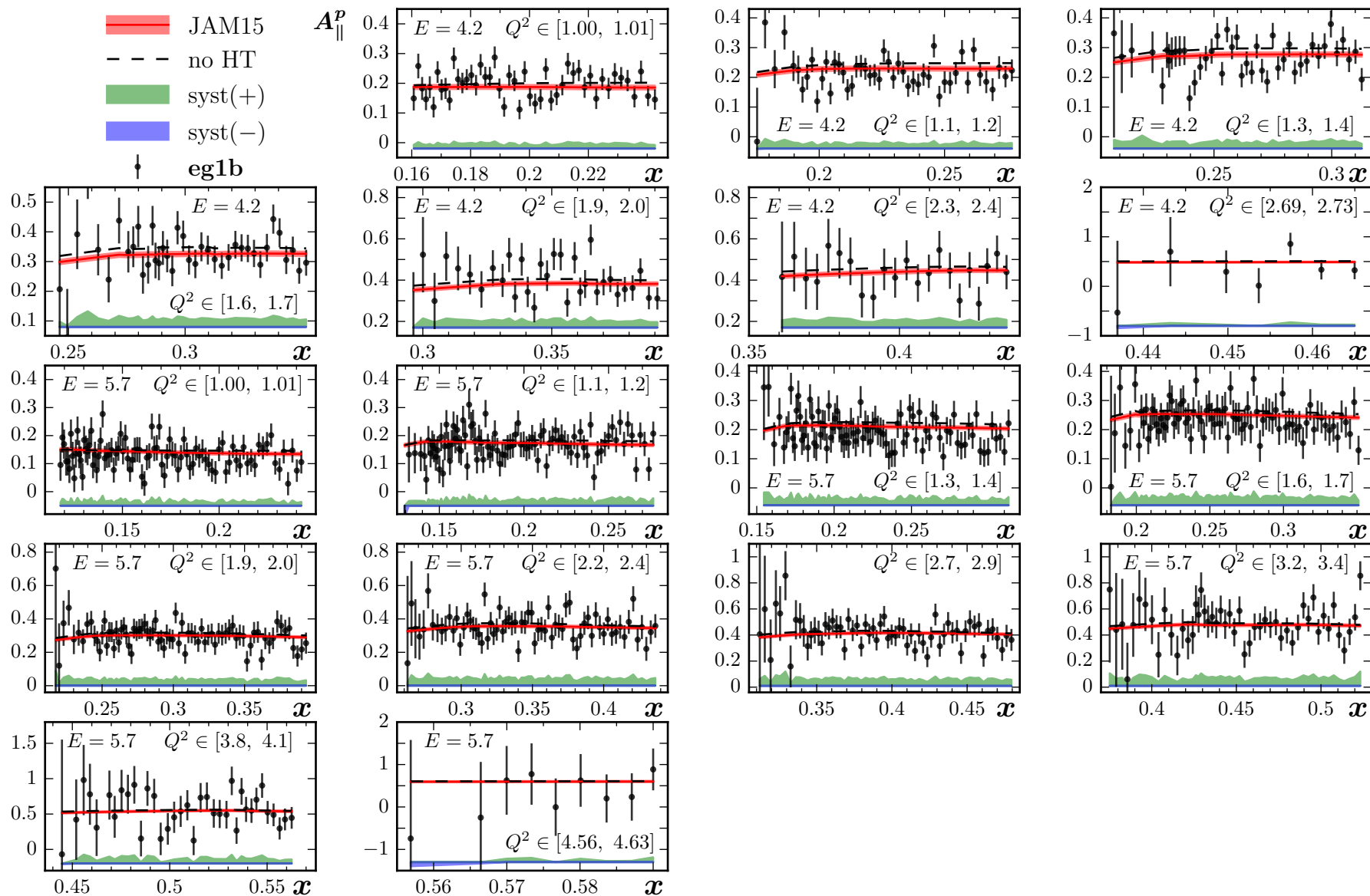
IMC analysis

previous world data



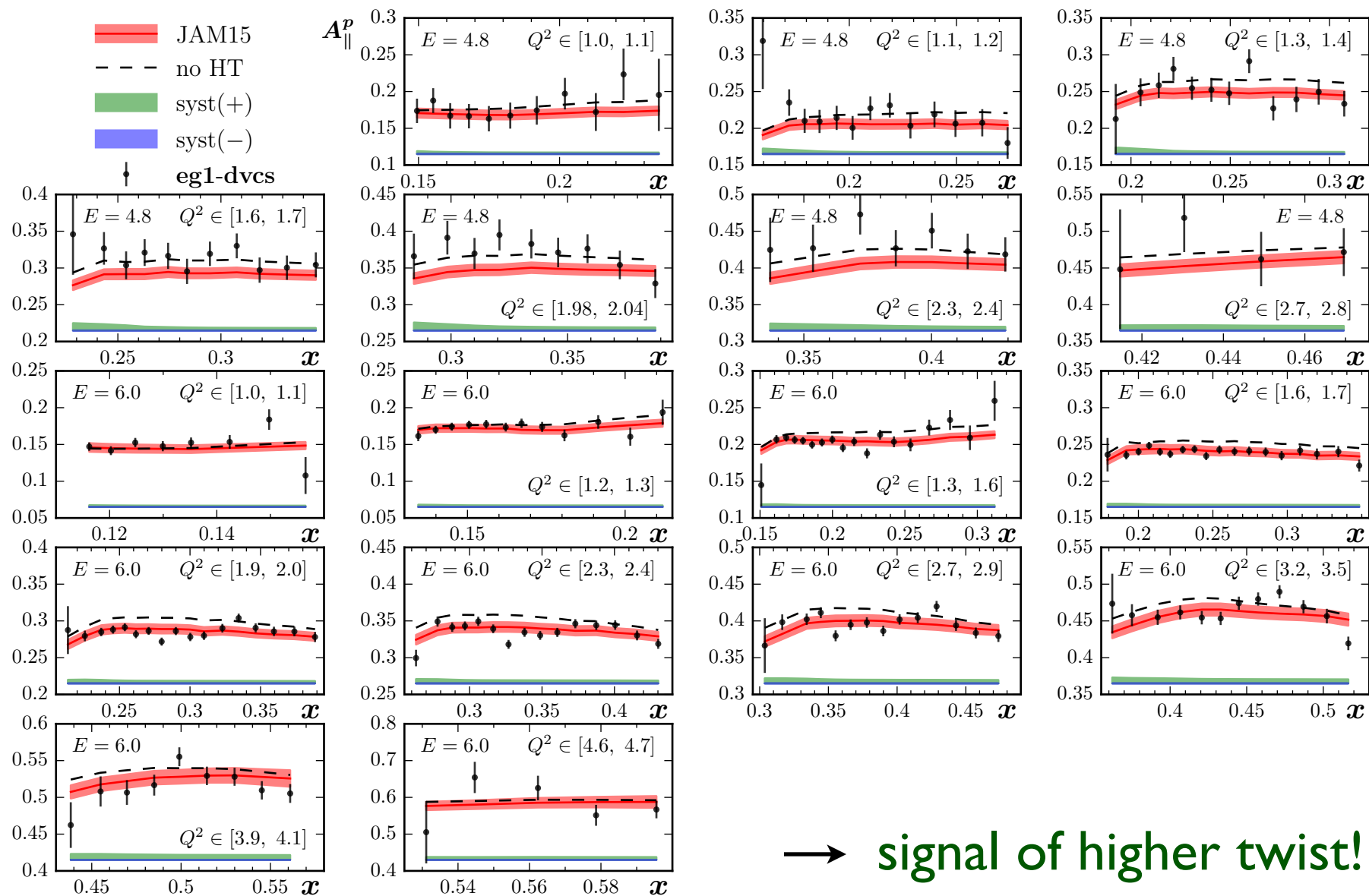
IMC analysis

■ JLab eg1b (CLAS) data



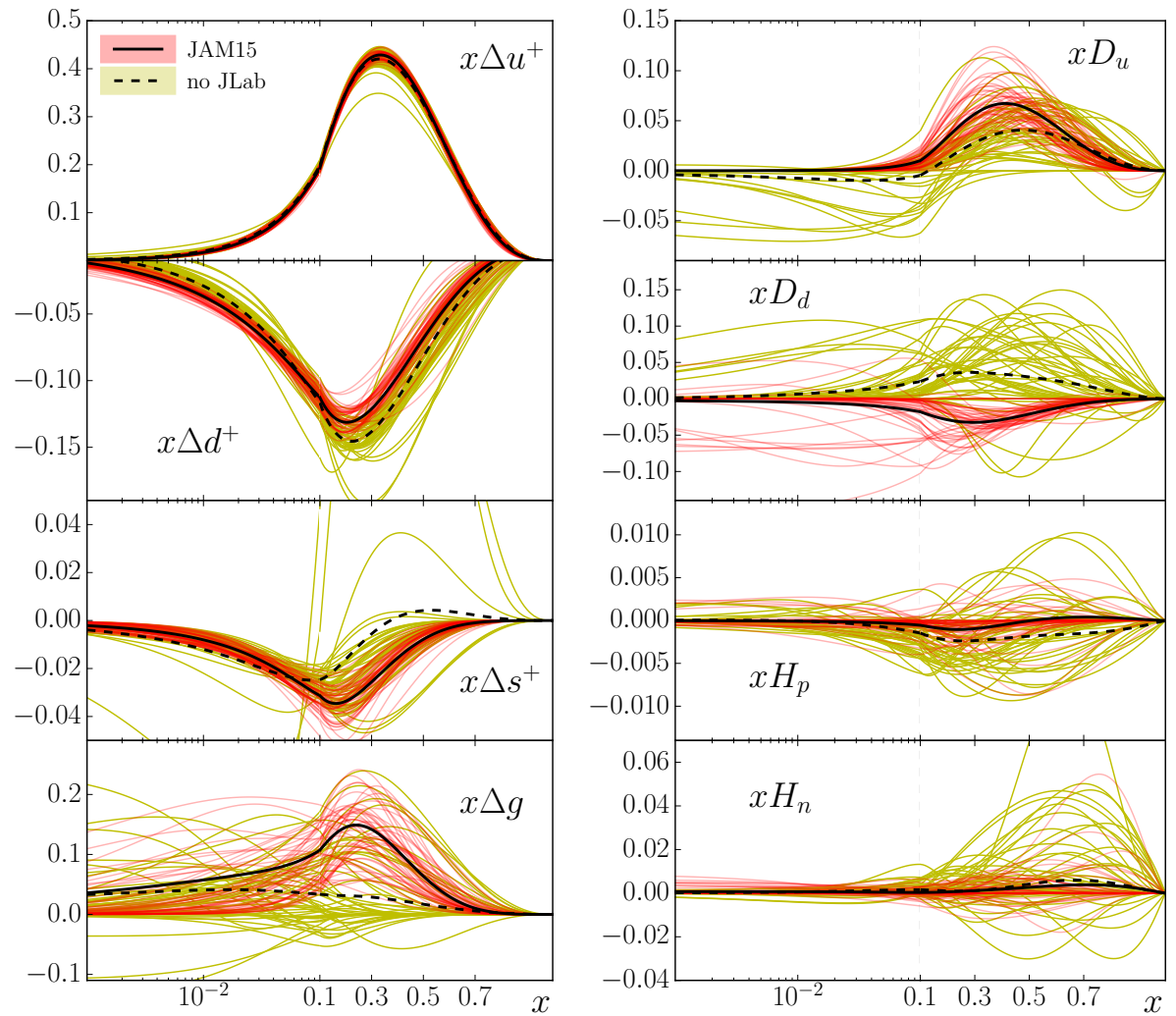
IMC analysis

■ JLab eg1-dvcs (CLAS) data



Impact of JLab data

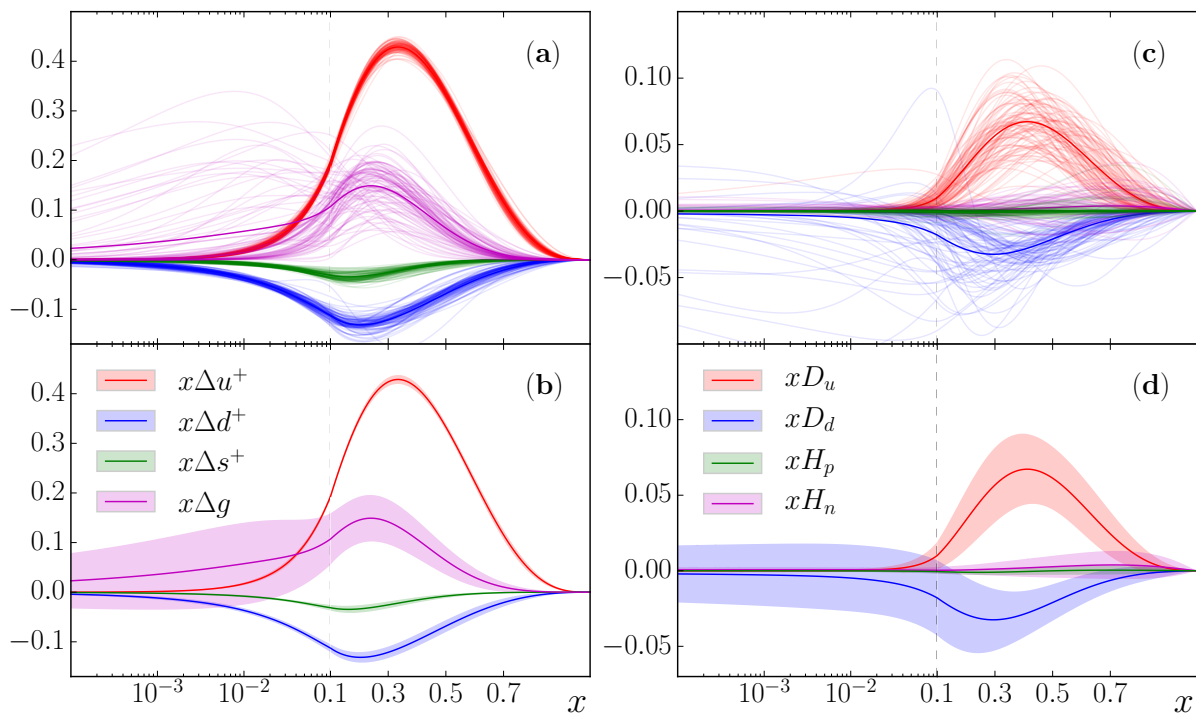
Experiment	Reference	Observable	Target	Number of points	χ^2_{dof}
EMC	[69]	A_1	p	10	0.40
SMC	[70]	A_1	p	12	0.47
SMC	[70]	A_1	d	12	1.62
SMC	[71]	A_1	p	8	1.26
SMC	[71]	A_1	d	8	0.57
COMPASS	[72]	A_1	p	15	0.92
COMPASS	[73]	A_1	d	15	0.67
COMPASS	[39]	A_1	p	51	0.76
SLAC E80/E130	[74]	A_{\parallel}	p	22	0.59
SLAC E142	[75]	A_1	${}^3\text{He}$	8	0.49
SLAC E142	[75]	A_2	${}^3\text{He}$	8	0.60
SLAC E143	[76]	A_{\parallel}	p	81	0.80
SLAC E143	[76]	A_{\parallel}	d	81	1.12
SLAC E143	[76]	A_{\perp}	p	48	0.89
SLAC E143	[76]	A_{\perp}	d	48	0.91
SLAC E154	[77]	A_{\parallel}	${}^3\text{He}$	18	0.51
SLAC E154	[77]	A_{\perp}	${}^3\text{He}$	18	0.97
SLAC E155	[78]	A_{\parallel}	p	71	1.20
SLAC E155	[79]	A_{\parallel}	d	71	1.05
SLAC E155	[80]	A_{\perp}	p	65	0.99
SLAC E155	[80]	A_{\perp}	d	65	1.52
SLAC E155x	[81]	\tilde{A}_{\perp}	p	116	1.27
SLAC E155x	[81]	\tilde{A}_{\perp}	d	115	0.83
HERMES	[82]	A_1	"n"	9	0.25
HERMES	[83]	A_{\parallel}	p	35	0.47
HERMES	[83]	A_{\parallel}	d	35	0.94
HERMES	[84]	A_2	p	19	0.93
JLab E99-117	[85]	A_{\parallel}	${}^3\text{He}$	3	0.27
JLab E99-117	[85]	A_{\perp}	${}^3\text{He}$	3	1.58
JLab E06-014	[17]	A_{\parallel}	${}^3\text{He}$	14	2.12
JLab E06-014	[18]	A_{\perp}	${}^3\text{He}$	14	1.06
JLab eg1-dvcs	[15]	A_{\parallel}	p	195	1.52
JLab eg1-dvcs	[15]	A_{\parallel}	d	114	0.94
JLab eg1b	[14]	A_{\parallel}	p	890	1.11
JLab eg1b	[16]	A_{\parallel}	d	218	1.02
Total				2515	1.07



→ reduced uncertainty in Δs^+ , Δg

→ nonzero twist-3 contributions

Impact of JLab data

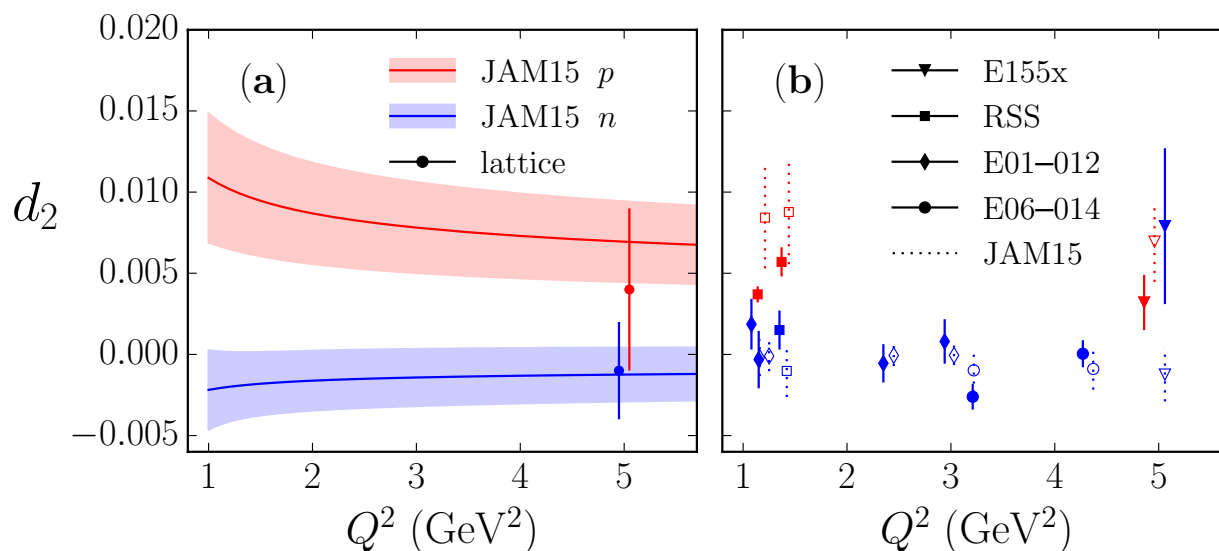


- twist-3 PDFs large!
- same sign as twist-2
- twist-4 term negligible

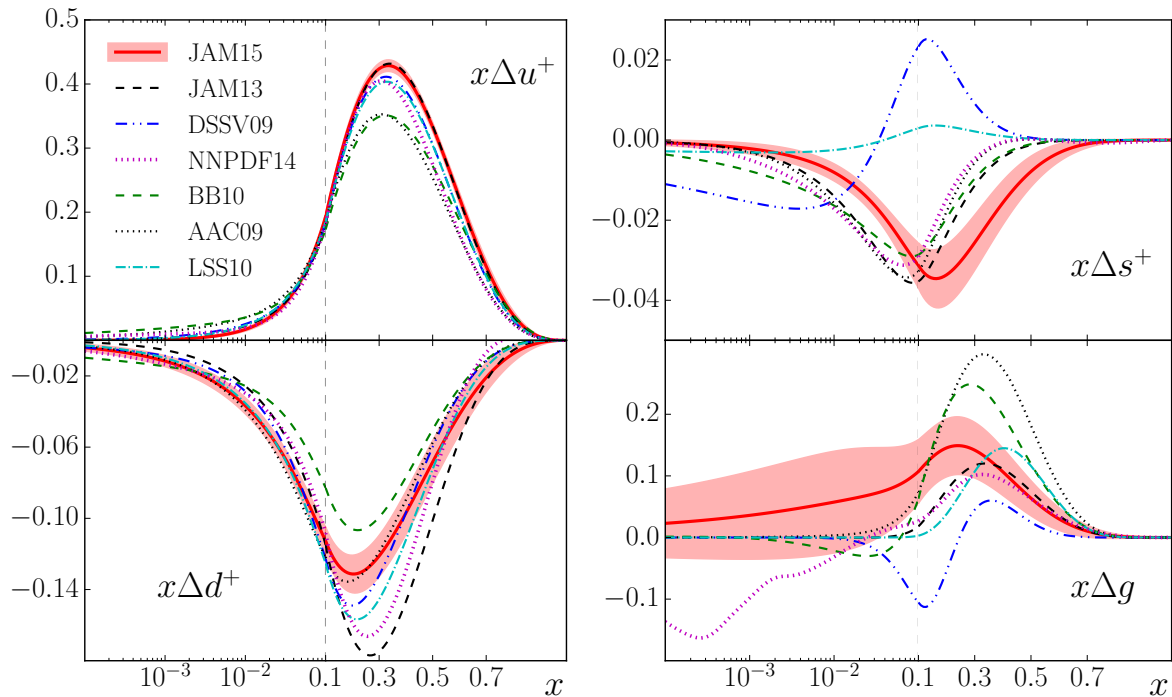
→ matrix element

$$d_2 = 2g_1^{(3)} + 3g_2^{(3)}$$

related to
“color polarizability”
or “transverse force”
acting on quarks



Comparison with other analyses



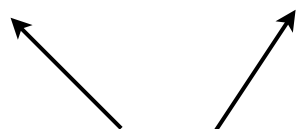
Moment	Truncated	Full
Δu^+	0.82 ± 0.01	0.83 ± 0.01
Δd^+	-0.42 ± 0.01	-0.44 ± 0.01
Δs^+	-0.10 ± 0.01	-0.10 ± 0.01
$\Delta \Sigma$	0.31 ± 0.03	0.28 ± 0.04
ΔG	0.5 ± 0.4	1 ± 15
d_2^p	0.005 ± 0.002	0.005 ± 0.002
d_2^n	-0.001 ± 0.001	-0.001 ± 0.001
h_p	-0.000 ± 0.001	0.000 ± 0.001
h_n	0.001 ± 0.002	0.001 ± 0.003

- u and d polarization similar to earlier results
- s -quark polarization *negative*
- gluon polarization similar to recent DSSV fits
 - moment unconstrained

Polarization of quark sea?

- Inclusive DIS data cannot distinguish between q and \bar{q}

→ semi-inclusive DIS sensitive to Δq & $\Delta \bar{q}$

$$\sim \sum_q e_q^2 [\Delta q(x) D_q^h(z) + \Delta \bar{q}(x) D_{\bar{q}}^h(z)]$$


→ but need fragmentation functions!

- Global analysis of DIS + SIDIS data gives different *sign* for strange quark polarization for different fragmentation functions!

→ $\Delta s > 0$ for “DSS” parametrization *de Florian et al., PRD75, 094009 (2007)*

$\Delta s < 0$ for “HKNS” parametrization *Hirai et al., PRD75, 114010 (2007)*

→ need to understand origin of differences in fragmentation!

IMC analysis of fragmentation functions

- Analyze single-inclusive $e^+ e^-$ annihilation data for pion & kaon production from DESY, CERN, SLAC & KEK from $Q \sim 10$ GeV to Z-boson pole

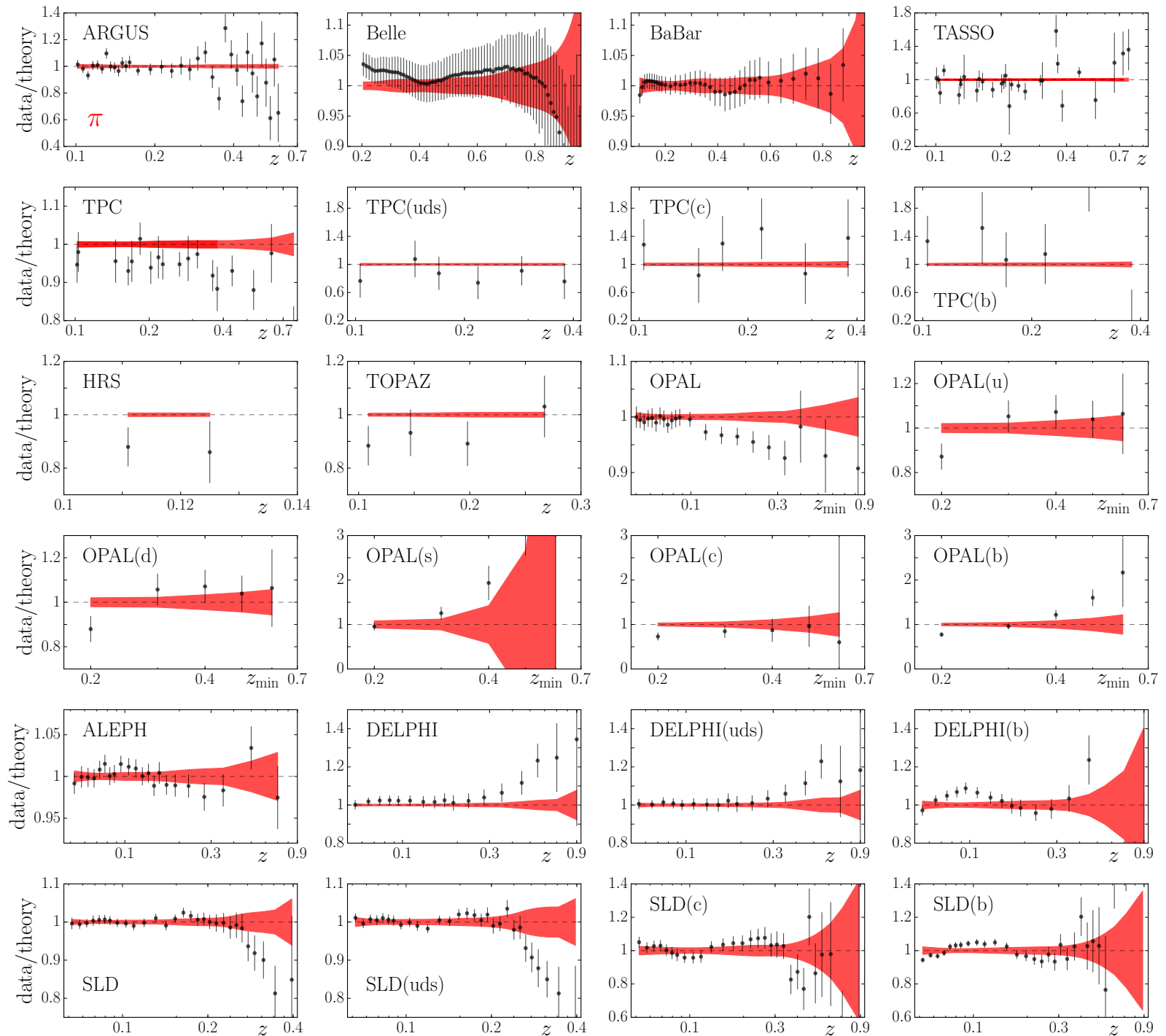
Experiment	Ref.	Observable	Q (GeV)	Pions			Kaons		
				N_{dat}	norm.	χ^2	N_{dat}	norm.	χ^2
ARGUS	[26]	Inclusive	9.98	35	1.024 (1.058)	51.1 (55.8)	15	1.007	8.5
Belle	[38,39]	Inclusive	10.52	78	0.900 (0.919)	37.6 (21.7)	78	0.988	10.9
BABAR	[40]	Inclusive	10.54	39	0.993 (0.948)	31.6 (70.7)	30	0.992	4.9
TASSO	[23–25]	Inclusive	12–44	29	(*)	37.0 (38.8)	18	(*)	14.3
TPC	[27–29]	Inclusive	29.00	18	1	36.3 (57.8)	16	1	47.8
		uds tag	29.00	6	1	3.7 (4.6)			
		b tag	29.00	6	1	8.7 (8.6)			
		c tag	29.00	6	1	3.3 (3.0)			
HRS	[30]	Inclusive	29.00	2	1	4.2 (6.2)	3	1	0.3
TOPAZ	[37]	Inclusive	58.00	4	1	4.8 (6.3)	3	1	0.9
OPAL	[32,33]	Inclusive	91.20	22	1	33.3 (37.2)	10	1	6.3
		u tag	91.20	5	1.203 (1.203)	6.6 (8.1)	5	1.185	2.1
		d tag	91.20	5	1.204 (1.203)	6.1 (7.6)	5	1.075	0.6
		s tag	91.20	5	1.126 (1.200)	14.4 (11.0)	5	1.173	1.5
		c tag	91.20	5	1.174 (1.323)	10.7 (6.1)	5	1.169	13.2
		b tag	91.20	5	1.218 (1.209)	34.2 (36.6)	4	1.177	10.9
		Inclusive	91.20	22	0.987 (0.989)	15.6 (20.4)	18	1.008	6.1
ALEPH	[34]	Inclusive	91.20	22	0.987 (0.989)	15.6 (20.4)	18	1.008	6.1
DELPHI	[35,36]	Inclusive	91.20	17	1	21.0 (20.2)	27	1	3.9
		uds tag	91.20	17	1	13.3 (13.4)	17	1	22.5
		b tag	91.20	17	1	41.9 (42.9)	17	1	9.1
SLD	[31]	Inclusive	91.28	29	1.002 (1.004)	27.3 (36.3)	29	0.994	14.3
		uds tag	91.28	29	1.003 (1.004)	51.7 (55.6)	29	0.994	42.6
		c tag	91.28	29	0.998 (1.001)	30.2 (40.4)	29	1.000	31.7
		b tag	91.28	29	1.005 (1.005)	74.6 (61.9)	28	0.992	134.1
Total:				459		599.3 (671.2)	391		395.0

$$\chi^2/N_{\text{dat}} = 1.31 (1.46)$$

$$\chi^2/N_{\text{dat}} = 1.01$$

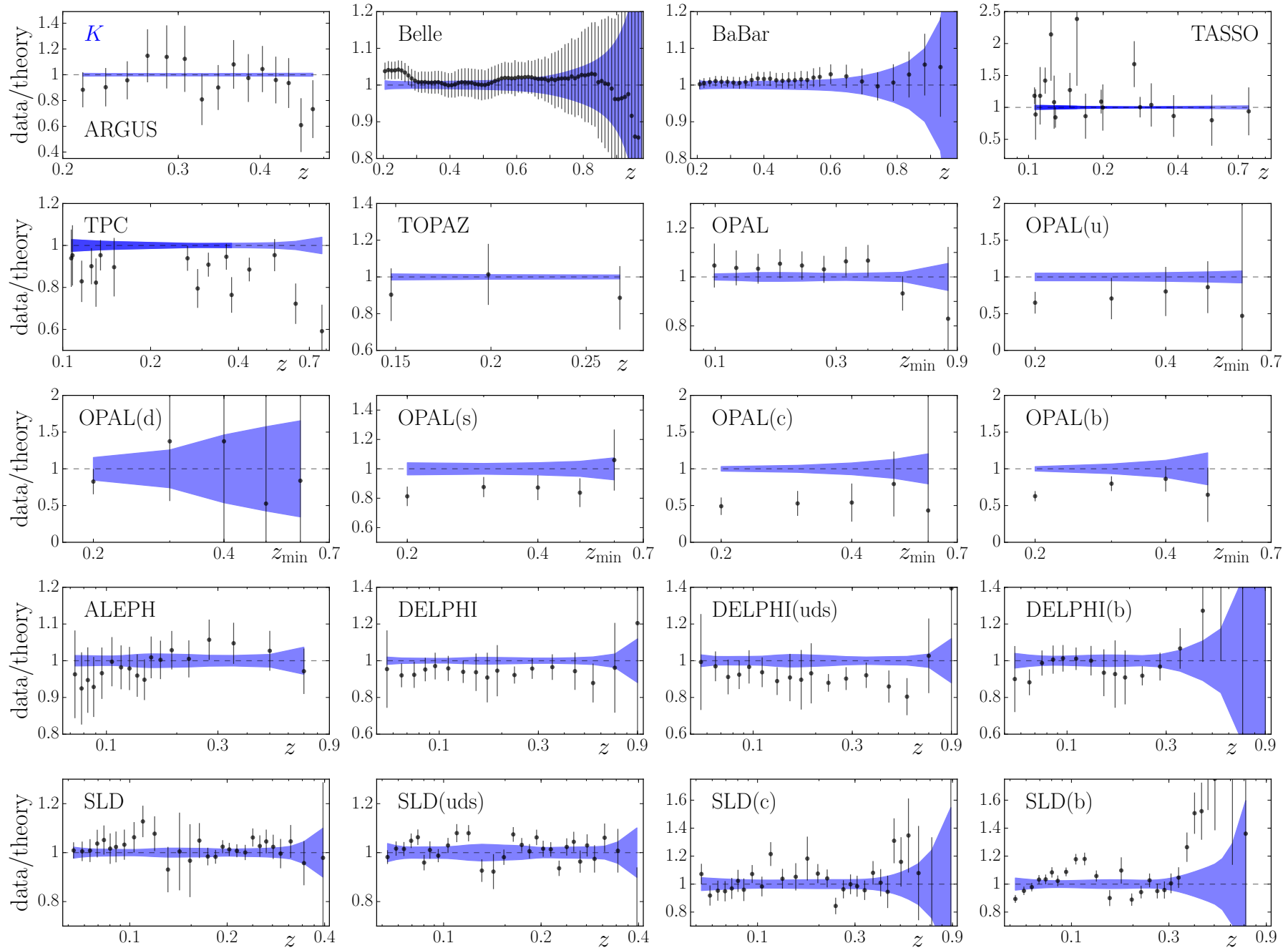
IMC analysis of fragmentation functions

■ pion data

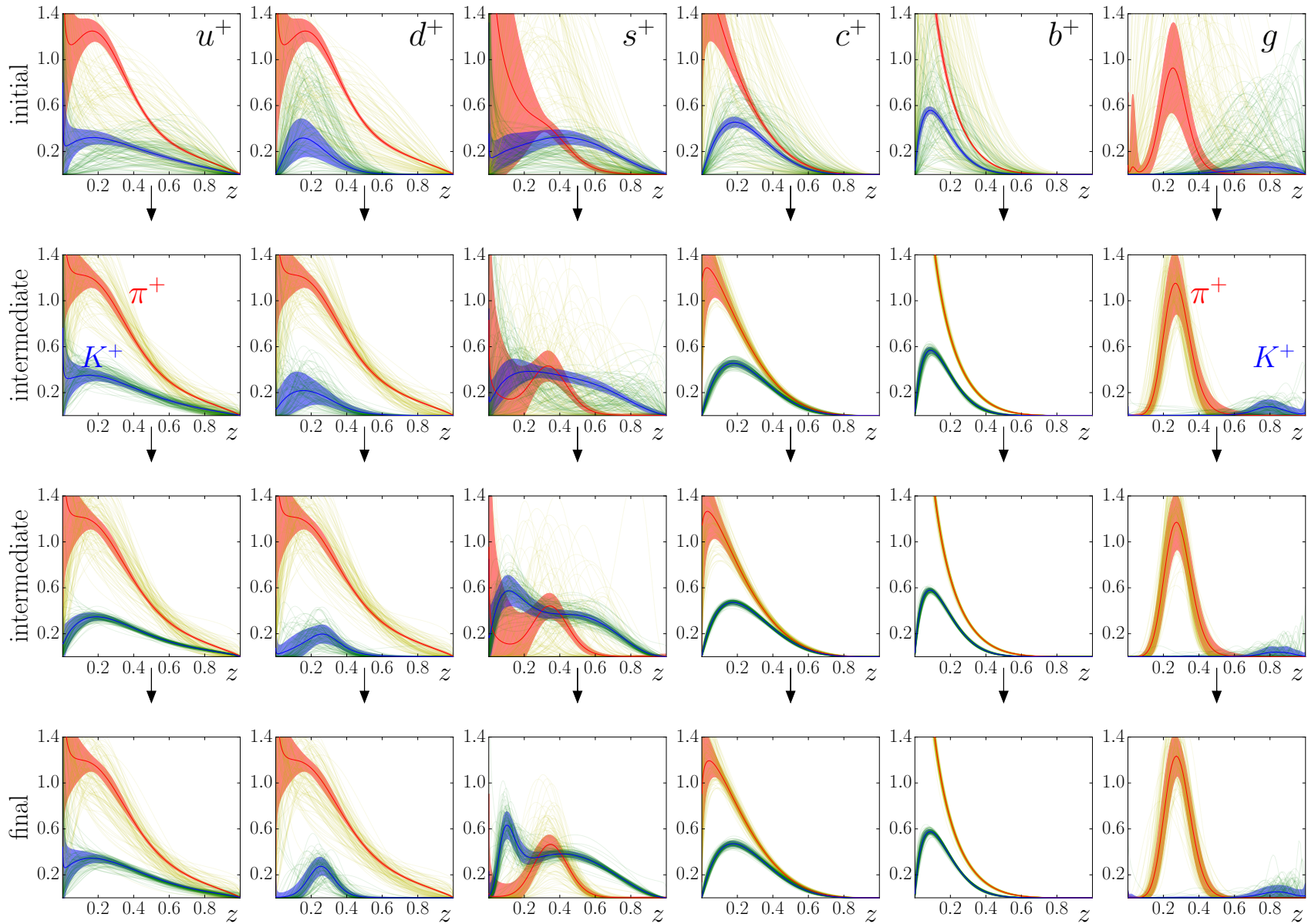


IMC analysis of fragmentation functions

kaon data

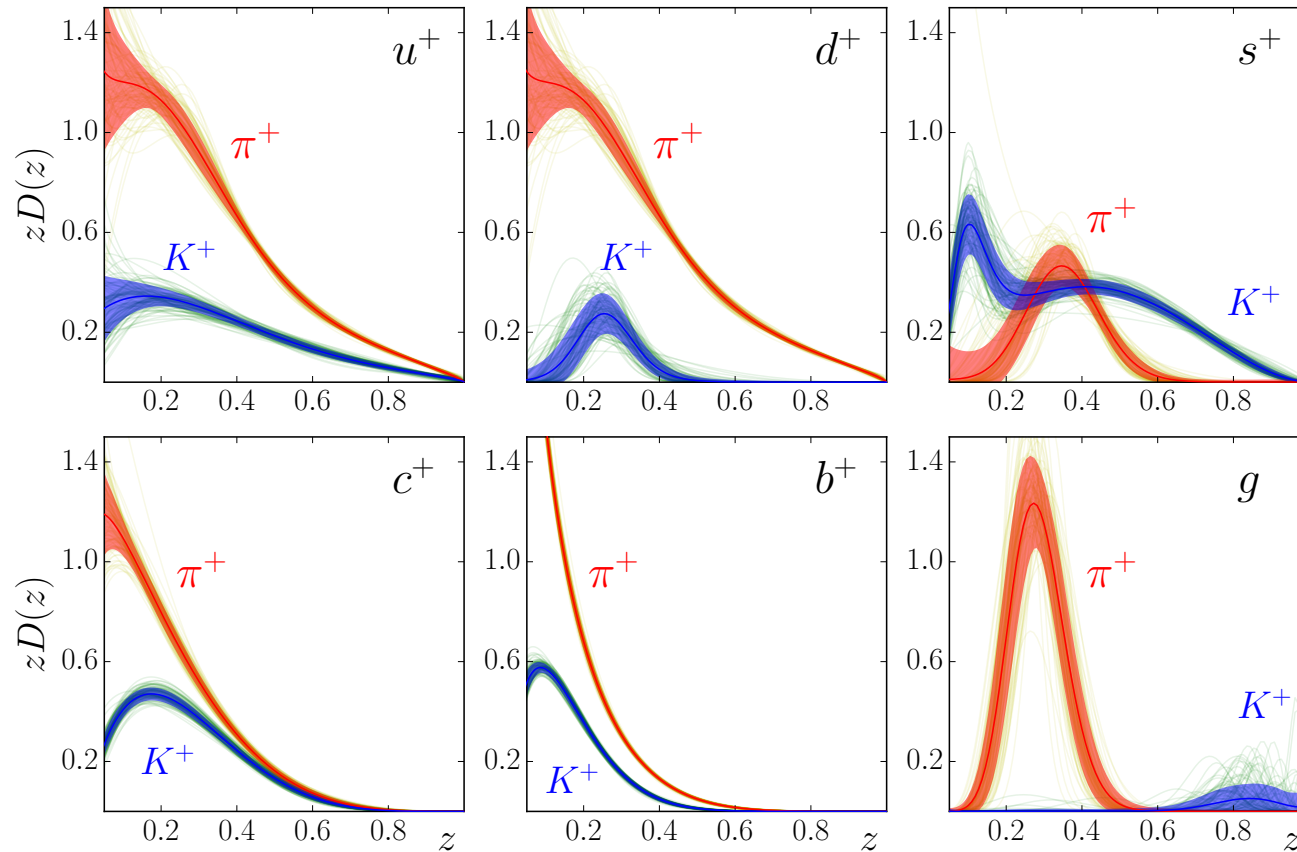


IMC analysis of fragmentation functions



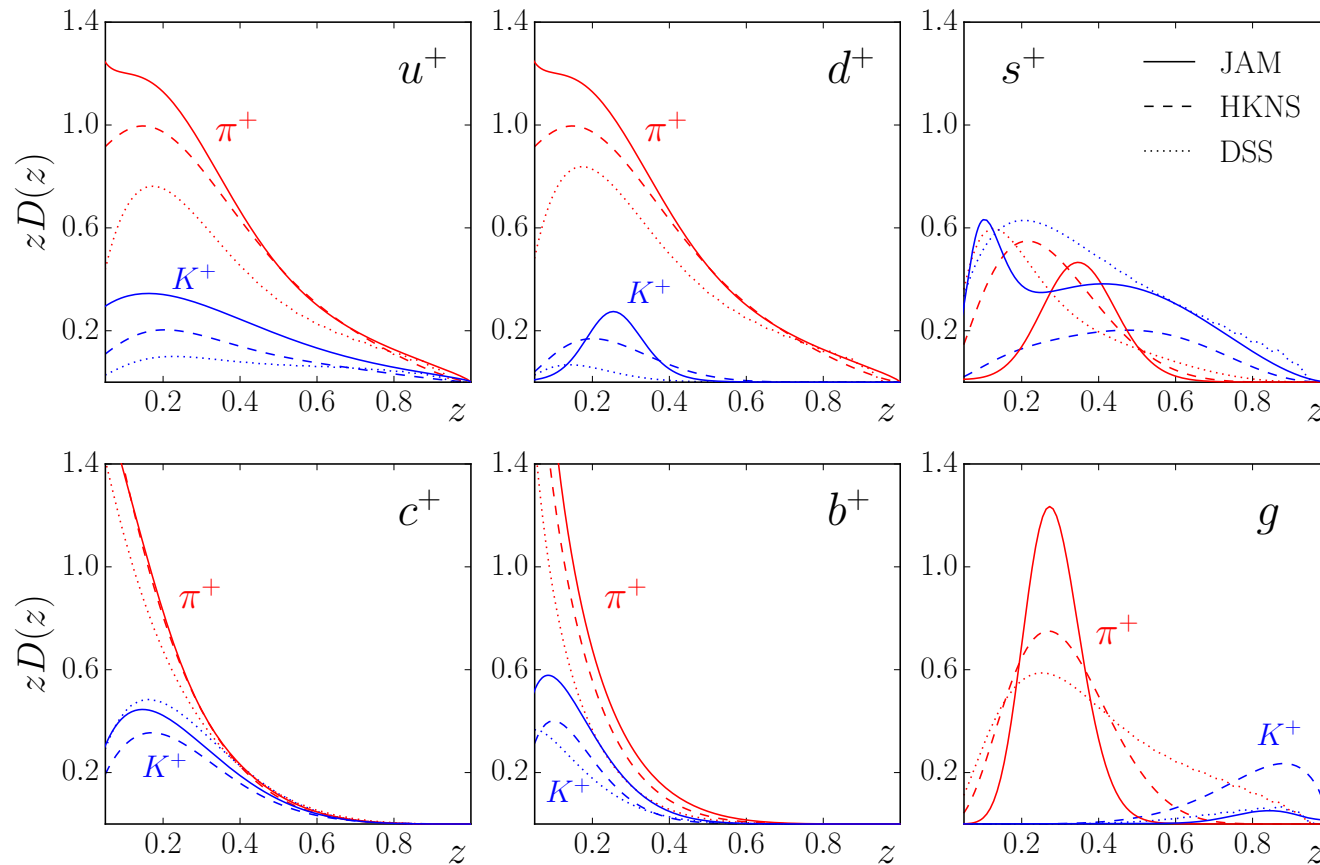
→ convergence after ~ 20 iterations

IMC analysis of fragmentation functions



- favored FFs well constrained
- unfavored FFs not as well constrained
- very hard $g \rightarrow K$ fragmentation

IMC analysis of fragmentation functions



- qualitatively similar behavior as in previous analyses
- nontrivial shape of $s \rightarrow K$ fragmentation
- JAM strange FF closer to DSS parametrization
— impact on Δ_{s^+} extraction?

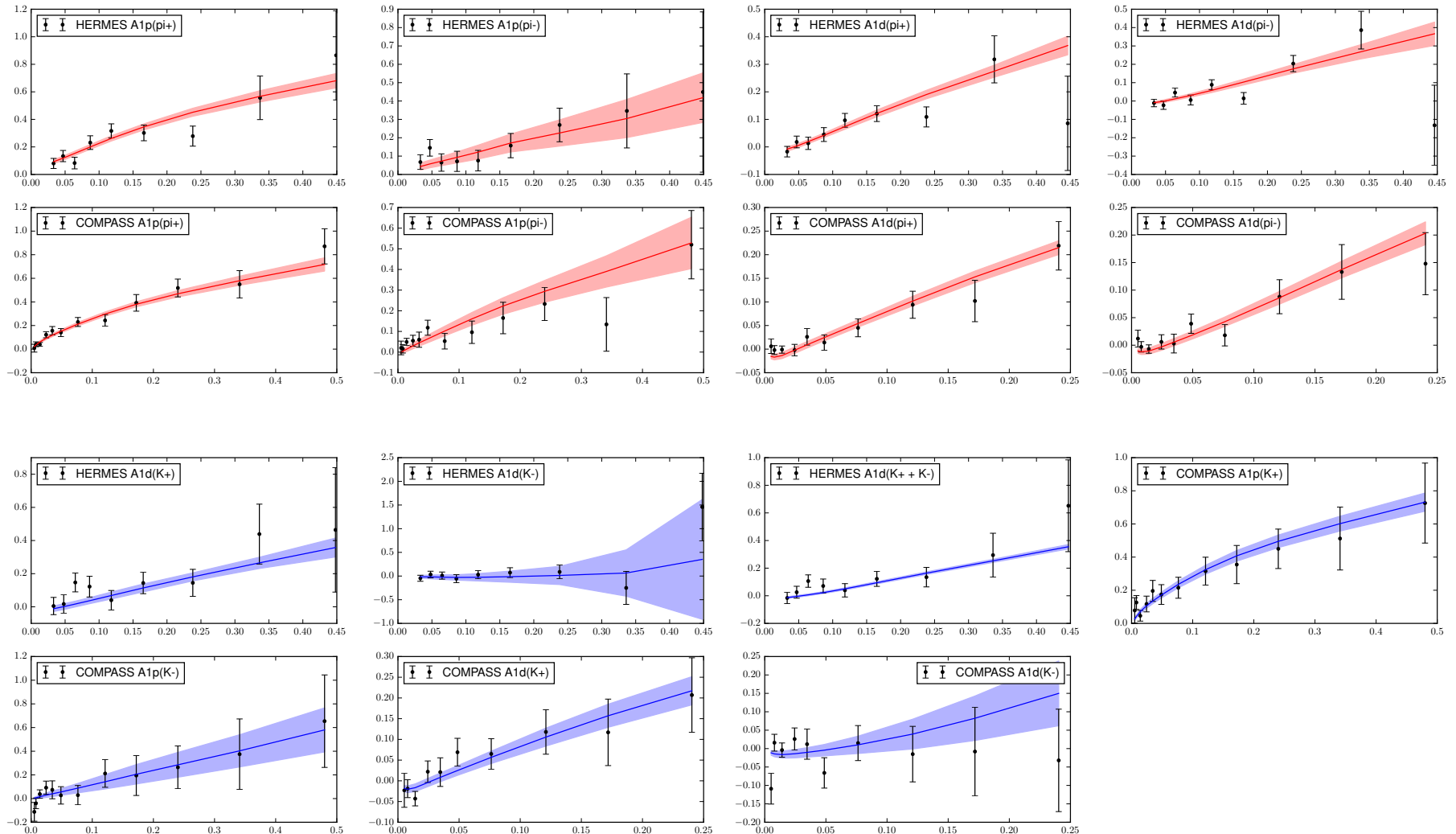
Outlook

- Short-term goal: combined analysis of DIS + SIDIS + SIA data to simultaneously extract *both* PDFs and fragmentation functions

Jacob Ethier et al. (2017)

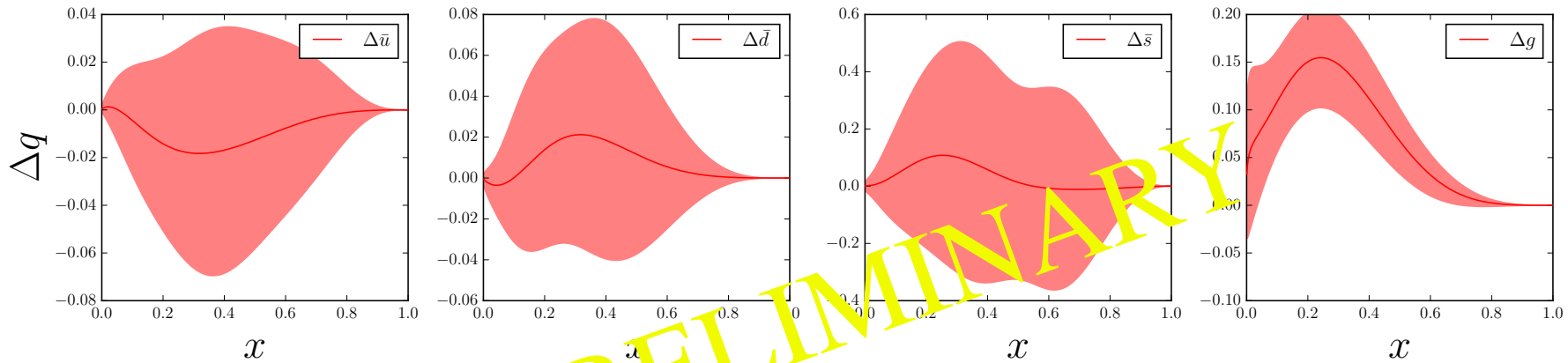
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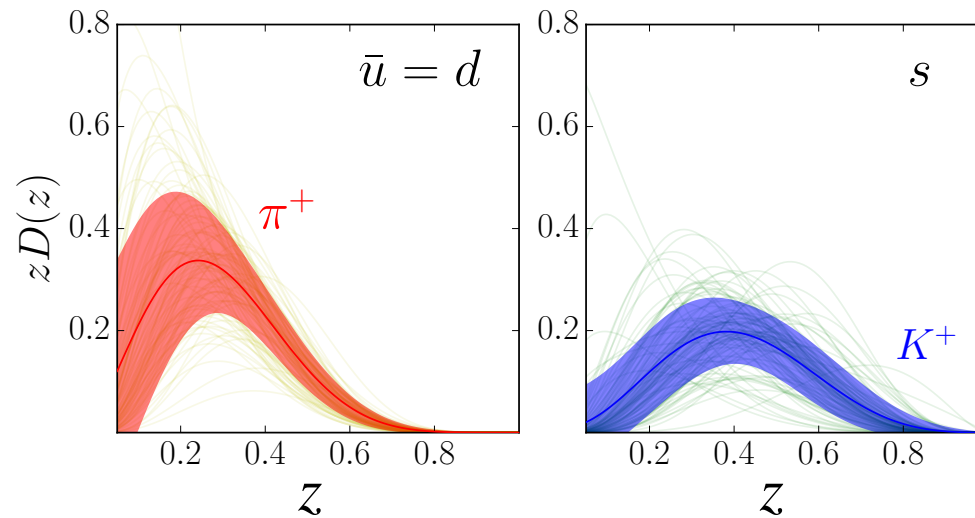
Outlook

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PRELIMINARY

first glimpse
of “unfavored”
PDFs and FFs...



Outlook

- Short-term goal: combined analysis of DIS + SIDIS + SIA data to simultaneously extract *both* PDFs and fragmentation functions

Jacob Ethier et al. (2017)

- Medium-term goal: perform “universal” analysis of all observables sensitive to collinear (unpolarized & polarized) PDFs and FFs

- Longer-term goal: apply IMC technology (where appropriate) to global QCD analysis of TMD PDFs and FFs