

Photoproduction of the $f_1(1285)$ Meson

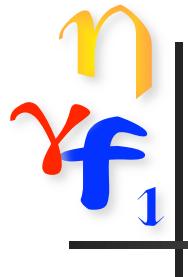
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Carnegie Mellon University

Ph.D. work of Ryan Dickson, completed 2011



Outline

- What are the $f_1(1285)$ and $\eta(1295)$ mesons?
- Identification of the state in CLAS/g11
- Final results for:
 - Mass and Width
 - Differential cross sections - model comparisons
 - Branching ratios $\eta\pi\pi$, $\gamma\rho^0$, $K\bar{K}\pi$
 - Dalitz plot analysis
 - spin and parity determination
 - clue to production mechanism
 - (only really new topic since 2011)
- CLAS publication



The Players:

- $f_1(1285)$ $I^G(J^{PC}) = 0^+(1^{++})$
 - Well-established axial-vector meson seen in several hadronic reactions;
 - ~7000 events reported world-wide
 - seen in PWA analyses
 - Possible “dynamically generated” $K\bar{K}^*$ – c.c. state
- $\eta(1295)$ $I^G(J^{PC}) = 0^+(0^{-+})$
 - A “controversial” state seen in $\pi^- p \rightarrow \pi \pi \pi n$
 - ~12000 events analyzed
 - Seen only in PWA, e.g. J. Manak et al., E852/BNL

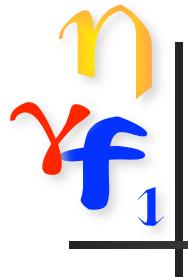


Quark Model for Mesons PDG 2014

Table 15.2: Suggested $q\bar{q}$ quark-model assignments for some of the observed light mesons. Mesons in bold face are included in the Meson Summary Table. The wave functions f and f' are given in the text. The singlet-octet mixing angles from the quadratic and linear mass formulae are also given for the well established nonets. The classification of the 0^{++} mesons is tentative: The light scalars $a_0(980)$, $f_0(980)$, and $f_0(500)$ are often considered as meson-meson resonances or four-quark states, and are omitted from the table. Not shown either is the $f_0(1500)$ which is hard to accommodate in the nonet. The isoscalar 0^{++} mesons are expected to mix. See the “Note on Scalar Mesons” in the Meson Listings for details and alternative schemes.

n	$2s+1\ell_J$	J^{PC}	$\mathbf{l} = 1$ $u\bar{d}, \bar{u}d, \frac{1}{\sqrt{2}}(\bar{d}\bar{d} - u\bar{u})$	$\mathbf{l} = \frac{1}{2}$ $u\bar{s}, \bar{d}s; \bar{d}s, -\bar{u}s$	$\mathbf{l} = 0$ f'	$\mathbf{l} = 0$ f	θ_{quad} [°]	θ_{lin} [°]
1	1S_0	0^{-+}	π	K	η	$\eta'(958)$	-11.4	-24.5
1	3S_1	1^{--}	$\rho(770)$	$K^*(892)$	$\phi(1020)$	$\omega(782)$	39.1	36.4
1	1P_1	1^{+-}	$b_1(1235)$	K_{1B}^\dagger	$h_1(1380)$	$h_1(1170)$		
1	3P_0	0^{++}	$a_0(1450)$	$K_0^*(1430)$	$f_0(1710)$	$f_0(1370)$		
1	3P_1	1^{++}	$a_1(1260)$	K_{1A}^\dagger	$f_1(1420)$	$f_1(1285)$		
1	3P_2	2^{++}	$a_2(1320)$	$K_2^*(1430)$	$f_2'(1525)$	$f_2(1270)$	32.1	30.5
1	1D_2	2^{-+}	$\pi_2(1670)$	$K_2(1770)^\dagger$	$\eta_2(1870)$	$\eta_2(1645)$		
1	3D_1	1^{--}	$\rho(1700)$	$K^*(1680)$		$\omega(1650)$		
1	3D_2	2^{--}		$K_2(1820)$				
1	3D_3	3^{--}	$\rho_3(1690)$	$K_3^*(1780)$	$\phi_3(1850)$	$\omega_3(1670)$	31.8	30.8
1	3F_4	4^{++}	$a_4(2040)$	$K_4^*(2045)$		$f_4(2050)$		
1	3G_5	5^{--}	$\rho_5(2350)$	$K_5^*(2380)$				
1	3H_6	6^{++}	$a_6(2450)$			$f_6(2510)$		
2	1S_0	0^{-+}	$\pi(1300)$	$K(1460)$	$\eta(1475)$	$\eta(1295)$		
2	3S_1	1^{--}	$\rho(1450)$	$K^*(1410)$	$\phi(1680)$	$\omega(1420)$		

† The $1^{+\pm}$ and $2^{-\pm}$ isospin $\frac{1}{2}$ states mix. In particular, the K_{1A} and K_{1B} are nearly equal (45°) mixtures of the $K_1(1270)$ and $K_1(1400)$. The physical vector mesons listed under 1^3D_1 and 2^3S_1 may be mixtures of D_1 and S_1 , or even have hybrid components.



Dynamically Generated Mesons

- The $f_1(1285)$ as a $\{\bar{K}K^* + \text{c.c.}\}$ composite state
 - Chiral Lagrangian + unitarization of the pseudoscalar - vector meson nonet interaction
 - Lattice calculations
 - Expect “non-standard” production mechanisms, if true

M. F. M. Lutz and E. E. Kolomeitsev Nucl Phys **A730** 392, (2004)
L. Roca, E. Oset, J. Singh Phys Rev **D72**, 014002 (2005)
F. Aceti, Ju-Jun Xie, E. Oset, arXiv:1505.06134 (2015)



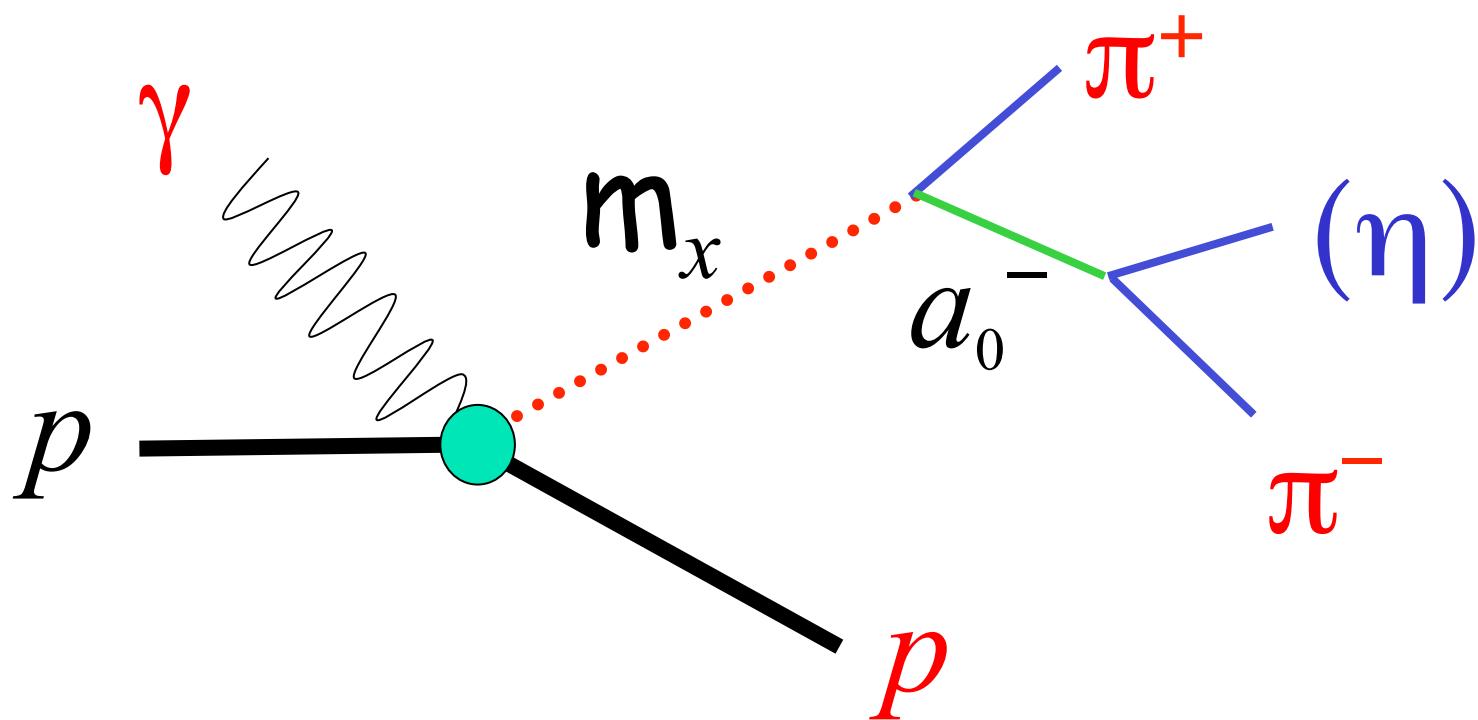
Properties of $f_1(1285)$ and $\eta(1295)$

	$f_1(1285)$	$\eta(1295)$	CLAS m_x
$I^G(J^{PC})$	$0^+(1^{++})$	$0^+(0^{-+})$	TBD
Mass (MeV)	$1281.9 \pm .5$	1294 ± 4	TBD
Width, Γ (MeV)	24.2 ± 1.1	55 ± 5	TBD
Decays:			
4π	$33 \pm 2\%$	-	-
$\eta\pi\pi$	$52 \pm 2\%$	Seen	TBD
$\rightarrow a_0(980)\pi$, no $a_0 \rightarrow K\bar{K}$	$36 \pm 7\%$	Seen	TBD
$\rightarrow \eta\pi\pi$, Excluding $a_0\pi$	$16 \pm 7\%$	-	TBD
$K\bar{K}\pi$	$9.0 \pm 0.4\%$	-	TBD
$\gamma\rho^0$	$5.5 \pm 1.3\%$	Not Seen	TBD



One Reaction Topology

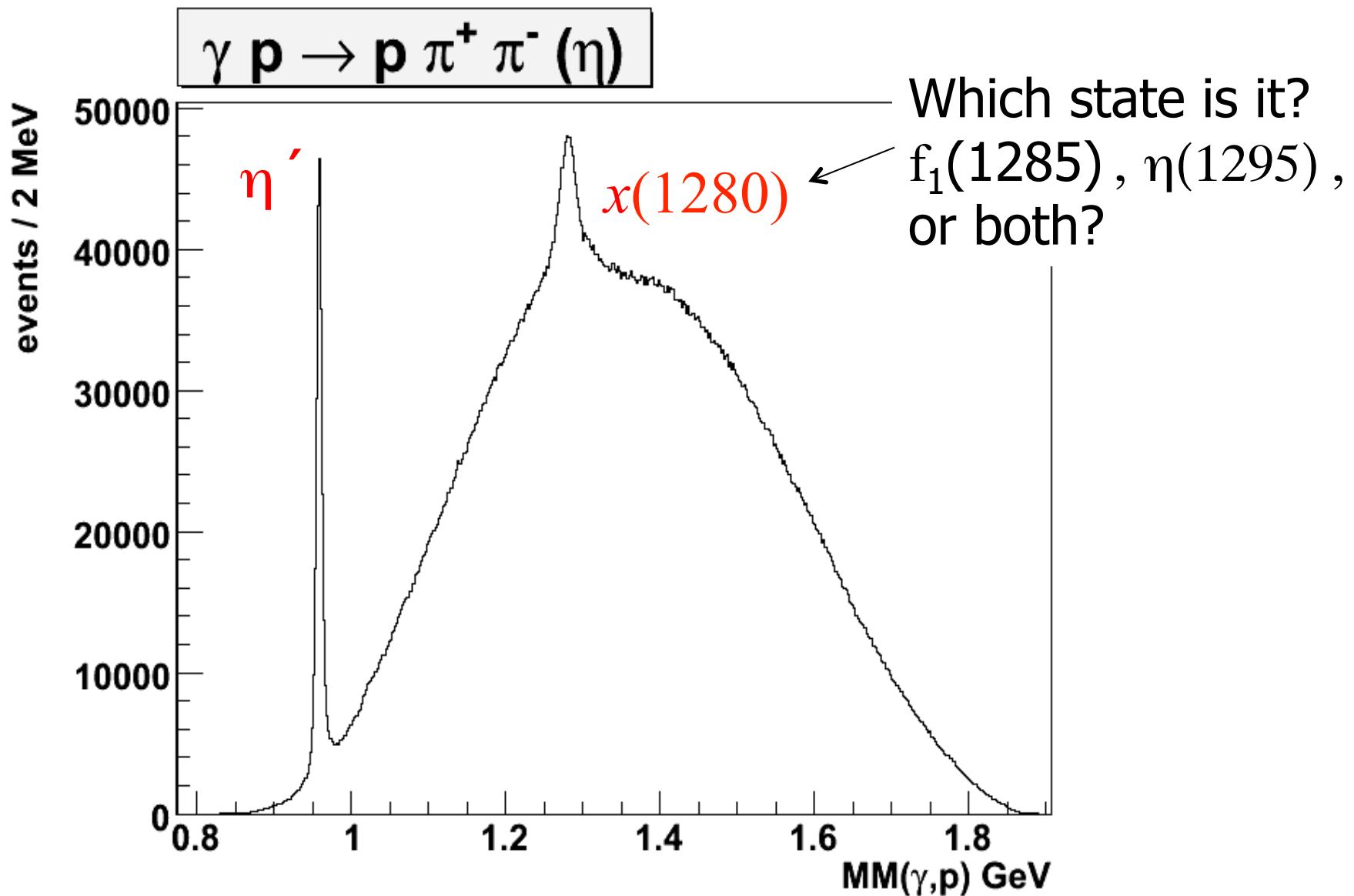
(example)



red = measured particles



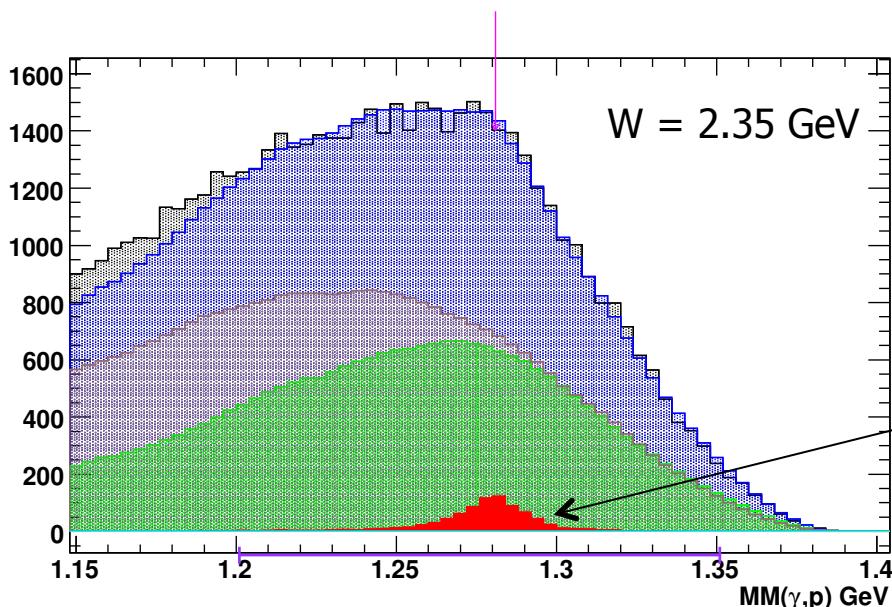
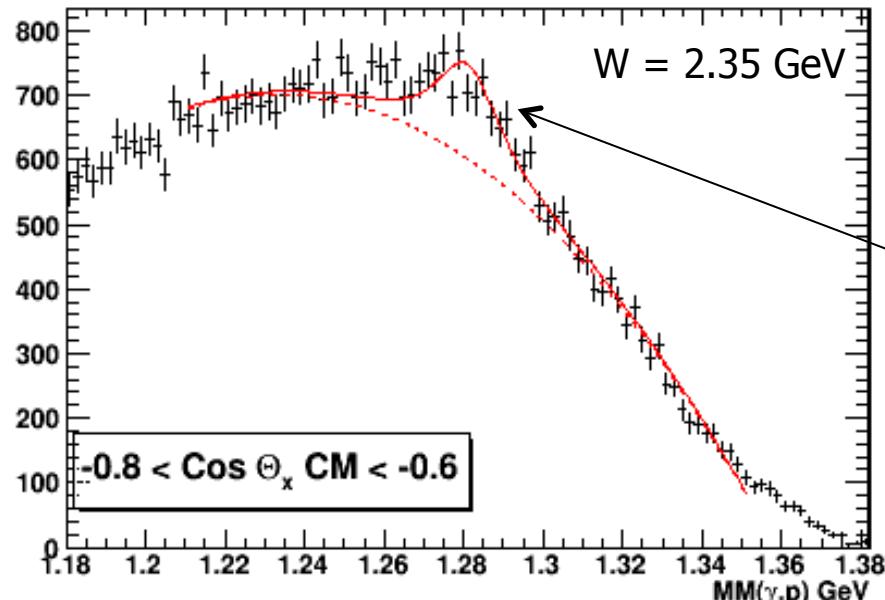
First Observation of the $f_1(1285)$ and/or $\eta(1295)$ in Photoproduction



Great statistics in CLAS g11 data: $\sim 1.5 \times 10^5$ $x(1280)$ events



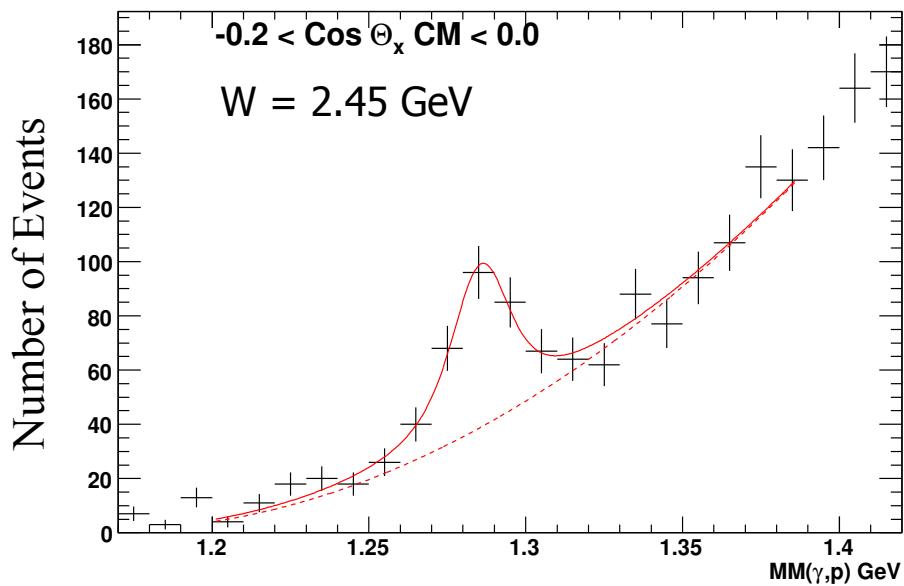
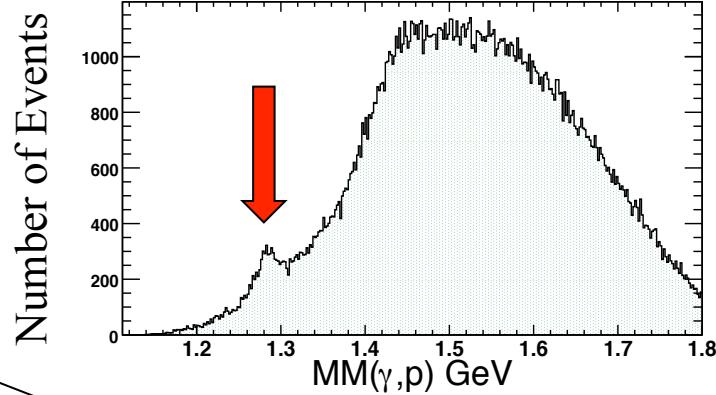
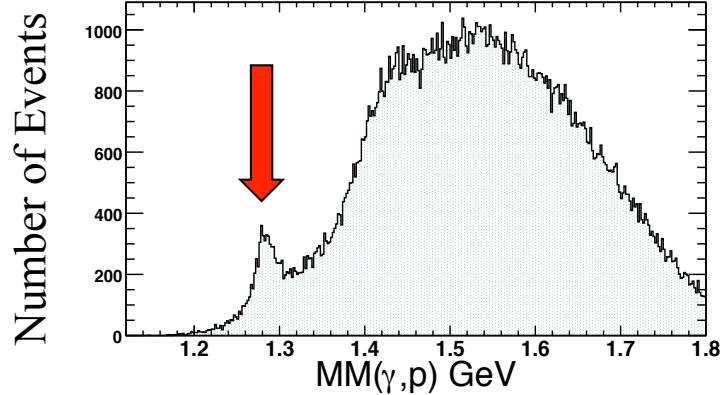
Two yield extraction methods



- Voigtian lines shape using known CLAS resolution
 - Convolution of BW and Gaussian
- Monte Carlo fitting using signal and estimated multi-pion backgrounds
 - $p \rho \pi \pi$ (green)
 - $p \phi_1(1370)$ (purple)
 - $p \chi(1280)$ (red) - signal
 - Total (blue)



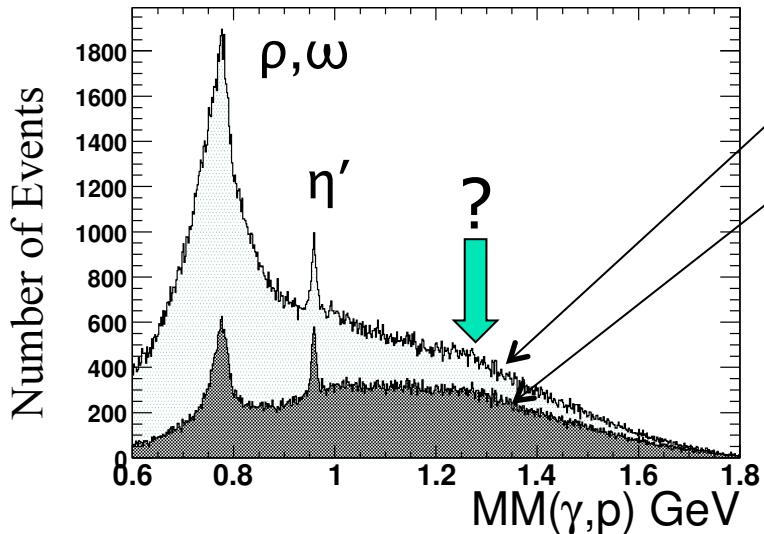
Two $x \rightarrow K K \pi$ decay modes



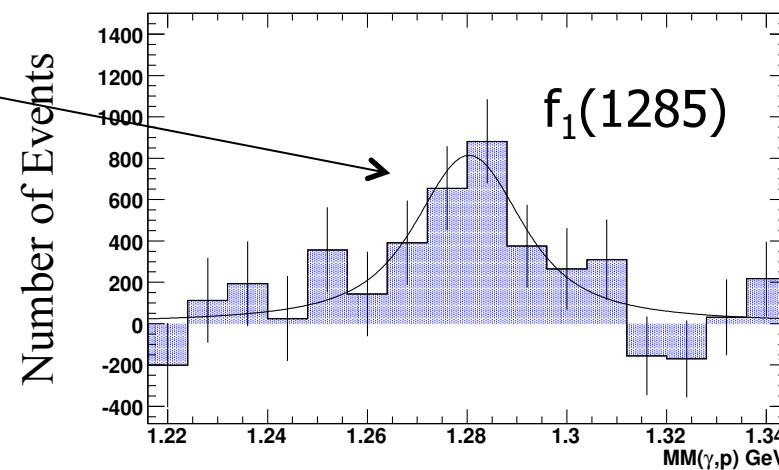
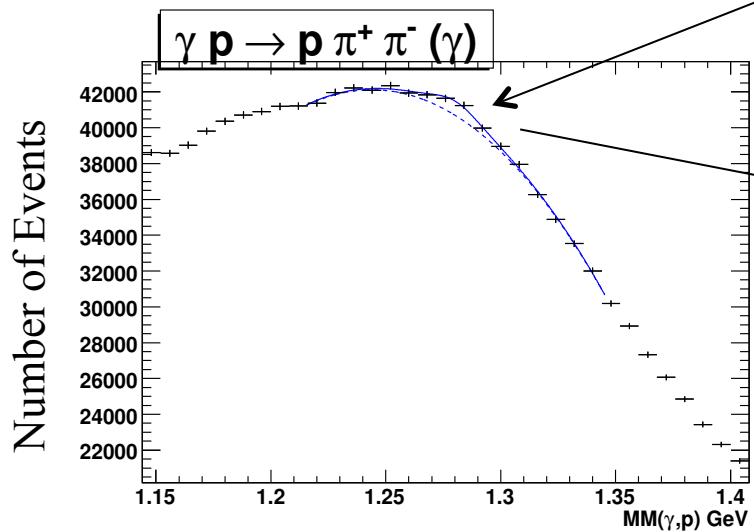
- Detect $p K^+ \pi^- (K^0)$
 - (left)
- Detect $p K^- \pi^+ (\bar{K}^0)$
 - (right)
- Combine channels prior to yield extraction using Voigtian + polynomial



Looking for γp^0 decays

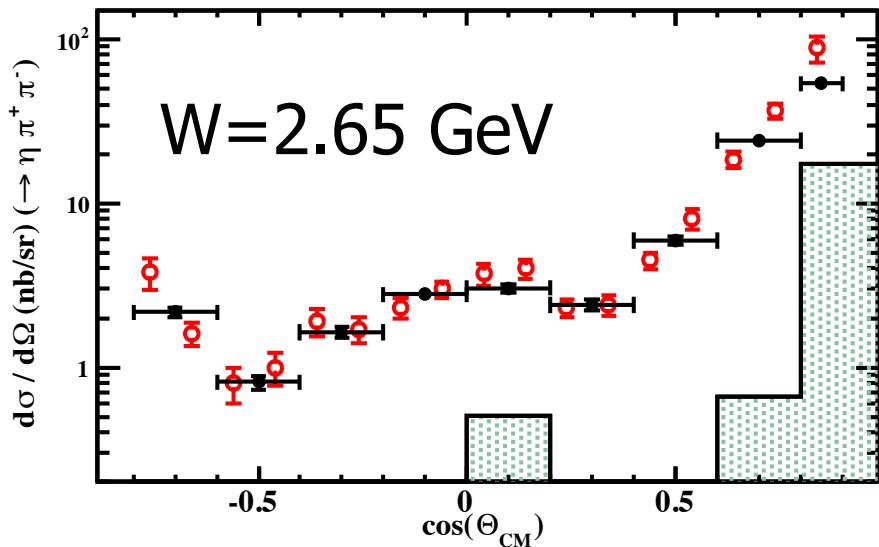
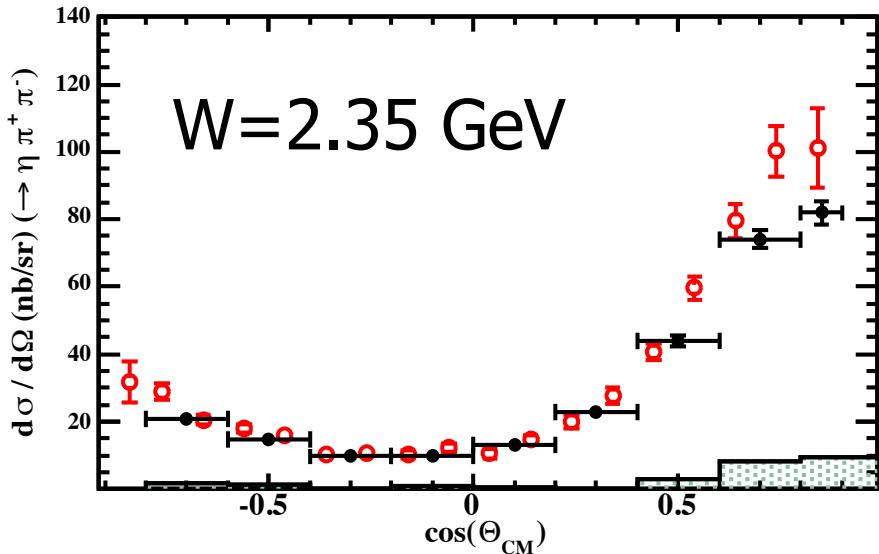


- Kinematic fit to $\gamma p \rightarrow p\pi^+\pi^-(\gamma)$
- Select $p_{\text{perp}} > 40 \text{ MeV}/c$
- 2nd kin. fit to $\gamma p \rightarrow p\pi^+\pi^-(\pi^0)$ to reject π^0 background
- Very small signal: only extract branching ratio to $\eta \pi^+ \pi^-$
 - Sum over all kinematics





Cross-check η' cross section



- Compare two CLAS analyses of η' photoproduction
 - Same data set using different methods
 - Red: Krahn & Williams
 - Black: Dickson (this work)
 - Good agreement
- Use difference as a measure of systematic uncertainty (histogram)

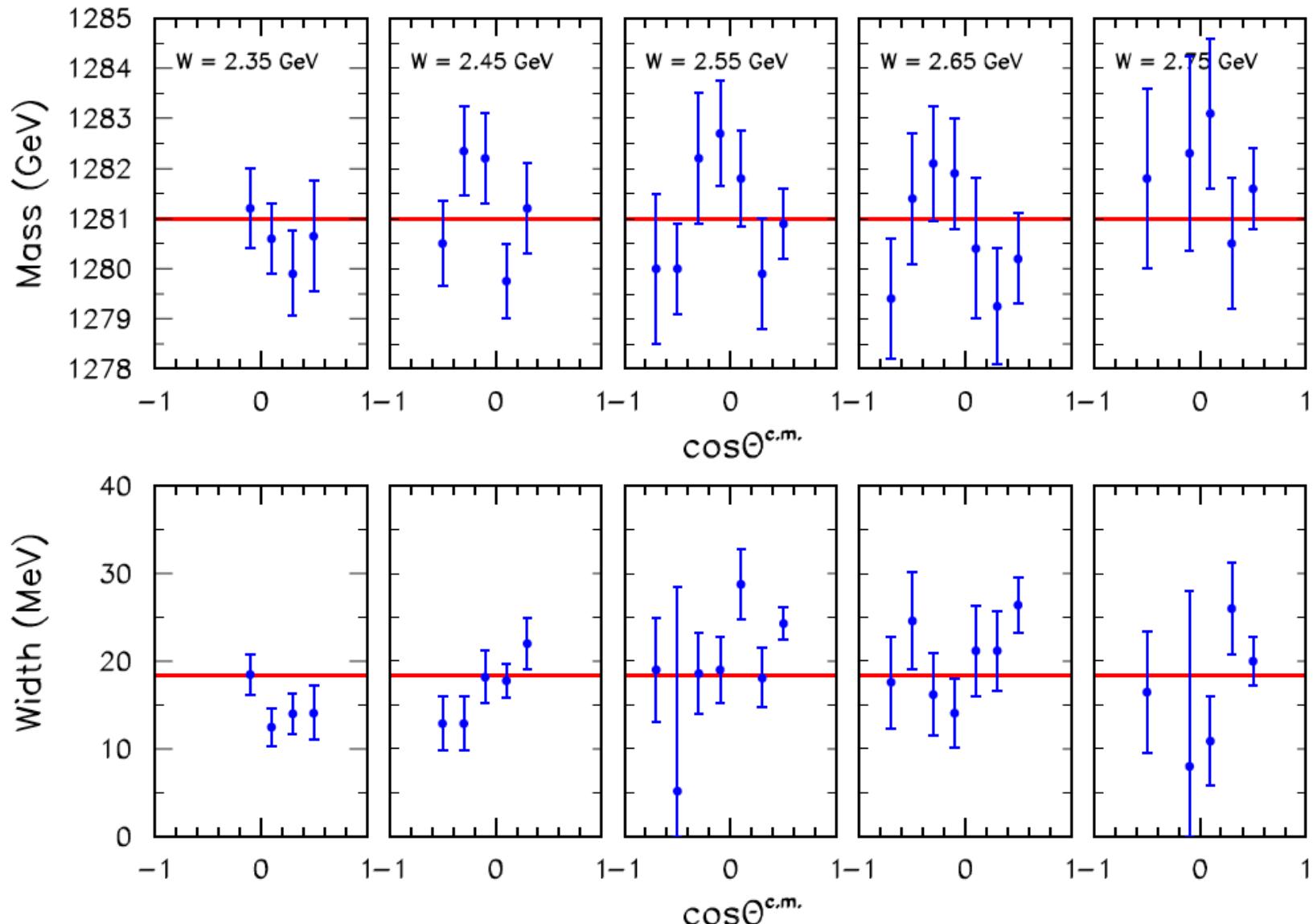
(Note log scale)



Results



Mass & Width Measurement





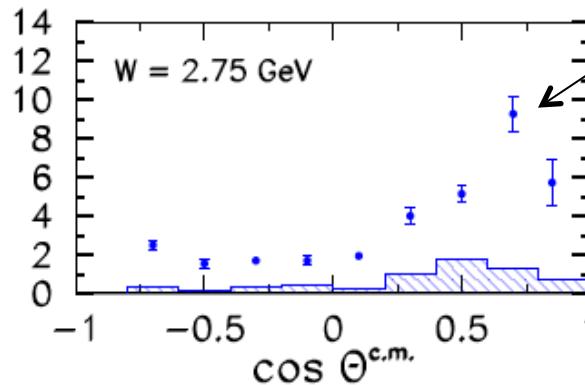
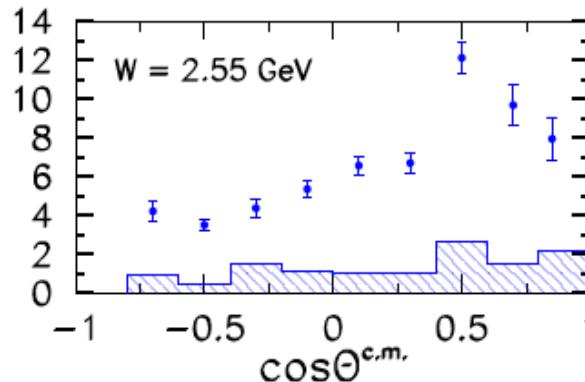
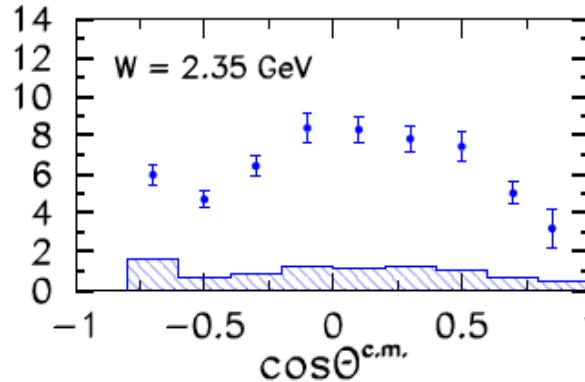
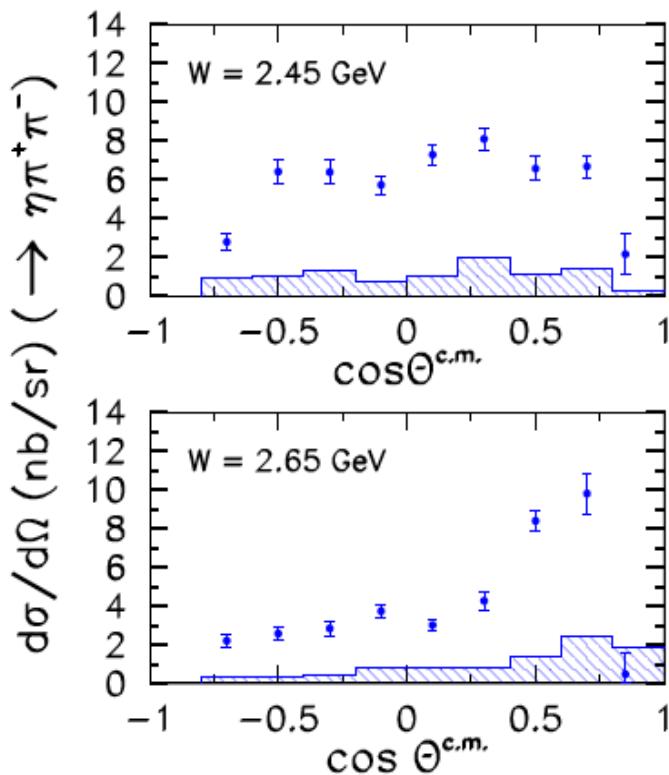
Mass & Width Measurement

Channel		Mass (MeV/c ²)	Width (MeV/c ²)
$\eta' \rightarrow \eta\pi^+\pi^-$	CLAS	958.48 ± 0.04	$\Gamma \ll \sigma_{exp}$
$x \rightarrow \eta\pi^+\pi^-$	CLAS	1281.0 ± 0.8	18.4 ± 1.4
η'	PDG	957.78 ± 0.06	0.198 ± 0.009
$f_1(1285)$	PDG	1281.9 ± 0.5	24.2 ± 1.1
$\eta(1295)$	PDG	1294 ± 4	55 ± 5

- Mass consistent with PDG value for $f_1(1285)$
- Width is smaller than PDG by several σ ...but we are right



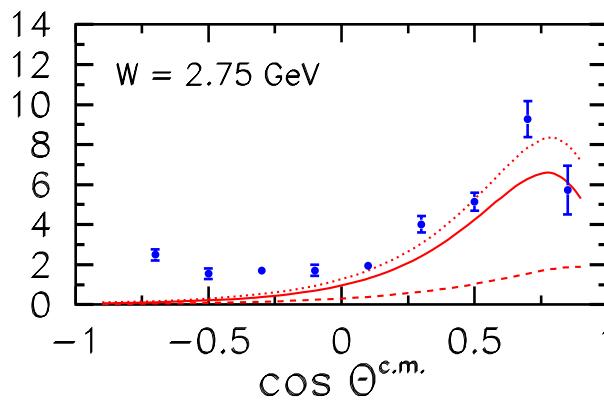
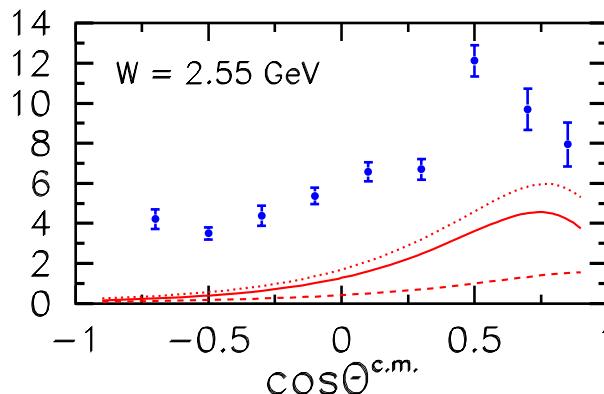
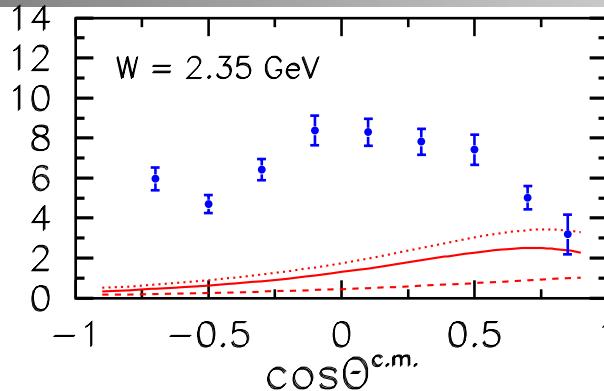
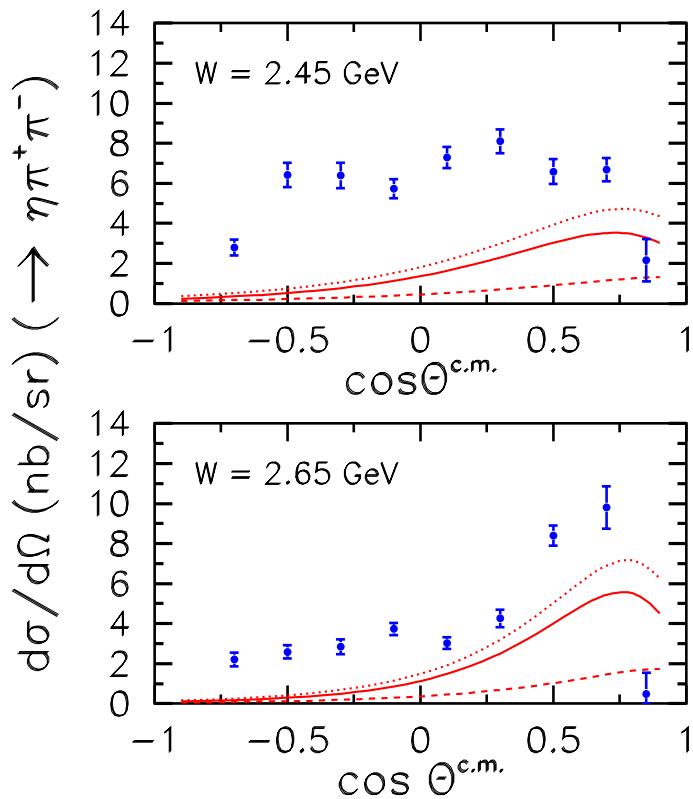
Cross Section vs. Angle and W



- Differential cross-section to
 - $\eta\pi^+\pi^-$ final state
 - not scaled since we don't measure total rate
- Systematics
- Very weak forward peaking seen
 - drop at most forward angles



Comparison with Models

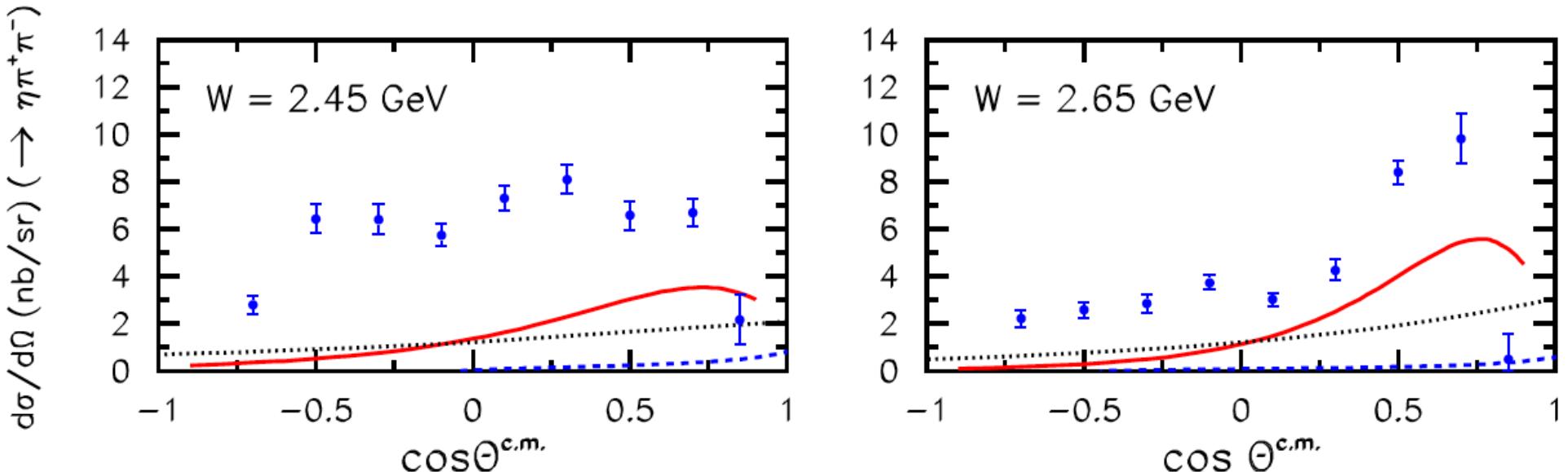


- N. Kochelev model
 - Effective Lagrangian
 - t-channel ρ and ω exchange
 - Solid: $f_1(1285)$
 - Dashed: $\eta(1295)$
 - Dotted: sum

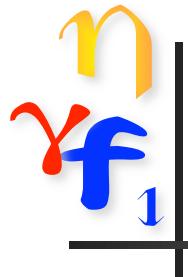
- Poor match to data



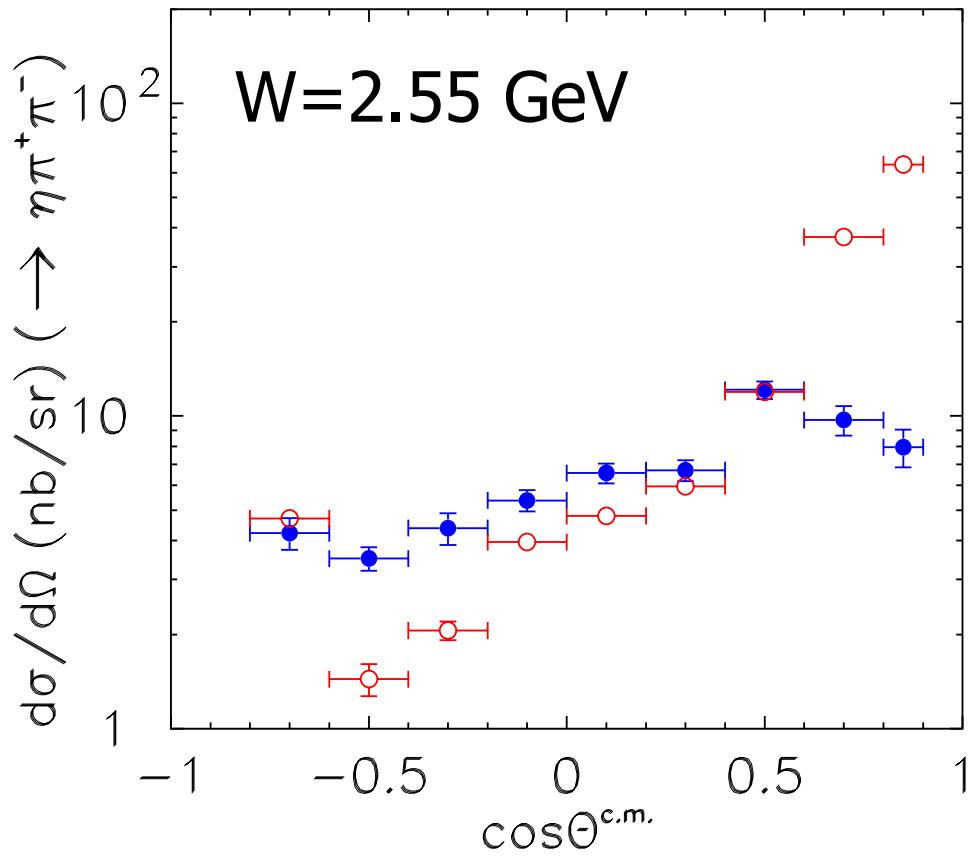
More models...



- Solid red: Effective Lagrangian with meson exch.
 - (same as previous page)
- Dashed: Effective Lagrangian with meson exch.
 - Uncontrolled hadronic form factor cut-offs
 - J-J. Xie (unpublished, private comm.)
- Dotted: "Holographic QCD" model
 - S. Domokos: meson exchange with specific recipe to compute couplings



Compare Mesons: f_1 and η'



- Compare $f_1(1285)$ and η'
 - Red: CLAS η'
 - Black: CLAS $f_1(1285)$
- Note logarithmic scale
- $f_1(1285)$ is produced “flatter” than the η'
 - Clue about production: not meson-exchange dominated like the η'

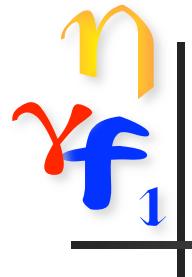


Branching Ratios

Item	Value	Stat. Uncert.	Syst. Uncert.	PDG $f_1(1285)$
$\eta\pi^+\pi^-$ Event Yield	1.33×10^5	4.9×10^3	2.9×10^3	
$\eta\pi^+\pi^-$ Acceptance	0.0652	9.7×10^{-5}	0.0072	
$K^\pm K^0\pi^\mp$ Event Yield	6570	180	340	
$K^\pm K^0\pi^\mp$ Acceptance	0.0149	3.18×10^{-5}	0.0016	
$\gamma\rho^0$ Event Yield	3790	790	850	
$\gamma\rho^0$ Acceptance	0.0248	6.4×10^{-5}	0.0050	
Isospin C.G. $\Gamma(K^\pm K^0\pi^\mp)/\Gamma(K\bar{K}\pi)$	2/3			
Isospin C.G. $\Gamma(\eta\pi^+\pi^-)/\Gamma(\eta\pi\pi)$	2/3			
$\gamma\rho^0$ correction from η' $d\sigma/d\Omega$	0.95			
Branching Fraction $\Gamma(K\bar{K}\pi)/\Gamma(\eta\pi\pi)$	0.216	0.010	0.031	0.171 ± 0.013
Branching Fraction $\Gamma(\gamma\rho^0)/\Gamma(\eta\pi\pi)$	0.047	0.010	0.015	0.105 ± 0.022

TABLE III. Relative branching fractions of the $f_1(1285)$ meson, with estimated uncertainties from all sources.

- $K\bar{K}\pi / \eta\pi\pi$ ratio agrees with PDG average
 - (isospin factors applied)
- $\gamma\rho^0 / \eta\pi\pi$ ratio smaller than PDG average by 55%

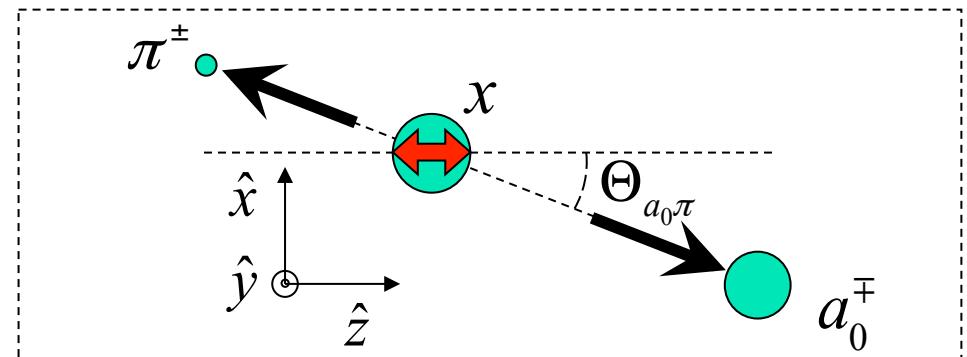


From decay: find spin-parity

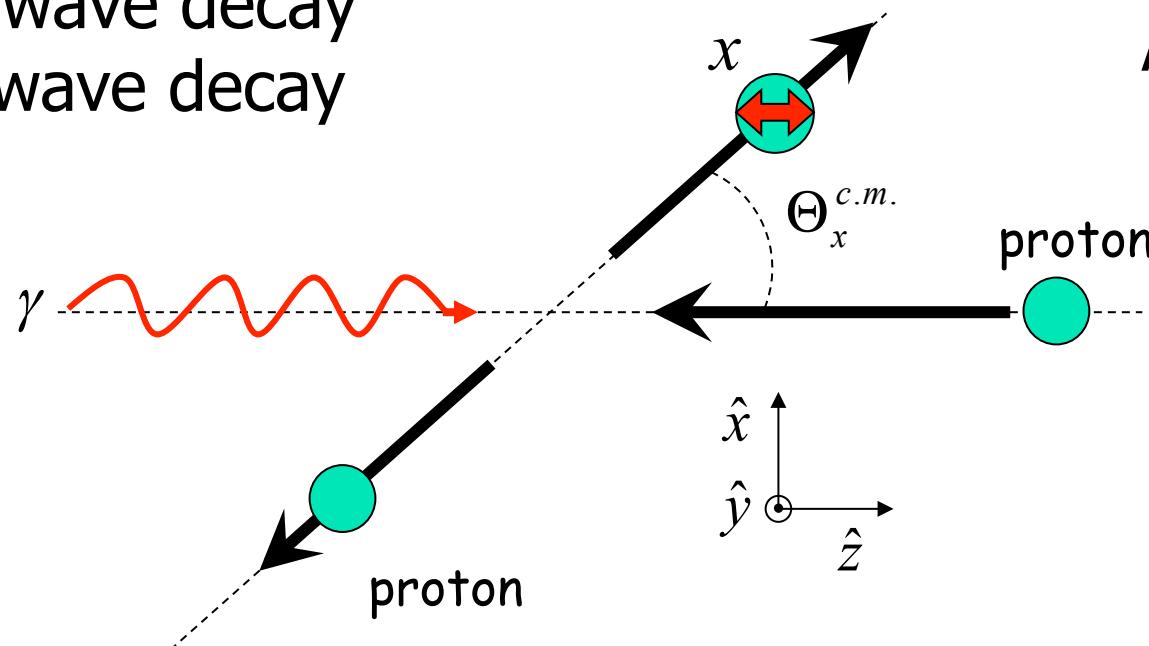
$$x \rightarrow a_0^\pm + \pi^\mp$$

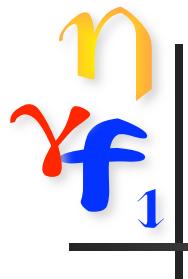
$$J^P \rightarrow 0^+ + 0^- + L^{-1^L}$$

f_1 : p -wave decay
 η : s -wave decay



Adair system



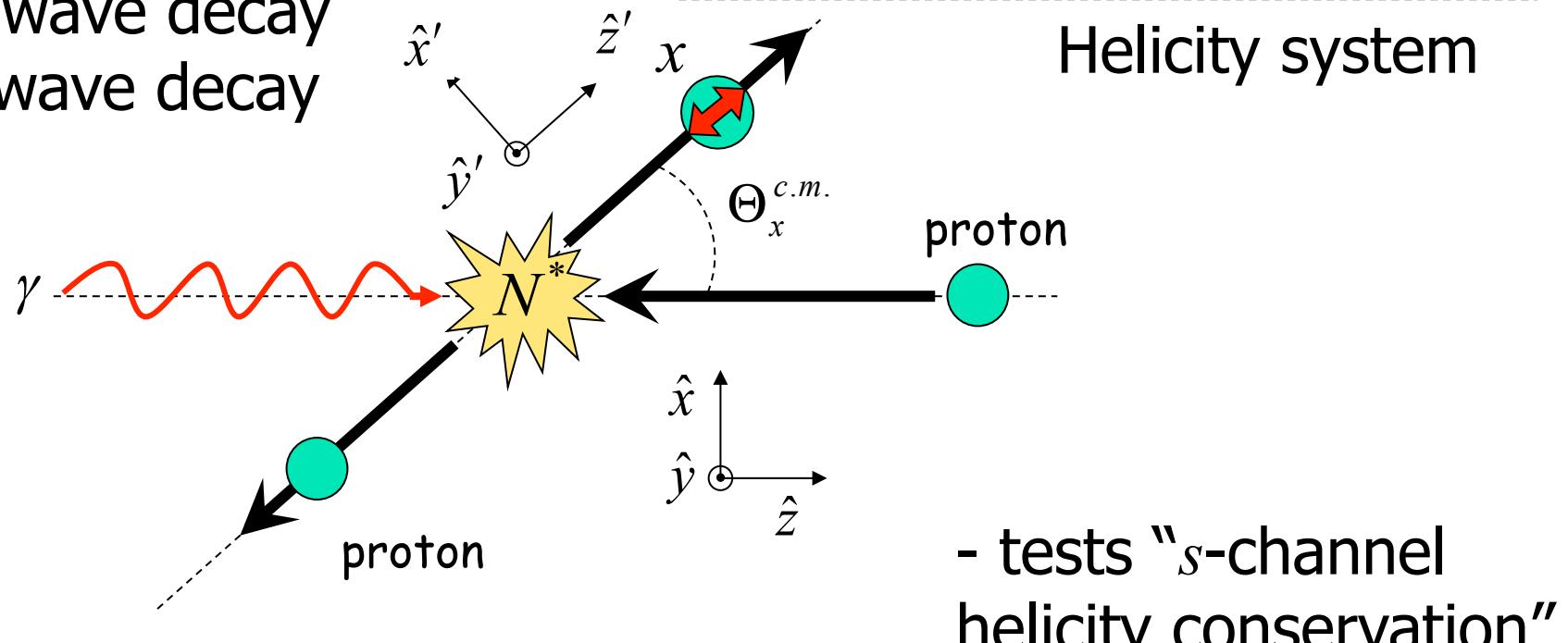


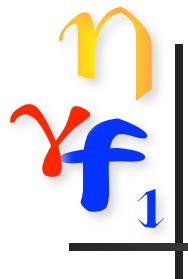
From decay: find spin-parity

$$x \rightarrow a_0^\pm + \pi^\mp$$

$$J^P \rightarrow 0^+ + 0^- + L^{-1^L}$$

f_1 : p -wave decay
 η : s -wave decay

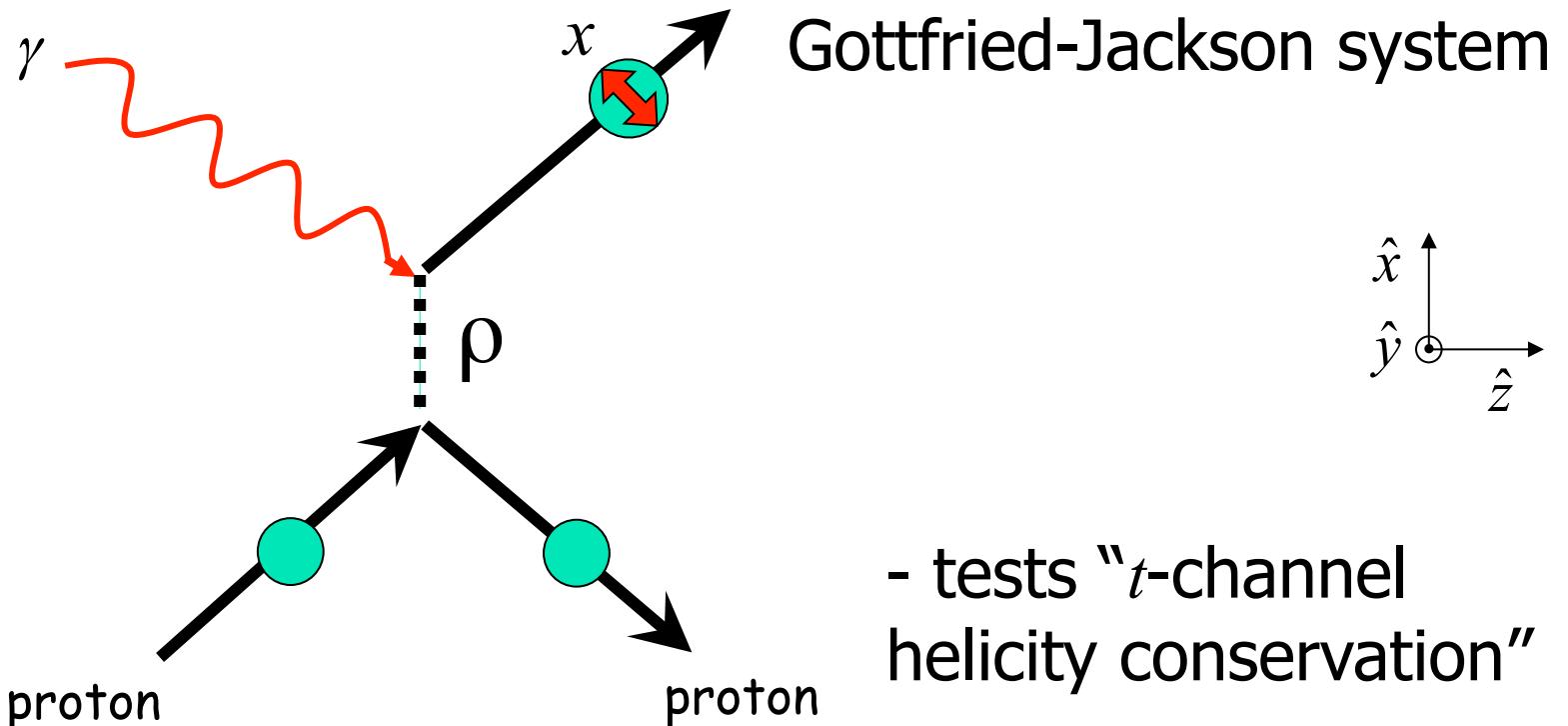
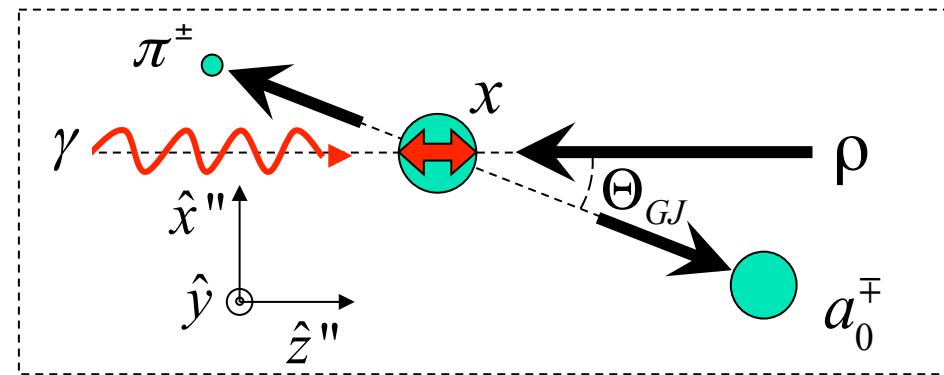




From decay: find spin-parity

$$x \rightarrow a_0^\pm + \pi^\mp$$

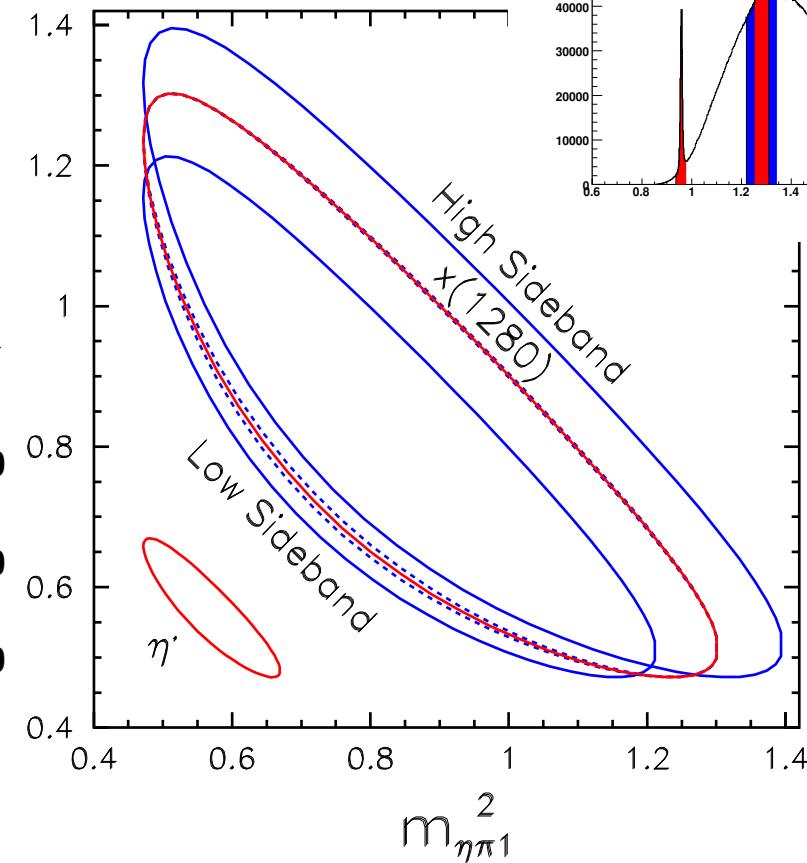
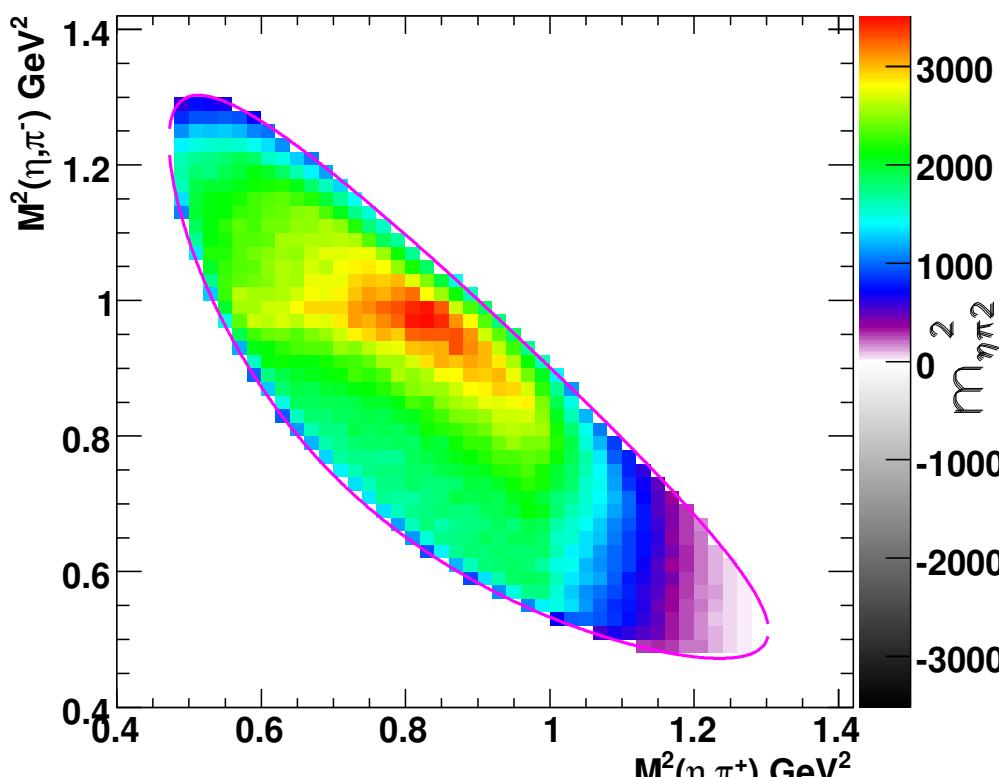
$$J^P \rightarrow 0^+ + 0^- + L^{-1^L}$$



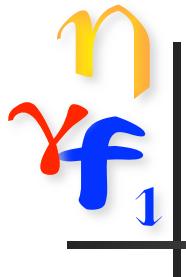


Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

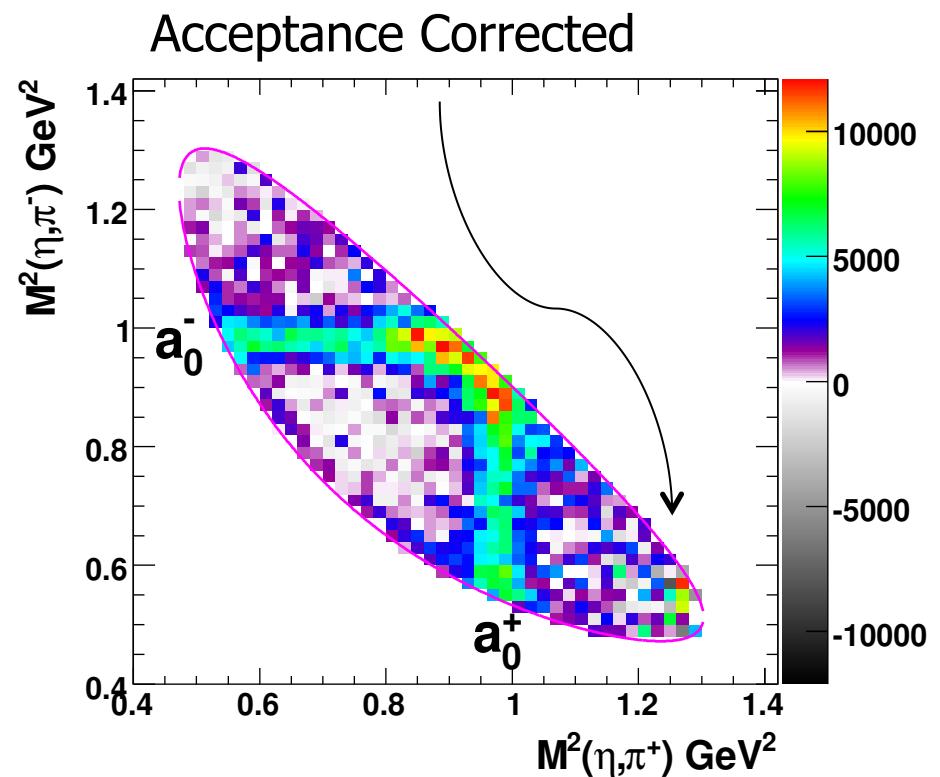
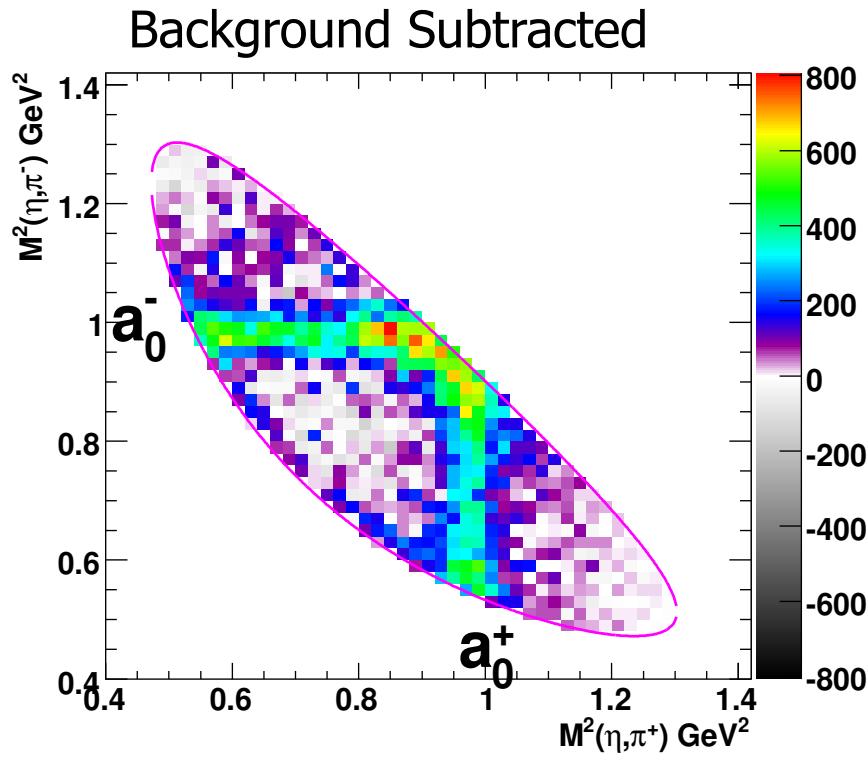
Raw Event Distribution



- Event-by-event, we must rescale meson sidebands to lie within Dalitz plot contour
- Algebraic method developed to do this projection...



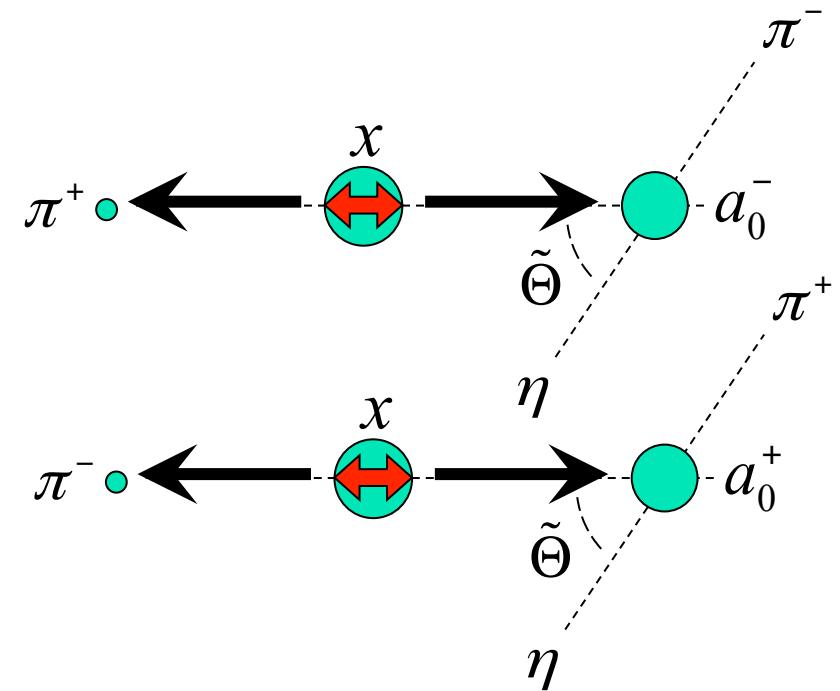
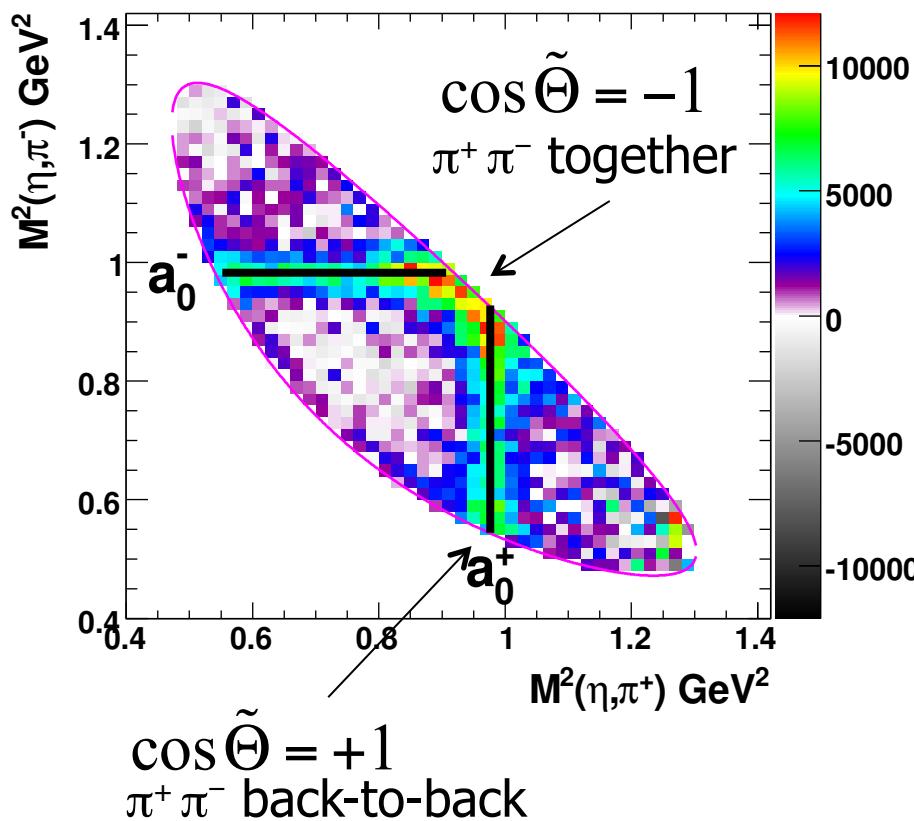
Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$



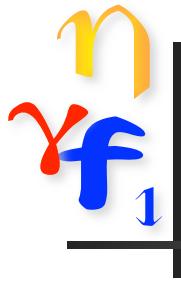
- Subtract huge multi-pion background to reveal...
- ... dominance of decay via $a_0^\pm \pi^\mp$ intermediate state.
- Strong interference of bands seen. Amplitude analysis!



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$



-two amplitudes $A_{m=\pm 1}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+})$ to sum for each event



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

$$A_{m=\pm 1}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) = BW(m_{a_0^+\pi^-}) W_{1,\pm 1}(\Theta_{a_0^+\pi^-}, \phi_{a_0^+\pi^-}) + BW(m_{a_0^-\pi^+}) W_{1,\pm 1}(\Theta_{a_0^-\pi^+}, \phi_{a_0^-\pi^+})$$

$$A_{m=0}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) = BW(m_{a_0^+\pi^-}) \left(W_{1,0}(\Theta_{a_0^+\pi^-}, \phi_{a_0^+\pi^-}) + W_{0,0} \right) + BW(m_{a_0^-\pi^+}) \left(W_{1,0}(\Theta_{a_0^-\pi^+}, \phi_{a_0^-\pi^+}) + W_{0,0} \right)$$

$$BW(m | m_0, \Gamma_0) = \frac{\sqrt{m_0 \Gamma_0}}{m_0^2 - m^2 - im_0 \Gamma_0} \frac{q(m)}{q(m_0)}$$

- a Breit–Wigner for each a_0
- angular distribution in the selected system

$$f_1 : \quad W_{L=1, m=0, \pm 1}(\Theta_H, \phi) = a Y_{1,+1}(\Theta_H, \phi) + b Y_{1,0}(\Theta_H, \phi) + c Y_{1,-1}(\Theta_H, \phi)$$

$$\eta : \quad W_{L=0, m=0}(\Theta_H, \phi) = d Y_{0,0}$$

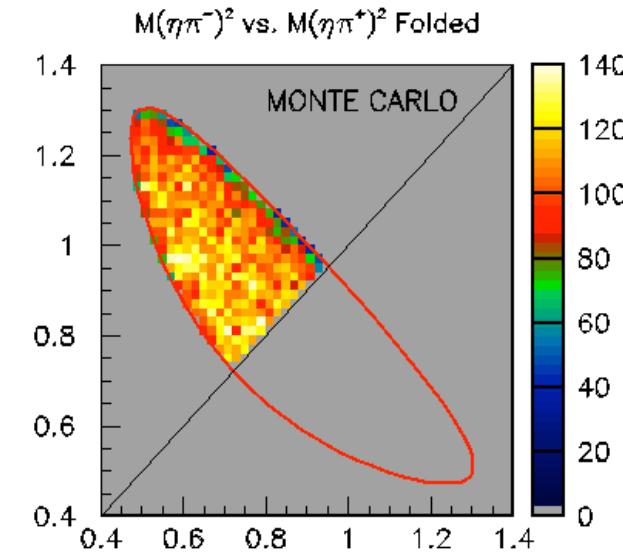
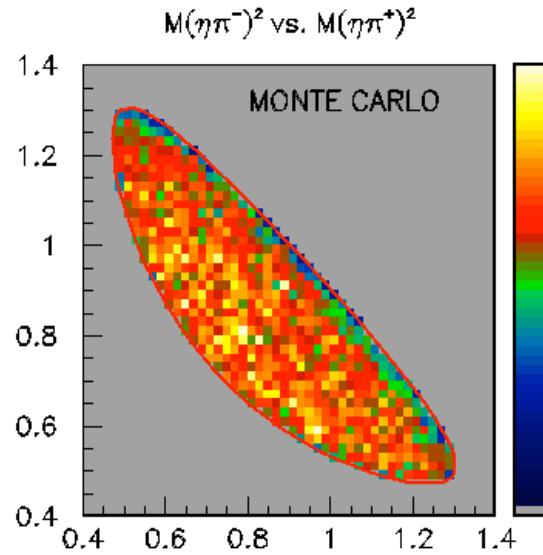
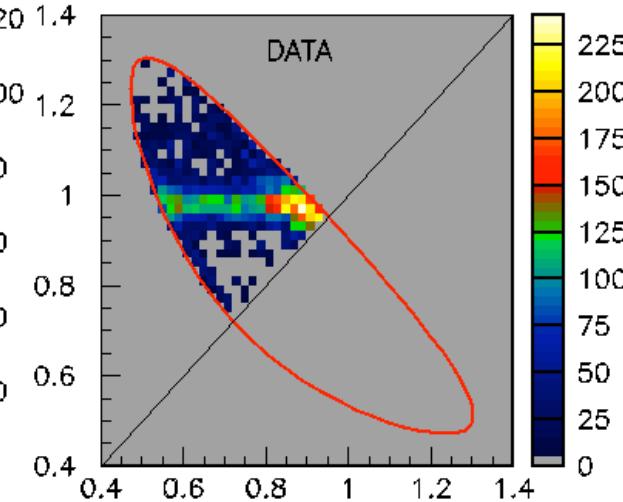
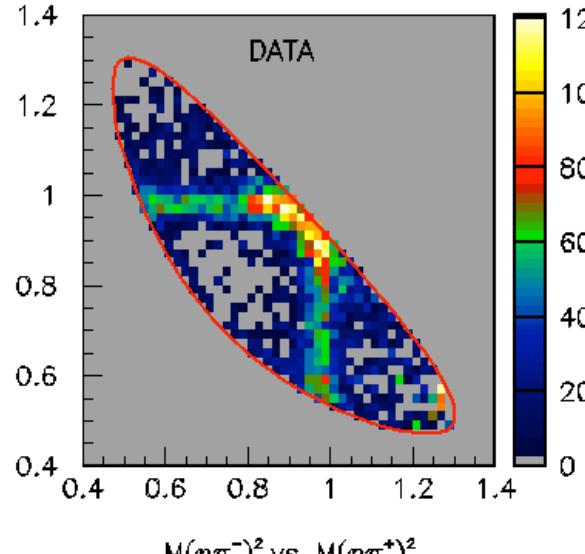
-total decay-weighted magnitude squared

$$T\left(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}\right) = \frac{q(m_{a_0^+\pi^-})}{q(m_0)} \frac{q(m_{a_0^-\pi^+})}{q(m_0)} \left(\left| A_{m=\pm 1}\left(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}\right) \right|^2 + \left| A_{m=0}\left(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}\right) \right|^2 \right)$$



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

$x(1280) \rightarrow \eta \pi\pi$ Dalitz Analysis

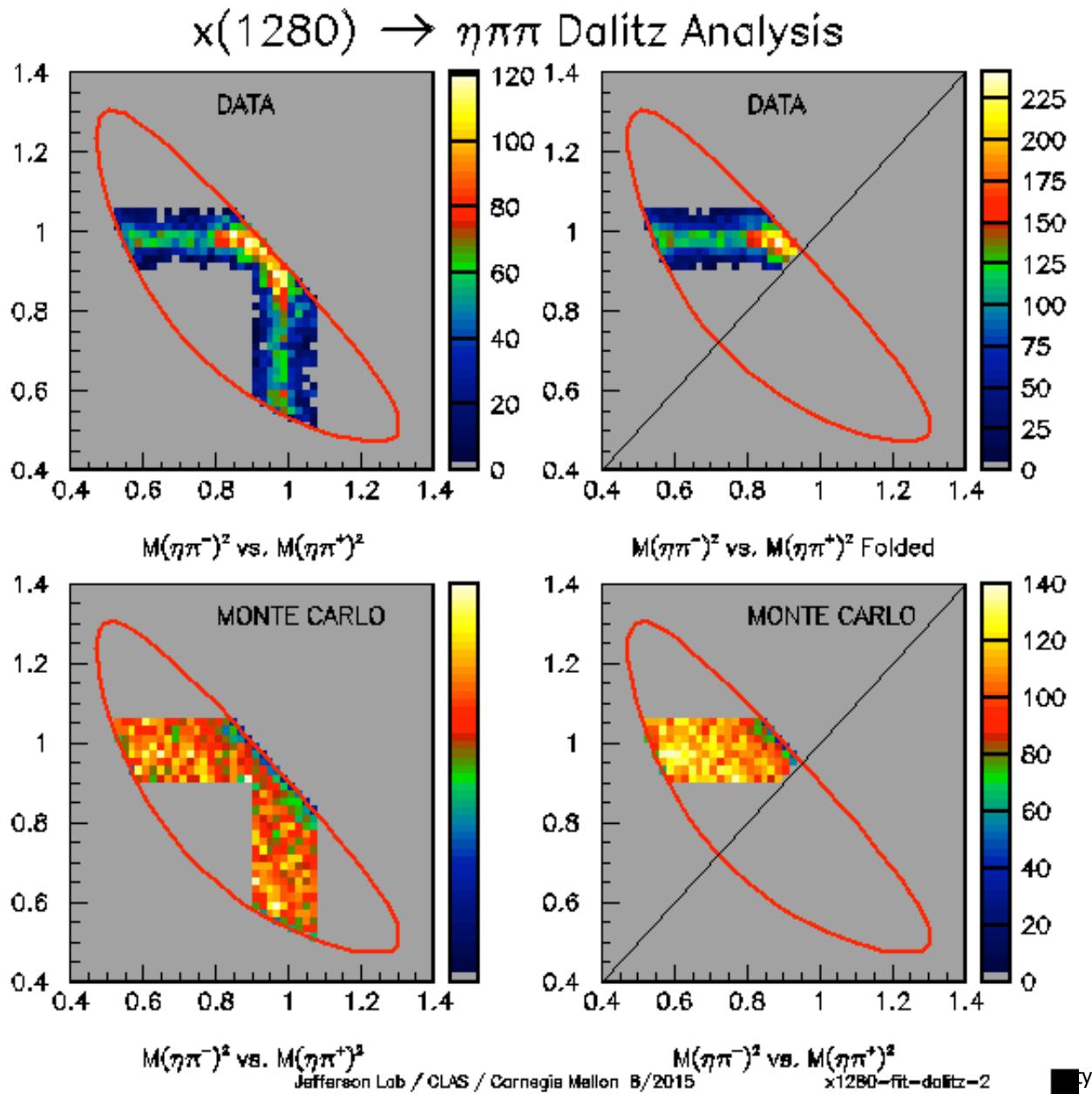


Jefferson Lab / CLAS / Carnegie Mellon 8/2015

- Fold data on symmetry axis
- Generate "phase space" Monte Carlo events with finite width of meson and CLAS resolution included
- "Weight" the events with amplitude-based intensity



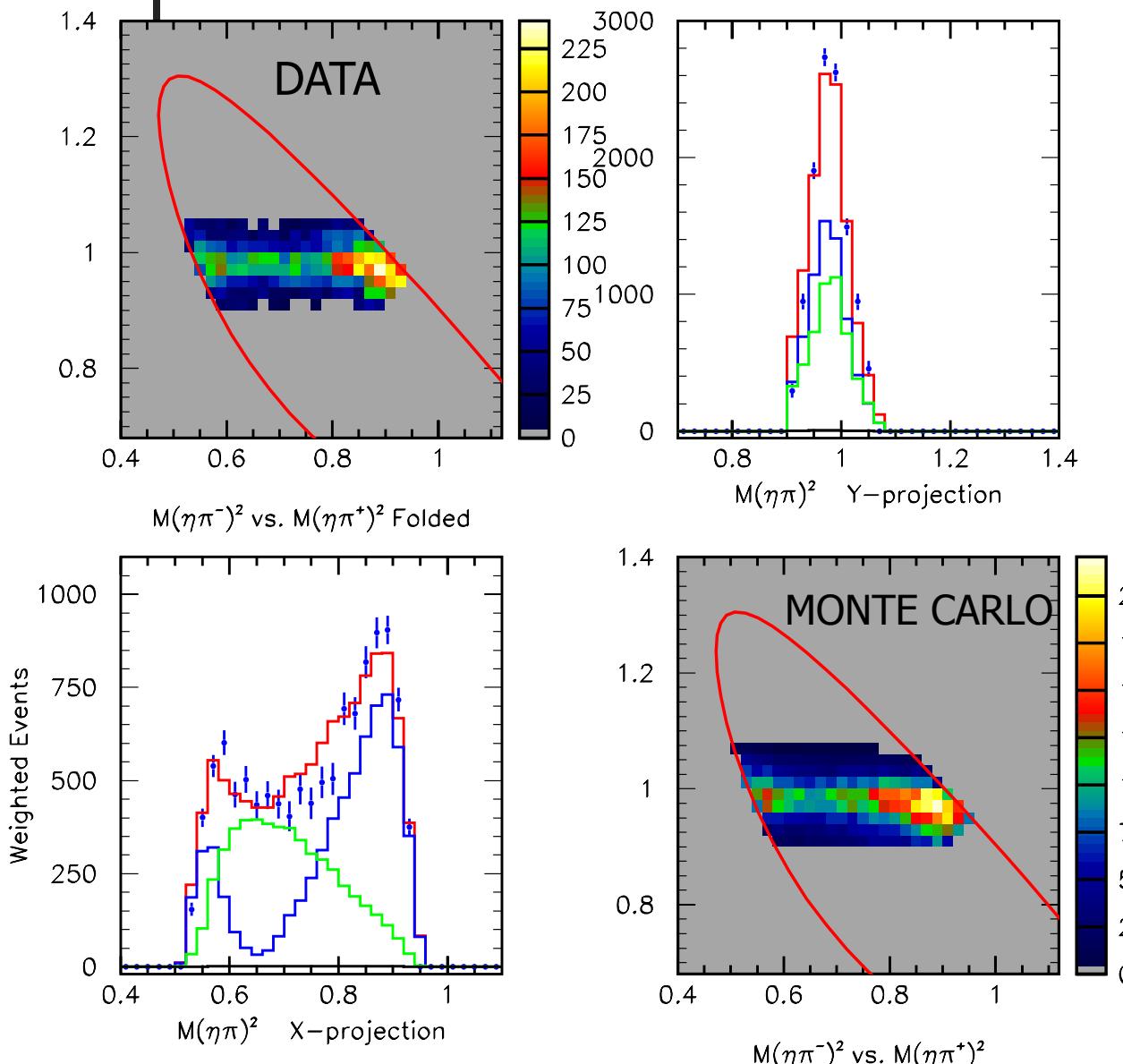
Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$



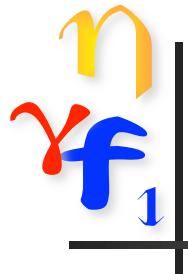
- Fit to full plot did not converge, so trim data to focus on 'bands'.
- Structure in unweighted Monte Carlo due to finite width and resolution effects



Helicity system fit



- *s*-channel helicity system
- Components:
 - Blue: L=1, m=0
 - Green: L=1, m=±1
 - Red: Total
- a_0^\pm interference reproduced
- *p*-wave decay and negative parity demonstrated
- Decaying meson is definitely the $f_1(1285)$



Helicity system fit

- The $f_1(1285)$ is “aligned” in the helicity system.
- The mix of $m = 0$ and $m = \pm 1$ is a property of the production mechanism in the range $2.30 < W < 2.80$ GeV.

$$P_{\pm} : P_0 = 31.8 : 69.2, \pm 1.4\%.$$

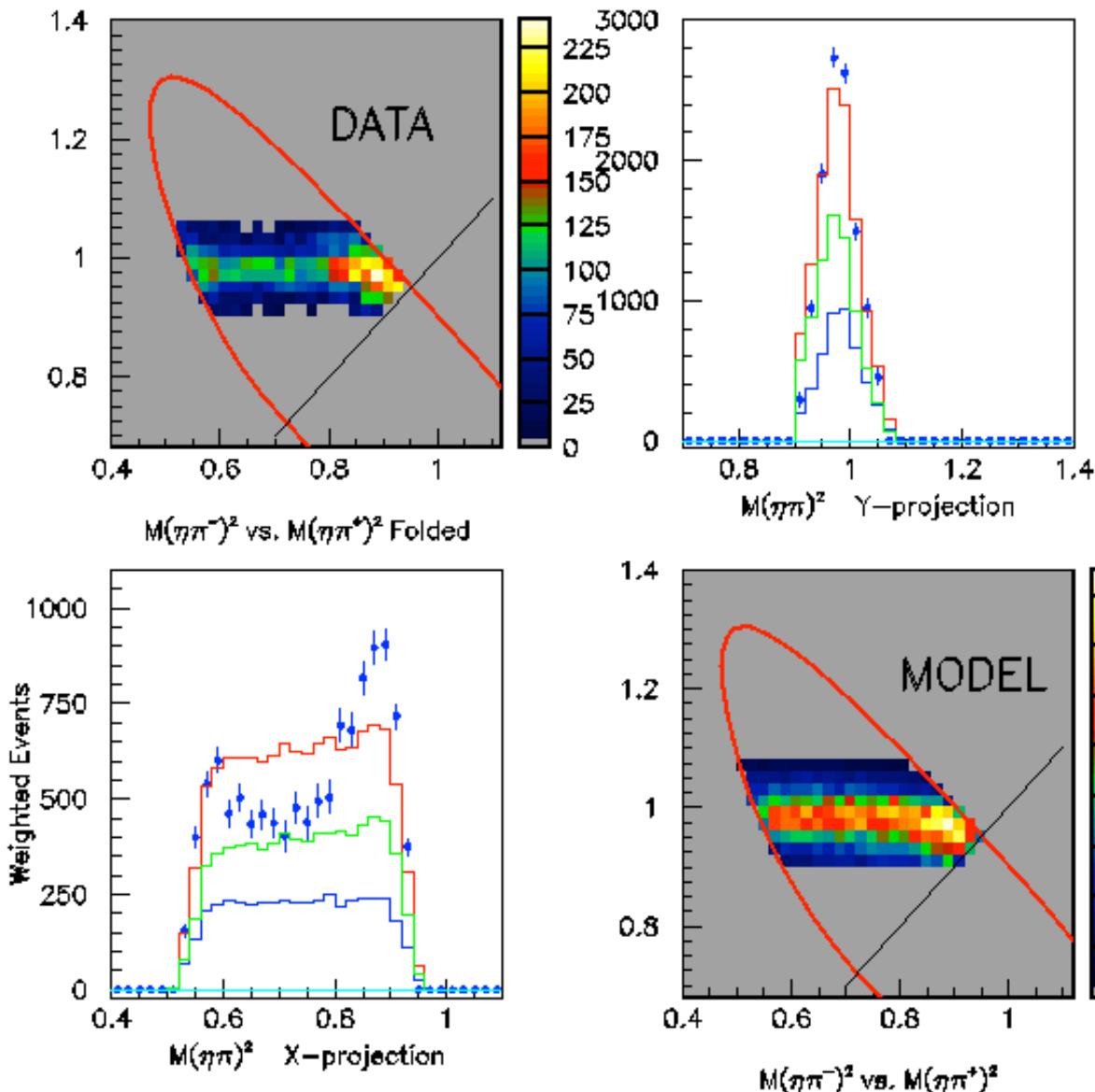
- Discuss later...
- We also measure the ratio

$$\frac{\Gamma(a_0\pi(noKK))}{\Gamma(\eta\pi\pi(total))} = 74 \pm 2(stat) \pm 9(syst)\%$$

- Agrees with PDG value



Gottfried-Jackson system fit

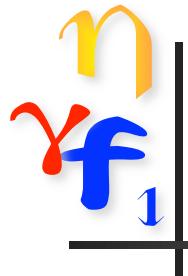


- t -channel helicity system
- Components:
 - Blue: $L=1, m=0$
 - Green: $L=1, m=\pm 1$
 - Red: Total
 - Cyan: $L=0$ fit
- a_0 interference NOT reproduced
- Decaying meson is not aligned in this system



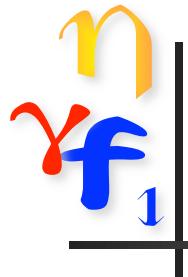
Properties of $f_1(1285)$ and $\eta(1295)$

	$f_1(1285)$	$\eta(1295)$	CLAS m_x
$I^G(J^{PC})$	$0^+(1^{++})$	$0^+(0^{++})$	$J^P = 1^+$
Mass (MeV)	$1281.9 \pm .5$	1294 ± 4	1281.0 ± 0.8
Width, Γ (MeV)	24.2 ± 1.1	55 ± 5	18.4 ± 1.4
Decays:			
4π	$33 \pm 2\%$	-	-
$\eta \pi \pi$	$52 \pm 2\%$	Seen	-
$\frac{\Gamma(a_0 \pi (no KK))}{\Gamma(\eta \pi \pi (total))}$	$69 \pm 13\%$	-	$74 \pm 9\%$
$\frac{\Gamma(K \bar{K} \pi)}{\Gamma(\eta \pi \pi)}$	$17.1 \pm 1.3\%$	-	$21.6 \pm 3.1\%$
$\frac{\Gamma(\gamma \rho^0)}{\Gamma(\eta \pi \pi)}$	$10.5 \pm 2.2\%$	Not seen	$4.7 \pm 1.8\%$



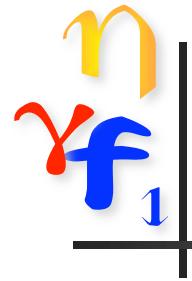
Speculation re $f_1(1285)$ production

- Alignment in helicity system suggests s -channel N^* production decays to $f_1(1285) p$
 - Can we infer J^P of the N^* baryon resonance?
 - $3/2^+ \rightarrow 1^+ + 1/2^+$ in s -wave leads to $P_\pm : P_0 = 1 : 2$ as seen in the data
 - $1/2^+ \rightarrow 1^+ + 1/2^+$ in s -wave leads to $P_\pm : P_0 = 2 : 1$, opposite to what data show
- But there are no known N^* states with low J at $W \sim 2.5$ GeV, so the question remains open



Conclusions

- The photoproduced meson CLAS sees at 1281 MeV is the $f_1(1285)$.
- The production mechanism is more consistent with N^* -decay (s -channel) than meson-exchange (t -channel)
 - Cross section is much "flatter" than η' production
 - The $f_1(1285)$ is aligned in the s -channel helicity system, as seen in the $\eta \pi^+ \pi^-$ Dalitz-plot amplitude analysis
- $\Gamma \sim 18.2$ MeV; narrower than PDG average
- Branching ratios measured:
 - $K K \pi / \eta \pi \pi$, $a_0 \pi / \eta \pi \pi$ and $\gamma \rho^0 / \eta \pi \pi$

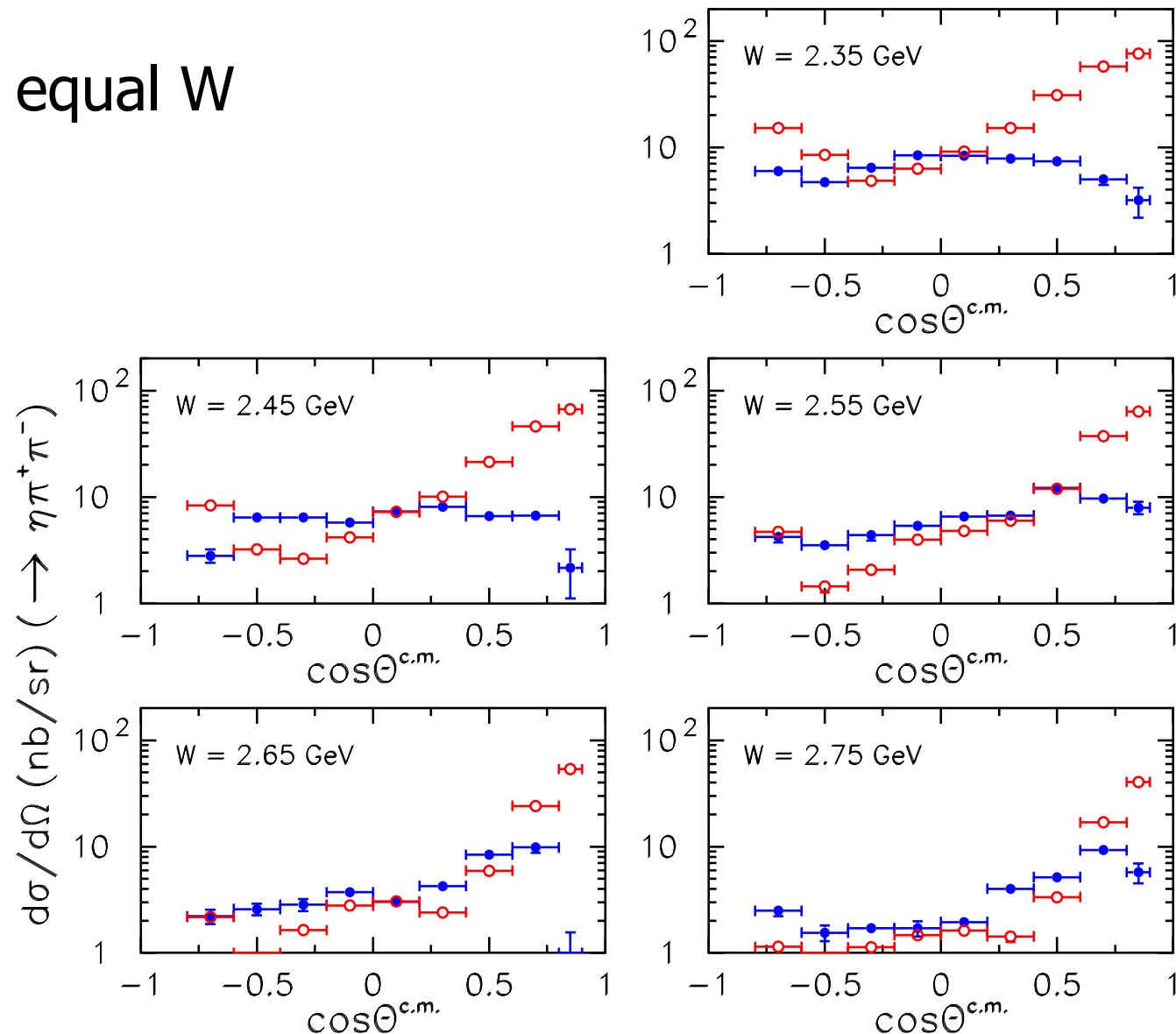


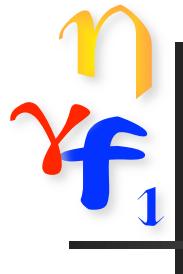
Backup Slides



Compare meson types

At equal W





Compare meson types

At equal excess energy
above threshold

