

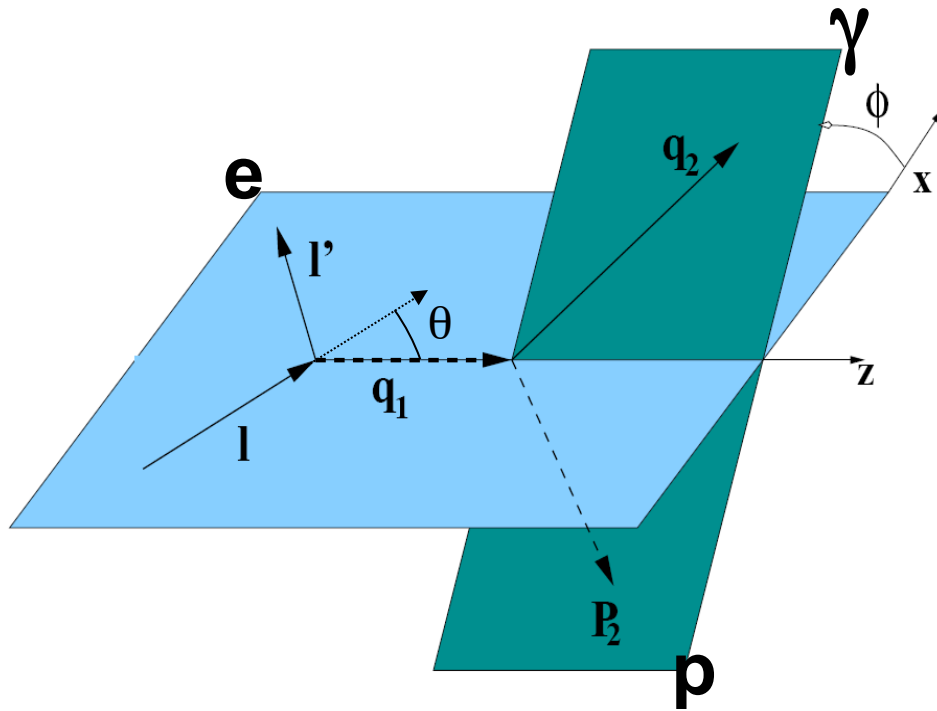
Measuring $P_b P_T$ using exclusive photon production

Harut Avakian

Deep processes working group meeting , JLab, June 17, 2016

- Hard exclusive photon production
 - BH propagators
- Extracting PBPT from double spin asymmetry
- Summary & Conclusions

Electroproduction Kinematics



$$Q^2 = -q_1^2 = 4EE' \sin(\theta / 2)$$

$$\nu = E - E'$$

$$x_B = -q_1^2 / 2p_1 q_1 = Q^2 / 2M\nu$$

$$y = \nu / E$$

$$t = (p_2 - p_1)^2 = \Delta^2$$

$\gamma^* \rightarrow \gamma$ require a finite longitudinal momentum transfer defined by the generalized Bjorken variable ξ

$$\xi = -\frac{(q_1 + q_2)^2}{2(p_1 + p_2)(q_1 + q_2)} \approx \frac{x_B}{2 - x_B}$$

$$\Delta_{\perp}^2 \approx (1 - \xi^2)(t - t_{\min})$$

$$t_{\min} \approx \frac{M^2 x^2}{1 - x + xM^2/Q^2}$$

Target Polarization Measurement from BH Double Spin Asymmetry

H. Avakian, V. Burkert, S. Chen, L. Elouadrhiri
Jefferson Lab, Newport News, VA 23606

Abstract

We present studies of the double spin asymmetry in the hard exclusive photon production. The double spin asymmetry which is dominated by the BH, is discussed as an alternative source of information on the product of beam and target polarizations for CLAS12 polarized target runs.

$$A_{LL} = \frac{(\frac{N^{\downarrow\uparrow}}{Q^{\downarrow\uparrow}} - \frac{N^{\uparrow\uparrow}}{Q^{\uparrow\uparrow}}) + (\frac{N^{\uparrow\downarrow}}{Q^{\uparrow\downarrow}} - \frac{N^{\downarrow\downarrow}}{Q^{\downarrow\downarrow}})}{f(\frac{N^{\uparrow\uparrow}}{Q^{\uparrow\uparrow}} + \frac{N^{\downarrow\uparrow}}{Q^{\downarrow\uparrow}} + \frac{N^{\uparrow\downarrow}}{Q^{\uparrow\downarrow}} + \frac{N^{\downarrow\downarrow}}{Q^{\downarrow\downarrow}})}$$

$$A_{LL} \sim \frac{c_{0,LP}^{BH}}{c_{0,unp}^{BH}}$$

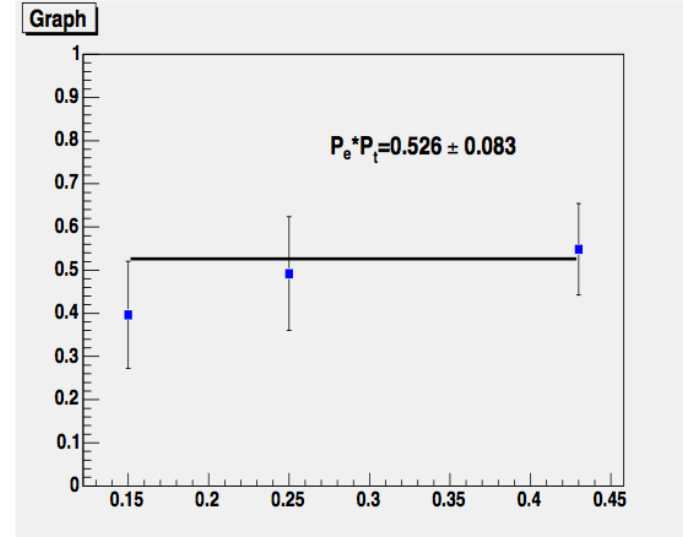
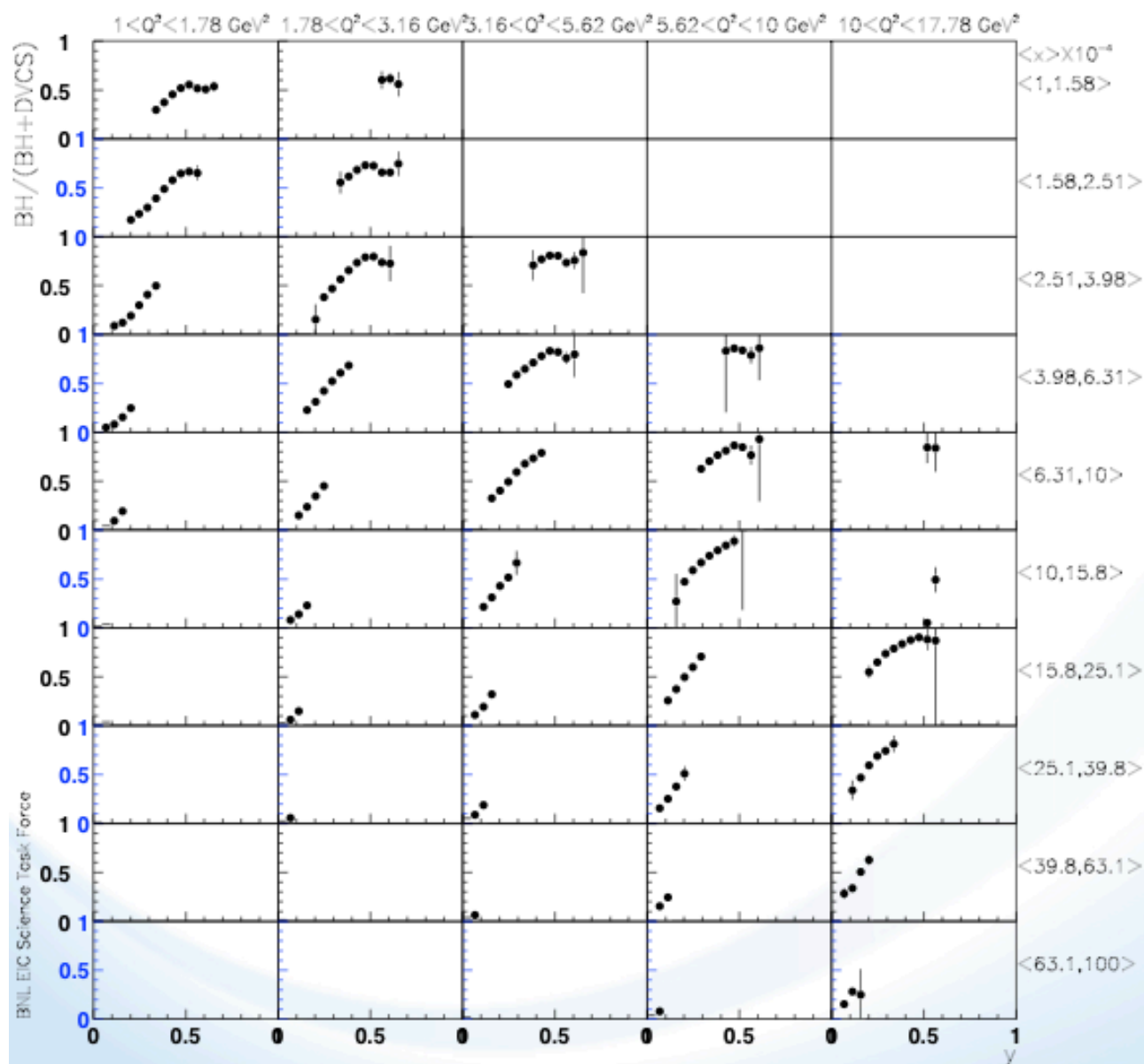


Figure 2: $P_B * P_T$ extracted using the A_{LL} as a function of t from EG1 data.

EIC: *MAGNITUDE OF BH CROSS SECTION*

20 X 250



in bins....

$$0.01 < y < 0.6$$

$$0.01 < |t| < 1.0 \text{ GeV}^2$$

$$\Theta_{e1} - \Theta_{e2} > 0$$

$$\Theta_{e1} < \pi - 0.02$$

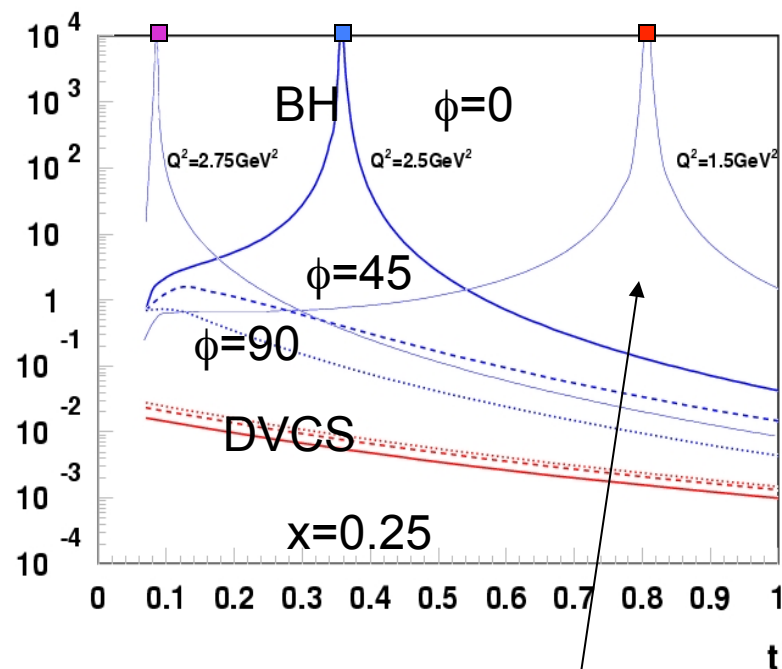
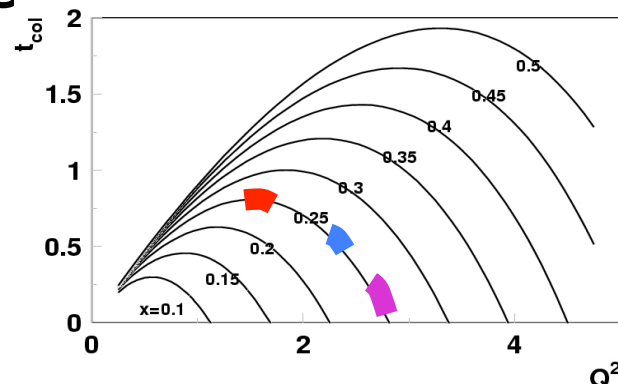
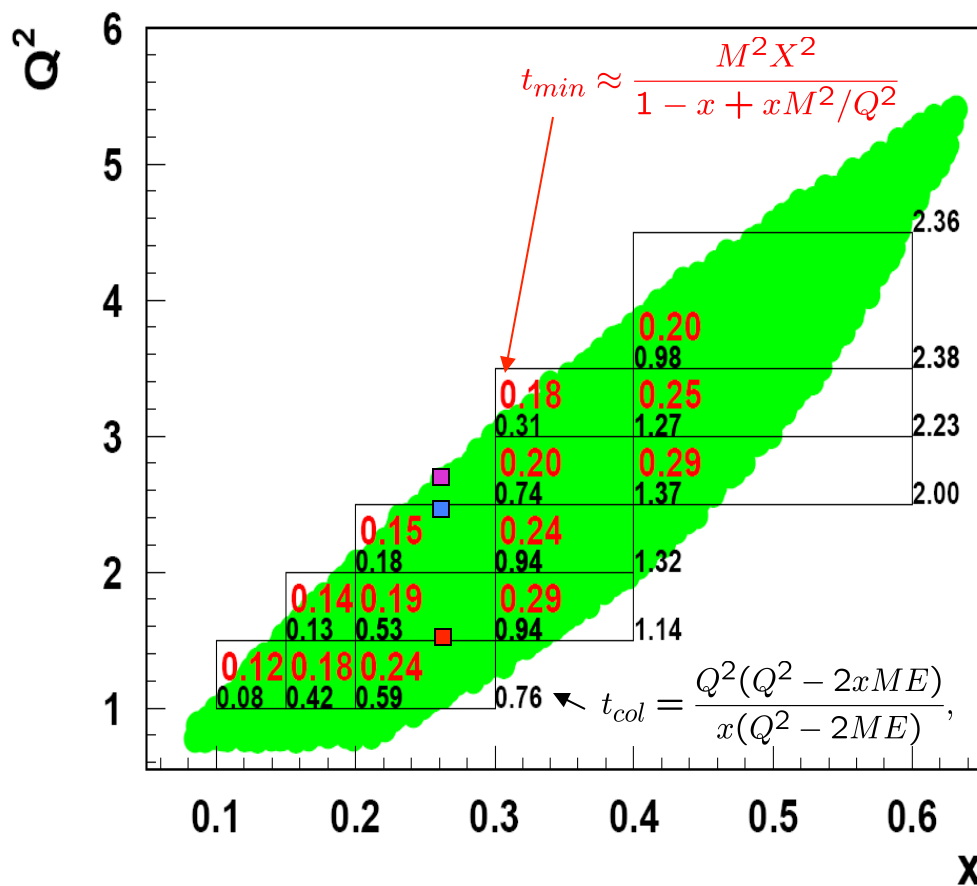
$$\Theta_{e2} < \pi - 0.02$$

$$E_{el} > 1 \text{ GeV}$$

$$E_{\gamma} > 1 \text{ GeV}$$

DVCS: BH propagators

$$\mathcal{I} = \frac{\pm e^6}{x_B y^3 \Delta^2 \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \left\{ c_0^{\mathcal{I}} + \sum_{n=1}^3 [c_n^{\mathcal{I}} \cos(n\phi) + s_n^{\mathcal{I}} \sin(n\phi)] \right\},$$



- Strong dependence on kinematics of prefactor ϕ -dependence, at $t=t_{col}$ $\mathcal{P}_1(\phi)=0$ require special attention in interpretation of beam averaged beam SSA and in particular x-section differences
- Fraction of pure DVCS increases with t and ϕ

ϕ -dependent amplitude

$$|T_{\text{BH}}|^2 = \frac{e^6}{x_{\text{B}}^2 y^2 (1 + \epsilon^2)^2 \Delta^2 \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \times \left\{ c_0^{\text{BH}} + \sum_{n=1}^2 c_n^{\text{BH}} \cos(n\phi) + s_1^{\text{BH}} \sin(\phi) \right\}$$

C_{BH}

$$|T_{\text{DVCS}}|^2 = \frac{e^6}{y^2 Q^2} \left\{ c_0^{\text{DVCS}} + \sum_{n=1}^2 \left[c_n^{\text{DVCS}} \cos(n\phi) + s_n^{\text{DVCS}} \sin(n\phi) \right] \right\}$$

$$\mathcal{P}_1 = -\frac{1}{y(1 + \epsilon^2)} \left\{ J + 2K \cos(\phi) \right\}$$

kinematic factors

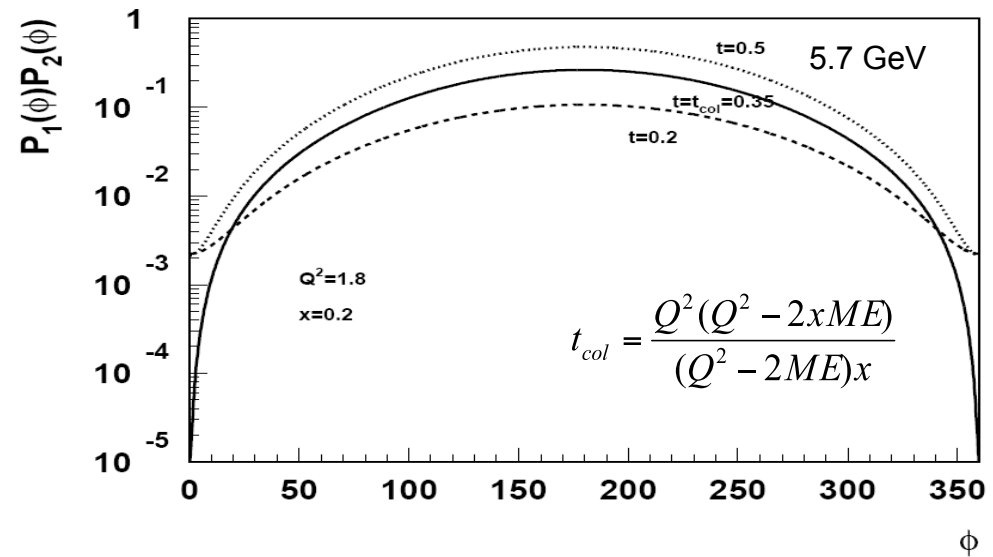
$$\mathcal{I} = \frac{\pm e^6}{x_{\text{B}} y^3 \Delta^2 \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \left\{ c_0^{\mathcal{I}} + \sum_{n=1}^3 \left[c_n^{\mathcal{I}} \cos(n\phi) + s_n^{\mathcal{I}} \sin(n\phi) \right] \right\},$$

$$J = \left(1 - y - \frac{y\epsilon^2}{2} \right) \left(1 + \frac{\Delta^2}{Q^2} \right) - (1 - x)(2 - y) \frac{\Delta^2}{Q^2}$$

C_{Int}

$$A_{\text{UL}}(\phi) \sim \frac{s_{1,\text{LP}}^{\mathcal{I}} \sin \phi}{c_{0,\text{unp}}^{\text{BH}} + (c_{1,\text{unp}}^{\text{BH}} + c_{1,\text{unp}}^{\mathcal{I}} + \dots) \cos \phi + \dots}$$

$$C_{\text{Int}} = C_{\text{BH}} * x/y * (1 + \epsilon^2)^2$$

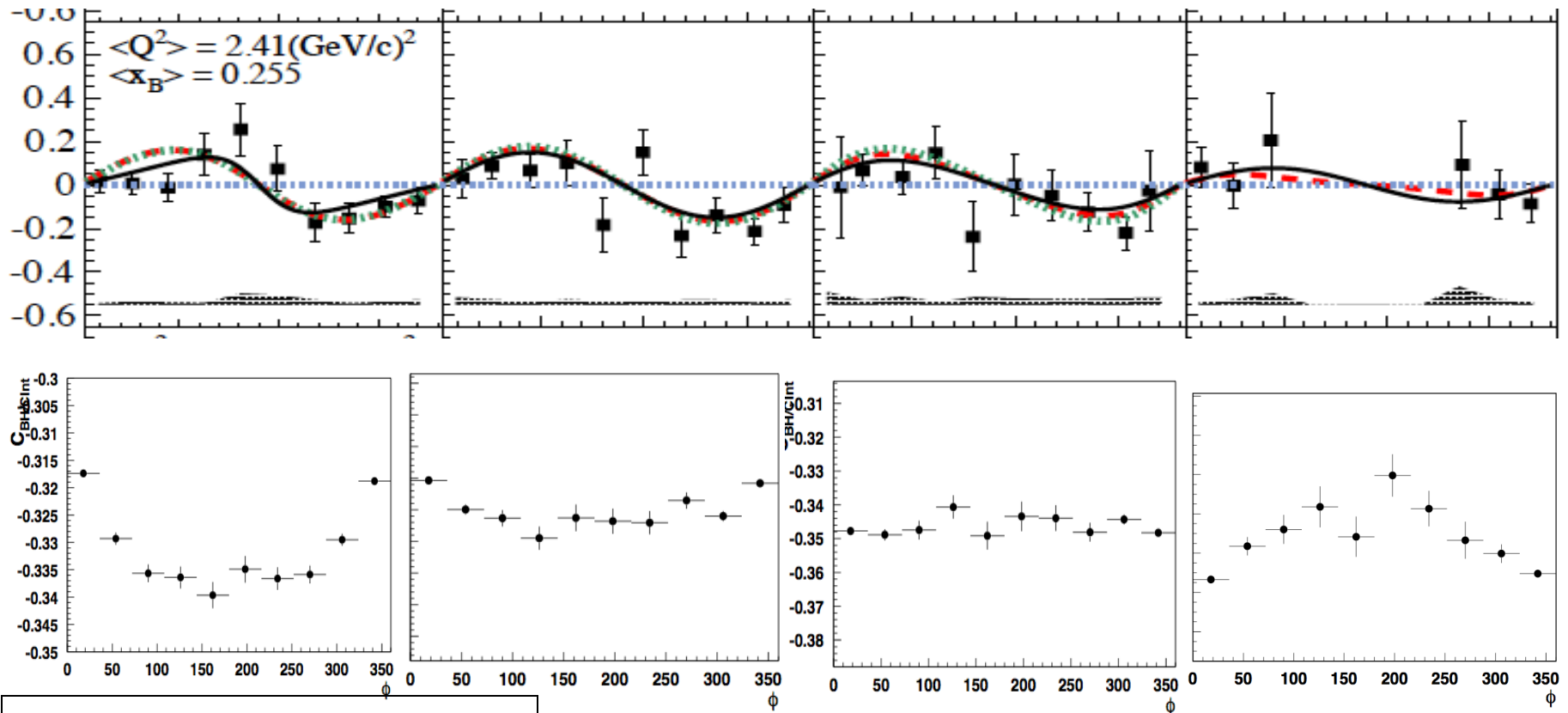


- Strong dependence on kinematics of prefactor ϕ -dependence, at $t \approx t_{\text{col}}$, $P_1(\phi) \rightarrow 0$
- Do the kinematic factors with propagators in T_{BH} and \mathcal{I} cancel in the ratio of

ϕ -dependent amplitude

Bin	x_B bin	θ_e bin	$\langle x_B \rangle$	$\langle Q^2 \rangle ((\text{GeV}/c)^2)$
1	$0.1 < x_B < 0.2$	$15^\circ < \theta_e < 48^\circ$	0.179	1.52
2	$0.2 < x_B < 0.3$	$15^\circ < \theta_e < 34^\circ$	0.255	1.97
3	$0.2 < x_B < 0.3$	$34^\circ < \theta_e < 48^\circ$	0.255	2.41
4	$0.3 < x_B < 0.4$	$15^\circ < \theta_e < 45^\circ$	0.345	2.60
5	$x_B > 0.4$	$15^\circ < \theta_e < 45^\circ$	0.453	3.31

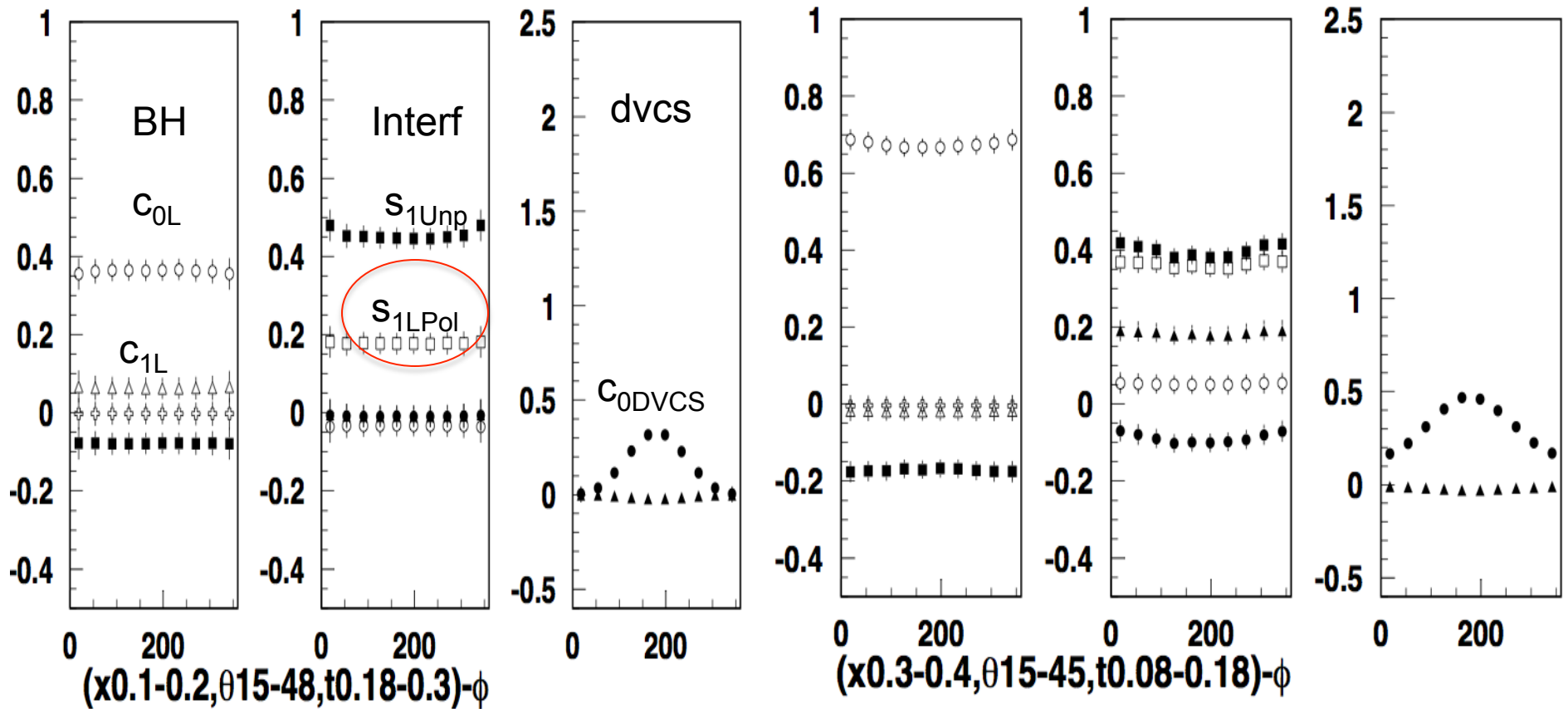
Bin	$-t$ range $(\text{GeV}/c)^2$	$\langle -t \rangle (\text{GeV}/c)^2$
1	$0.08 < -t < 0.18$	0.137
2	$0.18 < -t < 0.3$	0.234
3	$0.3 < -t < 0.7$	0.467
4	$0.7 < -t < 2.0$	1.175



•The ϕ -dependence of prefactor doesn't cancel: should be accounted in calculations

Azimuthal moments in $ep \rightarrow e'p'\gamma$

Ratio of different contributions to c_{0BH}



Different azimuthal moments become relevant in different kinematical regions

azimuthal moments in DVCS (example)

$$\mathcal{I} = \frac{\pm e^6}{x_B y^3 \mathcal{P}_1(\phi) \mathcal{P}_2(\phi) \Delta^2} \left\{ c_0^{\mathcal{I}} + \sum_{n=1}^3 [c_n^{\mathcal{I}} \cos(n\phi) + s_n^{\mathcal{I}} \sin(n\phi)] \right\},$$

$$\begin{Bmatrix} c_{1,\text{unp}}^{\mathcal{I}} \\ s_{1,\text{unp}}^{\mathcal{I}} \end{Bmatrix} = 8K \begin{Bmatrix} -(2 - 2y + y^2) \\ \lambda y(2 - y) \end{Bmatrix} \begin{Bmatrix} \Re \\ \Im \end{Bmatrix} C_{\text{unp}}^{\mathcal{I}}(\mathcal{F}),$$

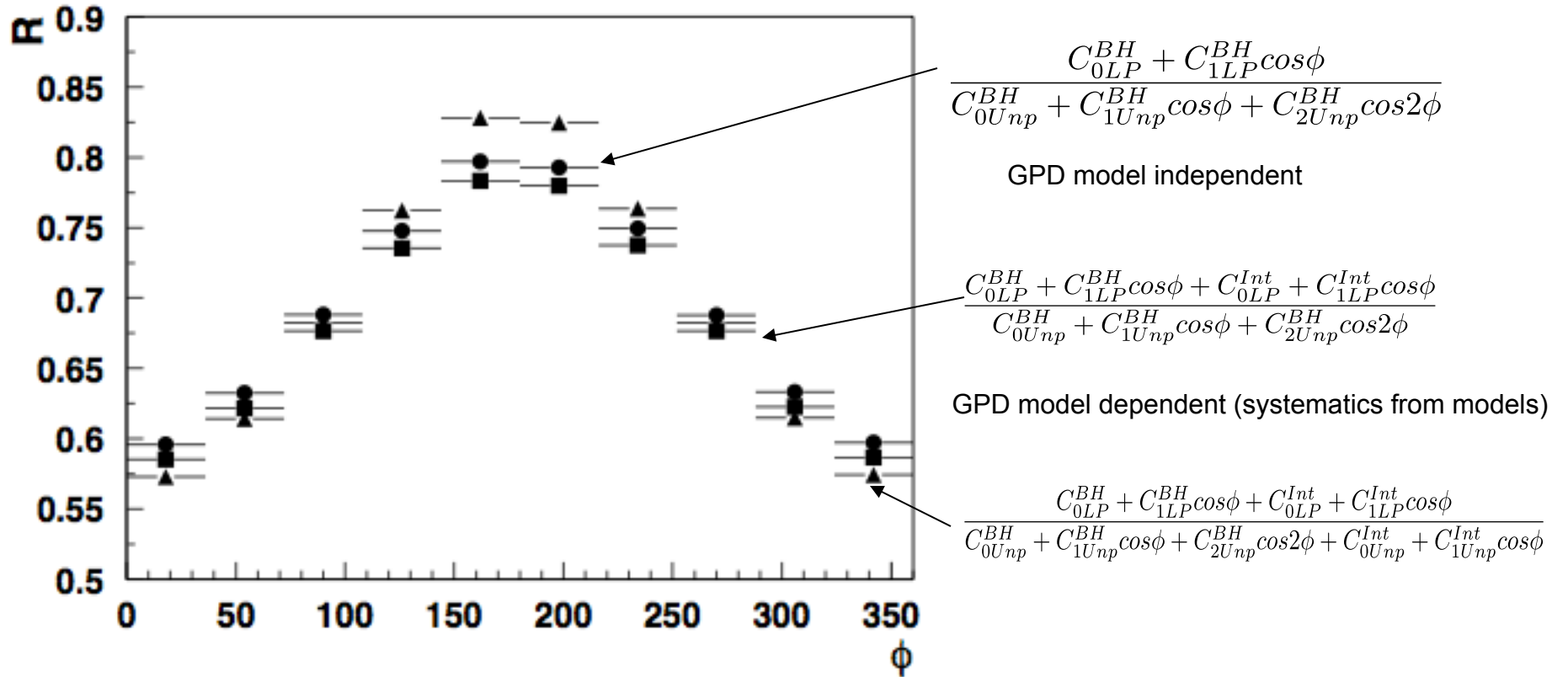
$$C_{\text{LP}}^{\mathcal{I}} = \frac{x_B}{2 - x_B} (F_1 + F_2) \left(\mathcal{H} + \frac{x_B}{2} \mathcal{E} \right) + F_1 \tilde{\mathcal{H}} - \frac{x_B}{2 - x_B} \left(\frac{x_B}{2} F_1 + \frac{\Delta^2}{4M^2} F_2 \right) \tilde{\mathcal{E}},$$

All moments involve several contributions with different Form Factors and GPDs multiplied by a kinematic term involving propagators

ϕ -dependent ratios (eg1dvcs paper)

Bin	x_B bin	θ_e bin	$\langle x_B \rangle$	$\langle Q^2 \rangle ((\text{GeV}/c)^2)$
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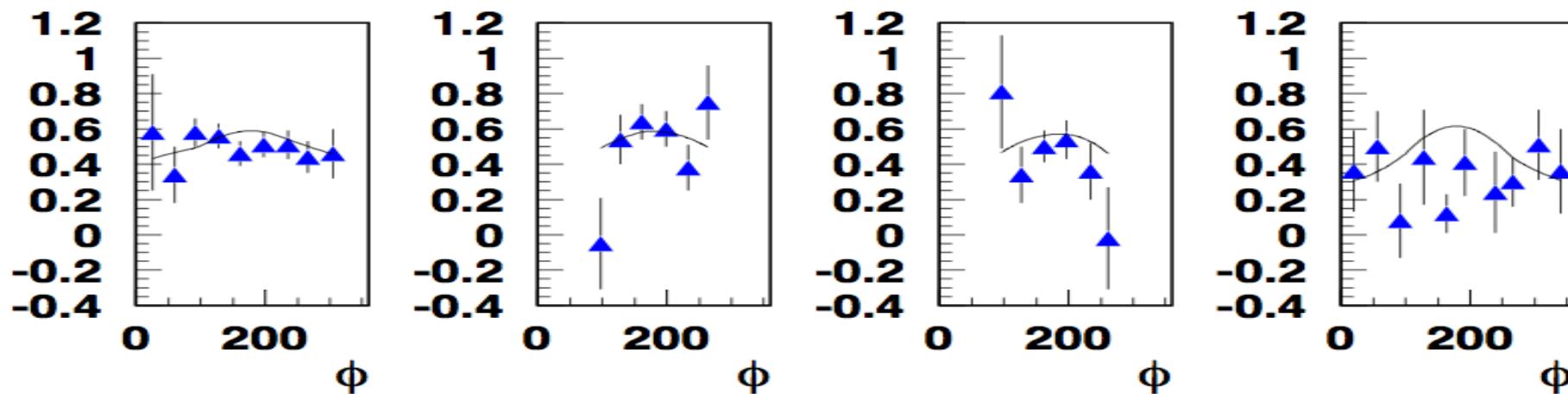
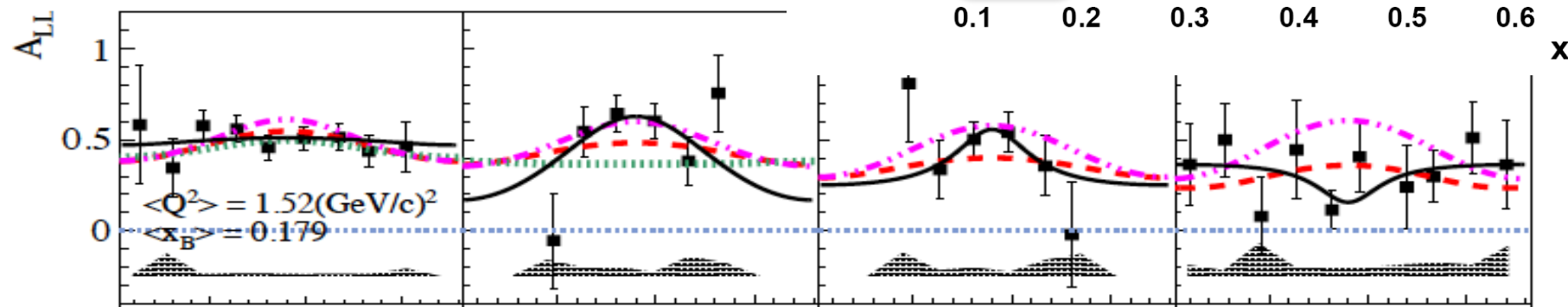
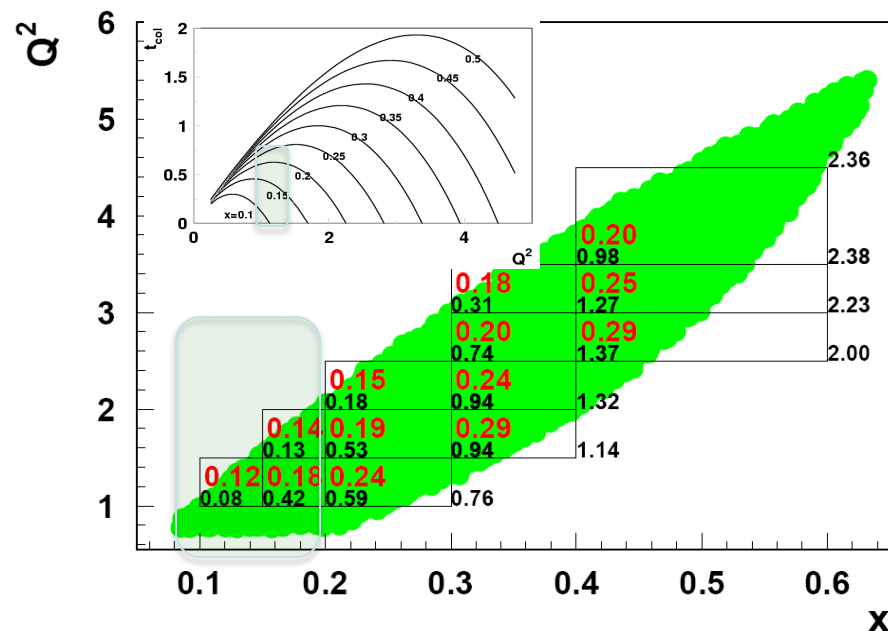
ϕ -dependent amplitude

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0.08

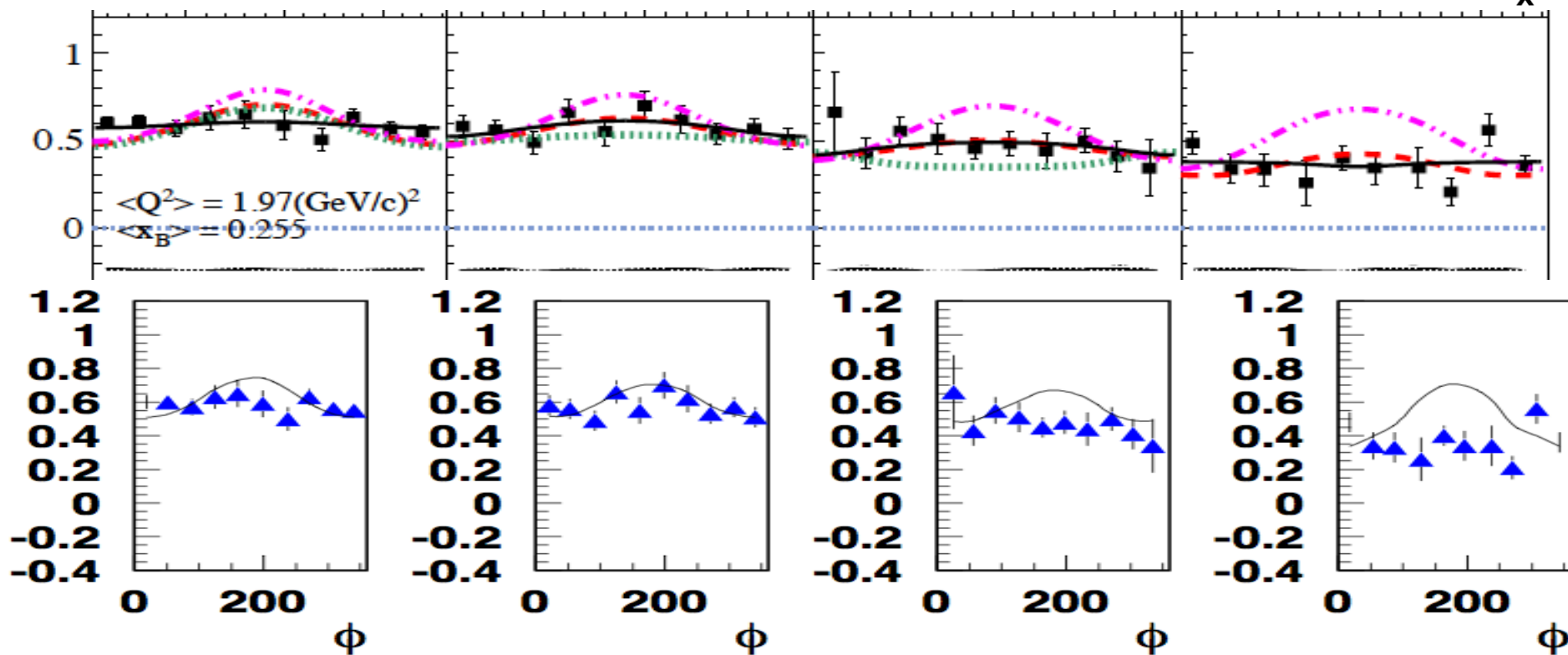
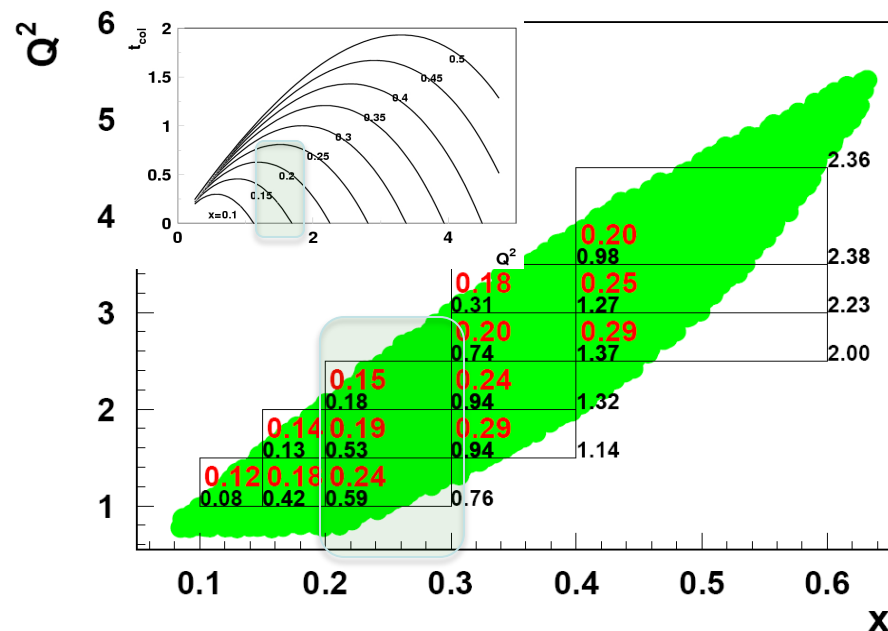
0.18



ϕ -dependent amplitude

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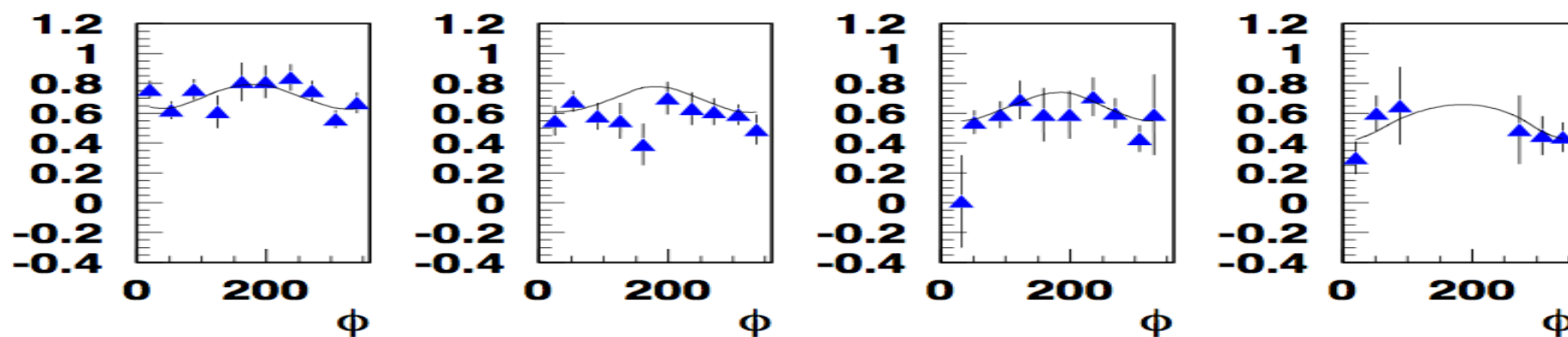
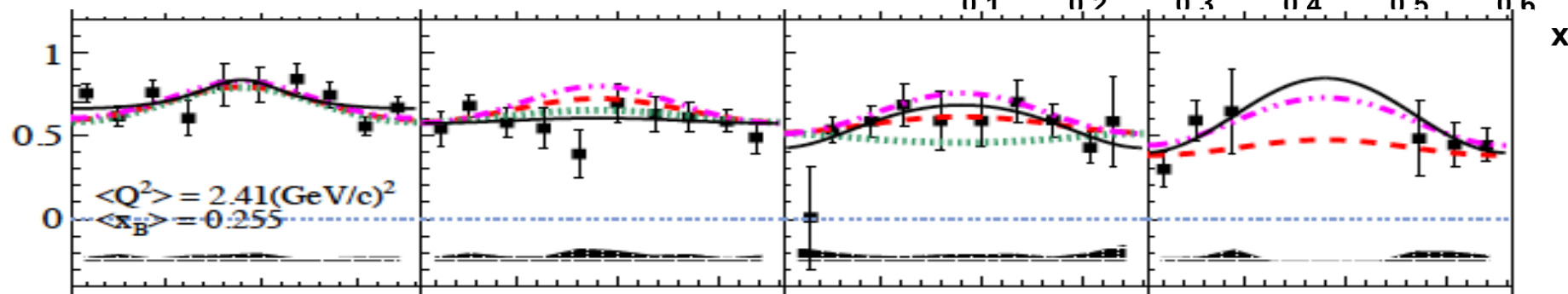
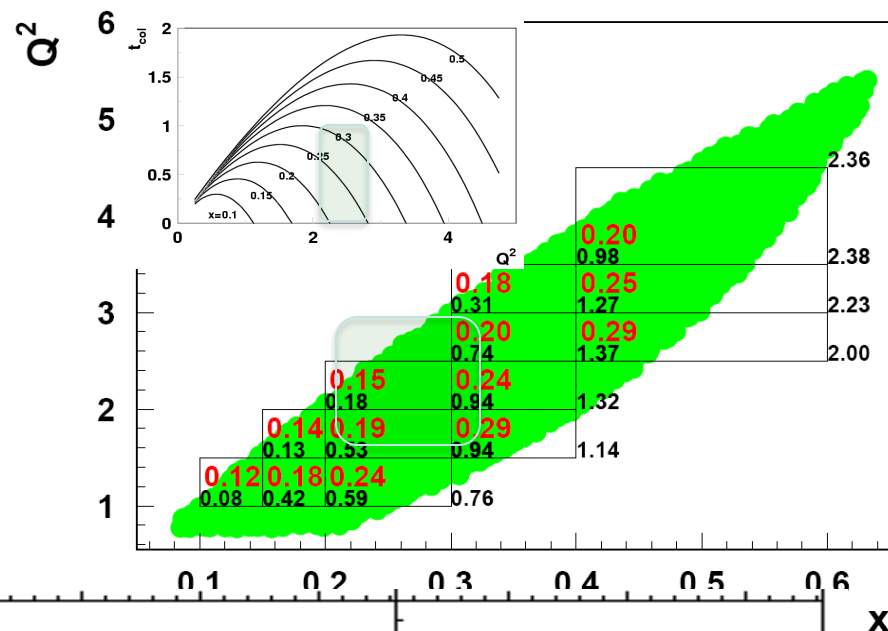
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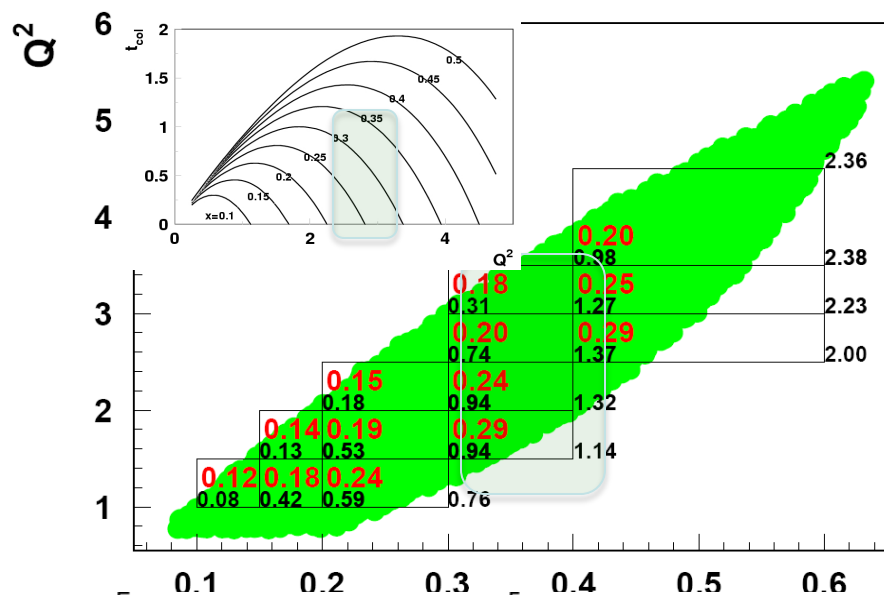
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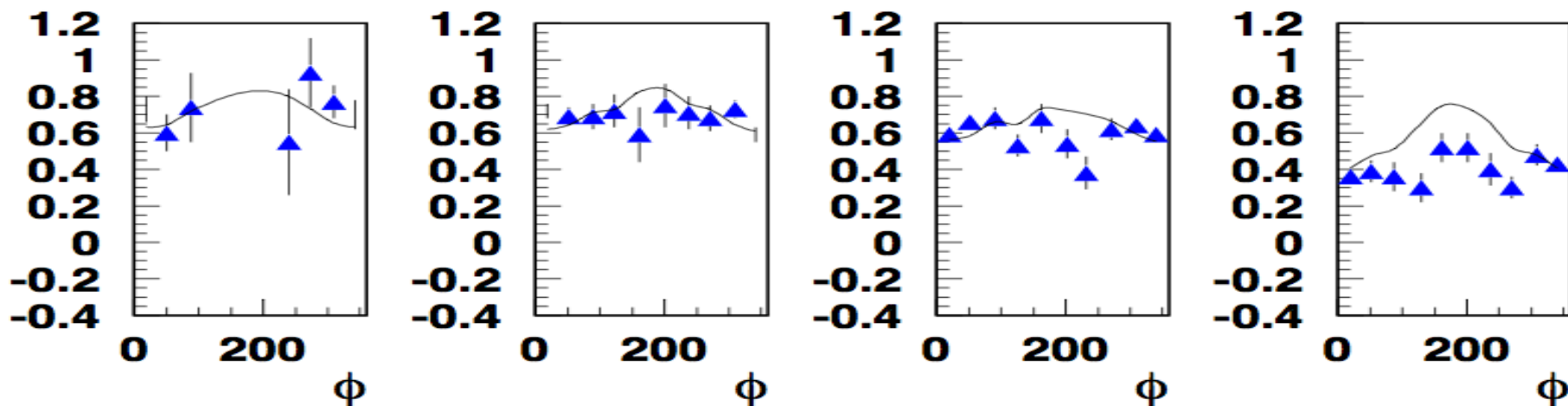
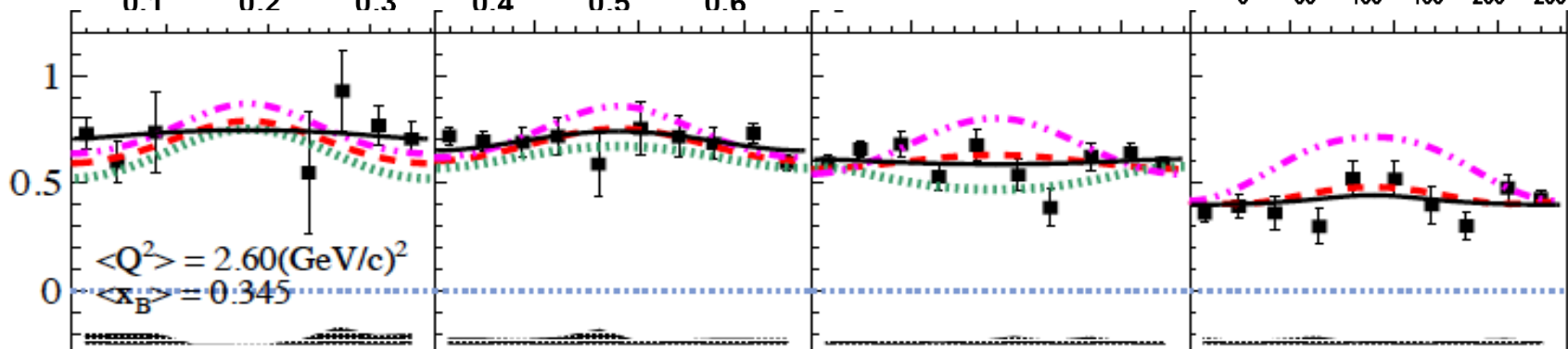
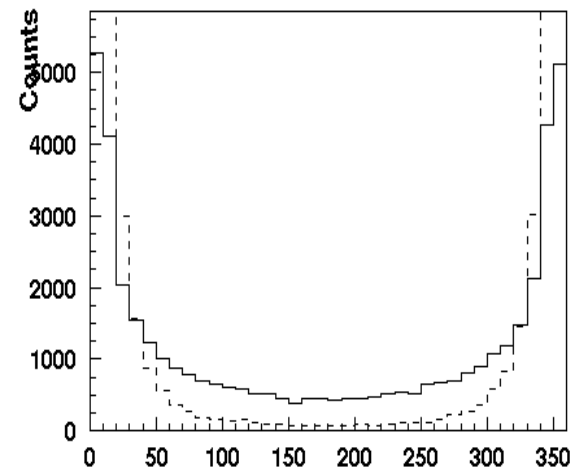
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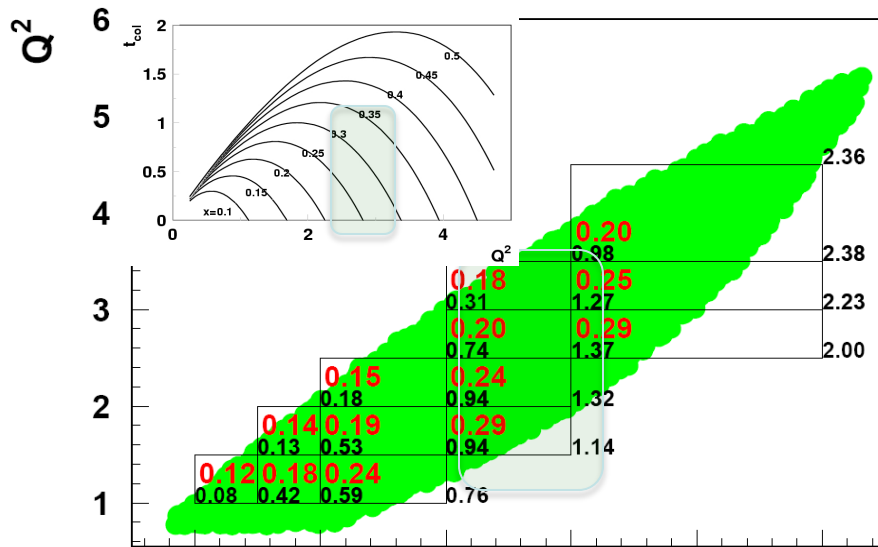
ϕ -dependent amplitude



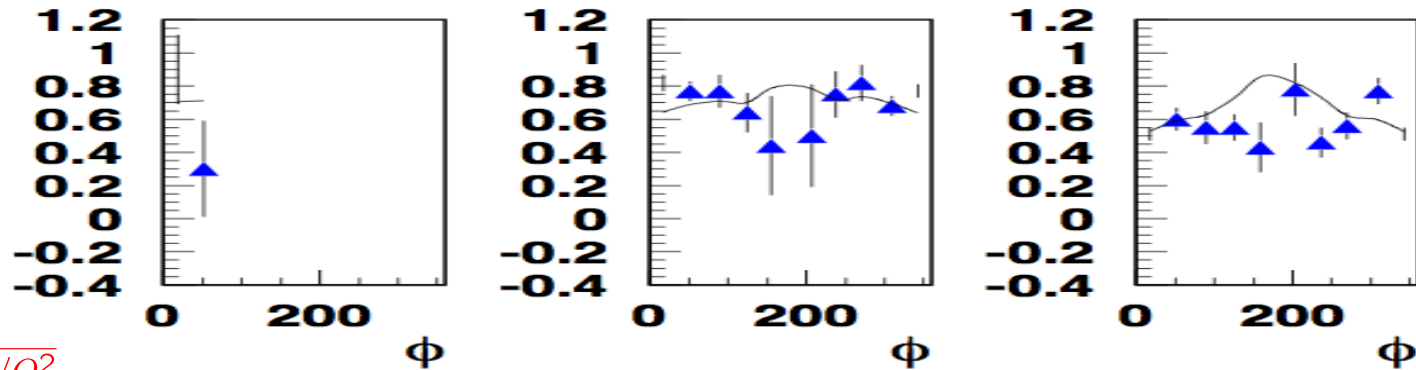
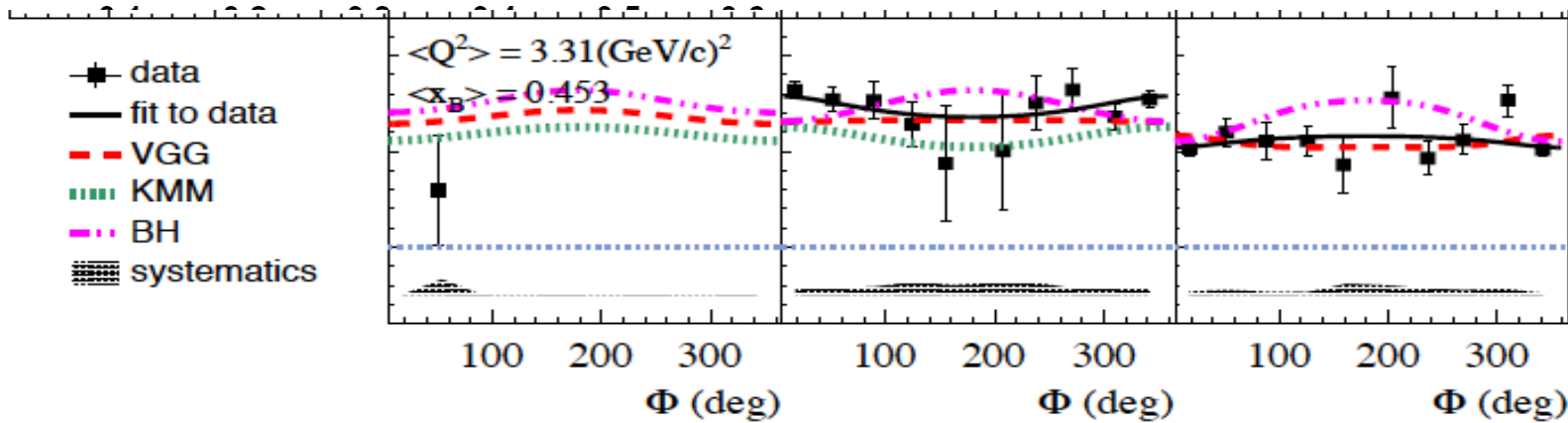
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ϕ -dependent amplitude

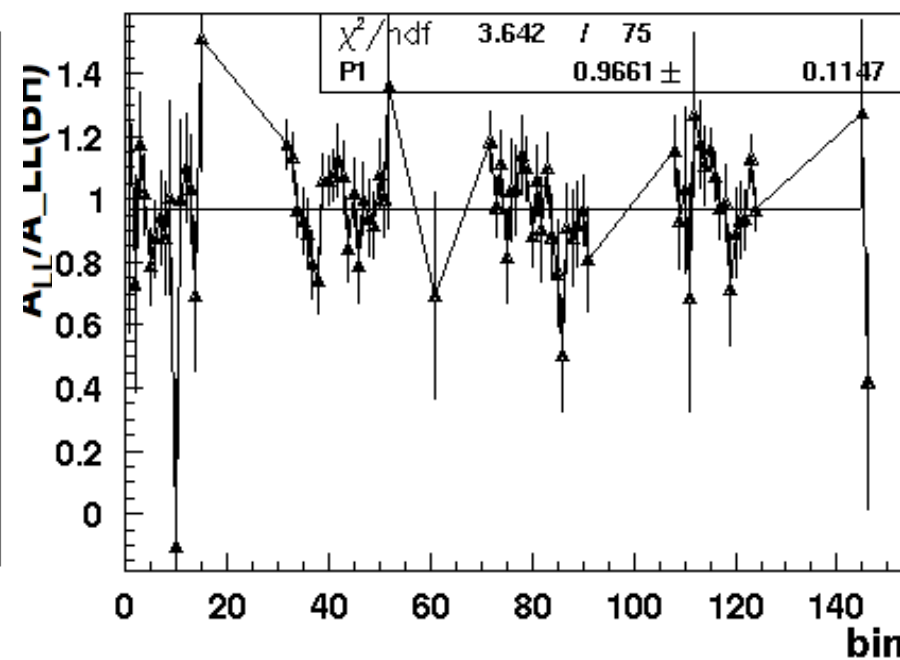
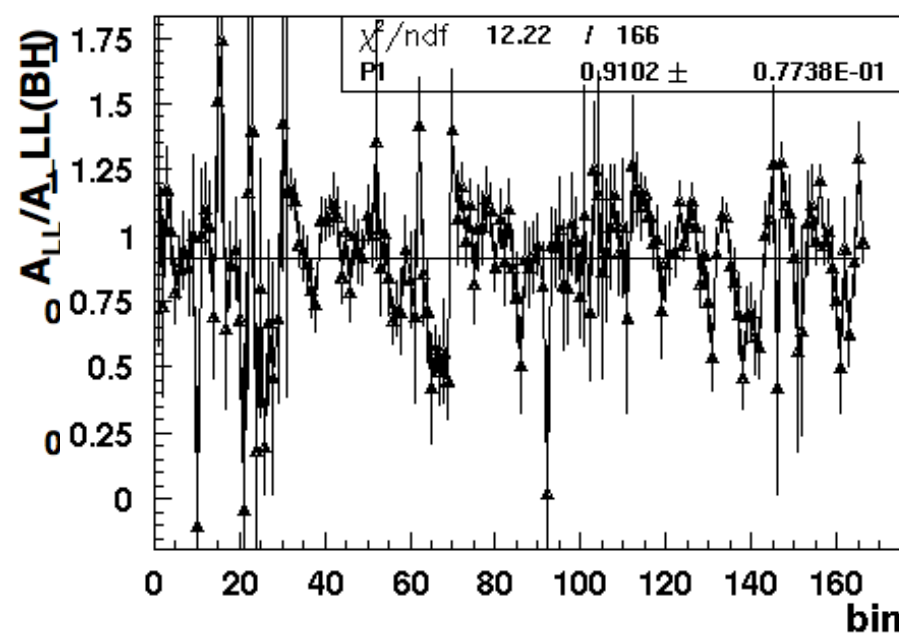
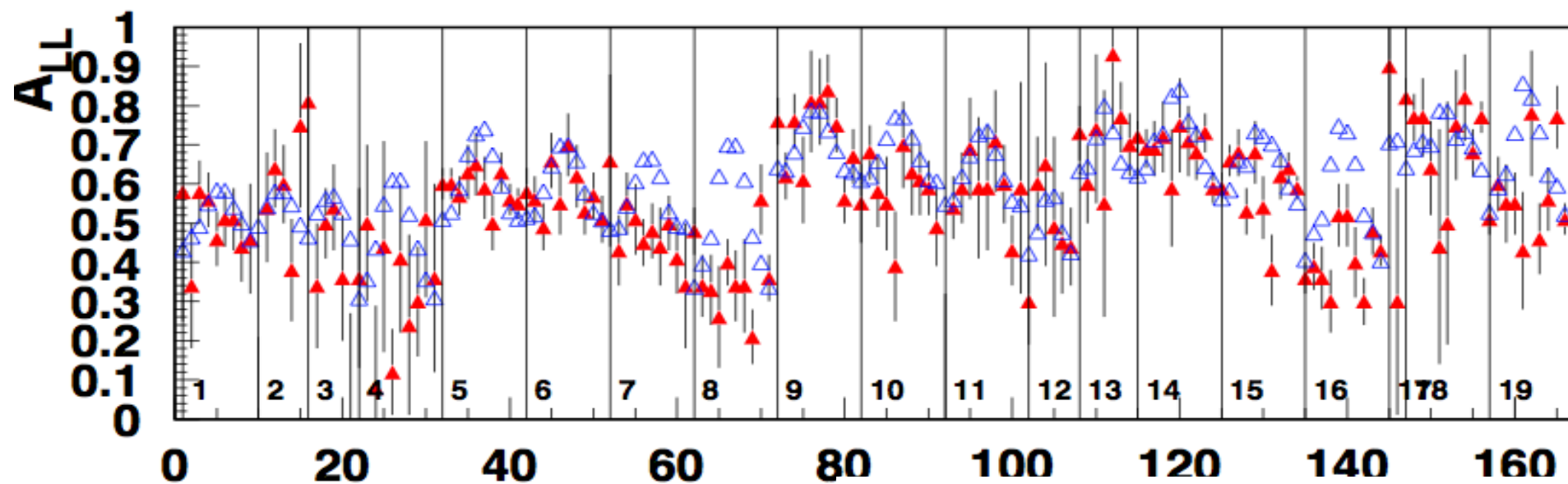


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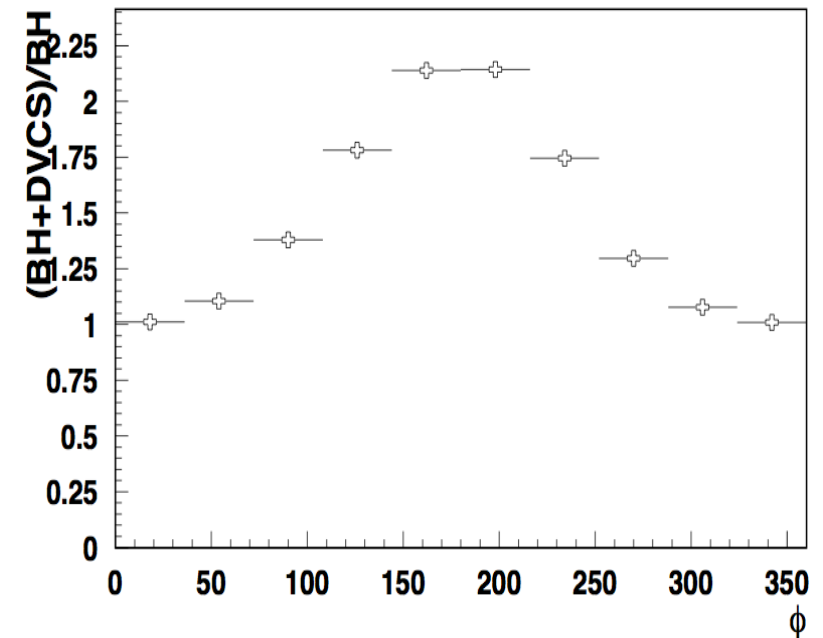
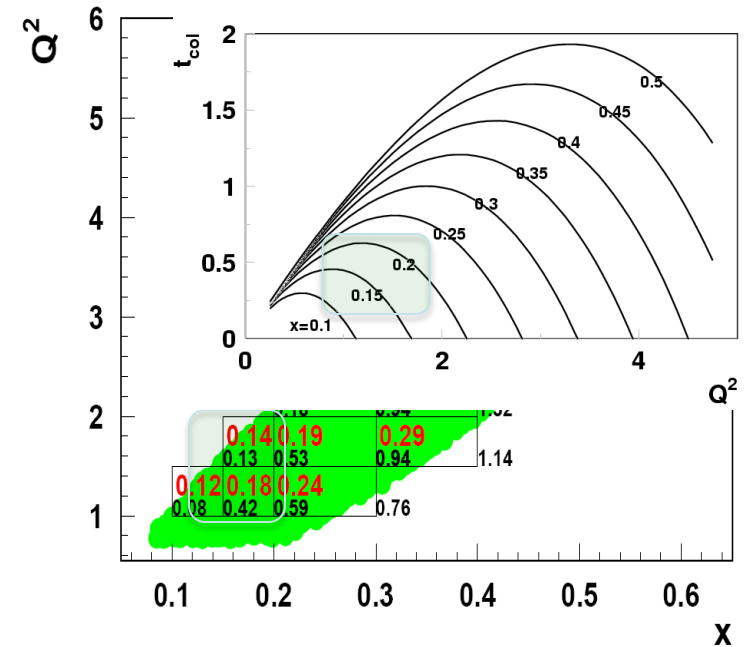
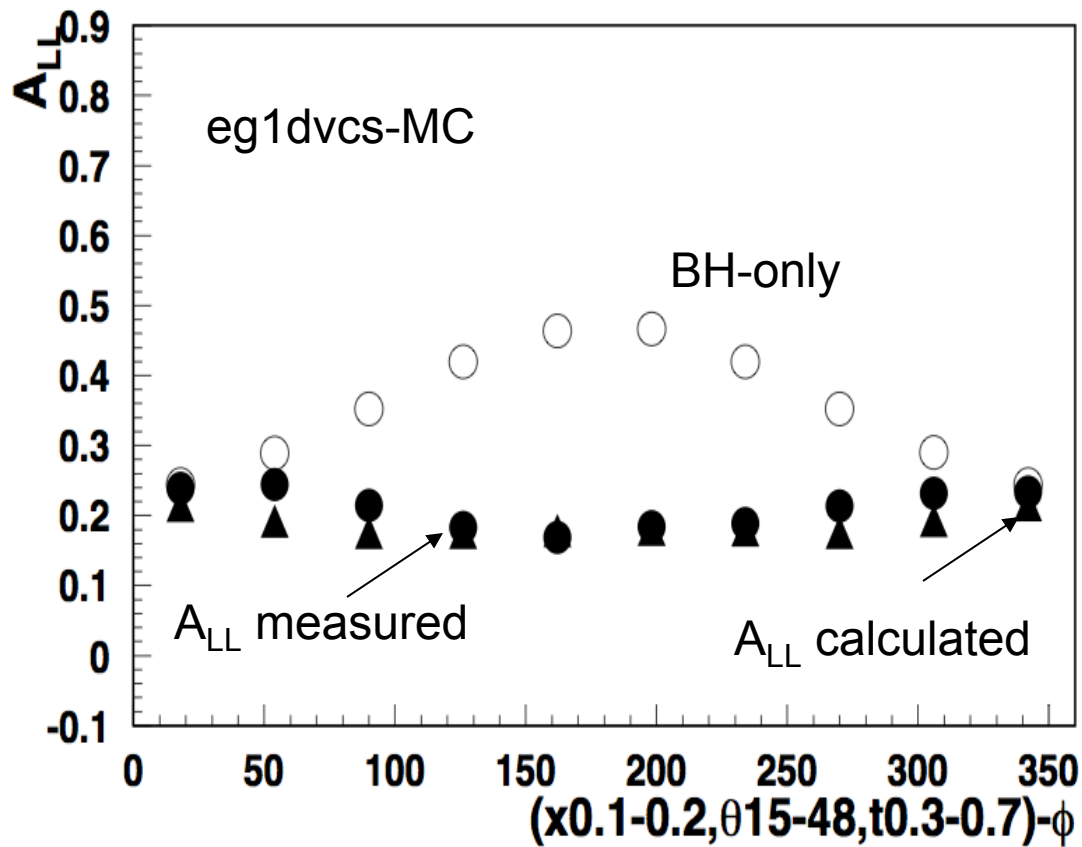


$$t_{min} \approx \frac{M^2 X^2}{1 - x + x M^2 / Q^2}$$

A_{LL} -data vs BH



MC studies: BH in A_{LL}



The A_{LL} ϕ -dependence dominated by BH only at relatively small ϕ

ϕ -dependent ratios (eg1dvcs paper)

Bin	x_B bin	θ_e bin	$\langle x_B \rangle$	$\langle Q^2 \rangle ((\text{GeV}/c)^2)$
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GPD model independent

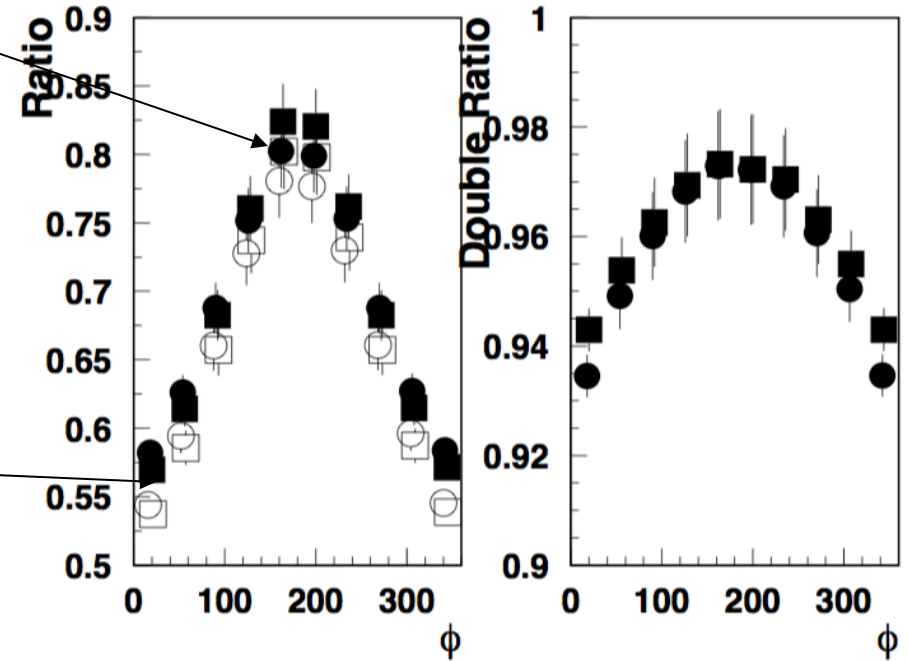
$$\frac{C_{0LP}^{BH} + C_{1LP}^{BH} \cos \phi}{C_{0Unp}^{BH} + C_{1Unp}^{BH} \cos \phi + C_{2Unp}^{BH} \cos 2\phi}$$

GPD model dependent (systematics from models)

$$\frac{C_{0LP}^{BH} + C_{1LP}^{BH} \cos \phi + C_{0LP}^{Int} + C_{1LP}^{Int} \cos \phi}{C_{0Unp}^{BH} + C_{1Unp}^{BH} \cos \phi + C_{2Unp}^{BH} \cos 2\phi + C_{0Unp}^{Int} + C_{1Unp}^{Int} \cos \phi}$$

Empty symbols correspond to **separate nominator and denominator calculations** and filled symbols to calculation of the ratio (right plot is for ratio)

$$|T_{BH}|^2 = \frac{e^6}{x_B^2 y^2 (1 + \epsilon^2)^2 \Delta^2 \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \times \left\{ c_0^{BH} + \sum_{n=1}^2 c_n^{BH} \cos(n\phi) + s_1^{BH} \sin(\phi) \right\}$$



• Difference ~5% from calculating as ratio of structure functions

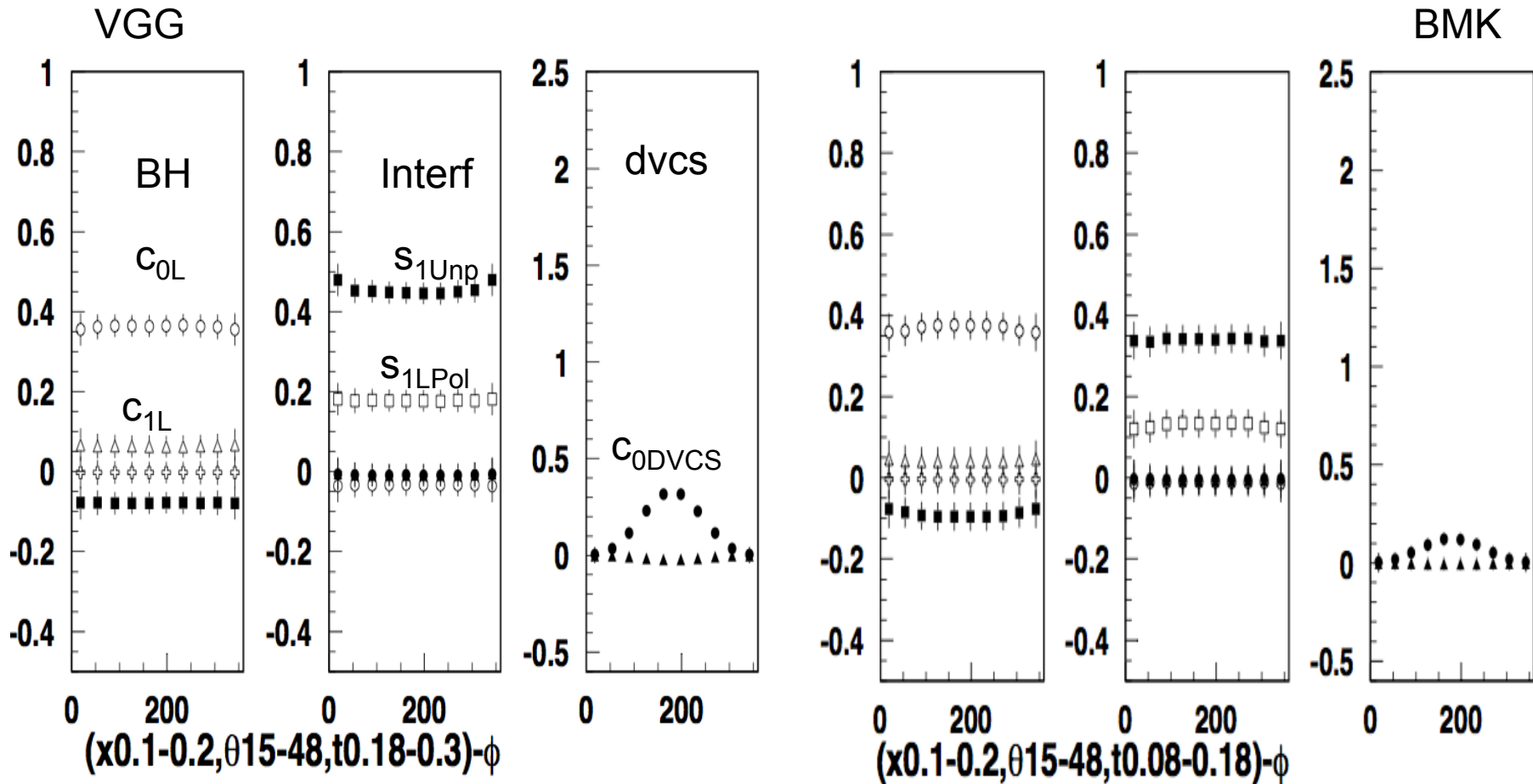
summary & plans

- Comparing with theory calculations should be done by integration over bins within the acceptance of numerator and denominator separately
- Smaller bins will reduce the systematics
- Compare the A_{LL} with calculations (eg1dvcs data) and develop procedure for extraction of the $P_B P_T$ from CLAS12/EIC
- Extract x-section differences for polarized case with and without asymmetries

support slides...

Azimuthal moments in $ep \rightarrow e'p'\gamma$

Ratio of different contributions to c_{0BH}



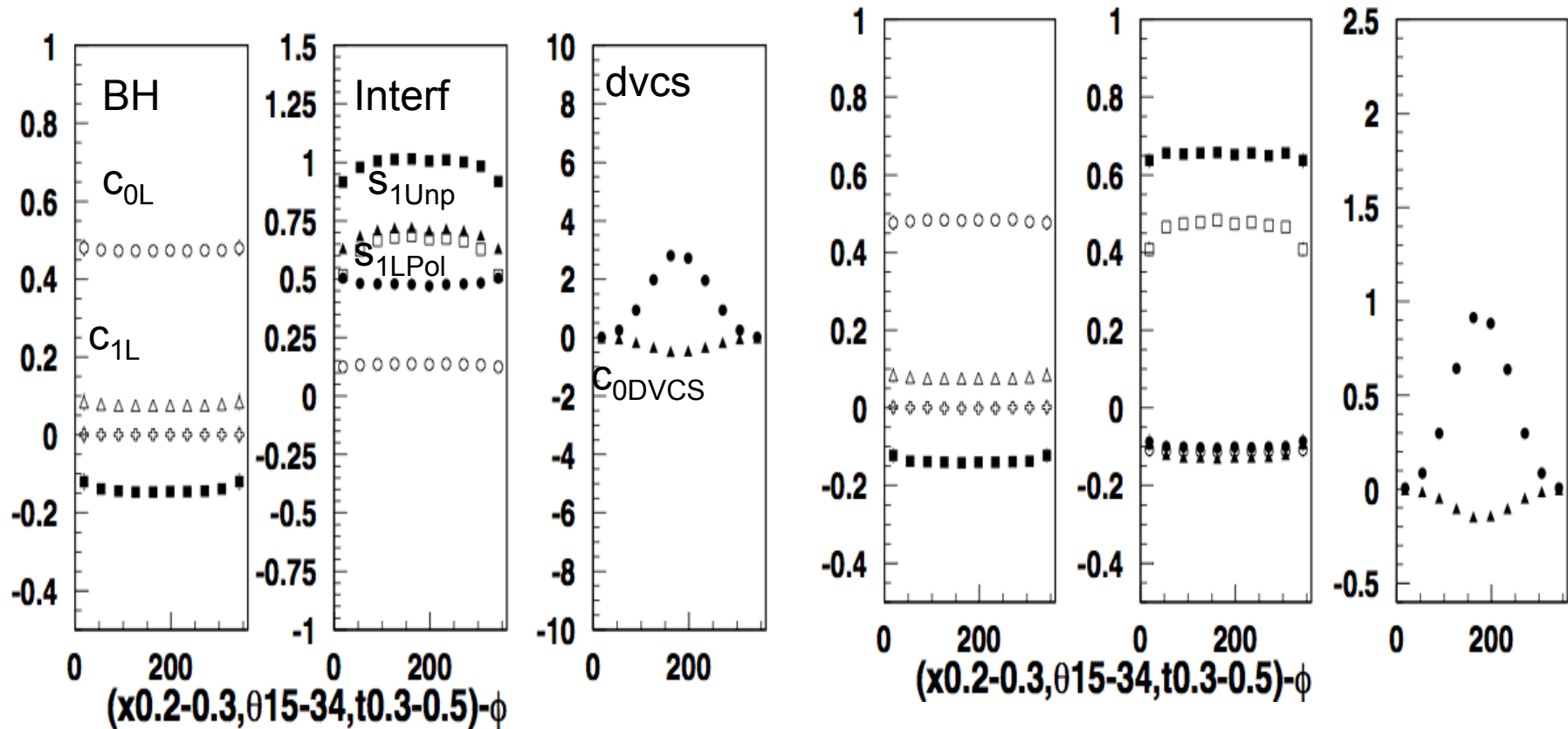
Different azimuthal moments become relevant in different kinematical regions

Azimuthal moments in $ep \rightarrow e'p'\gamma$

Ratio of different contributions to c_{0BH}

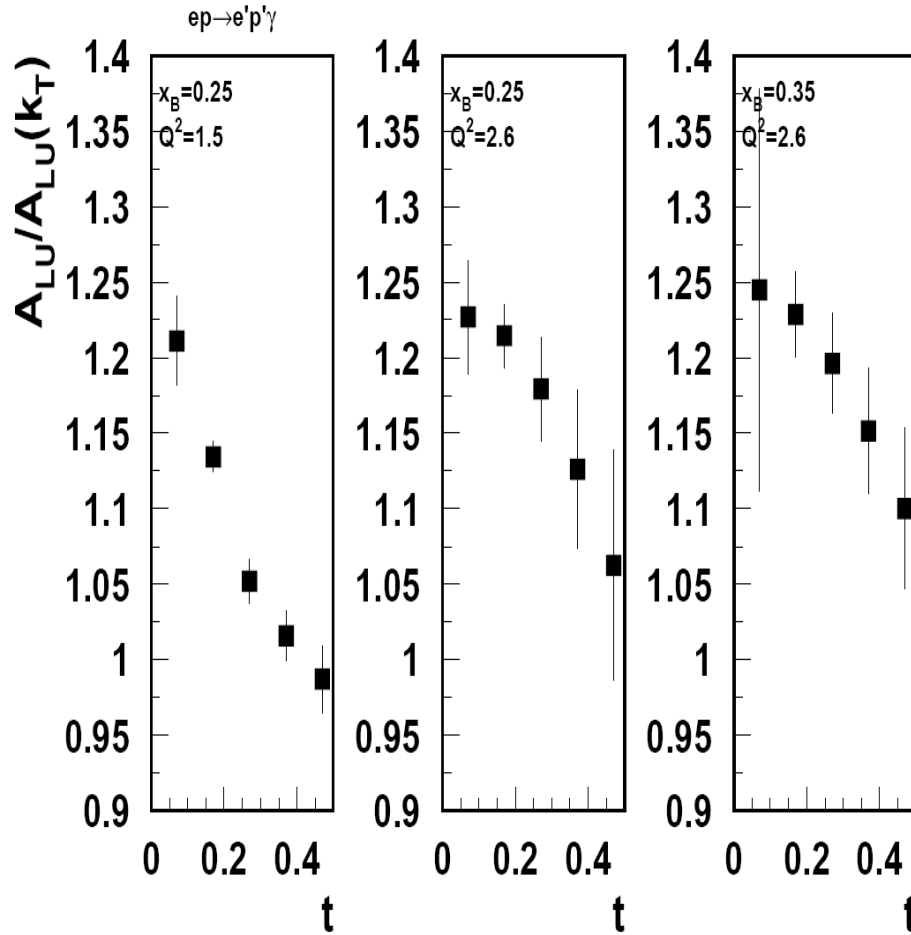
VGG

BMK

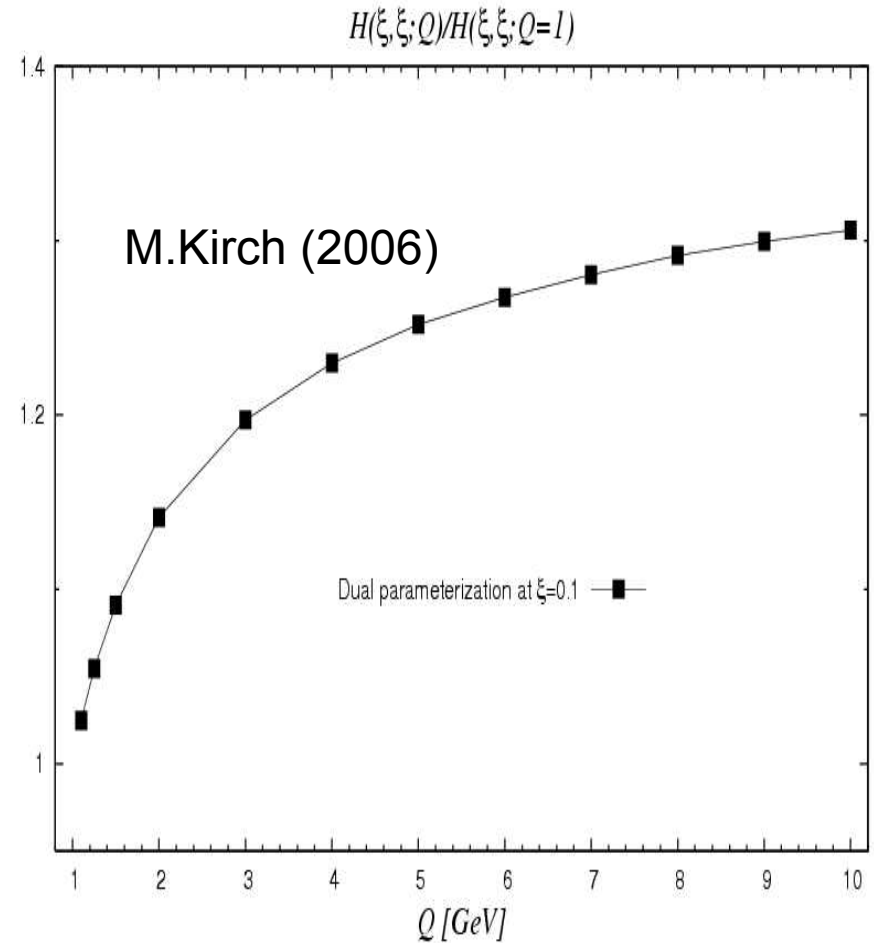


Different azimuthal moments become relevant in different kinematical regions

Sensitivity on theory input



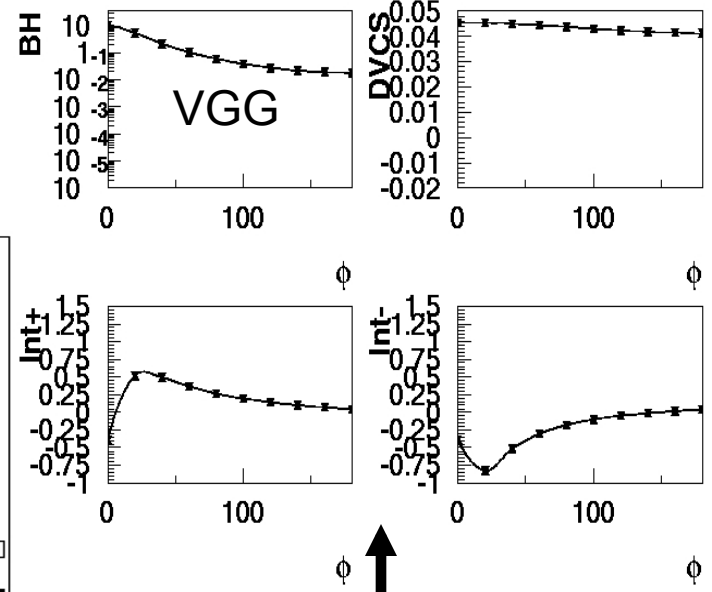
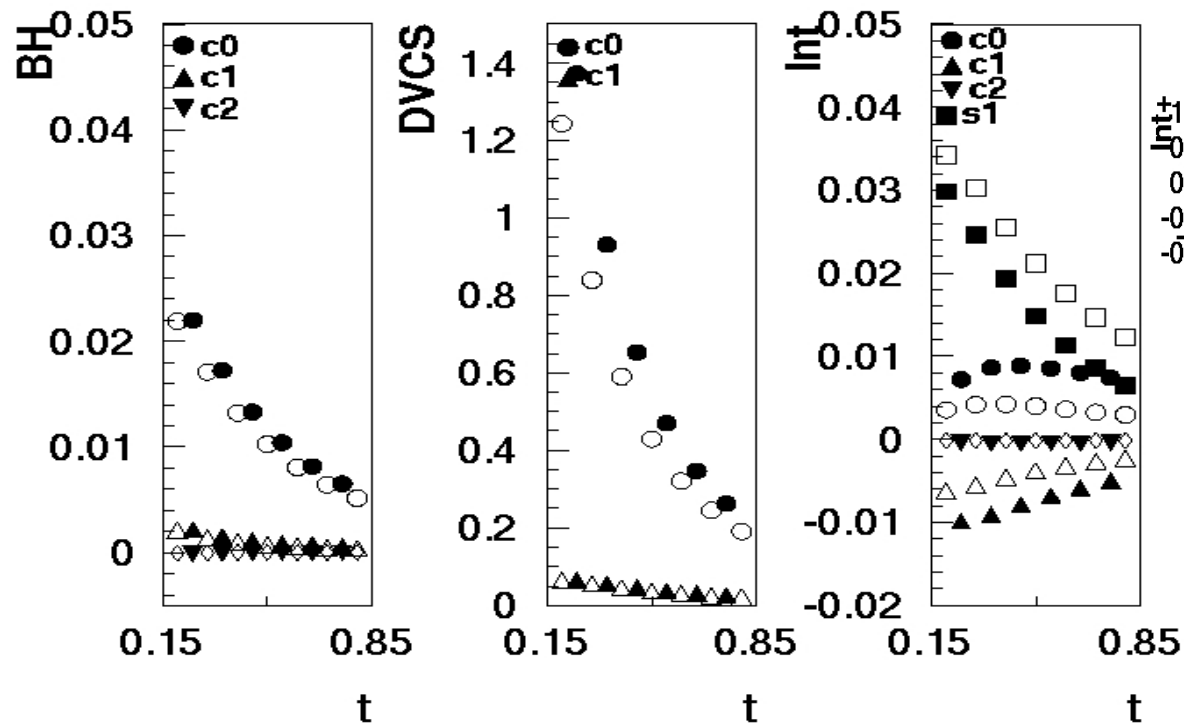
Dynamical HT may decrease the beam SSA at small t



Evolution effects significant at small **Q2**

Contributions to the DVCS cross section

	VGG	BMK
BH	exact	exact
Int	$BH_e \cdot DVCS_a$	$(BH \cdot DVCS)_a$



VGG x-section described as a sum of moments

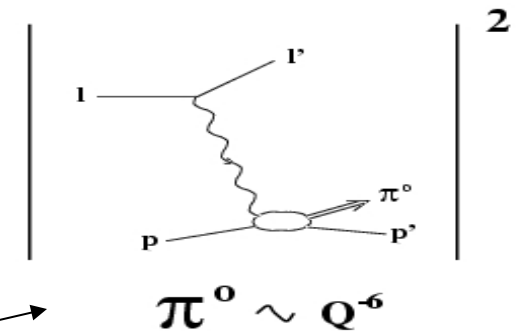
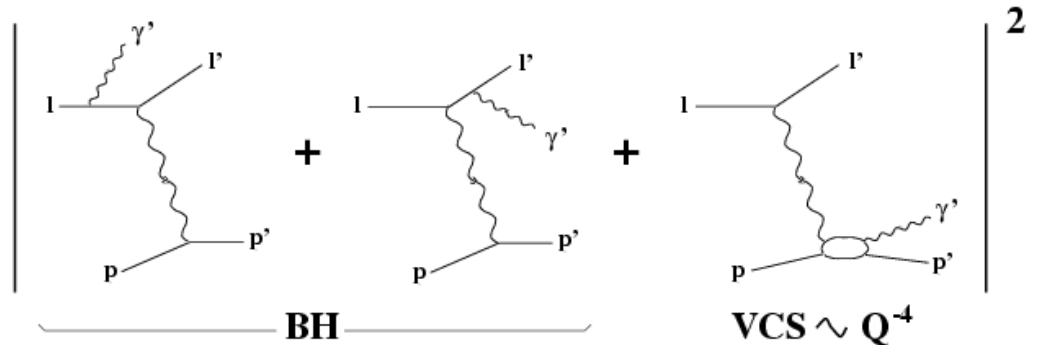
Reason for difference under studies (2002)

Azimuthal moments in the DVCS MC (BMK-open symbols) and Vanderhaeghen et al (filled symbols).

GPDs from $ep \rightarrow e'p'\gamma$

Requirements for precision
($<15\%$) measurements of
GPDs from DVCS SSA:

- Define the procedure to extract GPDs from A_{LU}
 - effect of finite bins (prefactor variations) $\sim 10\%$
 - other moments
- Define background corrections ($>1\gamma$)
 - pion contamination $\sim 10\%$
 - radiative background
 - ADVCS

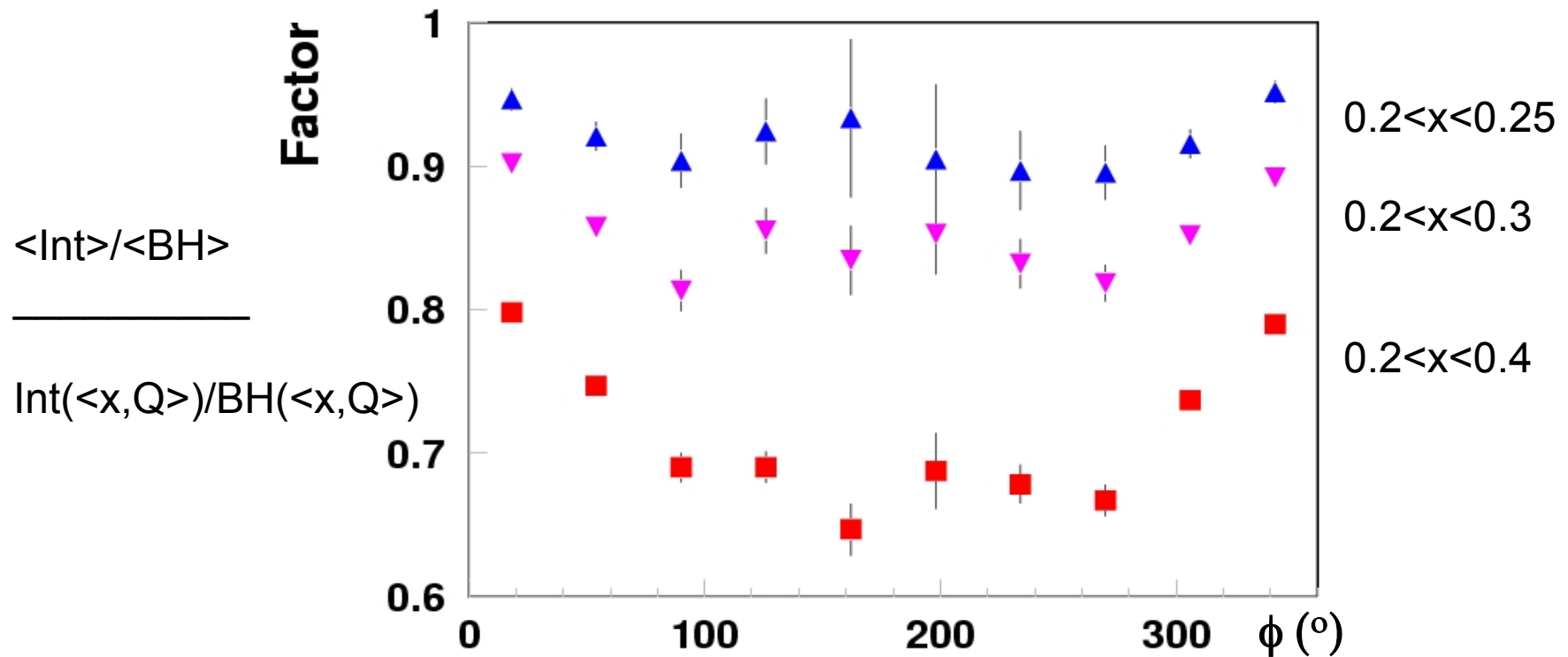


A complete simulation of the whole chain from particle detection to GPD extraction, including the DVCS and background (counts, asymmetries) as well as extraction procedure (averaging over kinematic factors) required to ensure the reliability of measured GPDs.

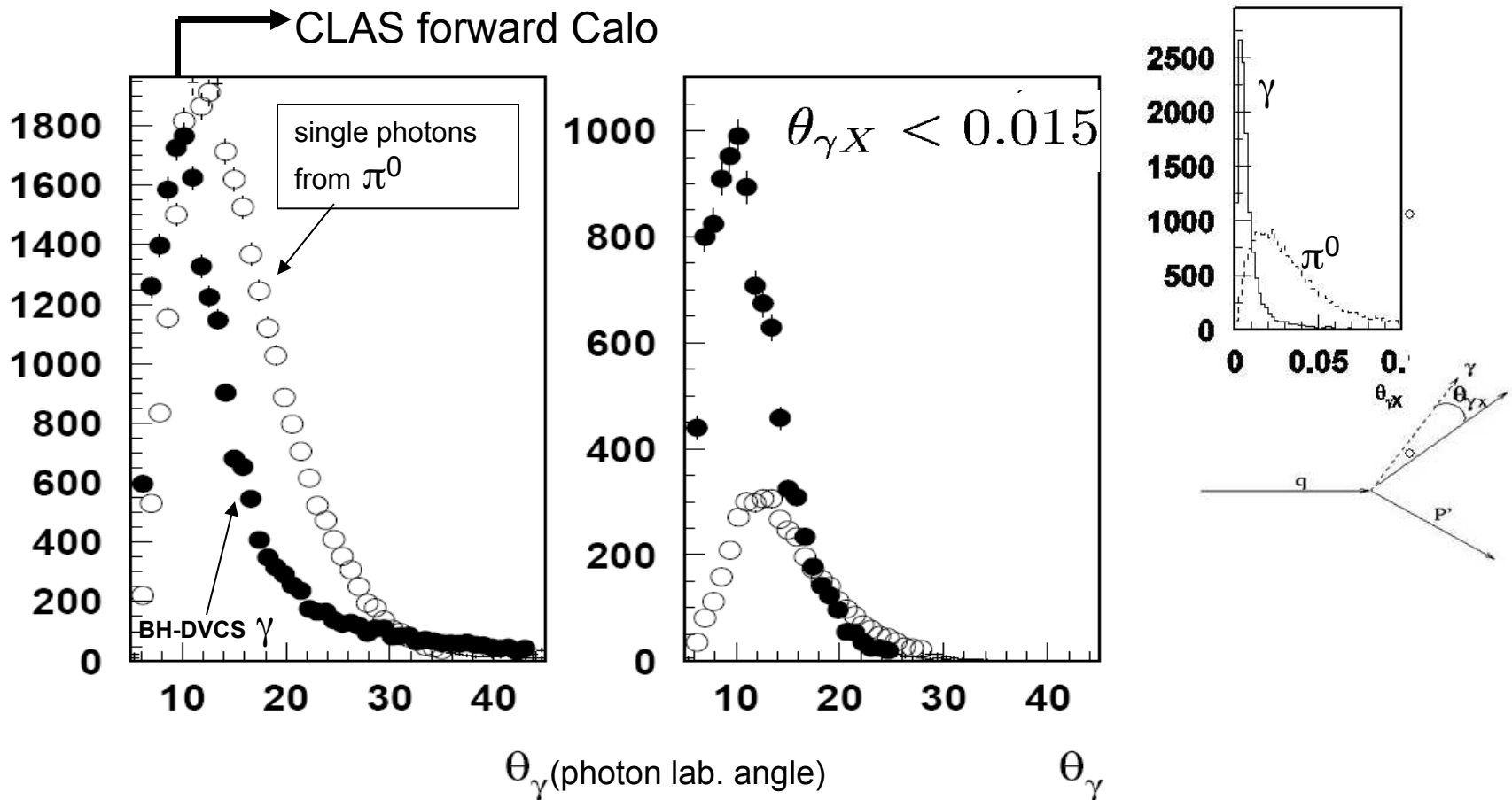
Correction factor as a function of bin size

ϕ – dependence of $\mathcal{P}_1 = -\frac{1}{y(1+\epsilon^2)} \{J + 2K \cos(\phi)\}$

in BH and INT terms doesn't cancel for finite bins



π^0 contamination in $ep\gamma$ -sample



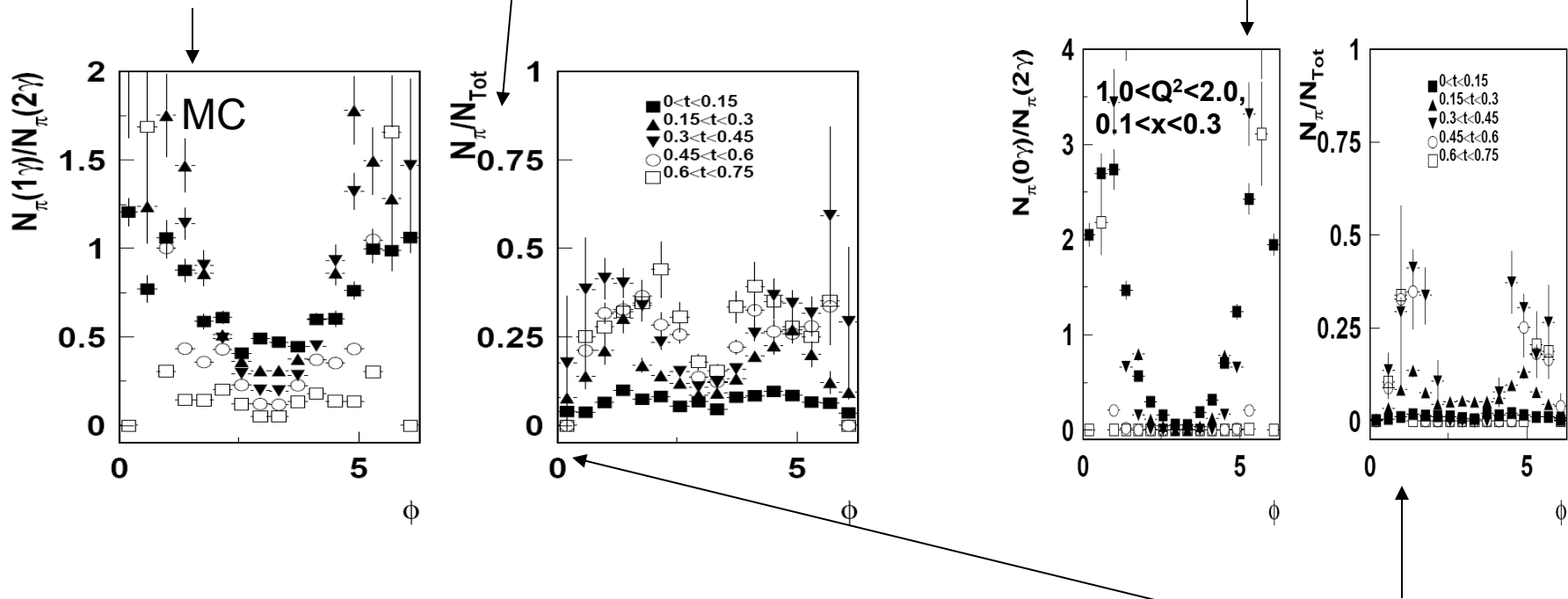
- At large angles detected photon can be used as veto (epX -sample).
- Cut on the direction of the measured photon (require detection of proton) significantly reduce the contamination ($ep\gamma$ -sample).

π^0 contamination

Main unknown in corrections of photon SSA are the π^0 contamination and its beam SSA.

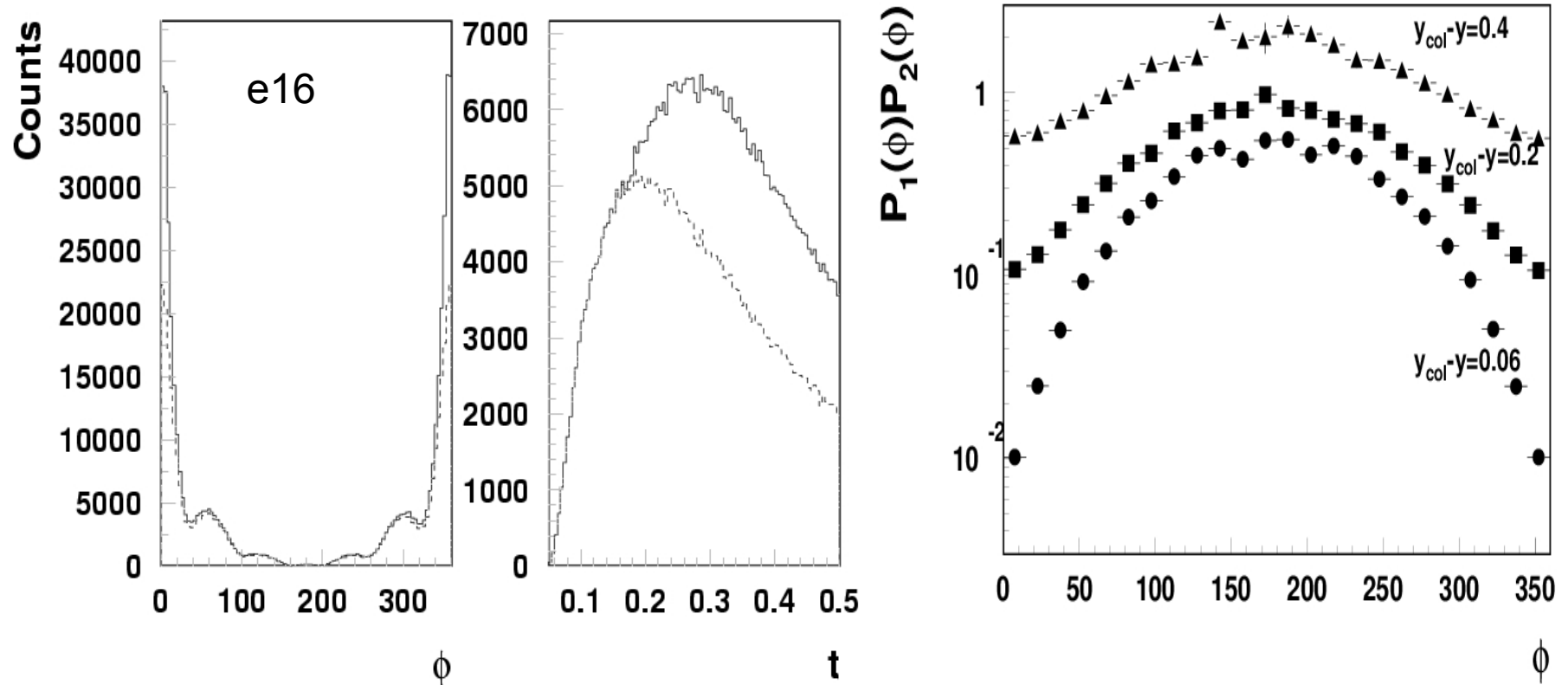
Extract from $e\pi^0$ MC the ratio of single to double photon detection probability

$$N_{\gamma}^{Data}(\pi^0) = N_{\pi^0}^{Data} \frac{N_{\gamma}^{MC}(\pi^0)}{N_{\pi^0}^{MC}},$$



Contamination from π^0 photons increasing at large t and x .

ϕ -dependence and collinearity cut

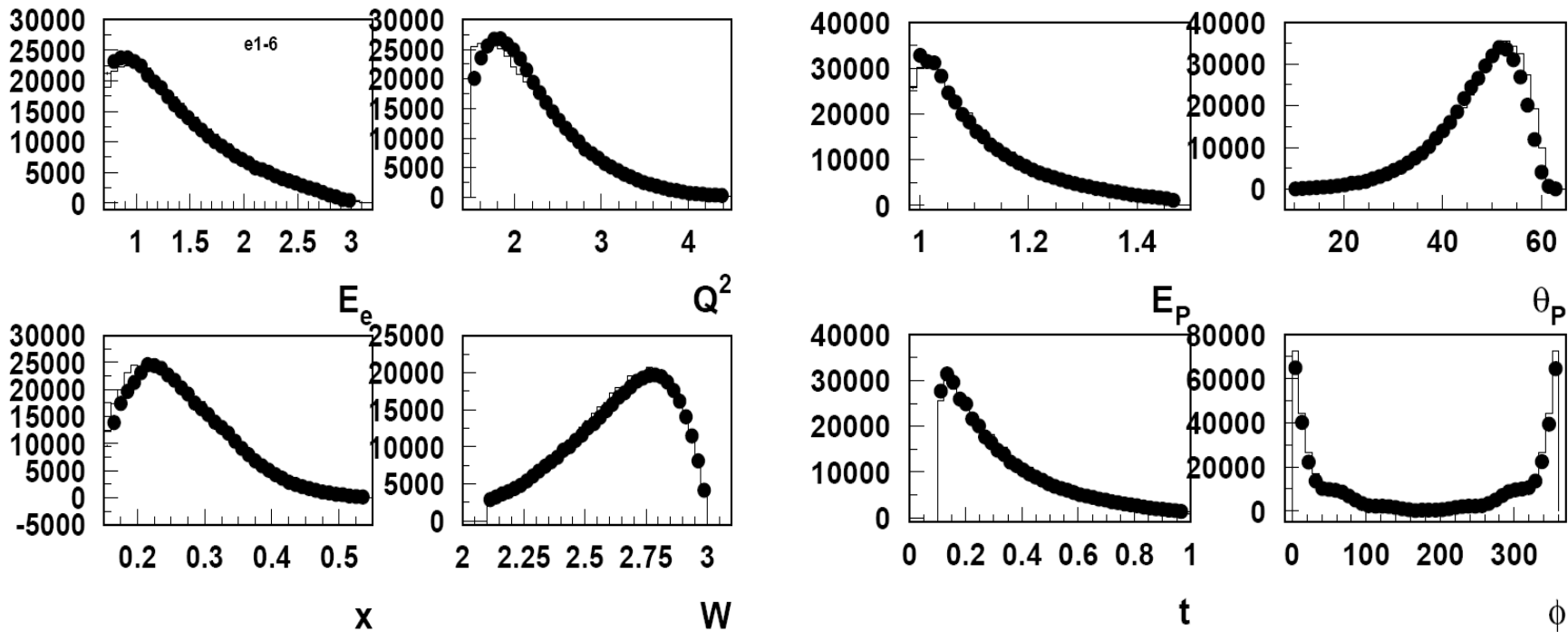


Collinearity cut $y_{\text{col}} - y > 0.025$ eliminates low ϕ and large t (the beam direction)

$$y = y_{\text{col}} \equiv \frac{Q^2 + \Delta^2}{Q^2 + x\Delta^2}$$

γ MC vs Data

- Exclusive photon production simulated using a realistic MC(based on S.Korotkov's code)

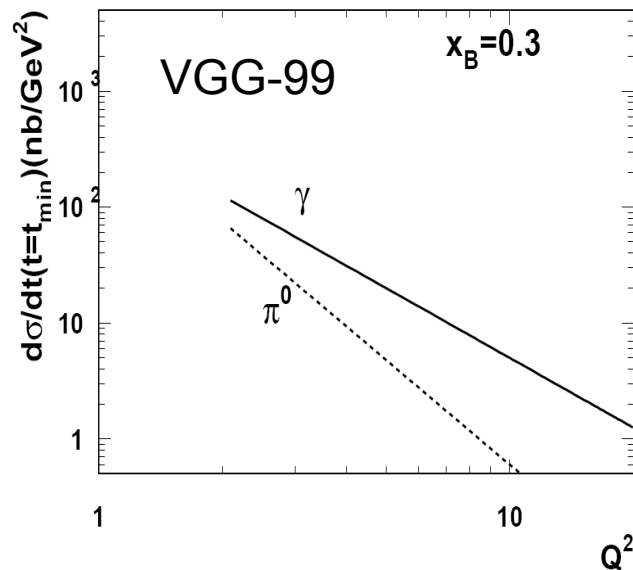
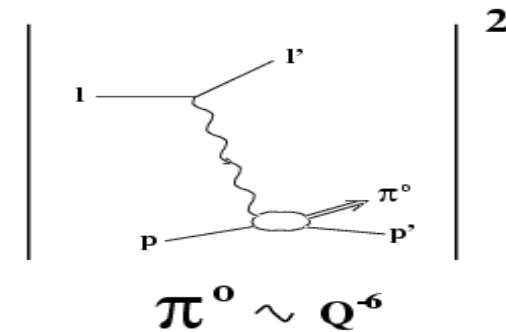
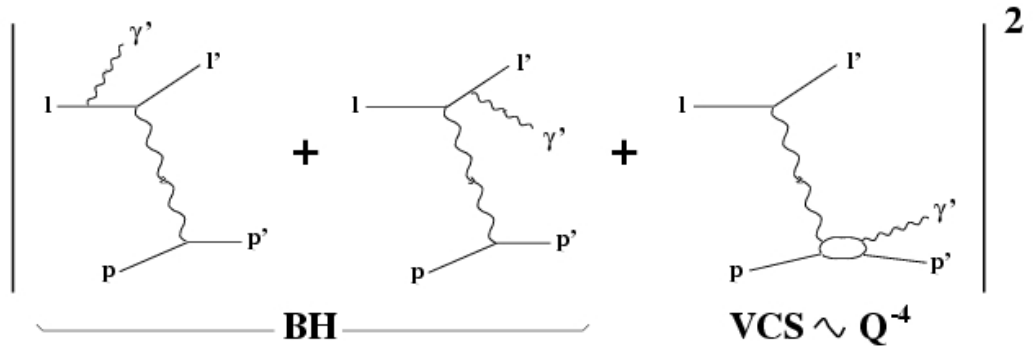


- Exclusive photon production simulated using a realistic MC(based on S.Korotkov's code)
- Kinematic distributions in x, Q^2, t consistent with the CLAS data

GPDs from $ep \rightarrow e'p'\gamma$

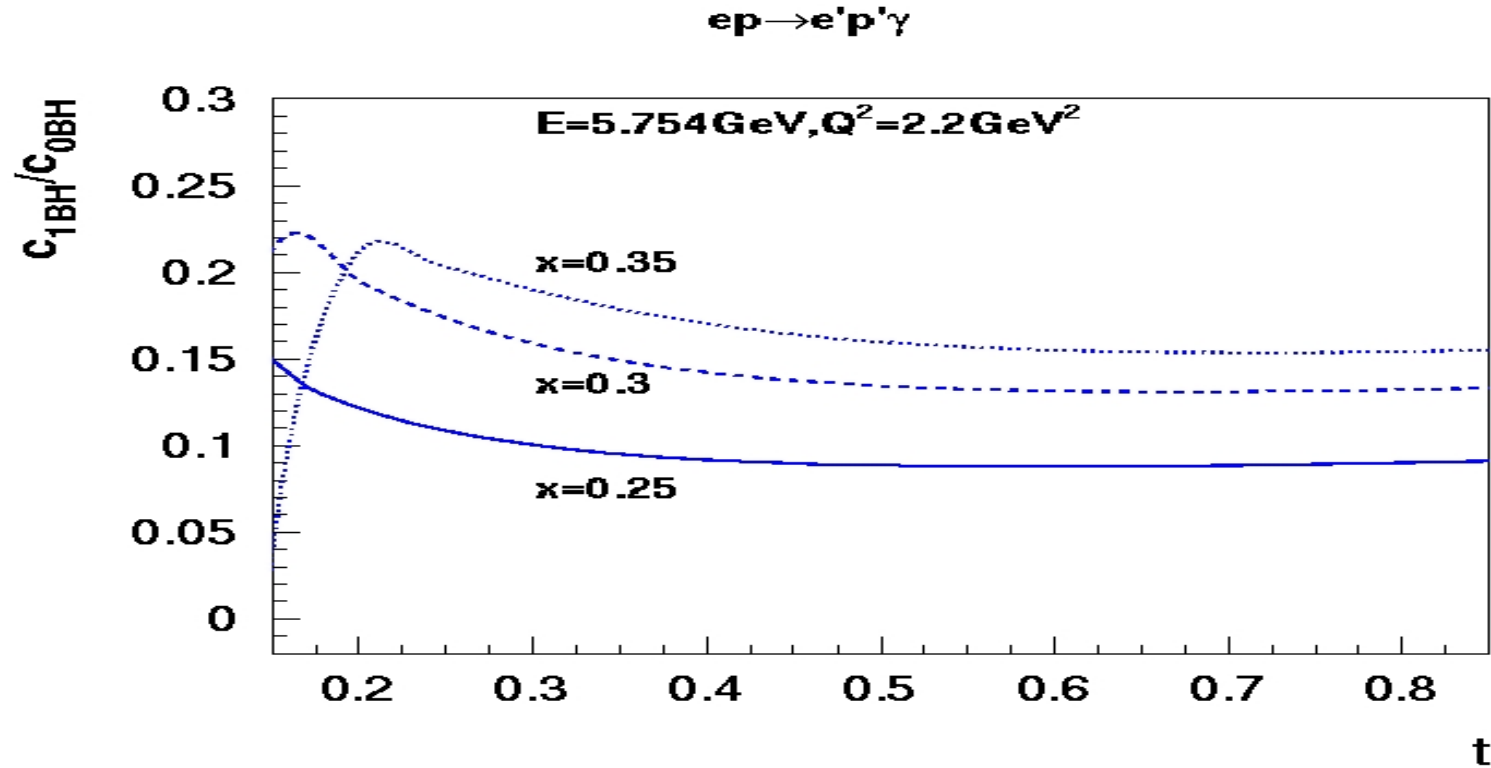
Requirements for precision ($<10\%$)
measurements of GPDs from DVCS SSA

- Define the procedure to extract GPDs from A_{LU}
 - effect of finite bins $\sim 10\%$
- Define background corrections
 - pion contamination $\sim 10\%$
 - radiative background



π^0 dominates the single photon
sample at low Q^2 in the
kinematics where BH is small

BH $\cos\phi$ moment



$$A_{LU} \propto \frac{\lambda s_2^I \sin \phi}{c_0^{BH} (1 + c_1^{BH} / c_0^{BH} \cos \phi)} \approx \frac{\lambda s_2^I \sin \phi - \lambda s_2^I (c_1^{BH} / 2c_0^{BH}) \sin 2\phi}{c_0^{BH}}$$

BH $\cos\phi$ moment can generate $\sim 3\%$ $\sin 2\phi$ in the A_{LU}