

Partons Transverse Momentum Distribution at Large x: A Window into Partons Dynamics in **Nucleon Structure within QCD** Trento, April 11-15, 2016

Main Topics

Recent Progress in Transverse Momentum Dependent (TMD) Distributions Evolution Global Extractions and Model Calculations of TMDs Transversity Distribution and Tensor Charge of the Nucleon Quarks Orbital Angular Momentum in the Nucleon

Lattice Calculations and TMDs Experimental Programs of TMDs including the SoLID detector at Jefferson Lab

Key-note participants

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Transversity **Tensor Charge** overview

Marco Radici INFN - Pavia







European Research Council

leading-twist TMD map







leading-twist TMD map — PDF map



leading-twist TMD map ------ PDF map



arXiv:1601.07782)

Transversity: Why



no h₁ for gluons (in Nucleon)



pure non-singlet evolution

Transversity: Why



playground for tests of perturbative and nonperturbative QCD

Tensor Charge

■ 1st Mellin moment of transversity ⇒ tensor "charge"

$$\delta q \equiv g_T^q = \int_0^1 dx \; \left[h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2) \right]$$

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no associated conserved current in \mathcal{L}_{QCD}

tensor 'charge' g_T scales with Q^2 C-oddaxial charge g_A conservedC-even

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axial charge g_A conserved C-even

tensor charge not directly accessible in \mathcal{L}_{SM} low-energy footprint of new physics at higher scales ?





Example: neutron β -decay n \rightarrow p e⁻ $\overline{\nu}_{e}$





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precision of $0.1\% \Rightarrow [3-5]$ TeV for BSM scale

neutron *β*-decay and tensor charge

tensor contribution to neutron β -decay

$$\mathcal{L}_{\text{eff}, T} \sim G_F V_{ud} \epsilon_T \bar{e} \sigma_{\mu\nu} \nu_{e\text{L}} \langle p | \bar{u} \sigma^{\mu\nu} d | n \rangle$$

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isospin symmetry

$$\langle p, S_p | \bar{u} \sigma^{\mu\nu} u - \bar{d} \sigma^{\mu\nu} d | p, S_p \rangle$$

same structure of isovector component of Ist Mellin moment of transversity

$$\langle p, S_p | \, \bar{q} \, \sigma^{\mu\nu} \, q \, | p, S_p \rangle = \left(P^{\mu} S_p^{\nu} - P^{\nu} S_p^{\mu} \right) \, g_T^q (Q^2)$$
$$= \left(P^{\mu} S_p^{\nu} - P^{\nu} S_p^{\mu} \right) \, \int dx \, h_1^{q-\bar{q}} (x, Q^2)$$

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knowledge of isovector tensor charge g_T^{u-d} affects precision of tensor coupling $G_F V_{ud} \epsilon_T g_T$ in β -decay

CP violation in **BSM**

in some BSM theories, the leading CP-violating (CPV) couplings are related to fermion Electric Dipole Moments (EDM)

$$\mathcal{L}_{\rm CPV} \supset ie \sum_{f=u,d,s,e} d_f \bar{f} \sigma_{\mu\nu} \gamma_5 f F^{\mu\nu} F^{\mu\nu} = \partial^{\mu} A^{\nu} - \partial^{\nu} A^{\mu}$$

neutron EDM
$$d_n = g_T^u d_u + g_T^d d_d + g_T^s d_s$$

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exp. bounds

+ improved knowledge on flavor-diagonal tensor charges

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exp. bounds

 + improved knowledge
 on flavor-diagonal tensor charges constraints on CP violation encoded in q EDM

Present extractions of transversity

nucleon polarization

	qua	rk pola	rization	
	U	L	Т	
U	f ₁		h_1^{\perp}	
L		g _{1L}	h_{1L}^{\perp}	
Т	$\mathbf{f_{1T}}^{\perp}$	g 1T	$h_1 h_{1T}^{\perp}$	



Present extractions of transversity





The status of the art

Kang et al., Ansel P.R. D93 (16) 014009 P.R. D	mino et al., 9 <mark>8</mark> 7 (13) 094019		
	₹ <u></u> 0.4		
$\sim = 0.2 = 1/2 $	0.2 r		
	v h _j		
	-0.2 0.1		
	0		
-0.05 Å -0.05 Å Kanp et al (2015)	-0.1		Vana
-0.15 - Anselmino et al (2015)	-0.2		Radic
0 0.2 04 0.6 0.8 1 X		0.2	0.4

TMD factorization

Radici et al.,



The status of the art



single-hadron fragmentation : the Collins effect



$$A_{\text{SIDIS}}^{\sin(\phi_h + \phi_S)}(x, z, P_T^2) \sim \frac{\sum_q e_q^2 h_1^q(x, \boldsymbol{k}_{\perp}^2) \otimes H_{1,q}^{\perp}(z, \boldsymbol{p}_{\perp}^2)}{\sum_q e_q^2 f_1^q(x, \boldsymbol{k}_{\perp}^2) \otimes D_{1,q}(z, \boldsymbol{p}_{\perp}^2)}$$



$$\begin{aligned} A_{e^+e^-}^{\cos 2\phi_1}(z_1, z_2, P_{1T}^2) &\sim \frac{\sin^2 \theta}{1 + \cos^2 \theta} \\ &\times \frac{\sum_q e_q^2 \ H_{1,q}^{\perp}(z_1, \boldsymbol{p}_{1\perp}^2) \ \otimes \ H_{1,\bar{q}}^{\perp}(z_2, \boldsymbol{p}_{2\perp}^2)}{\sum_q e_q^2 \ D_{1,q}(z_1, \boldsymbol{p}_{1\perp}^2) \ \otimes \ D_{1,\bar{q}}(z_2, \boldsymbol{p}_{2\perp}^2)} \end{aligned}$$

single-hadron fragmentation : the Collins effect

$$SIDIS$$

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$$\dots \otimes \dots \rightarrow \int d\mathbf{k}_{\perp} d\mathbf{p}_{\perp} \, \delta(z\mathbf{k}_{\perp}+\mathbf{p}_{\perp}-\mathbf{P}_T) \dots$$

$$h_1 h_2 X e^+ e^-$$

 $= \frac{6\pi\alpha^2}{2} A(y) \sum e_{-}^2 \int_{-\infty}^{\infty} db_T b_T J_0(a_T b_T) z^2 \tilde{D}_1^{q \to h}(z_1, b_T^2) z_2^2 \tilde{D}_1^{\bar{q} \to h}(z_2, b_T^2)$

$$\dots \otimes \dots \longrightarrow \int d\boldsymbol{p}_{1\perp} d\boldsymbol{p}_{2\perp} \, \delta(\boldsymbol{p}_{1\perp} + \boldsymbol{p}_{2\perp} + \frac{\boldsymbol{P}_{1T}}{z_1}) \dots$$

$$A_{e^+e^-}^{\cos 2\phi_1}(z_1, z_2, P_{1T}^2) \sim \frac{\sin^2 \theta}{1 + \cos^2 \theta} \times \frac{\sum_q e_q^2 \, H_{1,q}^\perp(z_1, \boldsymbol{p}_{1\perp}^2) \, \otimes \, H_{1,\bar{q}}^\perp(z_2, \boldsymbol{p}_{2\perp}^2)}{\sum_q e_q^2 \, D_{1,q}(z_1, \boldsymbol{p}_{1\perp}^2) \, \otimes \, D_{1,\bar{q}}(z_2, \boldsymbol{p}_{2\perp}^2)}$$

Collins effect : the TORINO extraction

- separate collinear x(z) and $k_{\perp}(p_{\perp})$ dependence
- Q^2 -independent Gaussian ansatz for k_{\perp} (p_{\perp}) dependence
- same Gaussian widths for $h_1 \& f_1$; different for $H_1^{\perp} \& D_1$

Anselmino et al., P.R. D**92** (15) 114023

> $\langle \mathbf{k}^2 \rangle = 0.57 \text{ GeV}^2$ $\langle \mathbf{p}^2 \rangle = 0.12 \text{ GeV}^2$ from analysis of SIDIS multiplicities

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- different collinear shape for favored & disfavored H_1^{\perp}
- DGLAP evolution of collinear dependence; Soffer bound built in $h_1(x,Q_0)$
- two schemes: chiral-odd evo for h_1 only; or for h_1 and H_1^{\perp}

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P.R. D92 (15) 114023

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- different collinear shape for favored & disfavored H_1^{\perp}
- DGLAP evolution of collinear dependence; Soffer bound built in $h_1(x,Q_0)$
- two schemes: chiral-odd evo for h_1 only; or for h_1 and H_1^{\perp}
- 4 parameters for h_1 , 5 for $H_1^{\perp} =>$ total 9 fit parameters
- 122 e⁺e⁻ data from (z_1, z_2) dep. and **BABAR** $(z_1, z_2, \mathbf{P}_{1T})$ dep.
- 146 SIDIS data from the and
- global χ^2 /dof in [0.84 1.2] at 95.45% C.L. ($\Leftrightarrow \Delta \chi^2 = 17.2$)

Collins effect with TMD evolution

first analysis implementing TMD evolution

Kang et al., *P.R.* D**93** (16) 014009

- NLO + NLL resummation
- Soffer bound built in "PDF term" $h_1(x,Q_0)$ as in TORINO param.
- different fav. & disfav. "PDF term" $H^{(3)}$ at Q_0 " " "
- chiral-odd evo for both "PDF terms", but only homogen. eq. for H⁽³⁾

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- total 13 fit parameters
- 122 e⁺e⁻ data from $\frac{2}{(z_1, z_2)}$ dep. and **BABAR** $(z_1, z_2, \mathbf{P}_{1T})$ dep.
- 140 SIDIS data from the and and and Jefferson Lab
- global χ^2 /dof = 0.88 with $\Delta \chi^2$ = 22.3

Transversity from Collins effect





Kang et al (2015) Anselmino et al (2013)





Transversity from Collins effect.





Collins function



0.1

0.2

Transversity from Collins effect.

0.1

0.2



di-hadron fragmentation

 $e p^{\uparrow} \rightarrow e'(\pi,\pi) X$

Radici, Jakob, Bianconi, P.R. D**65** (02) 074031 Bacchetta & Radici, P.R. D**67** (03) 094002



$$A_{\text{SIDIS}}^{\sin(\phi_R + \phi_S)}(x, z, M_h^2) \sim -\frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\triangleleft}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

 e^+e^-

$$e^+e^- \rightarrow (\pi^+\pi^-) (\pi^+\pi^-) X$$

$$\begin{aligned} A_{e^+e^-}^{\cos(\phi_R+\bar{\phi}_R)}(z,M_h^2,\bar{z},\bar{M}_h^2) &= \frac{\sin^2\theta_2}{1+\cos^2\theta_2} \\ &\times \frac{\sum_q e_q^2 \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\triangleleft}(z,M_h^2) \frac{|\bar{\mathbf{R}}_T|}{\bar{M}_h} H_{1,\bar{q}}^{\triangleleft}(\bar{z},\bar{M}_h^2)}{\sum_q e_q^2 D_{1,q}(z,M_h^2) D_{1,\bar{q}}(\bar{z},\bar{M}_h^2)} \end{aligned}$$

Artru & Collins, Z.Ph. C**69** (96) 277 Boer, Jakob, Radici, P.R. D**67** (03) 094003

di-hadron fragmentation

Radici, Jakob, Bianconi,



Boer, Jakob, Radici, P.R. D**67** (03) 094003
chiral-odd DiFF as quark spin analyzer



It is $\neq 0$ even if we integrate over the pair total transverse momentum $\int d(P_{h1T} + P_{h2T})$ (equivalent to take $P_{h1}+P_{h2} \parallel$ quark, as in figure) **quark polarization** connected to $2R_T = P_{h1T} - P_{h2T}$ (only if $h_1 \neq h_2$)

effect encoded in chiral-odd $H_1^{\triangleleft}(z, M_h^2)$ with $z=z_1+z_2$ and pair invariant mass M_h (<-> $|\mathbf{R}_T|$)

extraction of DiFF

extract DiFF from $e^+e^- \rightarrow (\pi^+\pi^-) (\pi^+\pi^-) X$

46 bins in (z, M_h) 9 parameters $\chi^2/d.o.f. = 0.57$

Courtoy et al., P.R. D85 (12) 114023



extraction of DiFF

extract DiFF from $e^+e^- \rightarrow (\pi^+\pi^-) (\pi^+\pi^-) X$

46 bins in (z, M_h) 9 parameters $\chi^2/d.o.f. = 0.57$

Courtoy et al., P.R. D85 (12) 114023





- no unpolarized data for D_1 need multiplicities for $e^+e^- \rightarrow (\pi^+\pi^-) X$ $e p \rightarrow e' (\pi^+\pi^-) X$
- little sensitivity to gluon D₁^g

- no data for z < 0.2
- approach valid for $M_h \ll Q$

$$A_{\text{SIDIS}}^{\sin(\phi_R + \phi_S)}(x, z, M_h^2) \sim -\frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\triangleleft}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

x-dep. of SSA given by PDFs only

$$A_{\text{SIDIS}}^{\sin(\phi_R + \phi_S)}(x, z, M_h^2) \sim -\frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^{\triangleleft}(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

x-dep. of SSA given by PDFs only

$$\begin{split} n_q^{\uparrow} &= \int dz \int dM_h^2 \, \frac{|\mathbf{R}|}{M_h} \, H_{1,sp}^{\triangleleft \, q}(z, M_h^2) \\ n_q &= \int dz \int dM_h^2 \, D_1^q(z, M_h^2) \\ n_q &= n_{\bar{q}} \qquad \begin{array}{c} n_q^{\uparrow} &= -n_{\bar{q}}^{\uparrow} \\ n_u^{\uparrow} &= -n_d^{\uparrow} \end{array} \end{split}$$

separate valence u and d

proton ¢омра deuteron

¢OMPAX

$$\begin{aligned} xh_{1}^{p}(x) &\equiv xh_{1}^{u_{v}}(x) - \frac{1}{4}xh_{1}^{d_{v}}(x) \\ &= -\frac{A(y)}{B(y)} \frac{[A_{UT}^{\sin(\phi_{R} + \phi_{S})}]_{p}}{e_{u}^{2}n_{u}^{\uparrow}} \frac{9}{4} \sum_{q=u,d,s} e_{q}^{2}xf_{1}^{q+\bar{q}}(x)n_{q} \\ xh_{1}^{D}(x) &\equiv xh_{1}^{u_{v}}(x) + xh_{1}^{d_{v}}(x) \\ &= -\frac{A(y)}{B(y)} \frac{[A_{UT}^{\sin(\phi_{R} + \phi_{S})}]_{D}}{e_{u}^{2}n_{u}^{\uparrow}} 3 \sum_{q=u,d,s} [e_{q}^{2}n_{q} + e_{\tilde{q}}^{2}n_{\tilde{q}}]xf_{1}^{q+\bar{q}}(x) \end{aligned}$$

q=u,d,s

 $\tilde{q} = d, u, s$

• parametrization at $Q_0^2 = 1 \text{ GeV}^2$

 $xh_1^{q_v}(x) = \tanh\left[\sqrt{x}\left(A_q + B_q x + C_q x^2 + D_q x^3\right)\right] \left[x\operatorname{SB}_q(x) + x\operatorname{\overline{SB}}_{\bar{q}}(x)\right]$

satisfies Soffer Bound at any Q² $2|h_1^q(x,Q^2)| \le 2 \operatorname{SB}_q(x) = |f_1^q(x) + g_1^q(x)|$

• parametrization at $Q_0^2 = 1 \text{ GeV}^2$

 $xh_{1}^{q_{v}}(x)x h_{1}^{q_{v}}(x)x h_{1}^{q_{v}}(x) + x \overline{SB}_{\bar{q}}(x) + x \overline{SB}_{\bar{q}}($

satisfies Soffer Bound at any Q²

 $2|h_1^q(x,Q^2)| \le 2 \operatorname{SB}_q(x) = |f_1^q(x) + 2g_1^q h_q^q(x,Q^2)| \le 2 \operatorname{SB}_q(x) = |f_1^q(x) + g_1^q(x)|$



• parametrization at $Q_0^2 = 1 \text{ GeV}^2$

 $xh_{1}^{q_{v}}(x)xh_{1}^{q_{v}}(x)xh_{1}^{q_{v}}(x)xh_{1}^{q_{v}}(x)xh_{1}^{q_{v}}(x)h_{1}^{$

satisfies Soffer Bound at any Q²

 $2|h_1^q(x,Q^2)| \leq 2h \lim_q Q^2 = f_1^q \lim_q Q^2 = f_1^q \lim_q Q^2 = f_1^q \lim_q Q^2 = 2 \operatorname{SB}_q(x) = |f_1^q(x) + g_1^q(x)|$



• parametrization at $Q_0^2 = 1$ GeV² $xh_1^{q_v}(x) = \tanh \left[\sqrt{x} \left(A_q + B_q x + C_q x^2 + D_q x^3\right)\right] \left[x \operatorname{SB}_q(x) + x \operatorname{SB}_{\bar{q}}(x)\right]$ $xh_1^{q_v}(x) = h_1^{q_v}(x) + h_1^{q_v}(x) + h_1^{q_v}(x) + h_1^{q_v}(x) + h_1^{q_v}(x) + h_1^{q_v}(x)) + h_1^{q_v}(x) + h_1^{q_v$

• parametrization at $Q_0^2 = 1 \text{ GeV}^2$ $xh_1^{q_v}(x) = \tanh \left[\sqrt{x} \left(A_q + B_q x + C_q x^2 + D_q x^3\right)\right] \left[x \operatorname{SB}_q(x) + x \operatorname{SB}_{\bar{q}}(x)\right]$ $xh_1^{q_v}(x) = h_1^{q_v}\left[\left(p_{q_v}^{q_v}(x) + p_{q_v}^{q_v}(x)\right) + p_{q_v}^{q_v}(x)\right] = \left[x \operatorname{SB}_q(x) + x \operatorname{SB}_{\bar{q}}(x)\right]$ rigid $intermation at any Q^2$ $satisfies Soffer Bound at any Q^2$ $2|h_1^q(x,Q^2)| \leq 2\frac{q_v}{q_v} = p_1^{q_v}(x) + q_1^{q_v}(x) + q_1^{q_v}(x)|$ $intermation at any Q^2$ extra-flexible

• 22 SIDIS data from thermes and

Airapetian et al., JHEP **0806** (08) 017 Adolph et al., P.L. **B713** (12)

Braun et al., E.P.J. Web Conf. **85** (15) 02018 history of upgrading fits

Bacchetta, Courtoy, Radici, P.R.L. **107** (11) 012001

Bacchetta, Courtoy, Radici, JHEP **1303** (13) 119 Radici et al., JHEP **1505** (15) 123













comparison with Collins effect

 $= \tanh\left[\sqrt{x} \left(A_q + B_q x + C_q x^2 + D_q x^3\right)\right] \left[x \operatorname{SB}_q(x) + x \operatorname{\overline{SB}}_{\bar{q}}(x)\right]$



comparison with Collins effect

 $= \tanh\left[\sqrt{x} \left(A_q + B_q x + C_q x^2 + D_q x^3\right)\right] \left[x \operatorname{SB}_q(x) + x \overline{\operatorname{SB}}_{\bar{q}}(x)\right]$



collinear factorization in hard processes

Artru & Collins, Z.Phys. **C69** (96) 277 Boer, Jakob, Radici, P.R.D**67** (03) 094003



Jaffe, Jin, Tang, P.R.L.**80** (98) 1166 Radici, Jakob, Bianconi, P.R.D**65** (02) 074031 Bacchetta & Radici, P.R. D**67** (03) 094002



Bacchetta & Radici, P.R. D70 (04) 094032

collinear factorization in hard processes

Artru & Collins, Z.Phys. C69 (96) 277 Boer, Jakob, Radici, P.R.D67 (03) 094003 DeFlorian & Vanni, P.L.**B578** (04) 139 Ceccopieri, Radici, Bacchetta, P.L.B650 (07) 81 (see also factorization e^+e^- Zhou and Metz, P.R.L. 106 (11) 172001 electron for M_h —evolution of DiFFs) standard DGLAP evolution eq.'s 2 pions positron lepton lepton proton 2 pions 2 pions proton protor factorization SIDIS factorization

> Jaffe, Jin, Tang, P.R.L.**80** (98) 1166 Radici, Jakob, Bianconi, P.R.D**65** (02) 074031 Bacchetta & Radici, P.R. D**67** (03) 094002

Bacchetta & Radici, P.R. D70 (04) 094032



$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

forward polarized particles at $\eta < 0$

B beam polarized

$$\frac{d\sigma^{0}}{d\eta \, d|\mathbf{P}_{T}| \, dM} = 2 \left|\mathbf{P}_{T}\right| \sum_{a,b,c,d} \int \frac{dx_{a} \, dx_{b}}{8\pi^{2}\bar{z}} f_{1}^{a}(x_{a}) f_{1}^{b}(x_{b}) \frac{d\hat{\sigma}_{ab\to cd}}{d\hat{t}} D_{1}^{c}(\bar{z}, M) \qquad \hat{t} = t \, x_{a}/\bar{z}$$

$$\frac{d\sigma_{UT}}{d\eta \, d|\mathbf{P}_T| \, dM} = |\mathbf{S}_{BT}| \, 2 \, |\mathbf{P}_T| \, \frac{|\mathbf{R}|}{M} \, \sin \theta \, \sum_{a,b,c,d} \int \frac{dx_a \, dx_b}{8\pi^2 \bar{z}} \, f_1^a(x_a) \, h_1^b(x_b) \, \frac{d\Delta \hat{\sigma}_{ab^{\uparrow} \to c^{\uparrow} d}}{d\hat{t}} \, H_1^{\triangleleft c}(\bar{z}, M) \, d\hat{t}$$

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specific spin asymmetry due to transversity and chiral-odd DiFF not possible for single-hadron production (no factorization th.)



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$$\frac{|\mathbf{R}|}{M} = \frac{1}{2}\sqrt{1 - 4\frac{m_{\pi}^2}{M^2}} \quad \mathcal{M} = \text{invariant mass of } (\mathbf{T} \ \mathbf{T})$$



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 η = pseudorapidity

conservation of momenta in $ab \rightarrow cd$ $\Rightarrow (\pi\pi)$ fract. energy fixed to $\bar{z} = \frac{|P_T|}{\sqrt{s}} \frac{x_a e^{-\eta} + x_b e^{\eta}}{x_a x_b}$



forward $A_{UT}(M)$



prediction of new STAR data using 68% of replicas forward $A_{UT}(M)$

run 2006Adamczyk et al. (STAR), P.R.L. 115 (2015) 242501run 2012K. Landry, talk at APS 2015

backward $A_{UT}(M)$



prediction of new STAR data using 68% of replicas backward $A_{UT}(M)$

run 2006Adamczyk et al. (STAR), P.R.L. 115 (2015) 242501run 2012K. Landry, talk at APS 2015

A_{UT}(η)



prediction of new STAR data using 68% of replicas $A_{UT}(\eta)$

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back to tensor charge



0

et al (2015) Radici et al (2015) Radici et al (2015)

et al (2015) Kang et al (2015) Kang et al (2015) 65 0 -1 0 0.2 0.4 0.6 -0.5 0.6 .4 -0.5 -1 o [0.1] [0.1]

back to tensor charge



g_T^{u-d} affects tensor coupling in β -decay



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FIG. 32. Comparison of the isovector nucleon tensor charge g_T from this paper at 68% C.L. (Kang et al 2015) at $Q^2 = 10$ GeV² and result from Ref. [18] (Radici et al 2015) at 68% CL and $Q^2 = 4$ GeV², and Ref. [17] at 95% CL standard and polynomial fit (Anselmino et al 2013) at $Q^2 = 0.8$ GeV². Other points are lattice computation at $Q^2 = 4$ GeV² of Bali et al Ref. [117], Gupta et al Ref. [118], Green et al Ref. [119], Aoki et al Ref. [127], Bhattacharya et al ref. [120], Gockeler et al Ref. [121]. Pitschmann et al is DSE calculation at $Q^2 = 4$ GeV² Ref. [112].

processes. These features have been clearly demonstrated in Figs. 20-21. In particular, the transverse momentum dependence illustrates the effects coming from the Sudakov resummation form factors where the perturbative part plays an important role due to large value of the resolution scale $Q \simeq 10.6$ (GeV). The associated scale evolution effects in the $\hat{H}^{(3)}(z)$ is another important aspect in the calculations. The evolution kernel is different from that of

g_T^{u-d} affects tensor coupling in β -decay



 $Q^2 = 4 \text{ GeV}^2 \text{ except}$ 2) Kang et al. 2015 $Q^2 = 10$ 3) Anselmino et al. 2013 $Q^2 = 0.8$

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precision of g_T^{u-d}

current most stringent constraints on BSM tensor coupling come from

• Dalitz-plot study of radiative pion decay $\pi^+ \rightarrow e^+ \nu_e \gamma$

Bychkov et al. (PIBETA), P.R.L. 103 (09) 051802

 measurement of correlation parameters in neutron β-decay of various nuclei
 Pattie et al., P.R. C88 (13) 048501



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JLab12 Di-hadron proposals



PR12-12-009

A 12 GeV Research Proposal to Jefferson Lab (PAC 39)

Measurement of transversity with dihadron production in SIDIS with transversely polarized target

H. Avakian^{†*}, V.D. Burkert, L. Elouadrhiri, T. Kageya, V. Kubarovsky M. Lowry, A. Prokudin, A. Puckett, A. Sandorfi, Yu. Sharabian, X. Wei Jefferson Lab, Newport News, VA 23606, USA

S. Anefalos Pereira[†], M. Aghasyan, E. De Sanctis, D. Hasch, L. Hovsepyan, V. Lucherini, M. Mirazita, S. Pisano, and P. Rossi INFN, Laboratori Nazionali di Frascati, Frascati, Italy

A. Courtoy[†] IFPA-Institut de Physique Universite de Liege (ULg), Allee du 6 Aout 17, bat. B5 4000 Liege, Belgium A. Bacchetta, M. Radici[†], B. Pasquini Universita' di Pavia and INFN Sezione di Pavia, via Bassi 6, 27100 Pavia, Italy

Dihadron Electroproduction in DIS with Transversely Polarized 3 He Target at 11 and 8.8 GeV

June 2, 2014

(A Proposal to Jefferson Lab (PAC 42))

J. Huang, X. Qian Brookhaven National Laboratory, Upton, NY, 11973

H. Yao College of William & Mary, Williamburg, VA

I. Akushevich. P.H. Chu. H. Gao (co-spokesperson). M. Huang. X. Li.

Hall B, using CLAS12 detector with transversely polarized HD-Ice target

PAC39: rating A, approval C1 (subject to further test on HD-Ice target)

Hall A, using SoLID detector with transversely polarized ³He target \Rightarrow separate *u* and *d*

PAC42: "valid addition" to approved E12-10-006 (E12-10-006A)

(x, Q²) (future) data coverage



Figure 2-EIC and data and sensitive times the

Aschenauer et al. (RHIC SPIN Coll.), arXiv:1602.03922

- transversity can be extracted from data using two independent methods: - Collins effect in single-hadron production

 Di-hadron production
- limited data set \rightarrow substantial overlap of results (except for d at large x)

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 - collinear factorization vs. TMD fact.
 - DGLAP evolution vs. TMD evolution
 - extension to p-p collisions

crosscheck of TMD approach

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 - extension to p-p collisions
- tensor charge useful for low-energy explorations of BSM new physics

definitely need of more data at (very) large and (very) small x

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