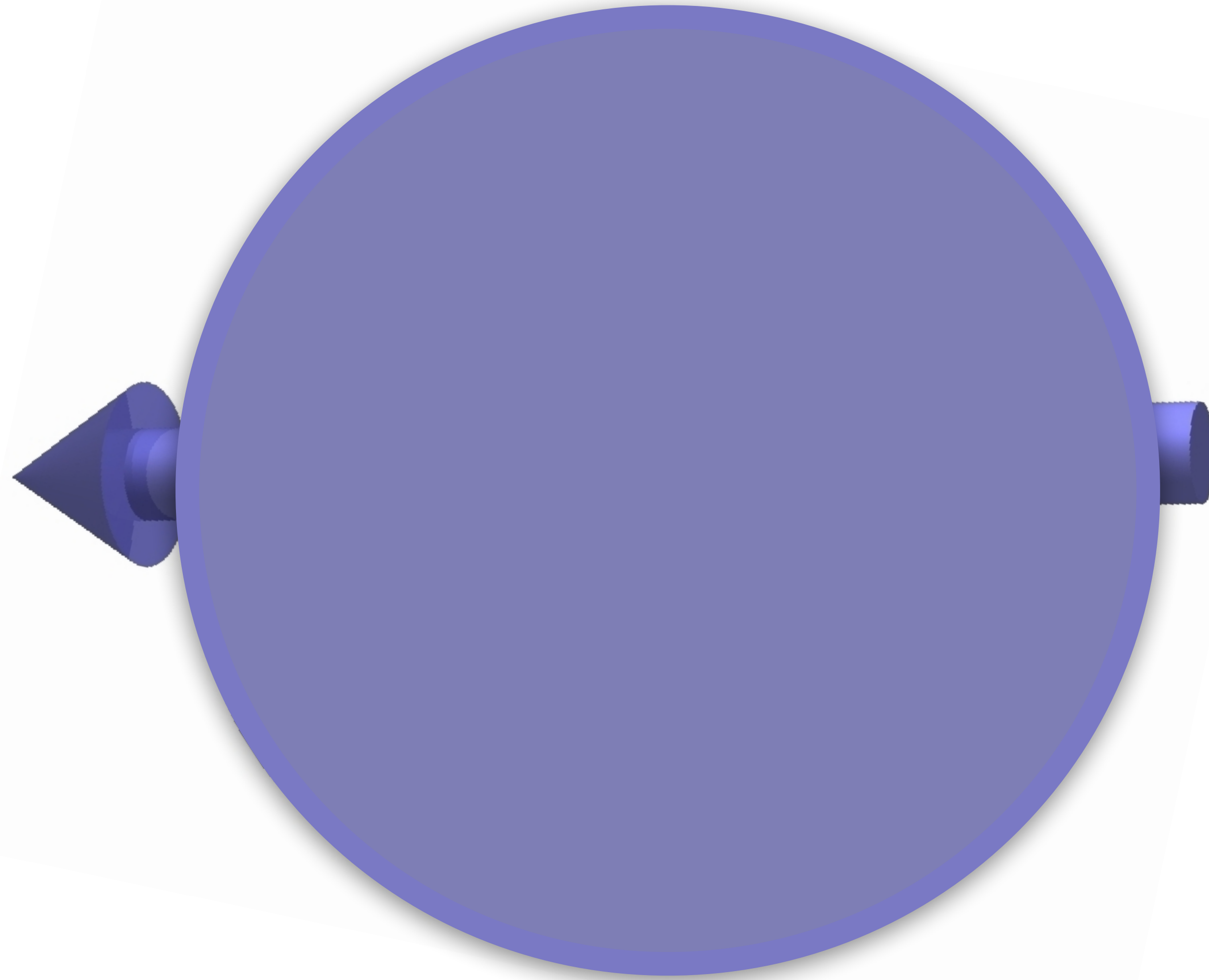


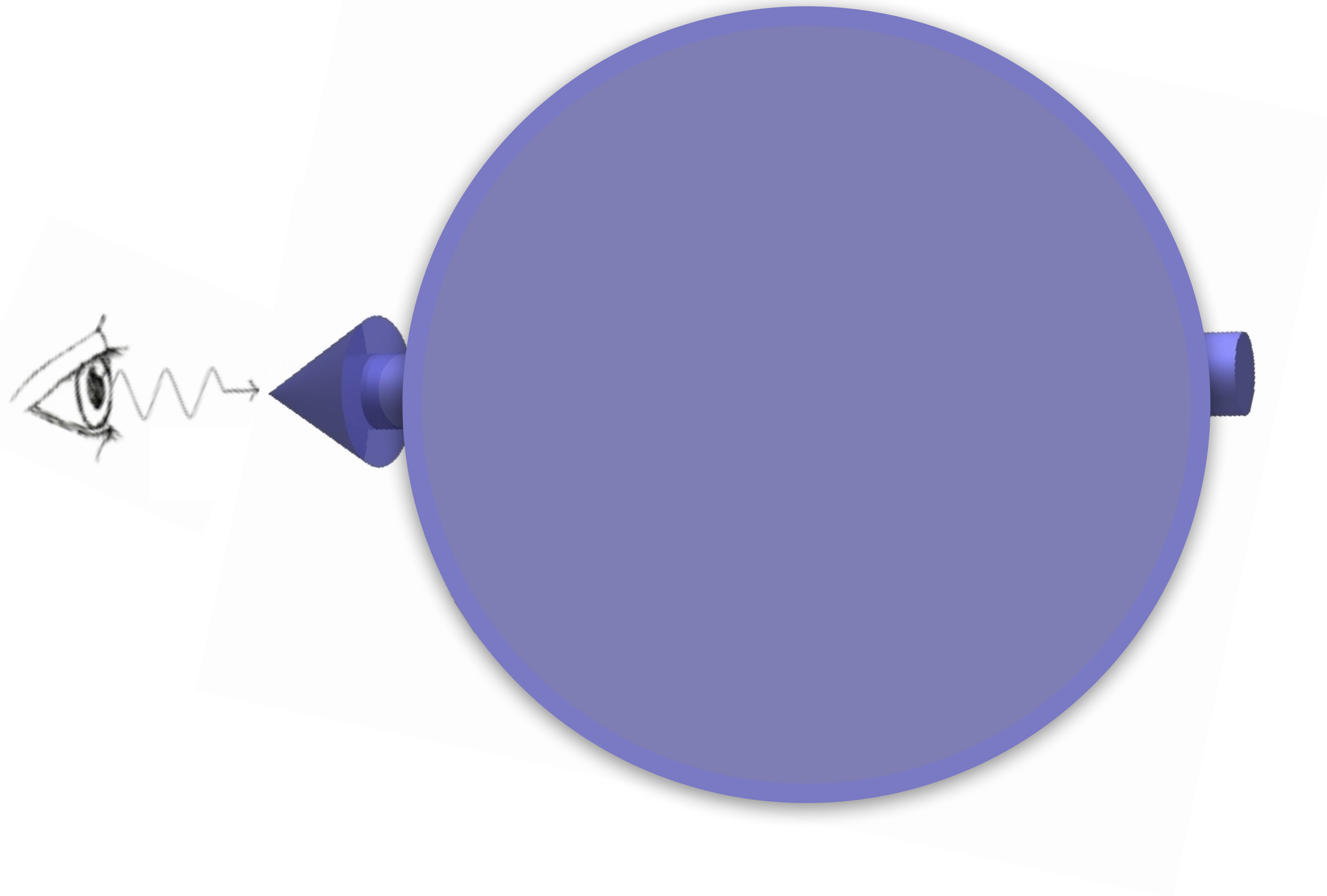
The spin structure of the proton from JLab to the LHC

Charlotte Van Hulse
VUB

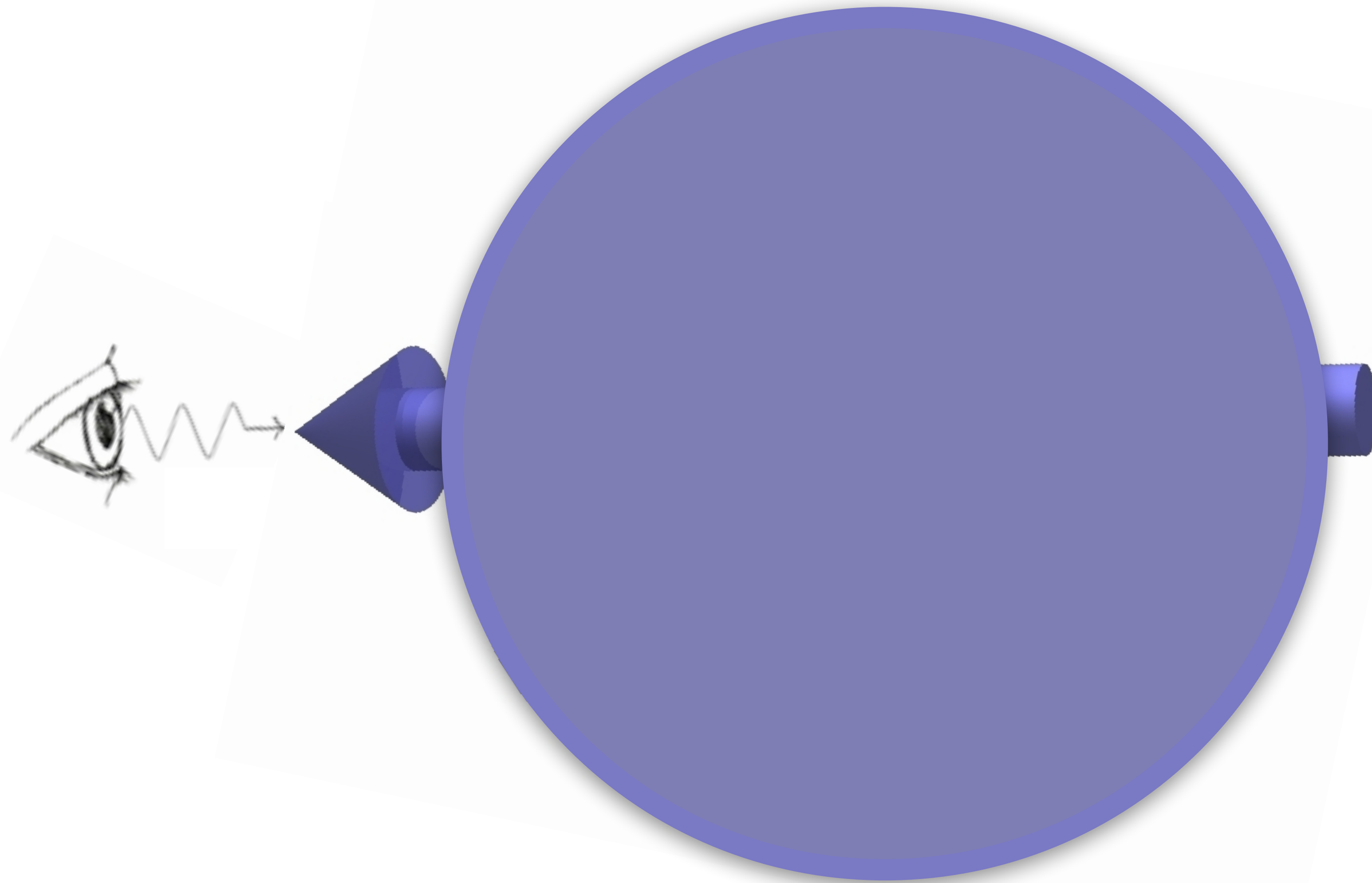
How it started



How it started



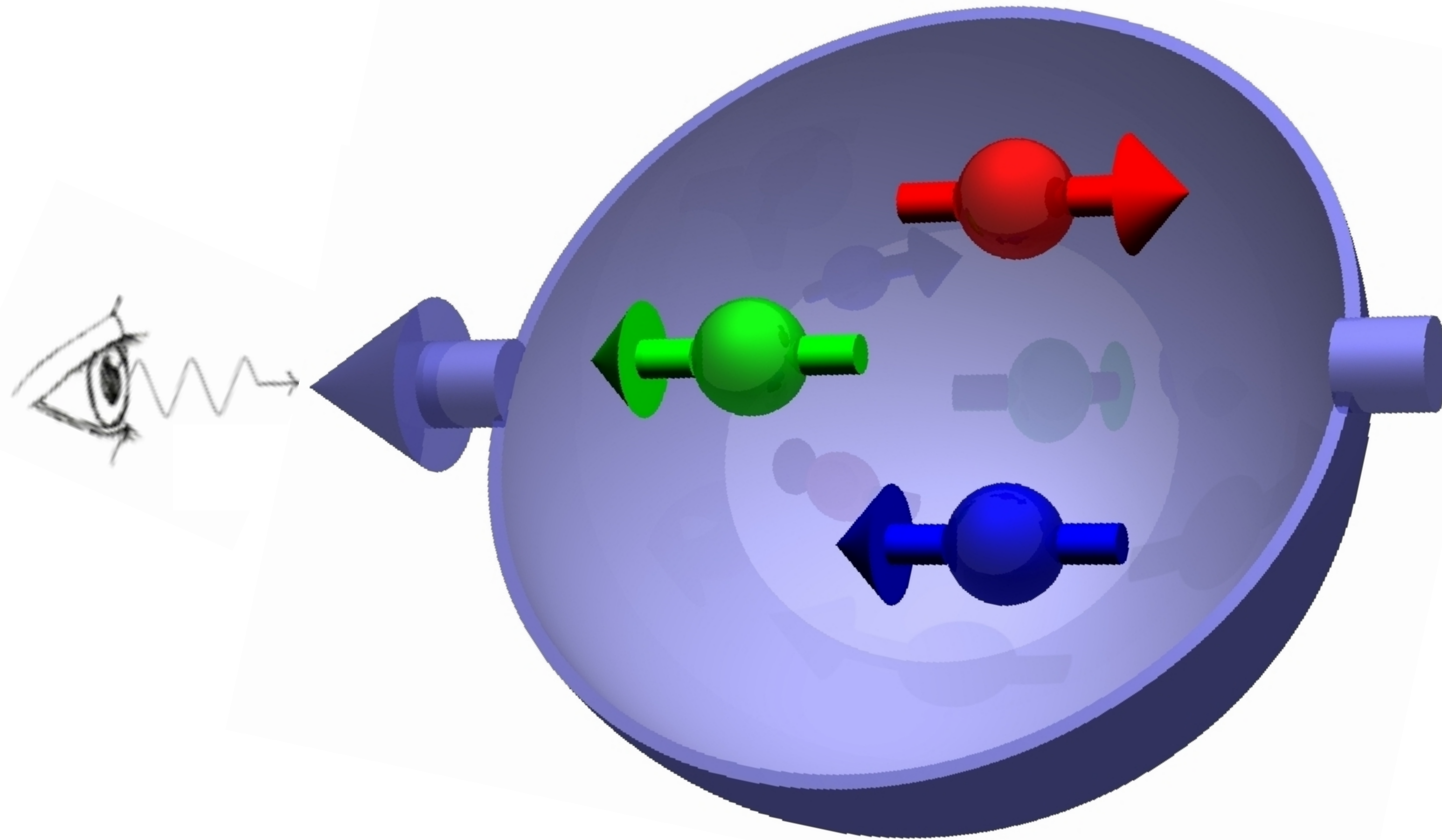
How it started



Proton spin = $\frac{1}{2}$

What is its origin?

How it started

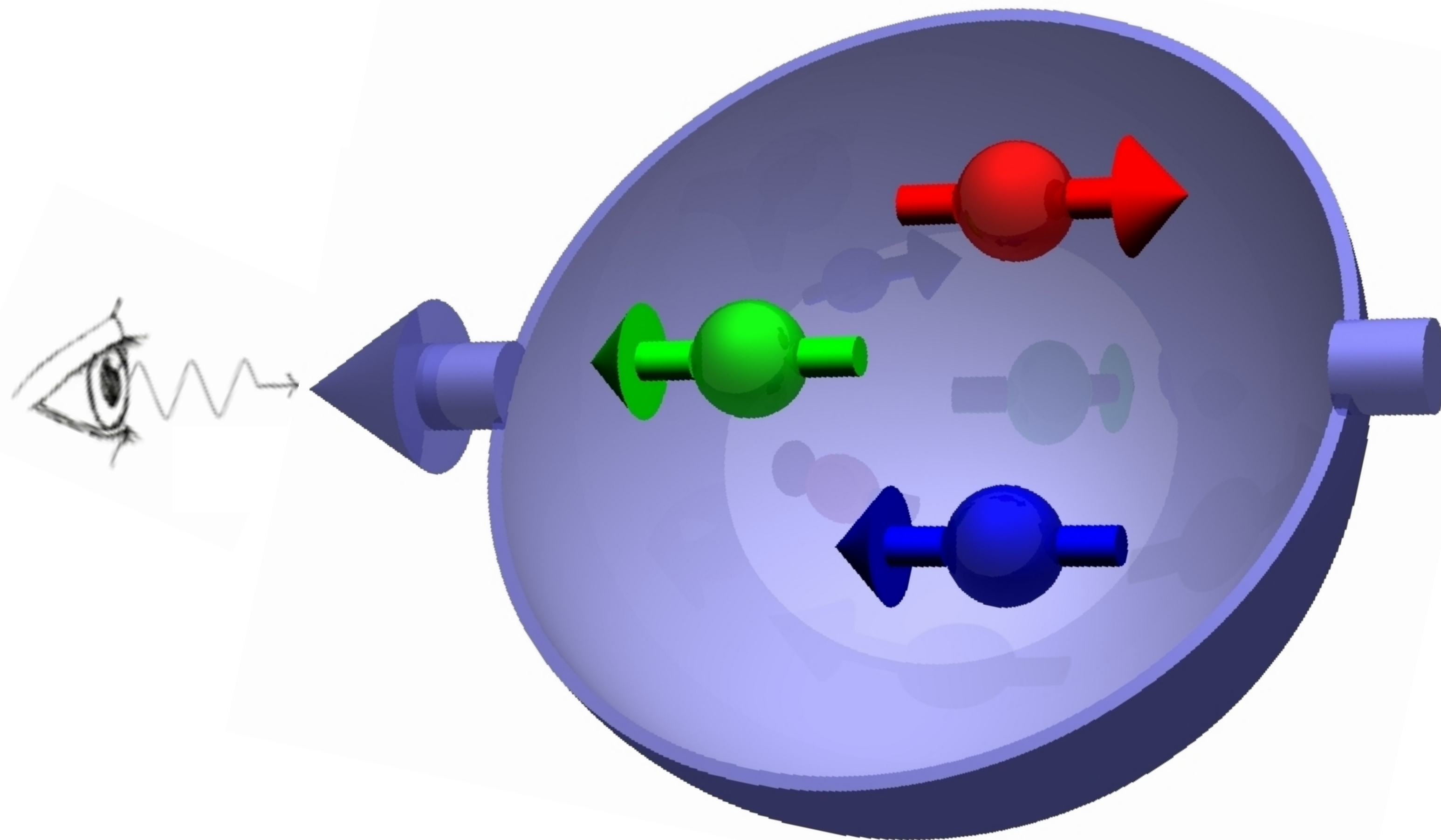


- Naive constituent quark model:

$$\frac{1}{2} = \sum \text{quark spin}$$

$$= \frac{1}{2} \Delta \Sigma$$

How it started

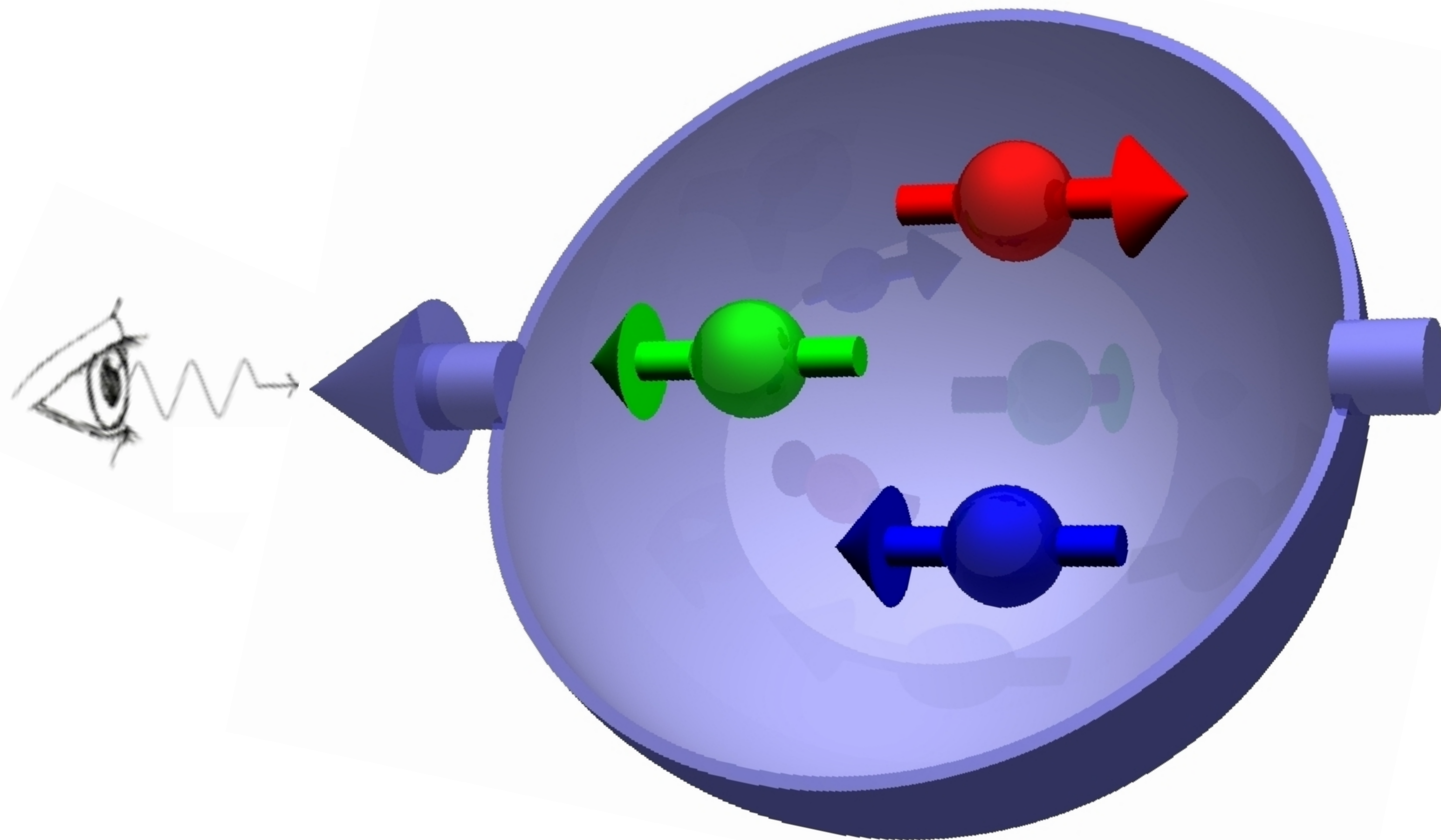


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How it started



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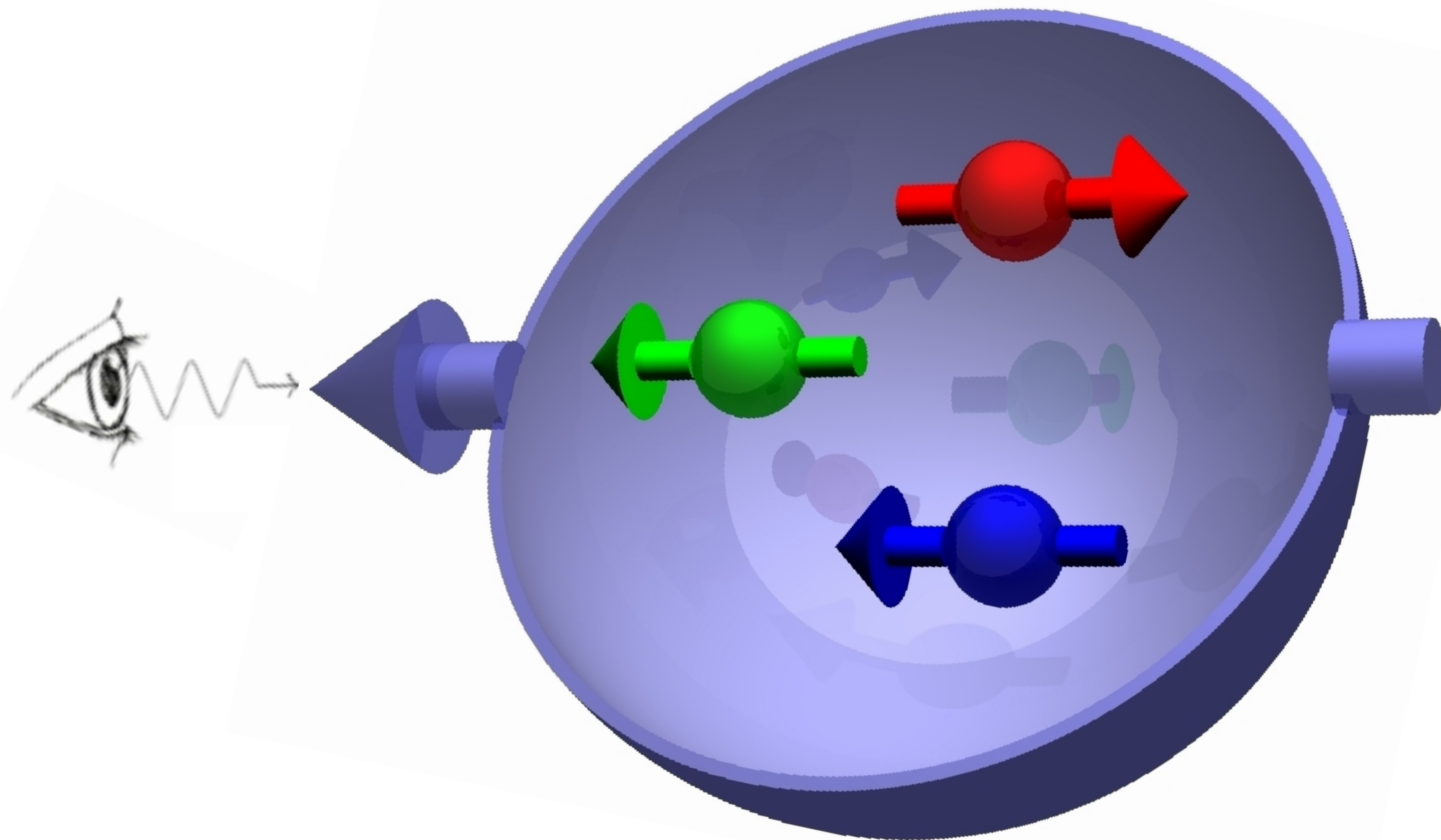
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$$\Delta\Sigma \approx 0.65$$

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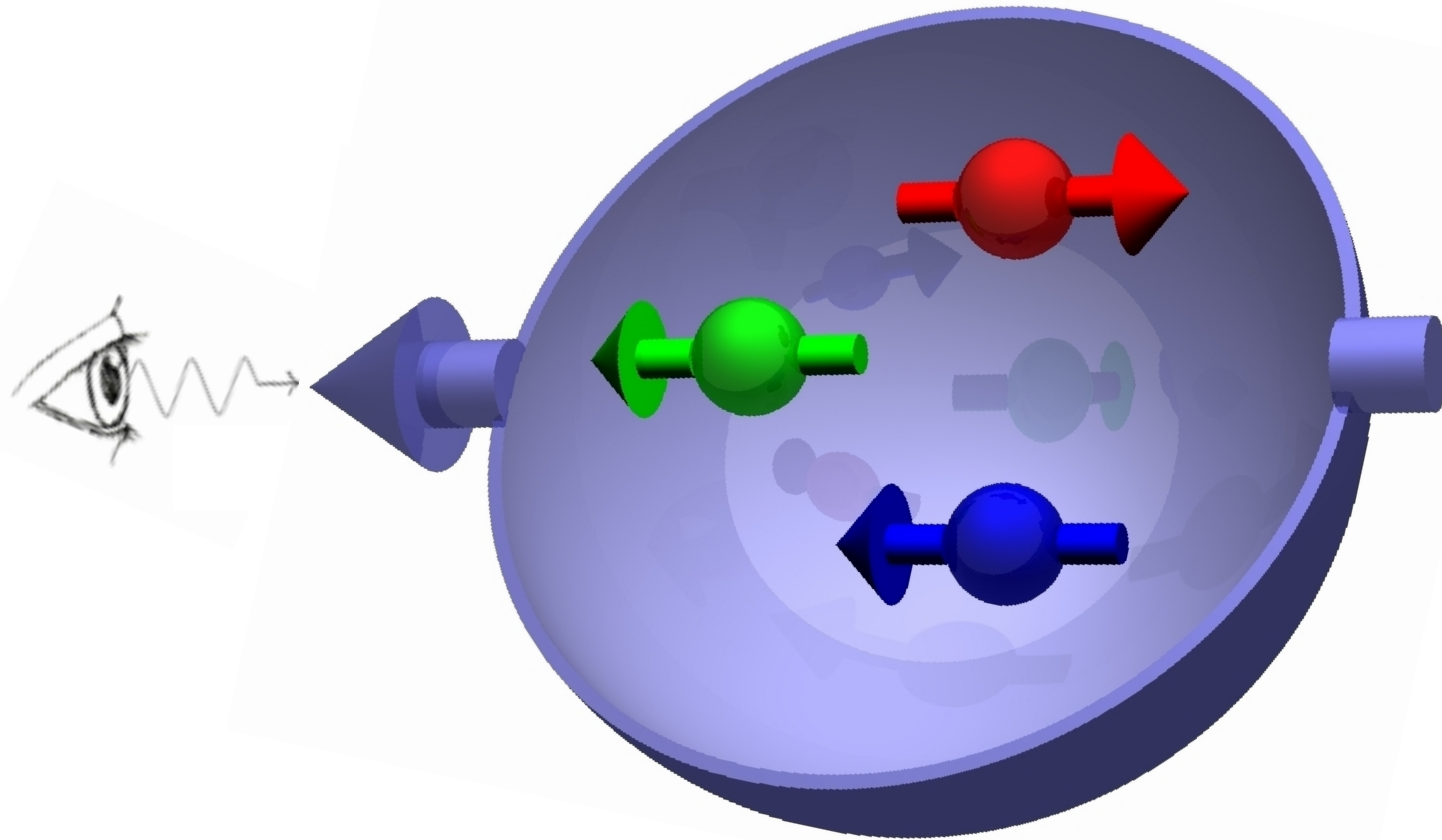
$$\Delta\Sigma \approx 0.65$$

- First measurement: EMC 1988

$$\Delta\Sigma = \Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s}$$

with $\Delta q = \overrightarrow{q} - \overleftarrow{q}$: helicity parton distribution function (PDF)

How it started



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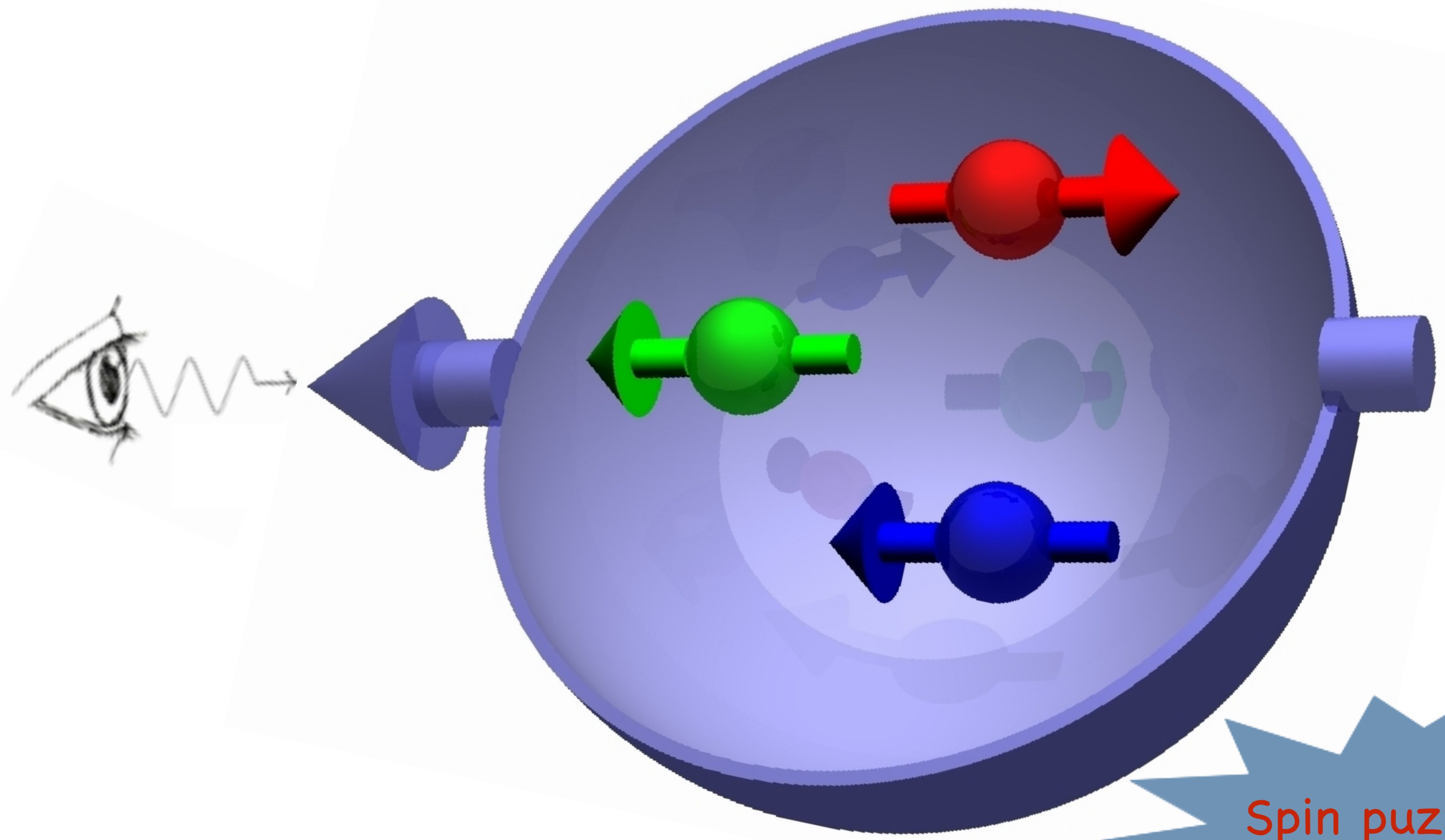
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$$\begin{aligned} \Delta\Sigma &= \Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s} \\ &= 0.14 \pm 0.09 \pm 0.21 \end{aligned}$$

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How it started



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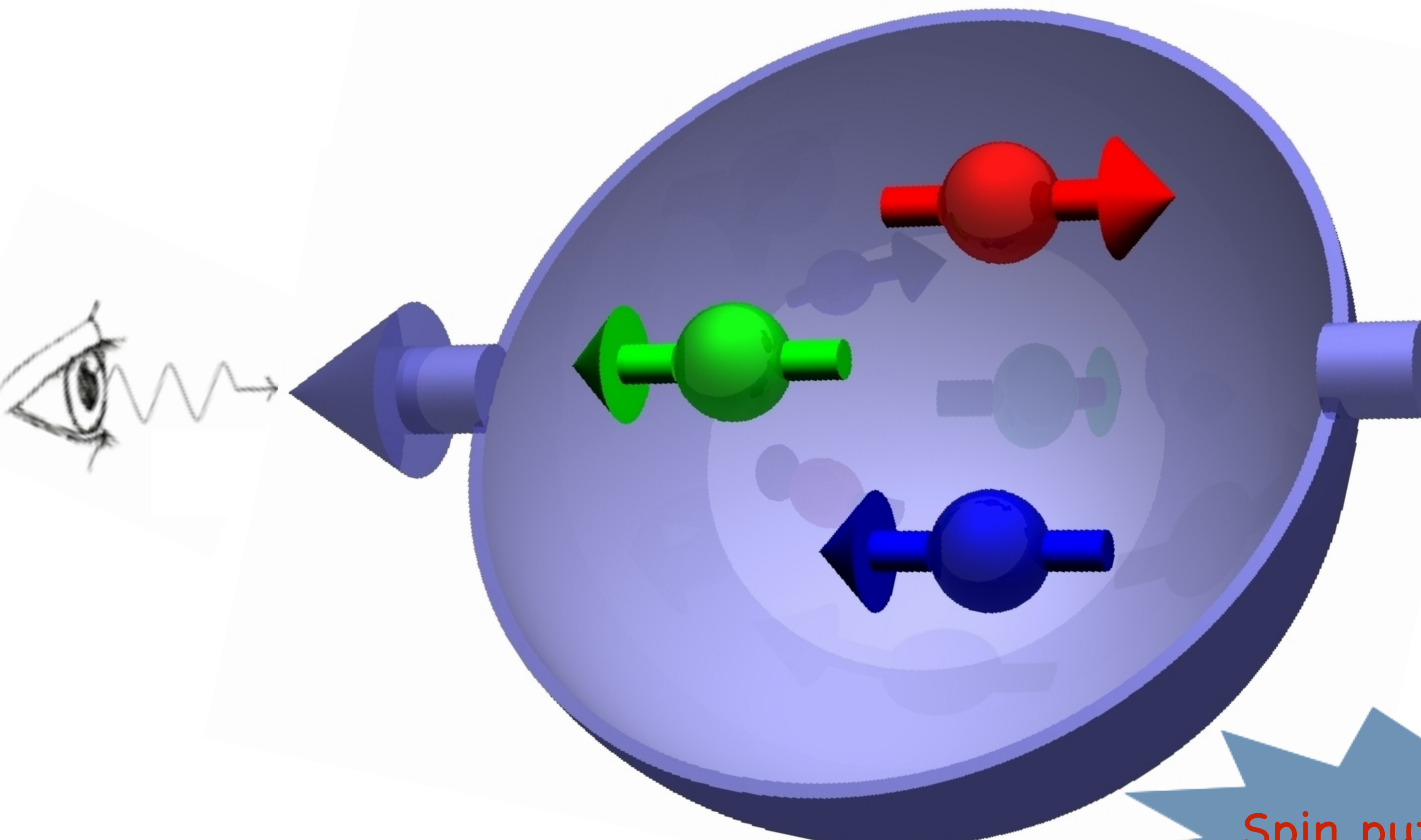
Spin puzzle

$$\Delta\Sigma = \Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s}$$

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How it started



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$$\Delta\Sigma = \Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s}$$

$$0.00 \pm 0.21$$

Spin puzzle

Spin crisis!

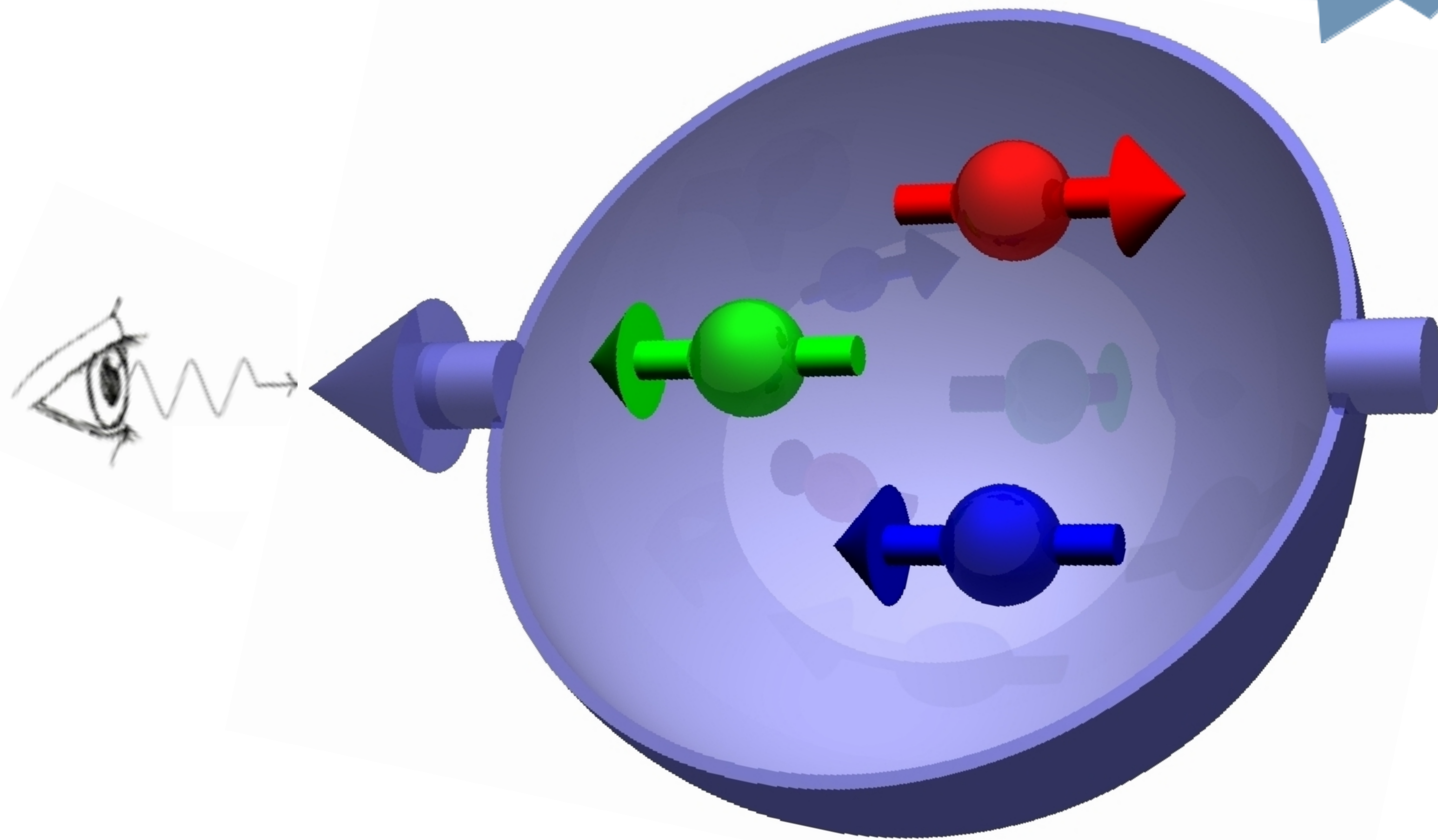
with $\Delta q = \int_0^1 q(x) dx$

parton distribution function (PDF)

How it started

Spin puzzle

Birth of new experiments:
SMC, HERMES, JLab, COMPASS

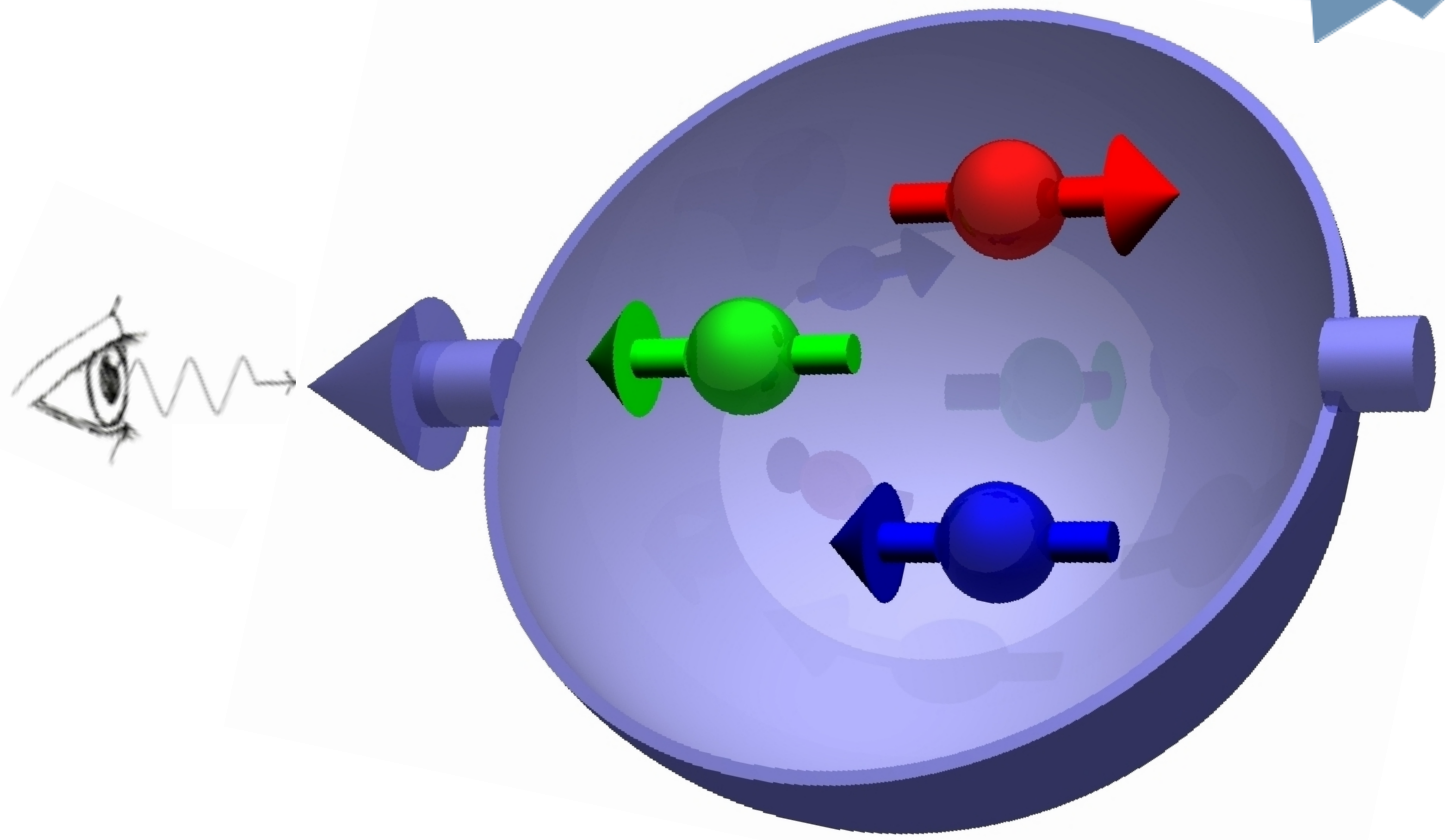


How it started

Spin puzzle

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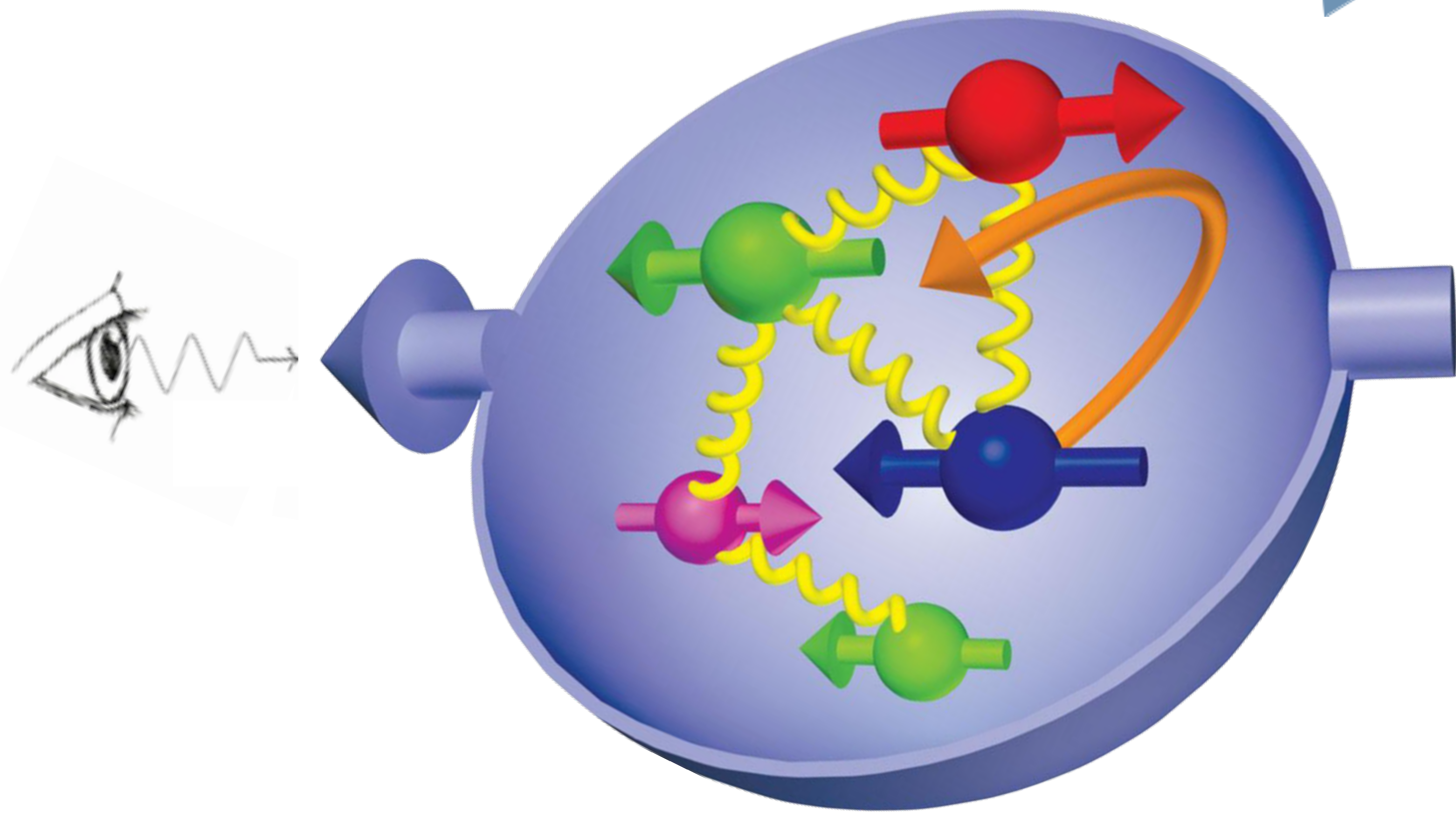
- Check EMC result



How it started

Spin puzzle

Birth of new experiments:
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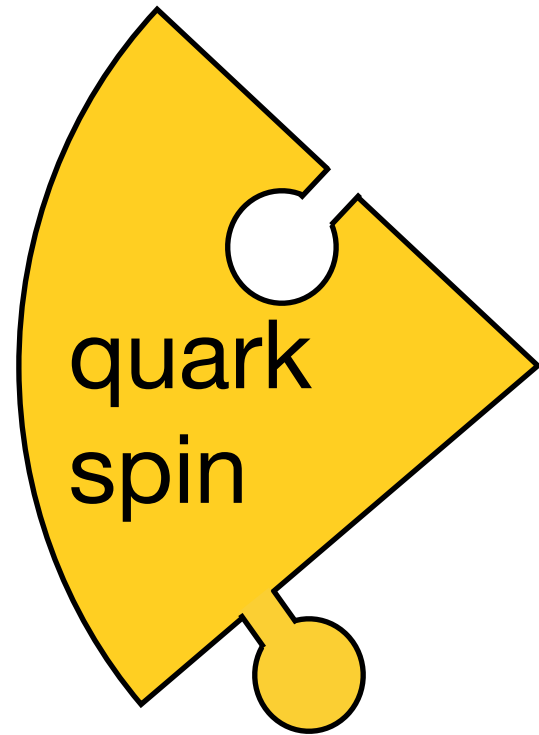
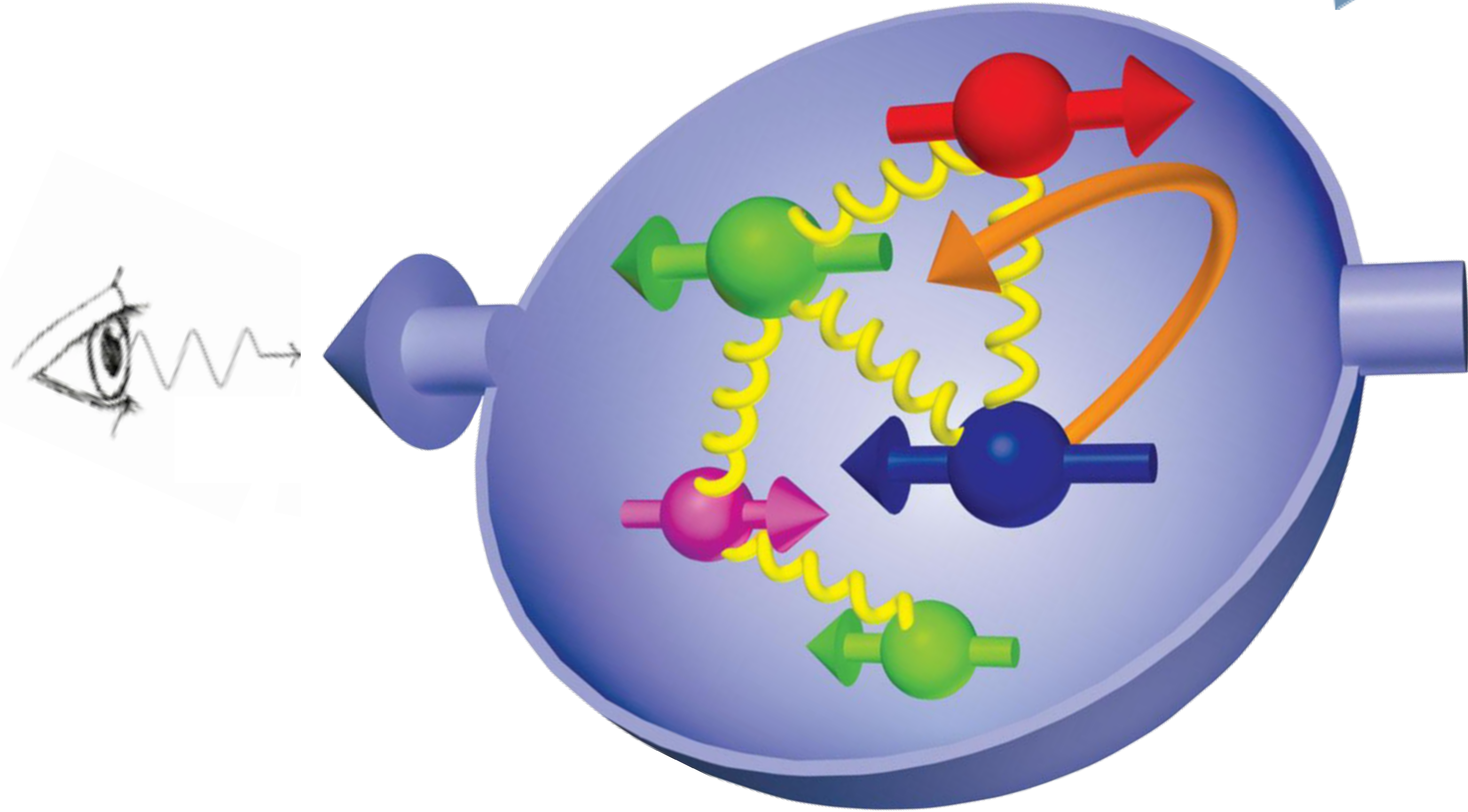
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- Find missing contributions

How it started

Spin puzzle

Birth of new experiments:
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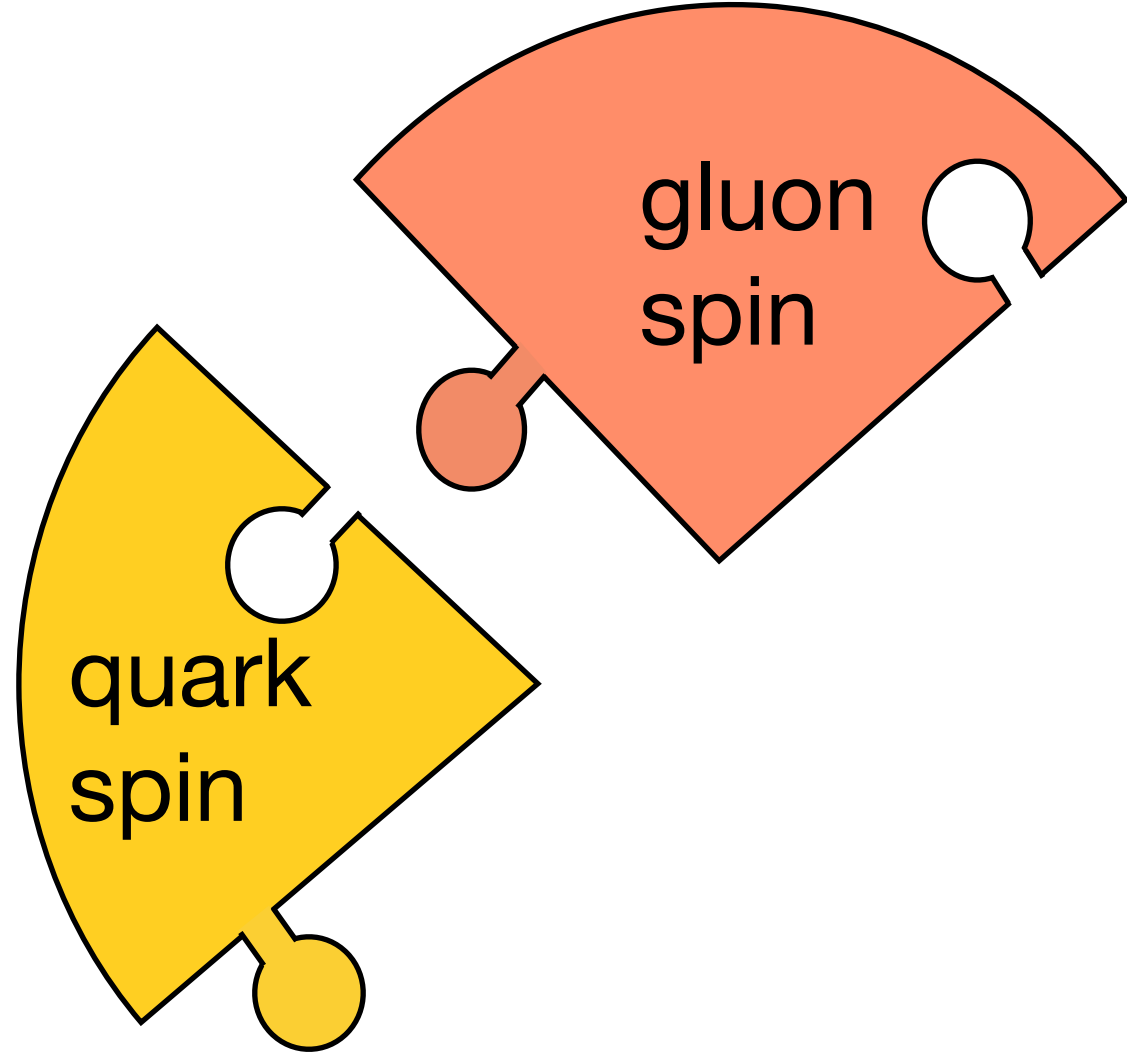
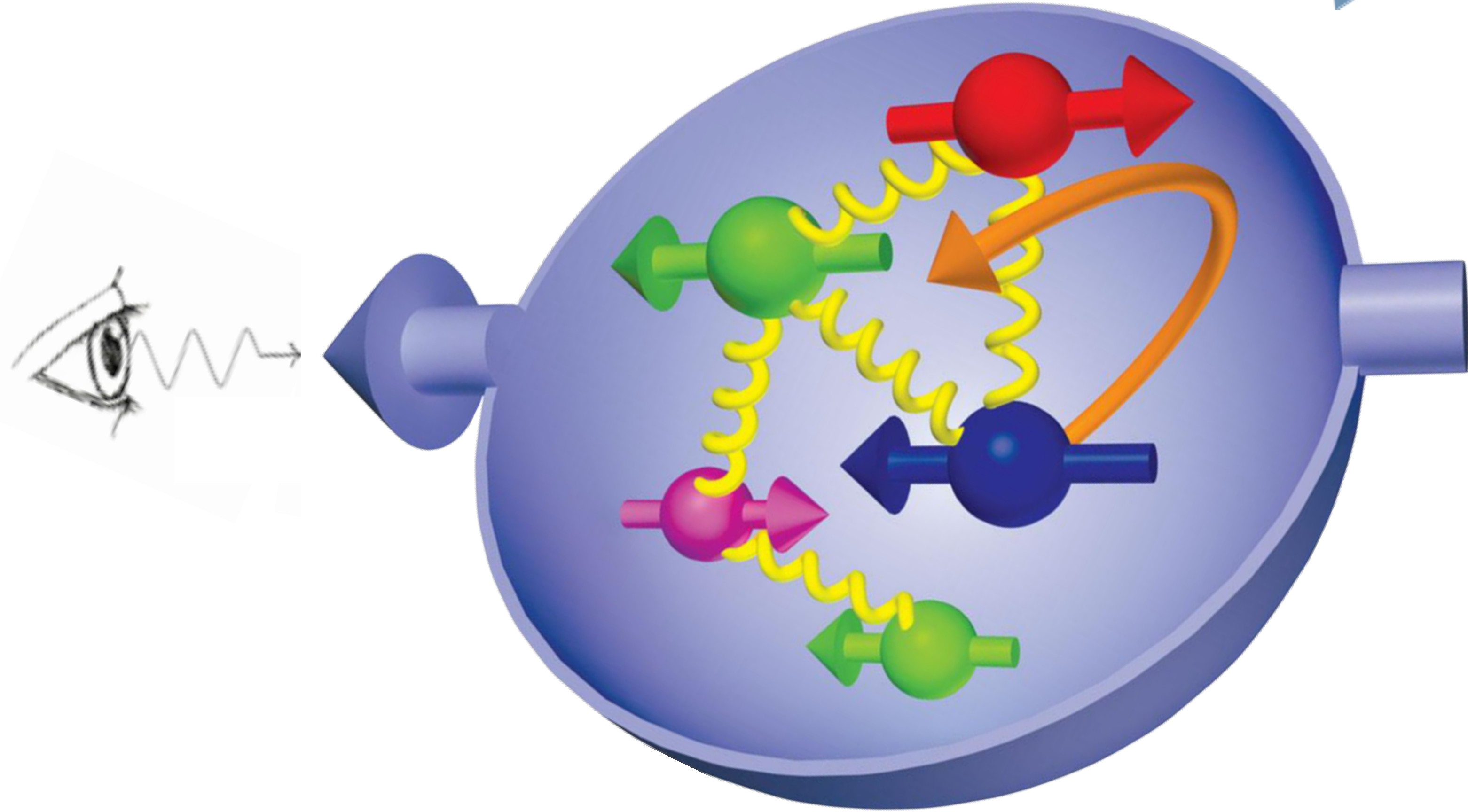


How it started

Spin puzzle

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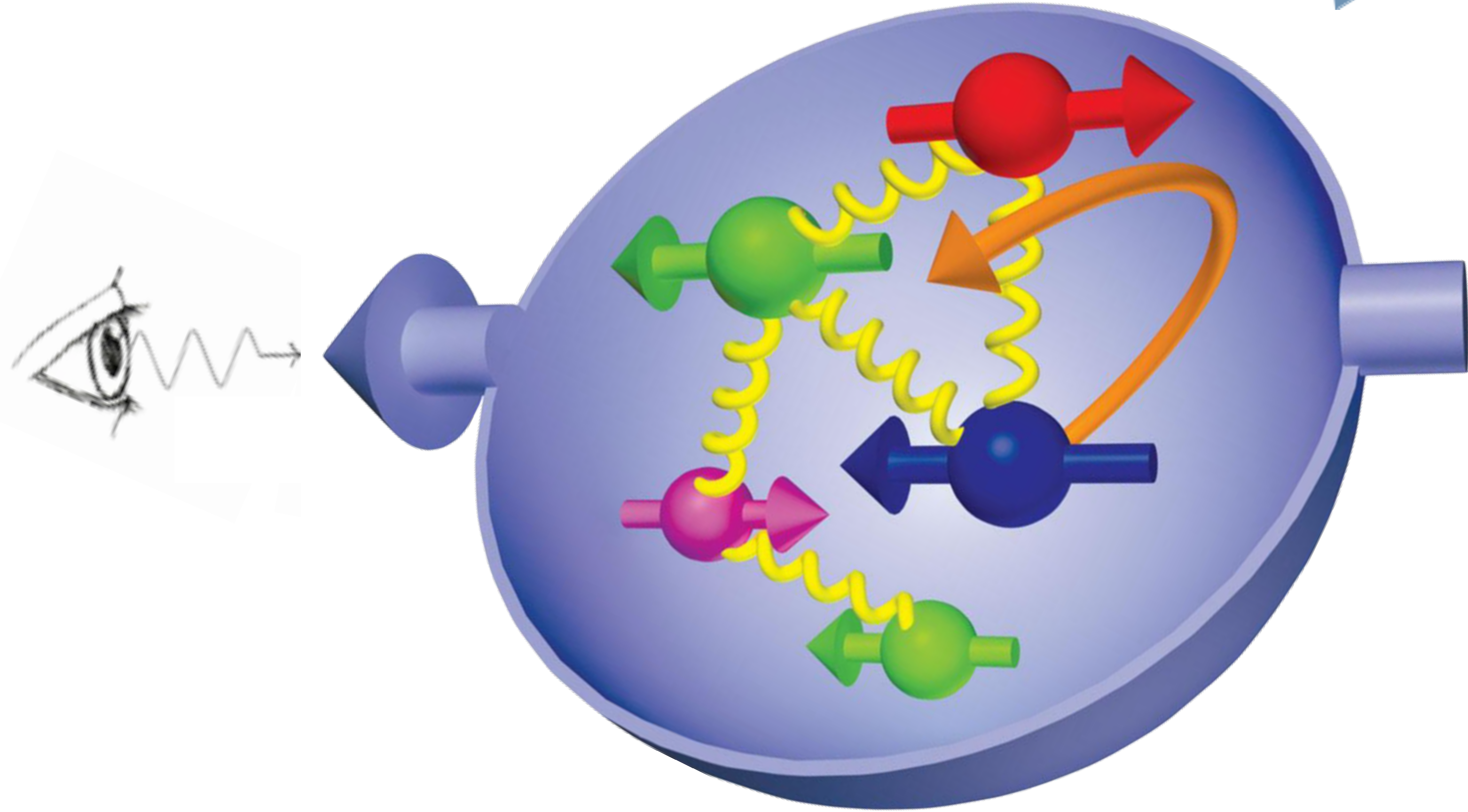
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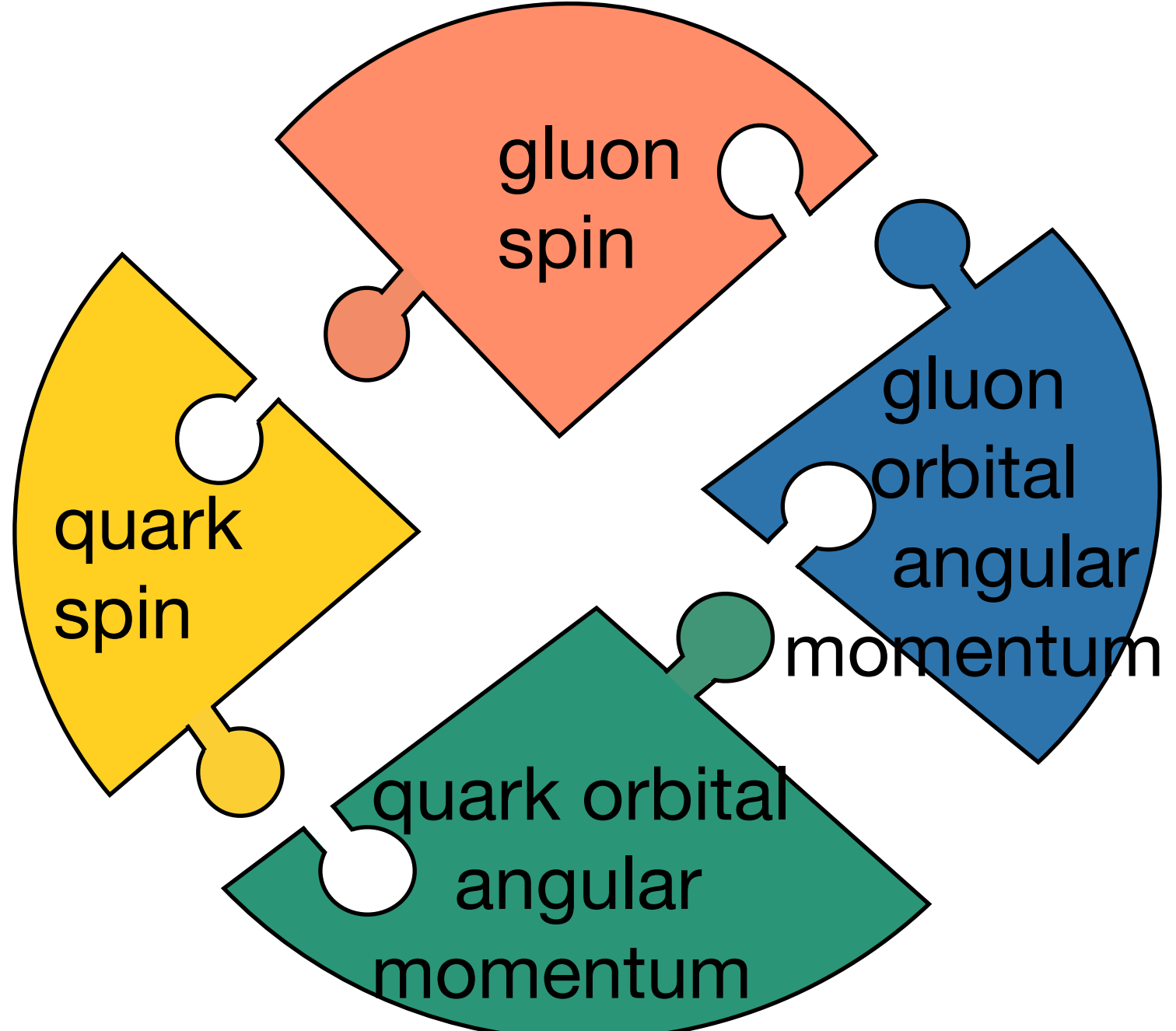
How it started

Spin puzzle

Birth of new experiments:
SMC, HERMES, JLab, COMPASS



- Check EMC result
- Find missing contributions



Experiments studying spin

$e^+ + e^-$ and $\vec{e} + \vec{p}, \vec{D}, \vec{He}$



SLAC
NATIONAL ACCELERATOR LABORATORY

Jefferson Lab



$\vec{e} + \vec{p}, \vec{D}, \vec{He}$

$\vec{p}\vec{p}$ collider



BROOKHAVEN
NATIONAL LABORATORY

$\vec{e} + \vec{p}, \vec{D}, \vec{He}$



DESY

COMPASS $\vec{\mu} + \vec{p}$ & $\pi + \vec{p}$

LHC $p + p$



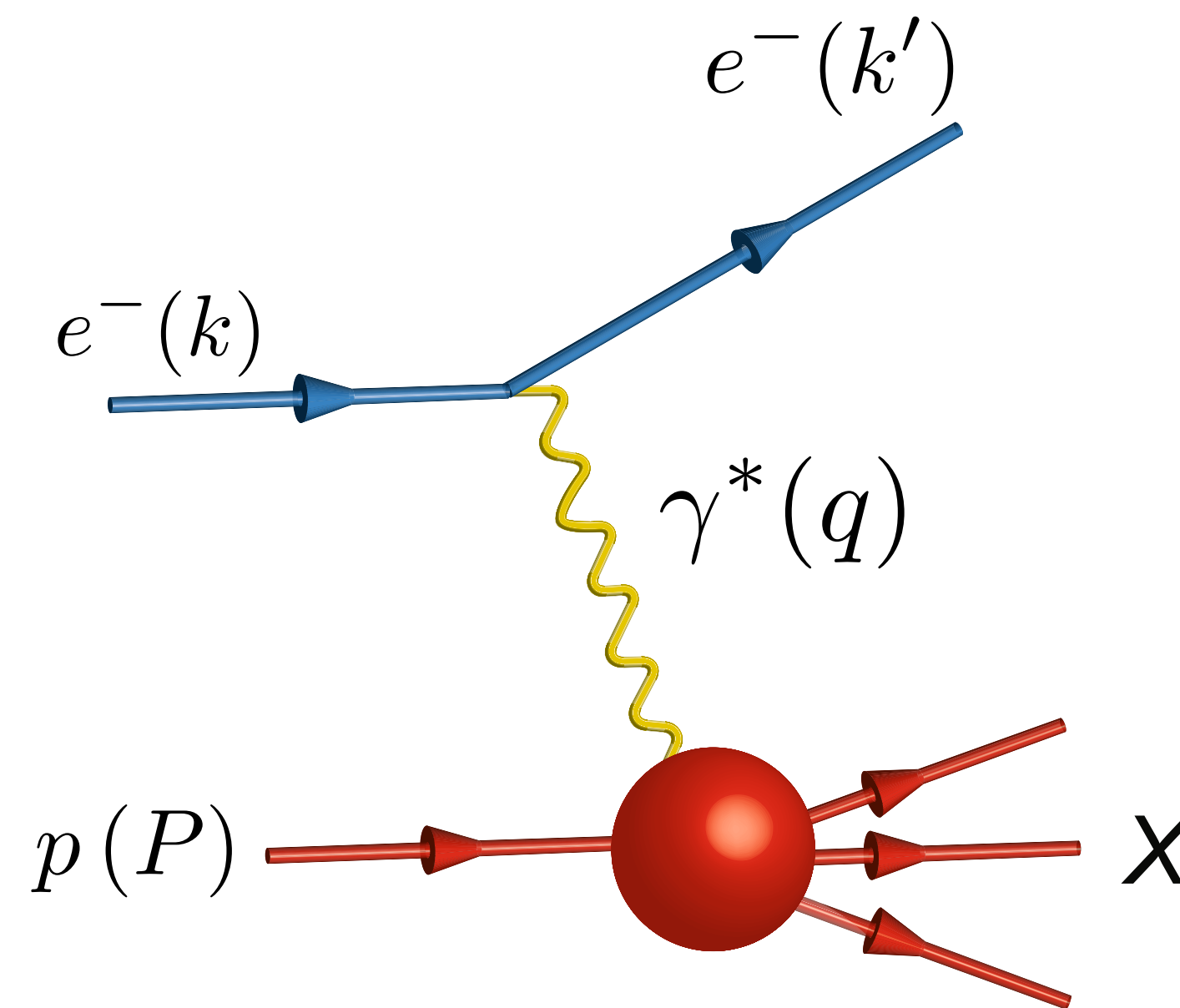
CERN

$e^+ + e^-$

KEK
High Energy Accelerator
Research Organization



Access to partons and their helicity

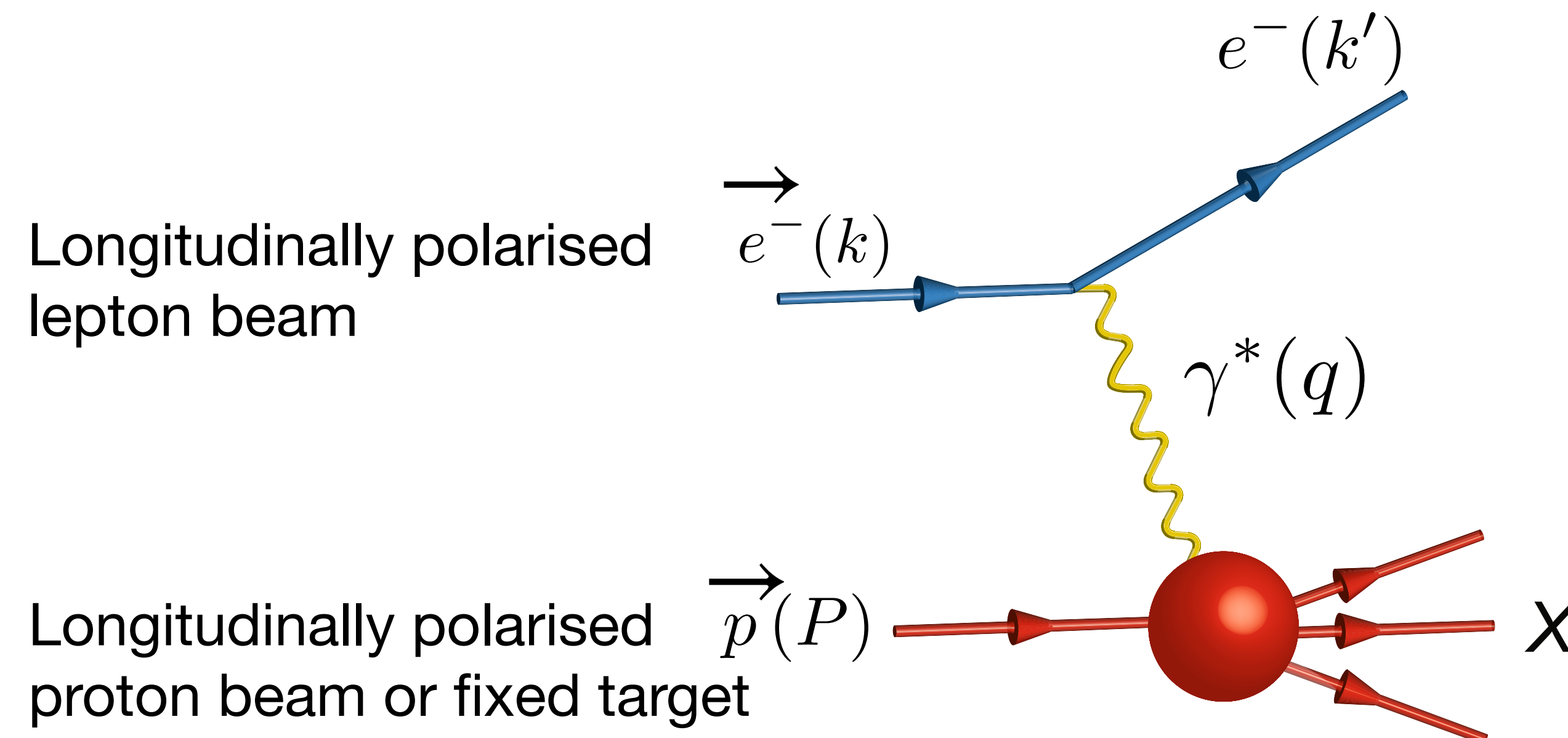


$$Q^2 = -q^2$$

Highly virtual photon:
 $Q^2 \gg 1 \text{ GeV}^2$
provides hard
scale of process
→ factorisation

$$x_B = \frac{Q^2}{2P \cdot q}$$

Access to partons and their helicity

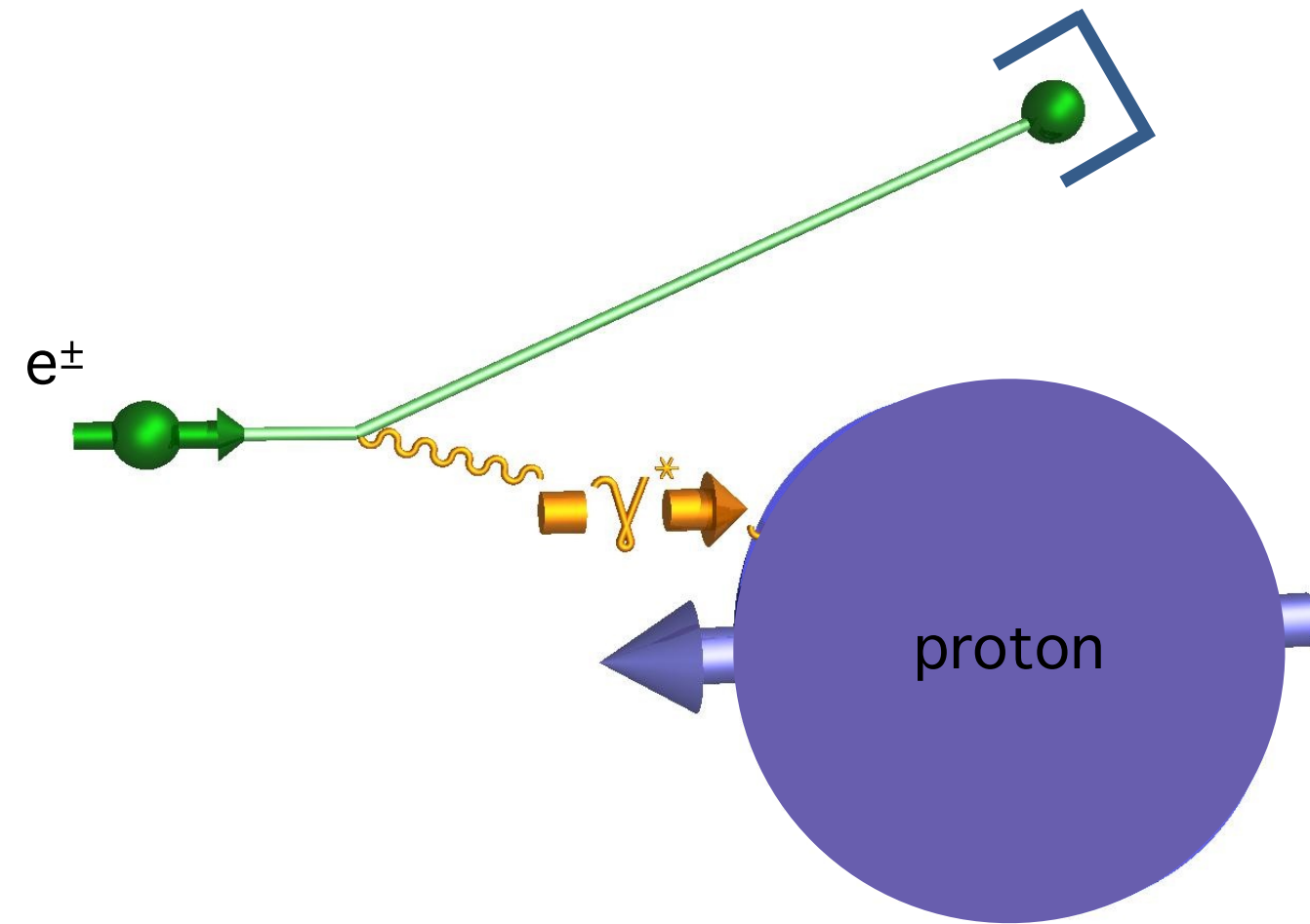


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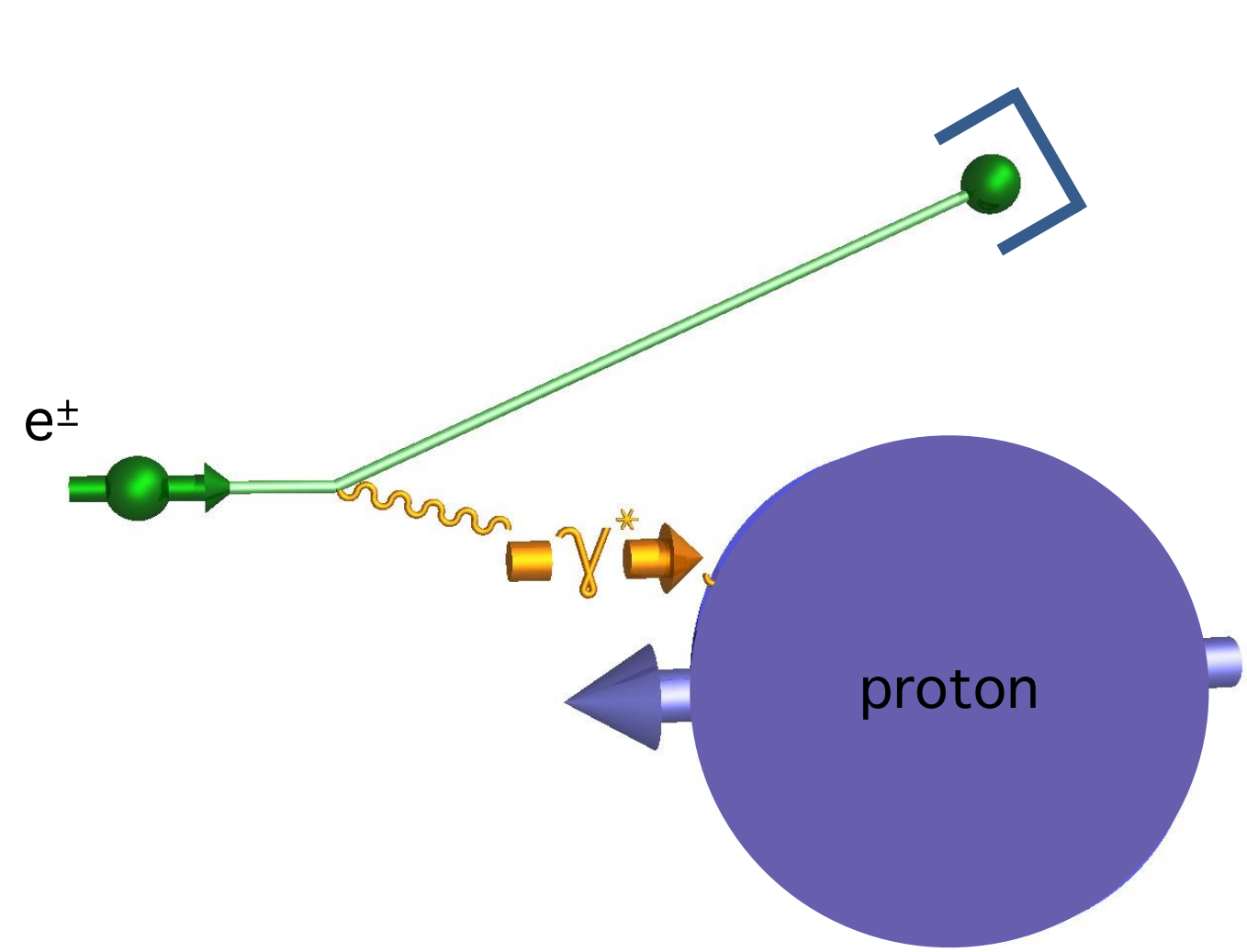
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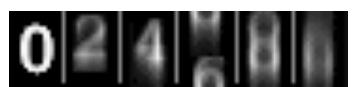
Measurement of the quark spin contribution

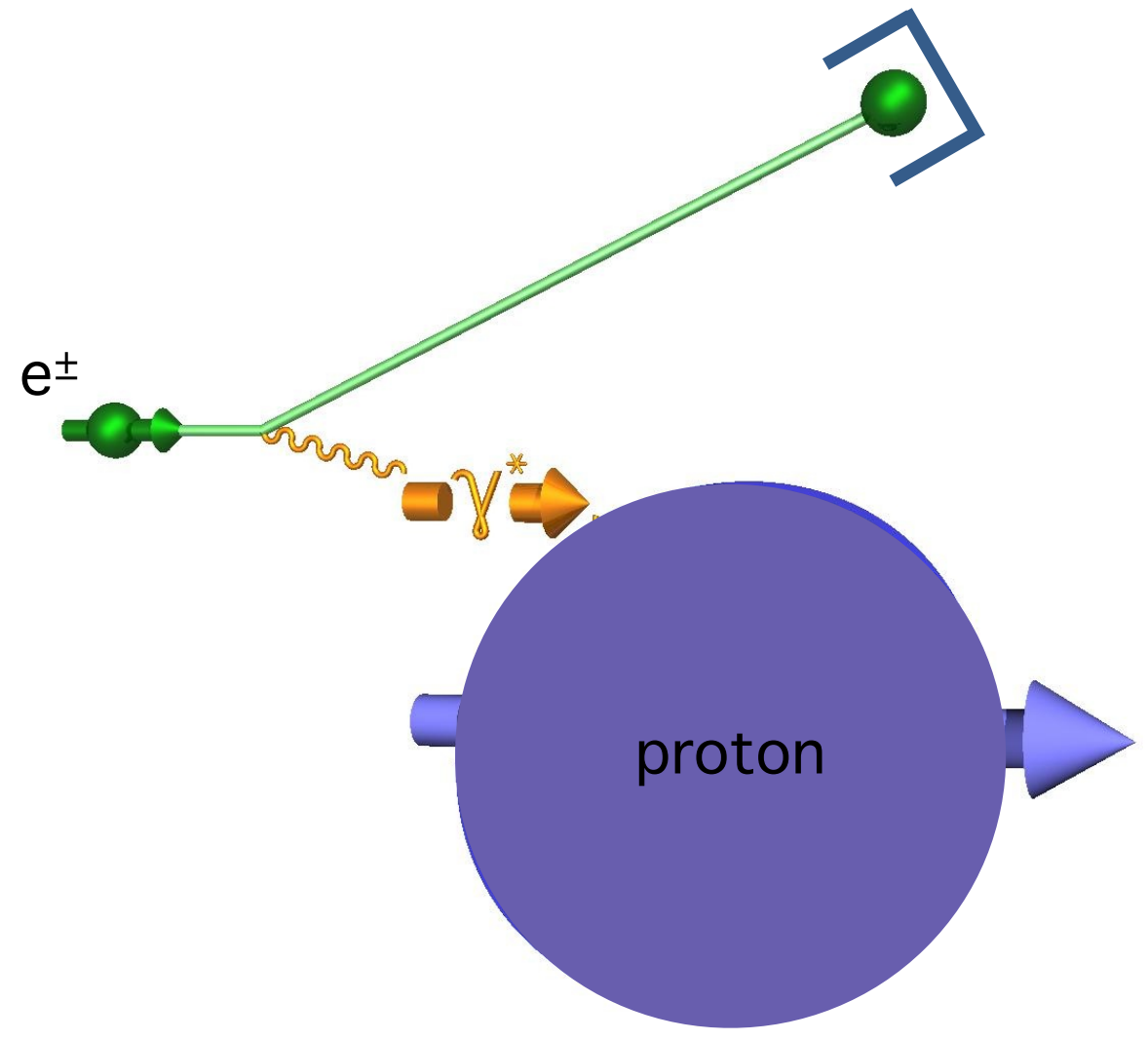


- longitudinally polarised proton
- longitudinally polarised e^\pm or μ^\pm beam
- count... 

Measurement of the quark spin contribution

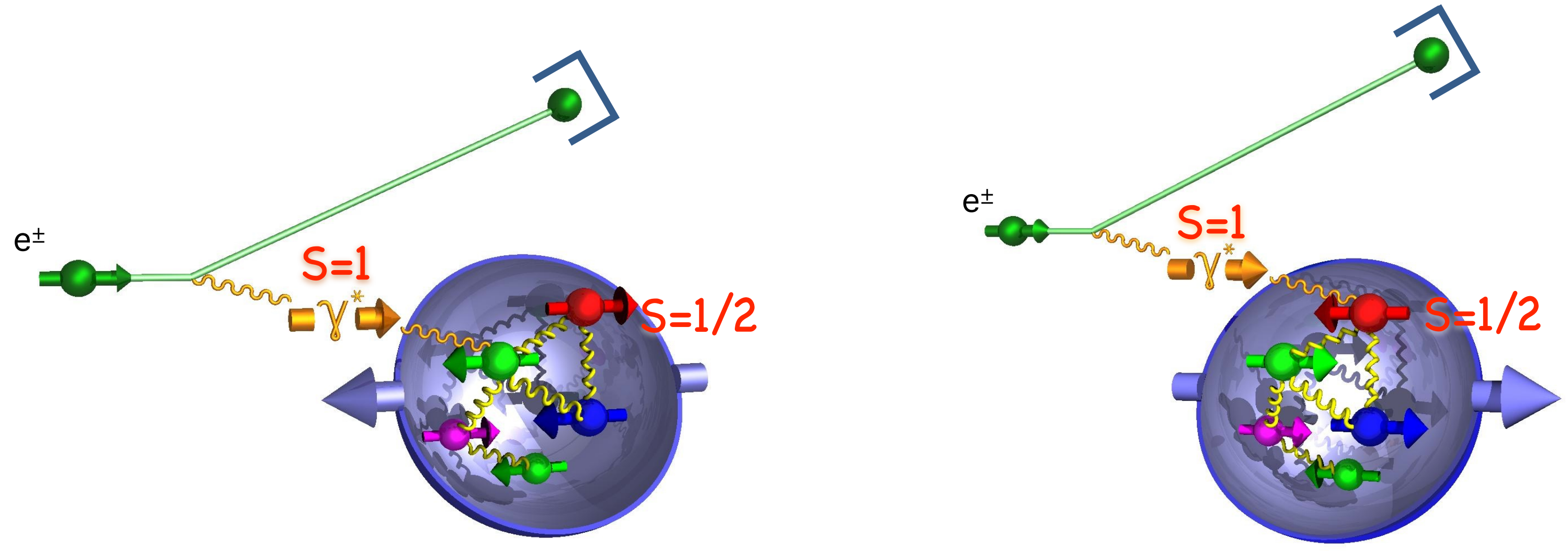


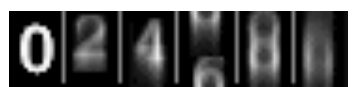
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- flip proton spin and count... 

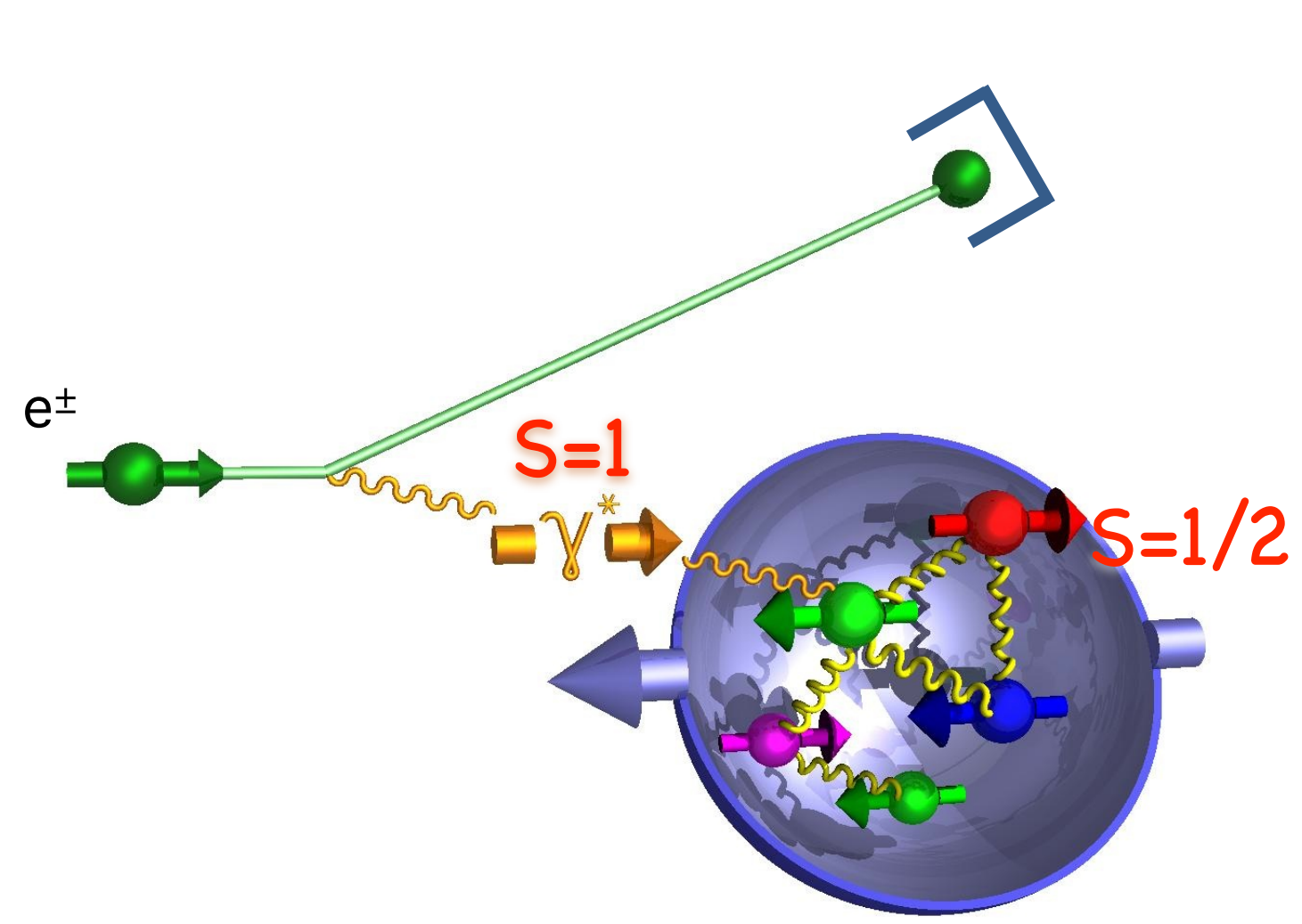
Measurement of the quark spin contribution

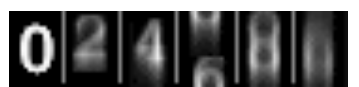


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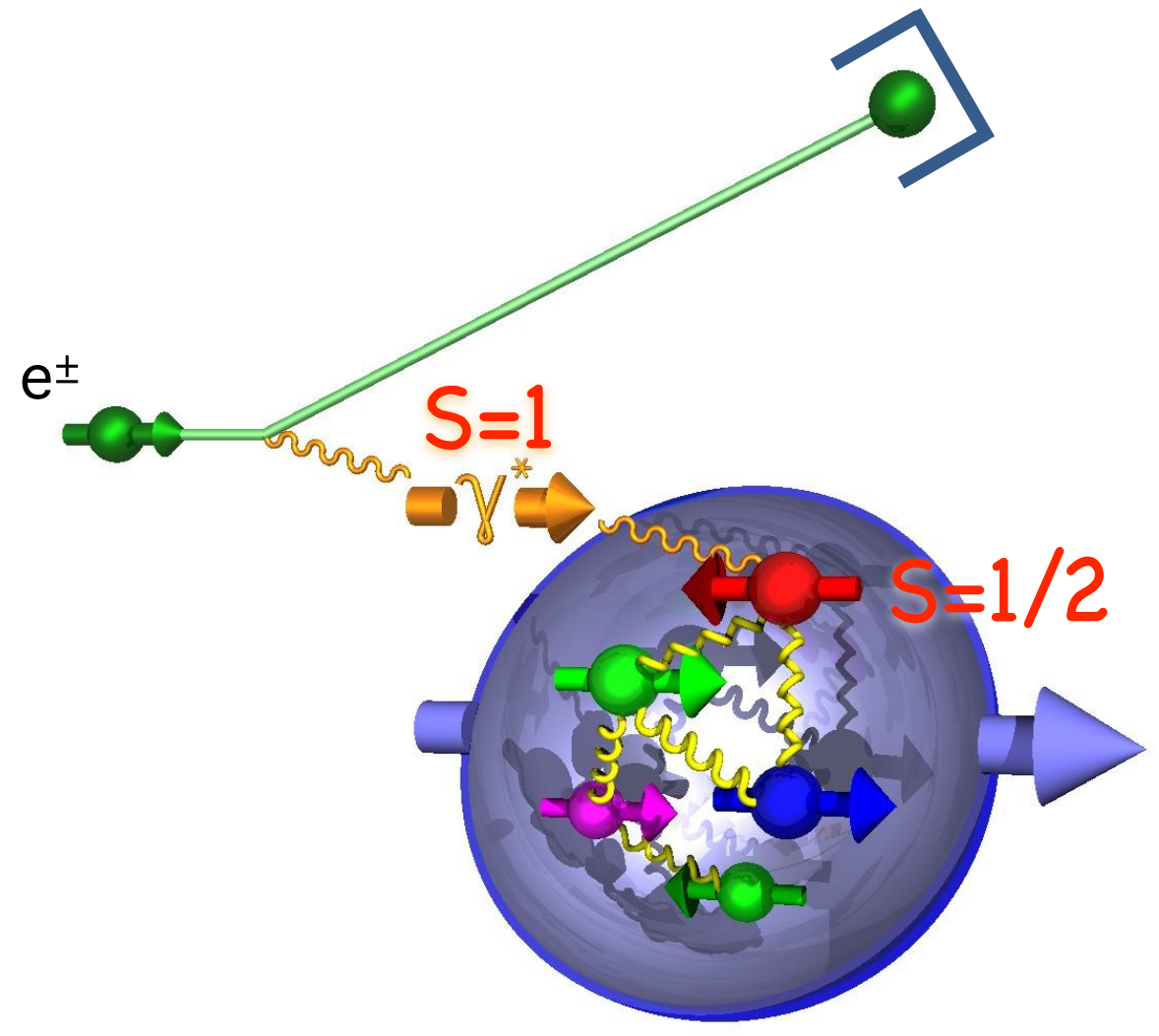
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Measurement of the quark spin contribution



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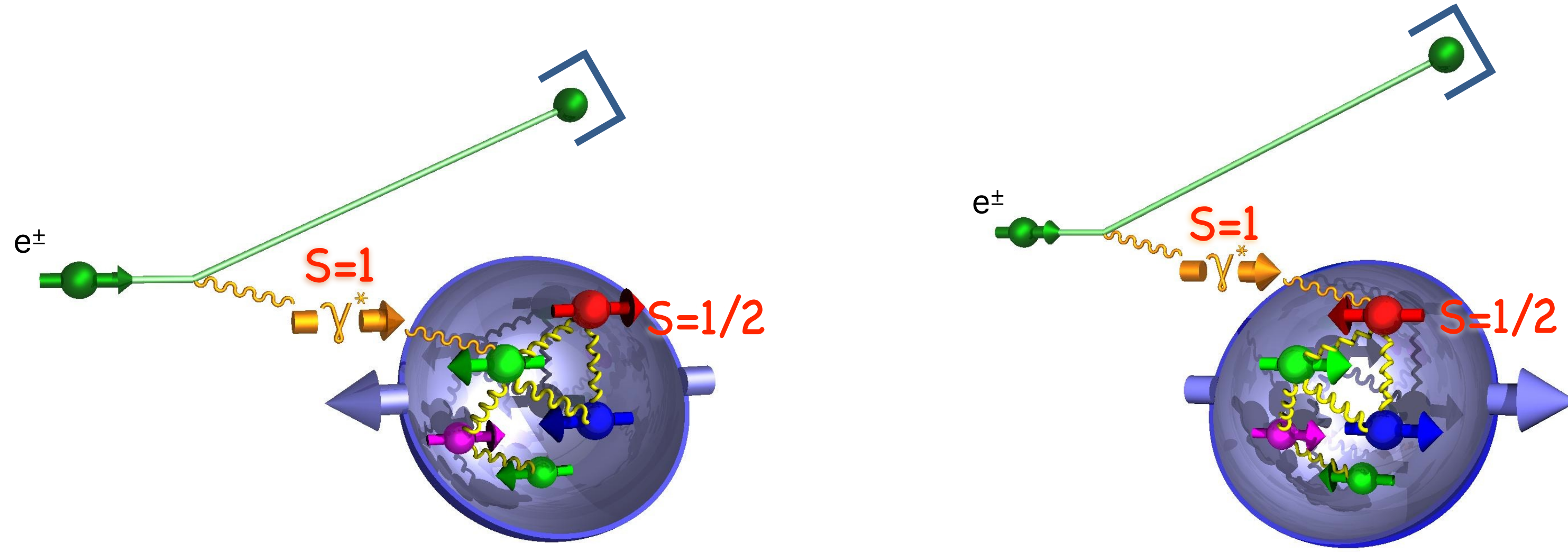
Access to quarks with spin aligned to proton spin



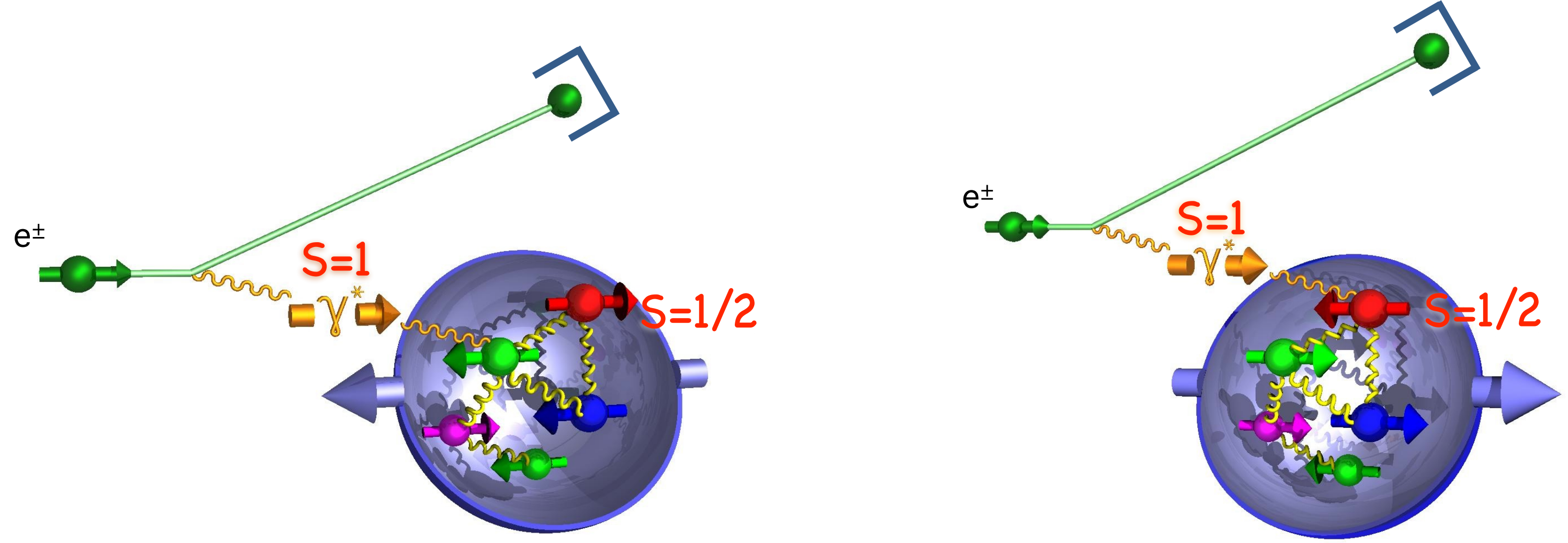
- flip proton spin and count... 

Access to quarks with spin anti-aligned to proton spin

Measurement of the quark spin contribution

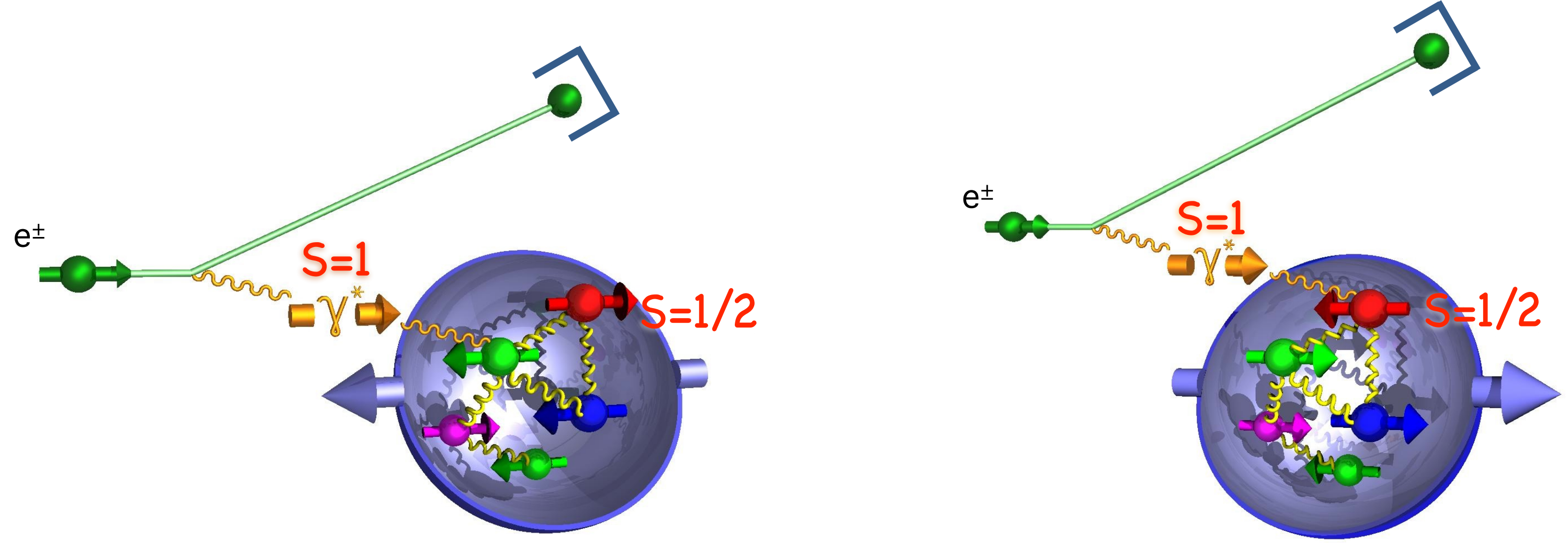


Measurement of the quark spin contribution



Asymmetry:
$$A_{LL} = \frac{\frac{\overleftarrow{N}}{\overleftarrow{L}} - \frac{\overrightarrow{N}}{\overrightarrow{L}}}{\frac{\overleftarrow{N}}{\overleftarrow{L}} + \frac{\overrightarrow{N}}{\overrightarrow{L}}}(x_B, Q^2)$$

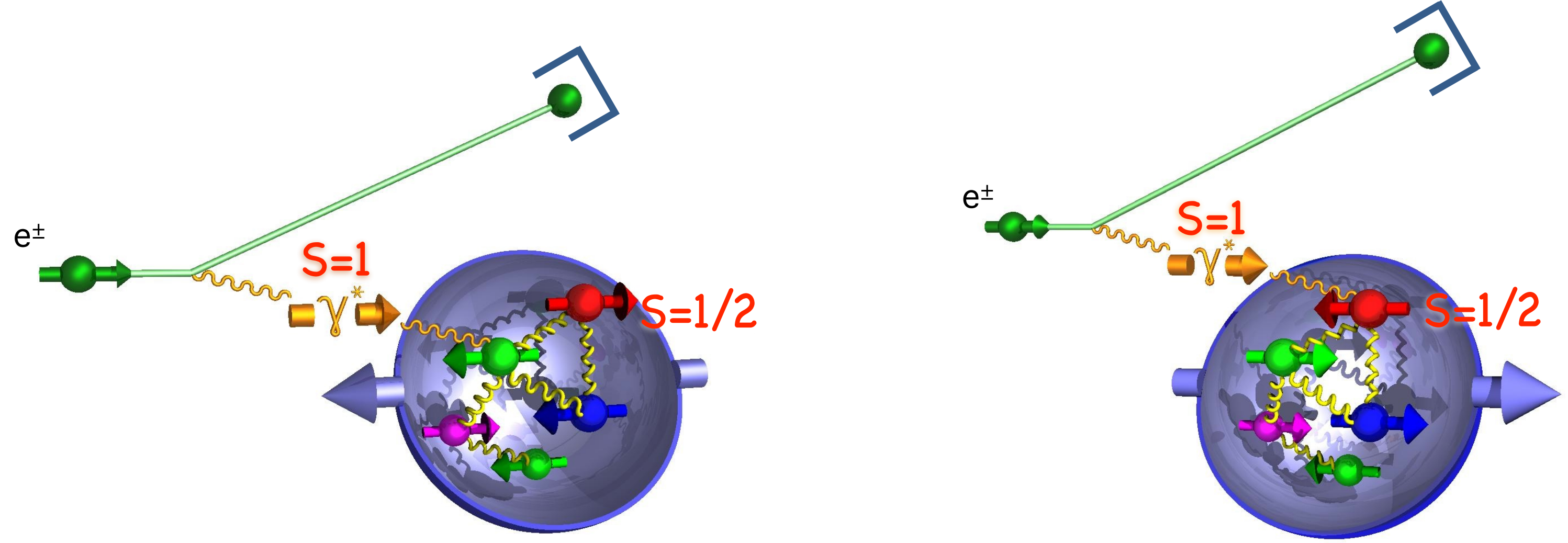
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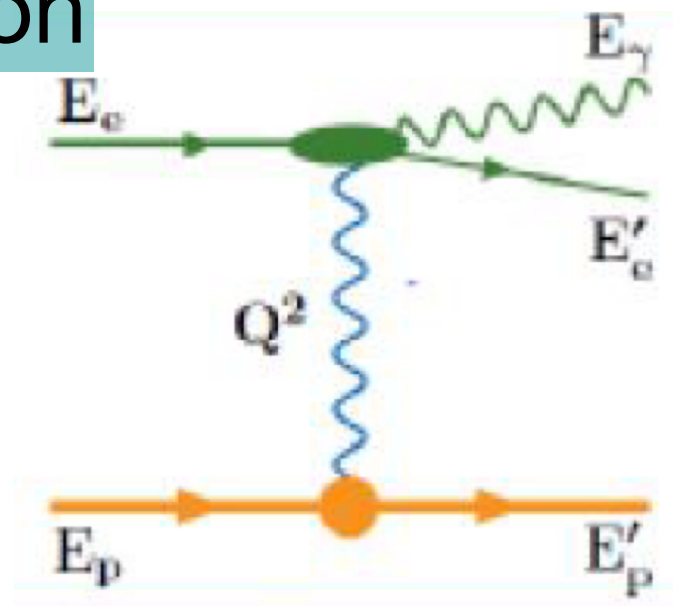
precise luminosity determination

Measurement of the quark spin contribution

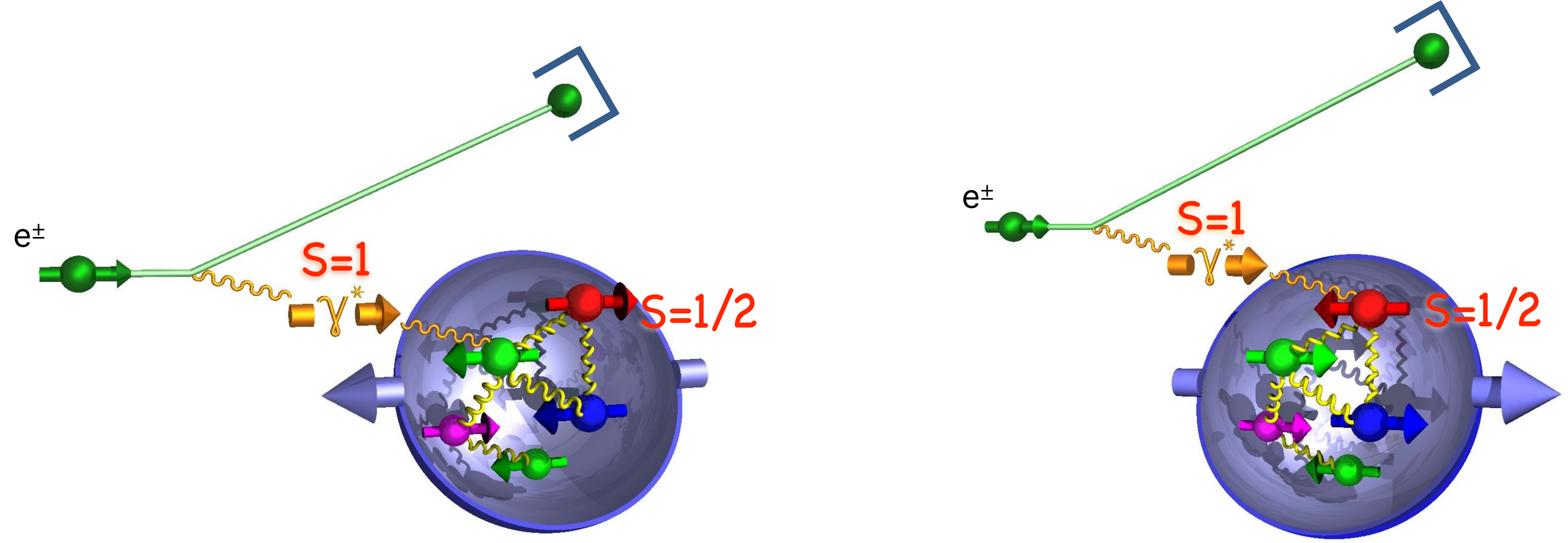


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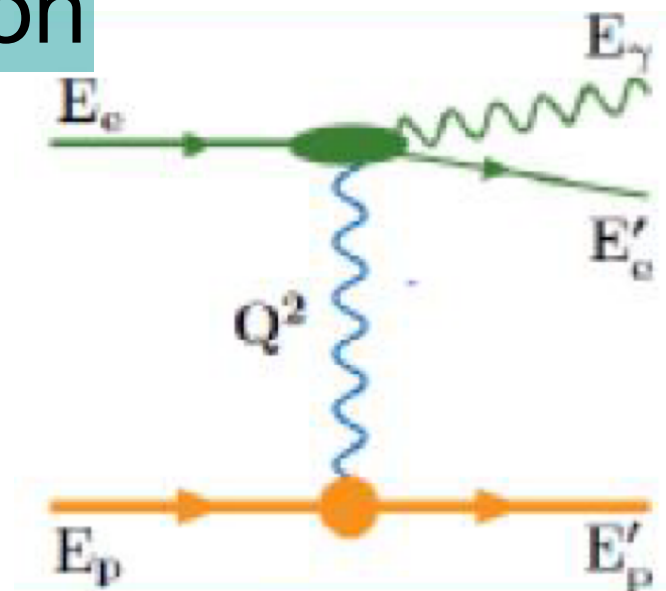
Measurement of the quark spin contribution



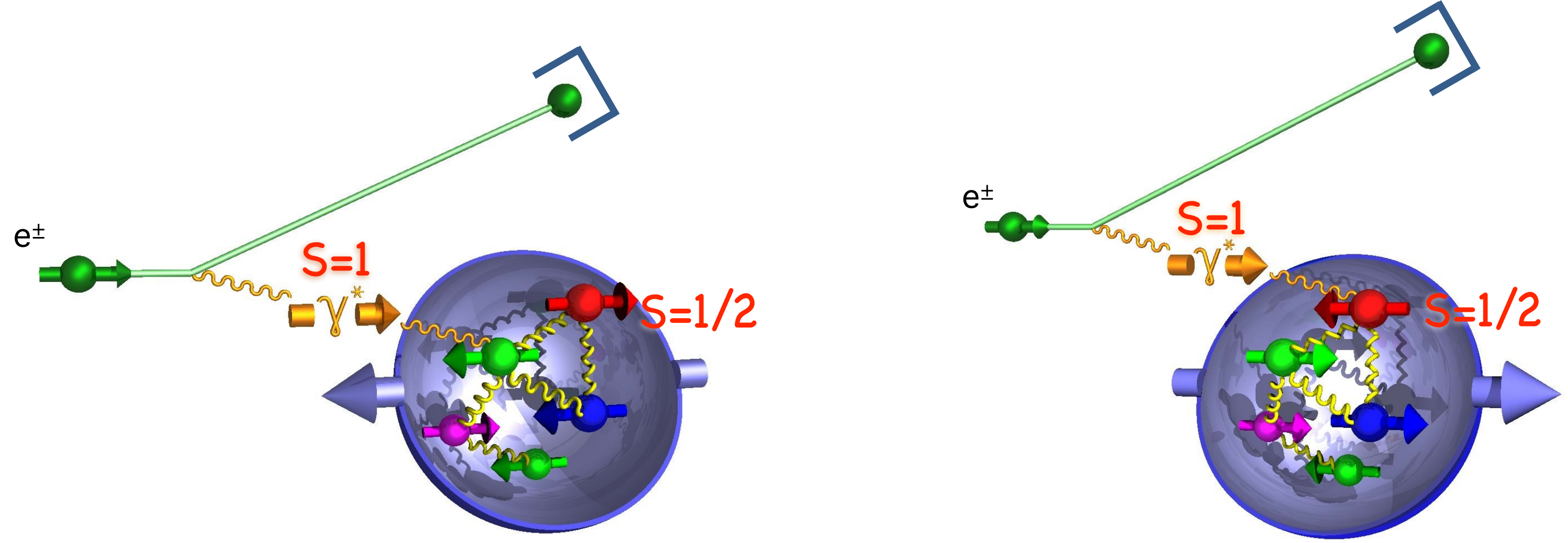
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high polarisation

precise luminosity determination



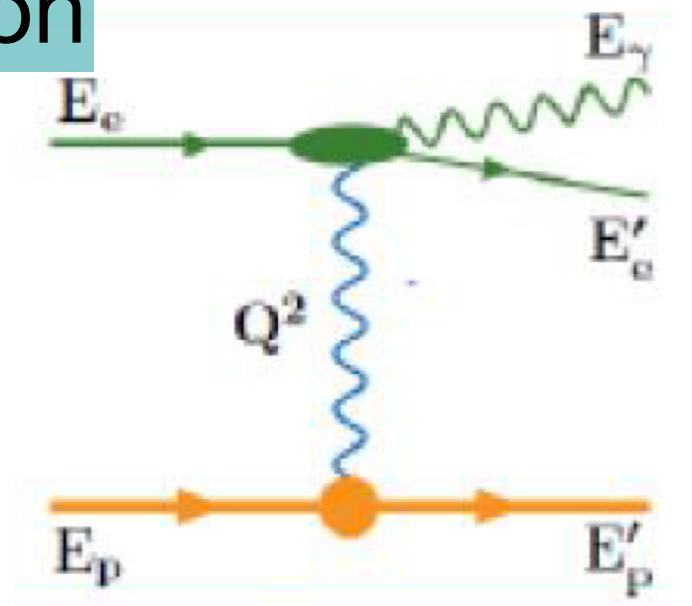
Measurement of the quark spin contribution



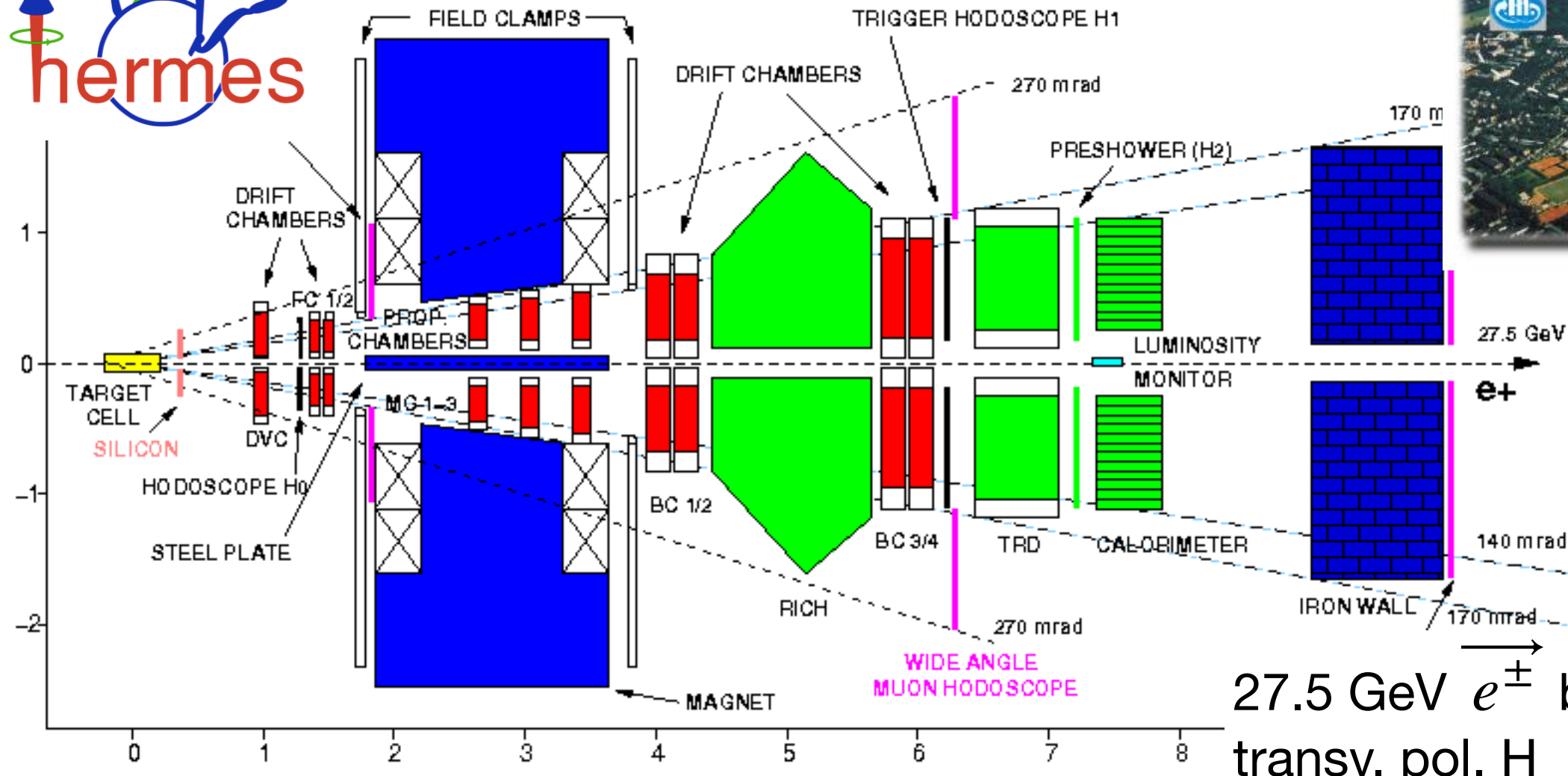
Asymmetry: $A_{LL} = \frac{\frac{\overleftarrow{N}}{\overleftarrow{L}} - \frac{\overrightarrow{N}}{\overrightarrow{L}}}{\frac{\overleftarrow{N}}{\overleftarrow{L}} + \frac{\overrightarrow{N}}{\overrightarrow{L}}}(x_B, Q^2) \propto g_1(x, Q^2) = \frac{1}{2} \sum_q e_q^2 \Delta q(x, Q^2)$

high polarisation

precise luminosity determination



Polarised DIS experiments



data taking
1995 – 2007

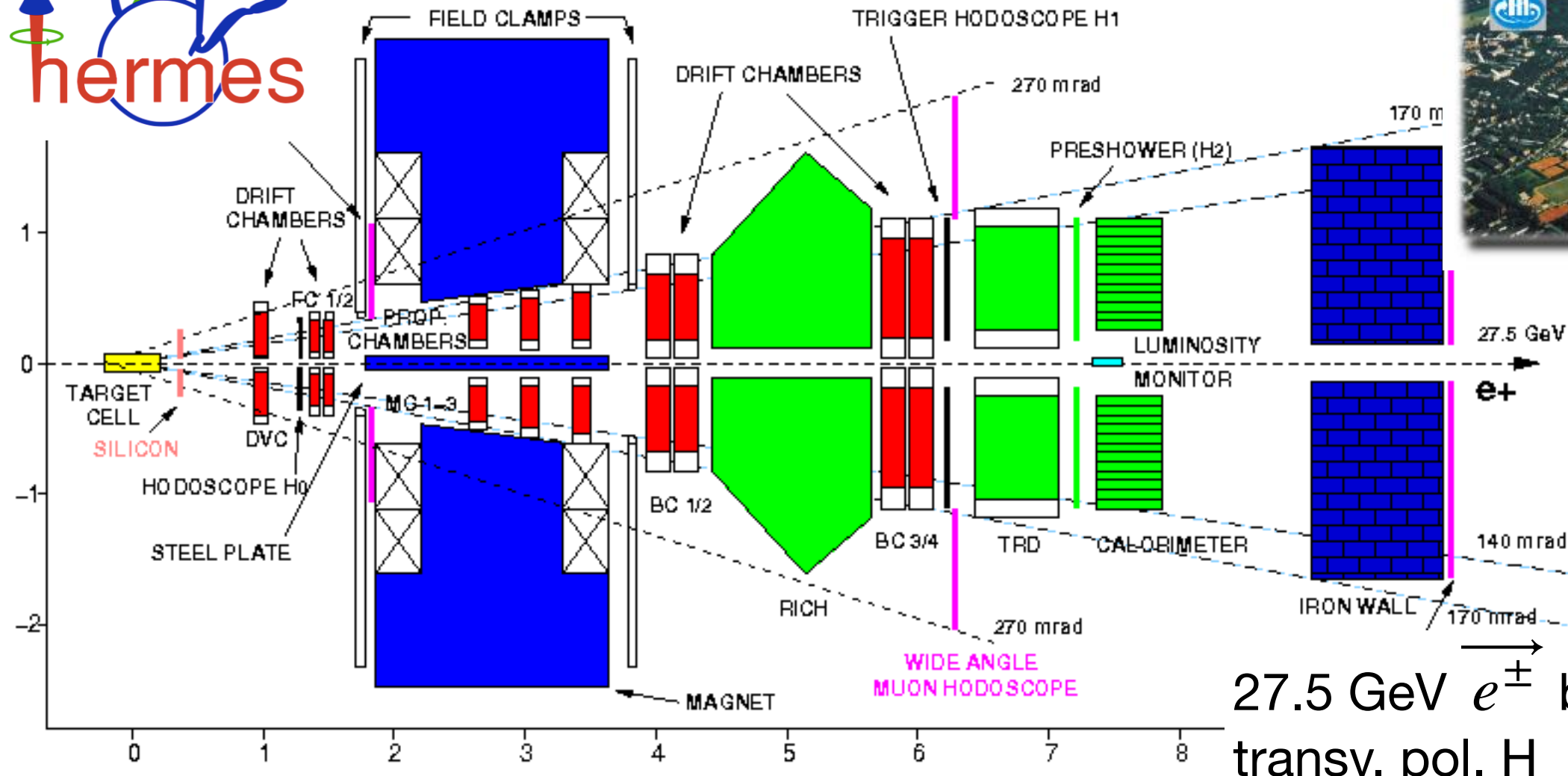
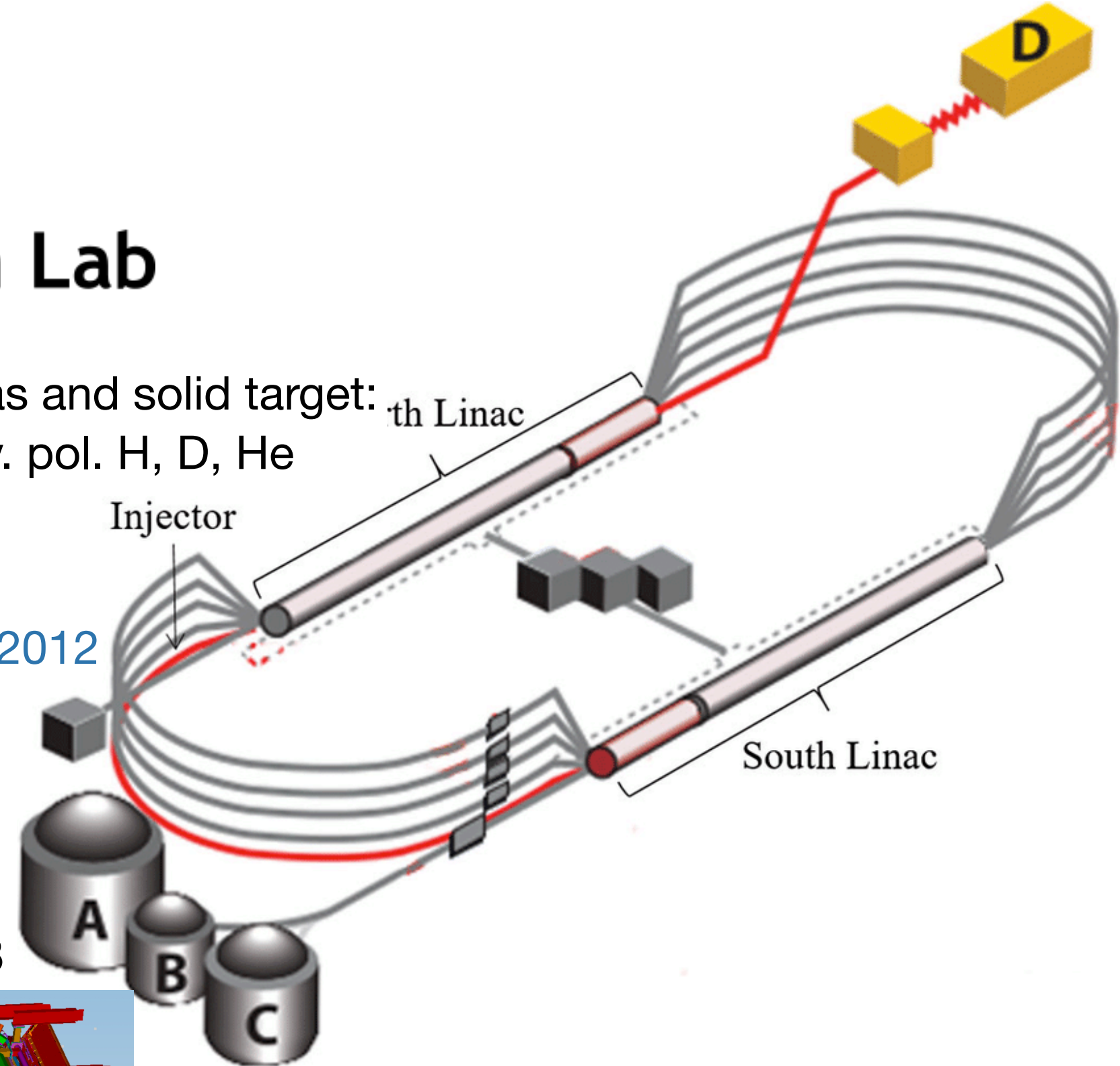
27.5 GeV e^\pm beam off gas target:
transv. pol. H
long. pol. H, D, He
unpol. H, D, He, Ne, Kr, Xe

Polarised DIS experiments

Jefferson Lab

e^- beam off gas and solid target:
long. and transv. pol. H, D, He

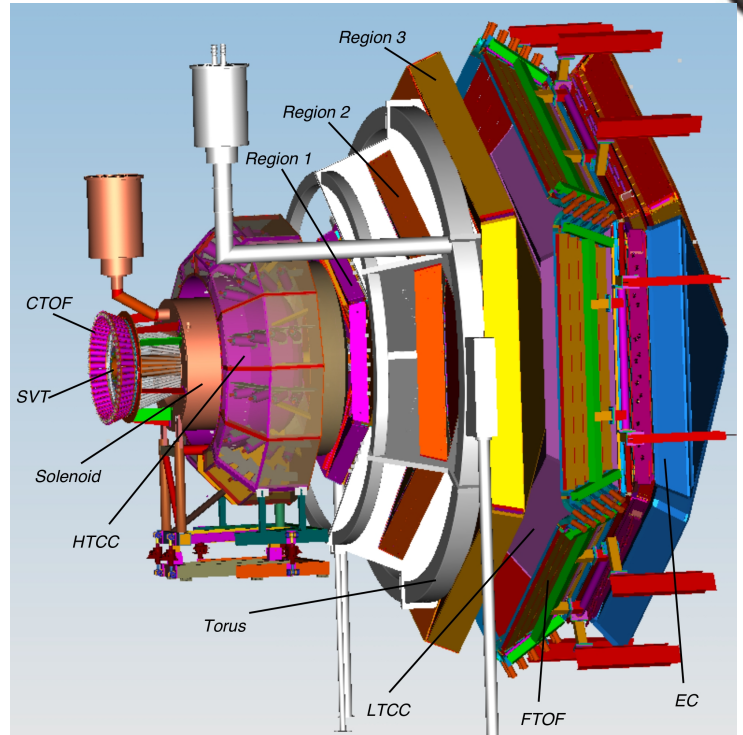
data taking
6 GeV: 2000 – 2012
12 GeV: 2009 –



data taking
1995 – 2007

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CLAS12 in Hall B

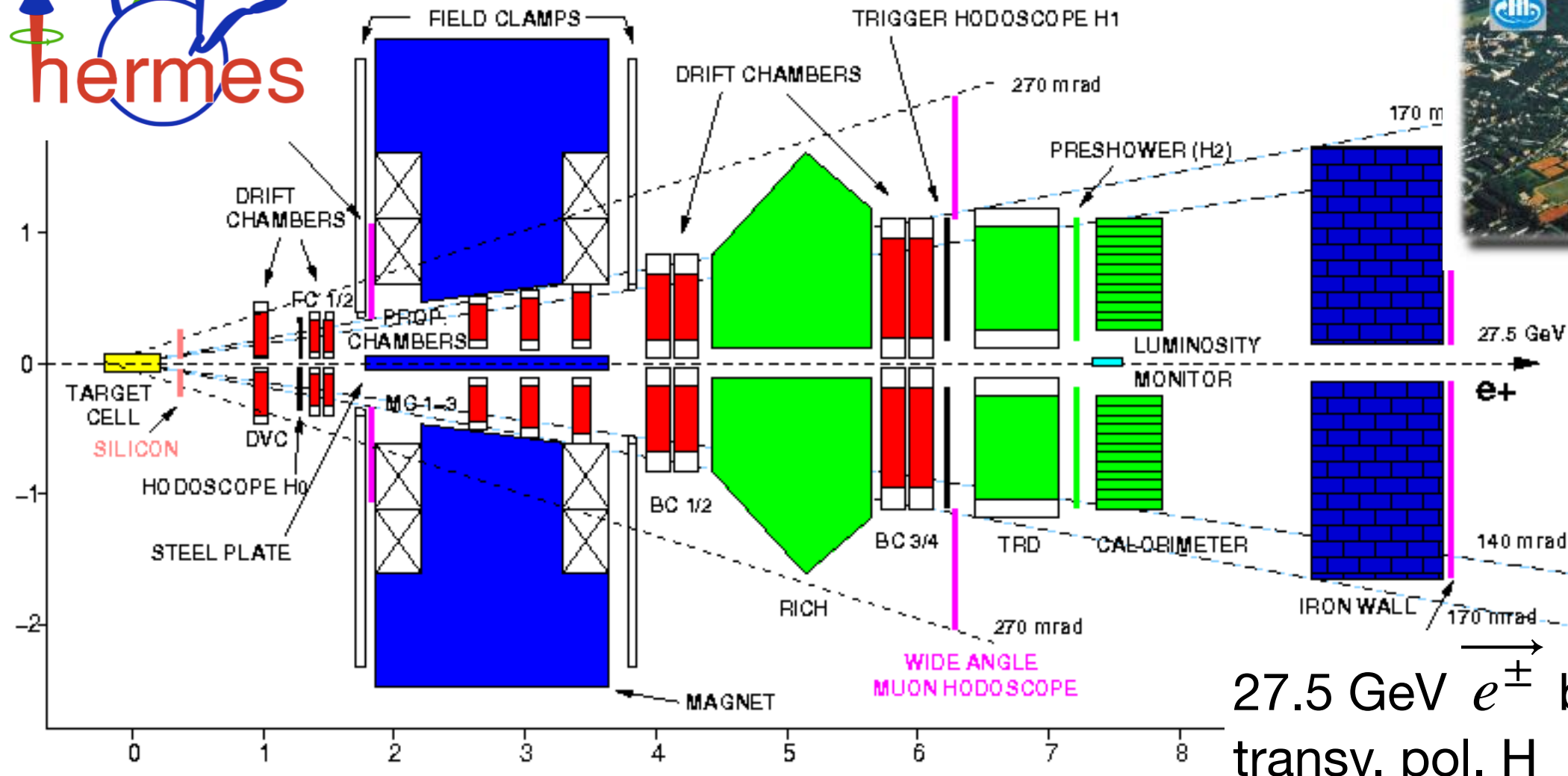
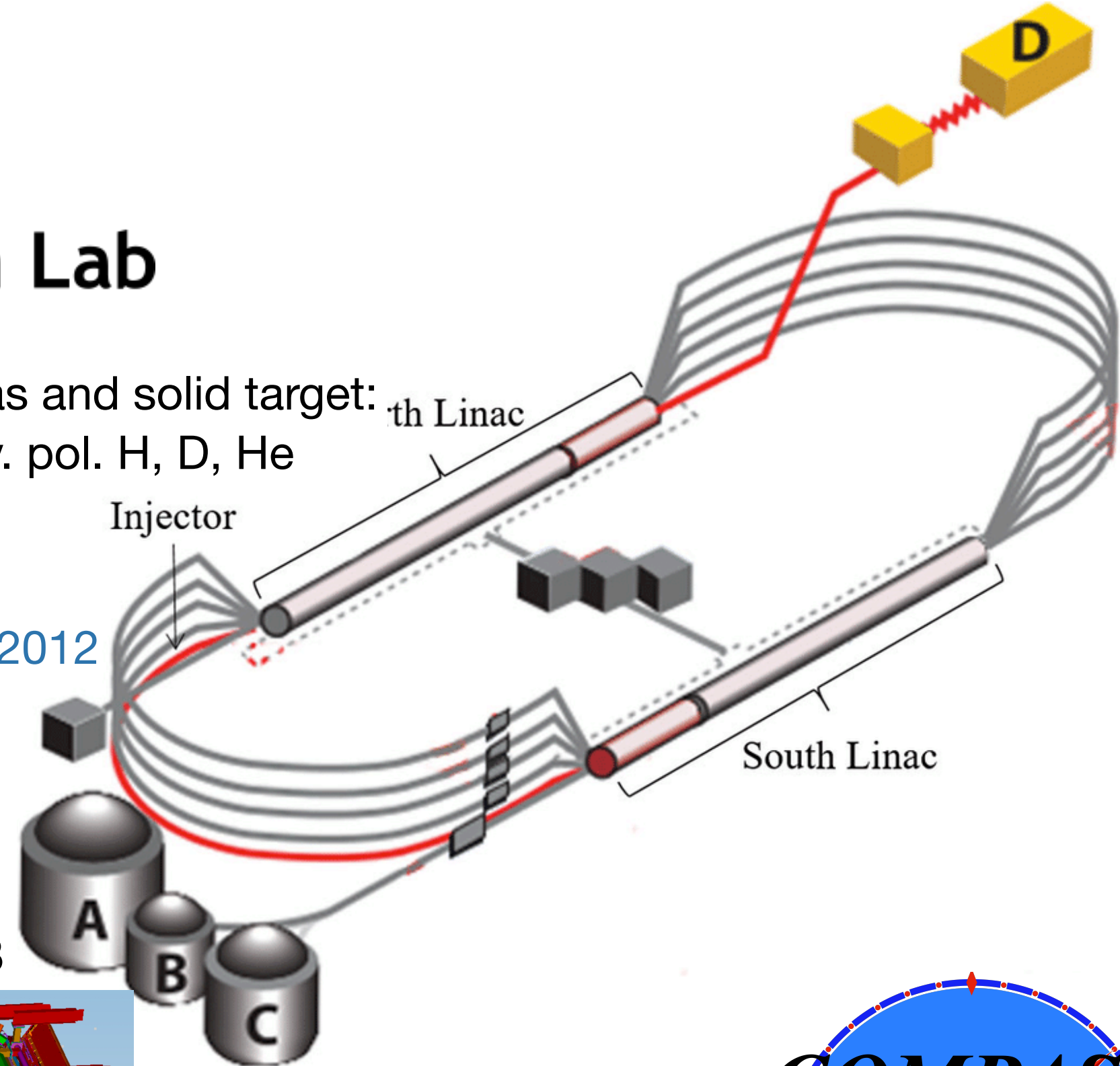


Polarised DIS experiments

Jefferson Lab

e^- beam off gas and solid target:
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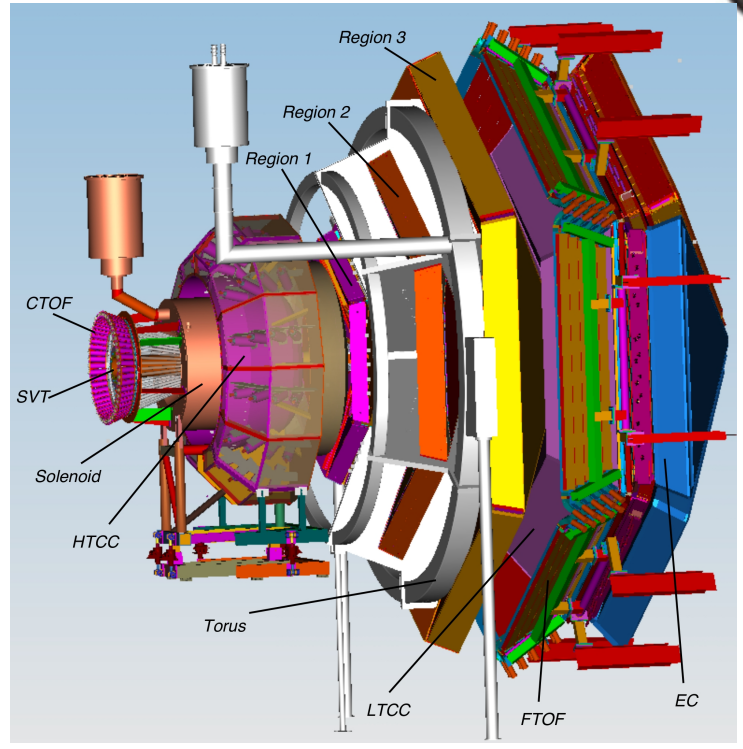
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data taking
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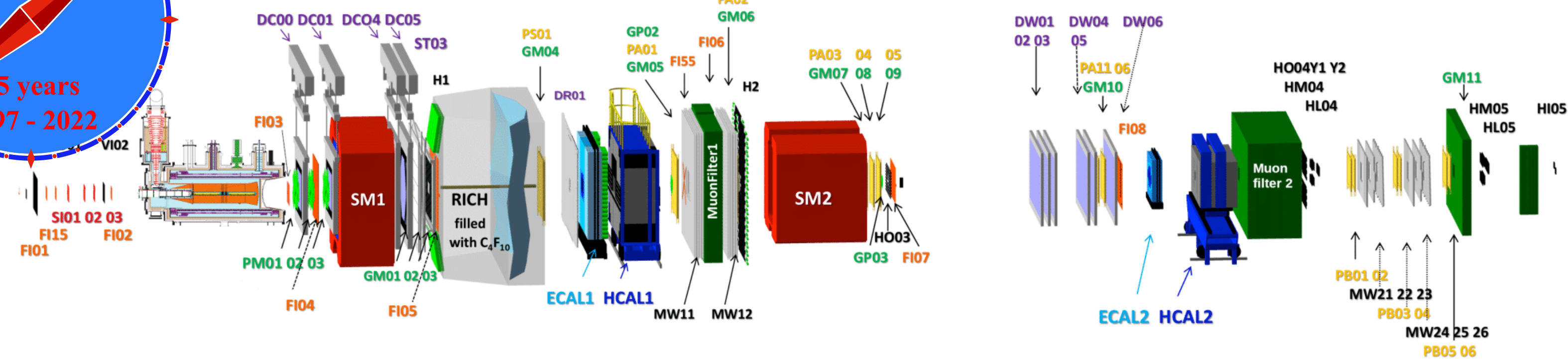
27.5 GeV e^\pm beam off gas target:
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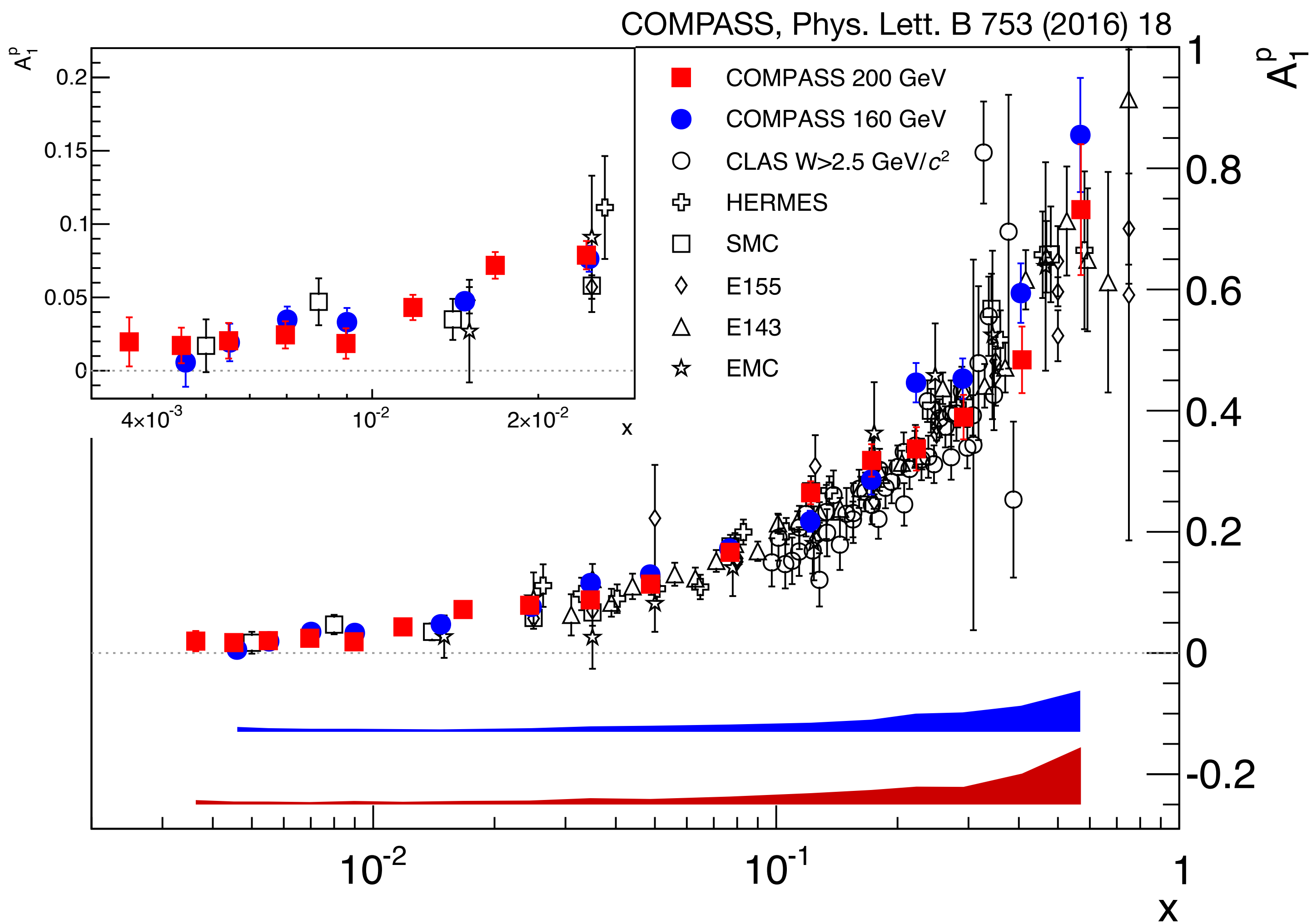


data taking
2002 – 2022

160–200 GeV μ^\pm beam off solid target:
long. and transv. pol. H and D

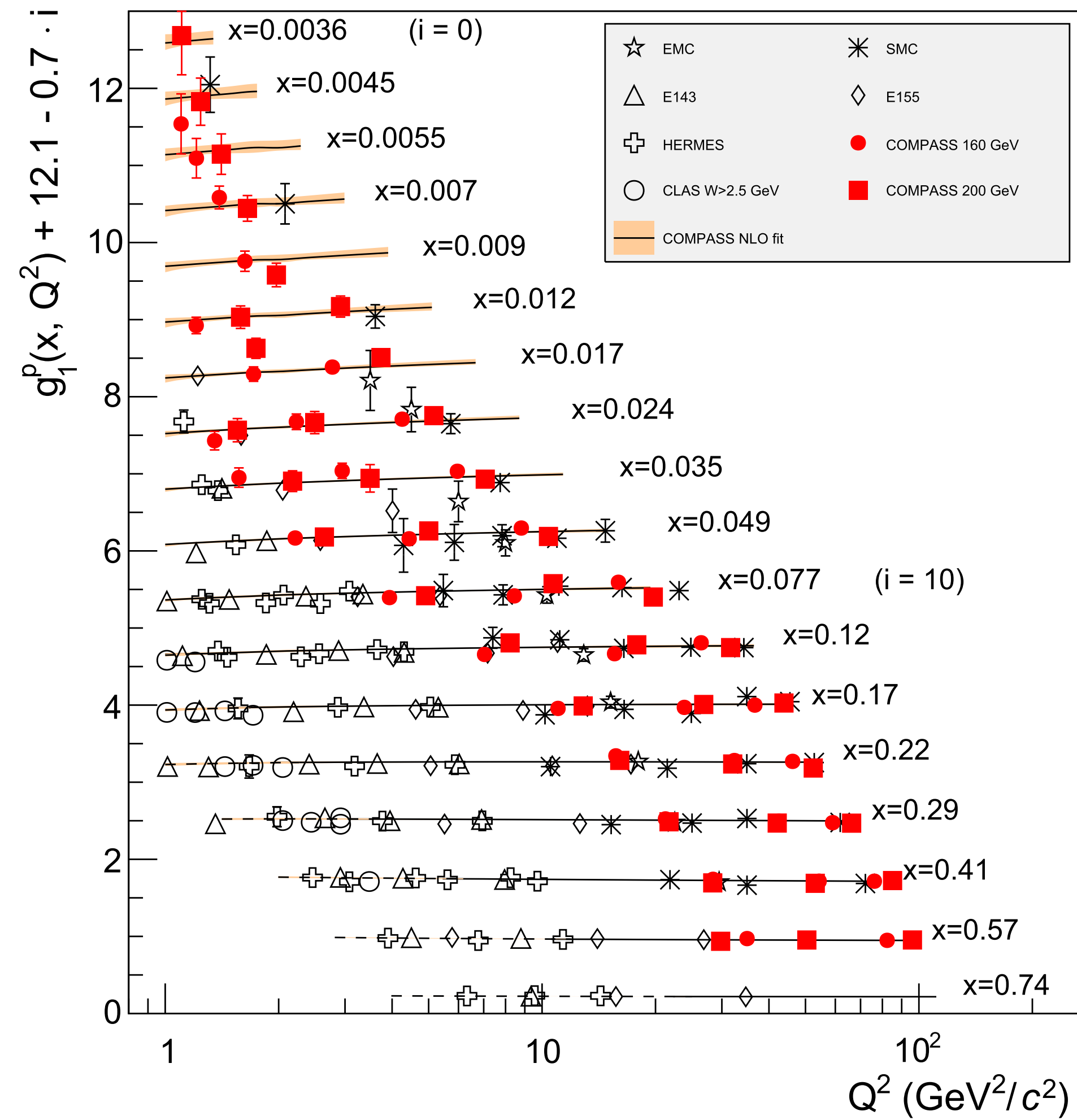


The asymmetry



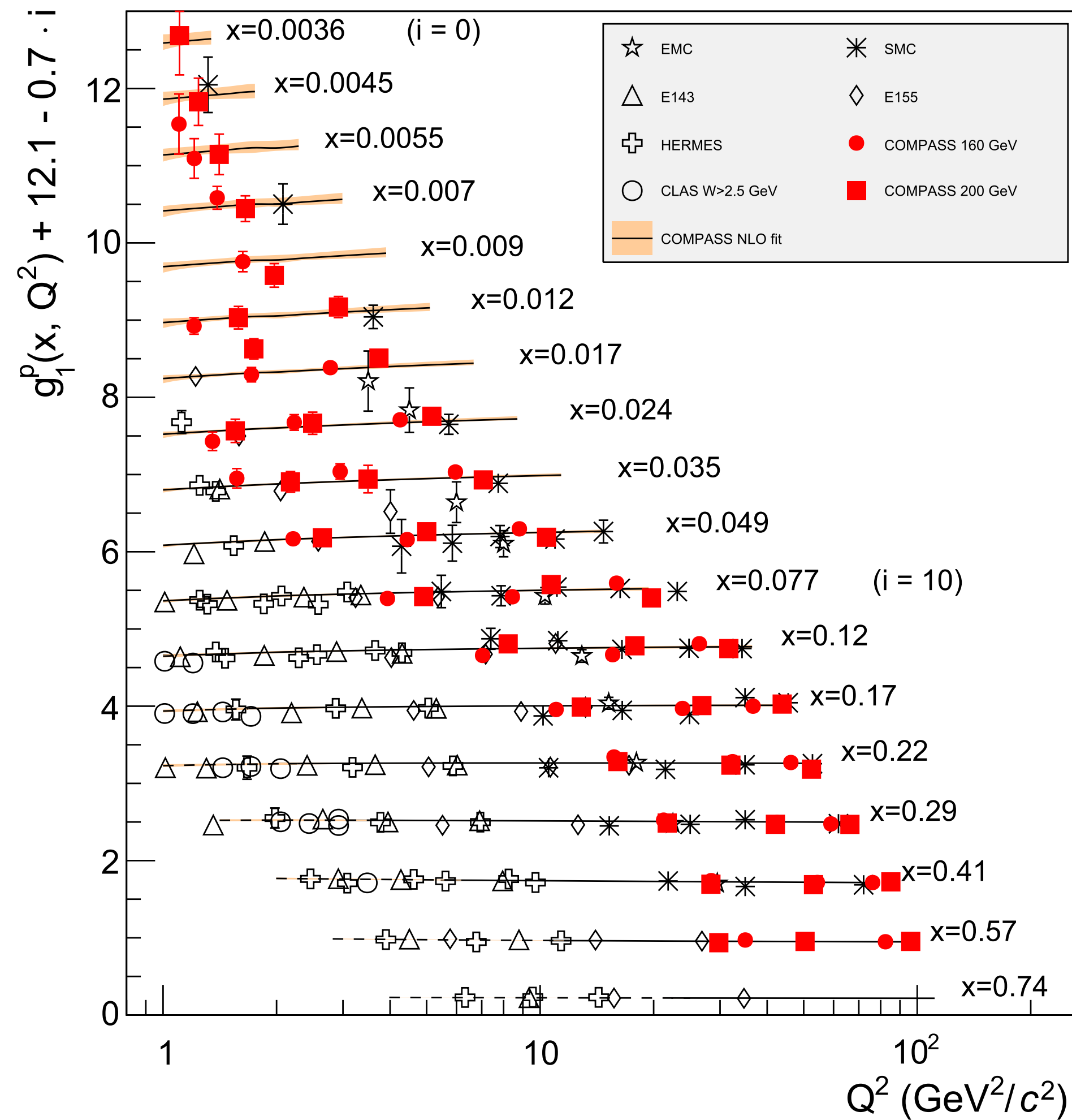
The asymmetry

g_1^p : world data



The asymmetry

g_1^p : world data

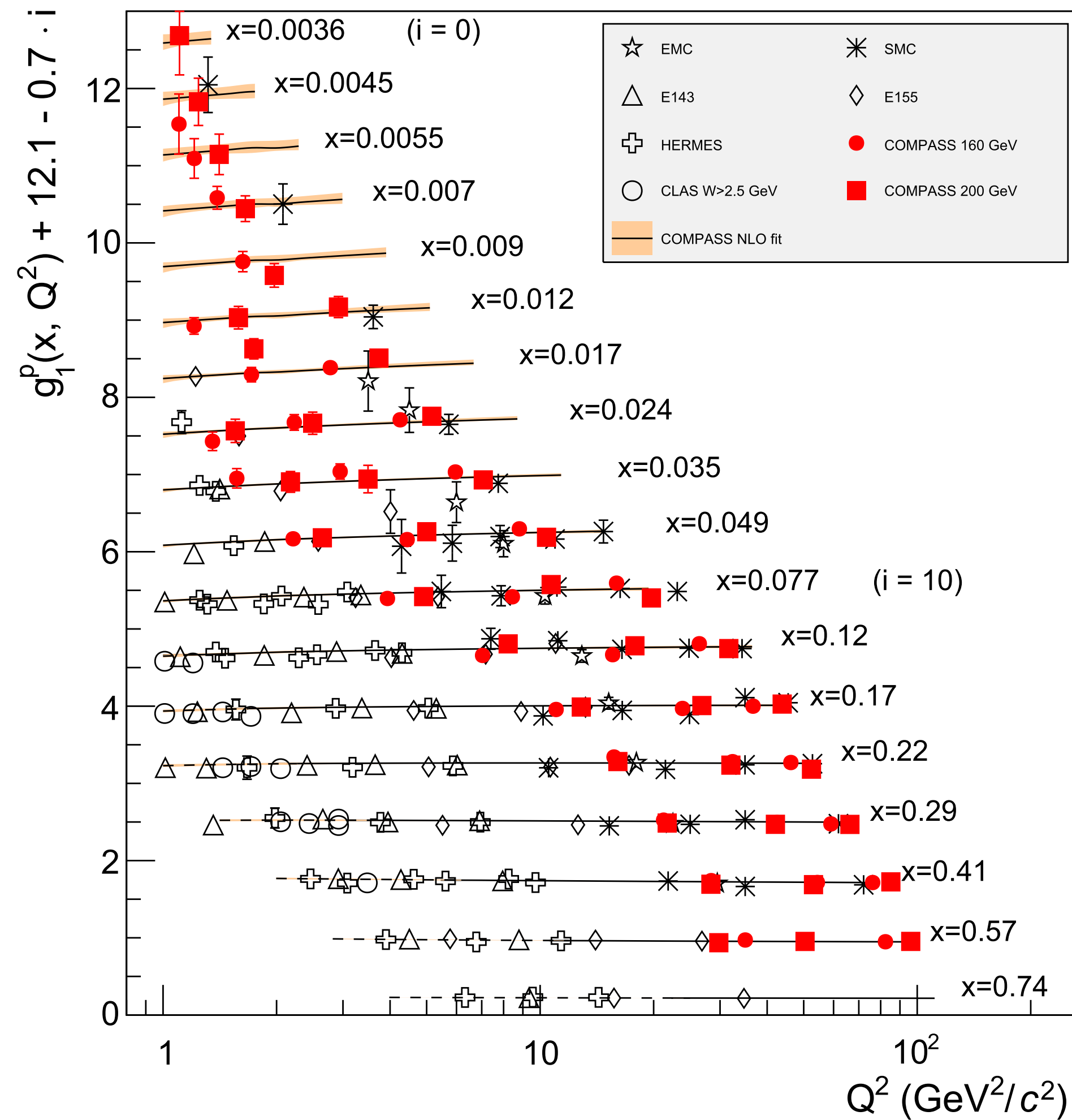


$$\int dx g_1(x, Q^2) = \frac{1}{36} (4\Delta\Sigma + 3\Delta q_3 + \Delta q_8)$$

Δq_3 from neutron β decay
 Δq_8 from hyperon β decay

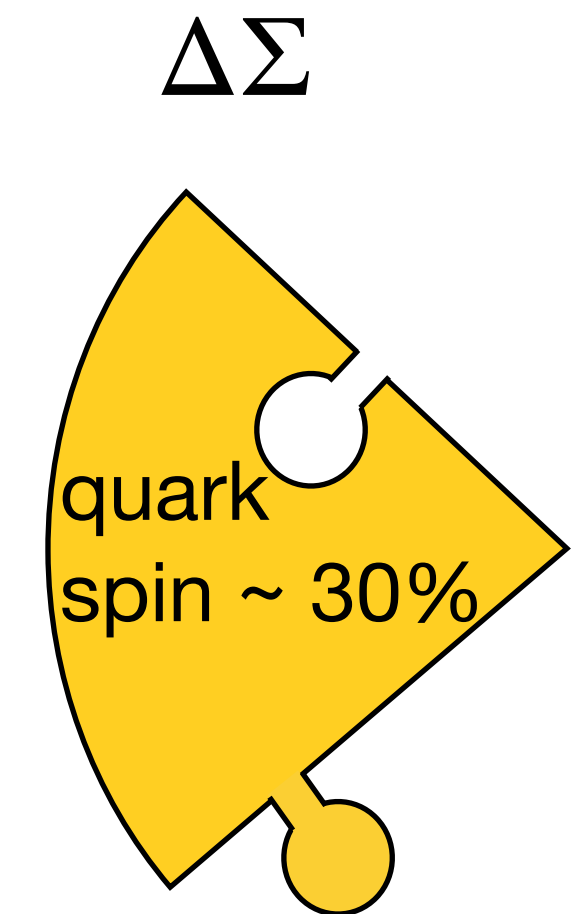
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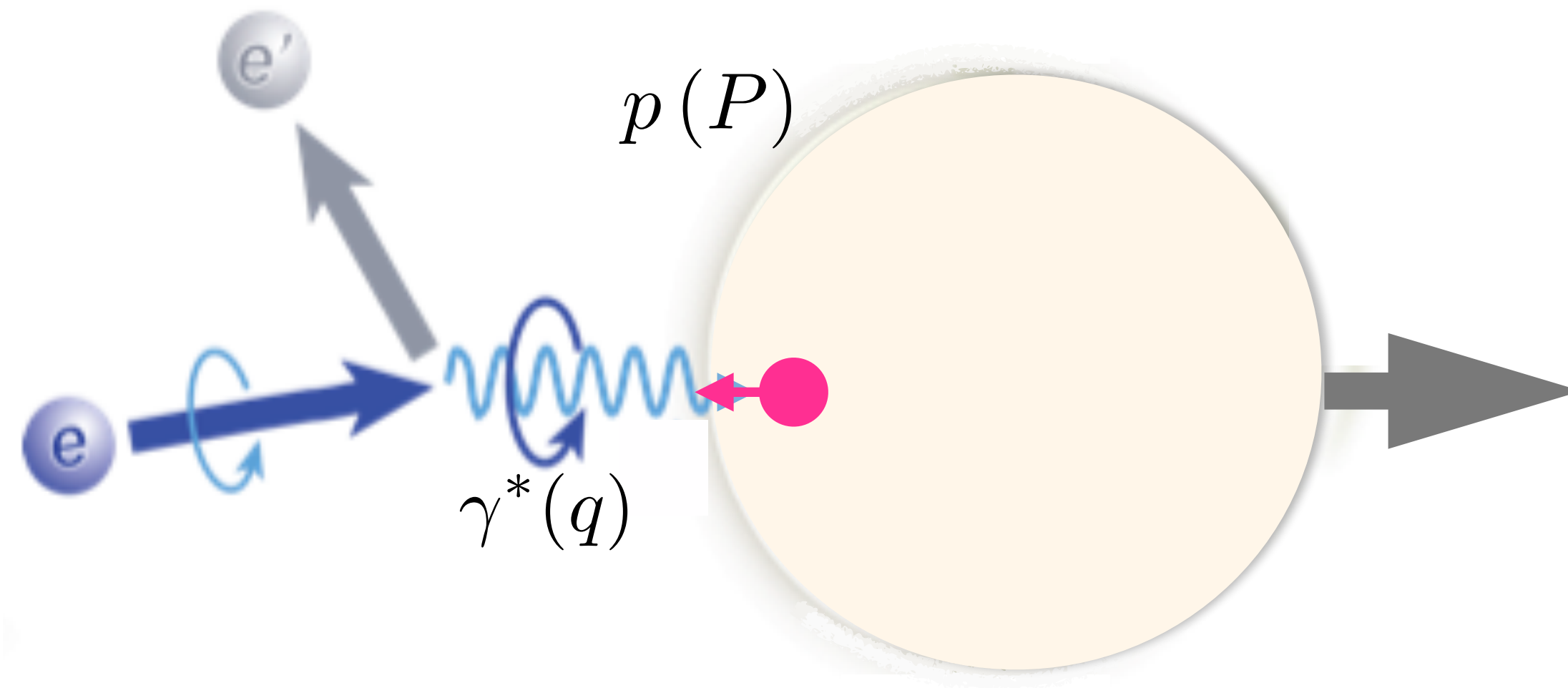
Δq_3 from neutron β decay
 Δq_8 from hyperon β decay



Quark flavour dependent helicity: single-hadron production in semi-inclusive DIS

$$Q^2 = -q^2$$

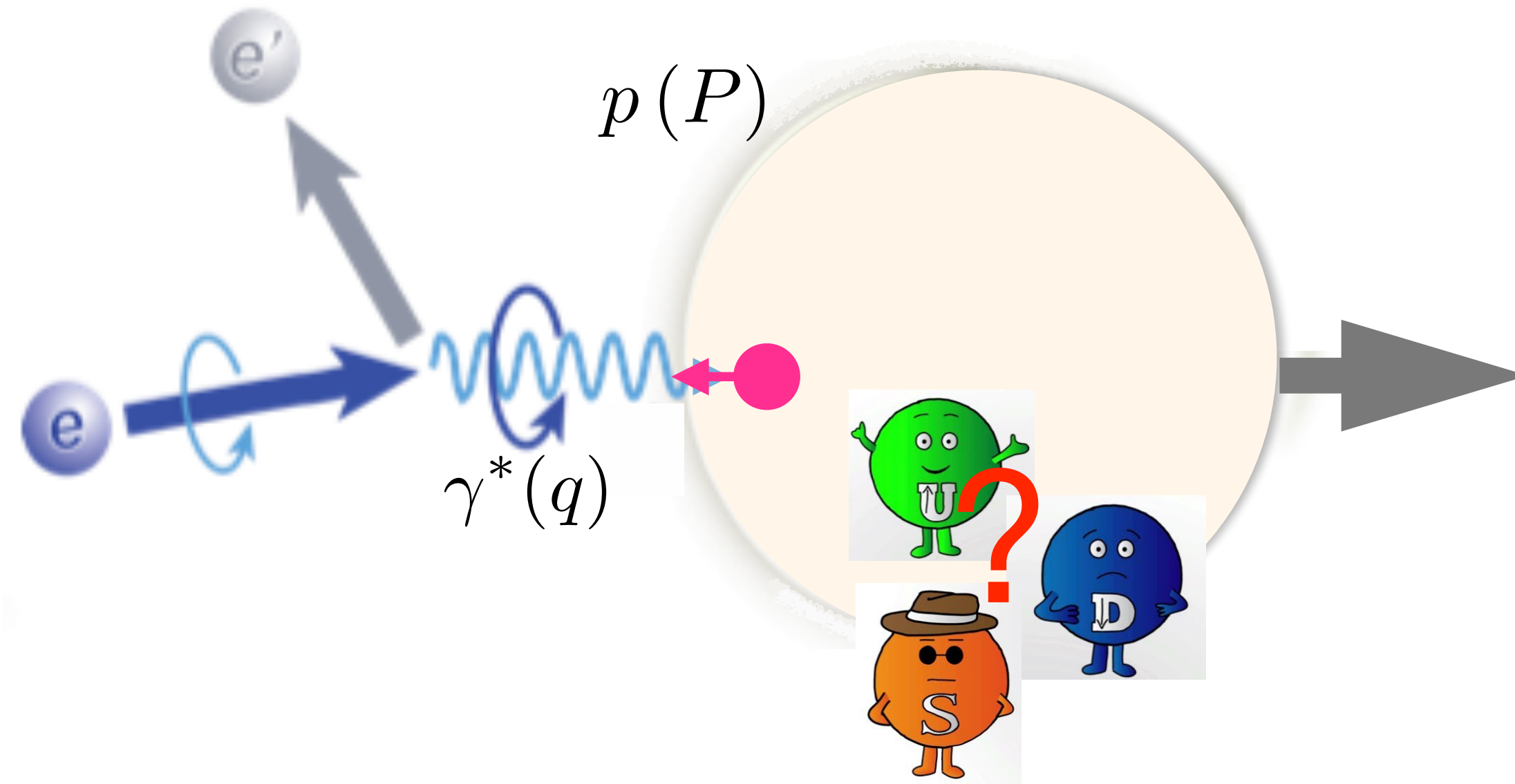
$$x_B = \frac{Q^2}{2P \cdot q}$$



Quark flavour dependent helicity: single-hadron production in semi-inclusive DIS

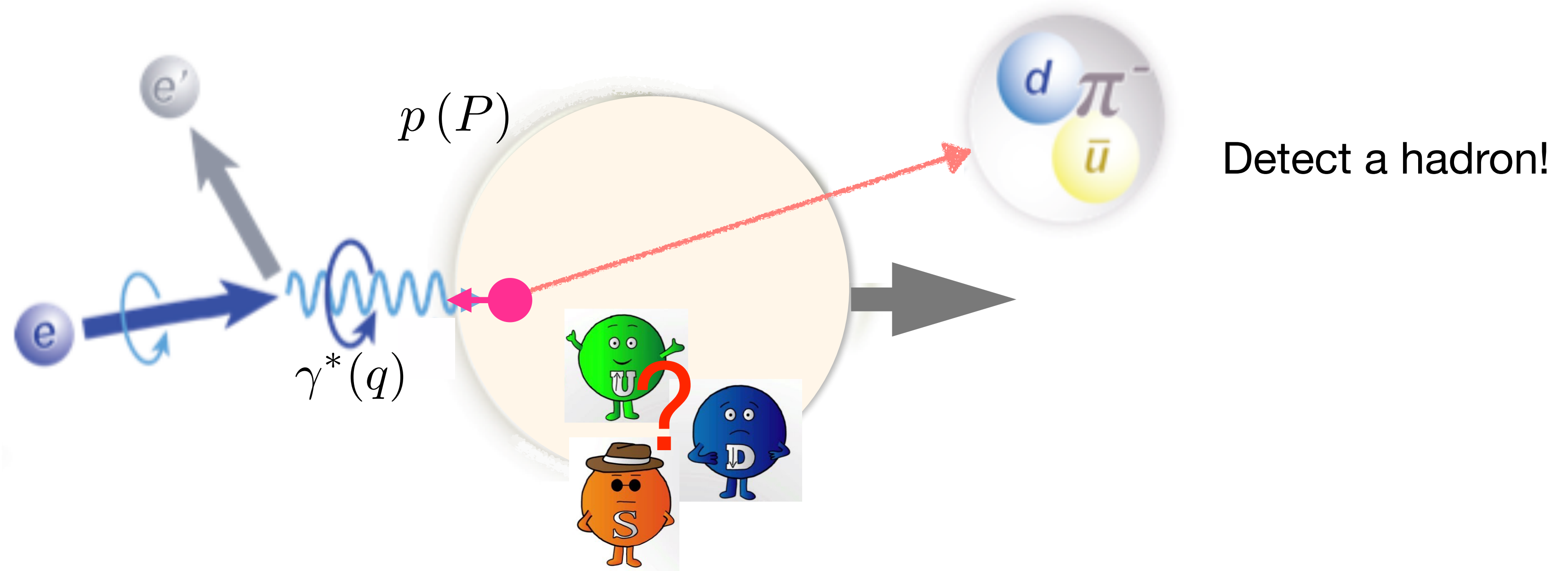
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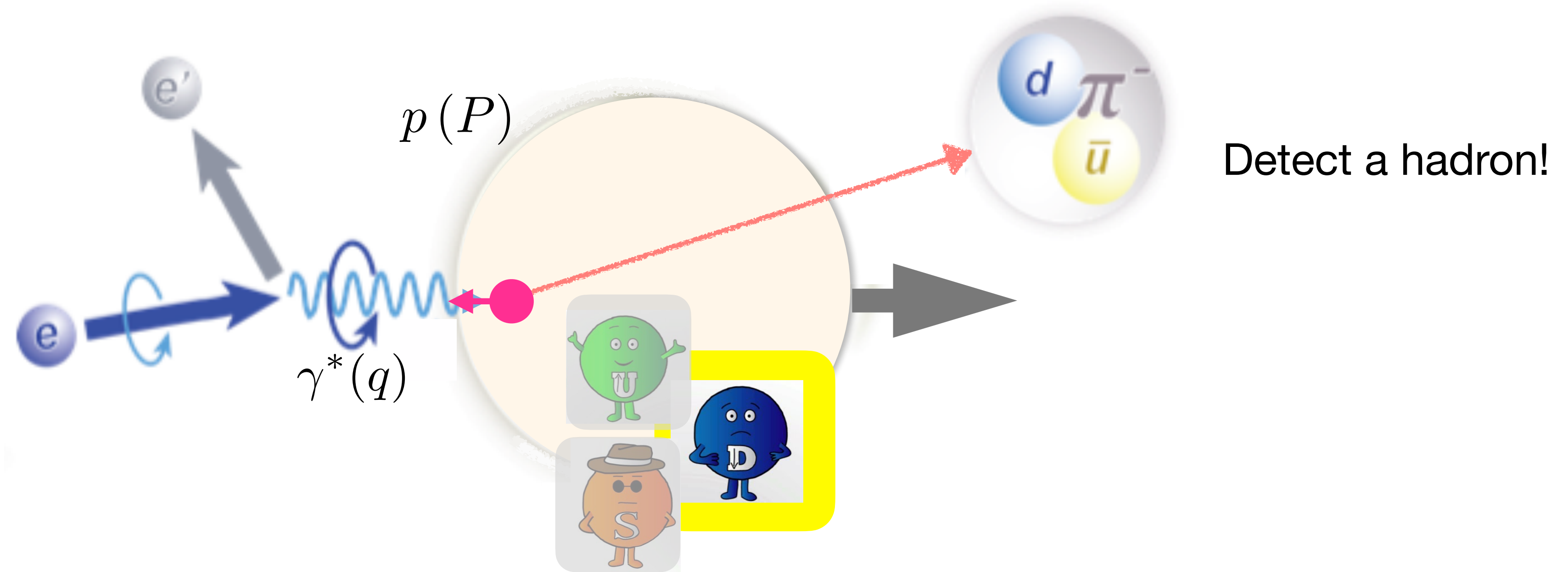
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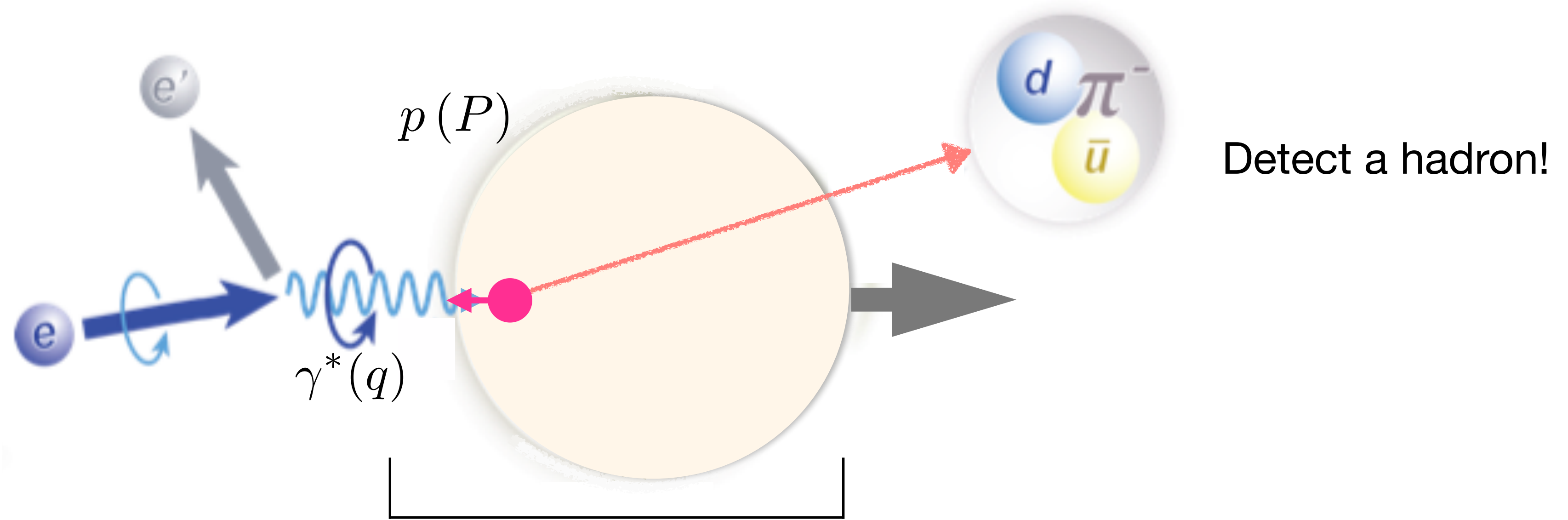
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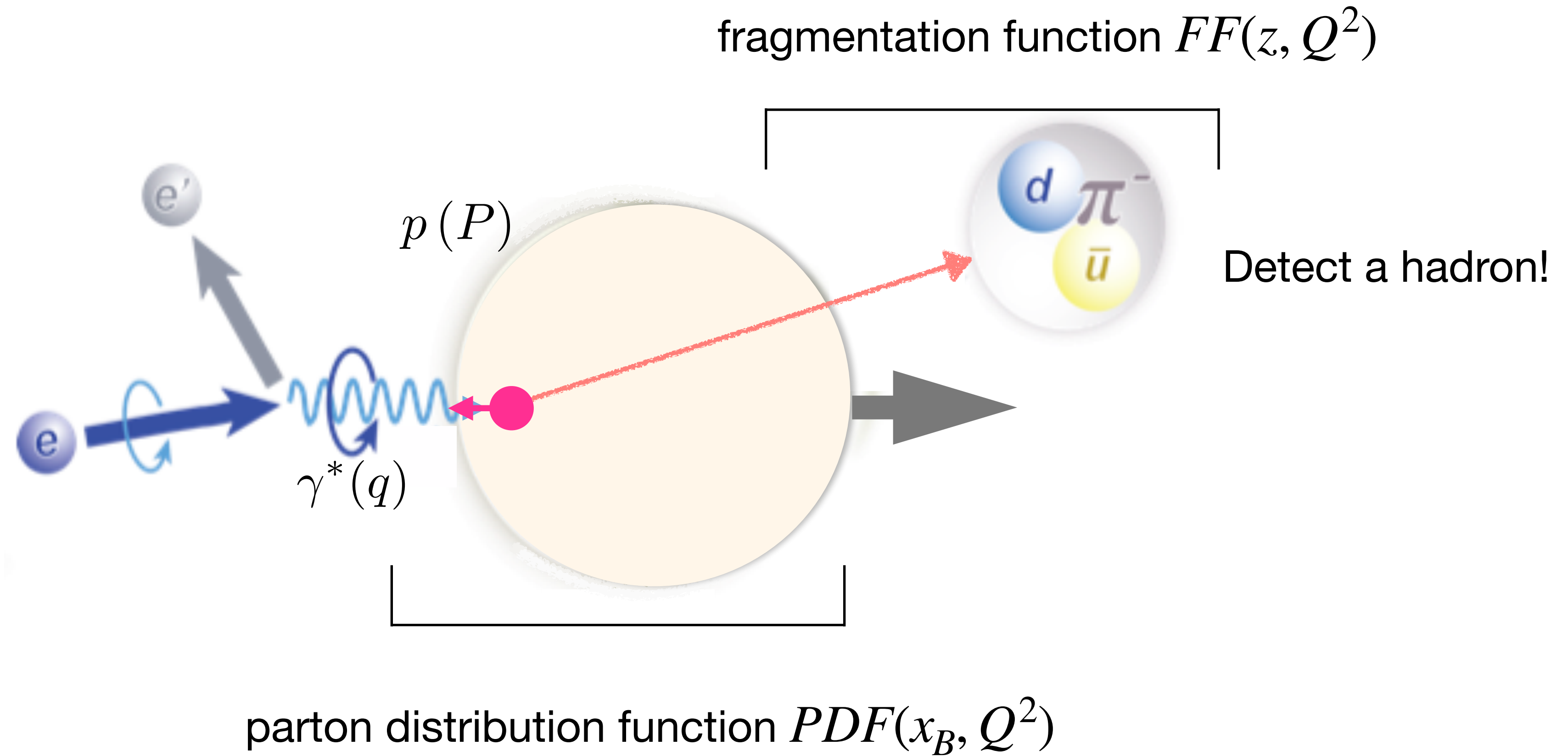


Quark flavour dependent helicity: single-hadron production in semi-inclusive DIS

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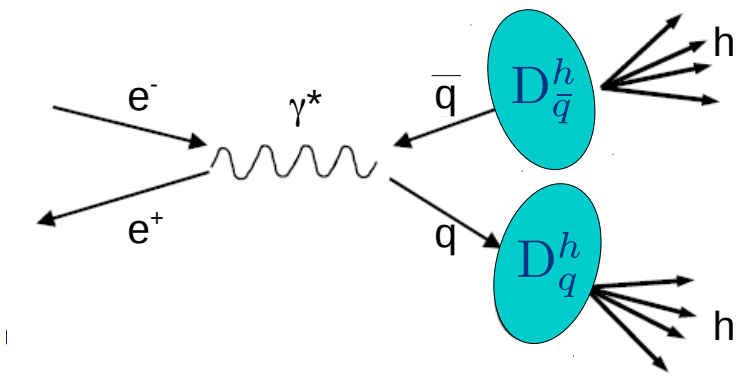
$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$



Quark flavour dependent helicity: single-hadron production in semi-inclusive DIS

fragmentation function:

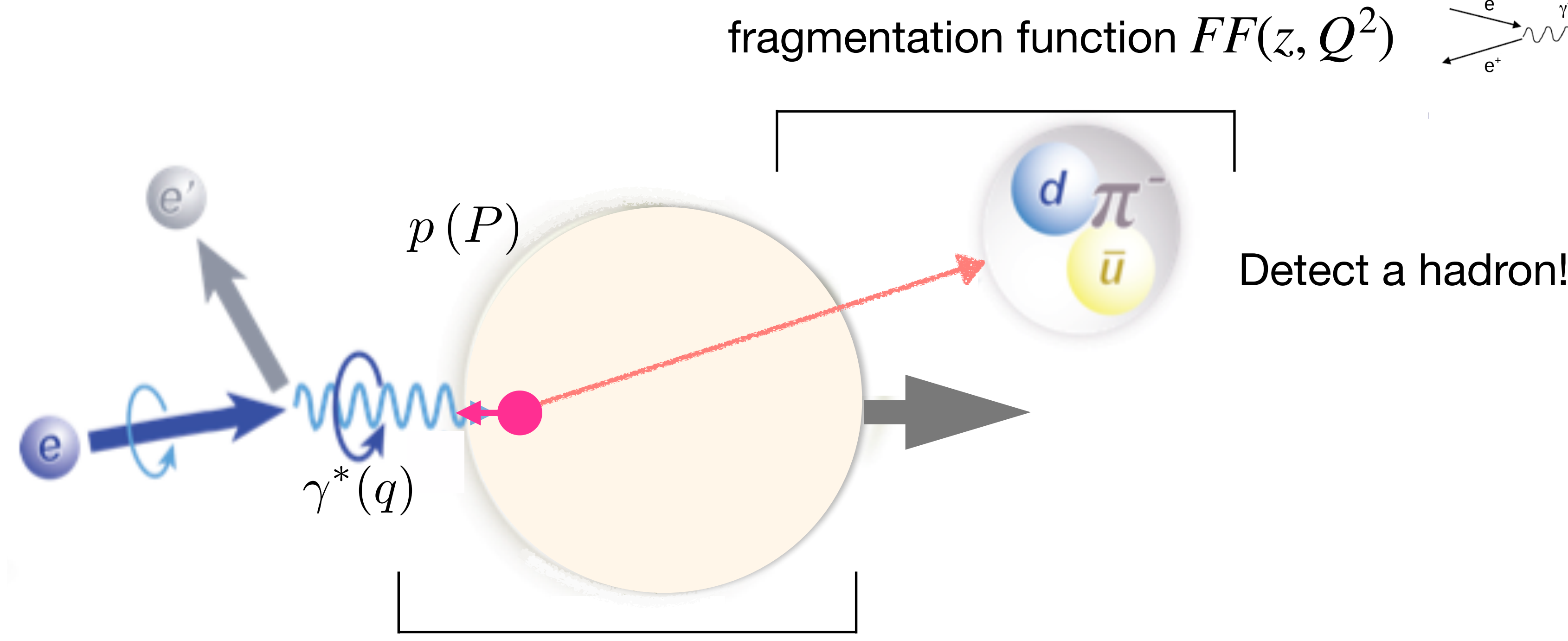
- e⁺e⁻ annihilation
- semi-inclusive DIS
- pp collisions



$$Q^2 = -q^2$$

$$x_B = \frac{Q^2}{2P \cdot q}$$

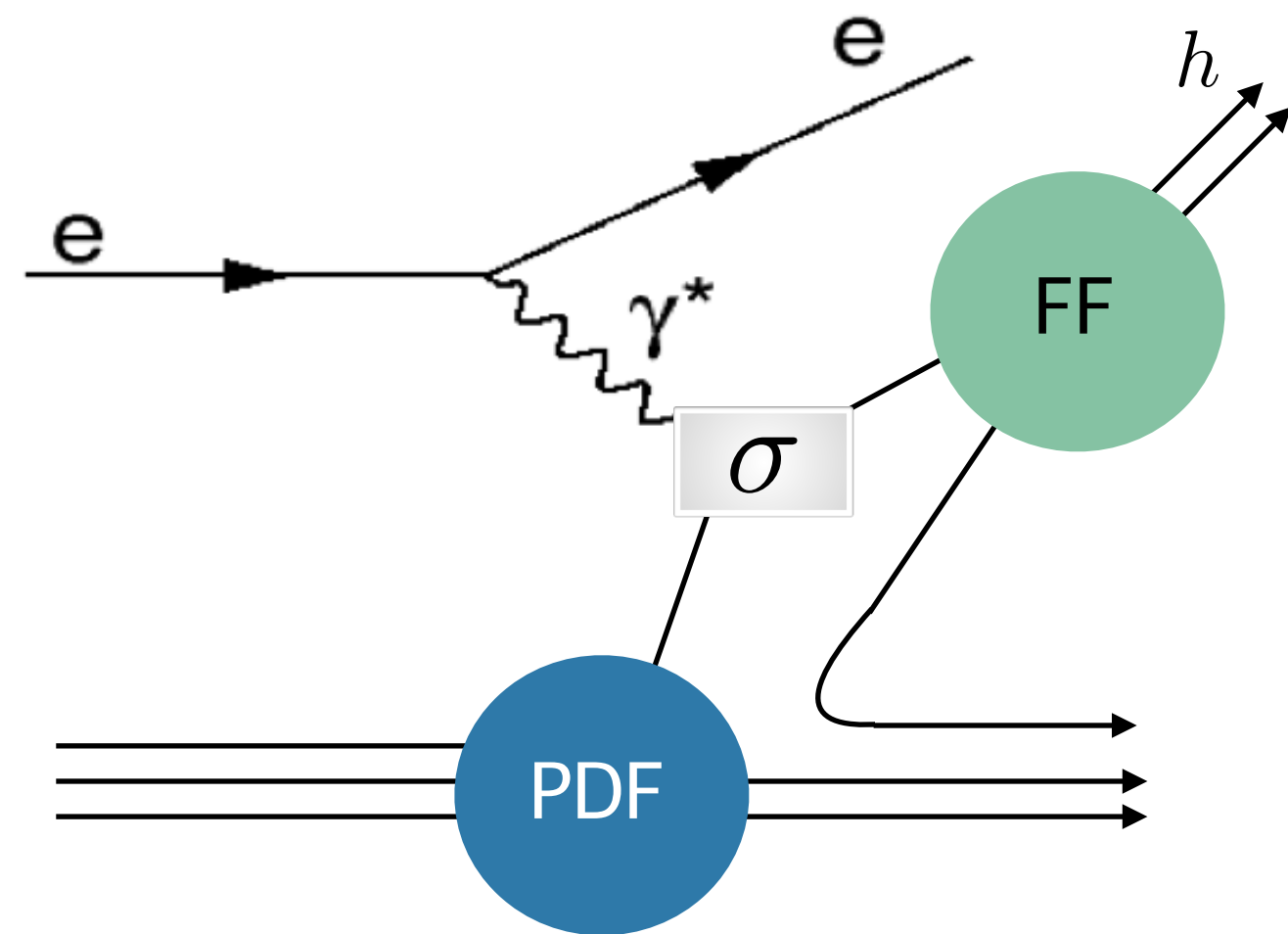
$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$



parton distribution function $PDF(x_B, Q^2)$

Detect a hadron!

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$$\text{Asymmetry: } \frac{\frac{\overleftrightarrow{N^h}}{\overleftrightarrow{L}} - \frac{\overrightarrow{N^h}}{\overrightarrow{L}}}{\frac{\overleftrightarrow{N^h}}{\overleftrightarrow{L}} + \frac{\overrightarrow{N^h}}{\overrightarrow{L}}}(x_B, Q^2, z)$$

$$\propto \sum_q e_q^2 \left[\Delta q \otimes w_1 D_1^{q \rightarrow h} \right]$$

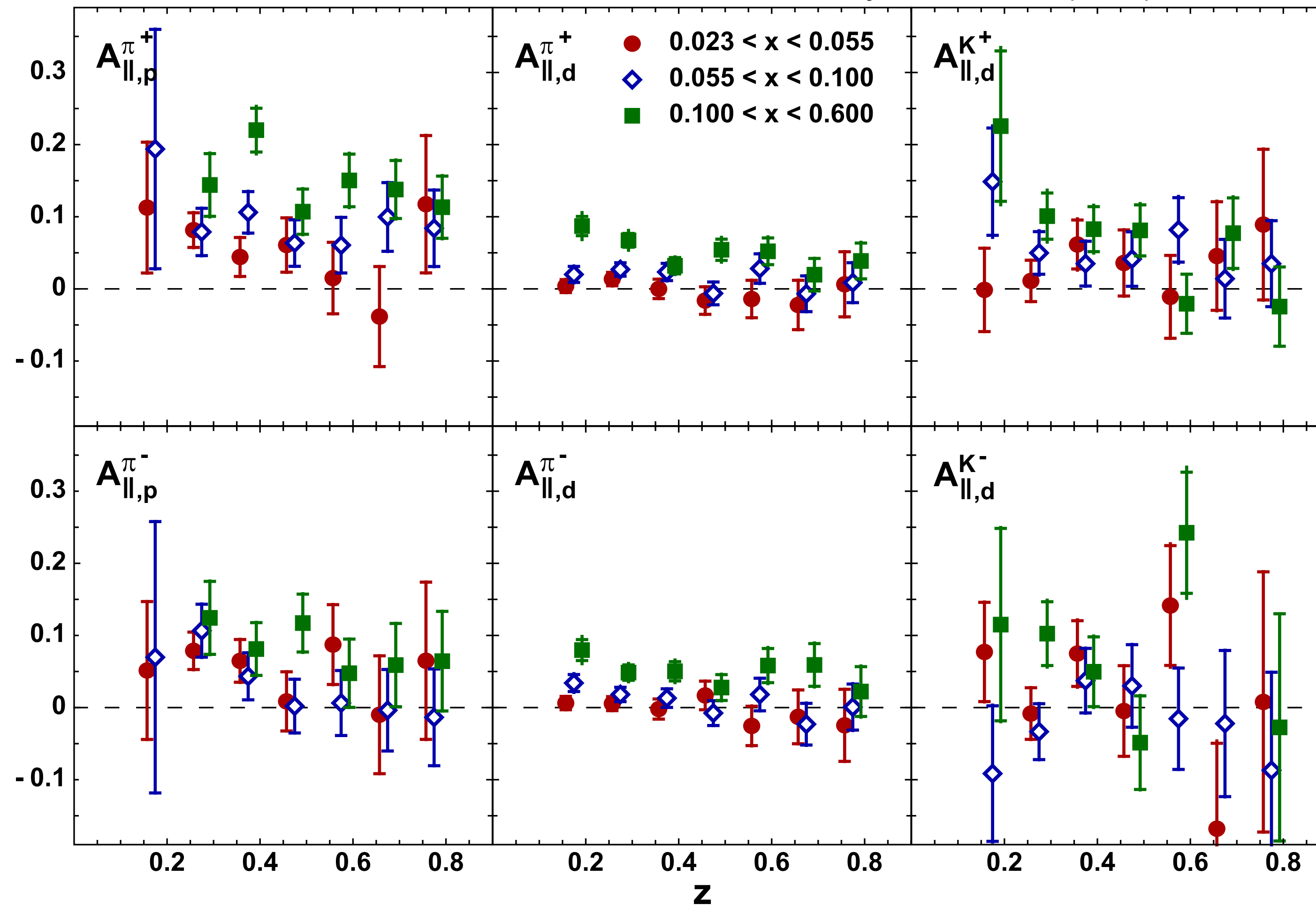
FF

Semi-inclusive measurements

→ access to flavour-dependent quark spin contribution

Single-hadron asymmetry from semi-inclusive DIS

HERMES, Phys. Rev. D **99** (2019) 11, 112001



Single-hadron asymmetry from semi-inclusive DIS

At leading order and leading twist

$$A_1^h(x, Q^2, z) = \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)}$$

and assuming $D^{q \rightarrow h^+} = D^{\bar{q} \rightarrow h^-}$:

$$A_{1,d}^{h^+ - h^-} = \frac{4\Delta u_v + \Delta d_v}{4u_v + d_v}$$

$$A_{1,p}^{h^+ - h^-} = \frac{4\Delta u_v - \Delta d_v}{4u_v - d_v}$$

Single-hadron asymmetry from semi-inclusive DIS

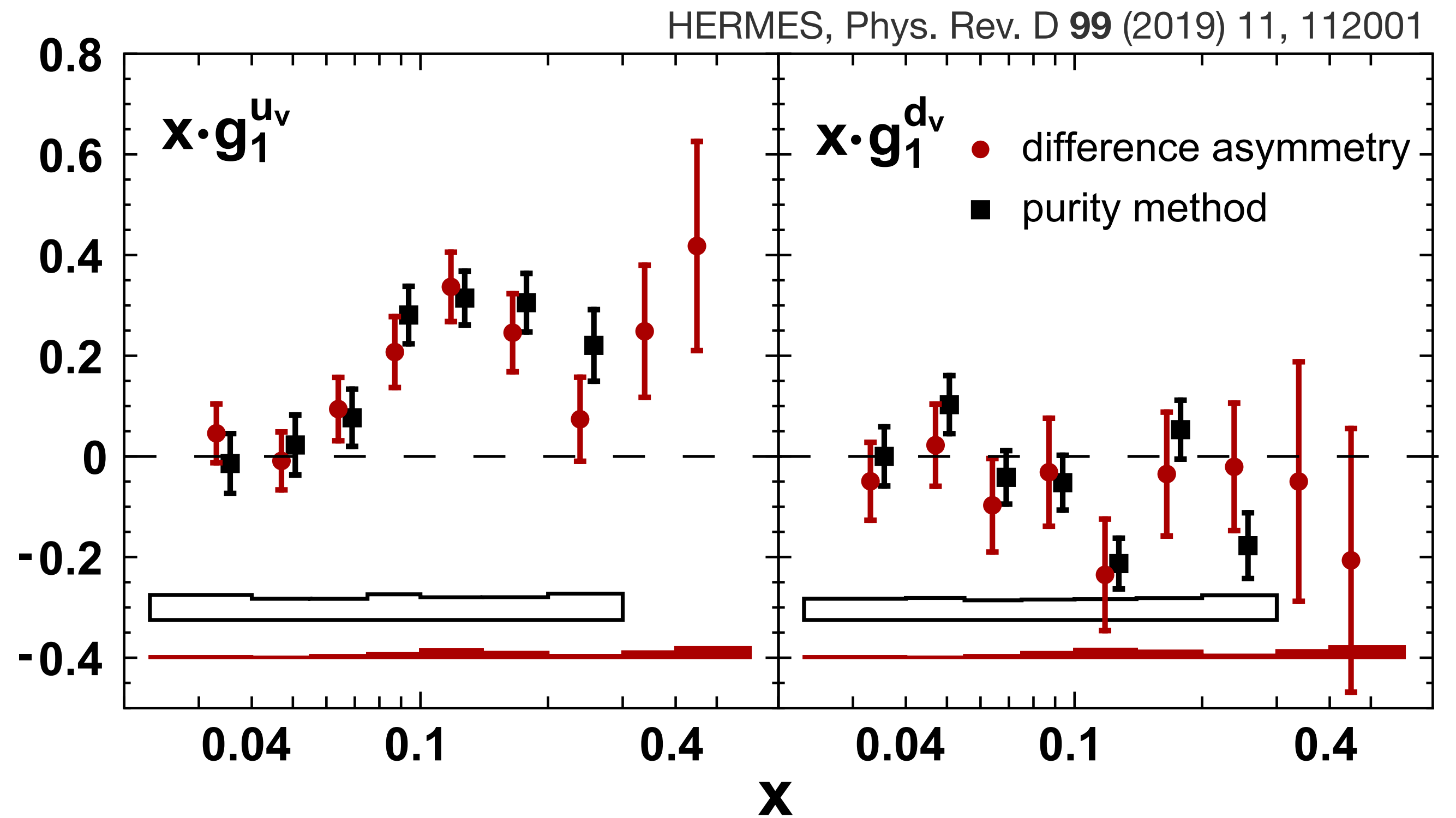
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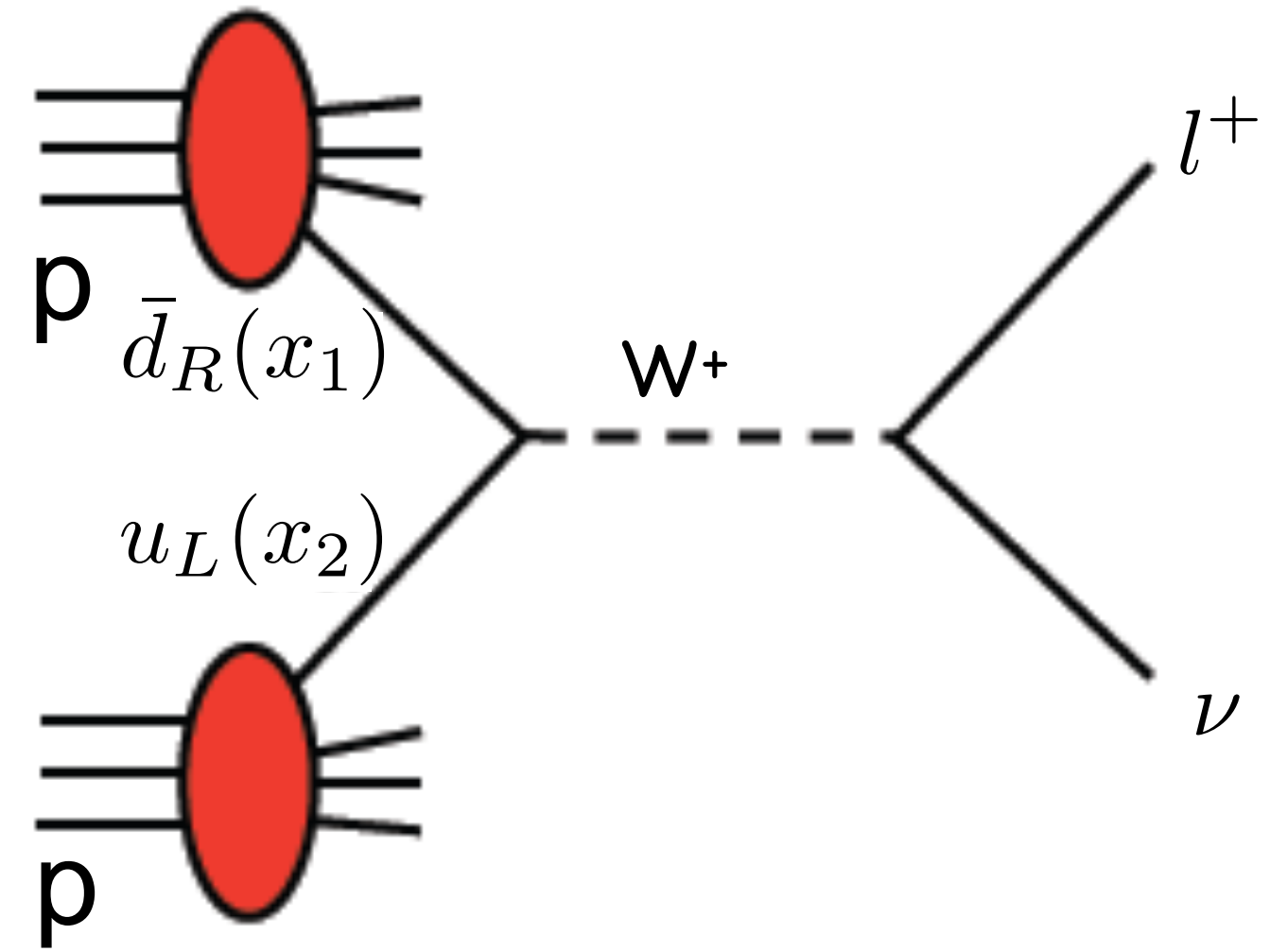
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Access to helicity distributions through pp collisions

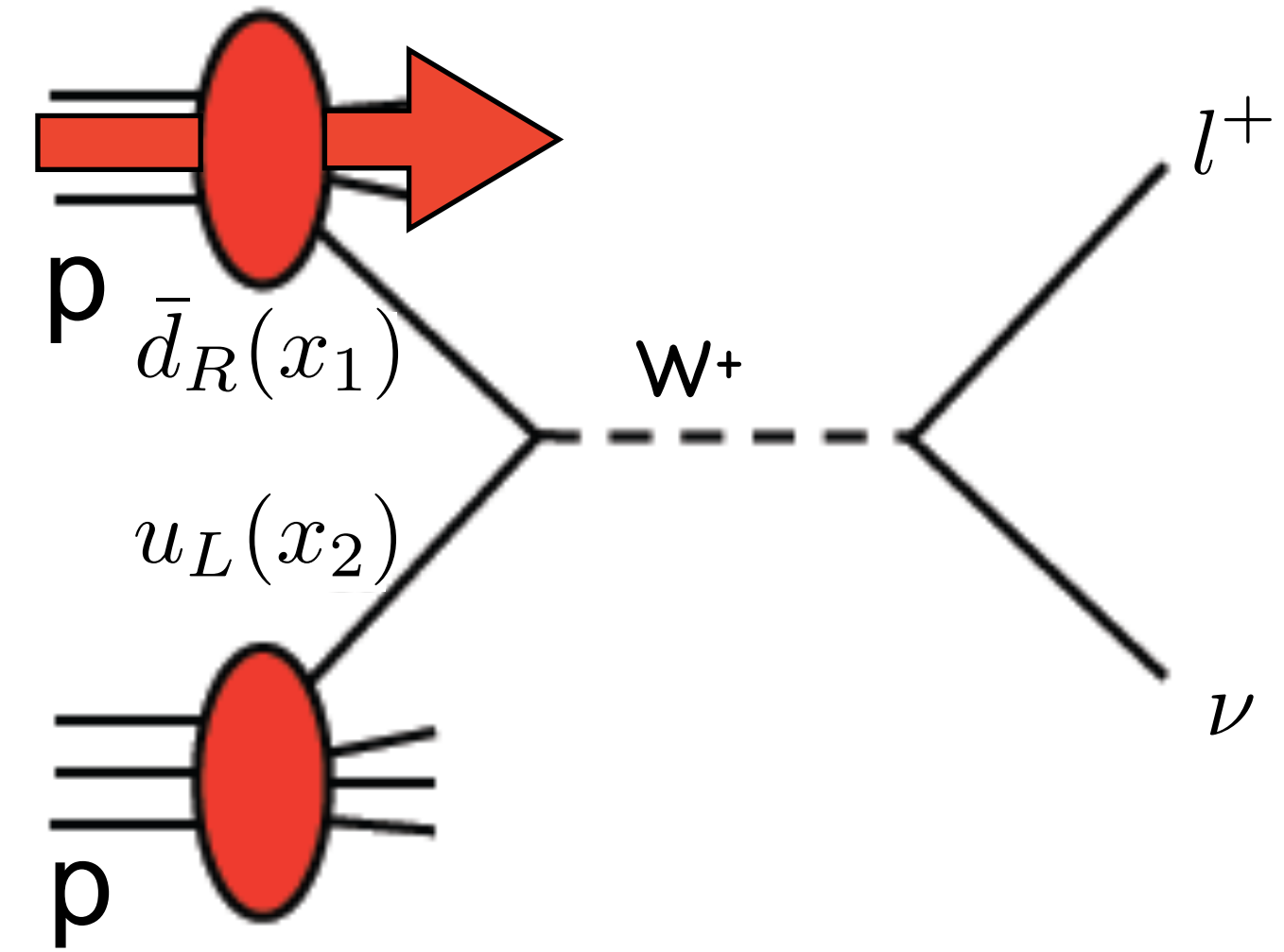
Weak interaction: only coupling to left-handed fermions
and right-handed anti-fermions: $u_L \bar{d}_R \rightarrow W^+$ and $\bar{u}_R d_L \rightarrow W^-$



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$$\vec{N} \sim \vec{\bar{d}}(x_1)u(x_2) + \vec{\bar{u}}(x_1)\vec{d}(x_2)$$

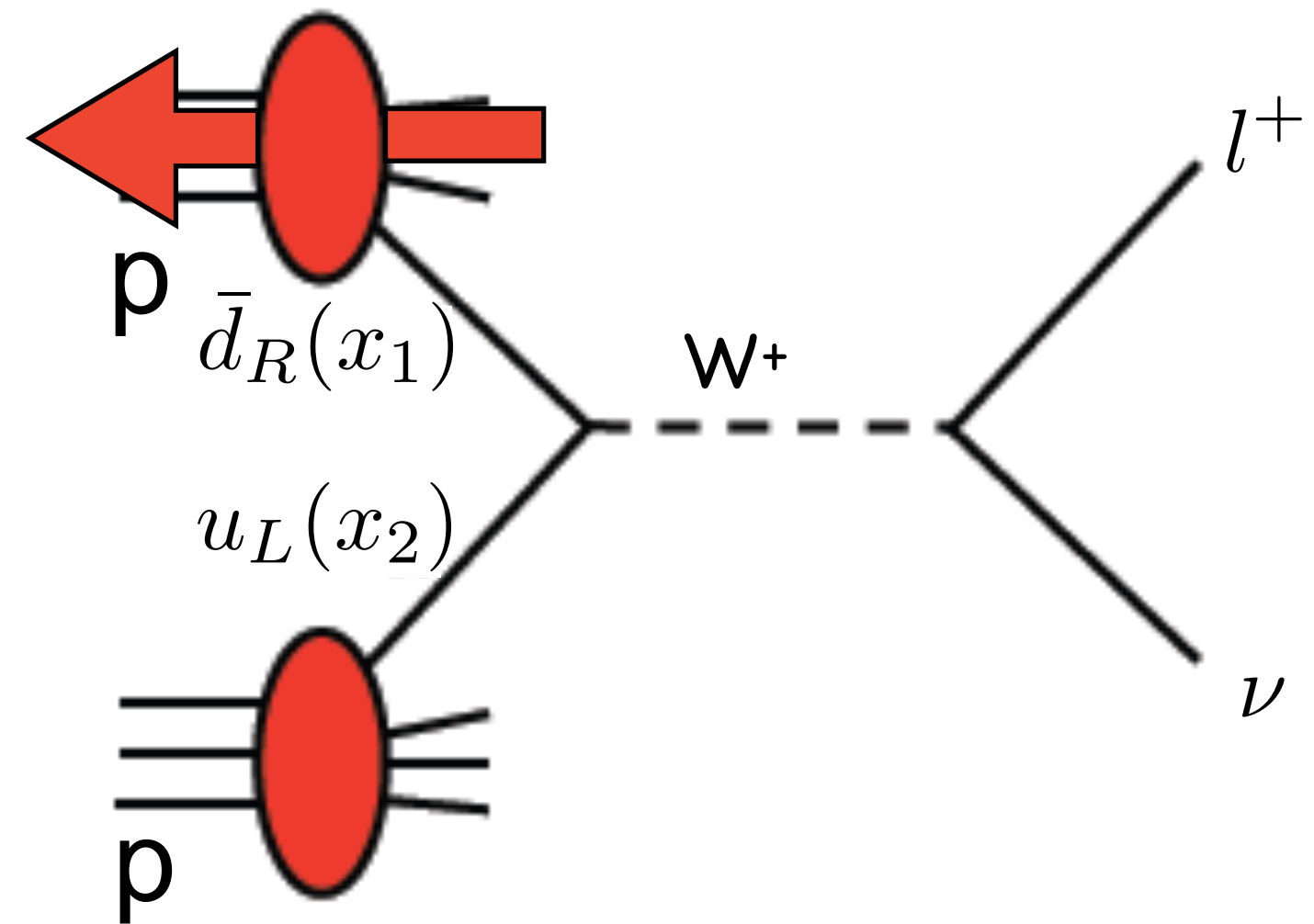


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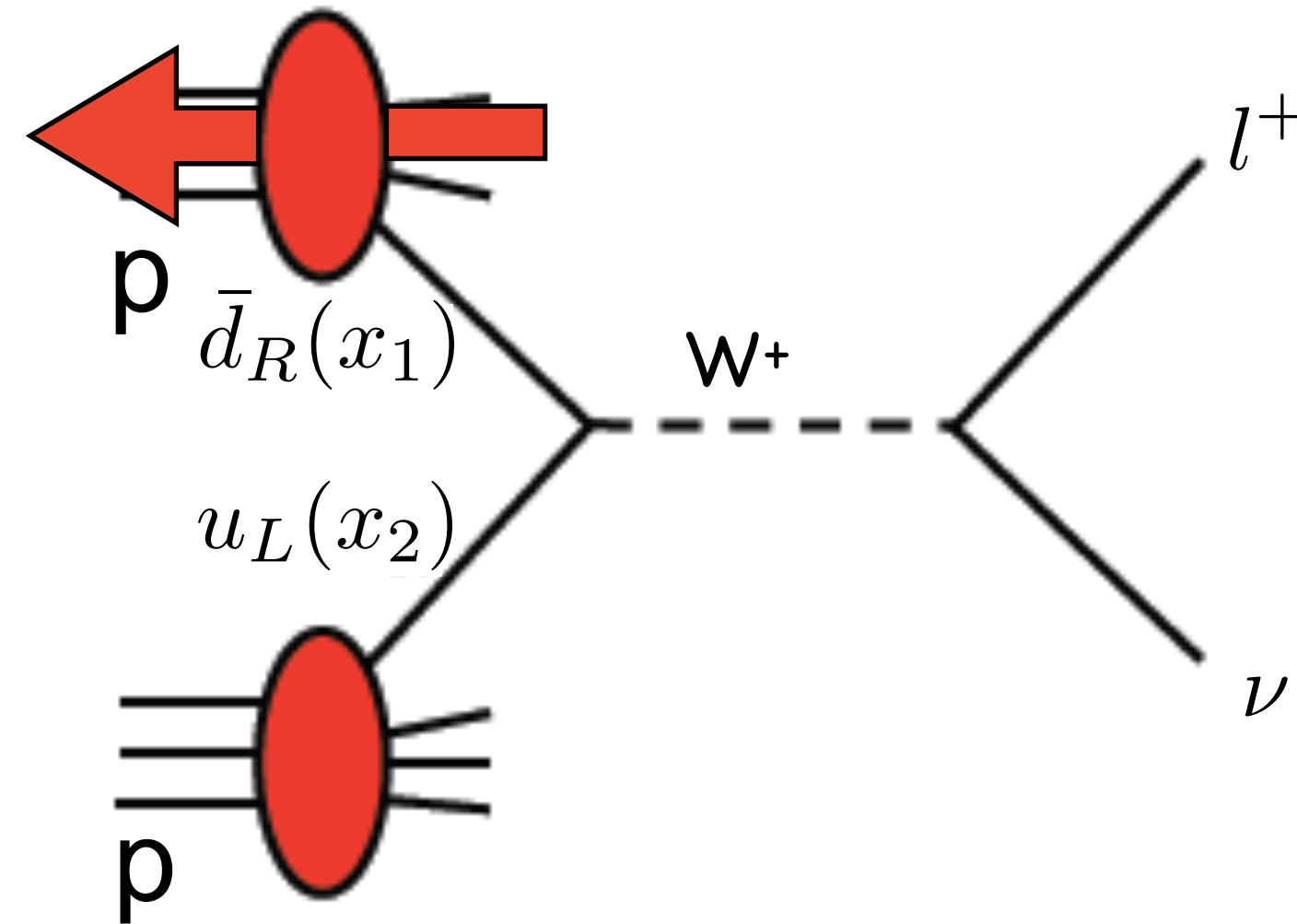
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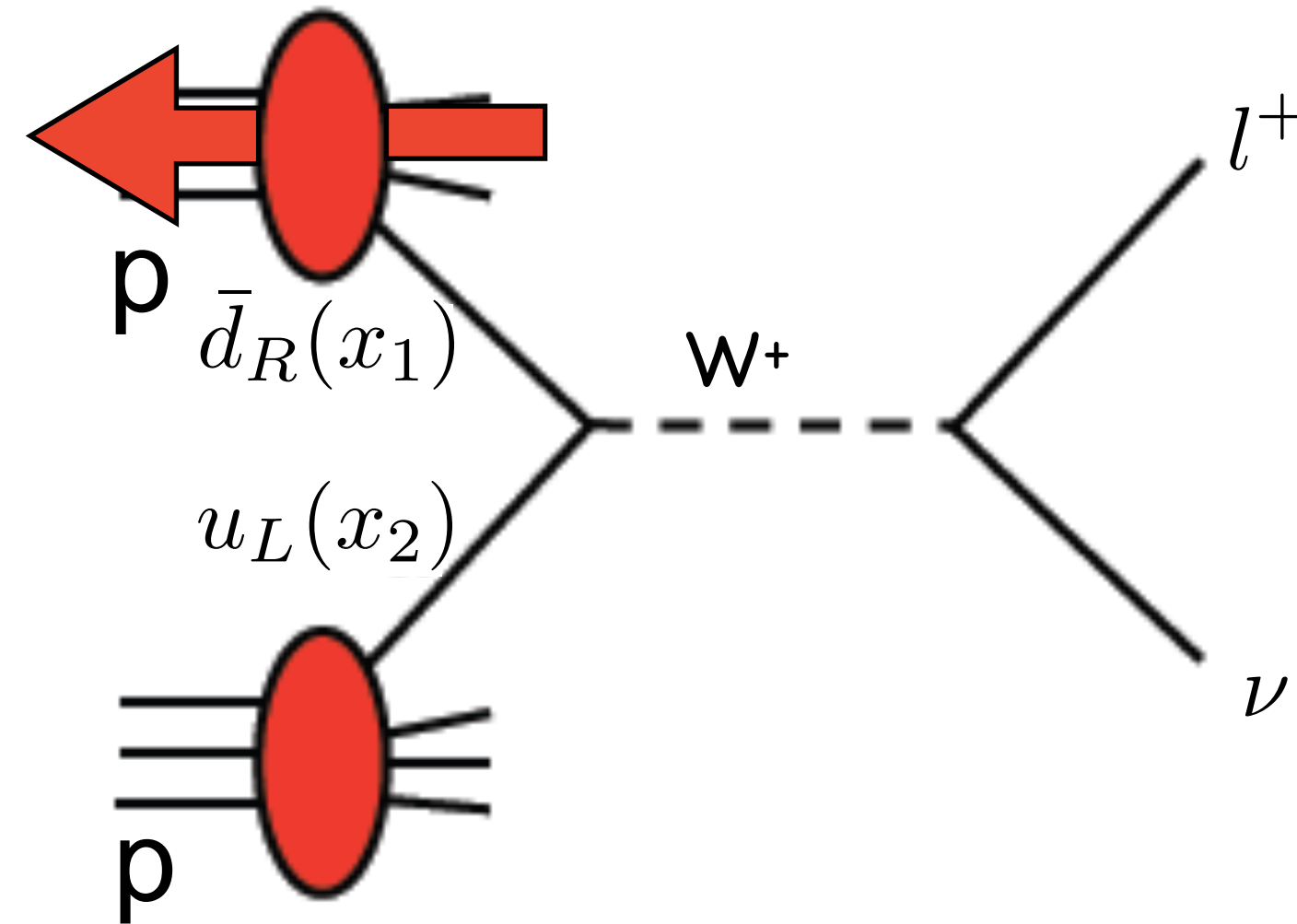


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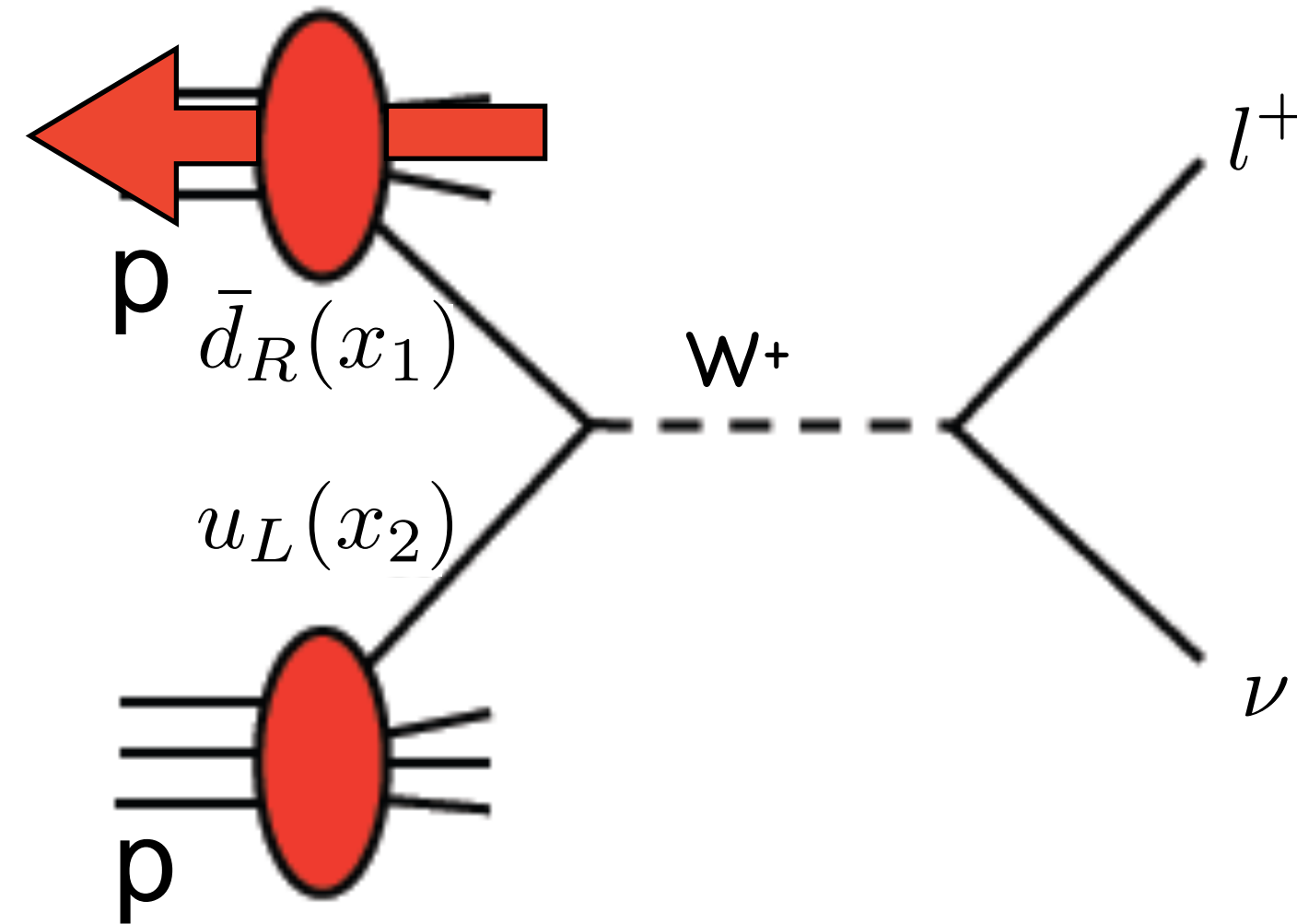
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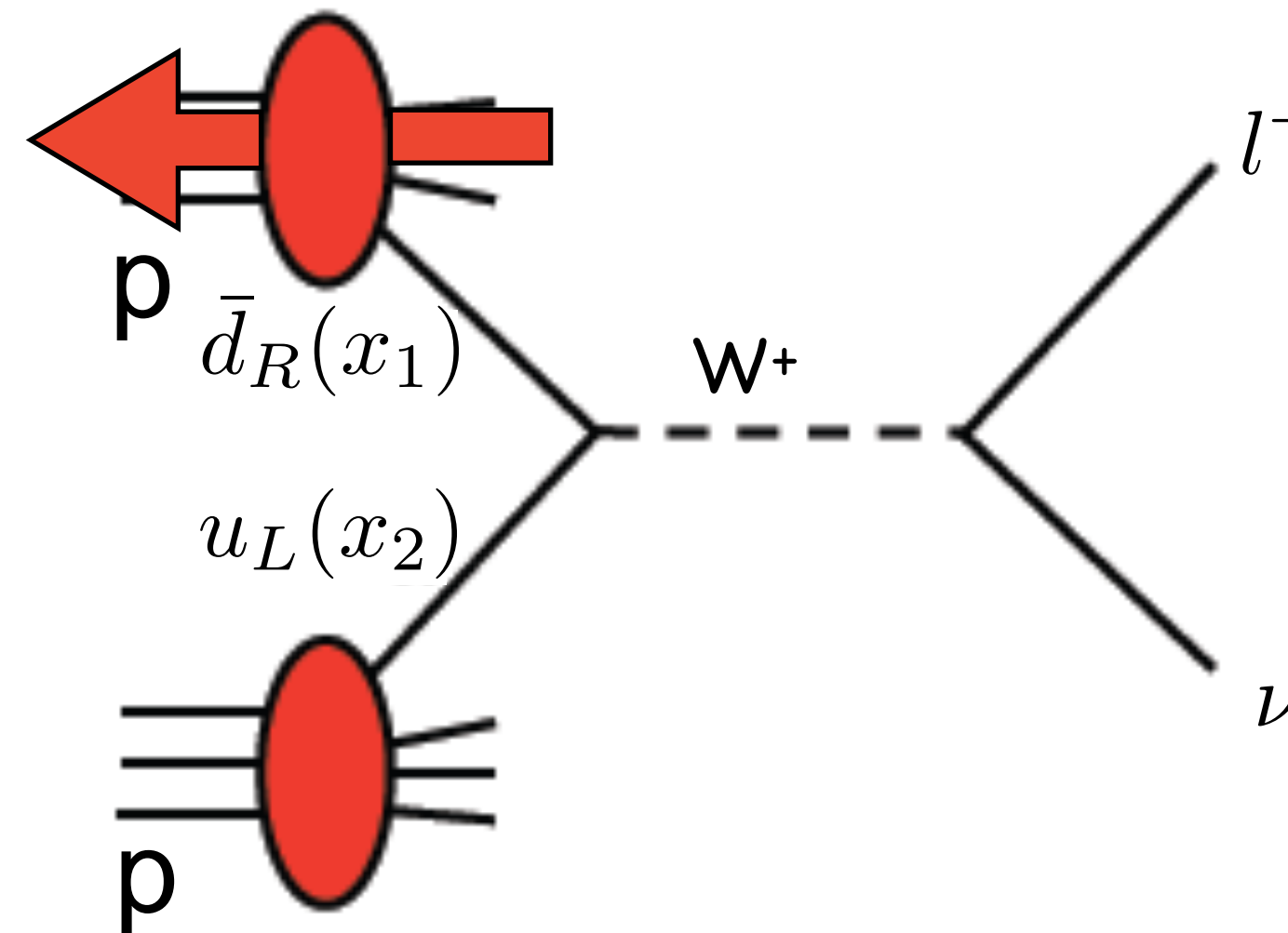
$$= \frac{\Delta \bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{\bar{d}(x_1)u(x_2) + u(x_1)\bar{d}(x_2)}$$

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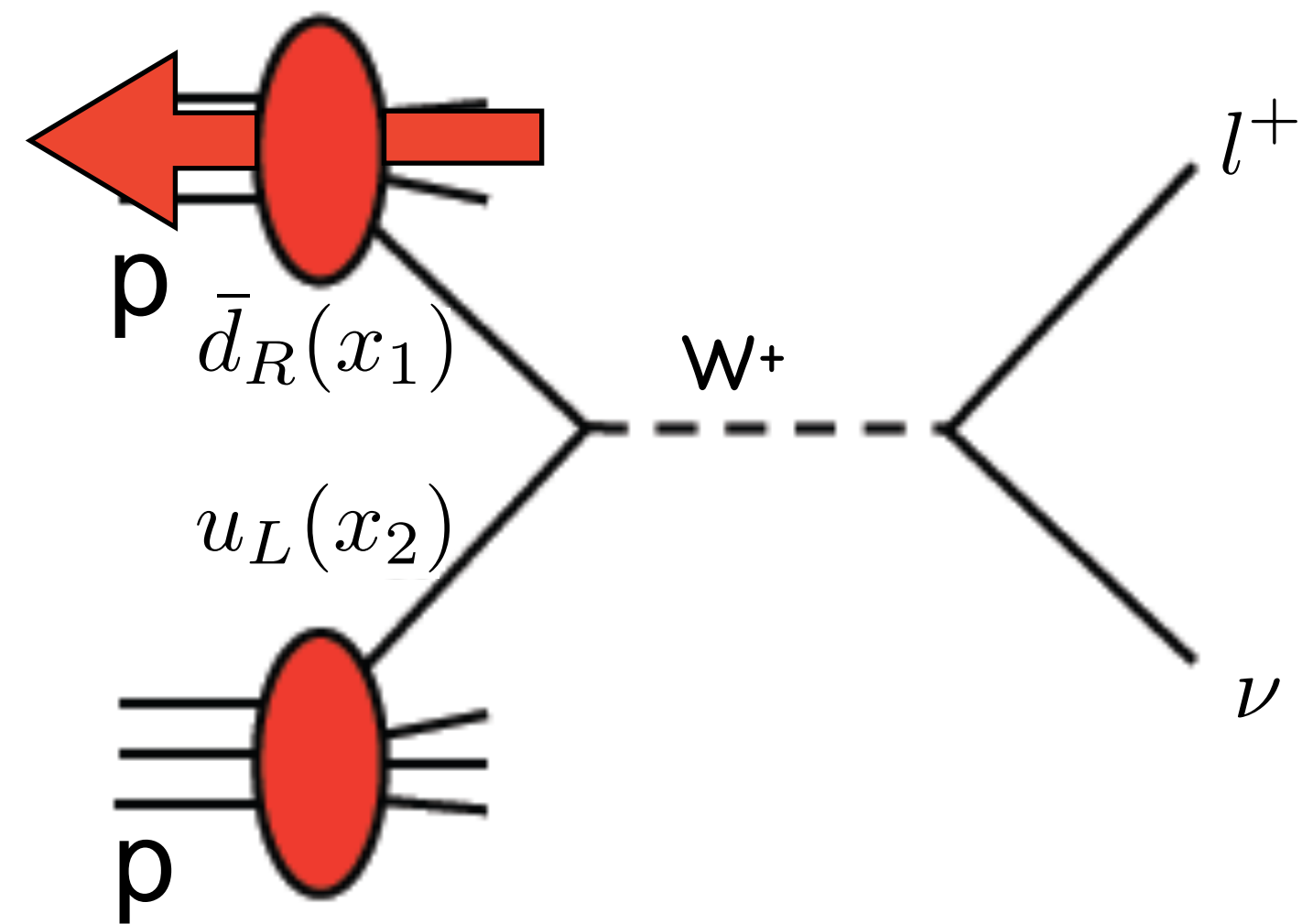
$$= \frac{\Delta \bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{\bar{d}(x_1)u(x_2) + u(x_1)\bar{d}(x_2)} \xrightarrow{x_1 \gg x_2} \frac{-\Delta u(x_1)}{u(x_1)}$$

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$x_1 \gg x_2$
 \swarrow
 $x_2 \gg x_1$
 \searrow

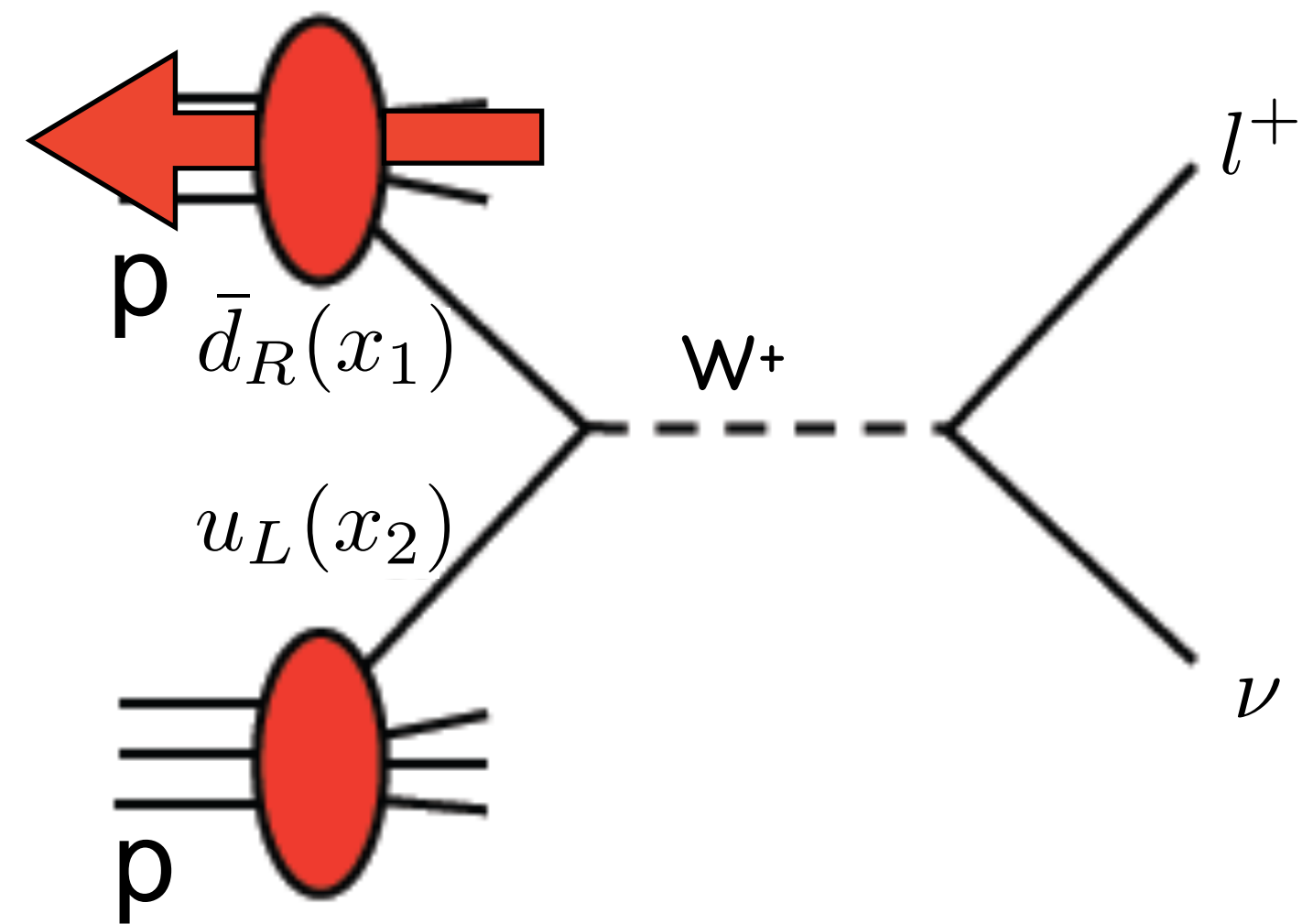
$\frac{-\Delta u(x_1)}{u(x_1)}$
 $\frac{\Delta \bar{d}(x_1)}{\bar{d}(x_1)}$

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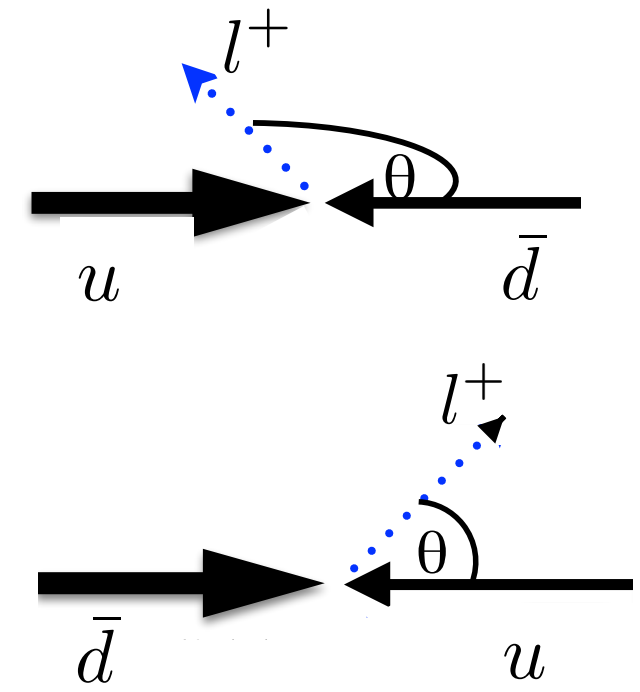


$$\rightarrow A_L^{W^+} = \frac{\vec{N} - \overleftarrow{N}}{\vec{N} + \overleftarrow{N}} = \frac{\vec{\bar{d}}(x_1)u(x_2) + \vec{\bar{u}}(x_1)\bar{d}(x_2) - \overleftarrow{\bar{d}}(x_1)u(x_2) - \overleftarrow{\bar{u}}(x_1)\bar{d}(x_2)}{\vec{\bar{d}}(x_1)u(x_2) + \vec{\bar{u}}(x_1)\bar{d}(x_2) + \overleftarrow{\bar{d}}(x_1)u(x_2) + \overleftarrow{\bar{u}}(x_1)\bar{d}(x_2)}$$

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$x_1 \gg x_2$
 $x_2 \gg x_1$

$\frac{-\Delta u(x_1)}{u(x_1)}$
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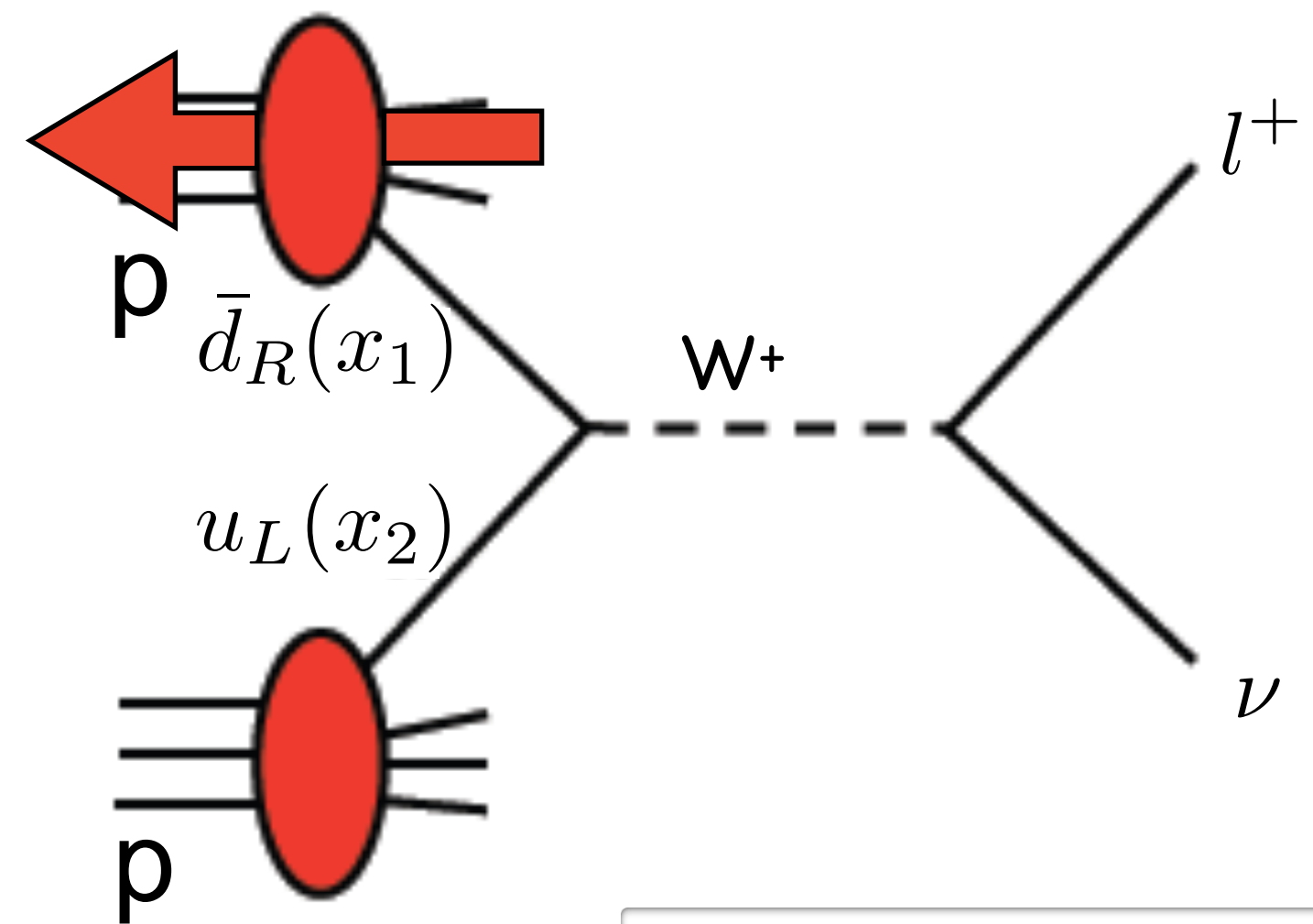


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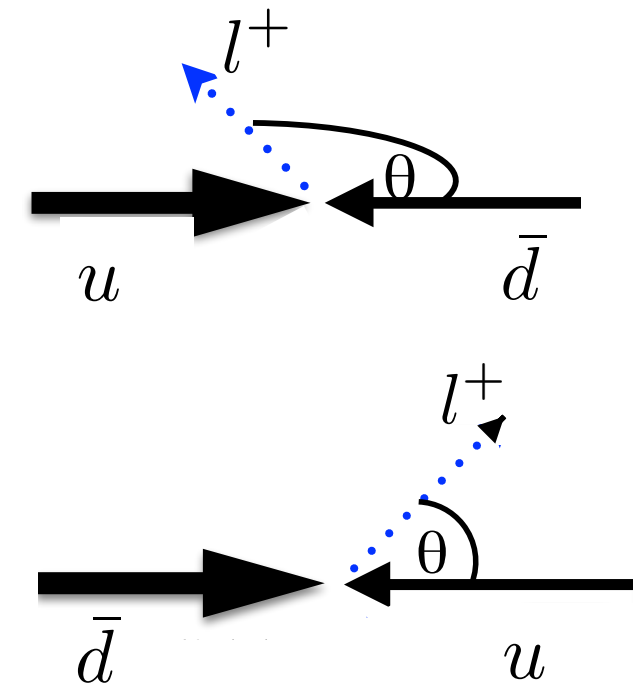
- Complementary access to Δq
- No need for FFs
- Higher Q^2 than (fixed-target) DIS

$$\rightarrow A_L^{W^+} = \frac{\vec{N} - \overleftarrow{N}}{\vec{N} + \overleftarrow{N}} = \frac{\vec{\bar{d}}(x_1)u(x_2) + \vec{\bar{u}}(x_1)\bar{d}(x_2) - \overleftarrow{\bar{d}}(x_1)u(x_2) - \overleftarrow{\bar{u}}(x_1)\bar{d}(x_2)}{\vec{\bar{d}}(x_1)u(x_2) + \vec{\bar{u}}(x_1)\bar{d}(x_2) + \overleftarrow{\bar{d}}(x_1)u(x_2) + \overleftarrow{\bar{u}}(x_1)\bar{d}(x_2)}$$

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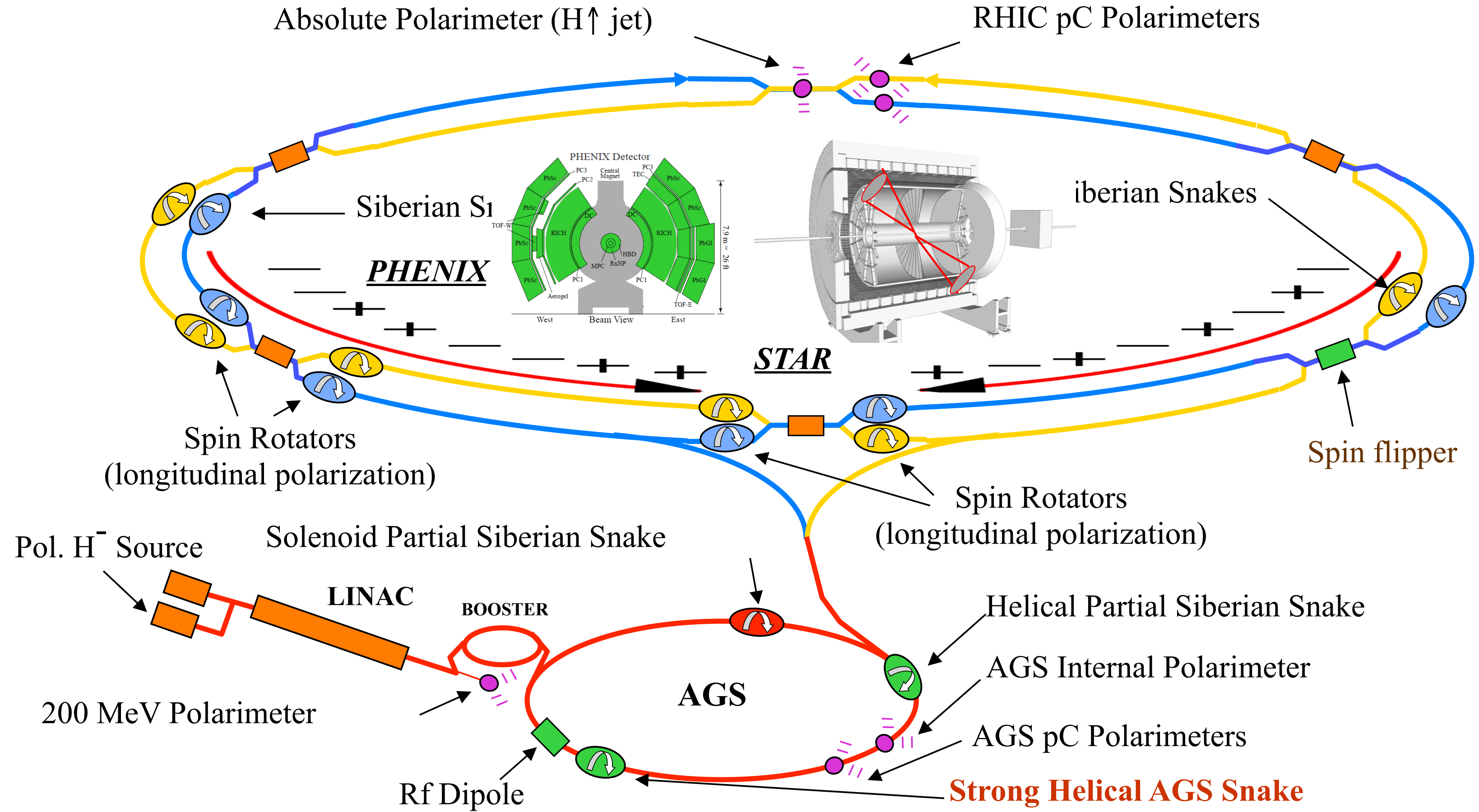
$\frac{-\Delta u(x_1)}{u(x_1)}$
 $\frac{\Delta \bar{d}(x_1)}{\bar{d}(x_1)}$



Polarised pp collisions

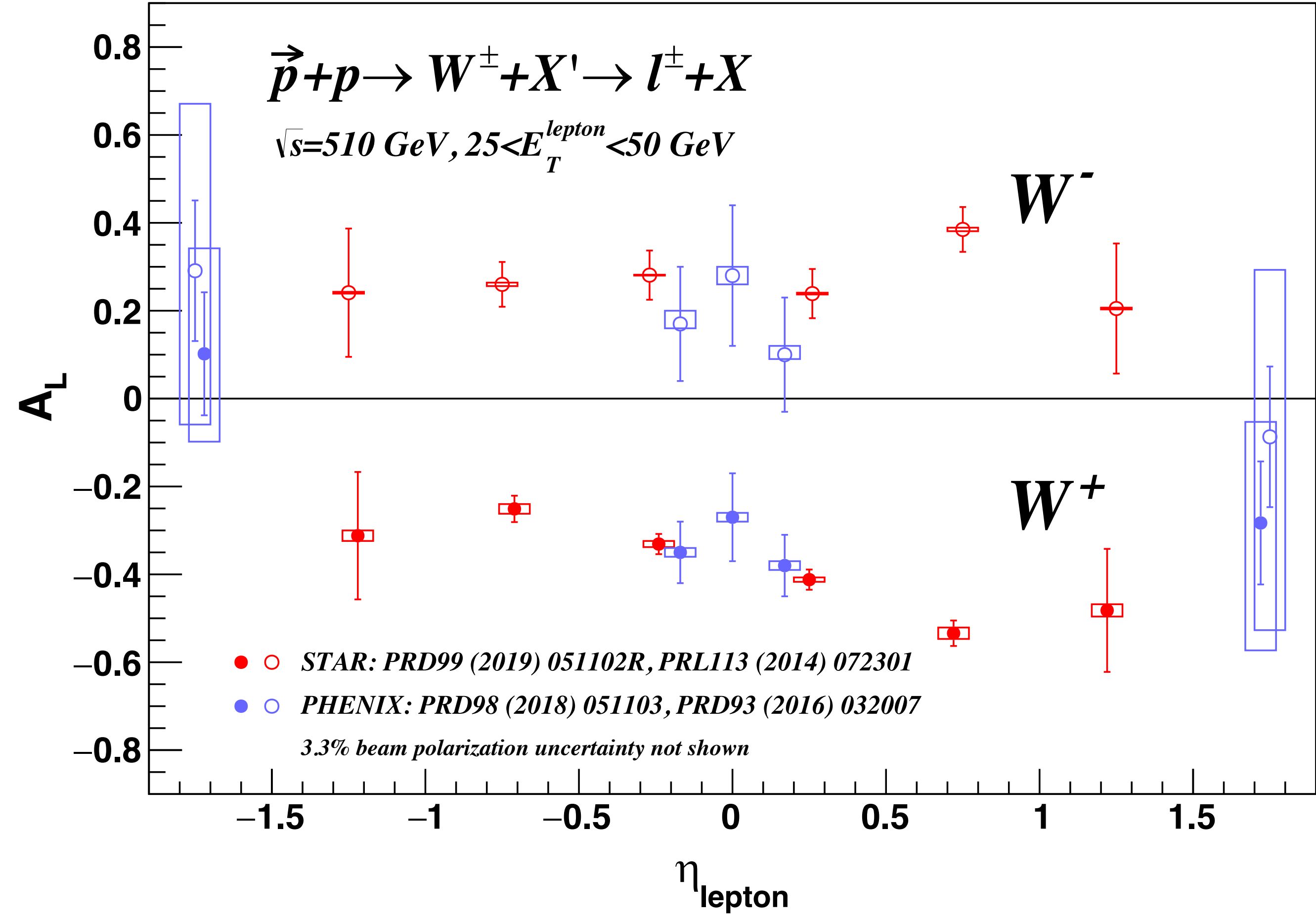
RHIC

data taking
2000 – 2026

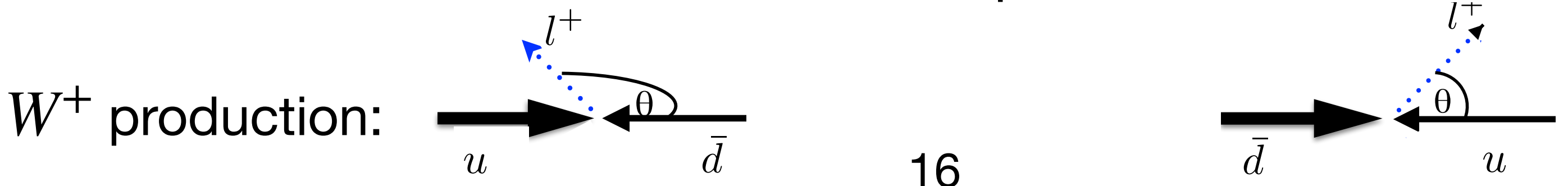
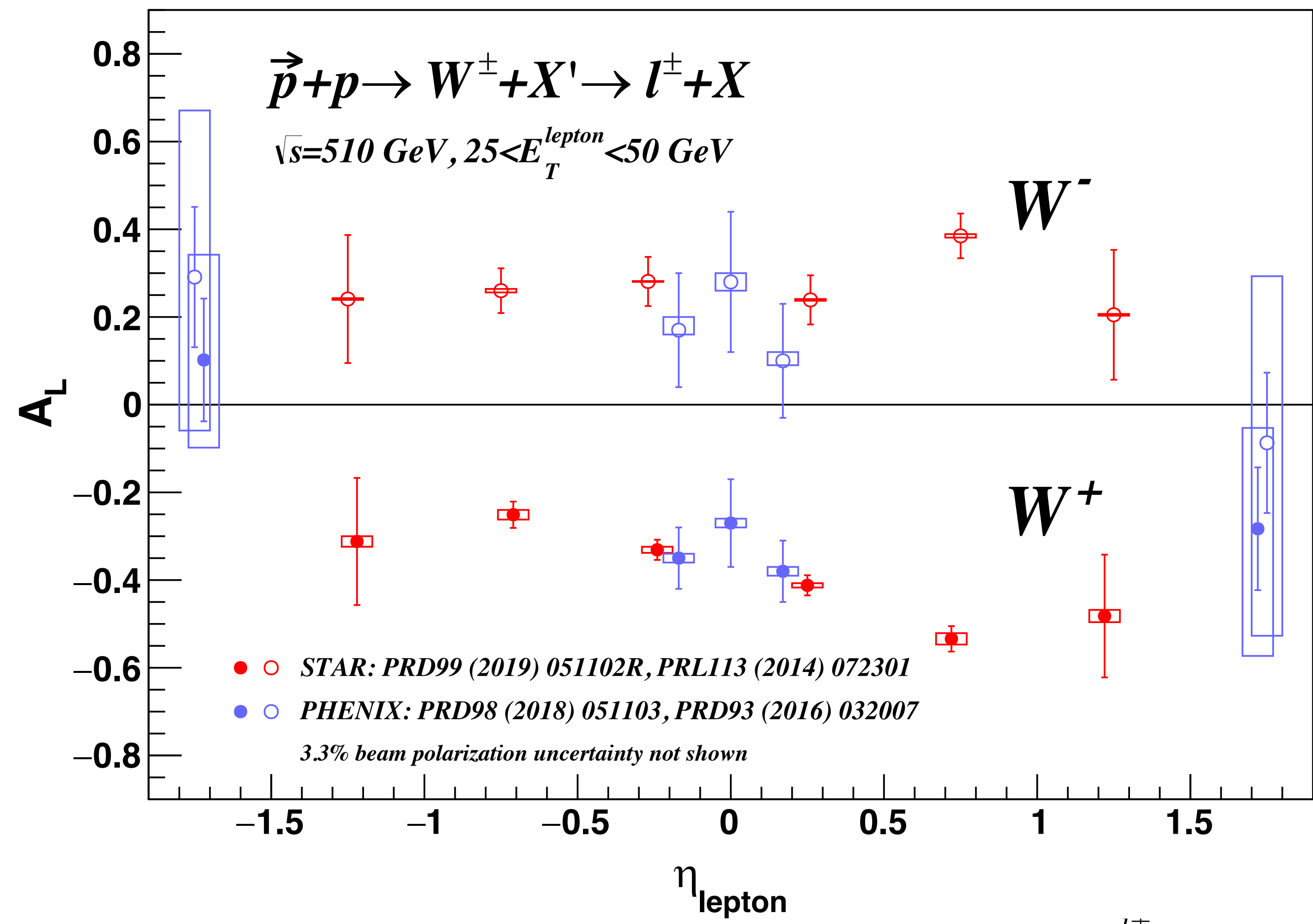


- Polarisation direction changes from bunch to bunch
- Spin rotators provide choice of spin orientation

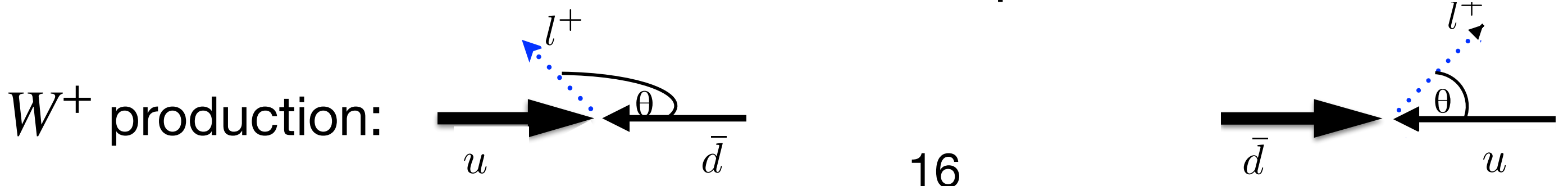
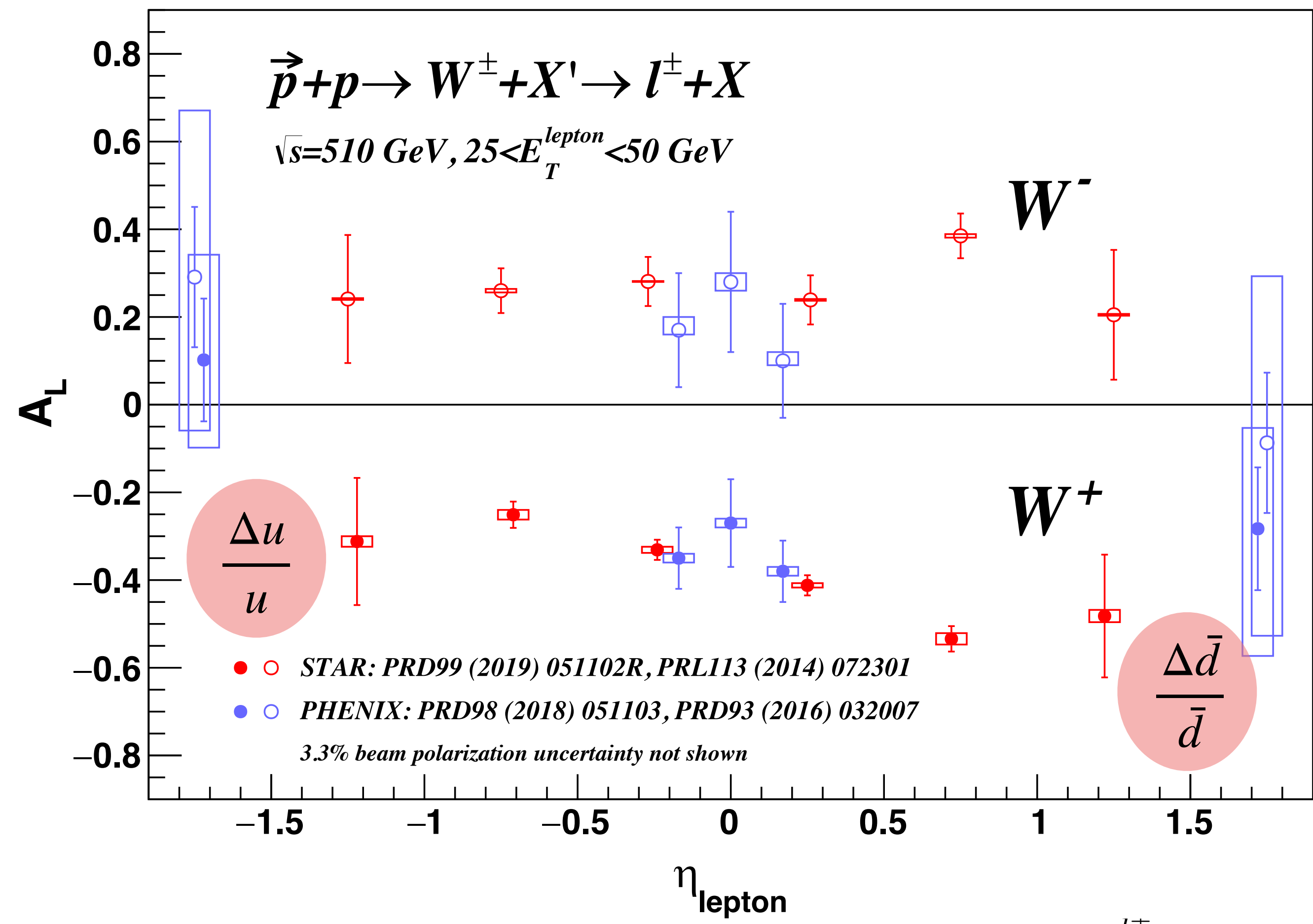
Longitudinal single-spin asymmetry in pp collisions



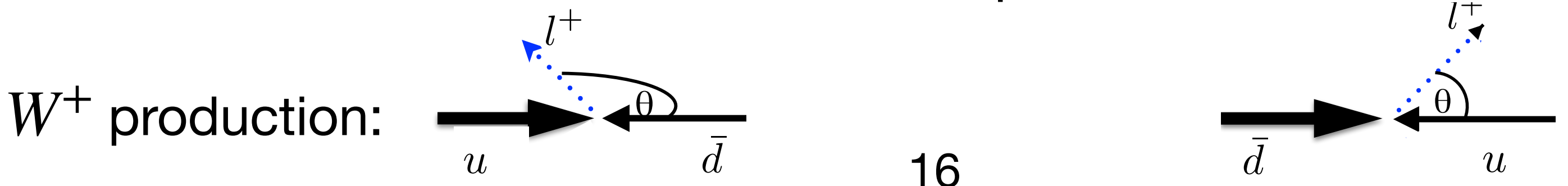
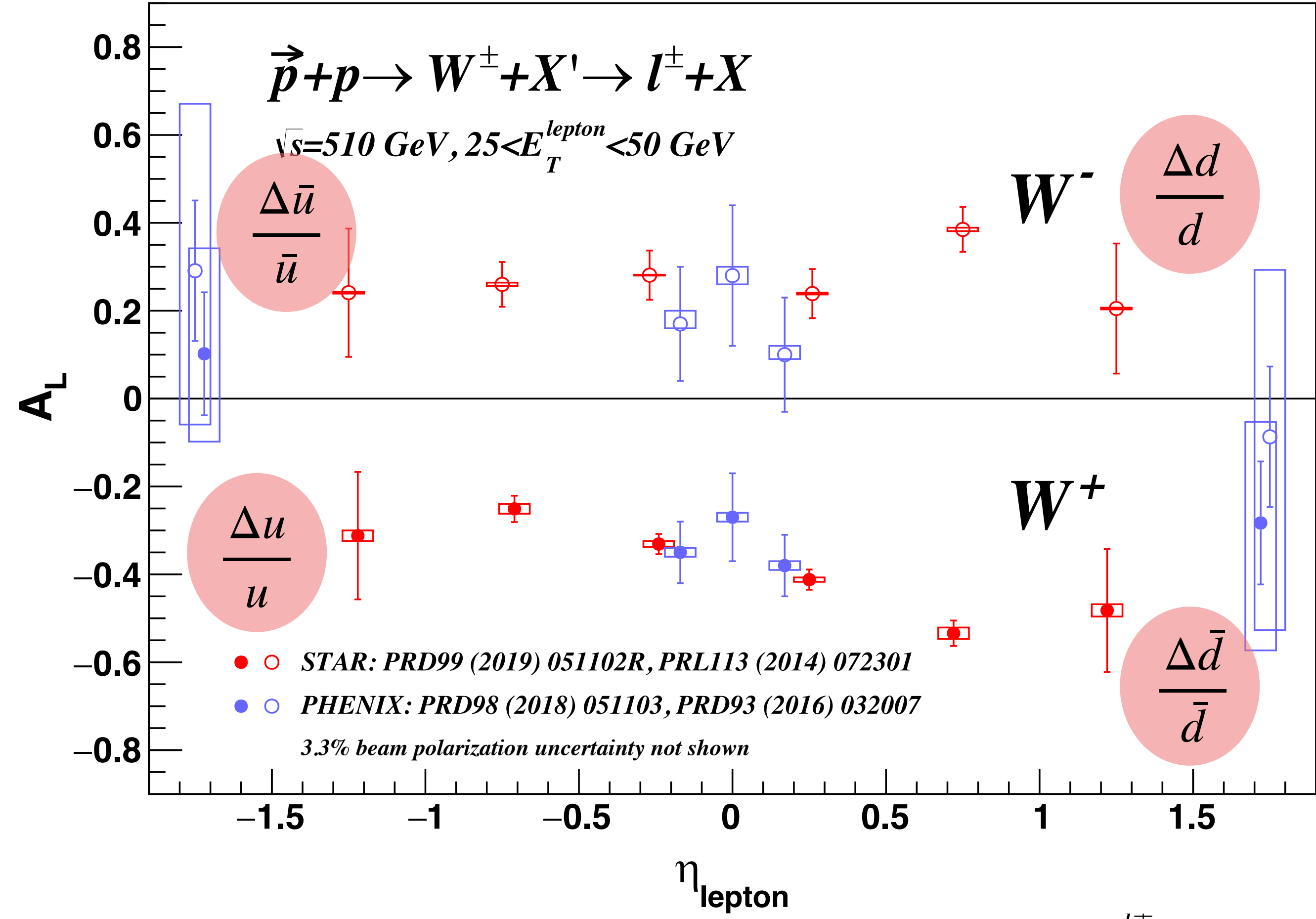
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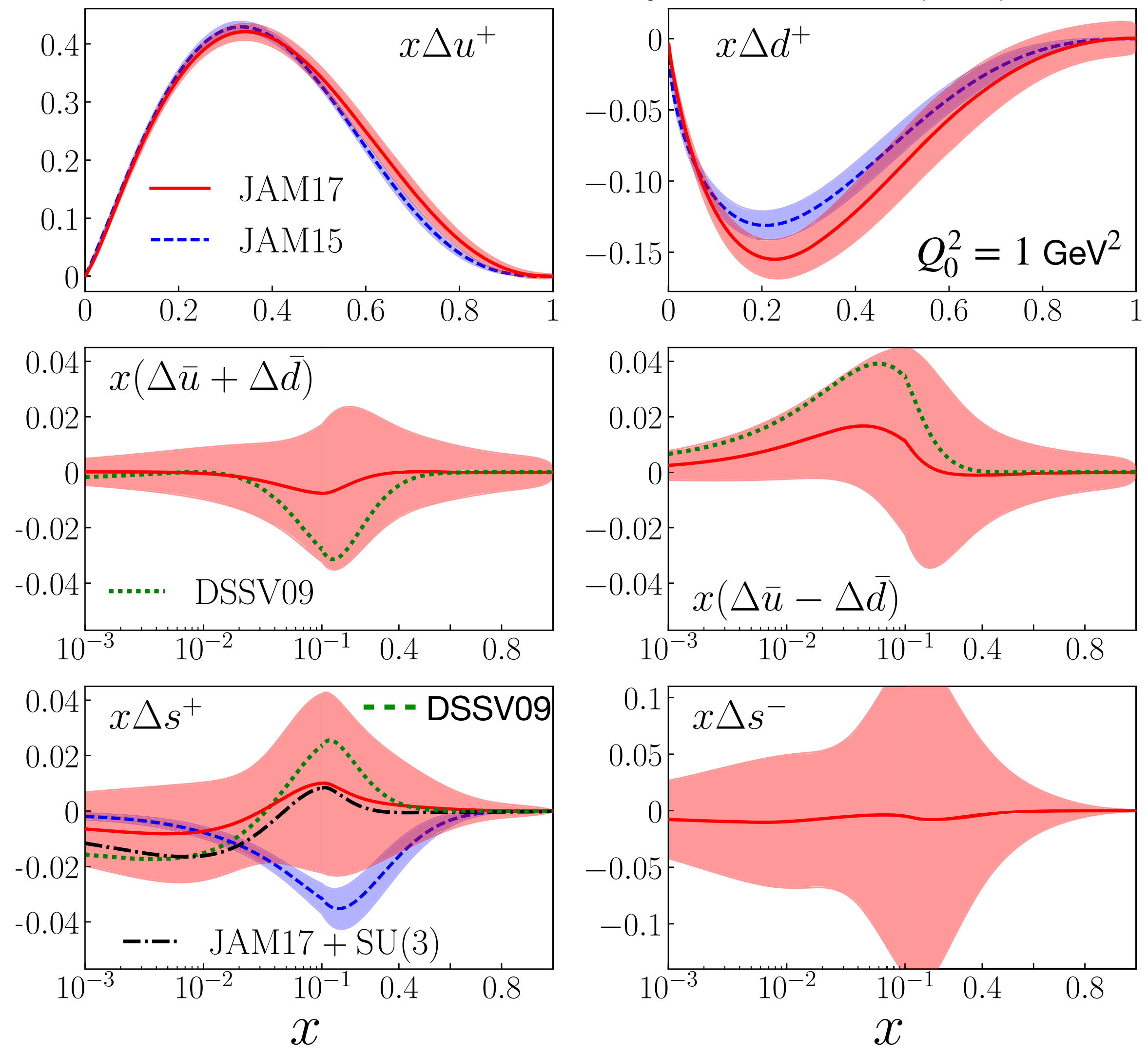
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Global fits: quark helicity PDFs

- Data:
- inclusive DIS
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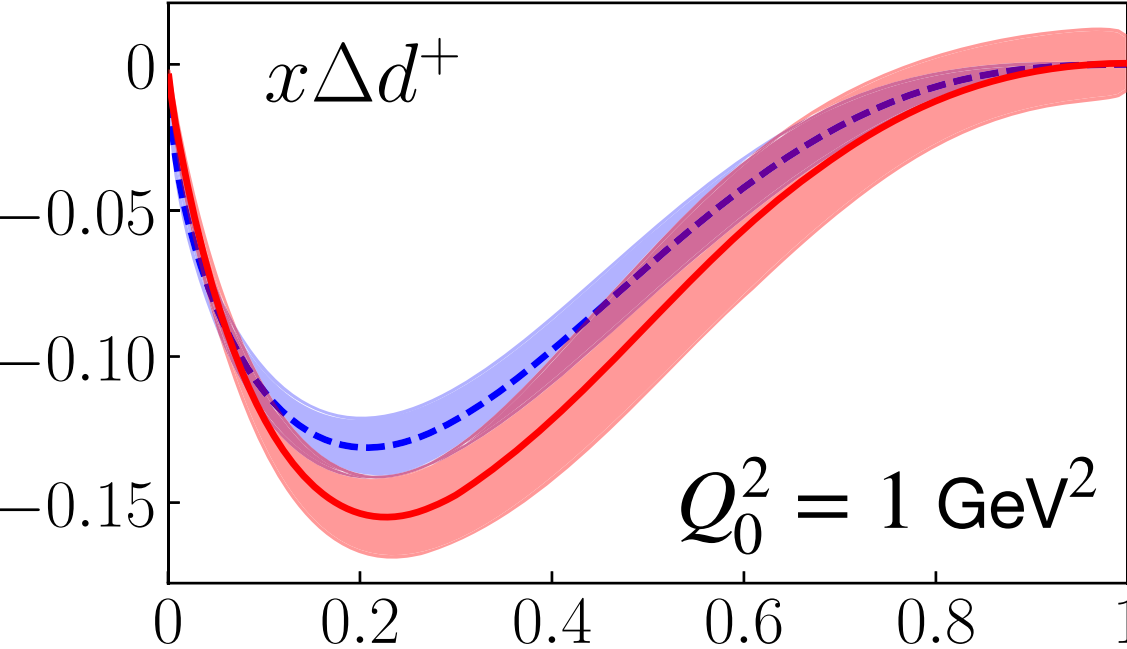
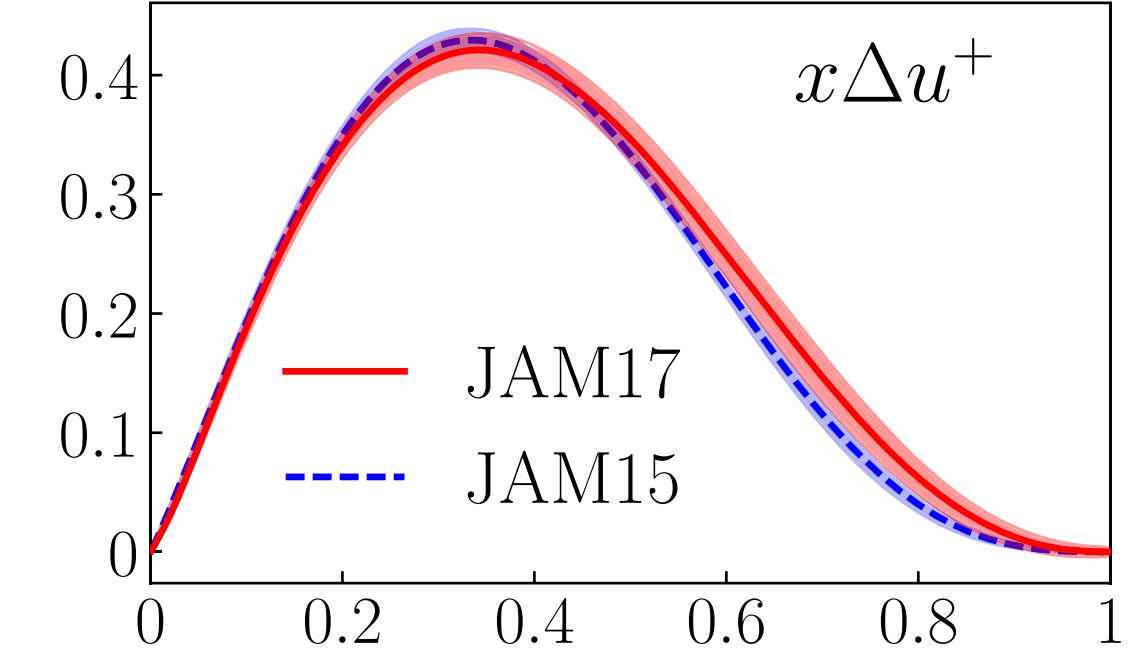
JAM Collaboration,
 Phys. Rev. Lett. **119** (2017) 132001



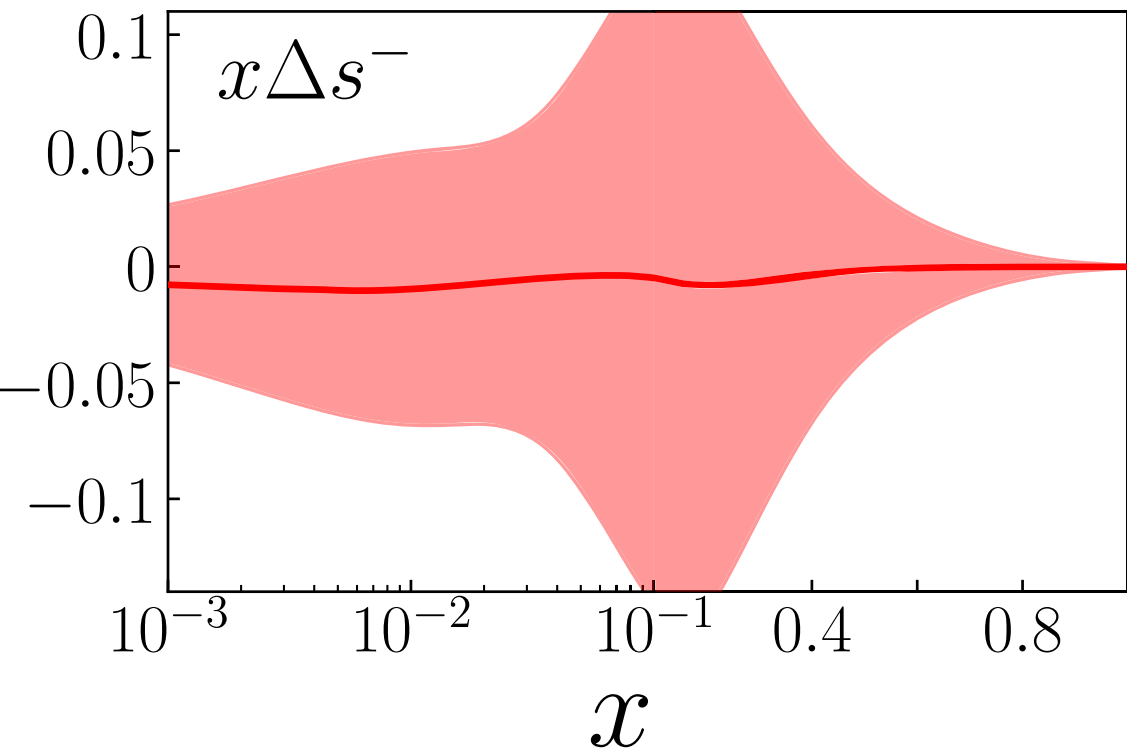
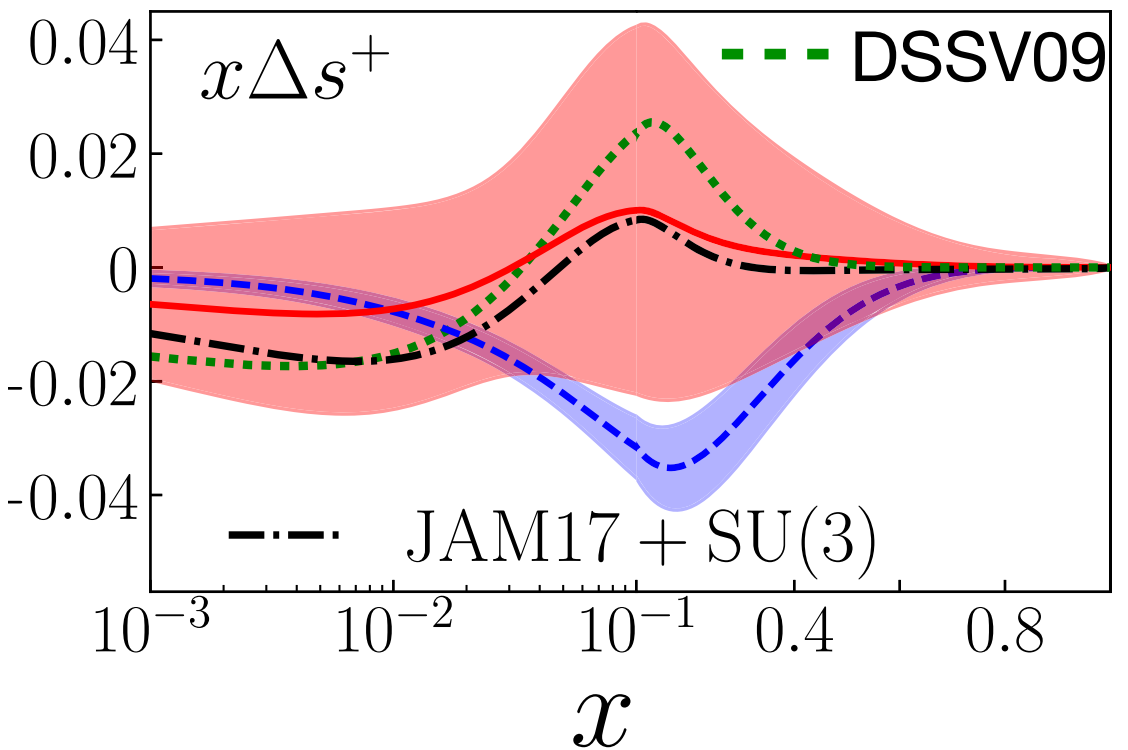
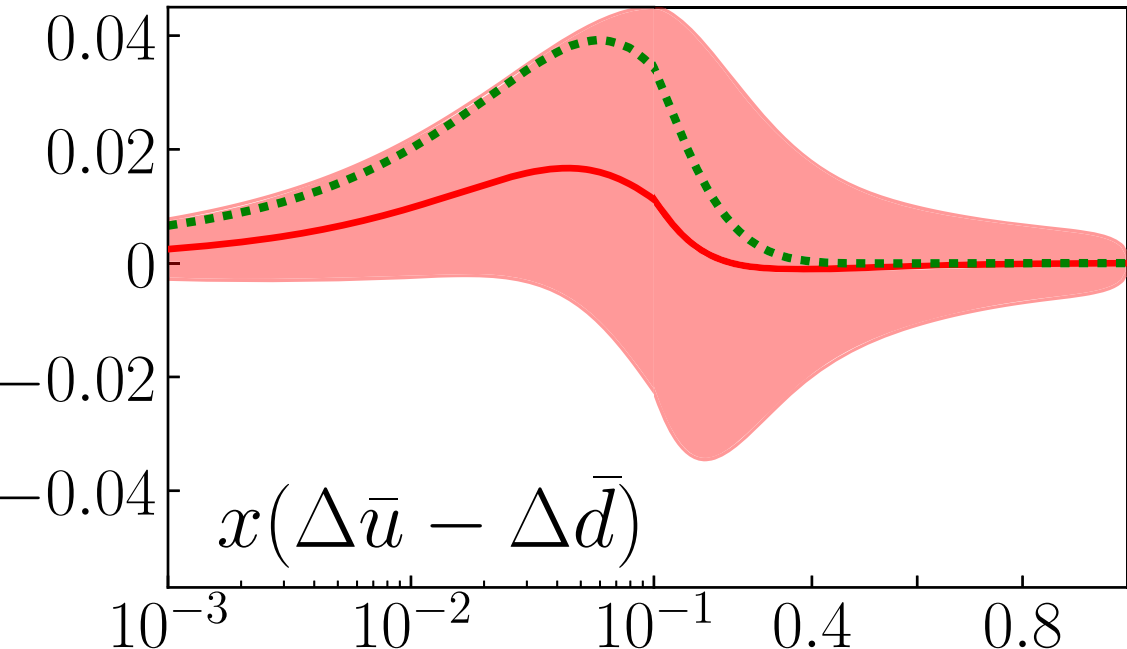
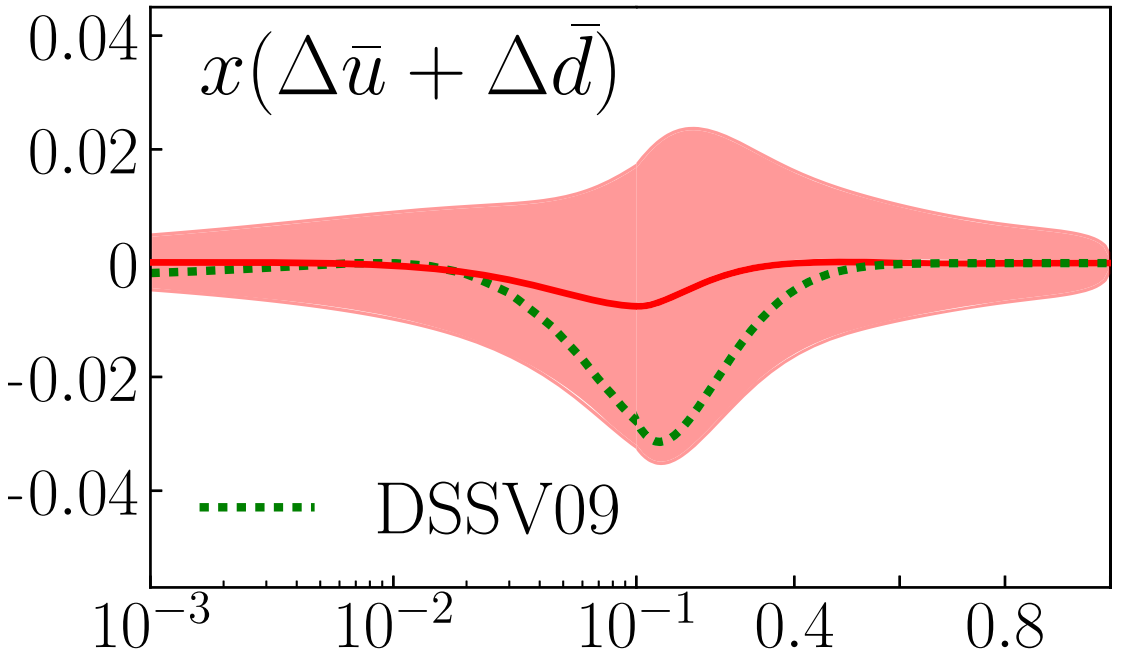
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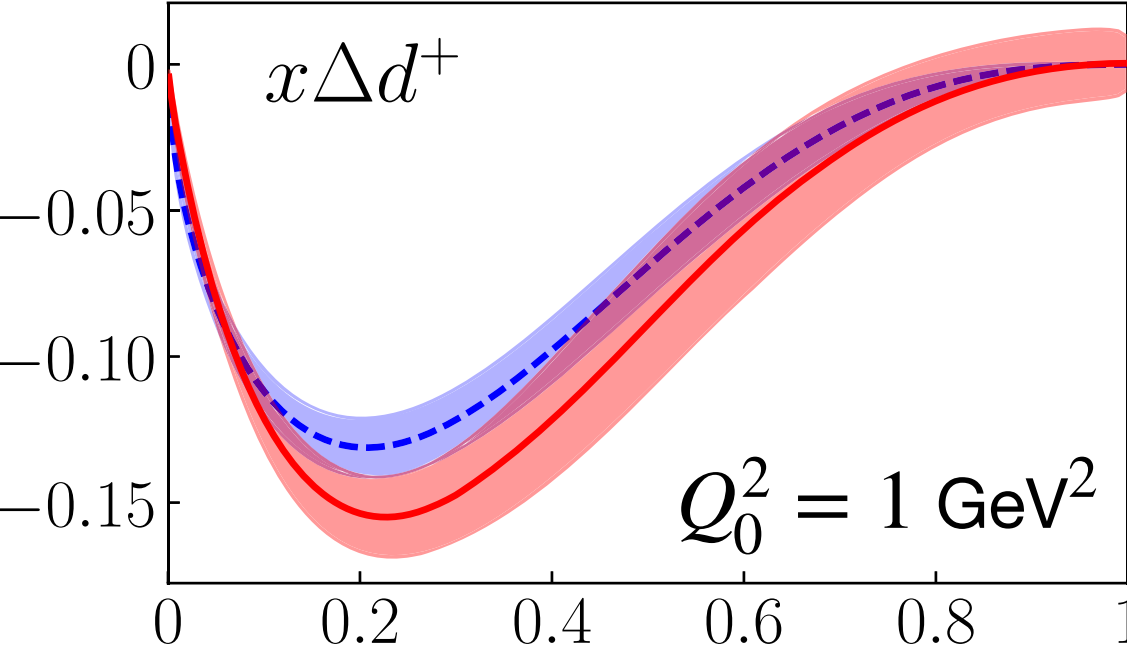
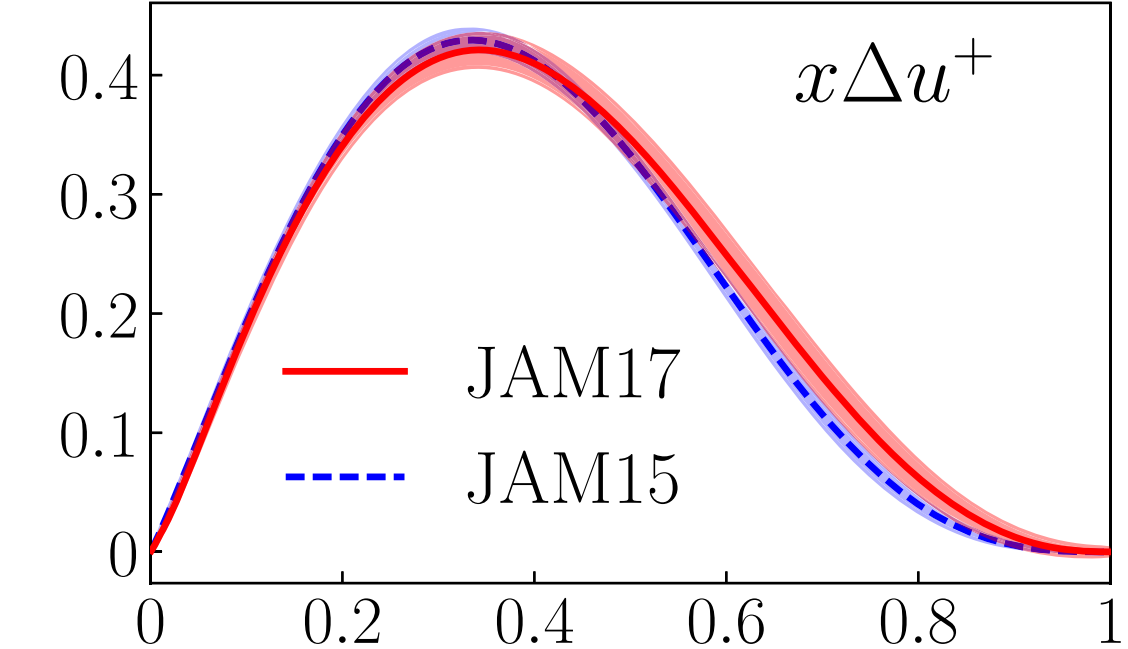
$\Delta q^+ = \Delta q + \Delta \bar{q}$:
 largely determined by inclusive DIS data



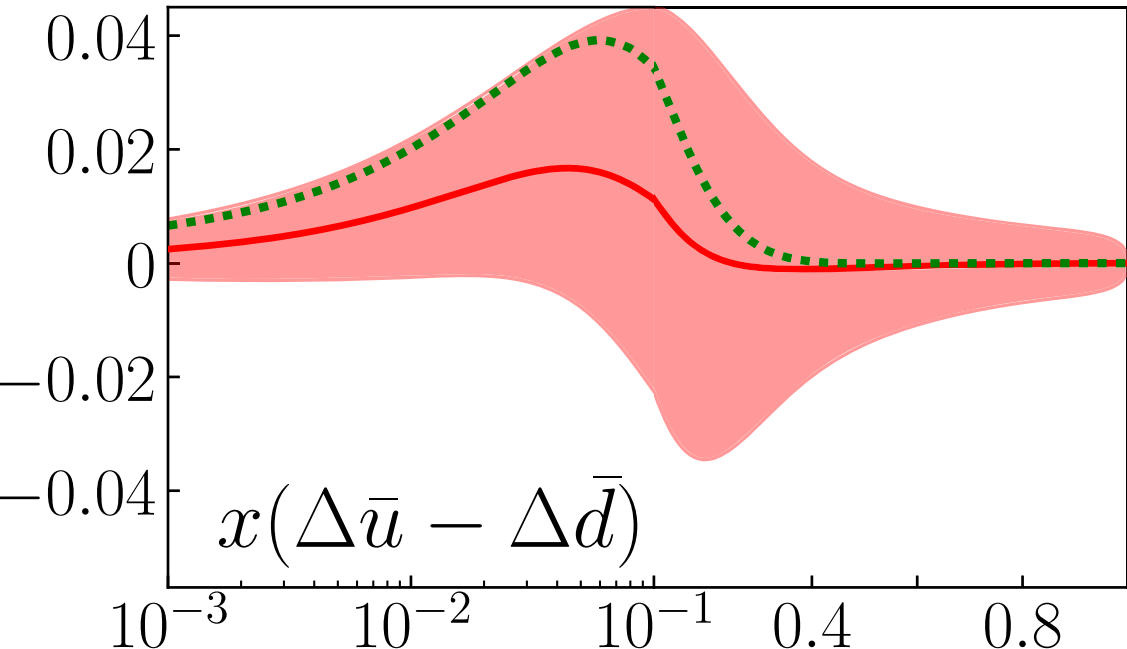
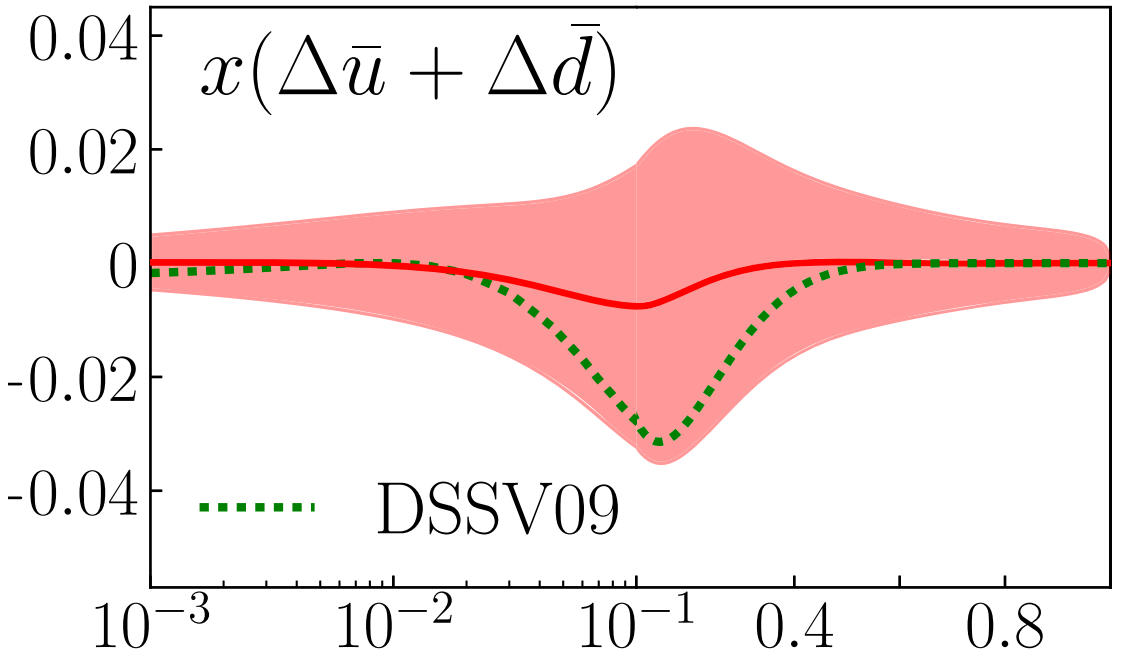
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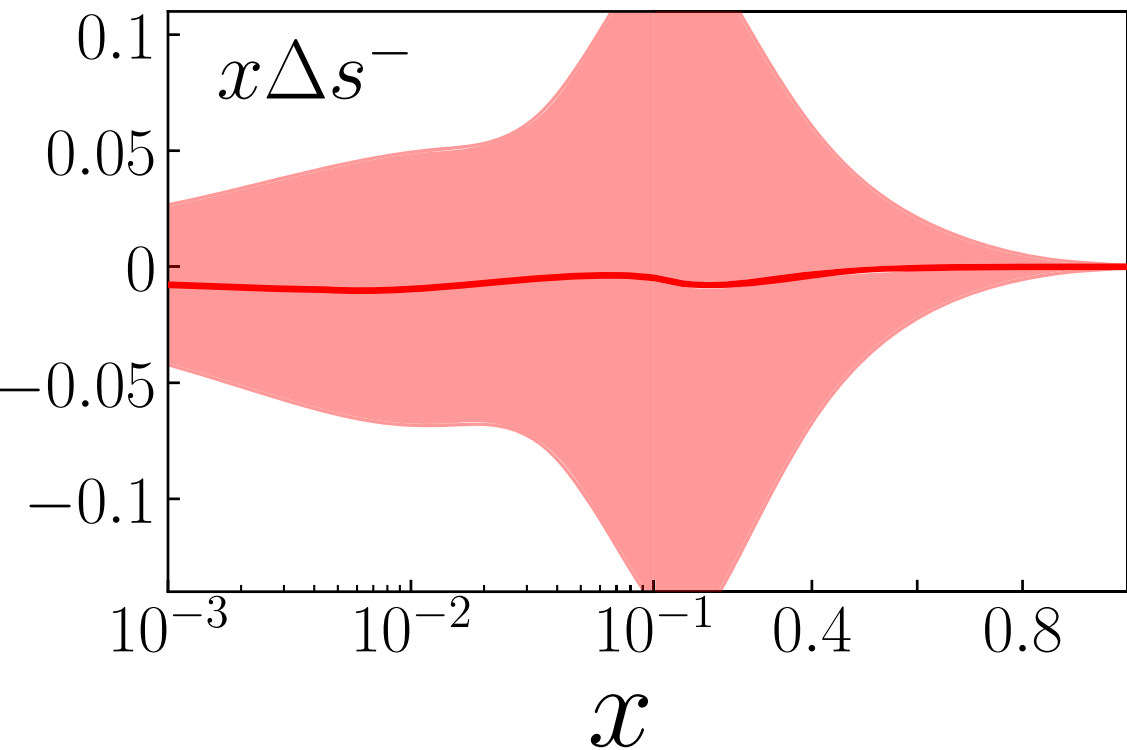
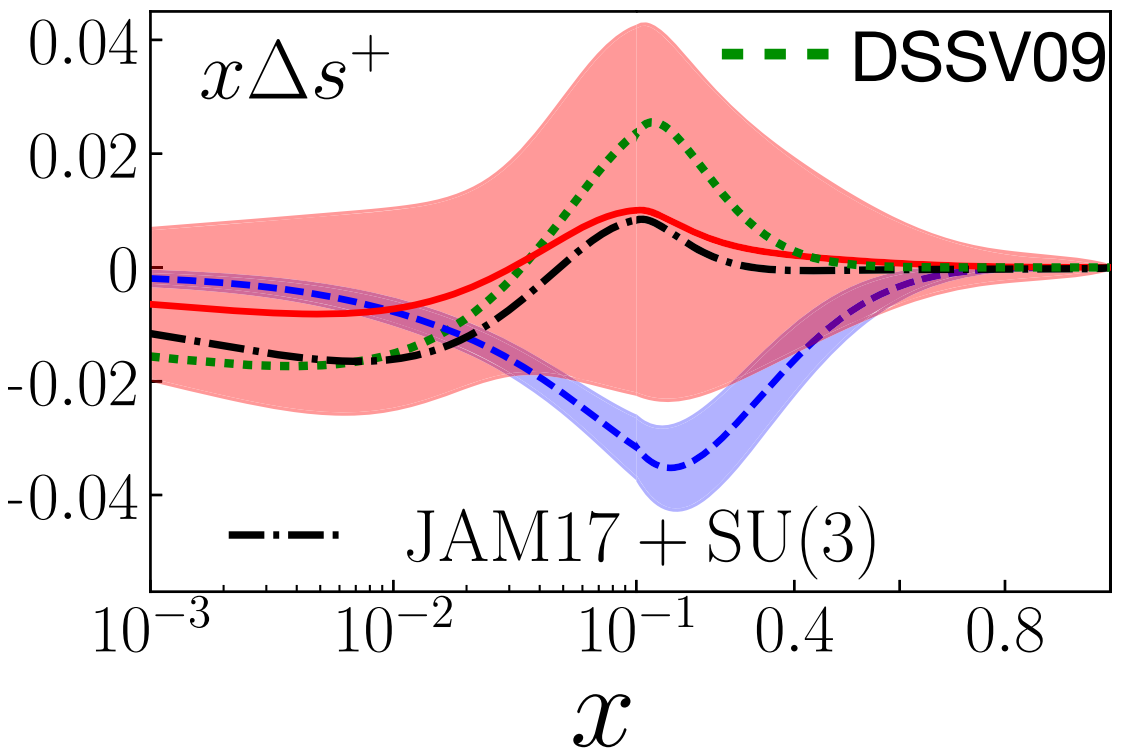
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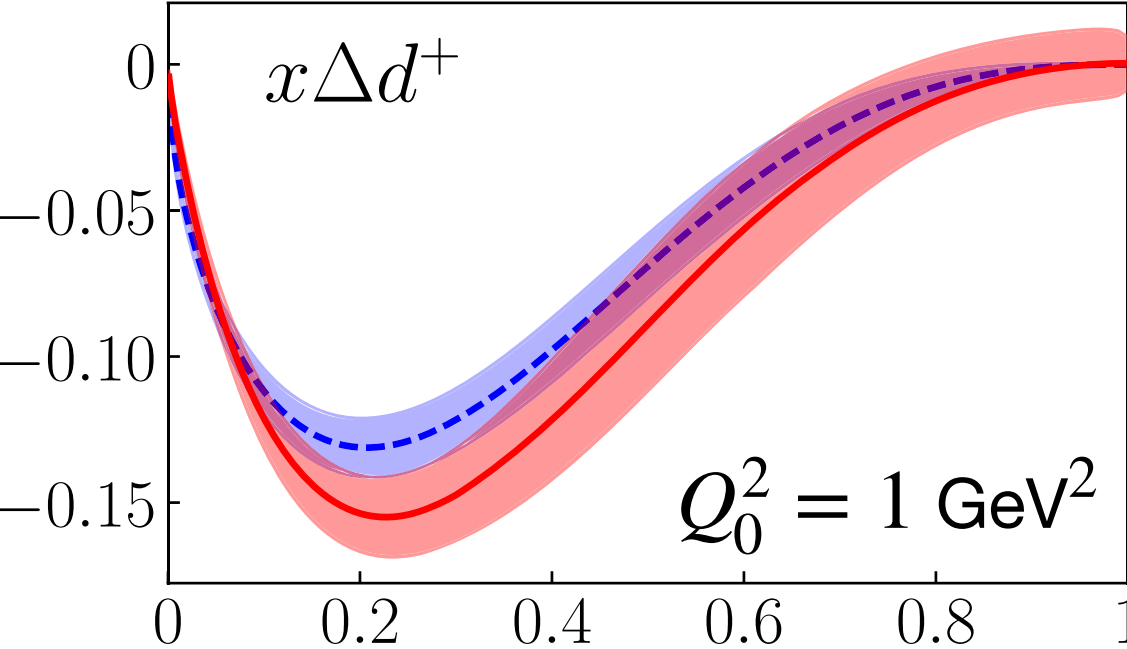
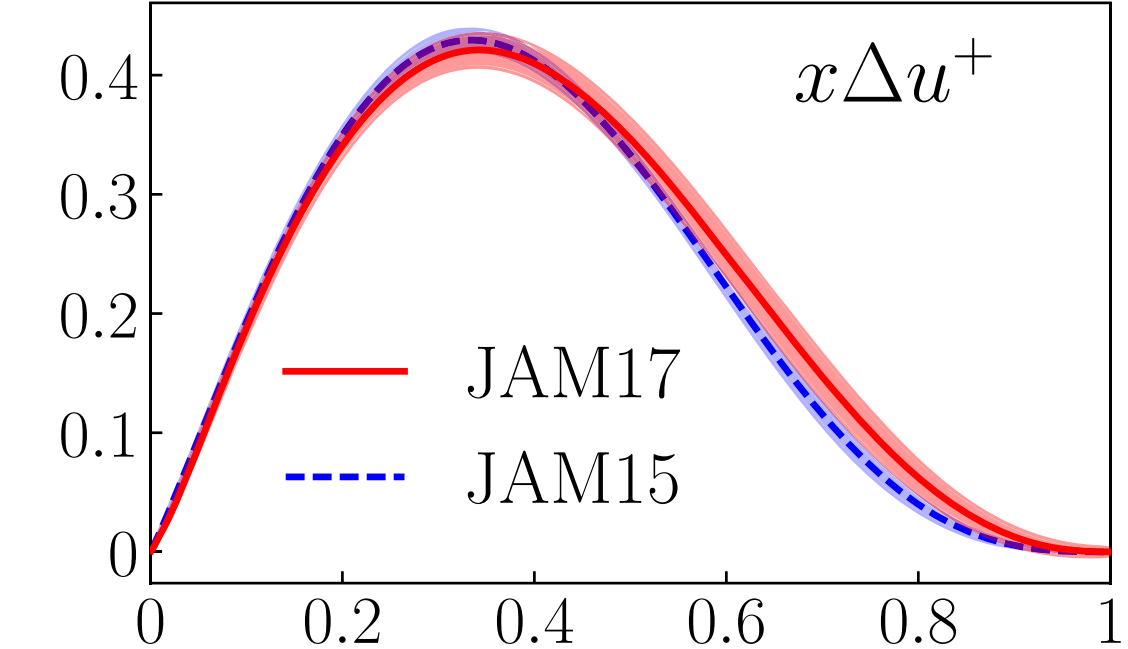
SIDIS: distinguish between q and \bar{q}
 $\Delta \bar{u} - \Delta \bar{d}$ slightly positive



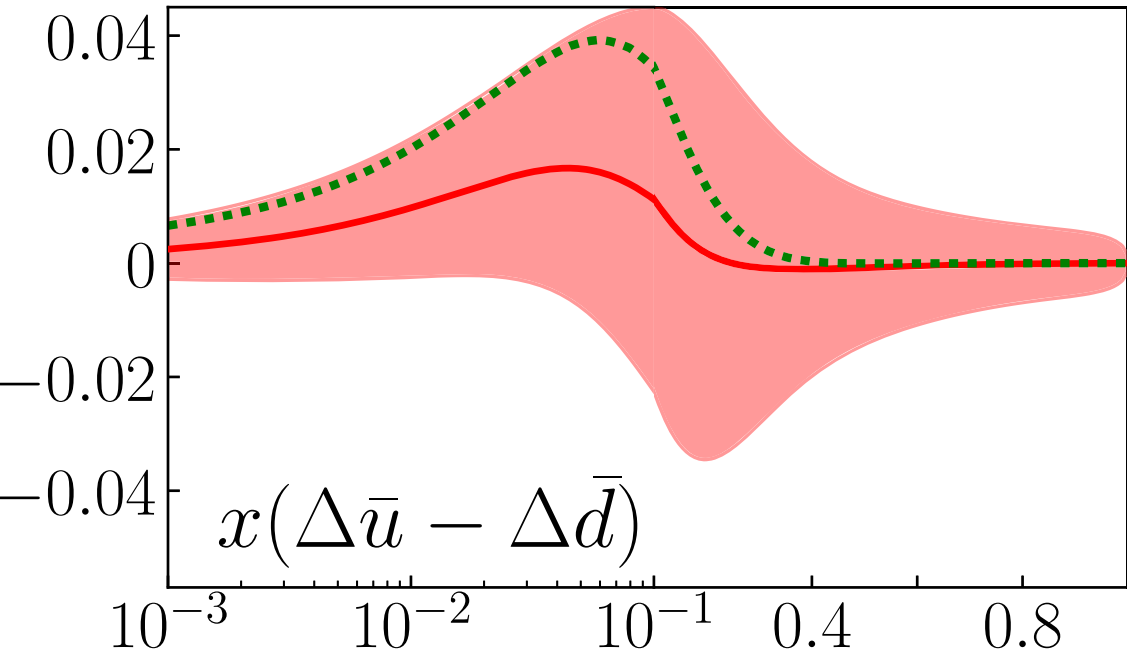
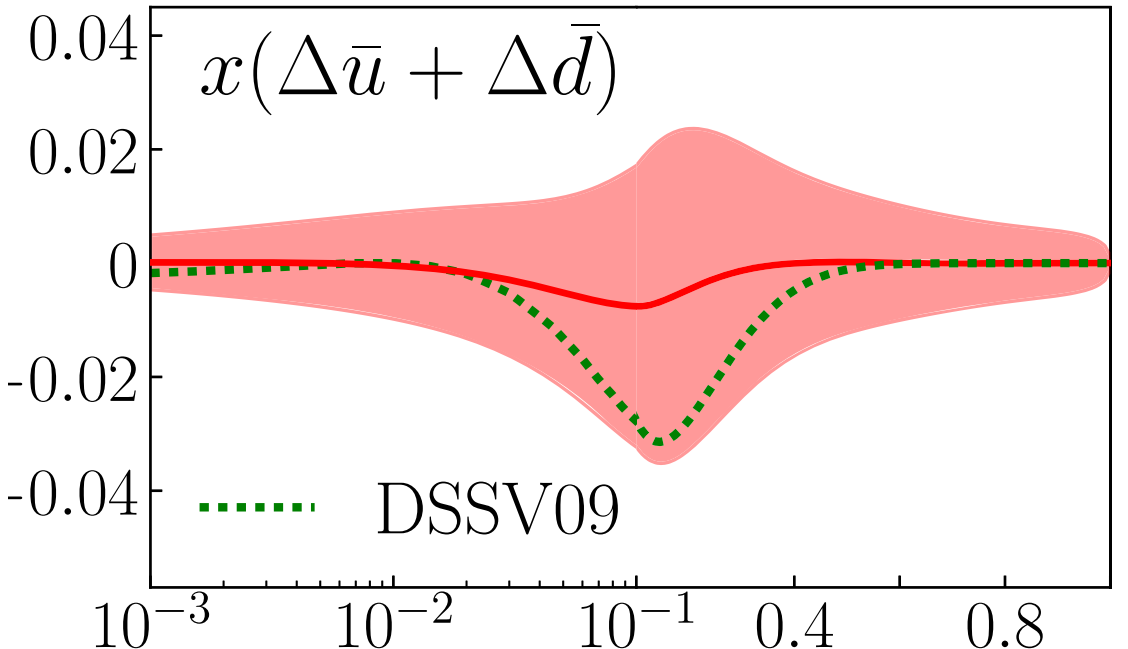
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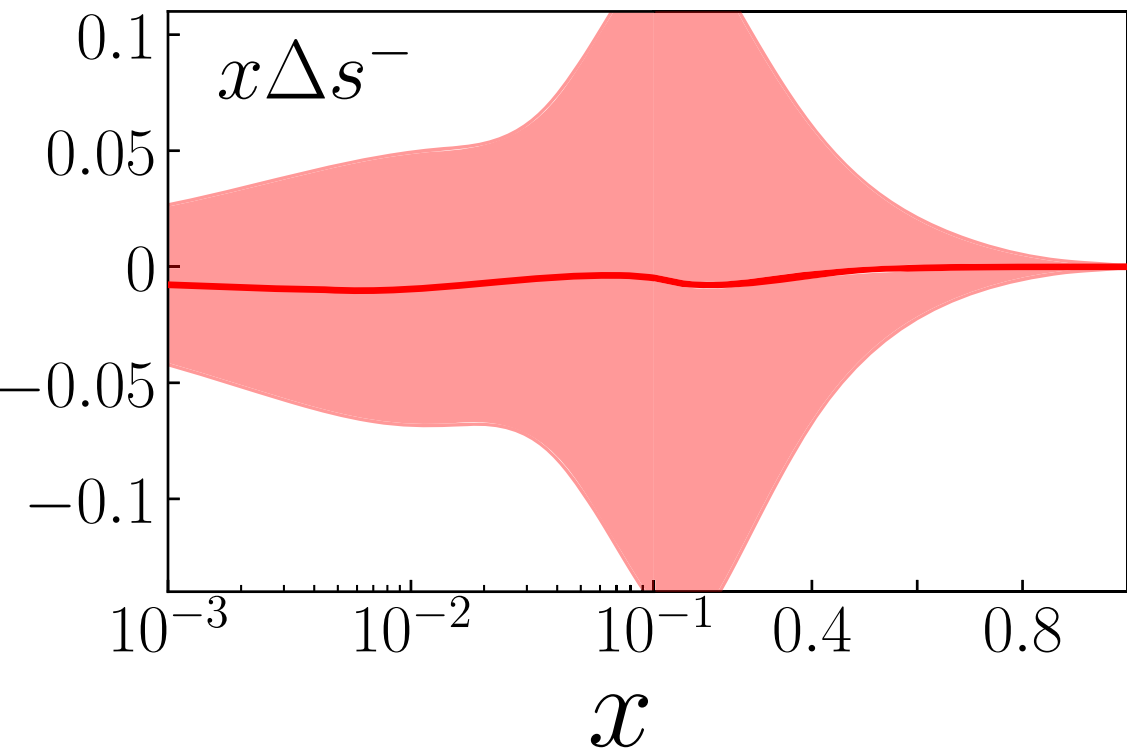
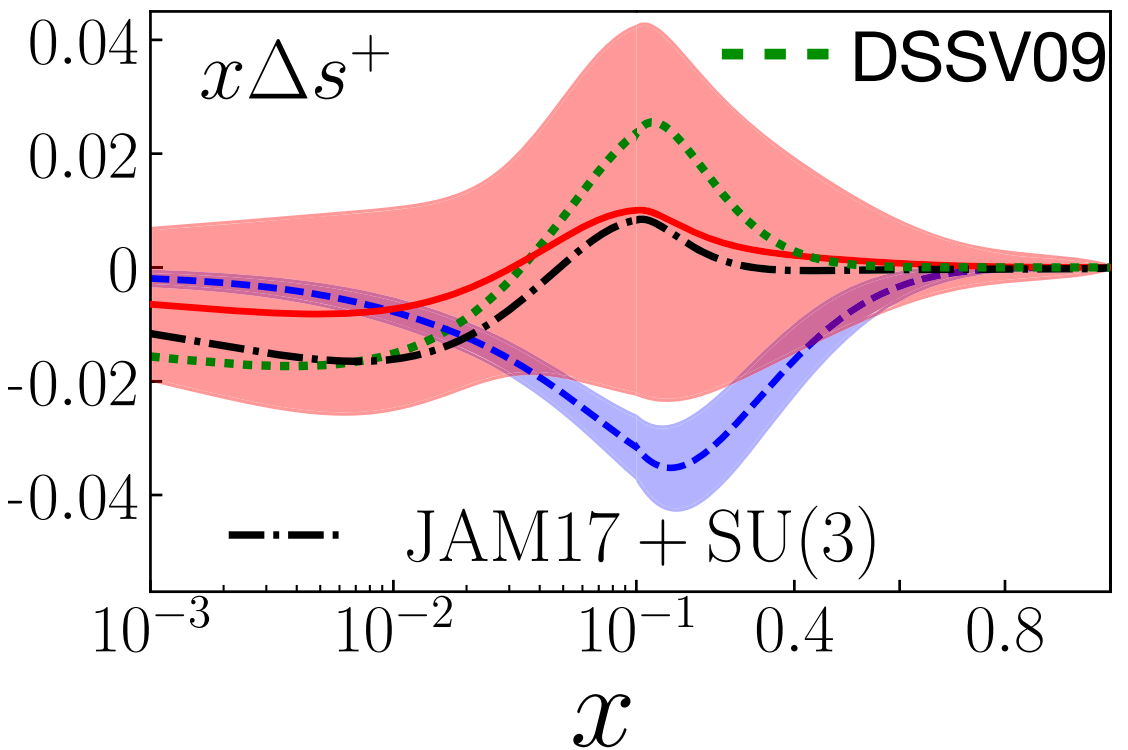
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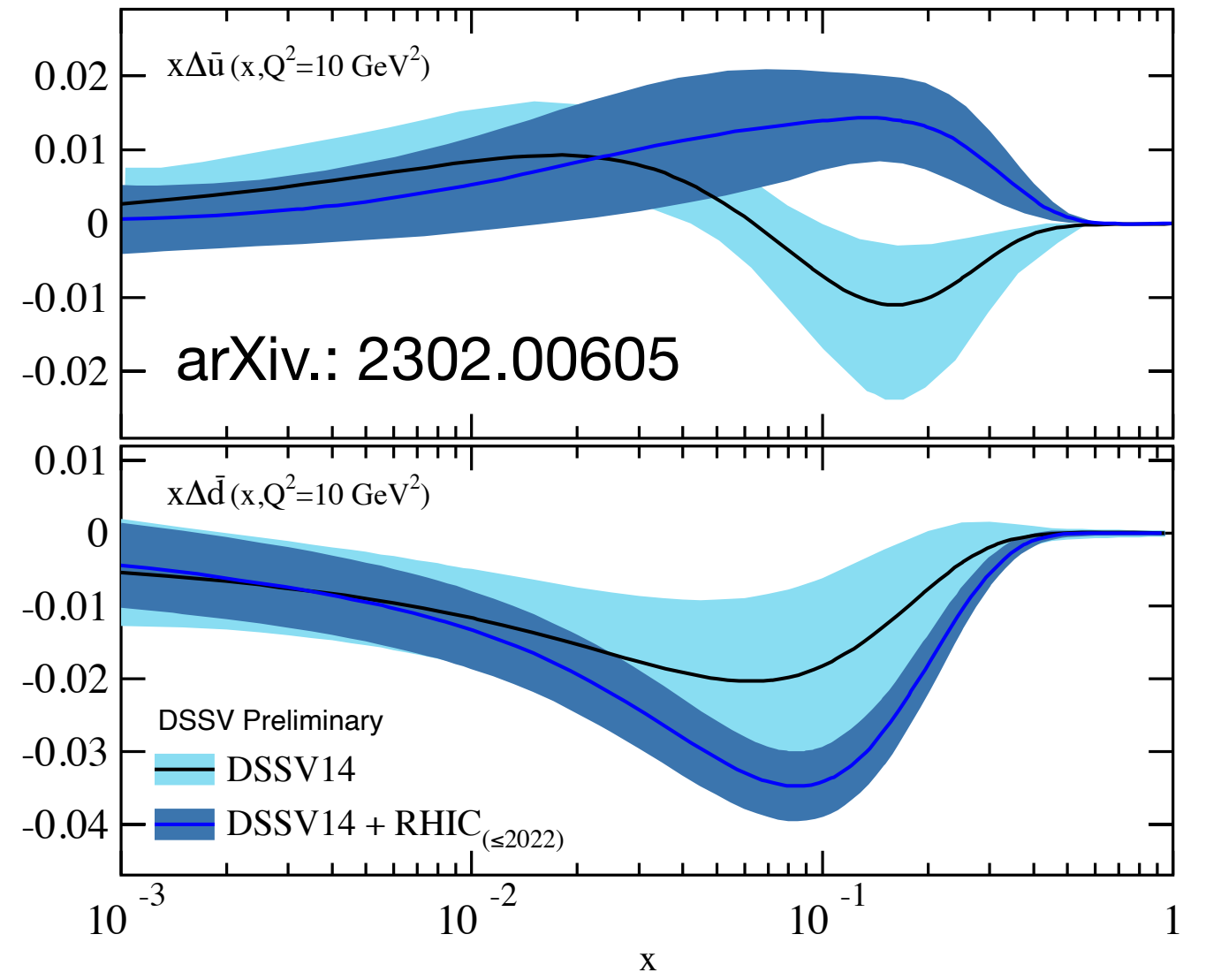
$\Delta q^+ = \Delta q + \Delta \bar{q}$:
largely determined by inclusive DIS data



SIDIS: distinguish between q and \bar{q}
 $\Delta \bar{u} - \Delta \bar{d}$ slightly positive



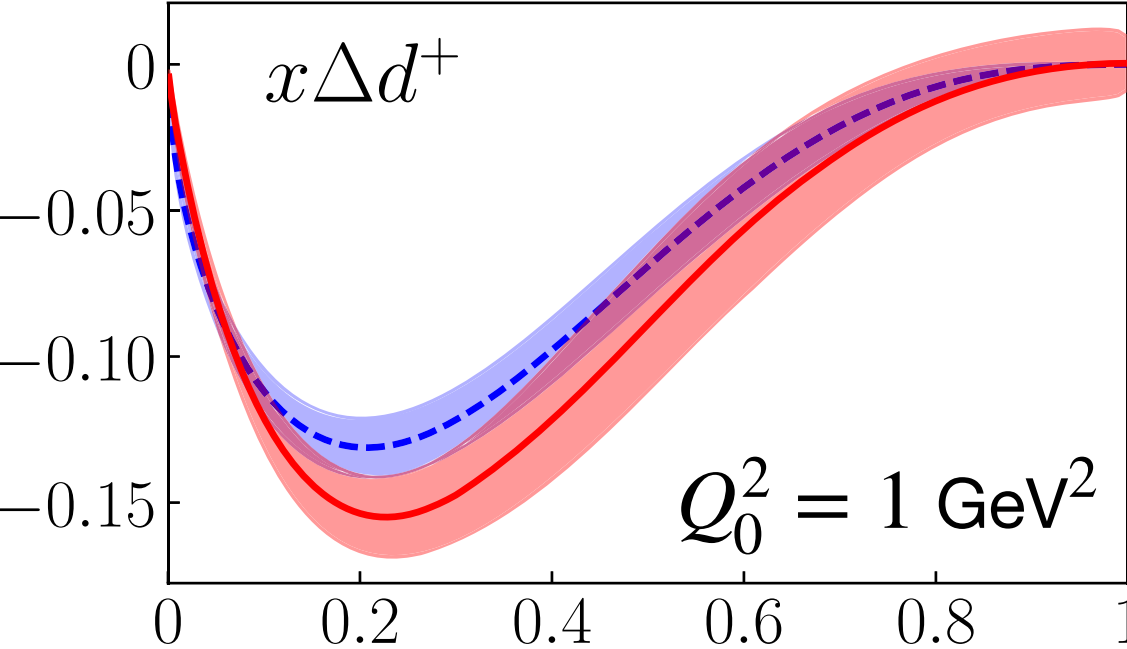
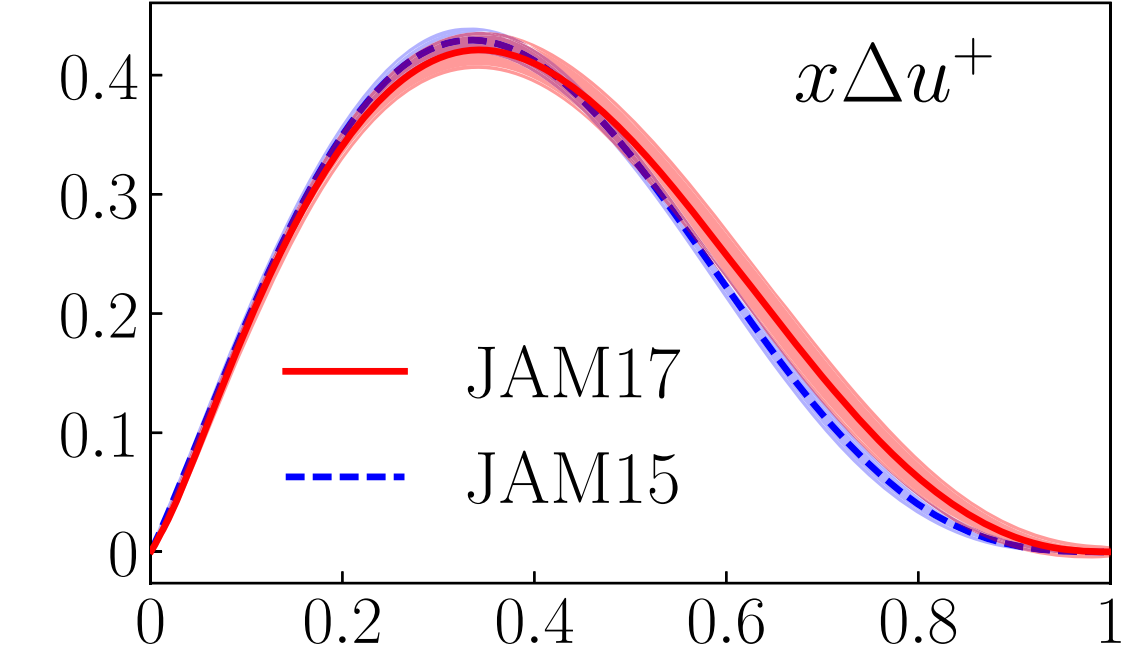
DSSV+RHIC $W A_L$ data: $\Delta \bar{u} > \Delta \bar{d}$



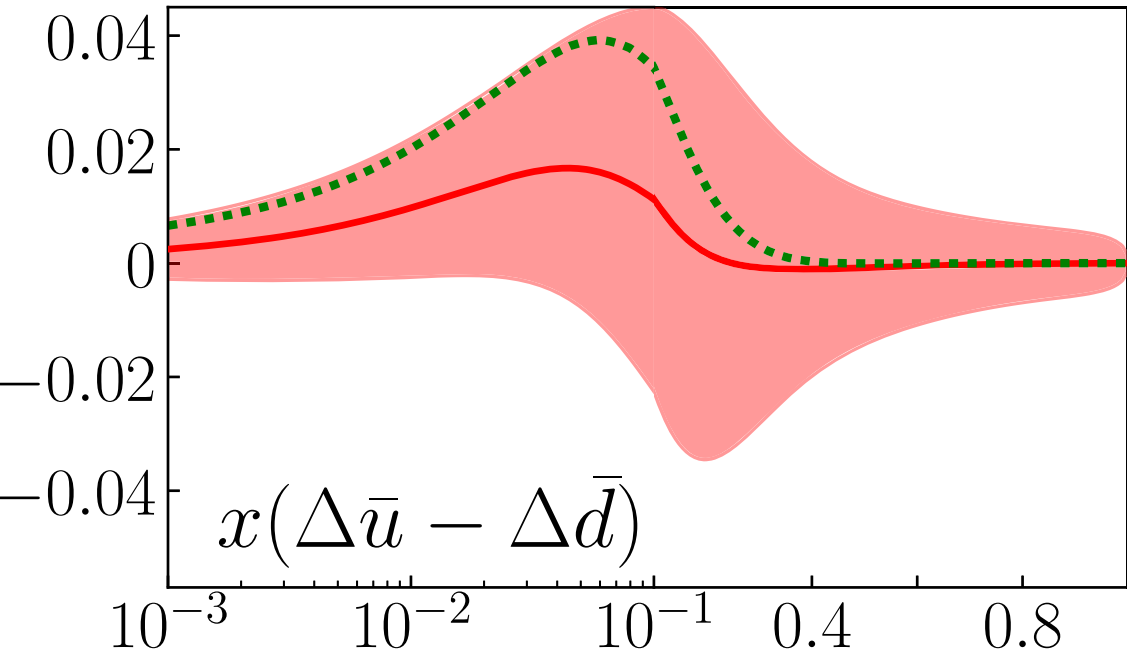
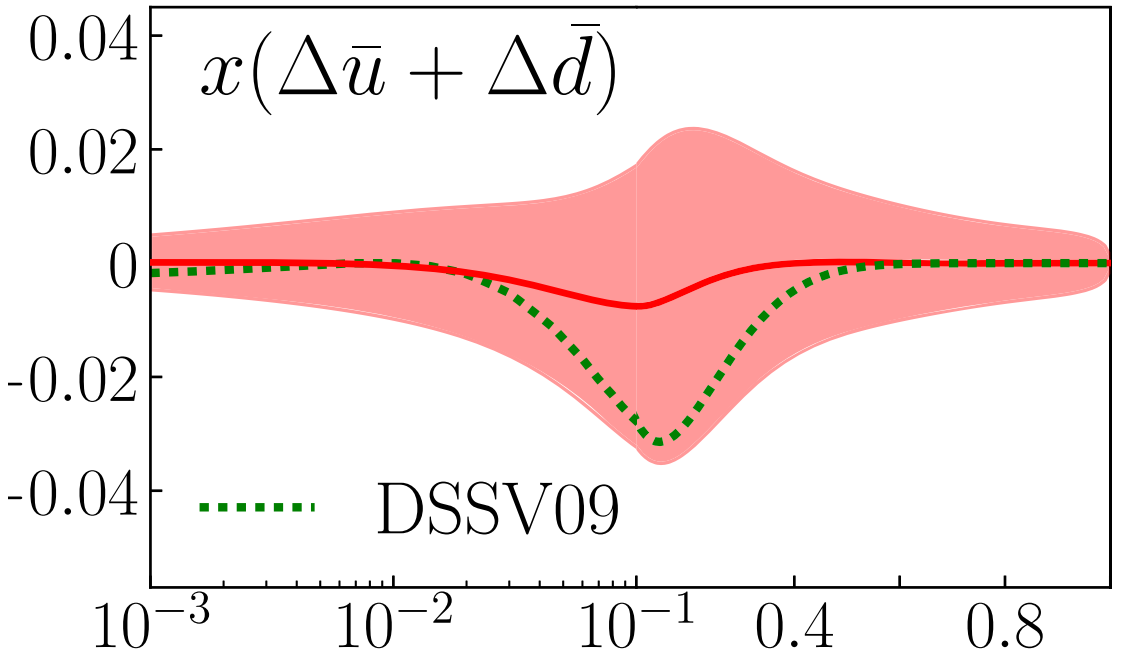
Global fits: quark helicity PDFs

- Data:
- inclusive DIS
 - SIDIS
 - e^+e^- annihilation

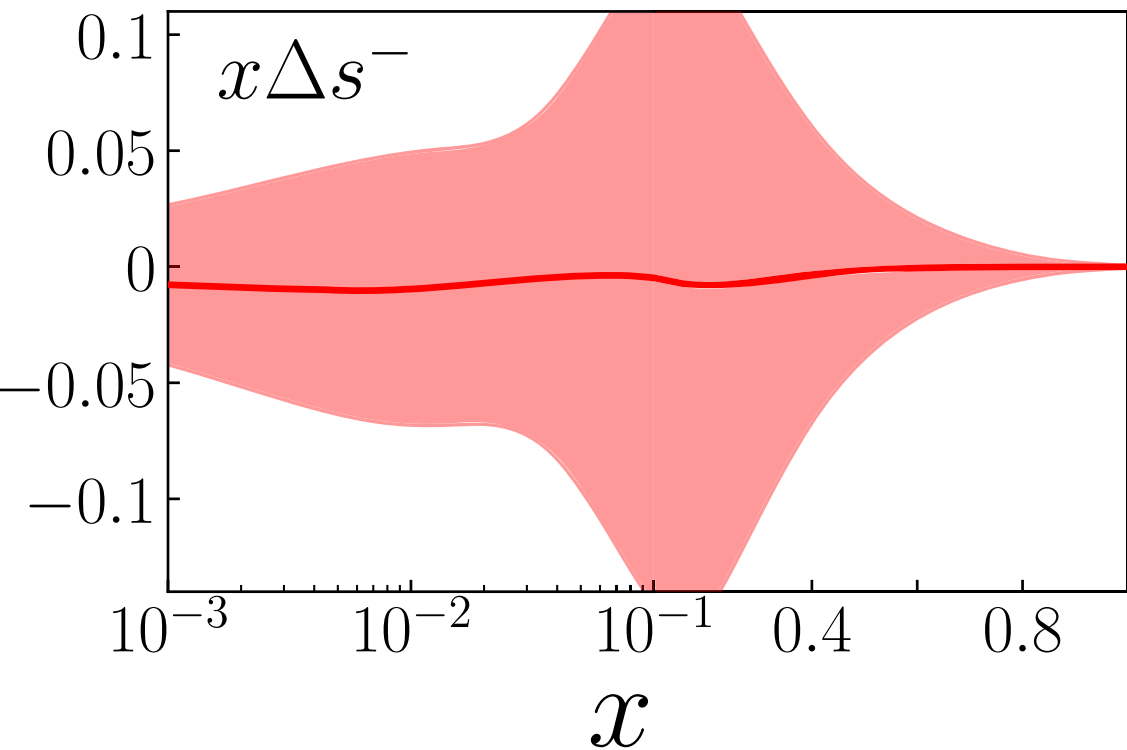
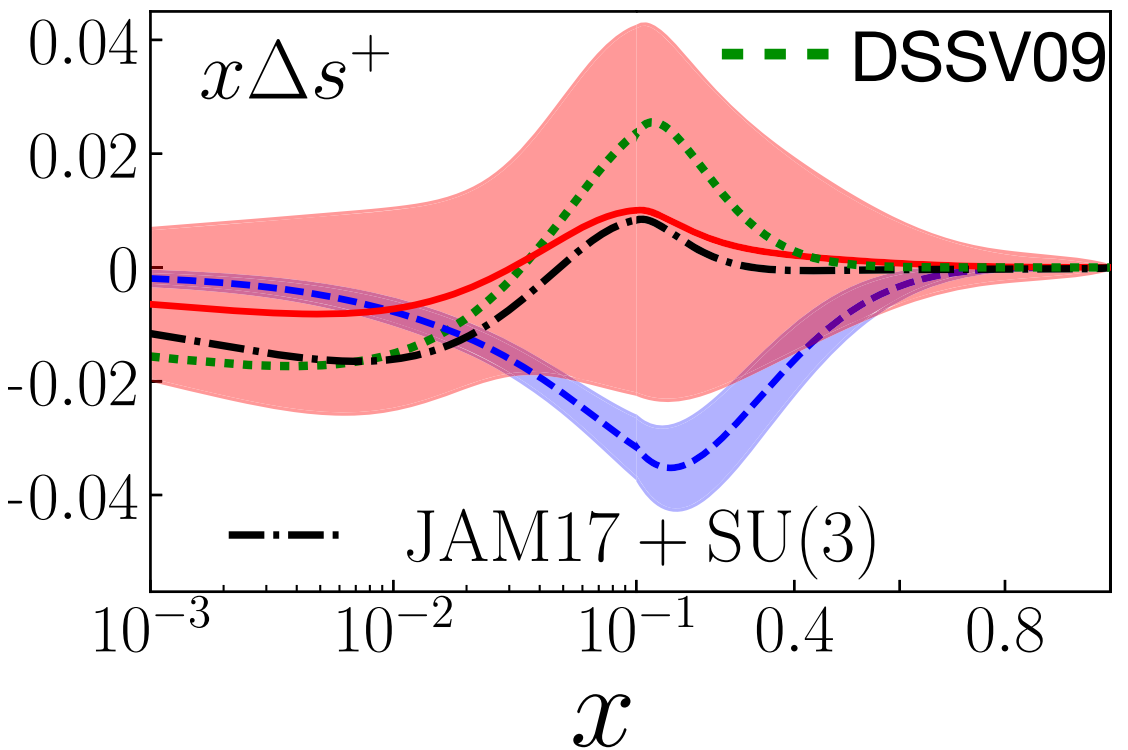
JAM Collaboration,
Phys. Rev. Lett. **119** (2017) 132001



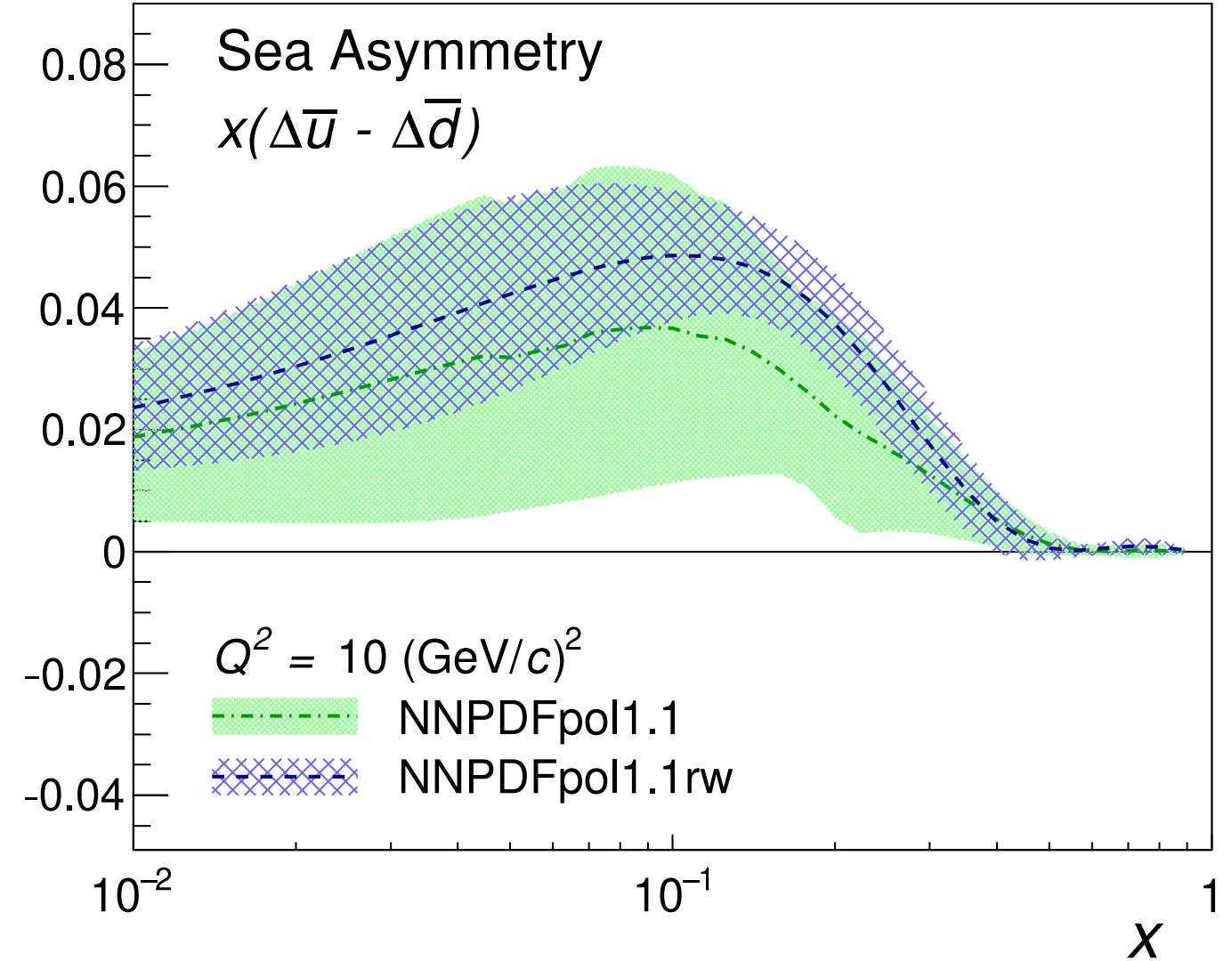
$\Delta q^+ = \Delta q + \Delta \bar{q}$:
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STAR, Phys. Rev. D **99** (2019) 051102

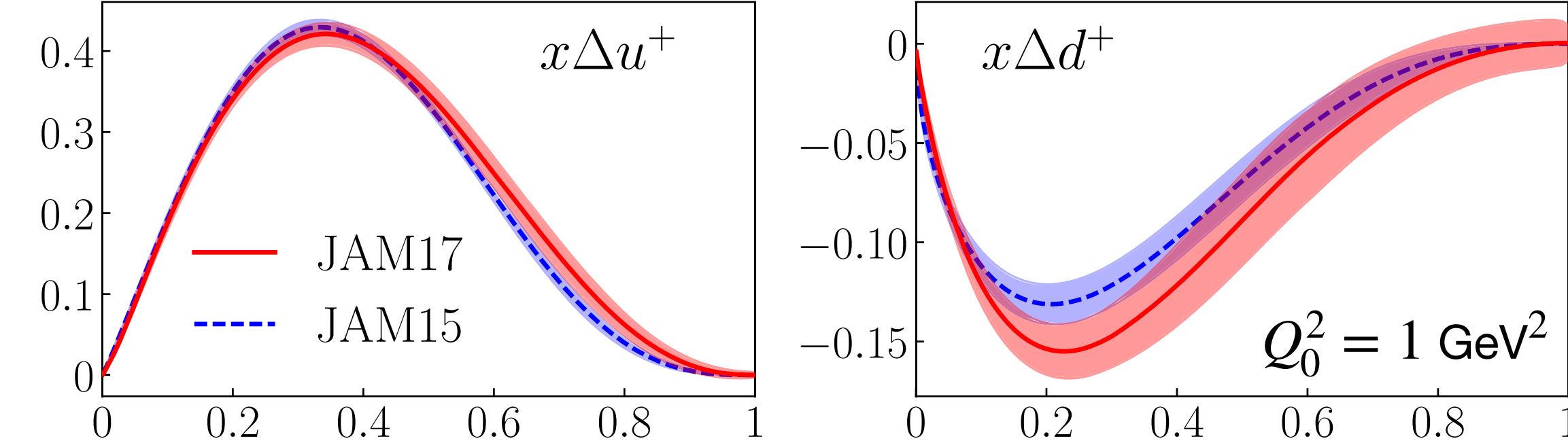


Global fits: quark helicity PDFs

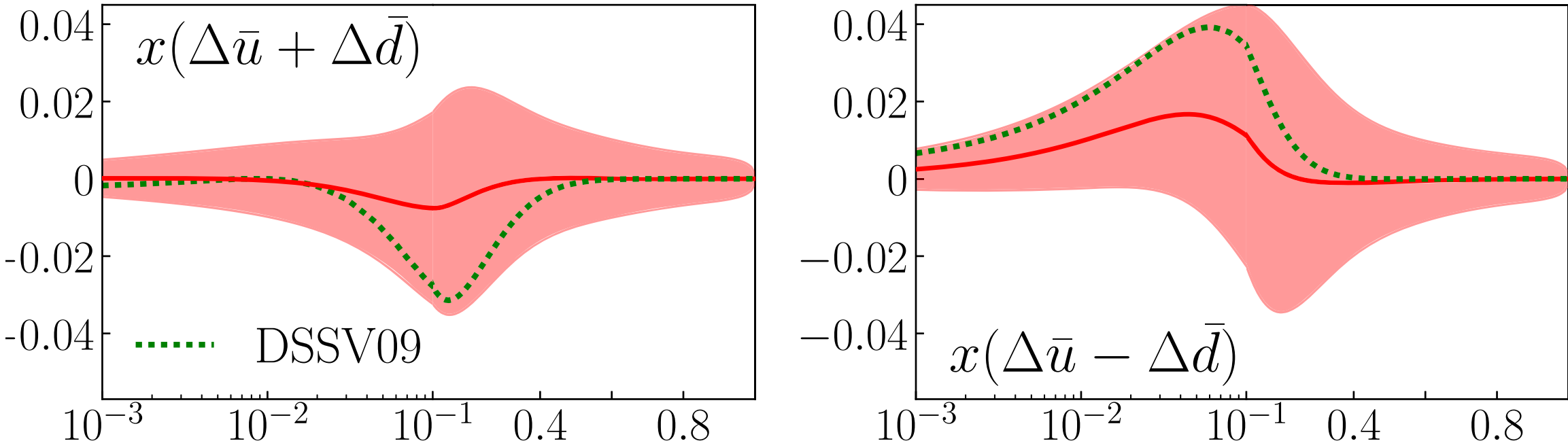
- Data:
- inclusive DIS
 - SIDIS
 - e^+e^- annihilation

Δs^+ :
 Consistent with 0
 Slightly >0 at intermediate x
 Shape determined by
 SIDIS K data

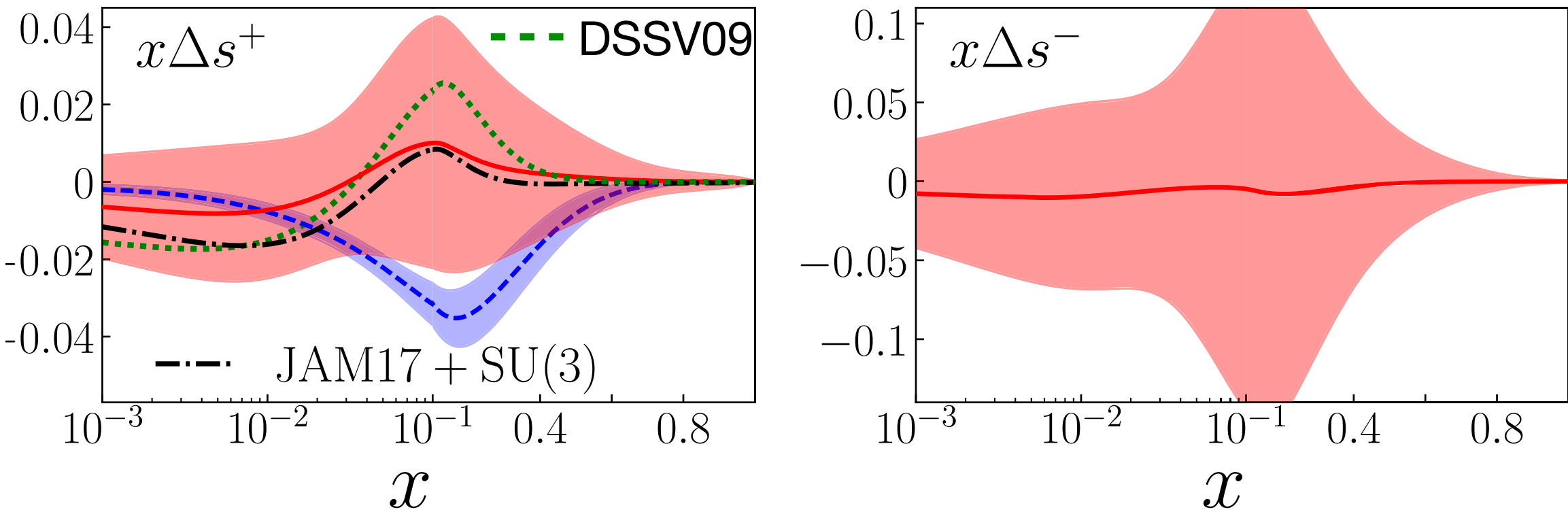
JAM Collaboration,
 Phys. Rev. Lett. **119** (2017) 132001



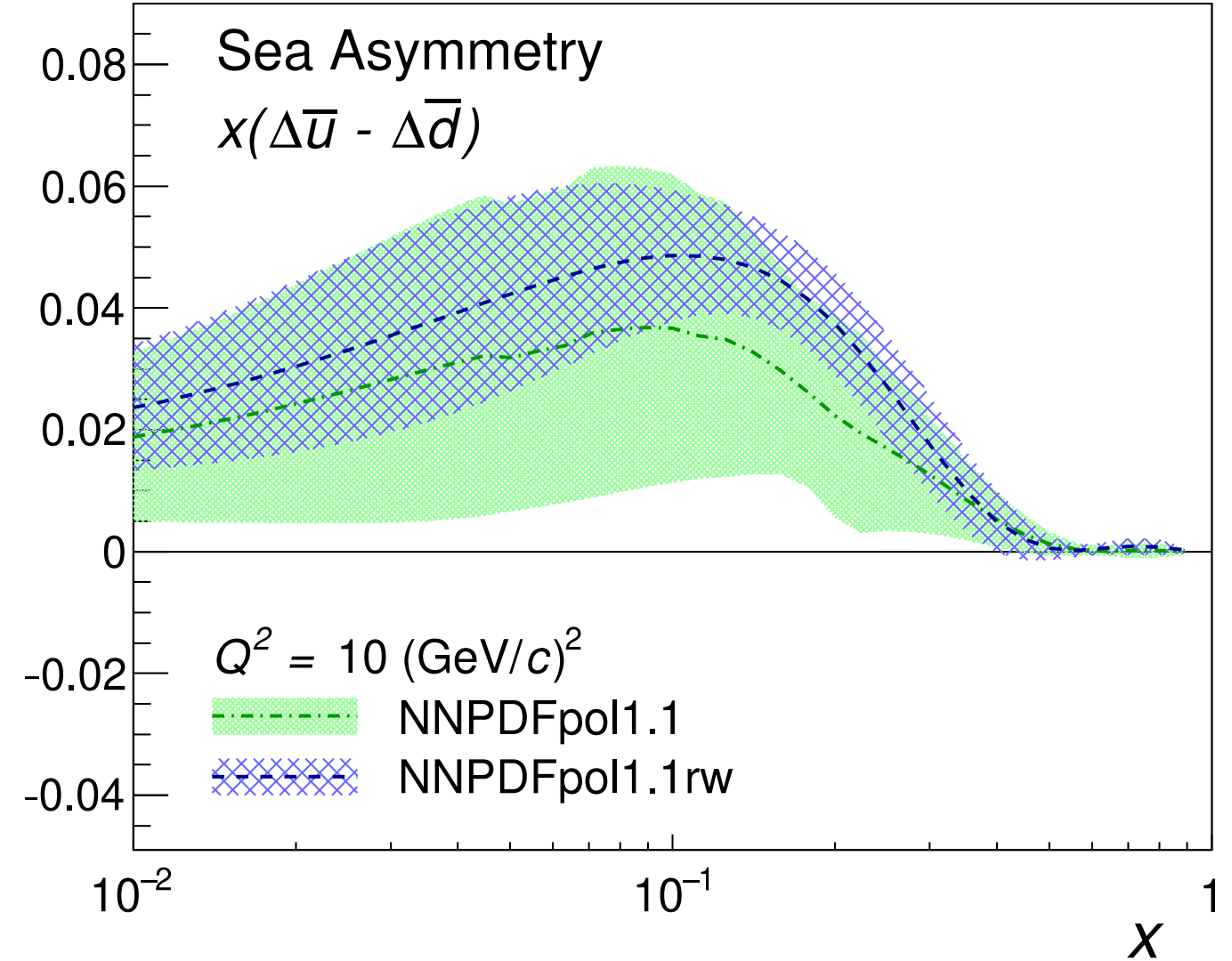
$\Delta q^+ = \Delta q + \Delta \bar{q}$:
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SIDIS: distinguish between q and \bar{q}
 $\Delta \bar{u} - \Delta \bar{d}$ slightly positive



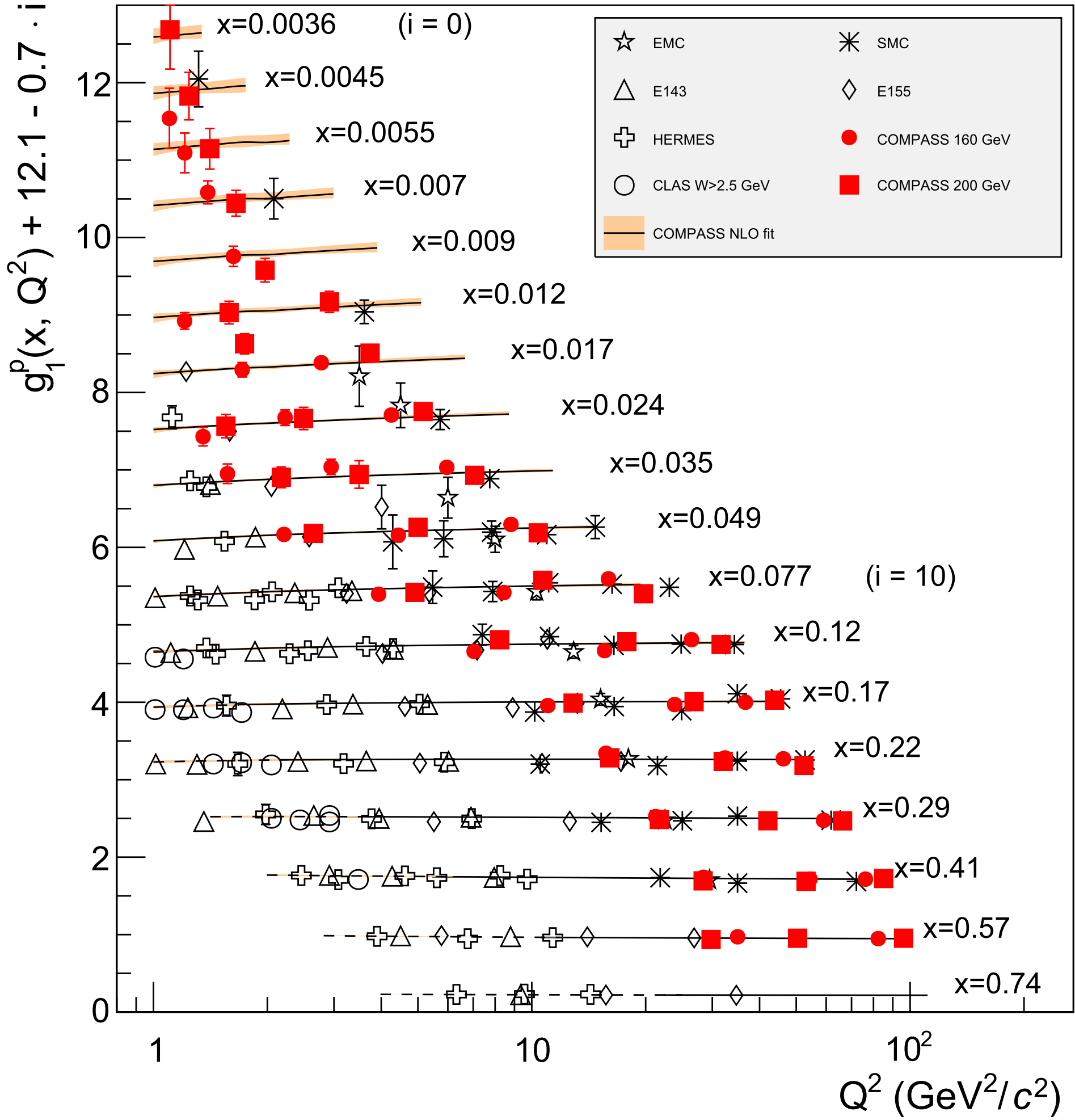
STAR, Phys. Rev. D **99** (2019) 051102



Glueon helicity

g_1^p : world data

Phys. Lett. B 753 (2016) 18

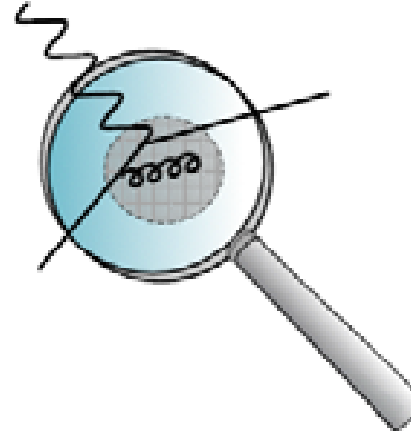
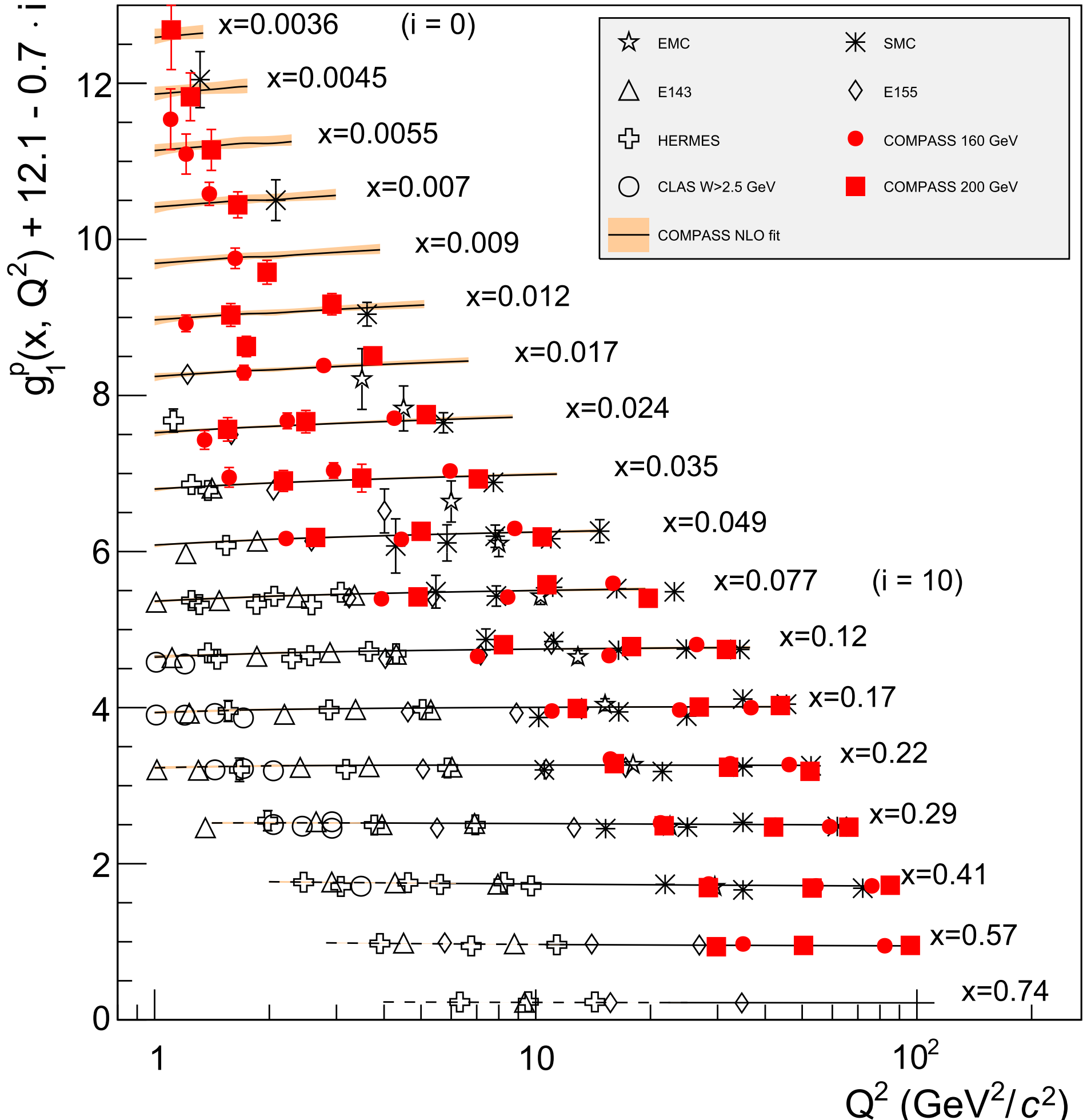


scaling violation from $g_1(x, Q^2)$

Gloun helicity

g_1^p : world data

Phys. Lett. B 753 (2016) 18



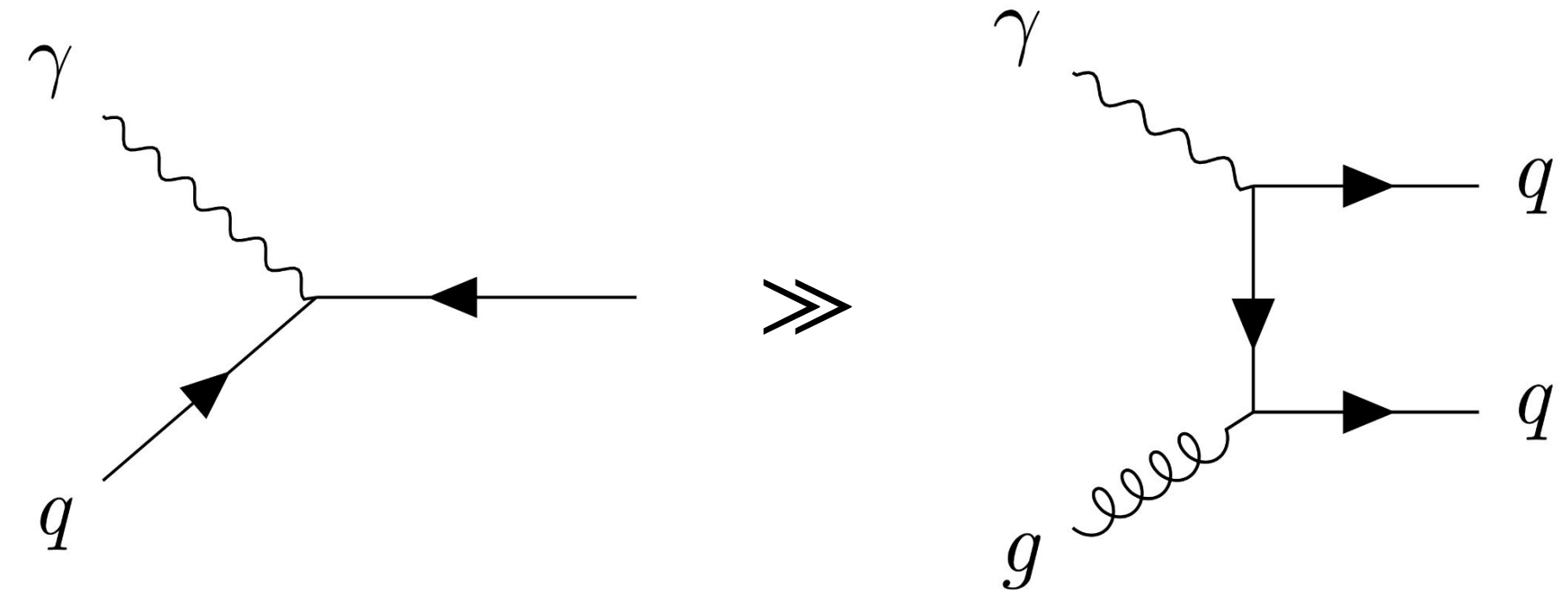
scaling violation from $g_1(x, Q^2)$

$$\frac{dg_1(x, Q^2)}{d \ln Q^2} \propto -\Delta g(x, Q^2)$$

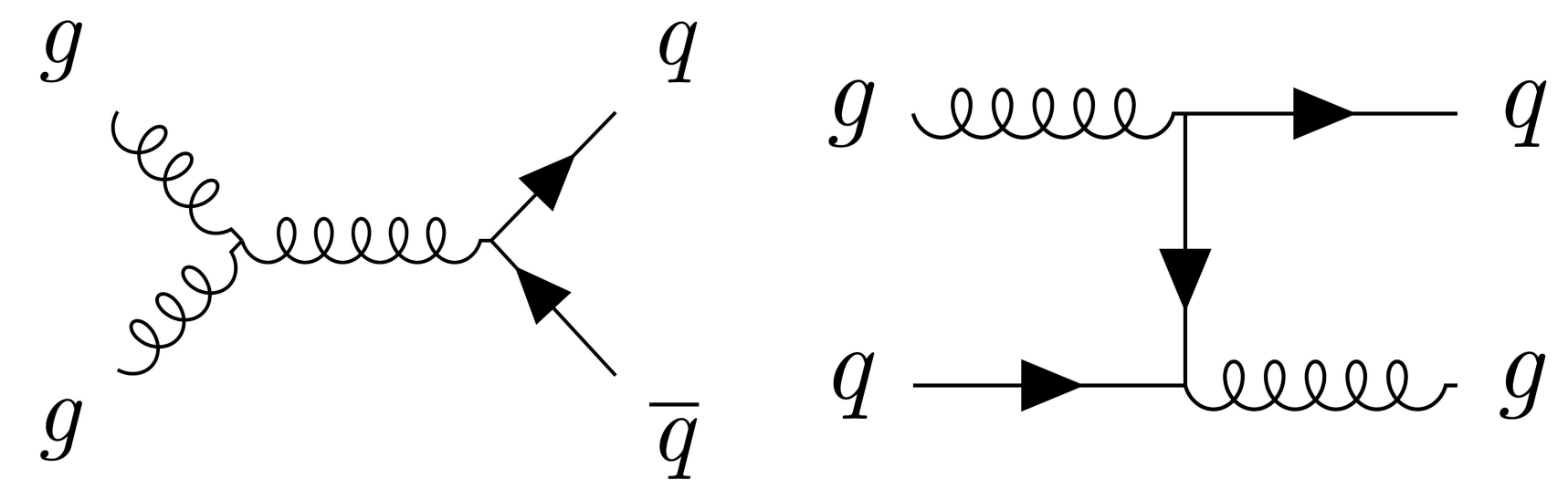
→ gluon spin

Double-spin asymmetry in pp collisions

Inclusive DIS: gluons only enter at NLO



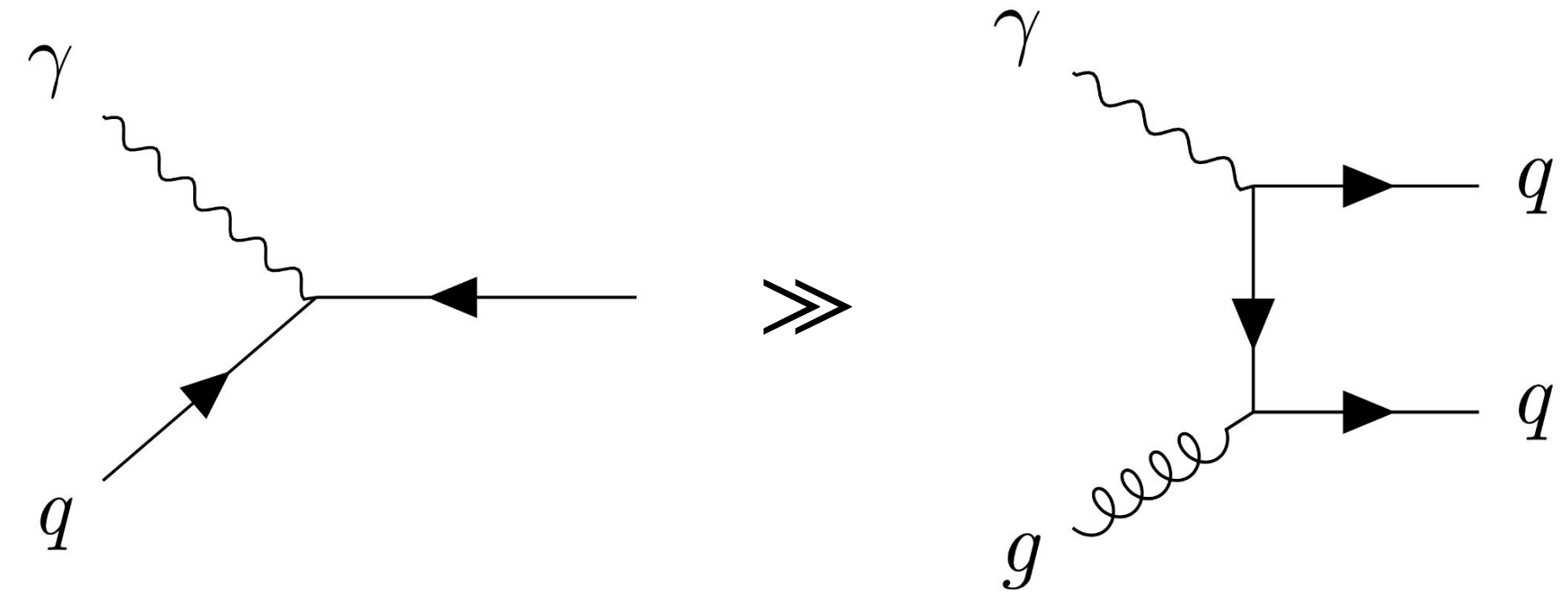
pp collisions: gluons enter at LO



- Inclusive jet production
- Inclusive dijet production
- π^0 and π^\pm production
- Direct photon production

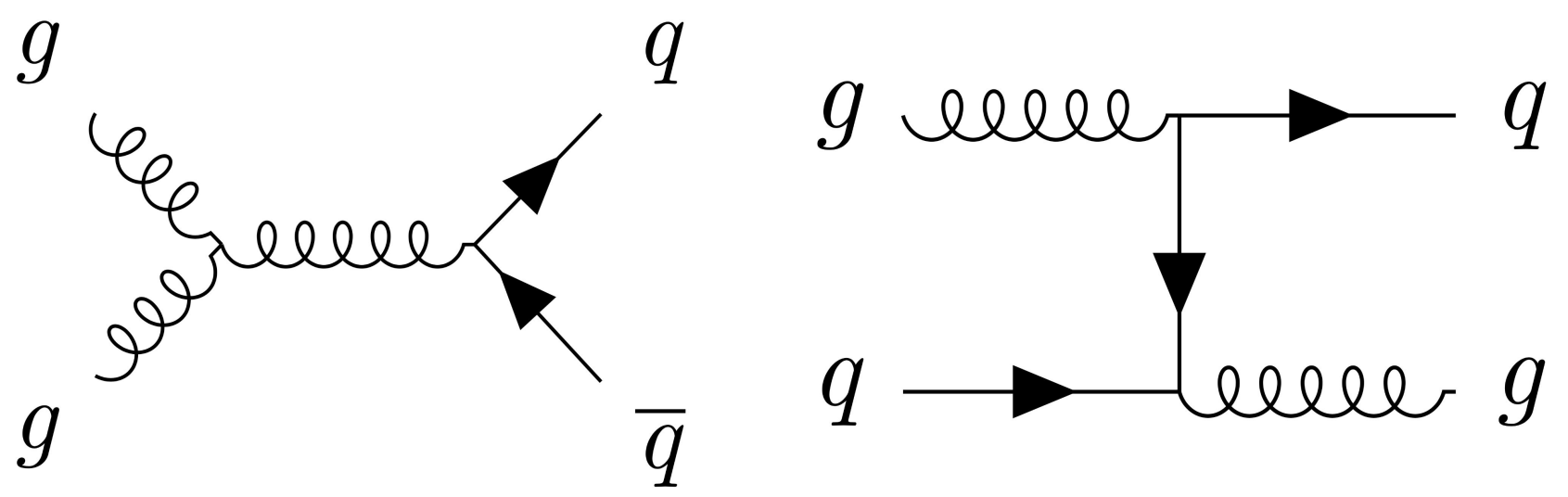
Double-spin asymmetry in pp collisions

Inclusive DIS: gluons only enter at NLO



- Increased sensitivity to gluons:
 - heavy-quark production
 - high- p_T hadrons

pp collisions: gluons enter at LO



- Inclusive jet production
- Inclusive dijet production
- π^0 and π^\pm production
- Direct photon production

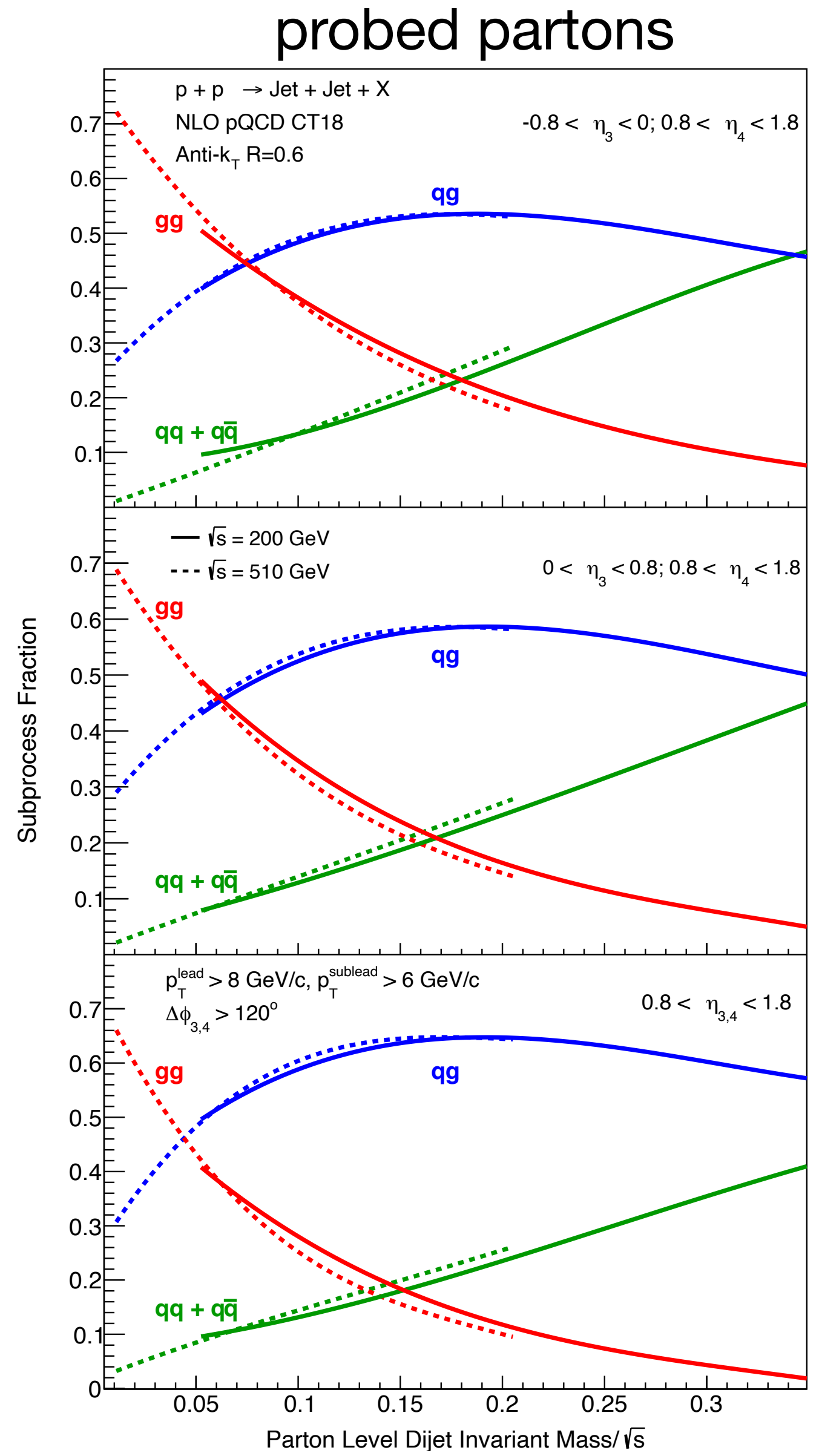
Longitudinal double-spin asymmetry in pp collisions

$$A_{LL} = \frac{\frac{\vec{N}^{\text{dijet}}}{\vec{L}} - \frac{\vec{N}^{\text{dijet}}}{\vec{L}}}{\frac{\vec{N}^{\text{dijet}}}{\vec{L}} + \frac{\vec{N}^{\text{dijet}}}{\vec{L}}}(x_B, Q^2)$$
$$\propto \frac{\Delta f(x_1, Q^2)\Delta f(x_2, Q^2)}{f(x_1, Q^2)f(x_2, Q^2)}$$

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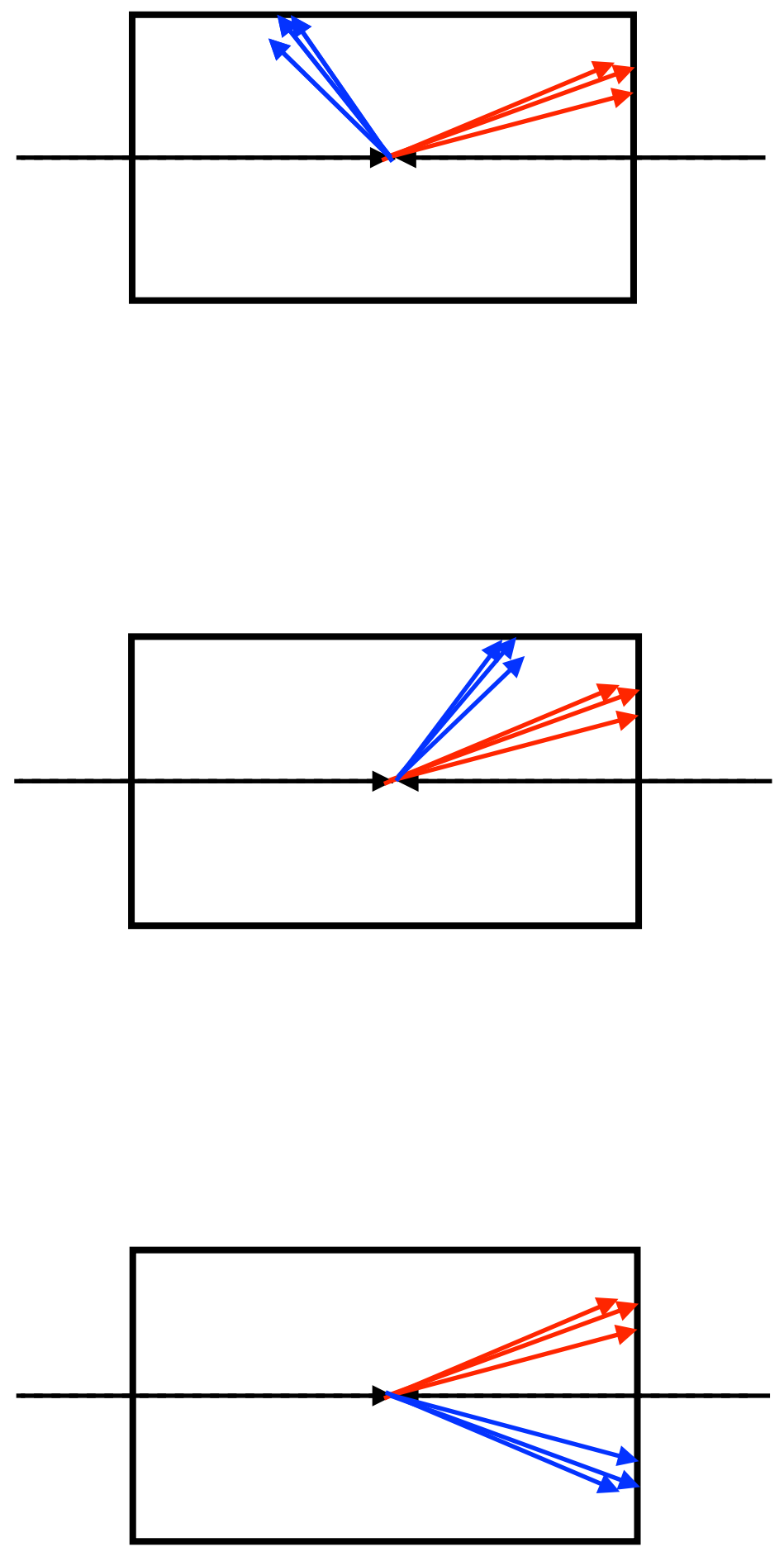
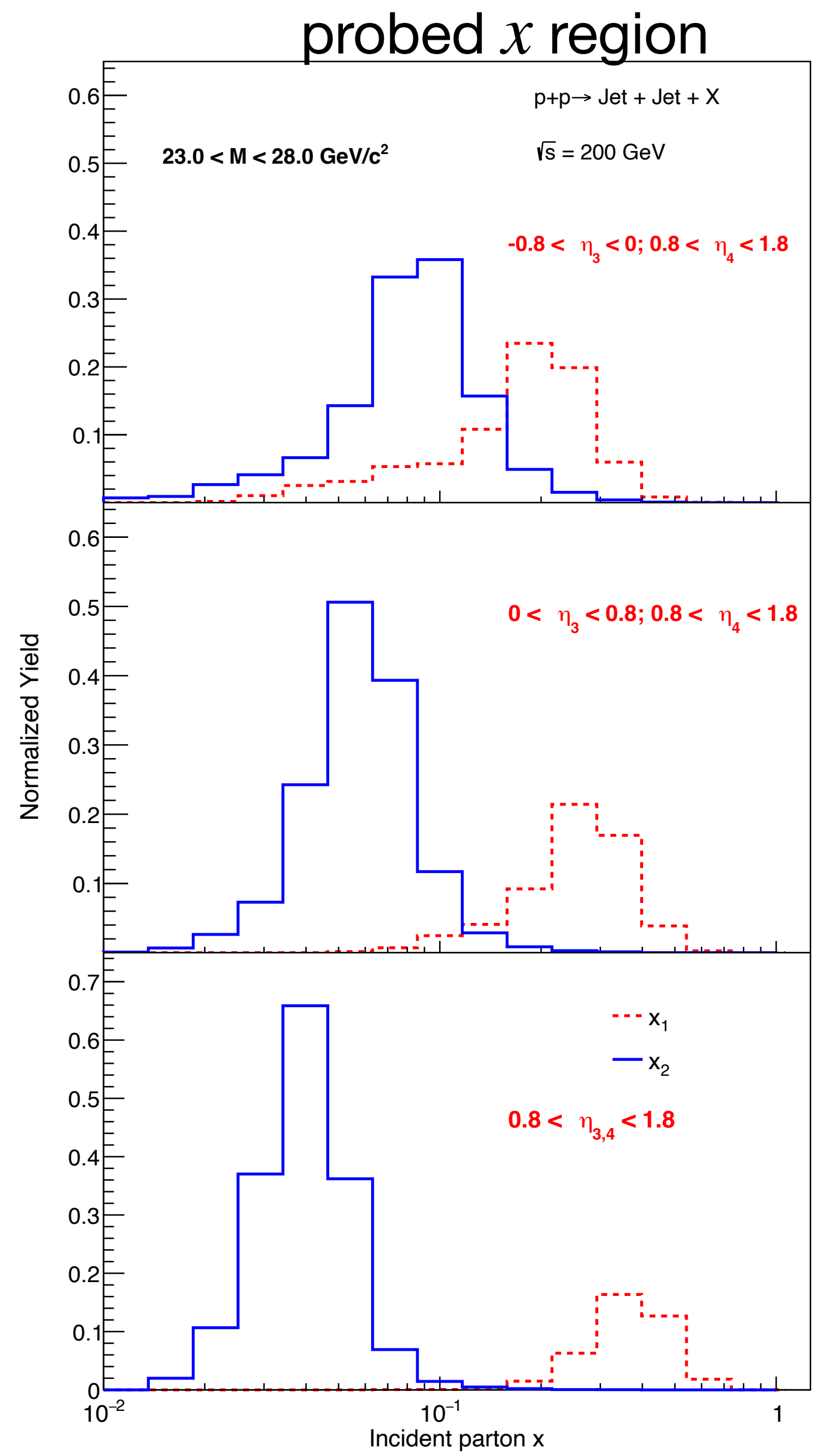
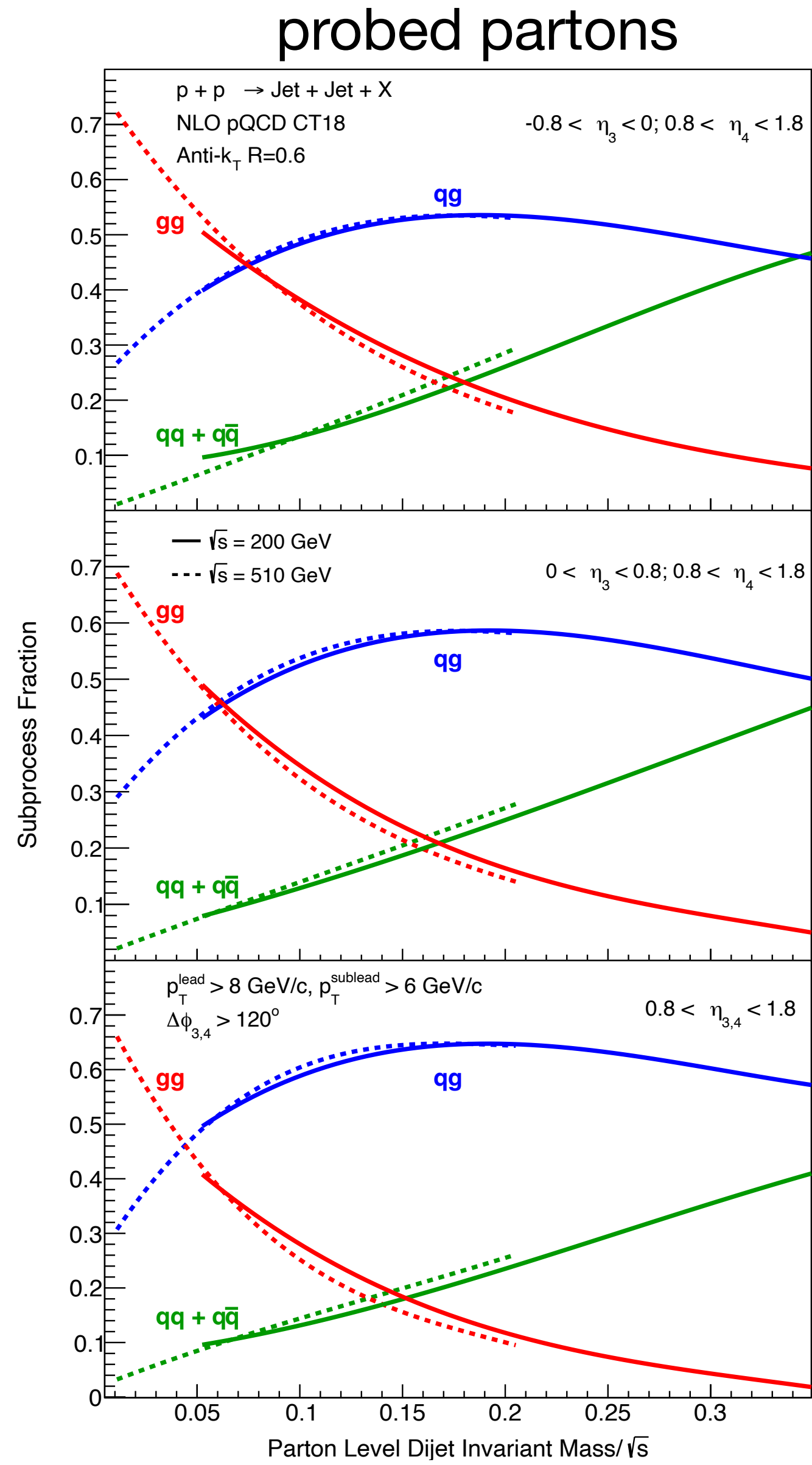
$$\propto \frac{\Delta f(x_1, Q^2) \Delta f(x_2, Q^2)}{f(x_1, Q^2) f(x_2, Q^2)}$$



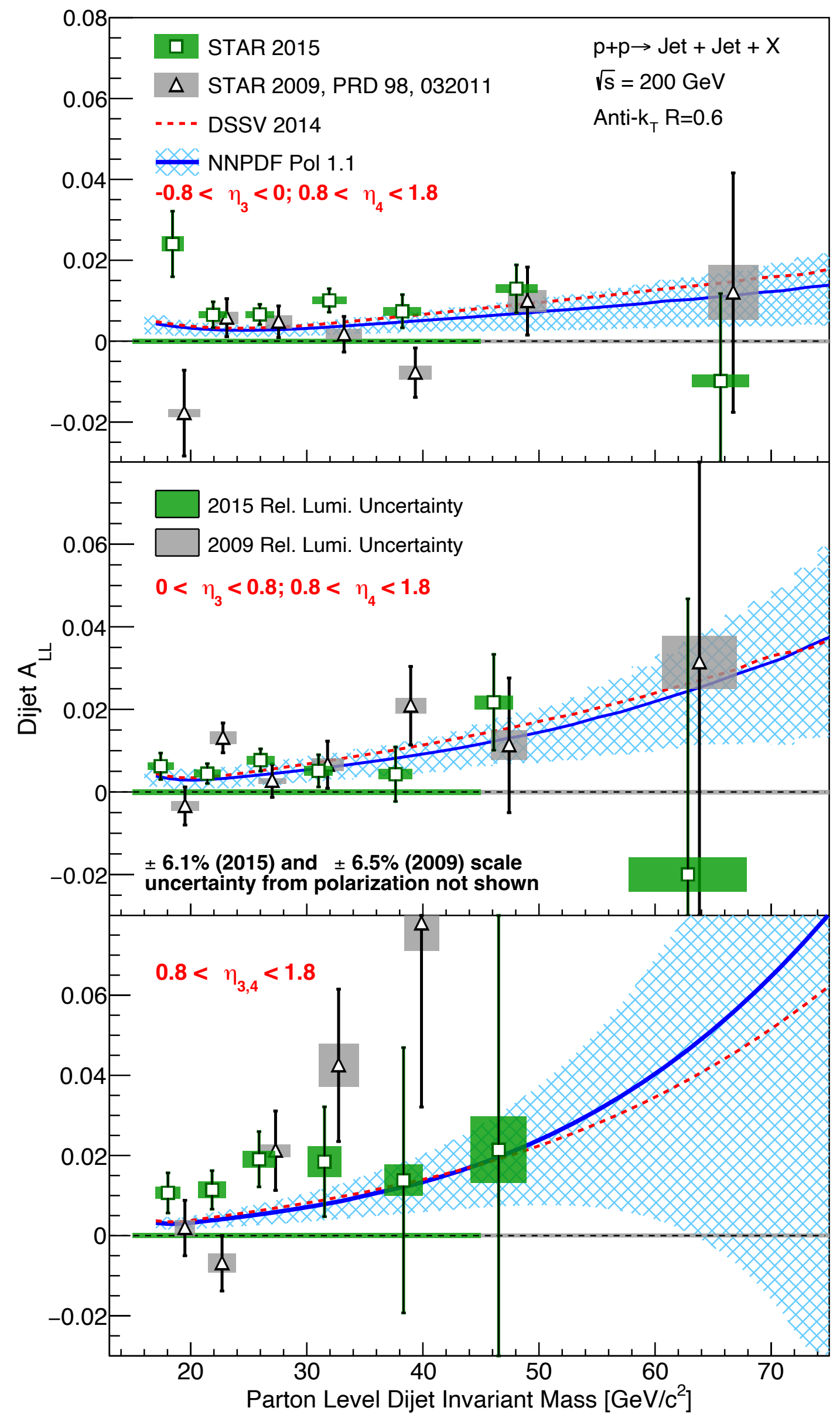
Longitudinal double-spin asymmetry in pp collisions

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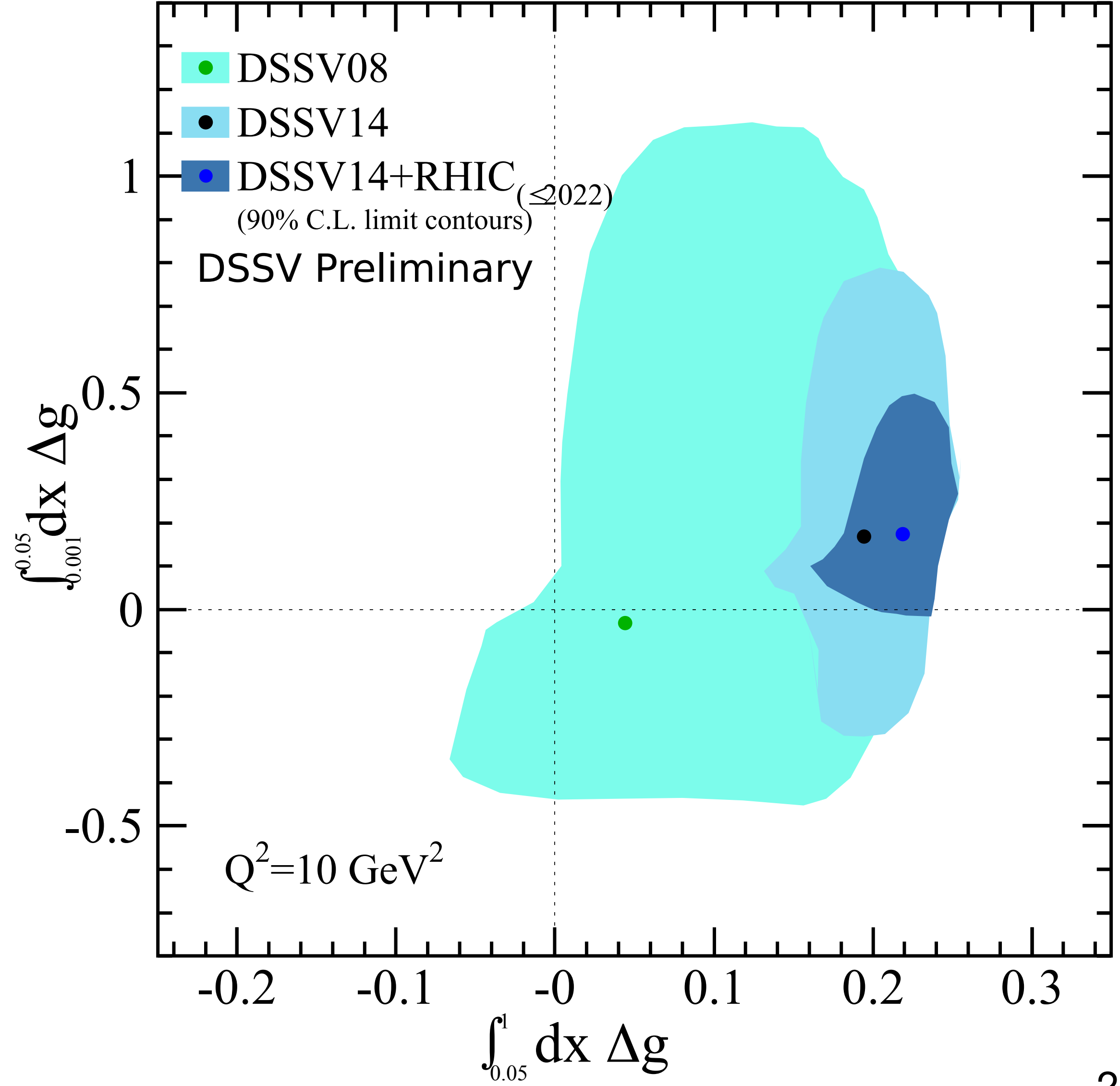


Longitudinal double-spin asymmetry measurement



Global fits: gluon helicity PDF

arXiv.: 2302.00605

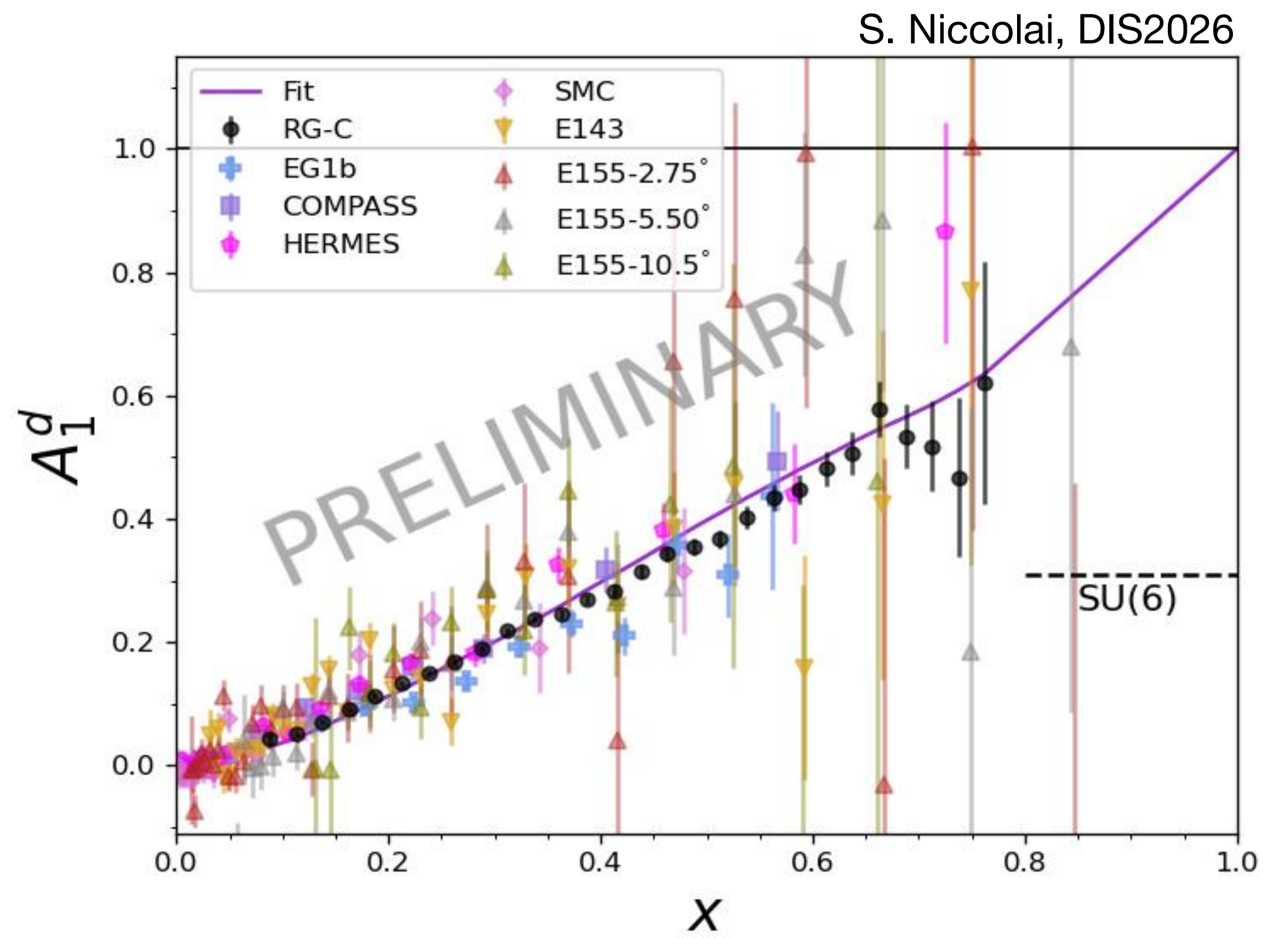
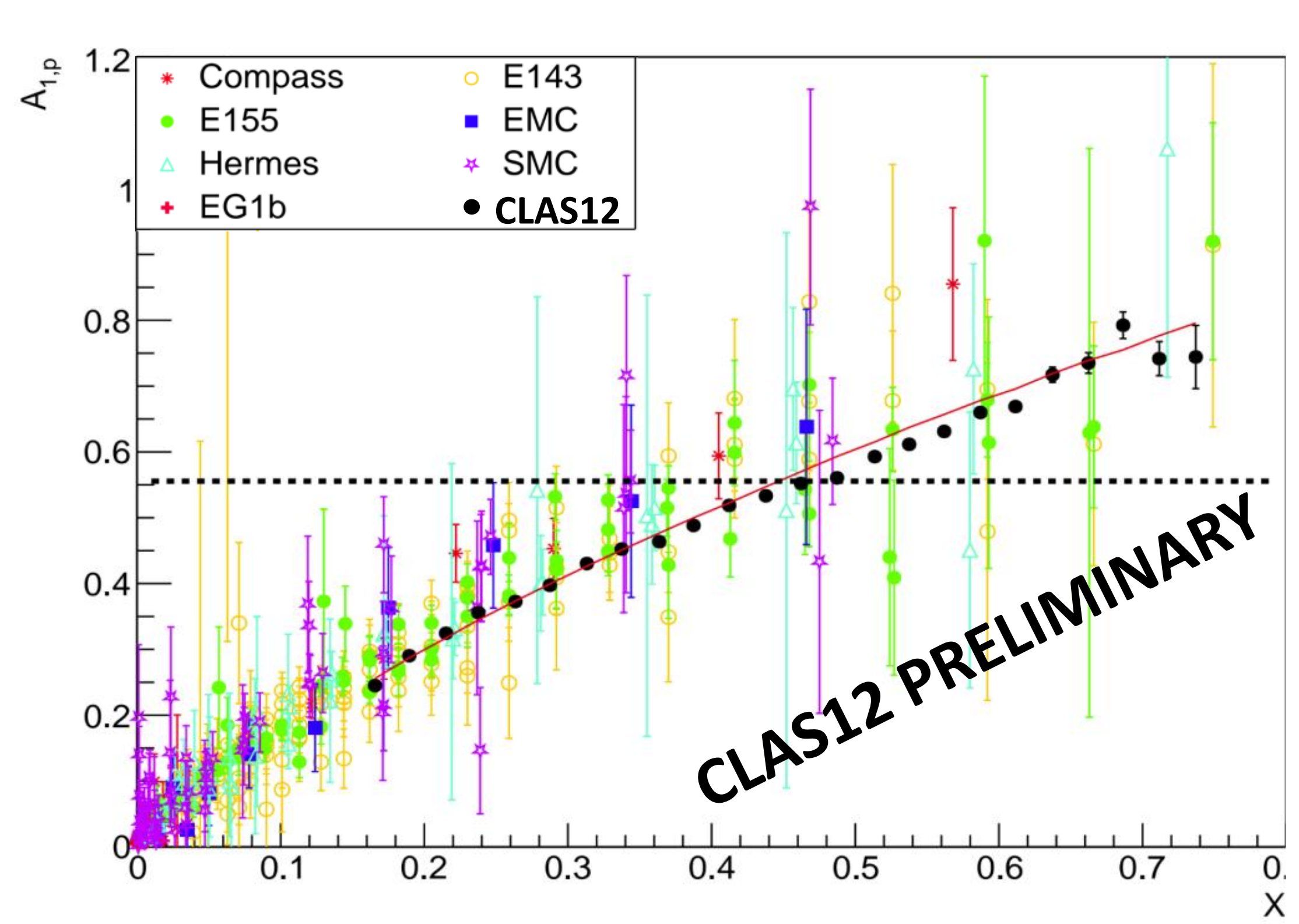


(SI)DIS provide limited constraints on ΔG

RHIC jet and pion A_{LL} data:

$\Delta G > 0$ for $x > 0.05$

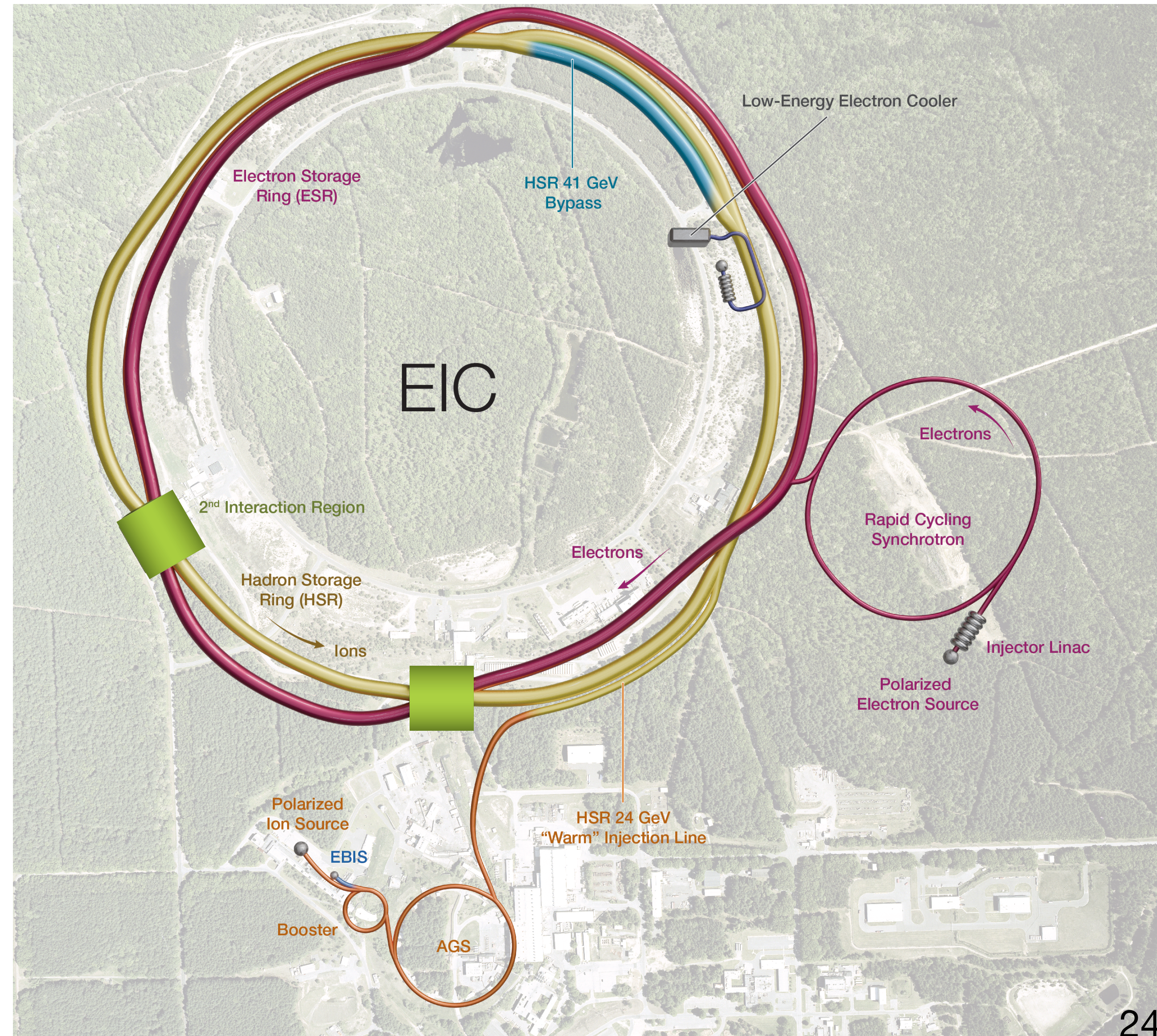
Future: probing the valence region with CLAS12



S. Niccolai, DIS2026

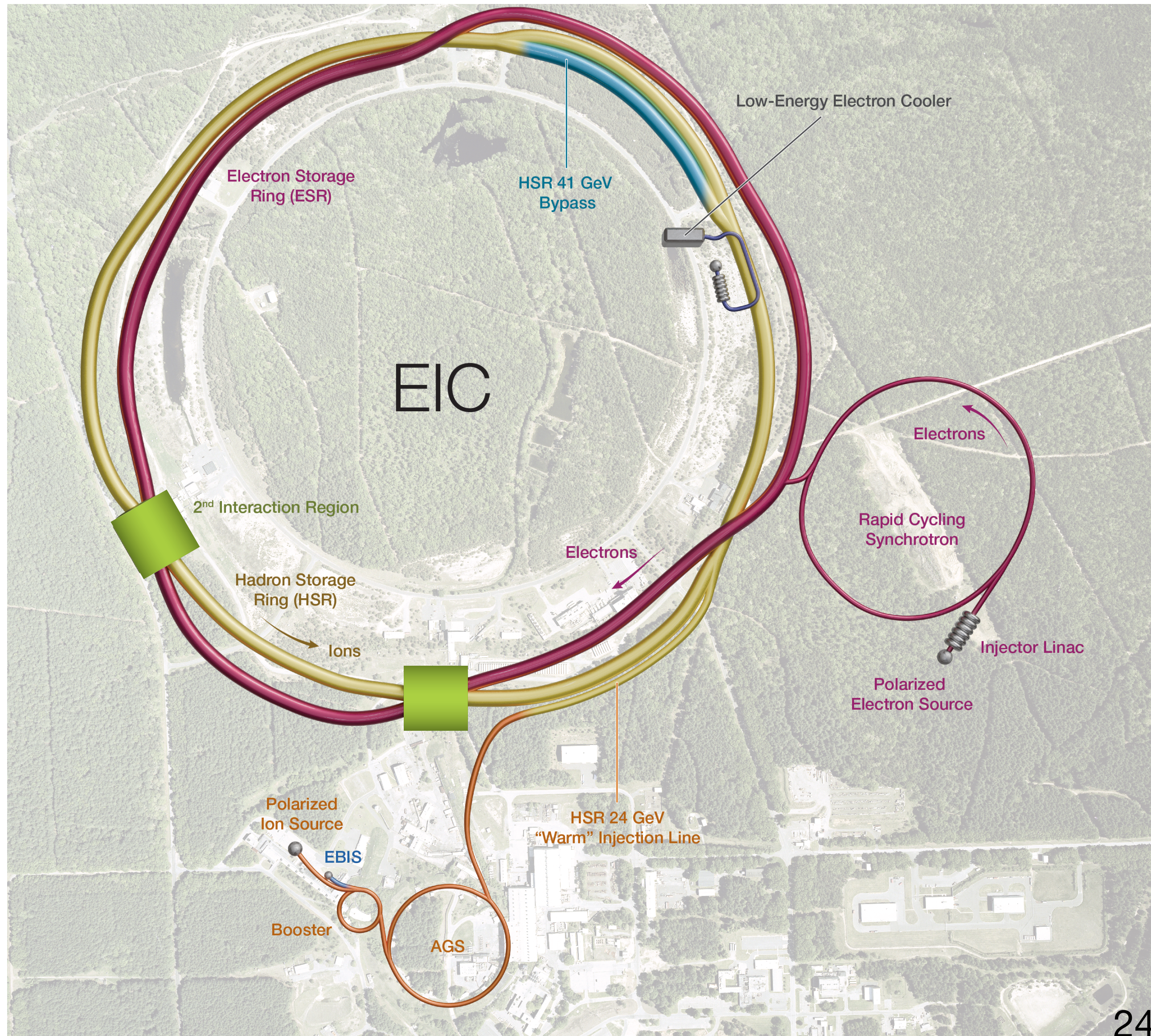
Valence region
 Flavour decomposition combining p and D data

Future: the electron-ion collider (EIC)



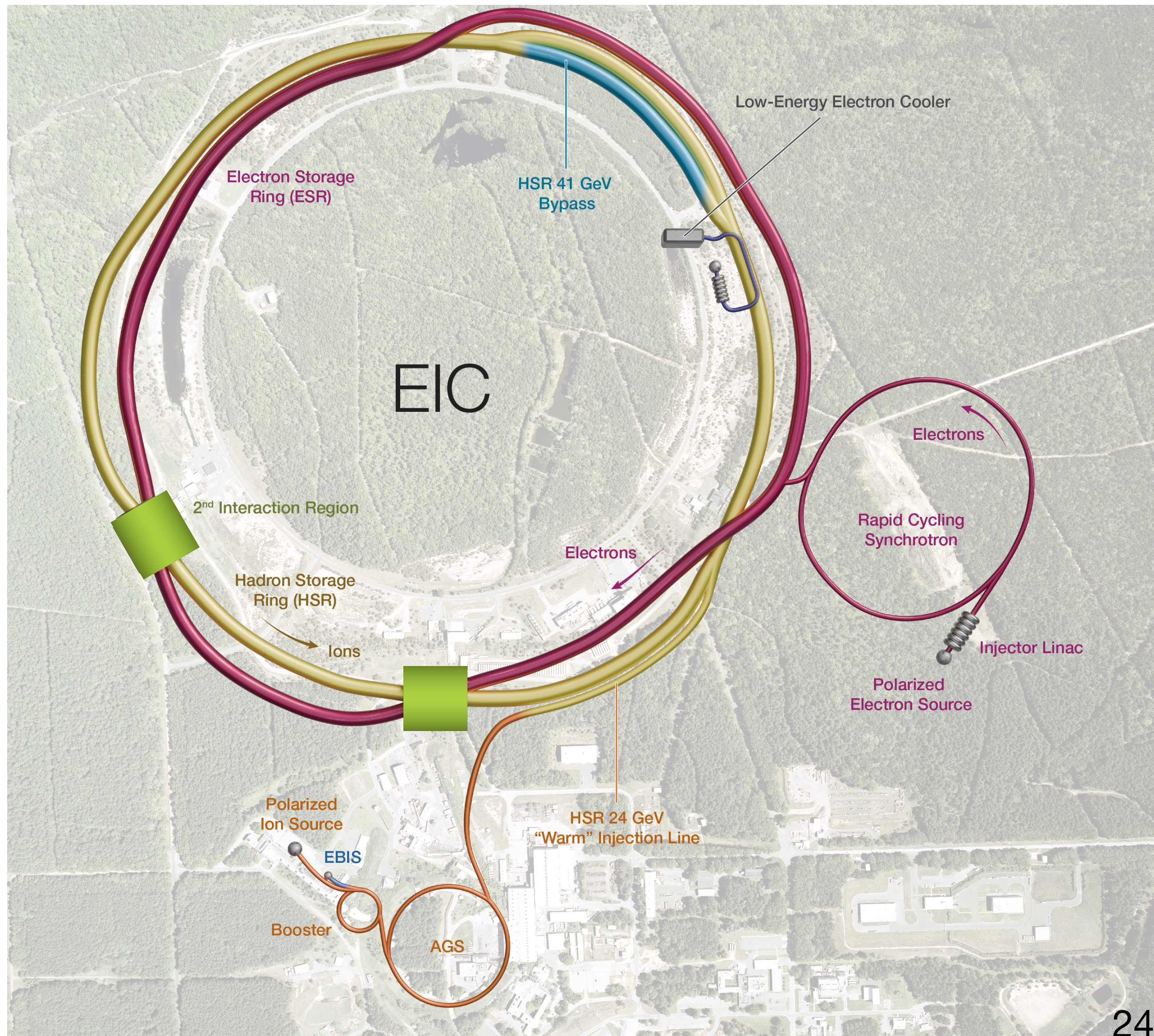
- Based on RHIC:
 - use existing hadron storage ring energy: 41, 100–275 GeV
 - add electron storage ring in RHIC tunnel energy: 5–10 GeV

Future: the electron-ion collider (EIC)



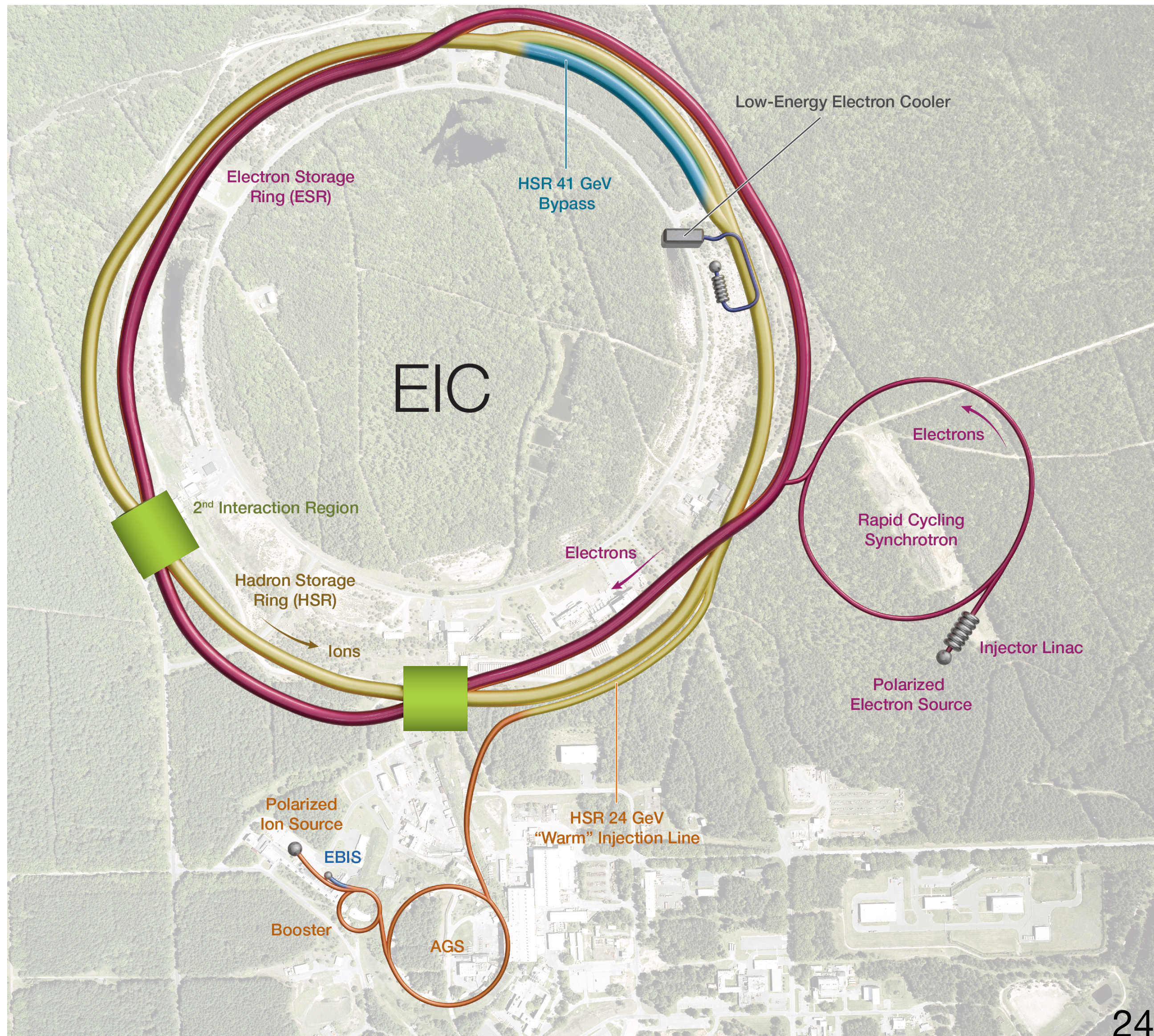
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- $\sqrt{s} = 29 - 100 \text{ GeV}$ (140 GeV upgradable)

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- $\vec{e} + \vec{p}^\uparrow, \vec{He}^\uparrow$
~ 70% polarisation

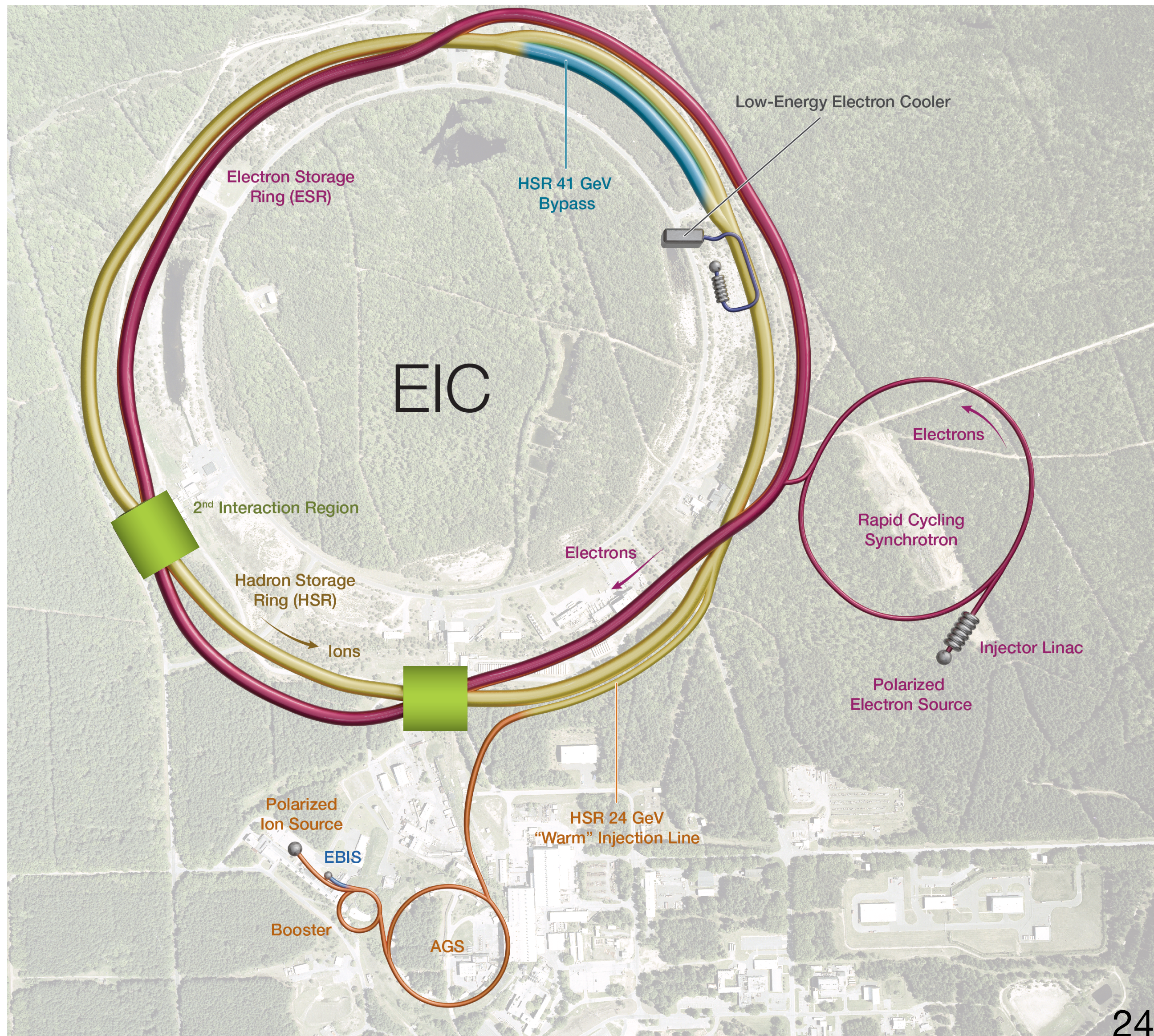
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~ 70% polarisation
+ heavier, unpolarised ions, up to Uranium

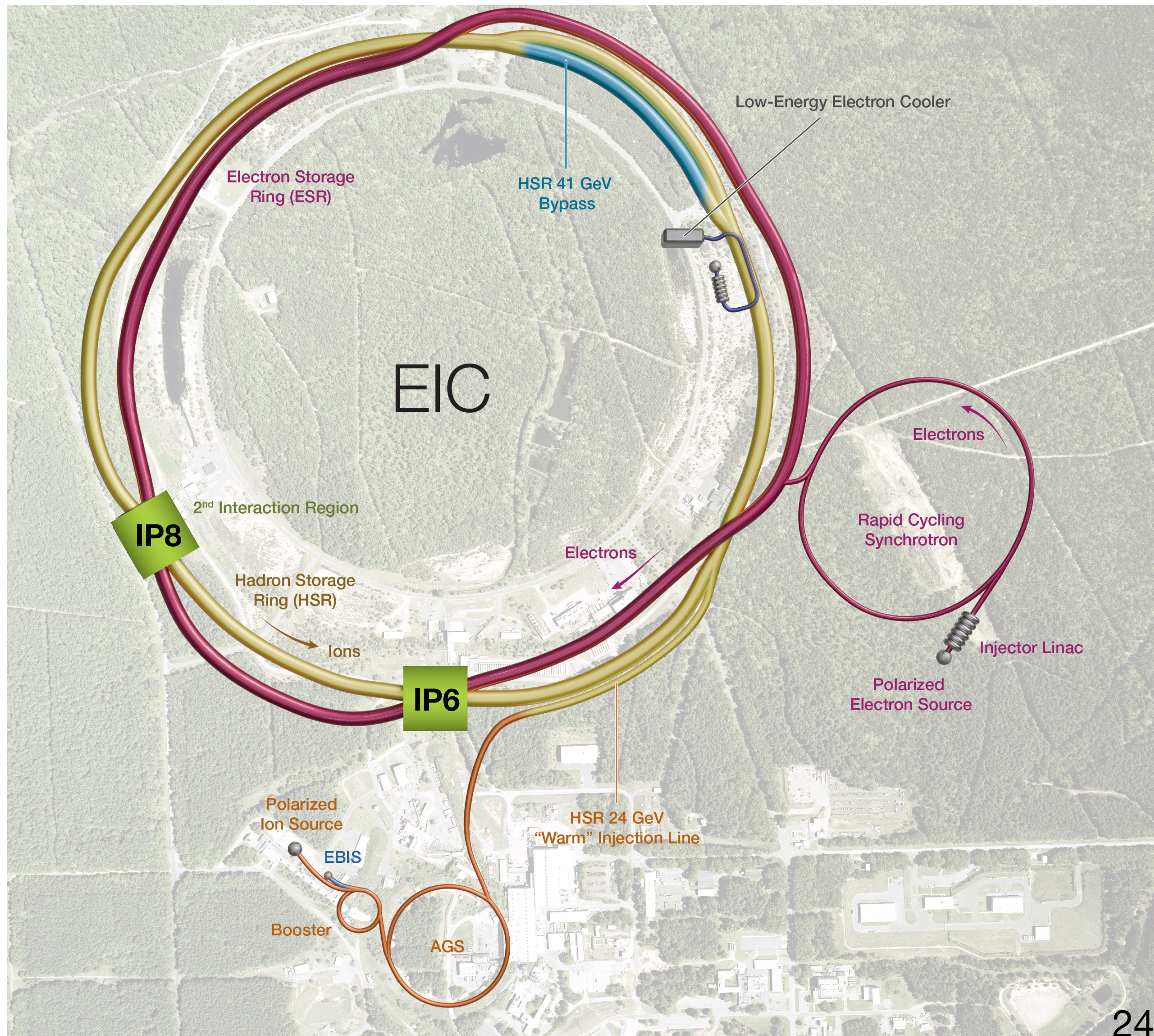
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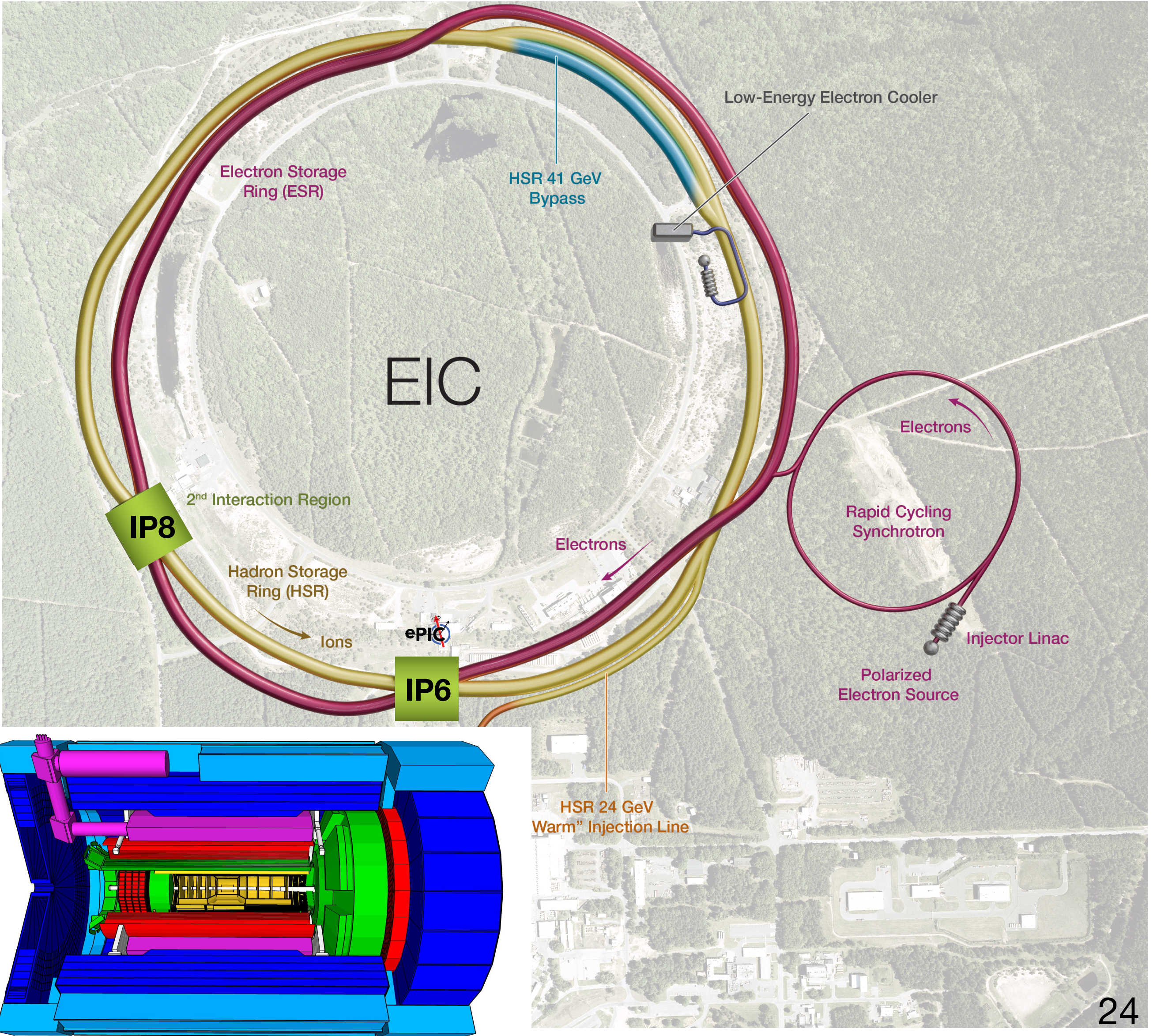
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- $\mathcal{L} = 10^{33-34} \text{ cm}^{-2} \text{ s}^{-1}$
 ↔ $\mathcal{L}_{\text{int}} = 10 - 100 \text{ fb}^{-1}/\text{year}$

Future: the electron-ion collider (EIC)



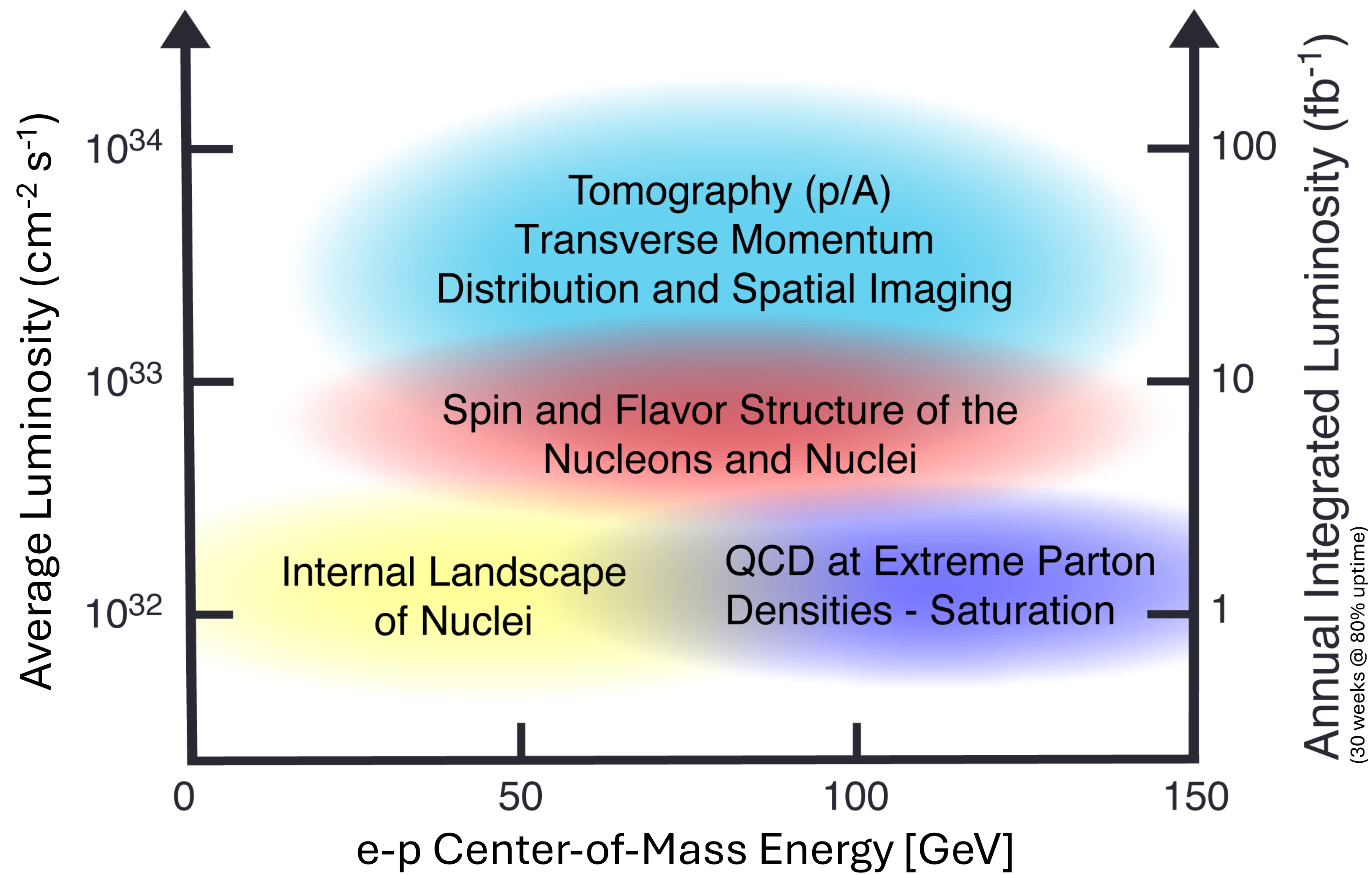
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Future: the electron-ion collider (EIC)

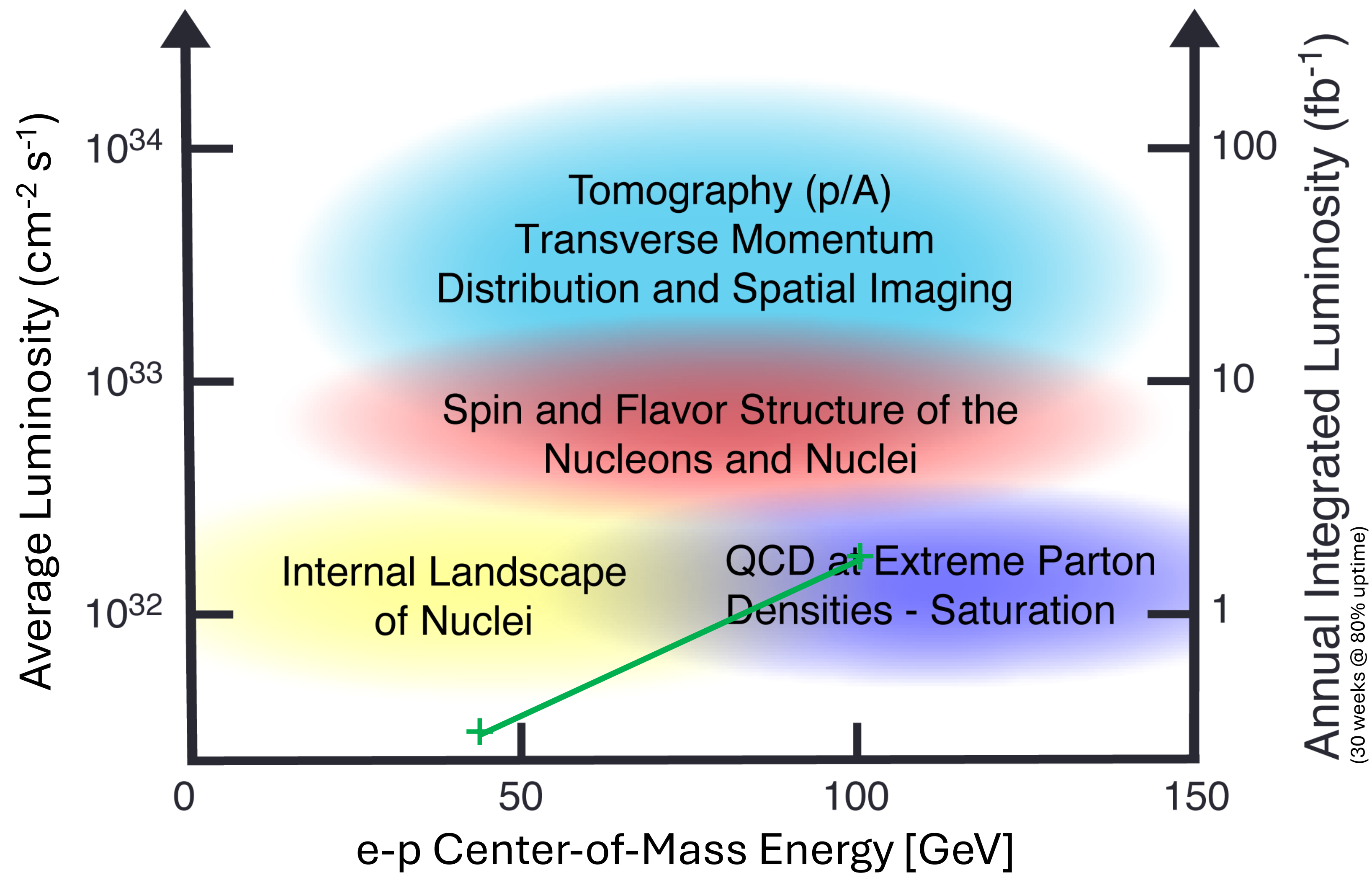


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The various data-collection stages

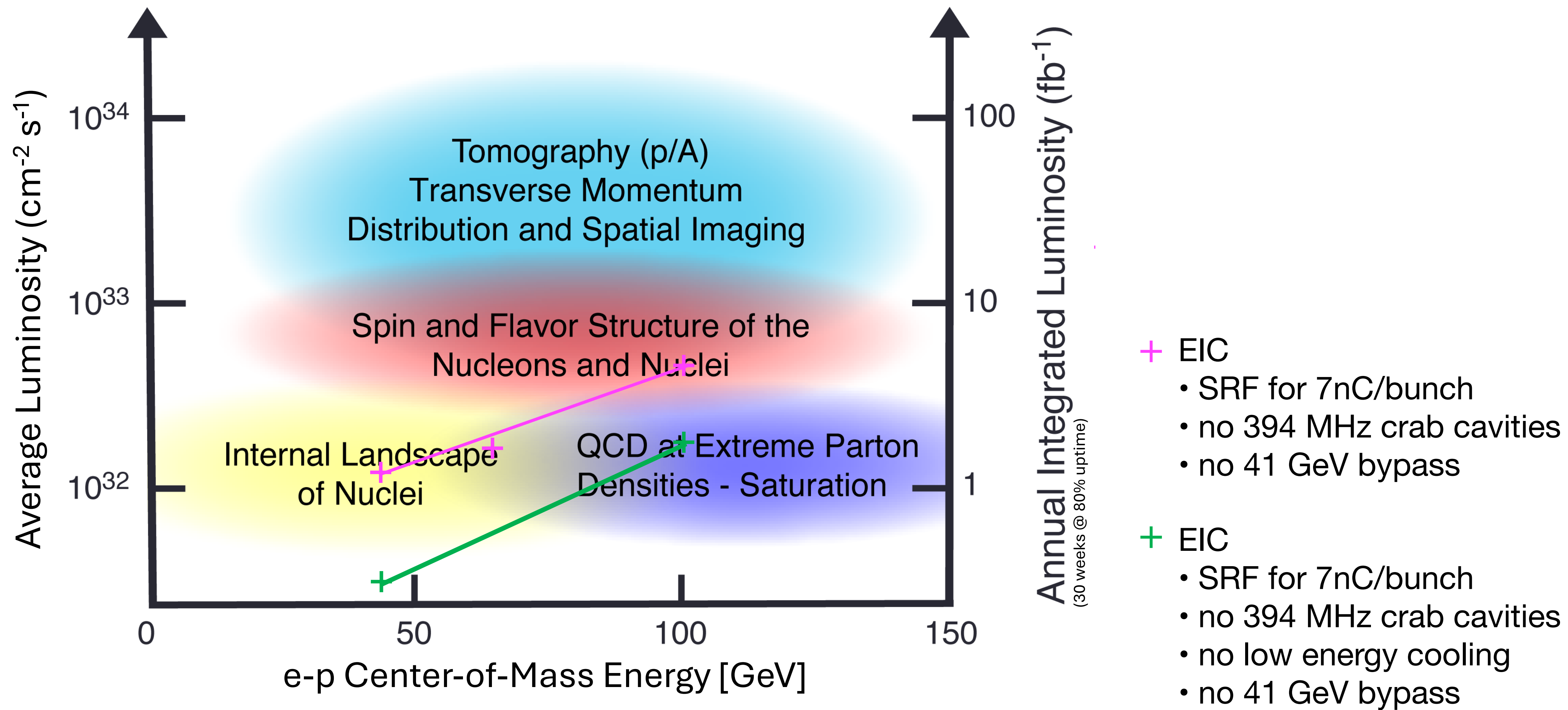


The various data-collection stages

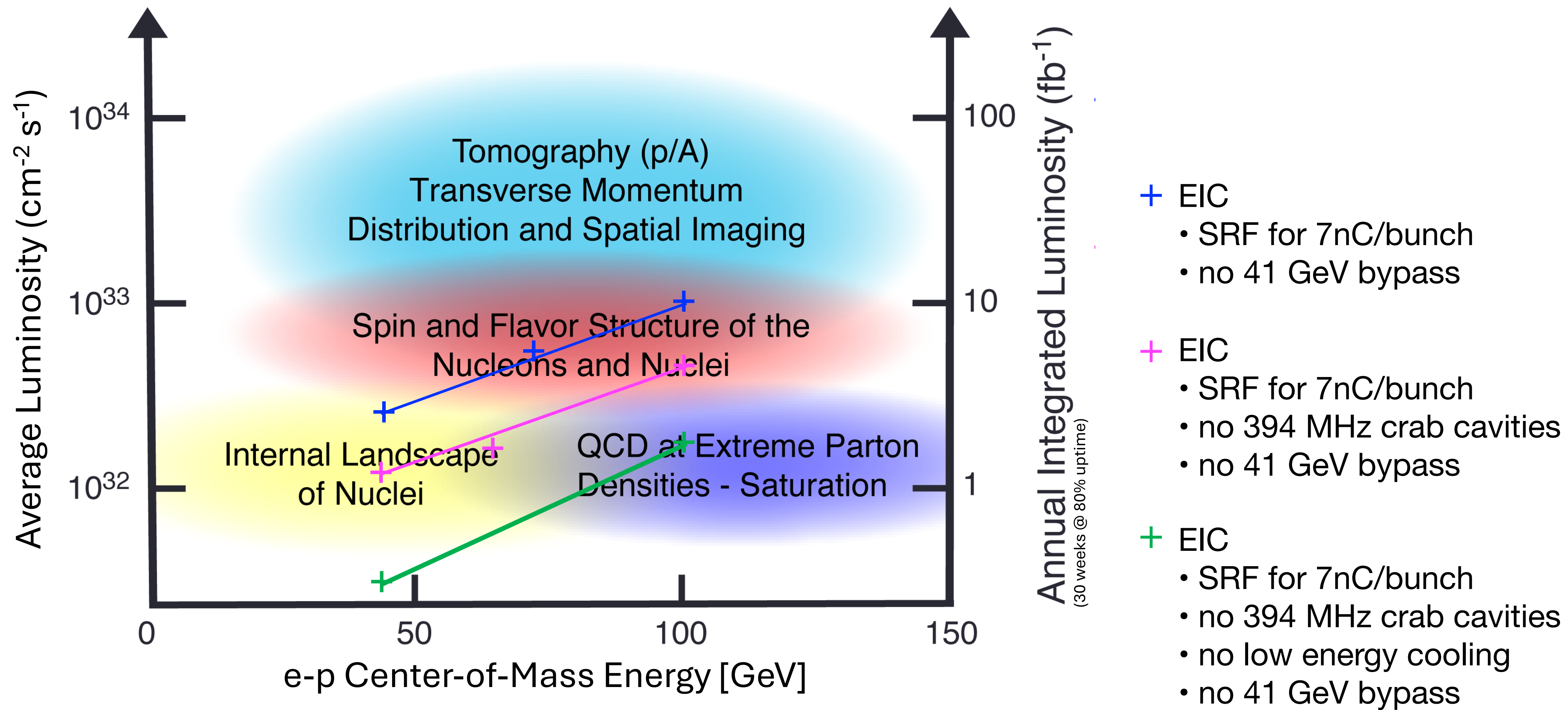


- + EIC
 - SRF for 7nC/bunch
 - no 394 MHz crab cavities
 - no low energy cooling
 - no 41 GeV bypass

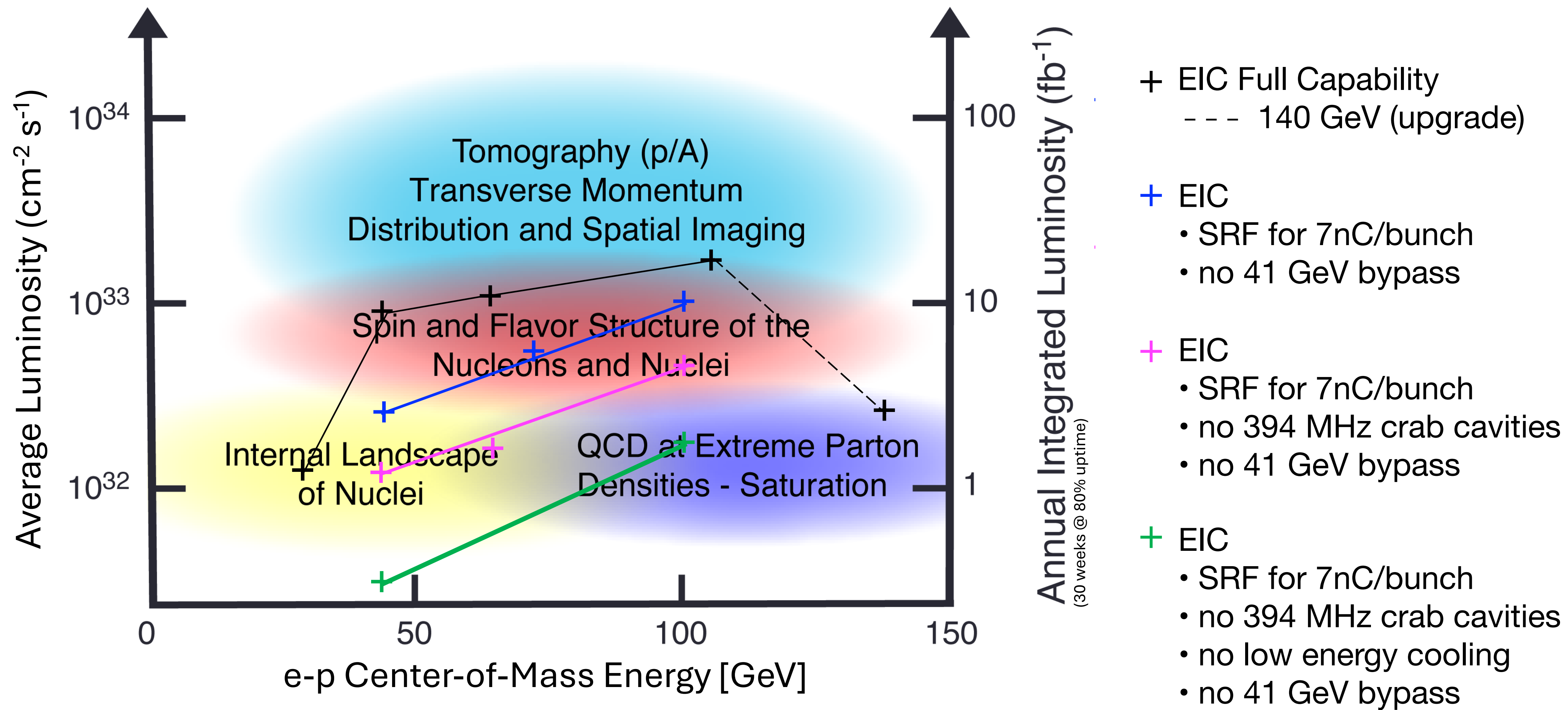
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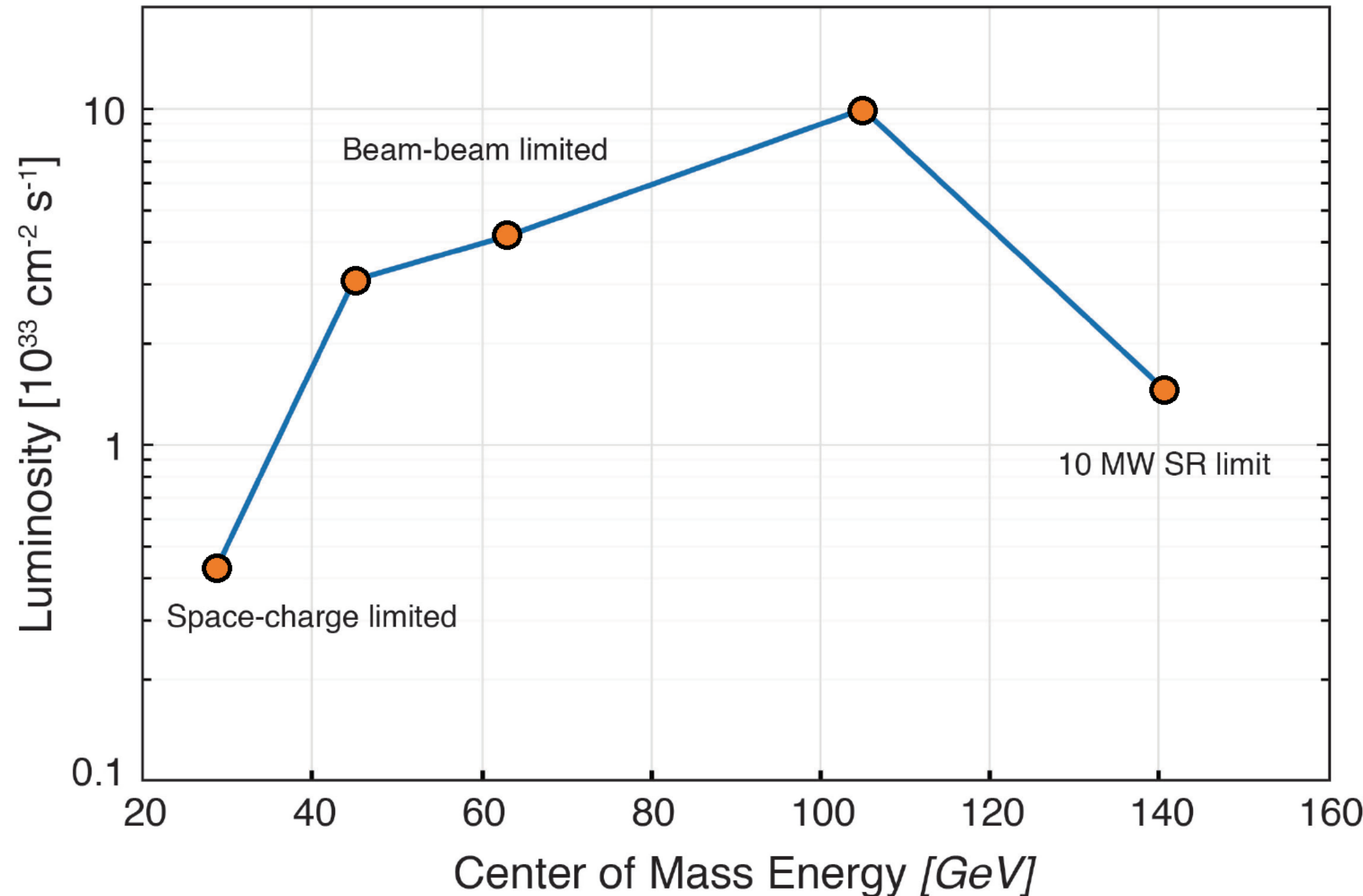
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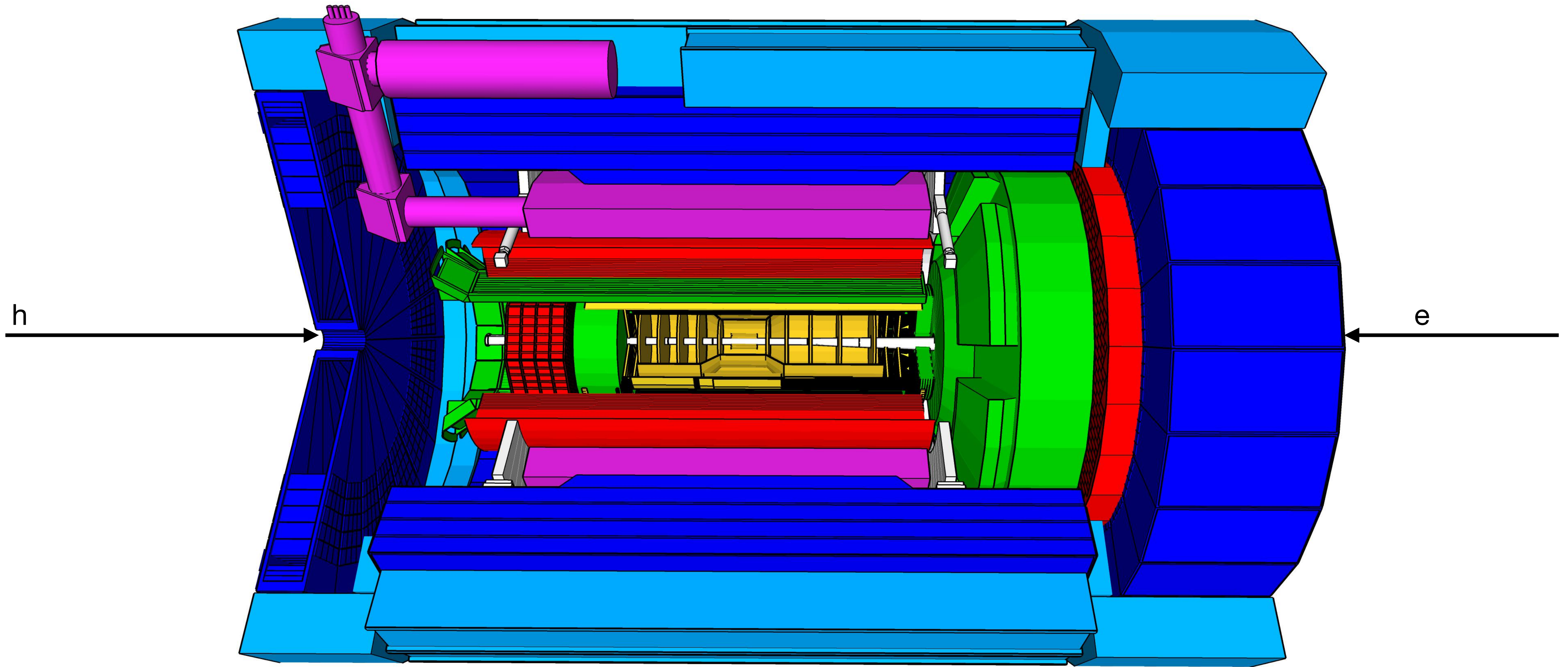


Luminosity and centre-of-mass energy: ep collisions

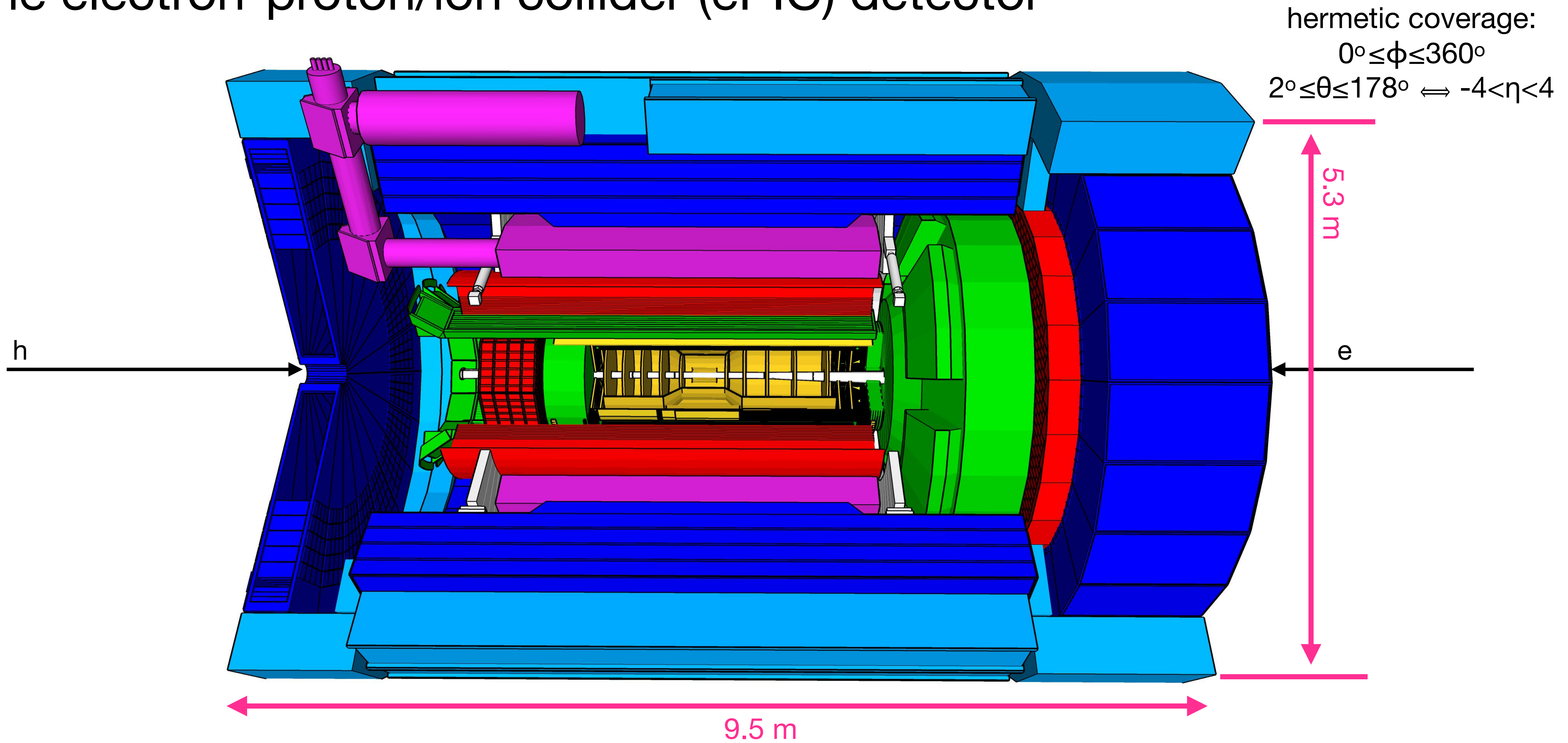


Luminosity for eA similar within factor 2–3

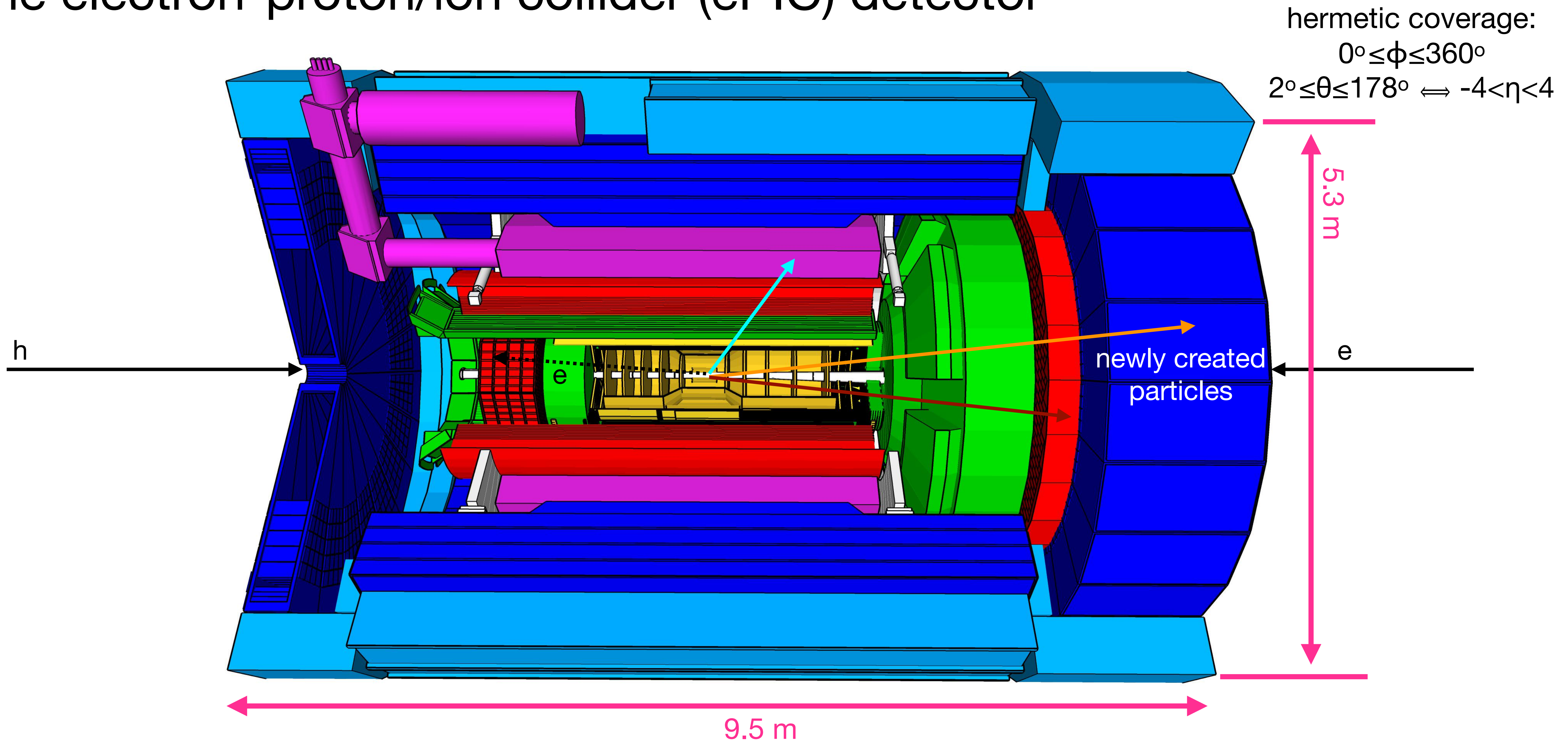
The electron-proton/ion collider (ePIC) detector



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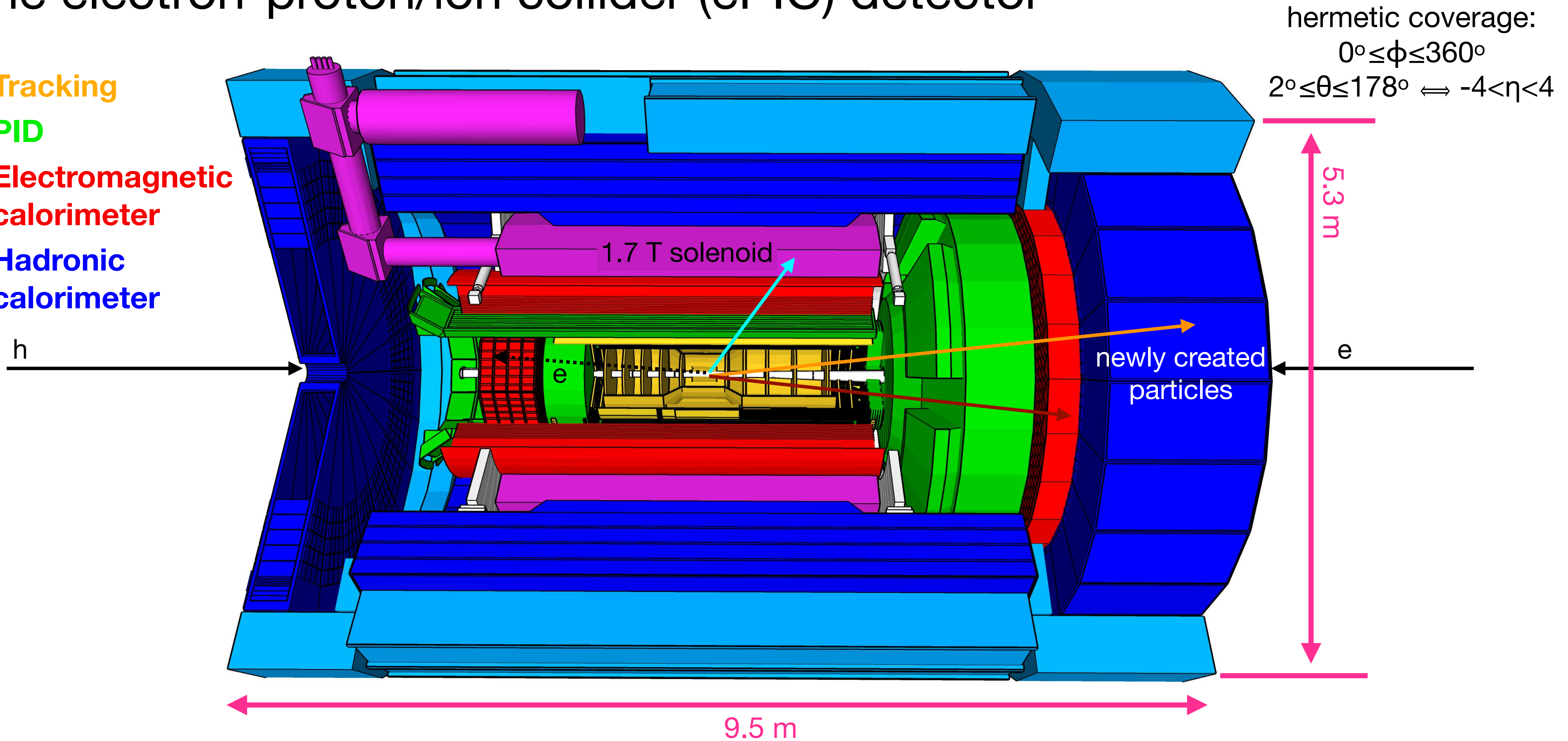


The electron-proton/ion collider (ePIC) detector



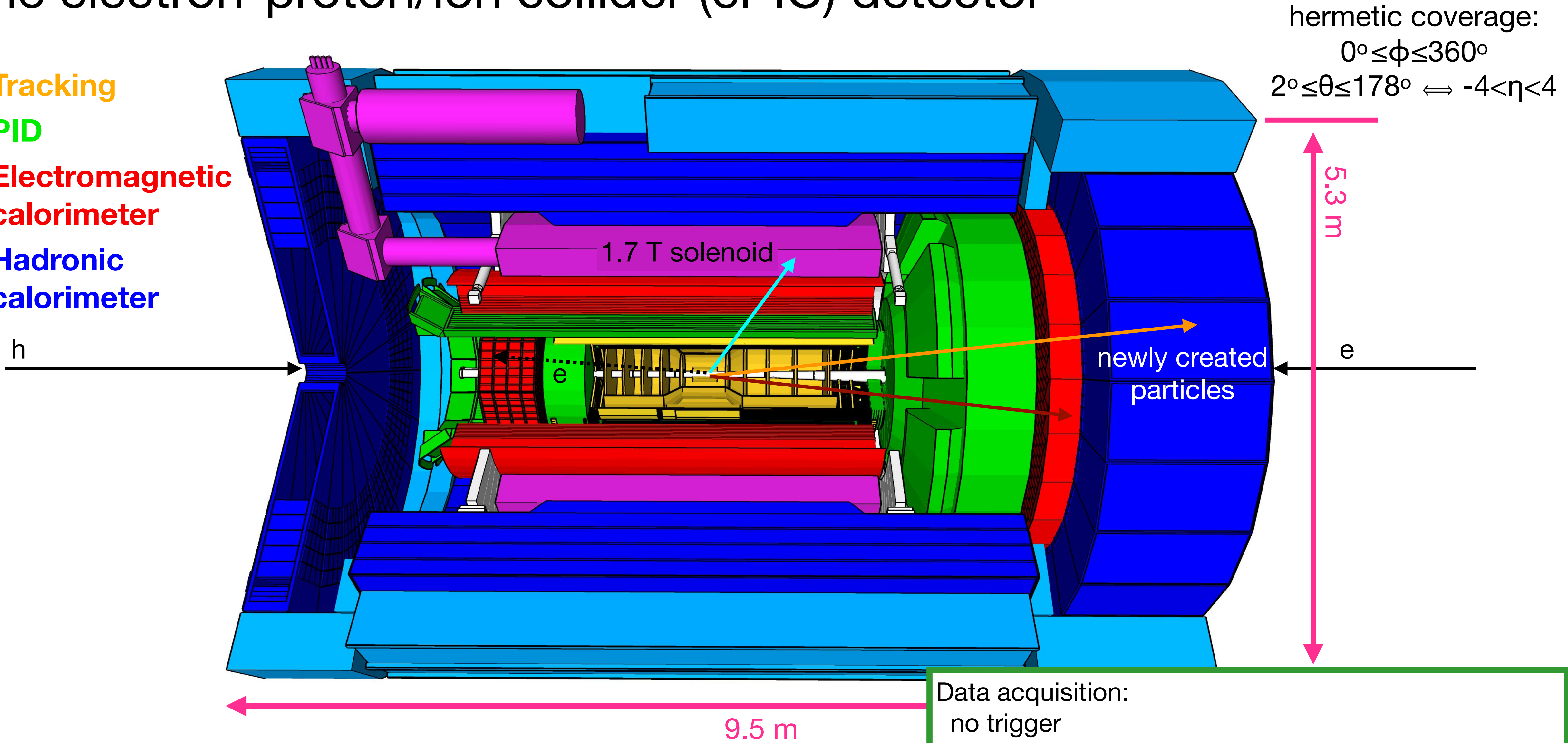
The electron-proton/ion collider (ePIC) detector

- Tracking
- PID
- Electromagnetic calorimeter
- Hadronic calorimeter



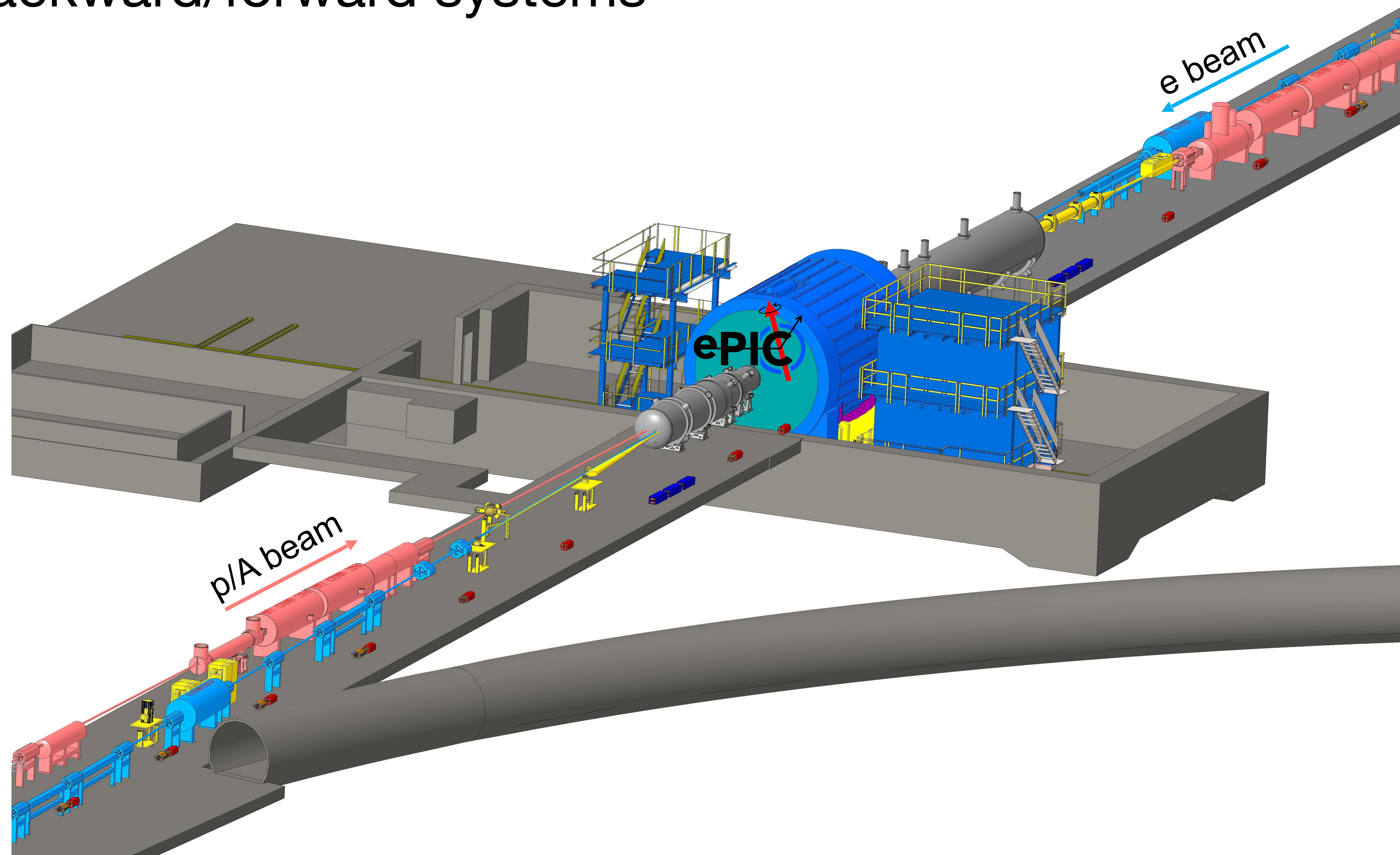
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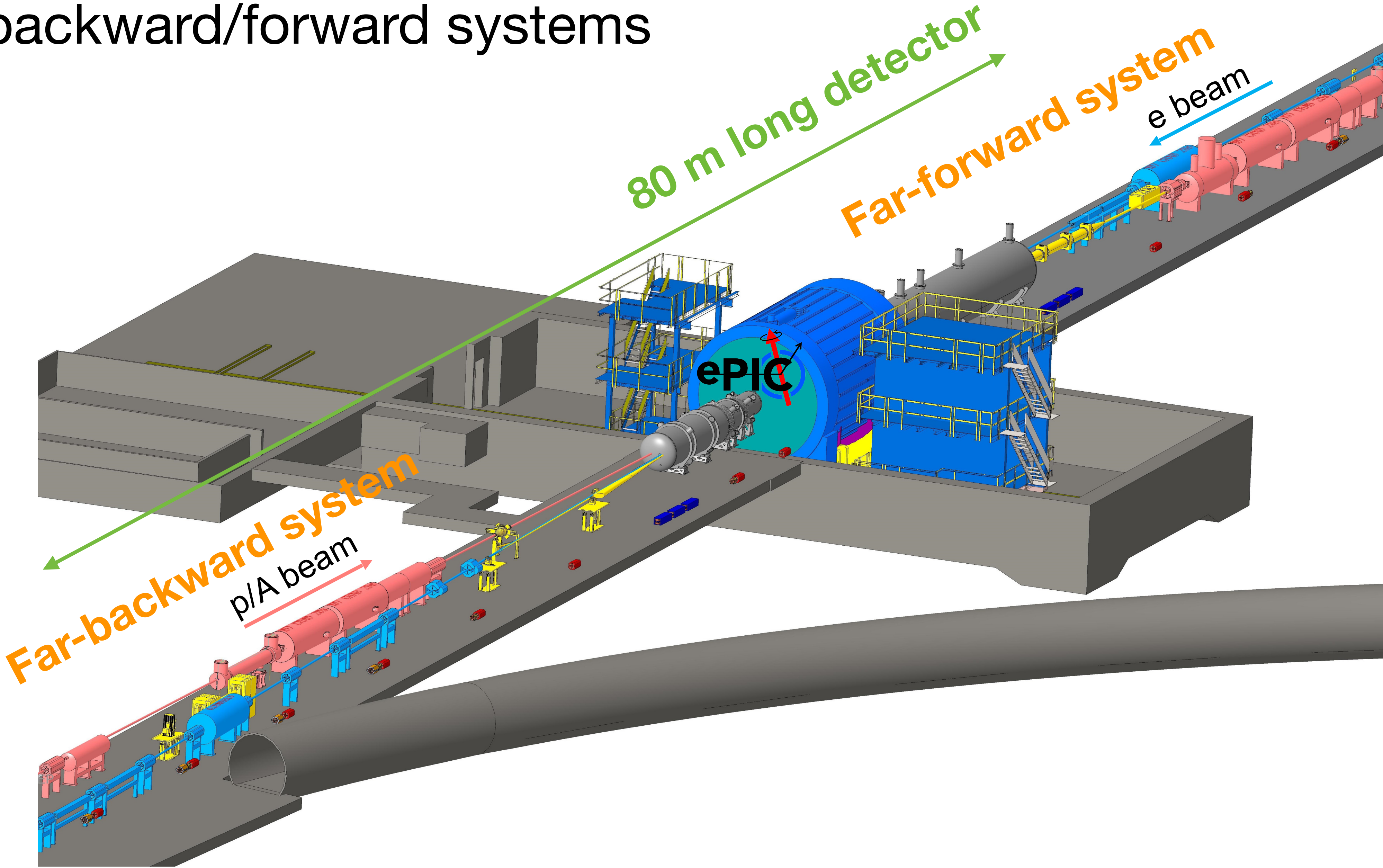


Data acquisition:
 no trigger
 all collision data is digitised
 with strong zero-suppression at front-end electronics

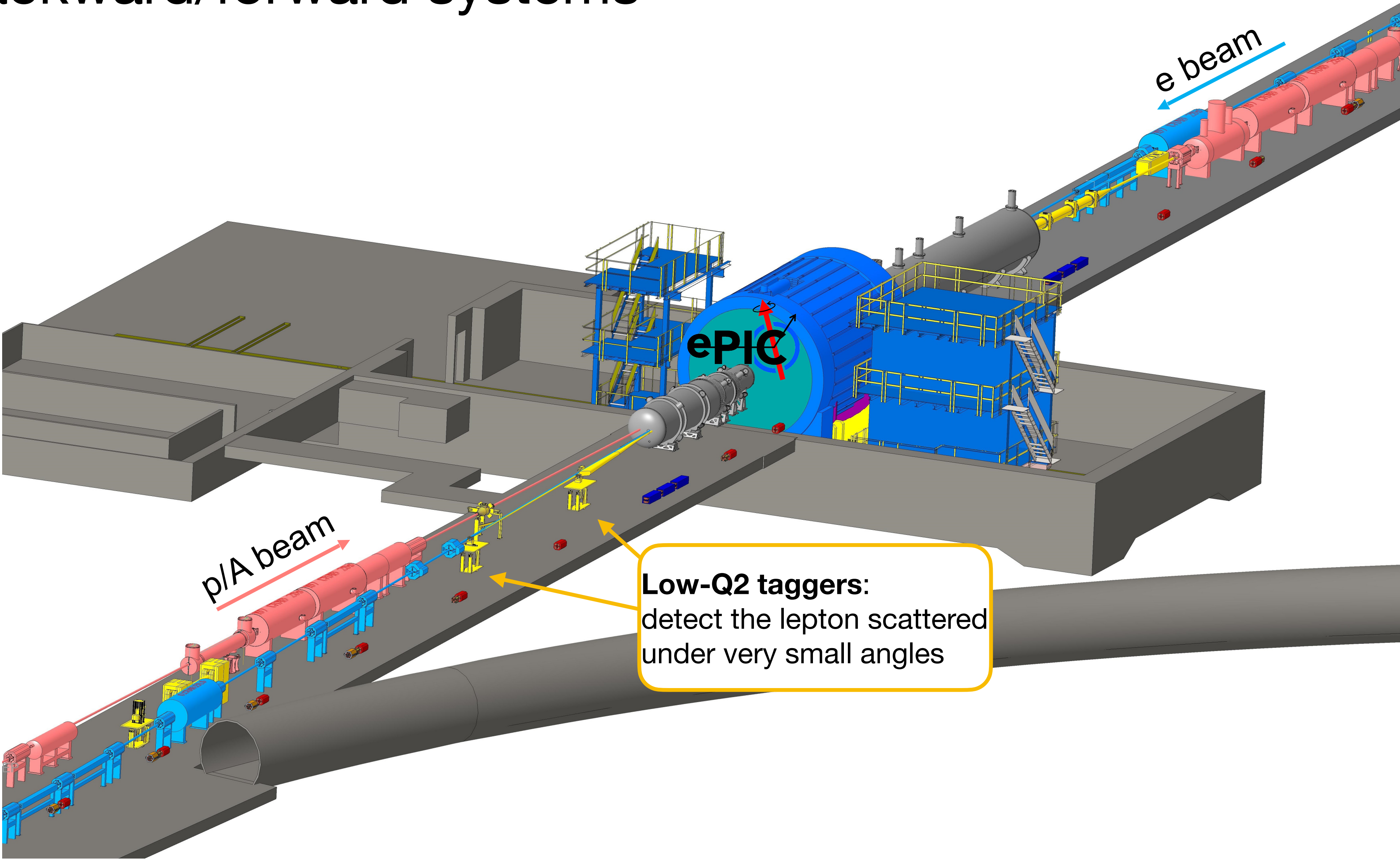
Far backward/forward systems



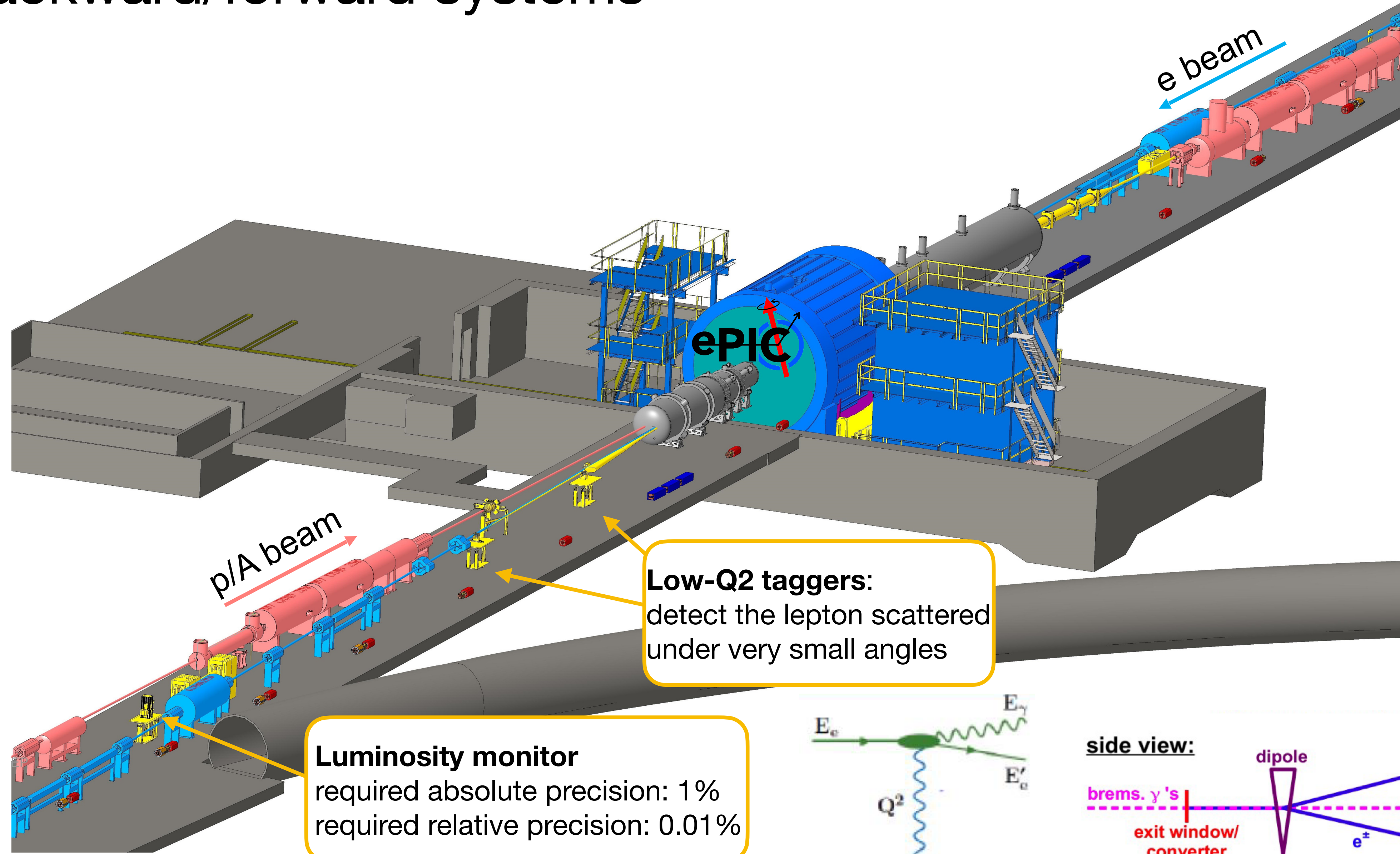
Far backward/forward systems



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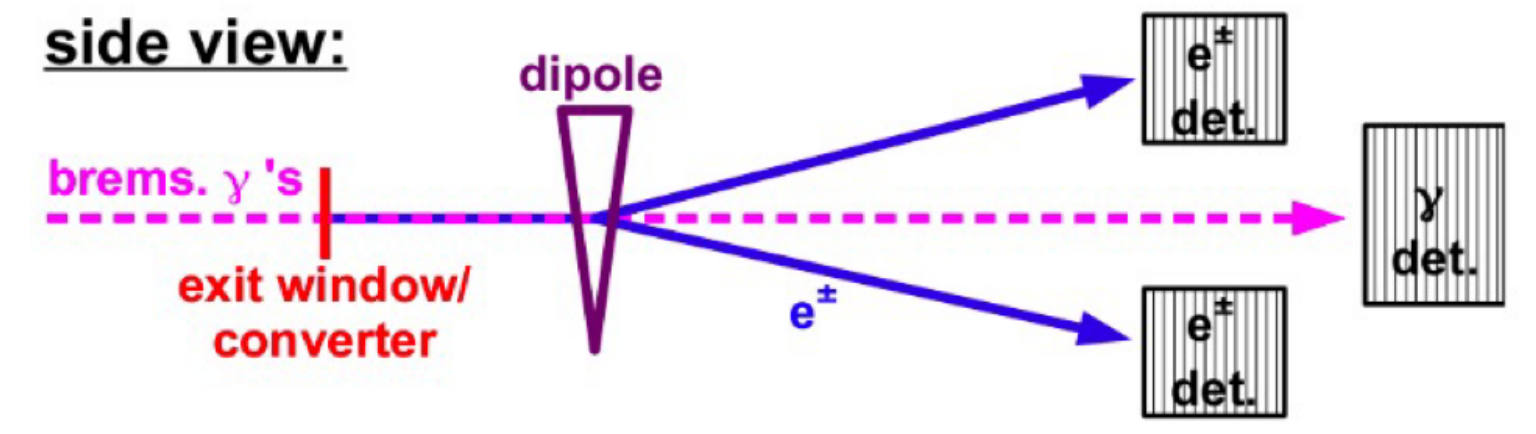
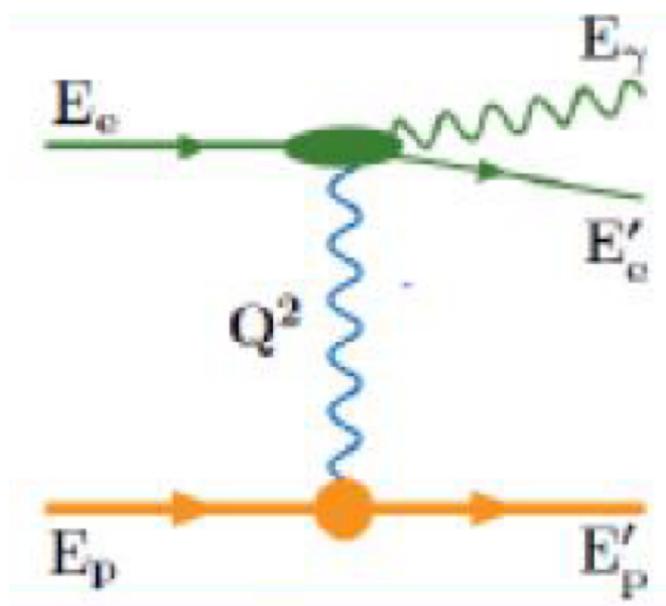


Far backward/forward systems

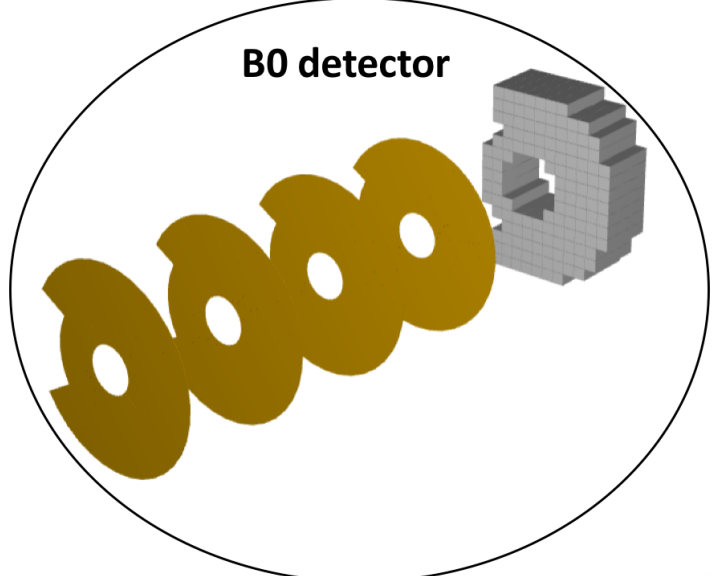


Low-Q2 taggers:
detect the lepton scattered under very small angles

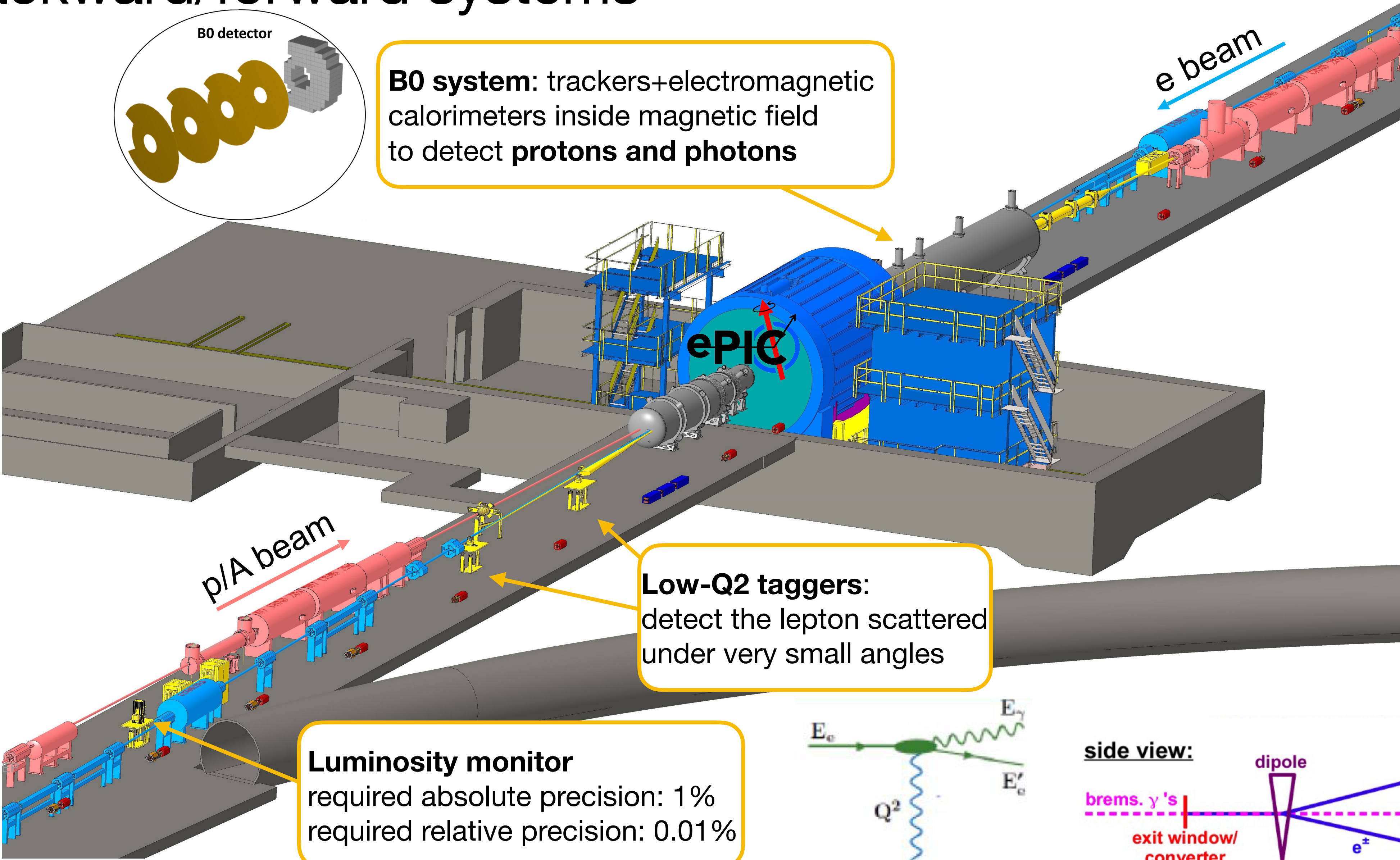
Luminosity monitor
required absolute precision: 1%
required relative precision: 0.01%



Far backward/forward systems

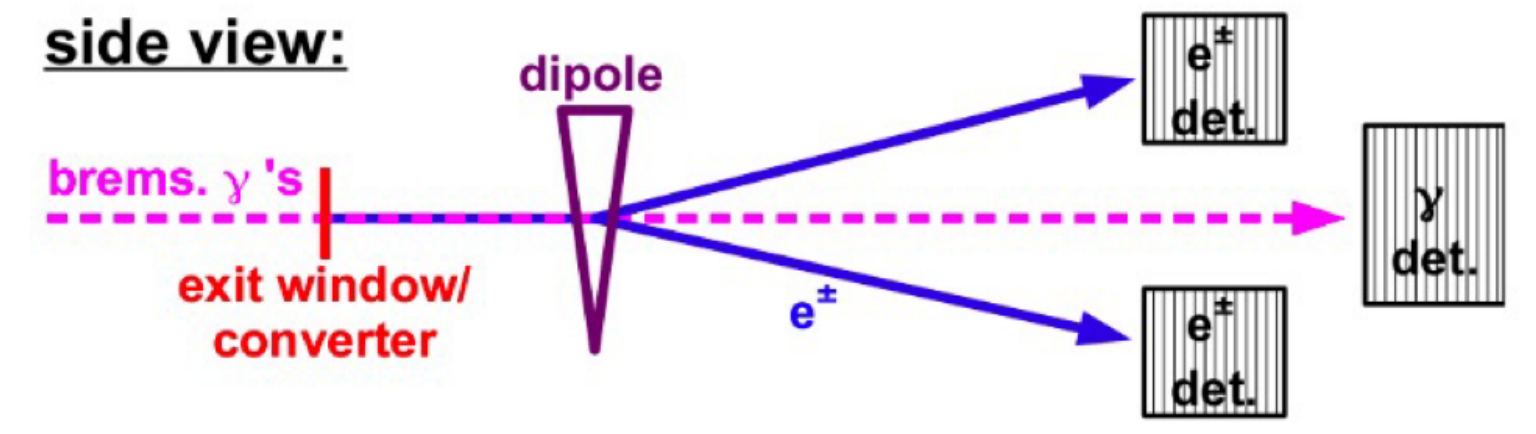
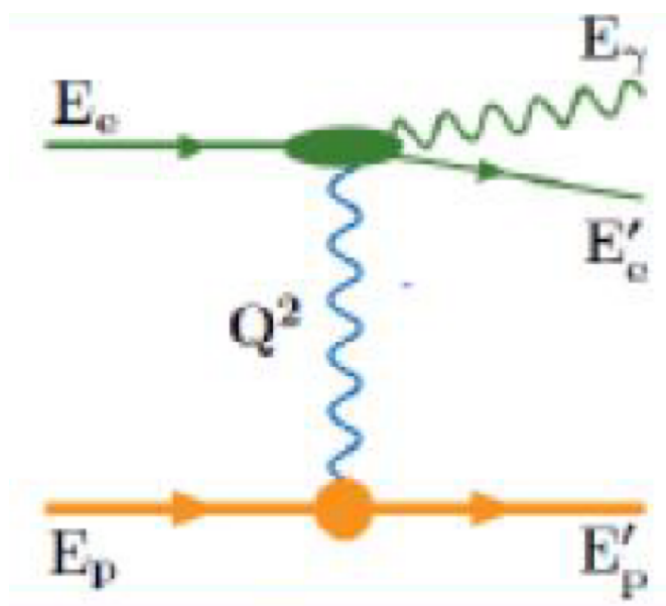


B0 system: trackers+electromagnetic calorimeters inside magnetic field to detect **protons and photons**

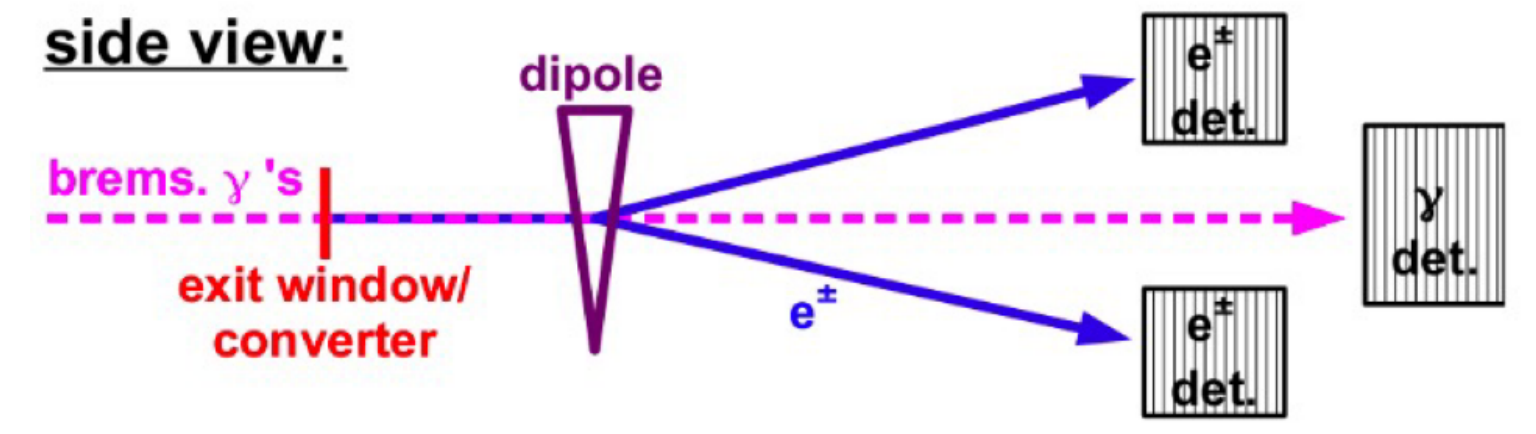
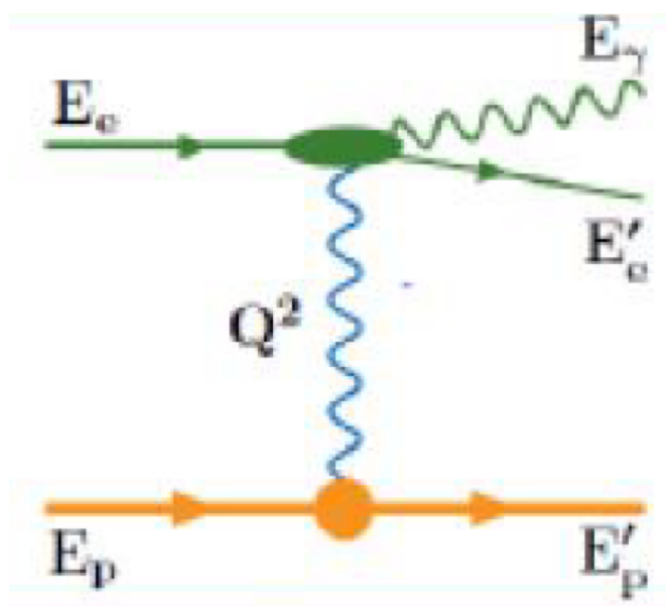
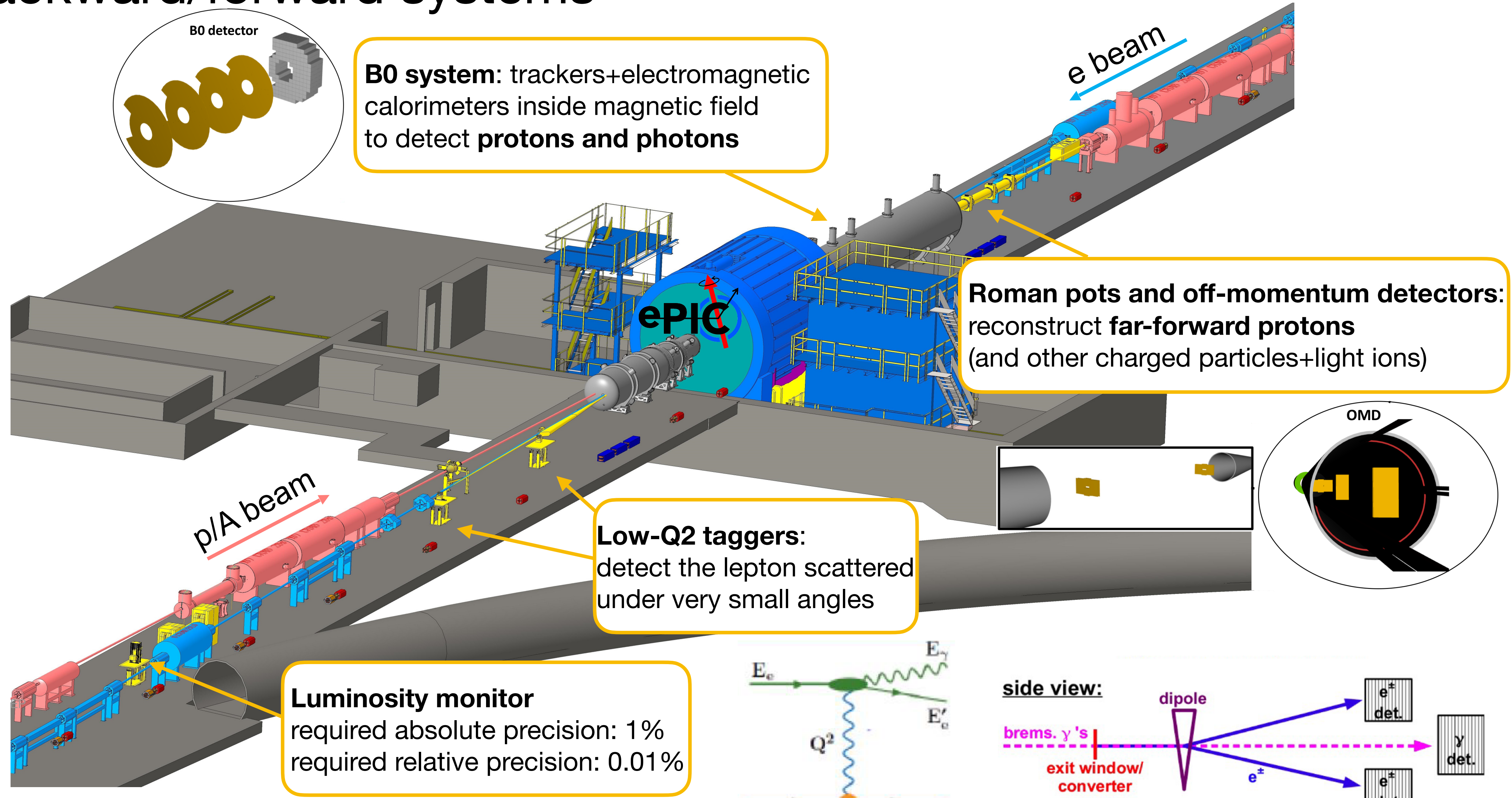


Low-Q2 taggers: detect the lepton scattered under very small angles

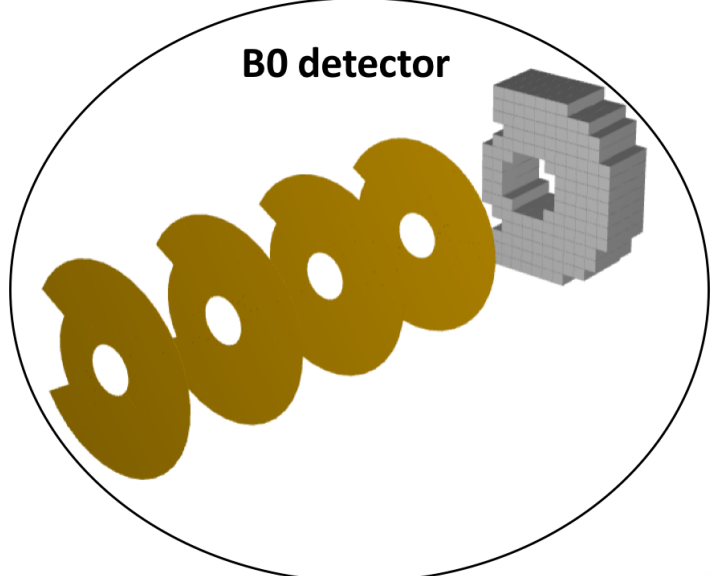
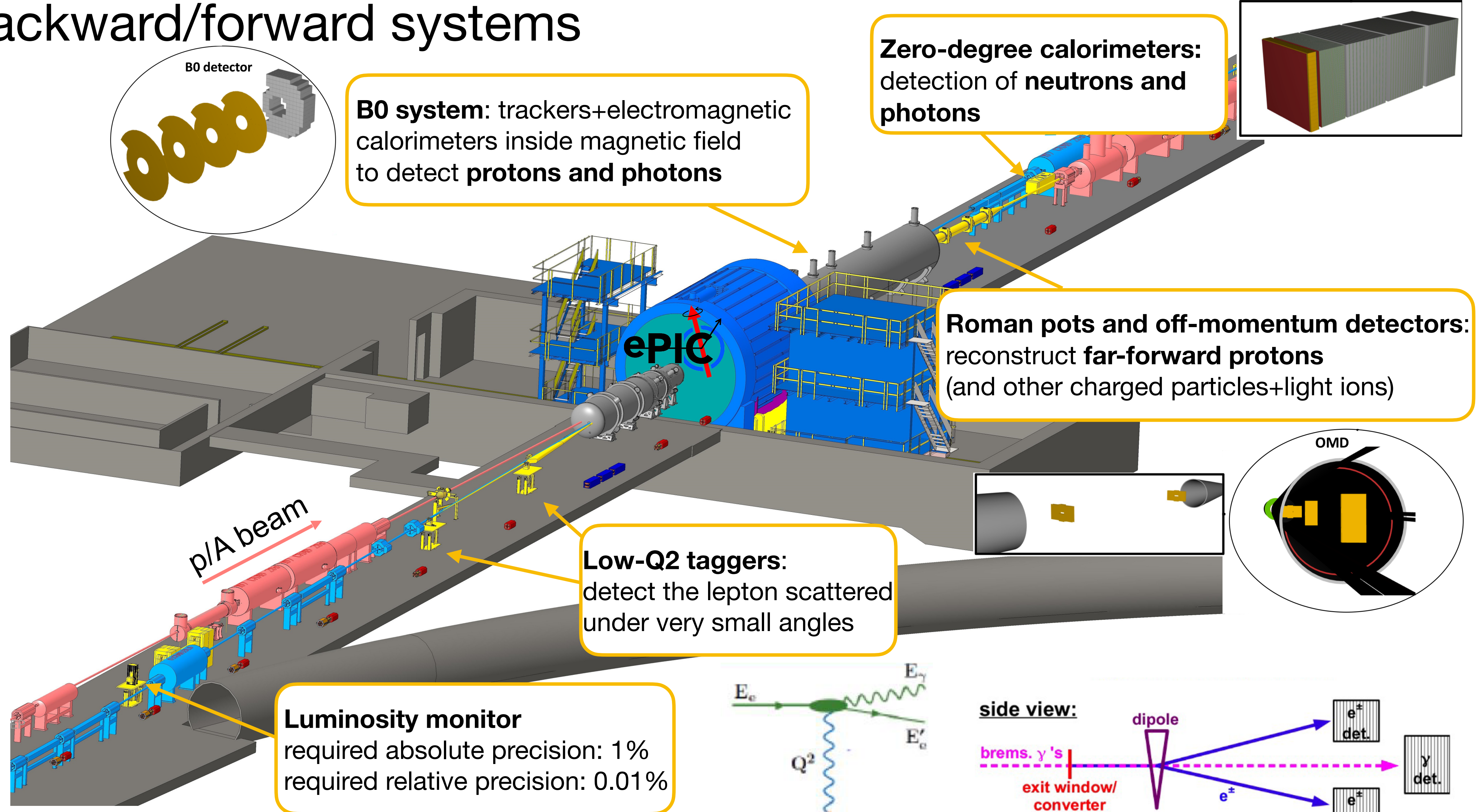
Luminosity monitor
 required absolute precision: 1%
 required relative precision: 0.01%



Far backward/forward systems

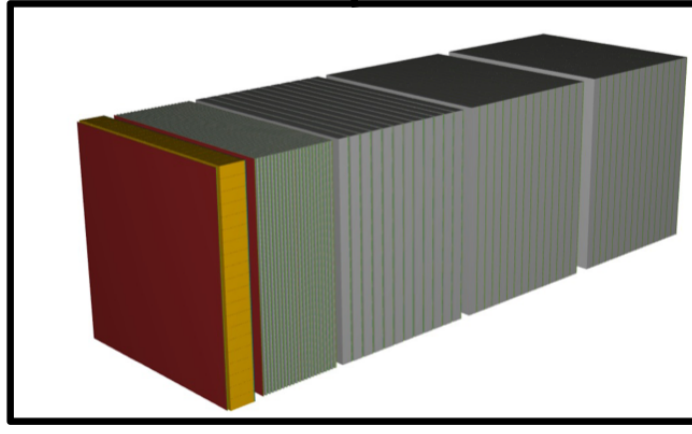


Far backward/forward systems



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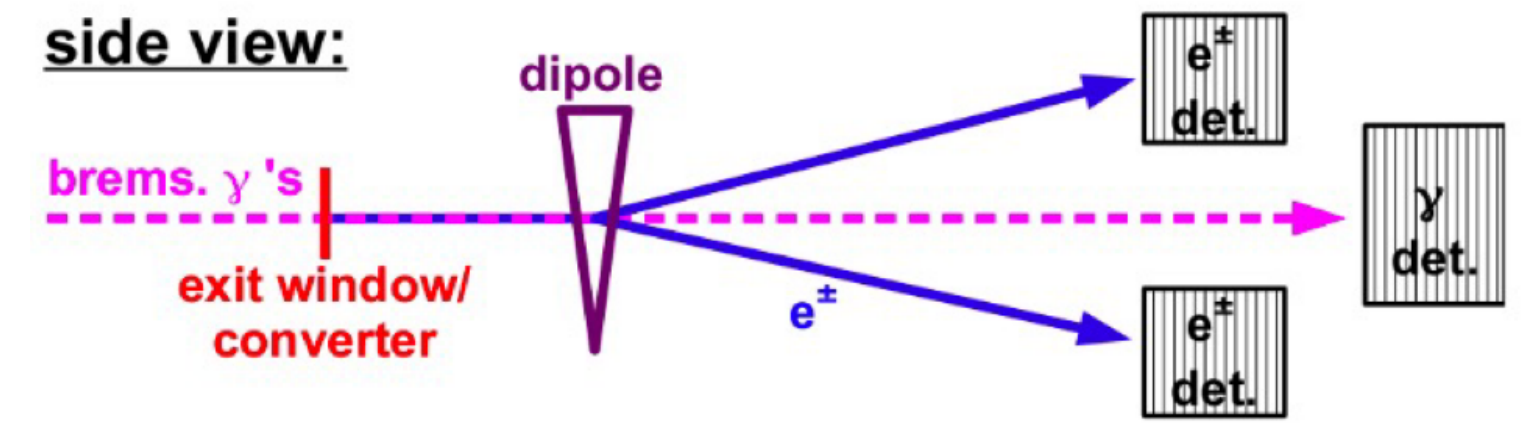
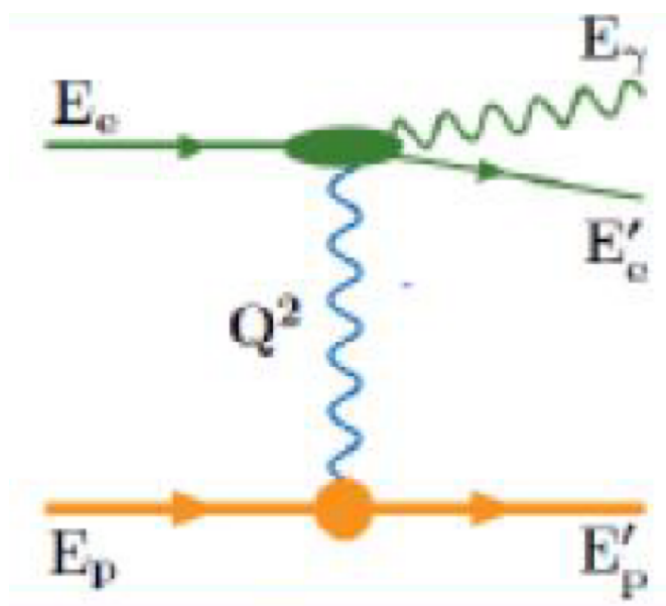
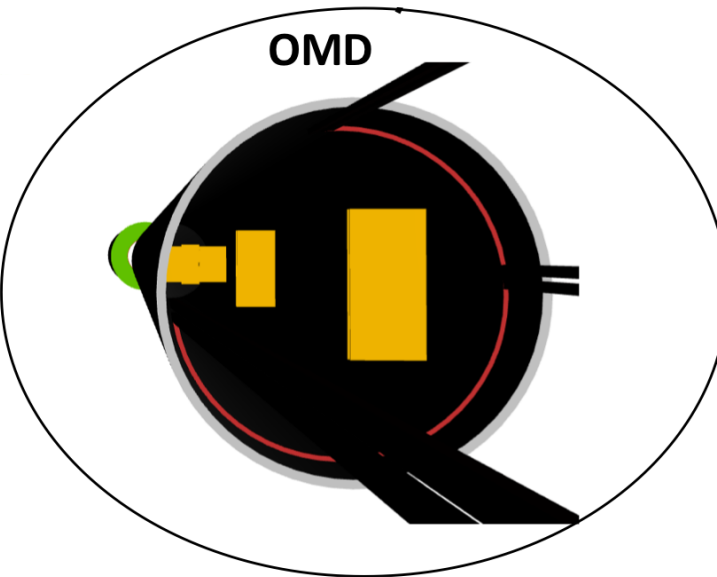
Zero-degree calorimeters: detection of **neutrons and photons**



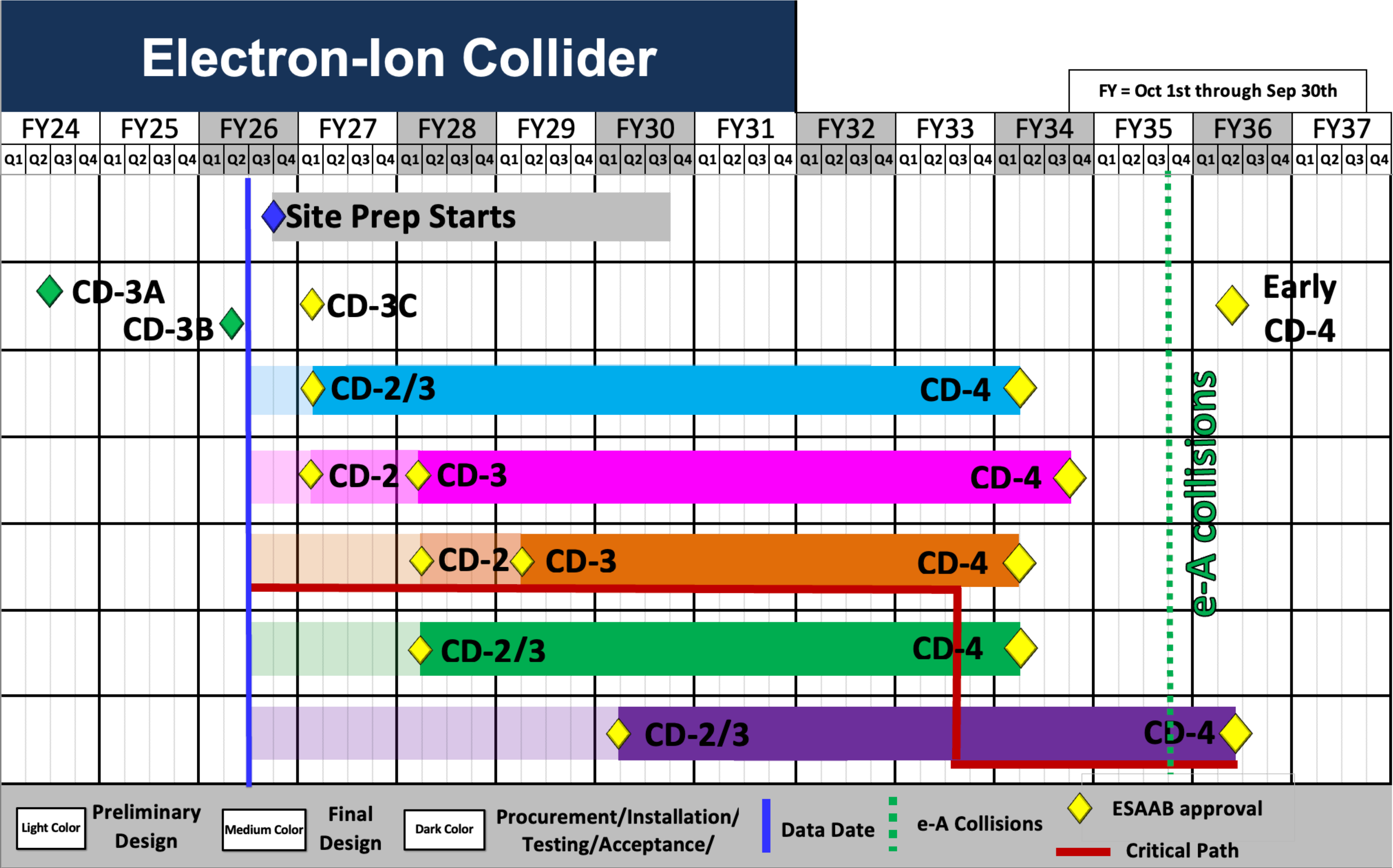
Roman pots and off-momentum detectors: reconstruct **far-forward protons** (and other charged particles+light ions)

Low-Q2 taggers: detect the lepton scattered under very small angles

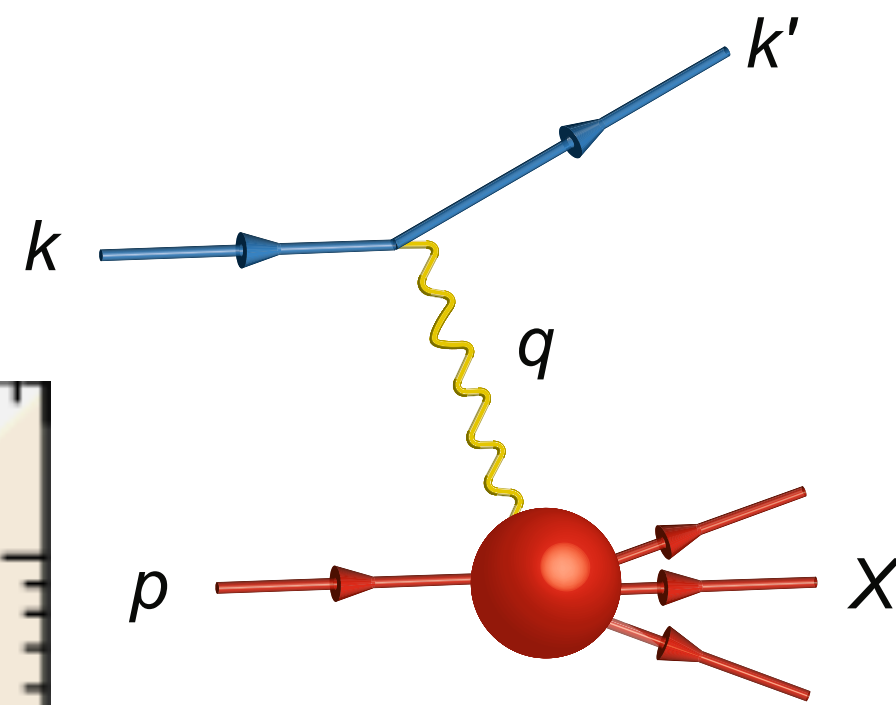
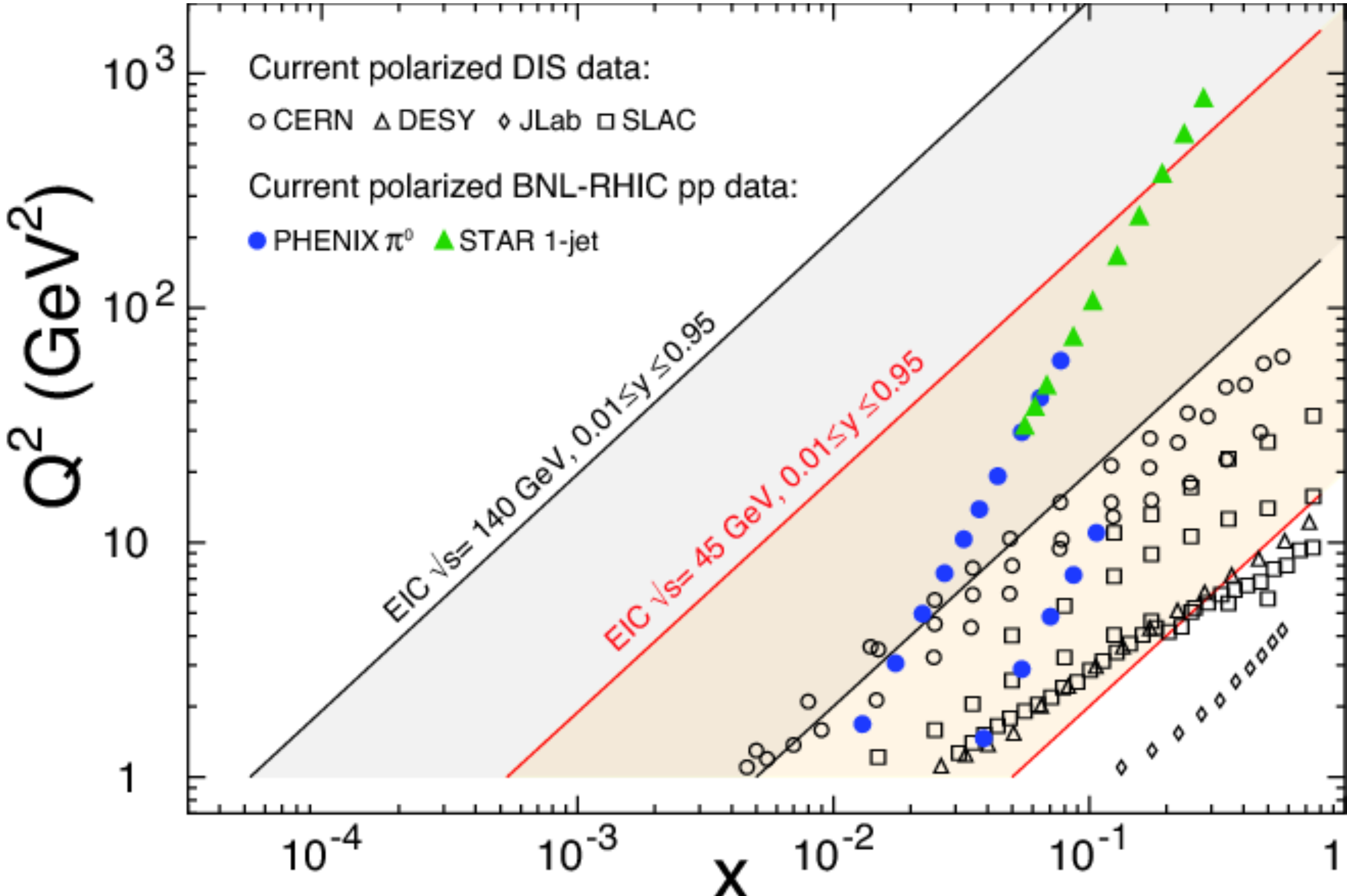
Luminosity monitor
 required absolute precision: 1%
 required relative precision: 0.01%



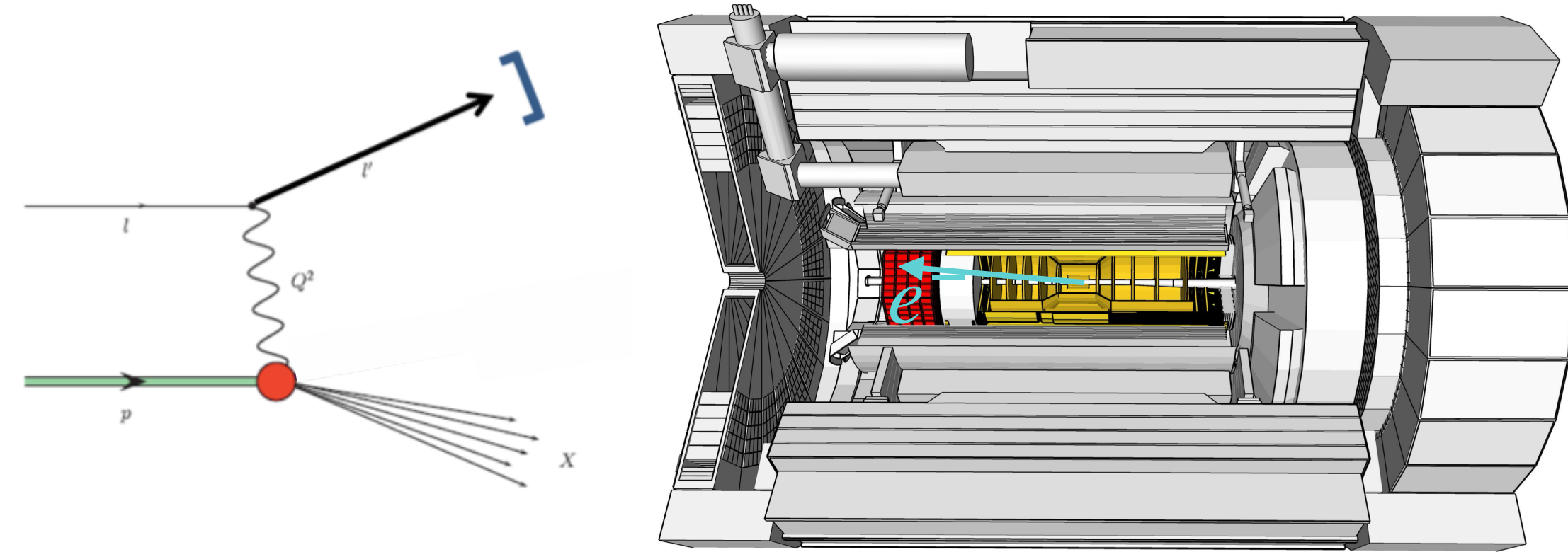
Timeline



Kinematic coverage at the EIC



Gluon helicity distribution of the proton

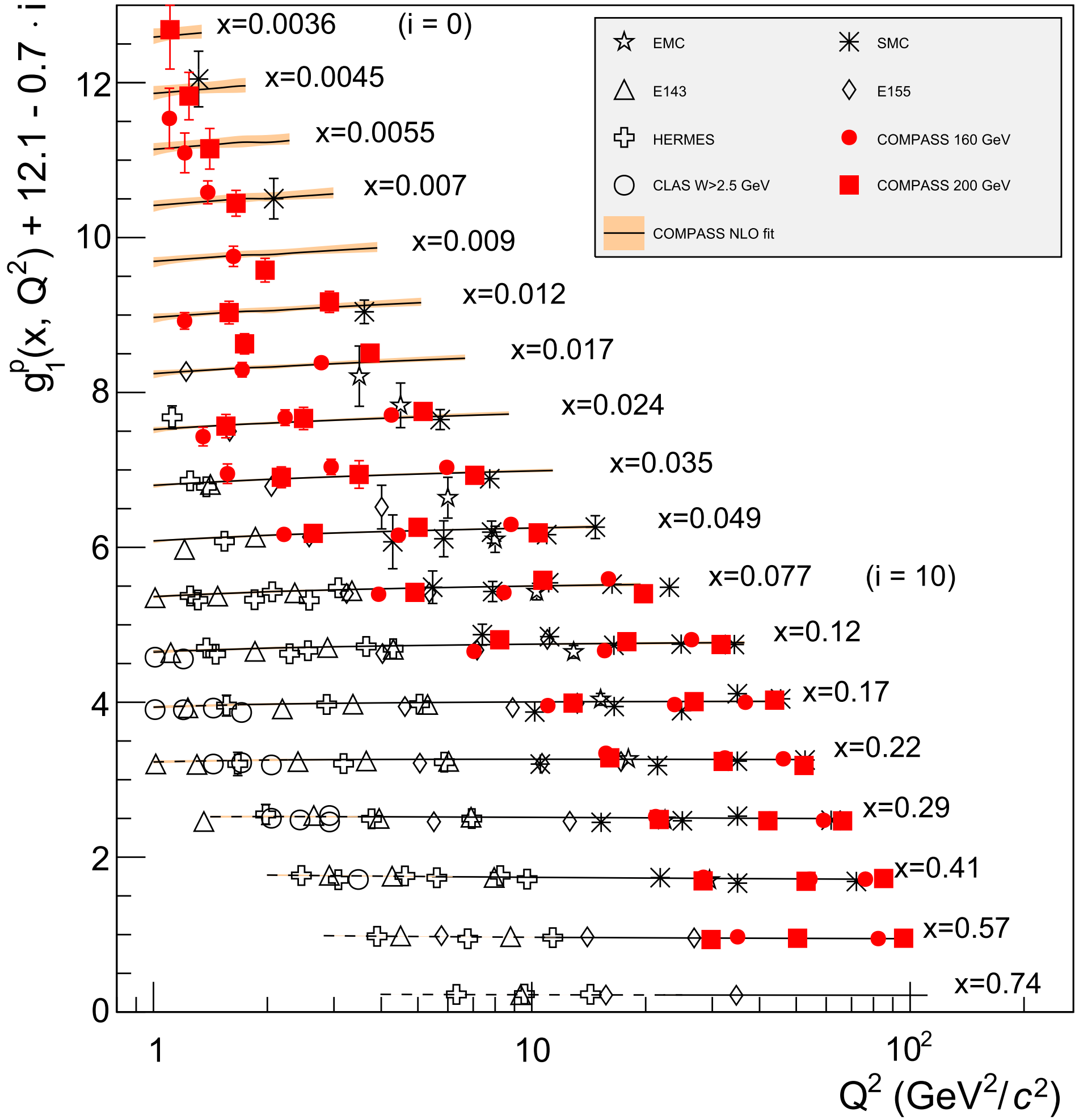


- High e^- purity needed:
suppression of π contamination via EMCAL
- Precise track reconstruction needed:
trackers and EMCAL

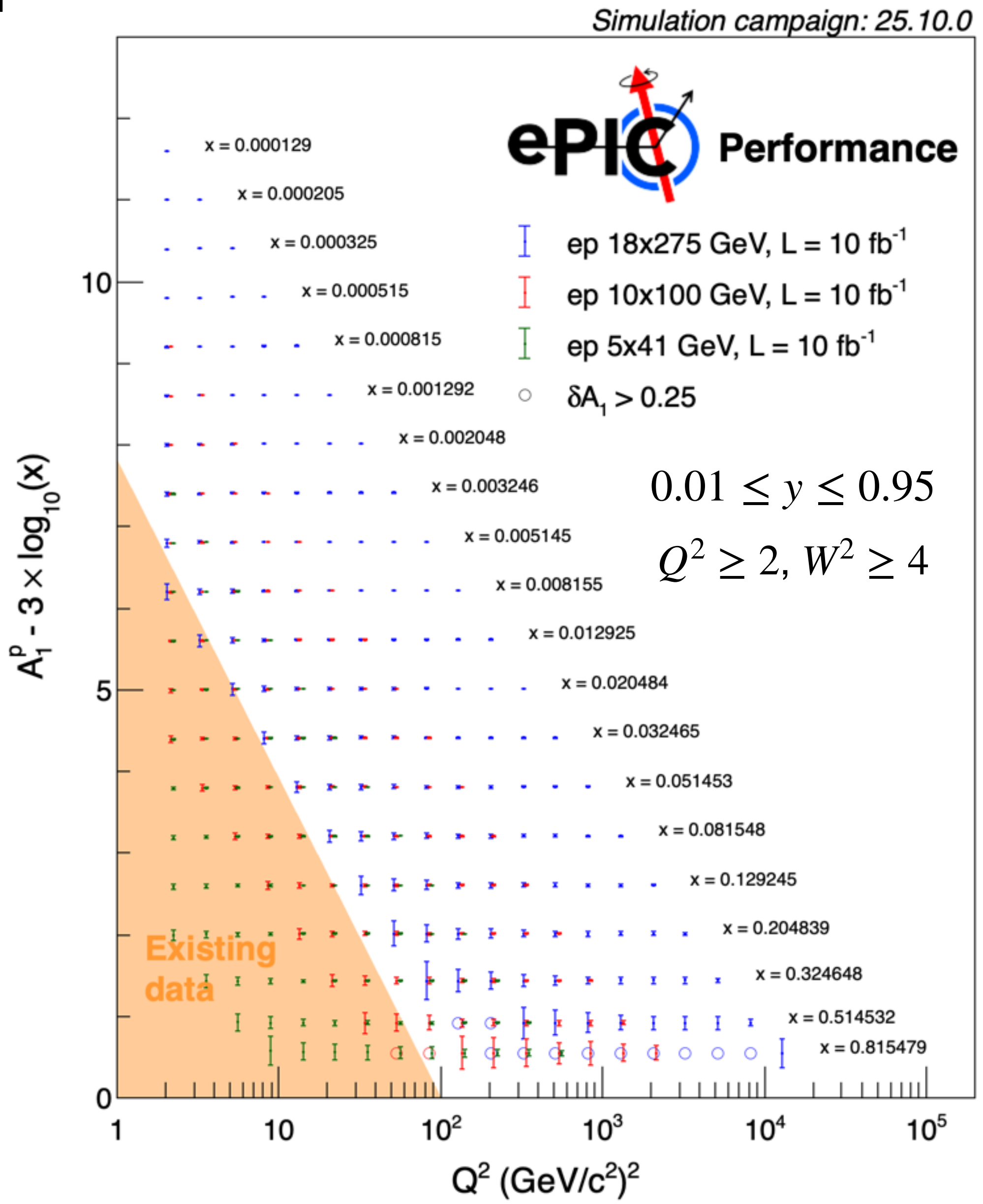
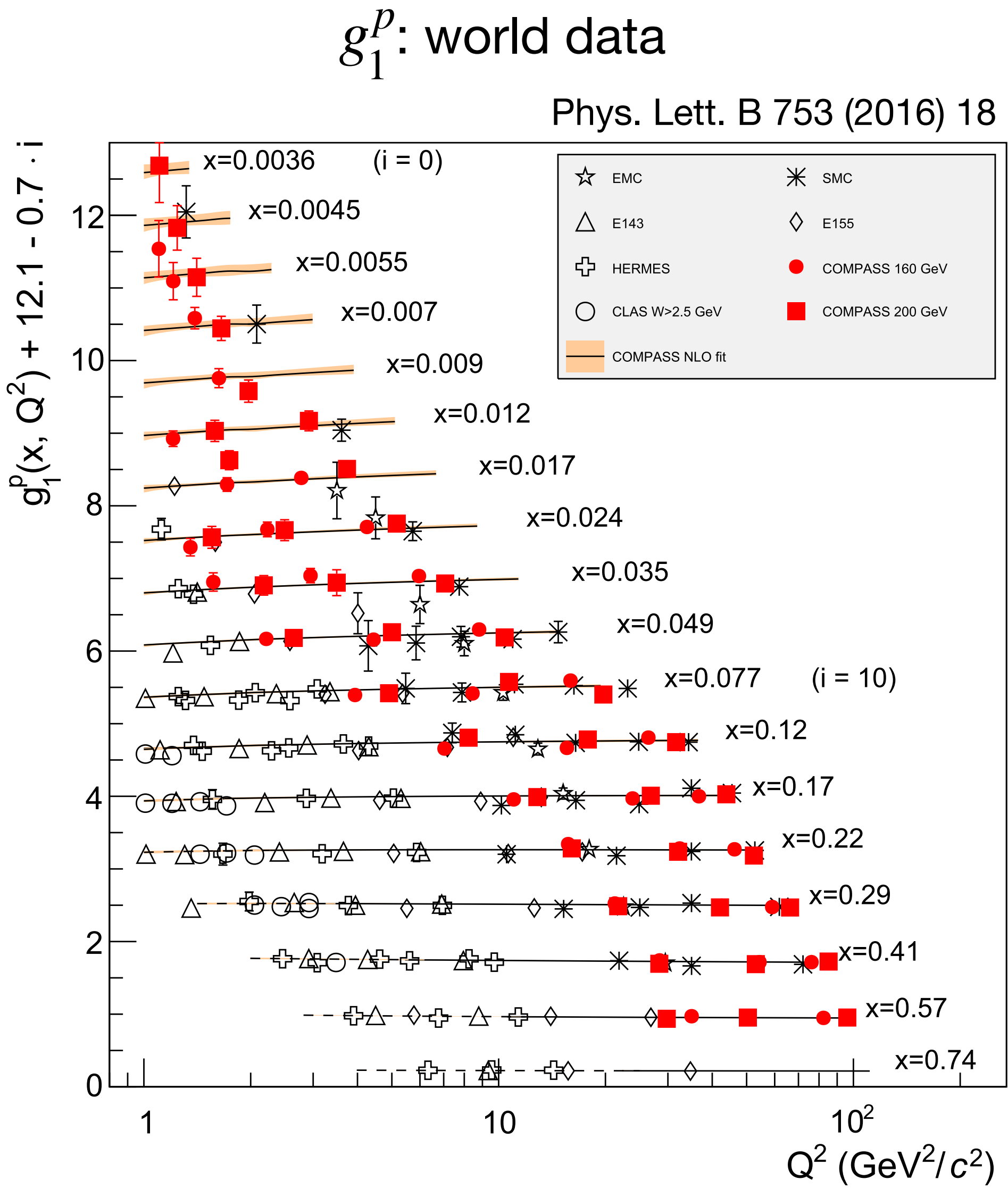
Glucan helicity distribution of the proton

g_1^p : world data

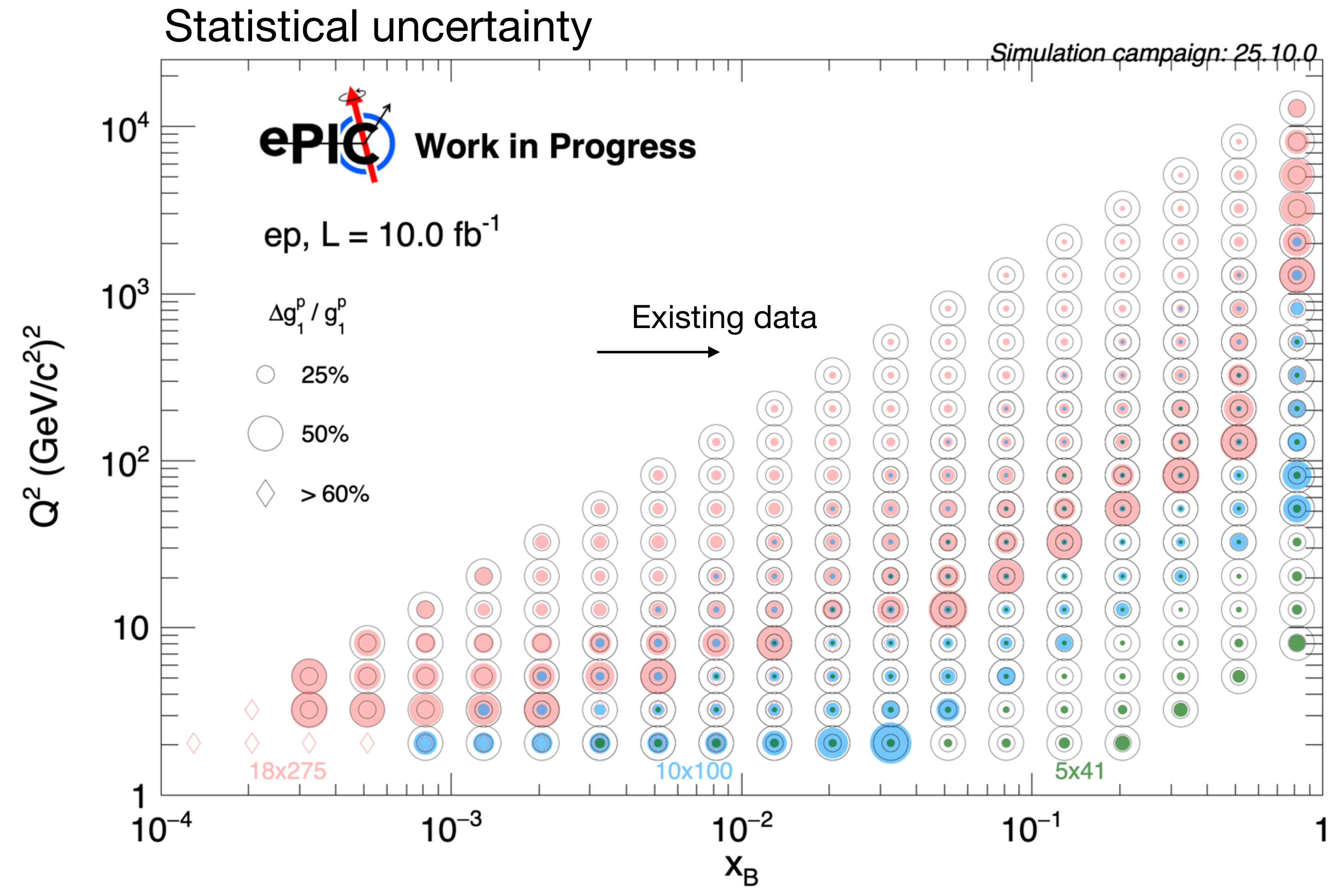
Phys. Lett. B 753 (2016) 18



Gluon helicity distribution of the proton



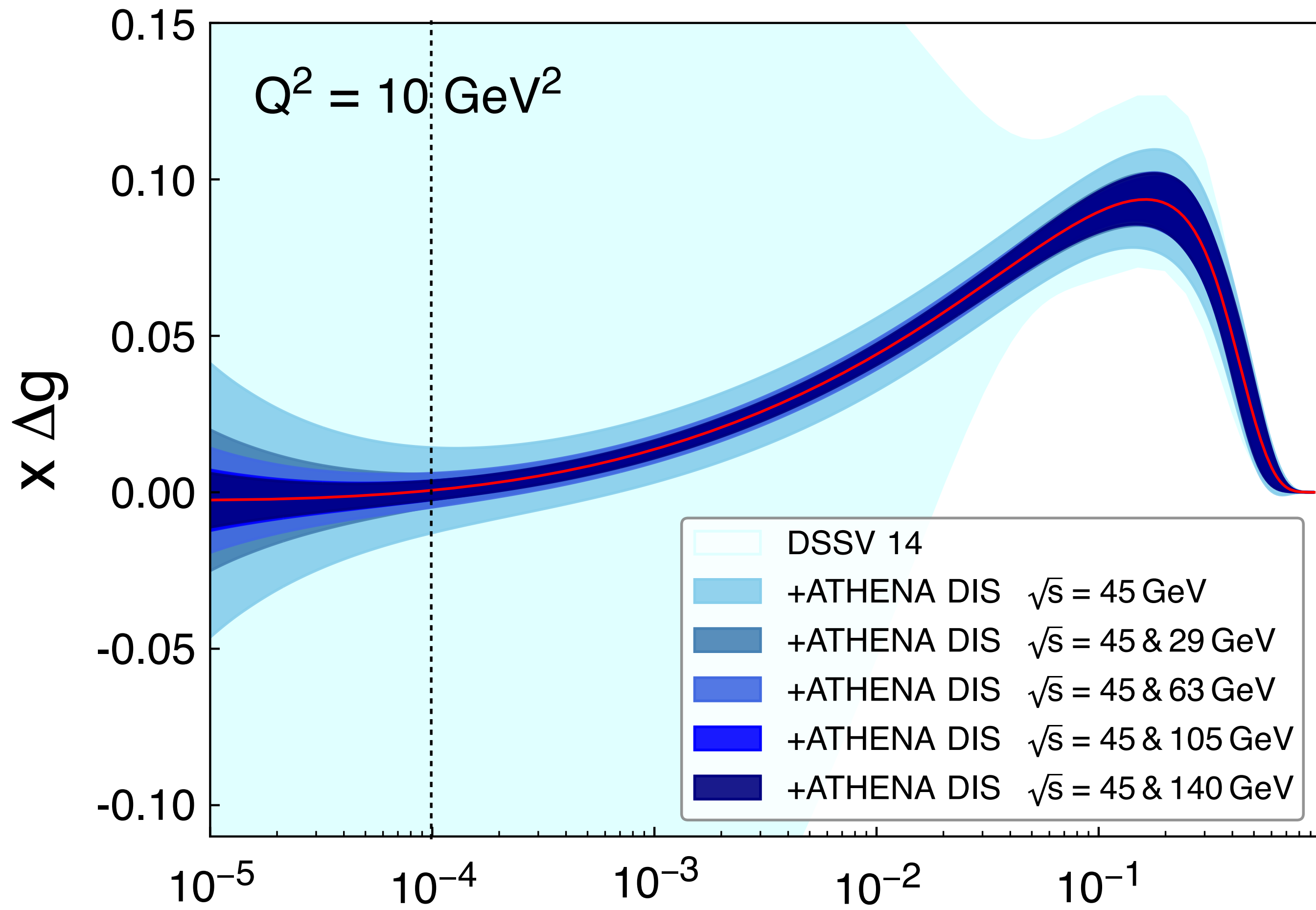
Glauon helicity distribution of the proton



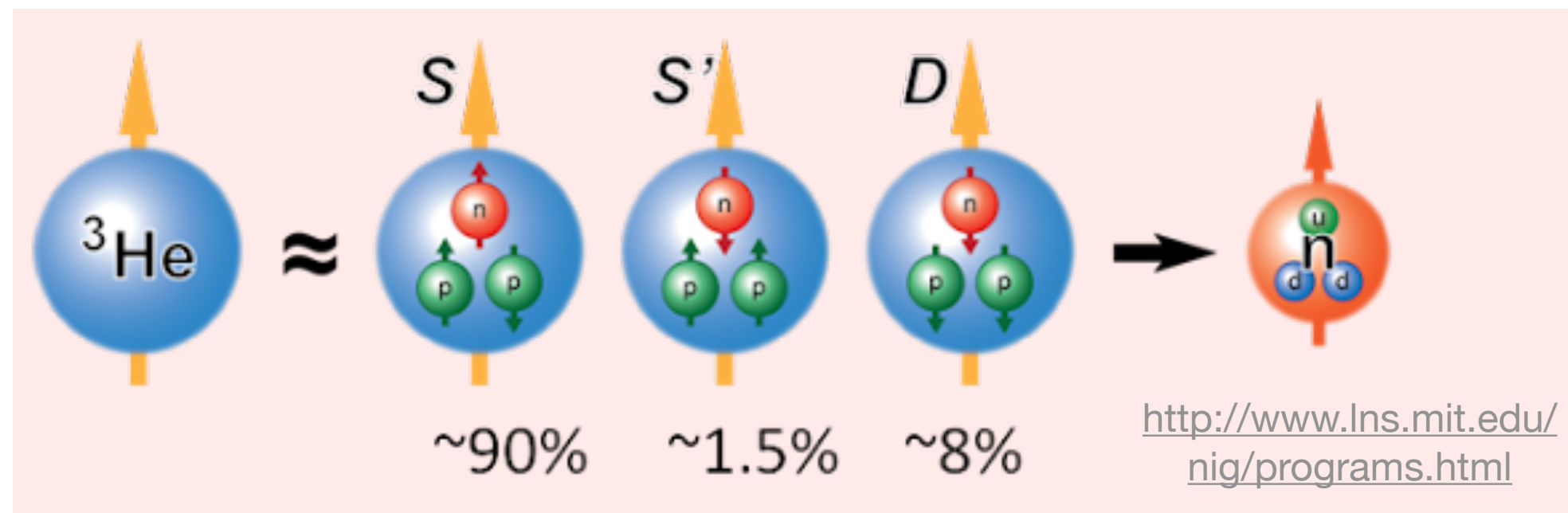
Gluon helicity distribution of the proton

Expected impact on Δg

ATHENA, JINST 17 (2022) 10, P10019



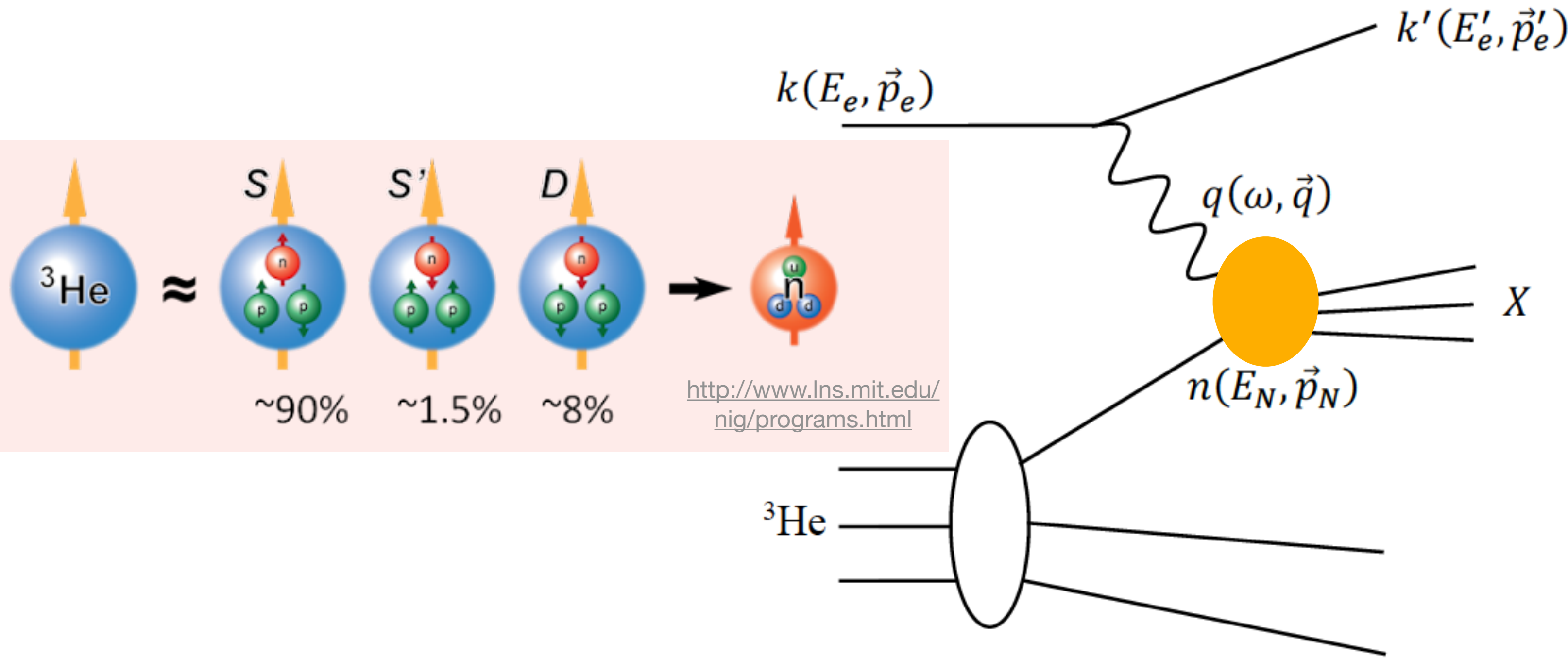
Gluon helicity distribution of the neutron



Gluon helicity distribution of the neutron

Access to spin structure of the neutron

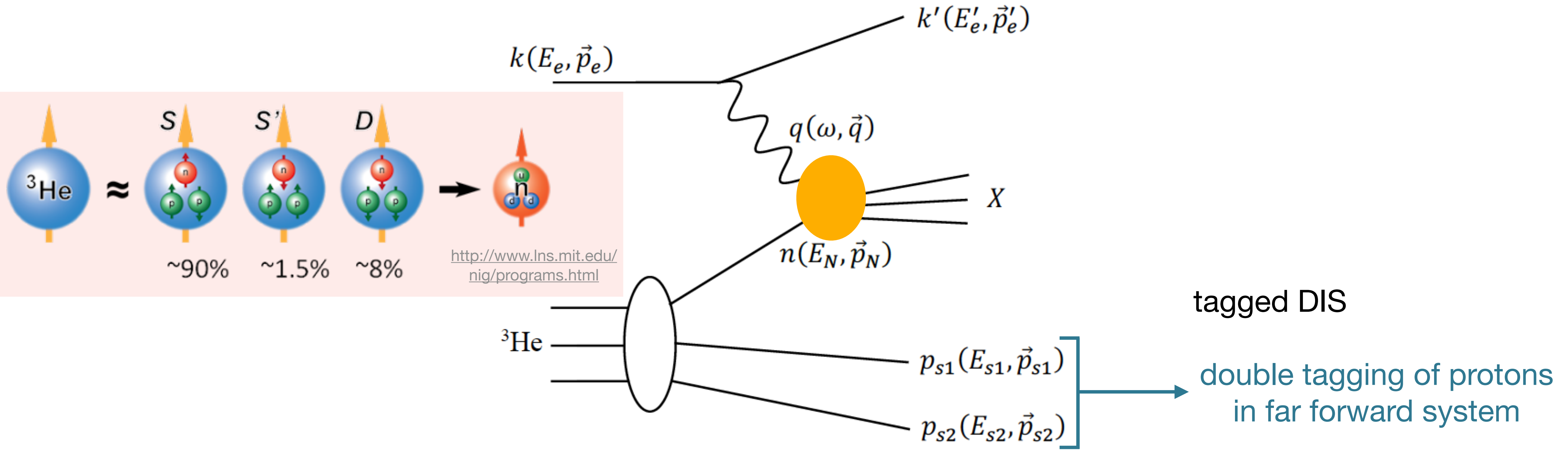
inclusive DIS



Gluon helicity distribution of the neutron

Access to spin structure of the neutron

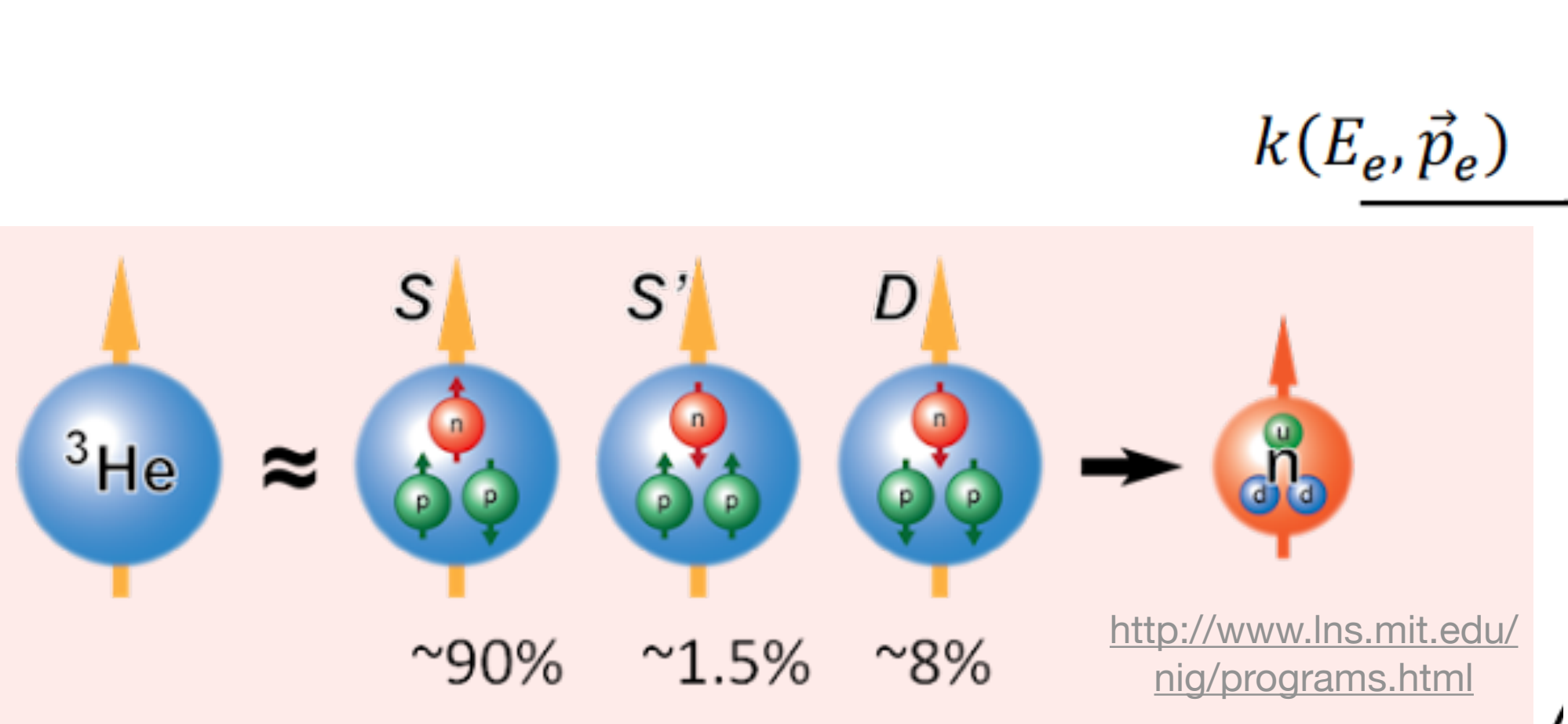
inclusive DIS



Gluon helicity distribution of the neutron

Access to spin structure of the neutron

inclusive DIS

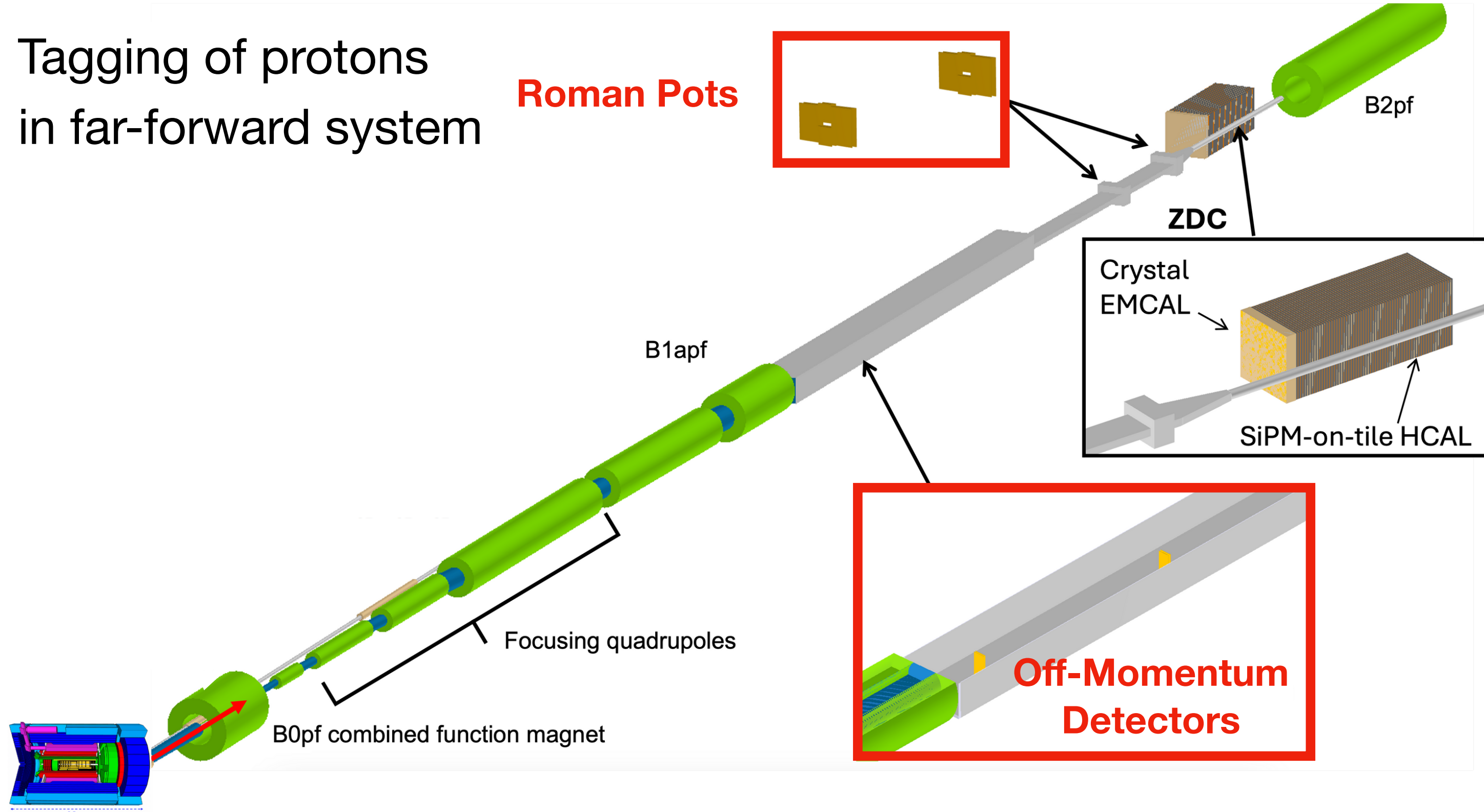


$k(E_e, \vec{p}_e)$ \rightarrow $k'(E'_e, \vec{p}'_e)$

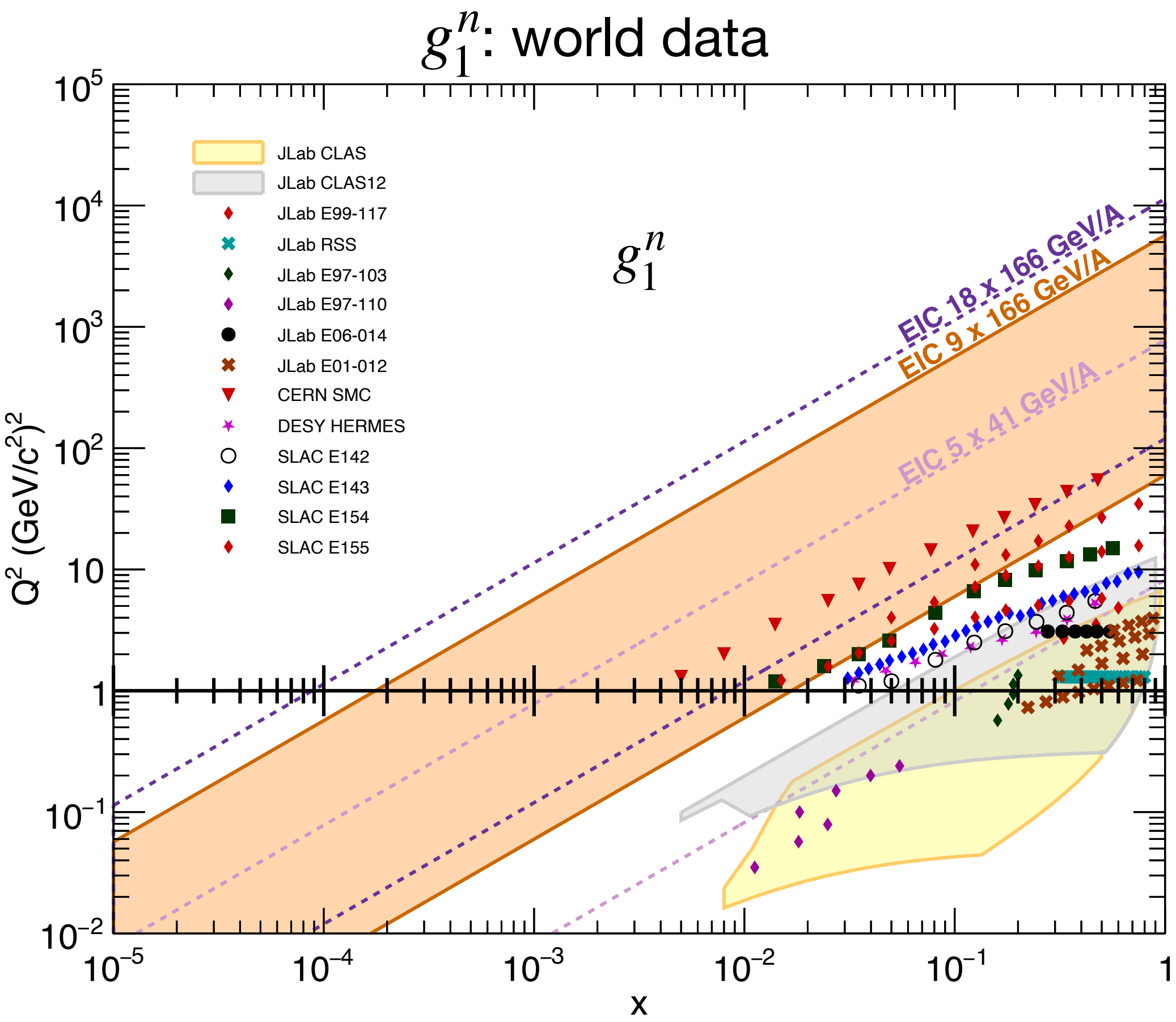
$a(\omega, \vec{a})$

Tagging of protons in far-forward system

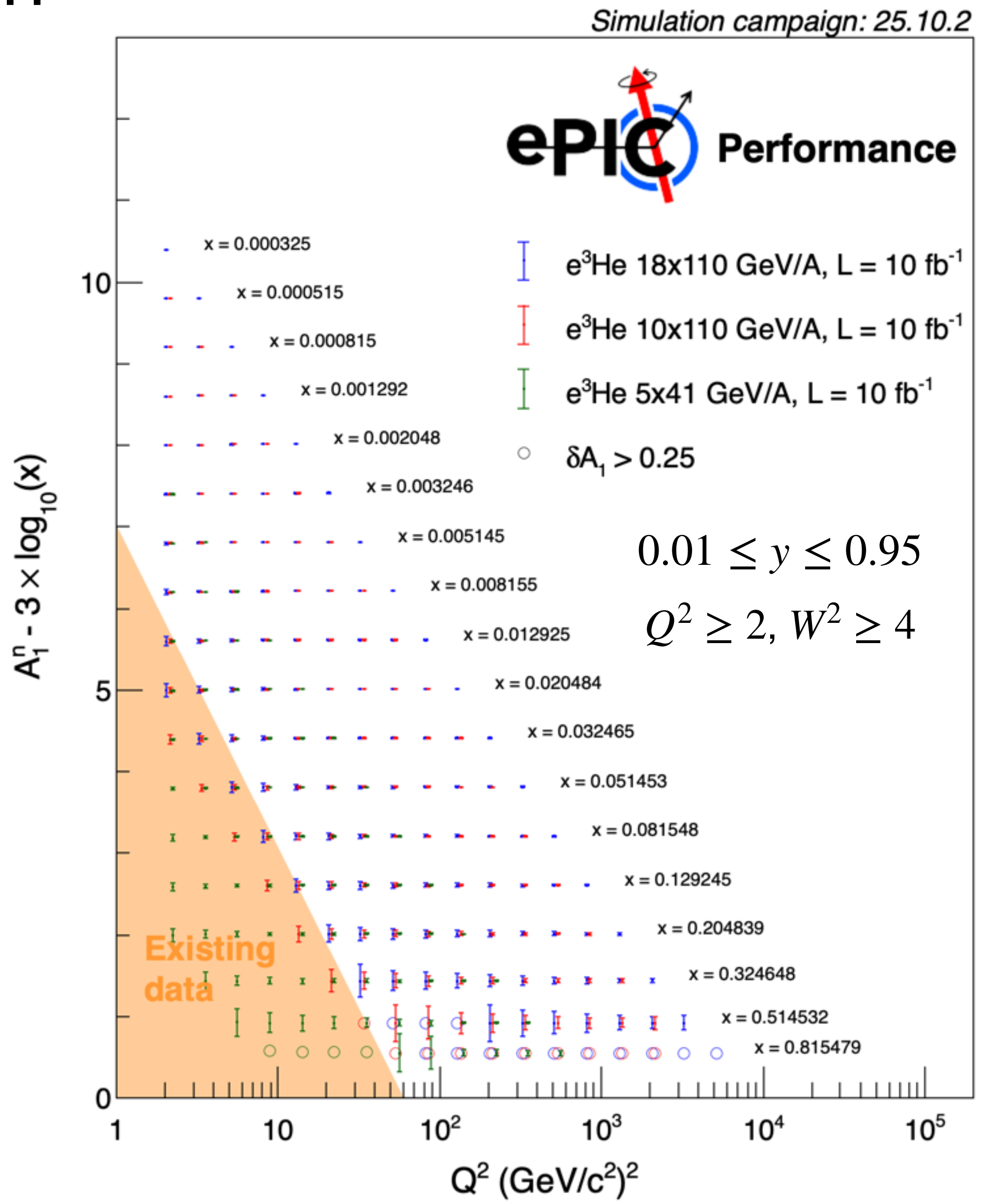
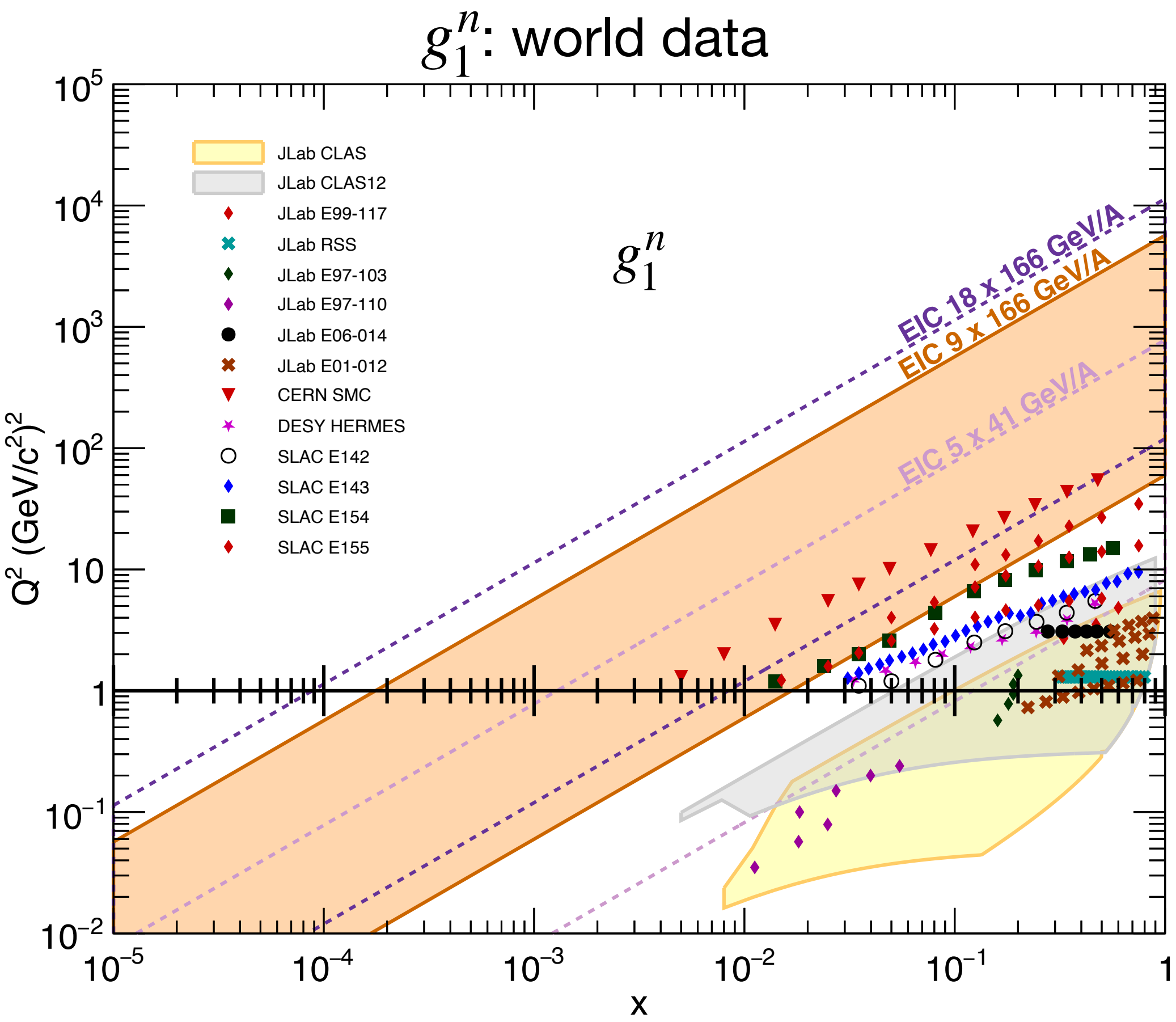
^3He



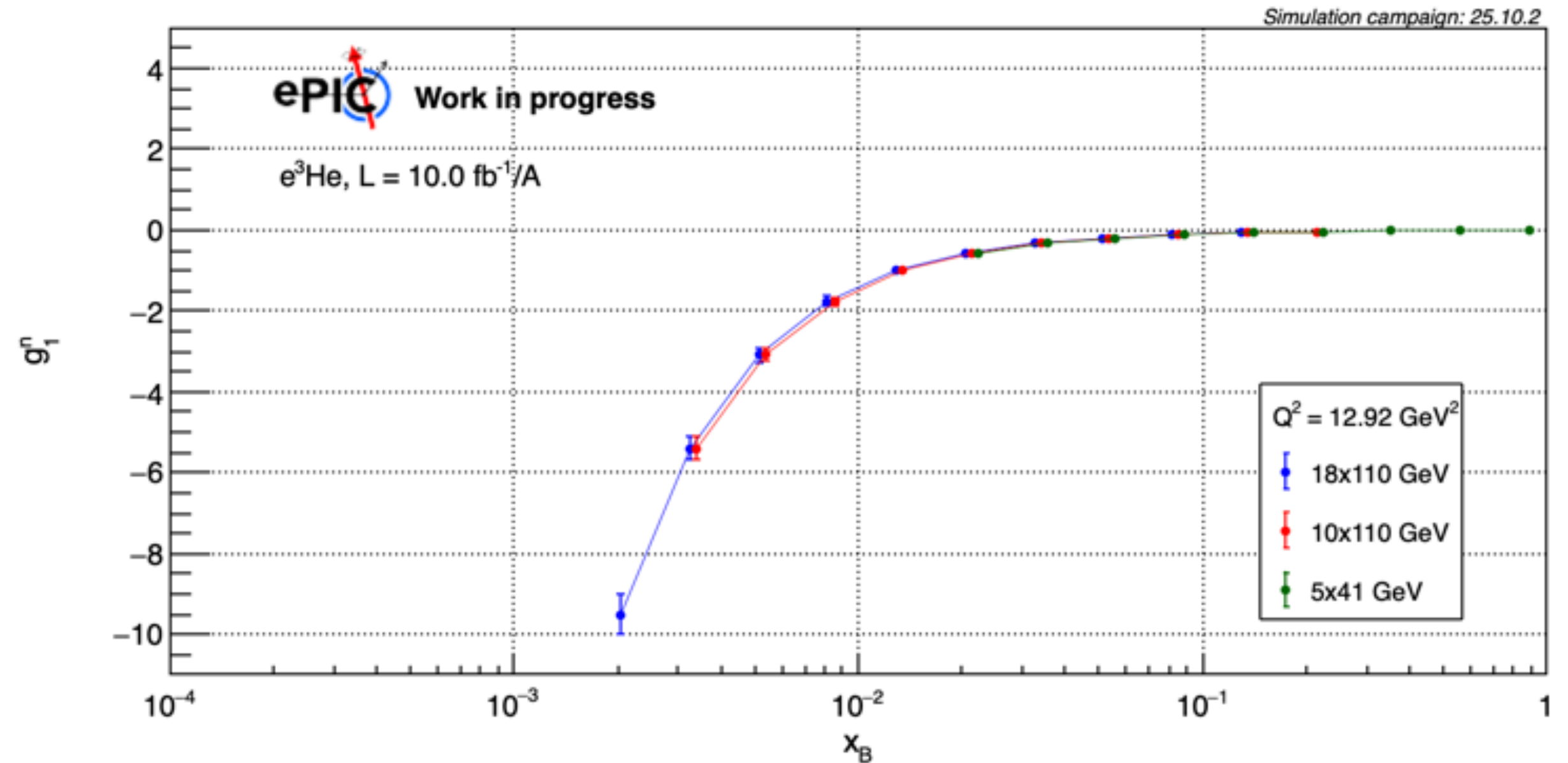
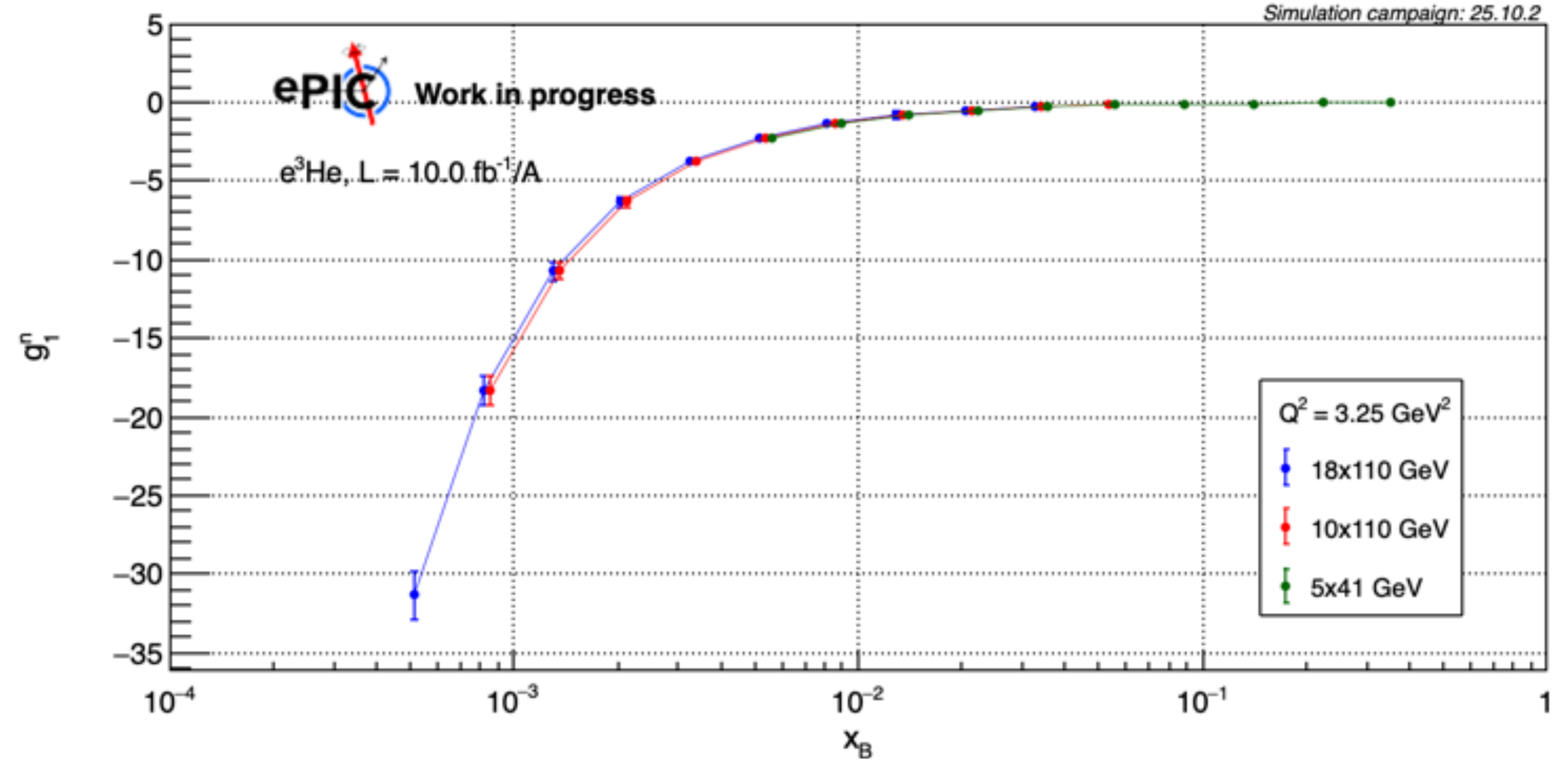
Gluon helicity distribution of the neutron

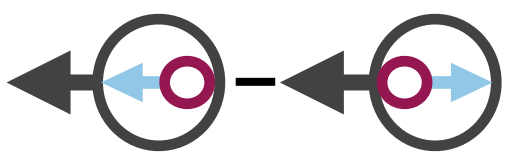


Gluon helicity distribution of the neutron

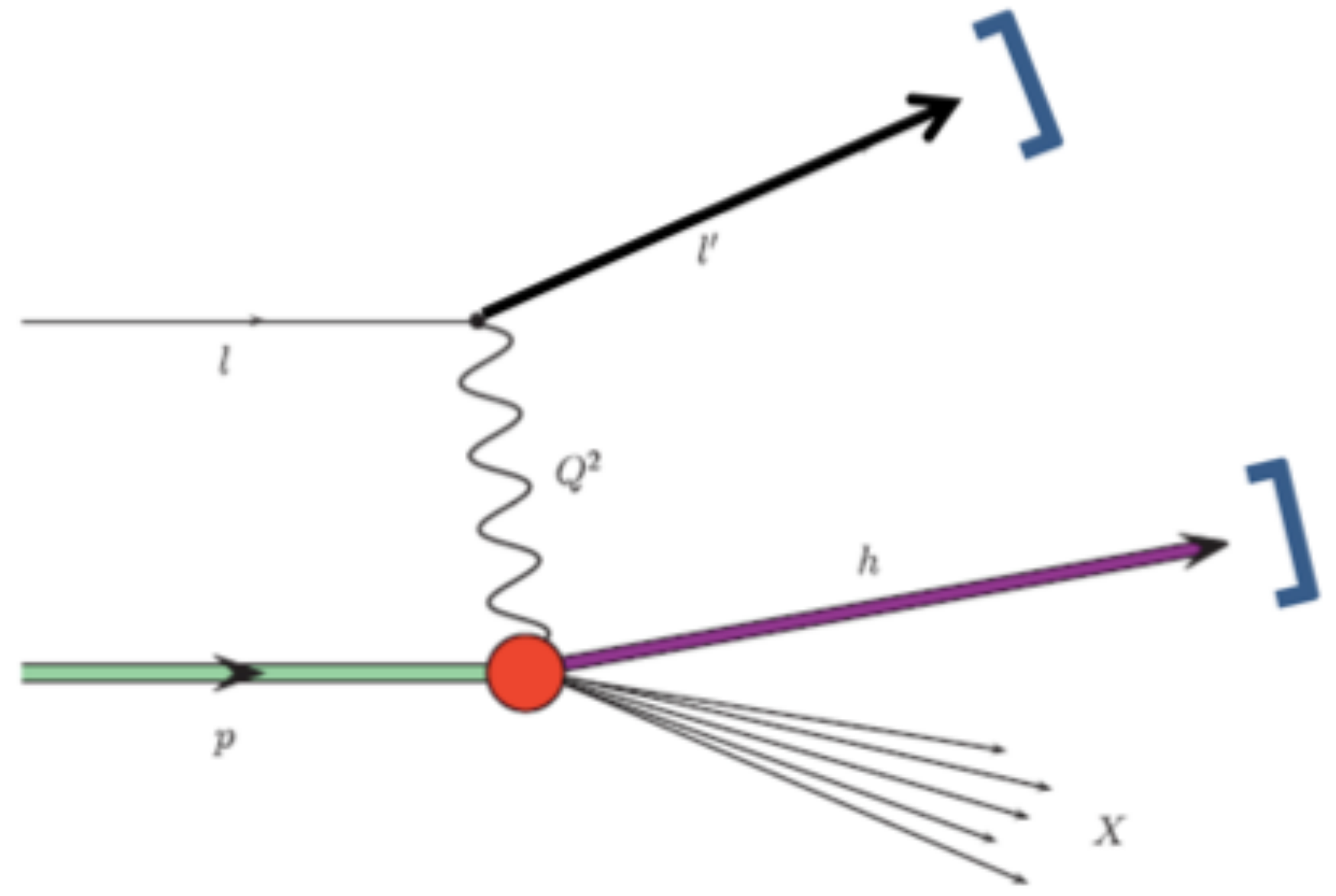


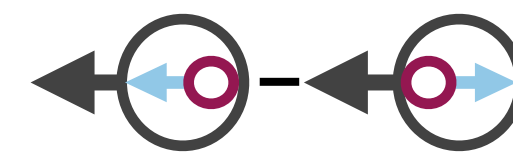
Gluon helicity distribution of the neutron



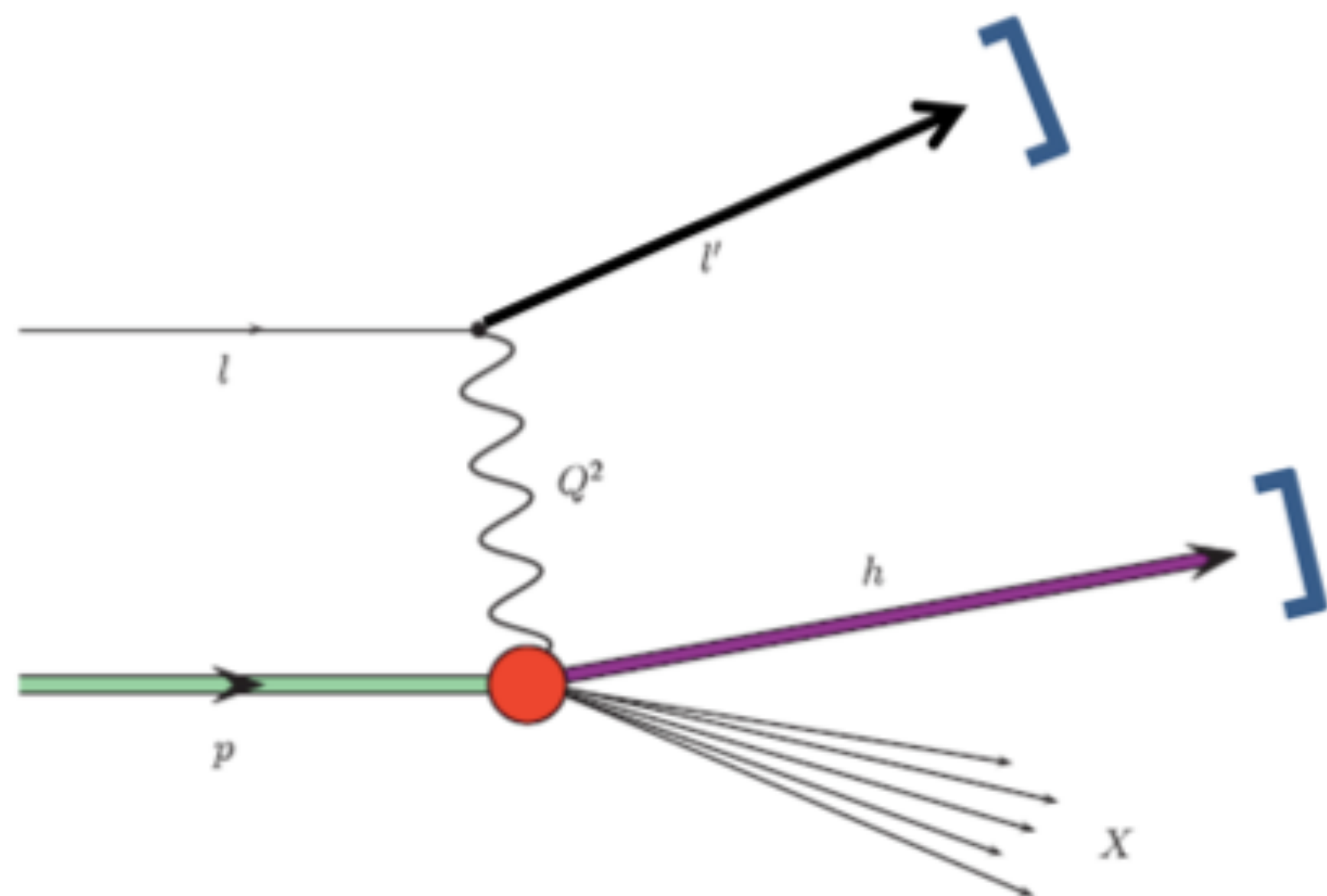


Quark helicity distributions of the proton

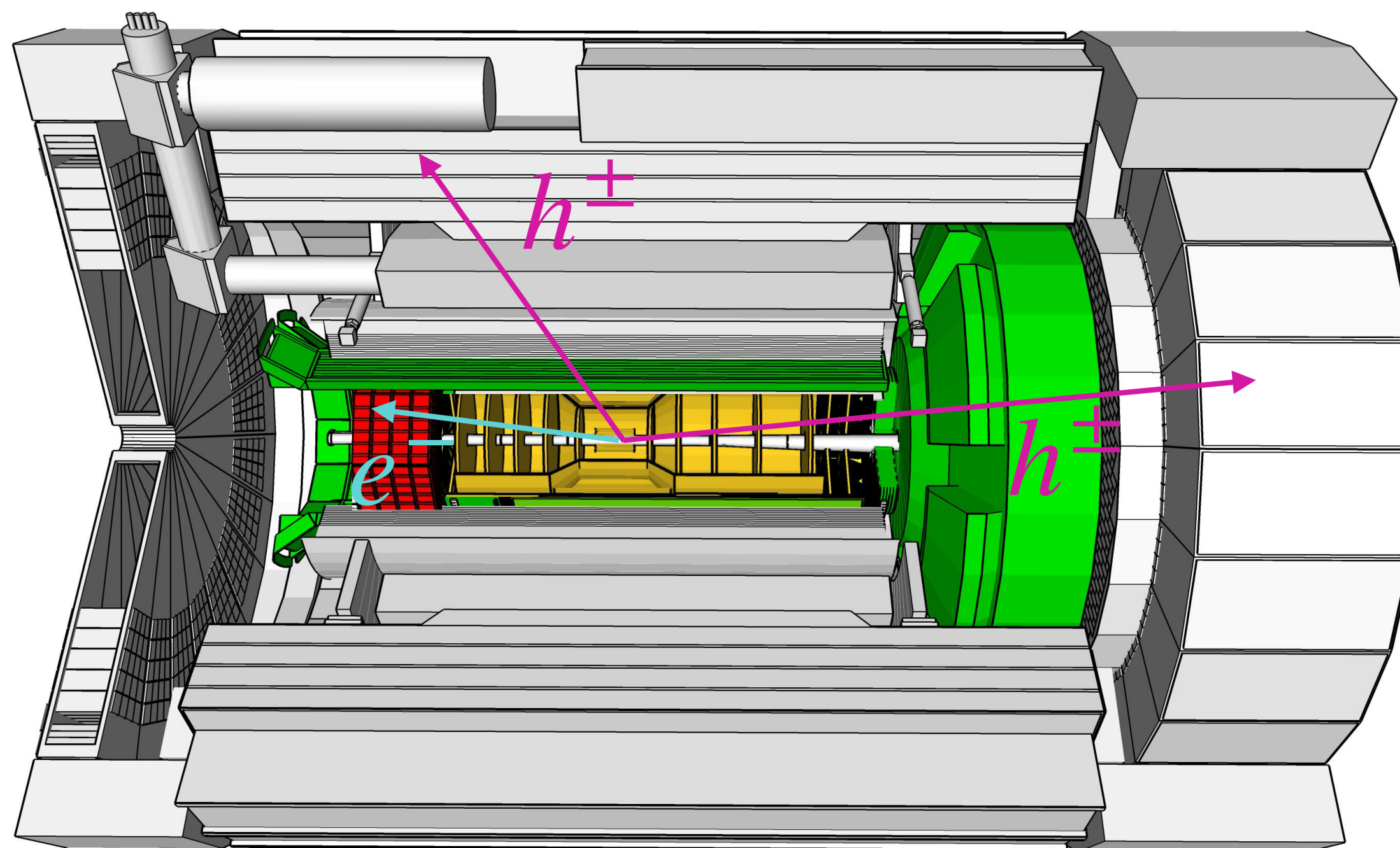




Quark helicity distributions of the proton

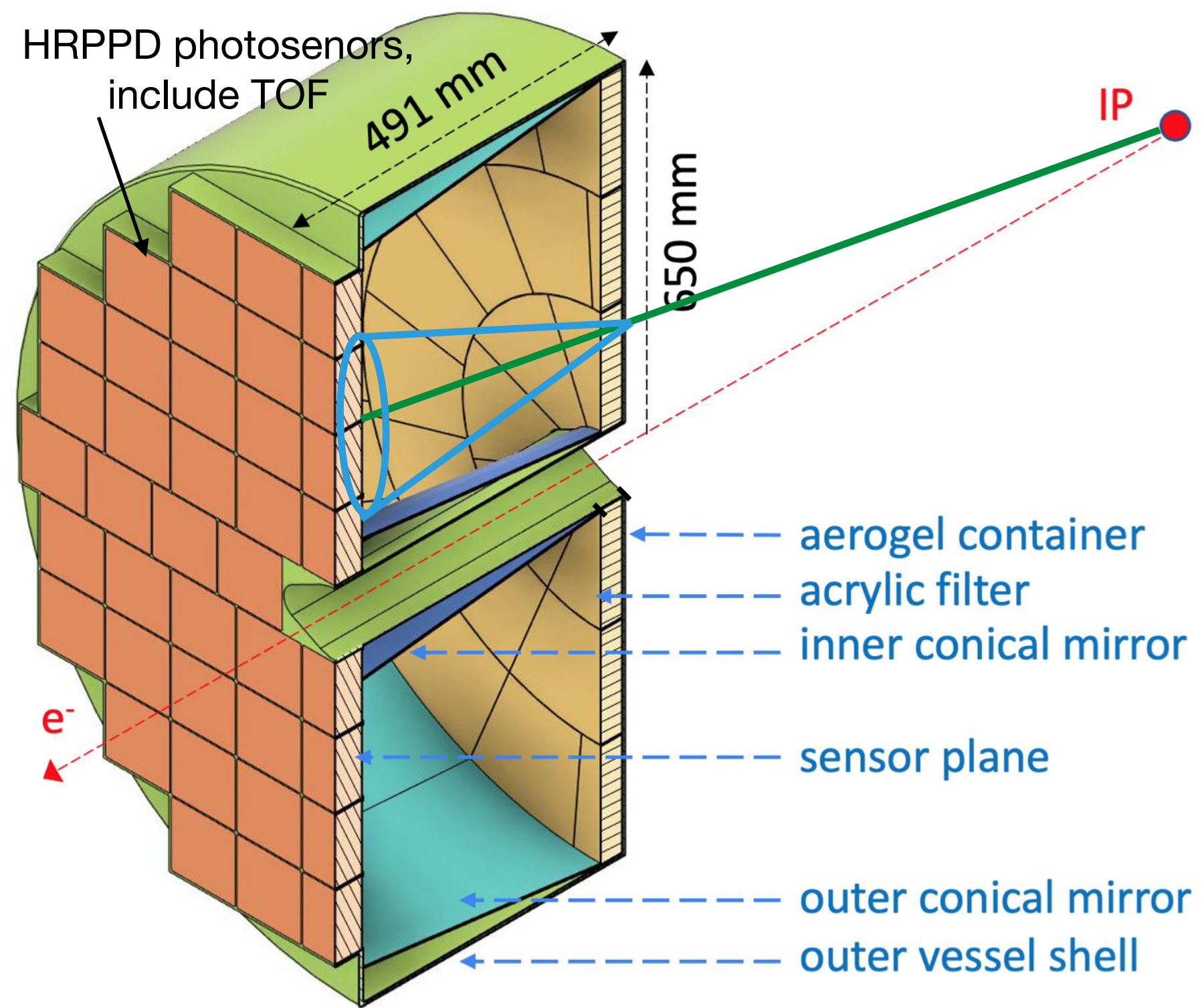


Hadron particle identification:
pions, kaons and protons



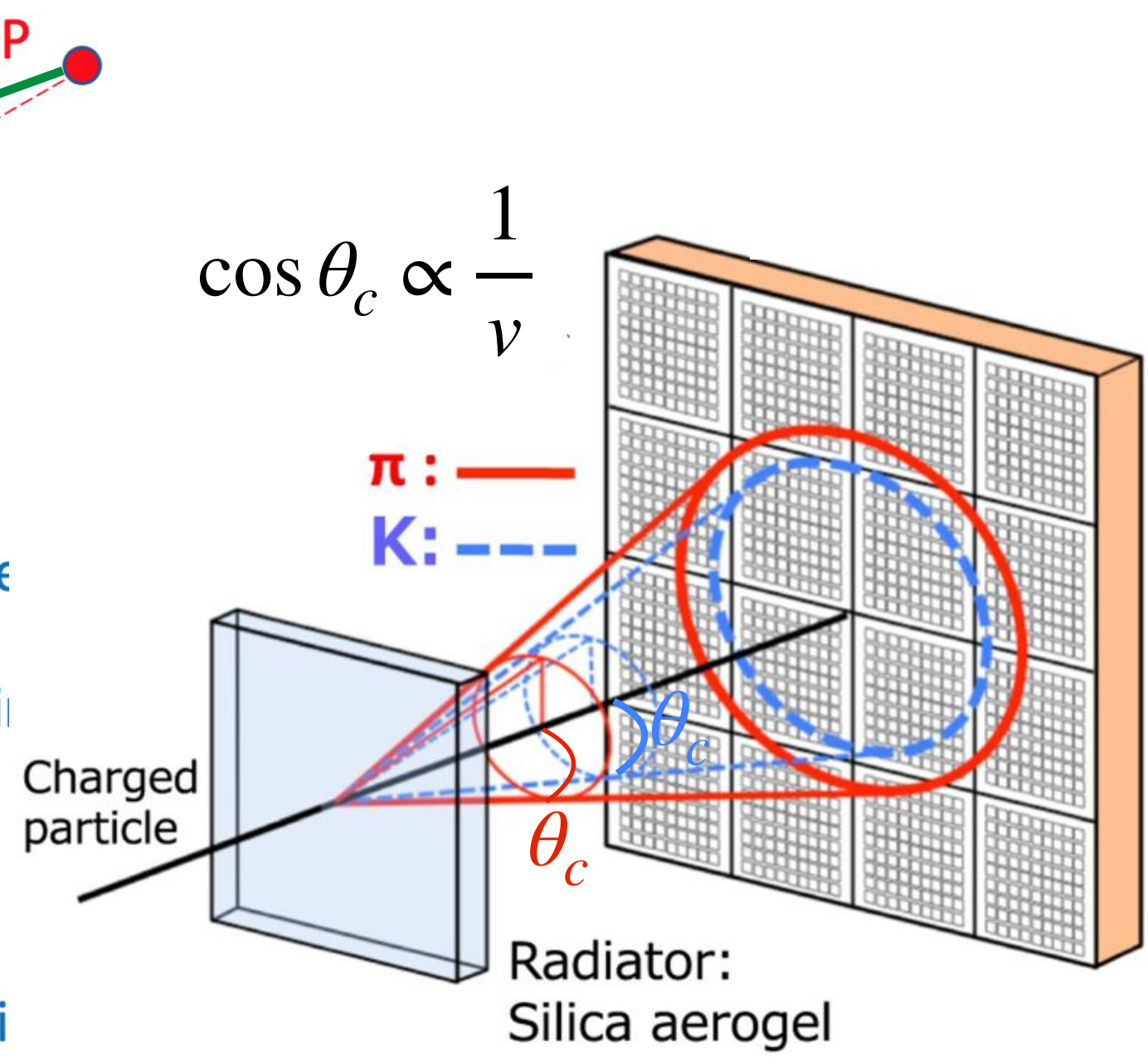
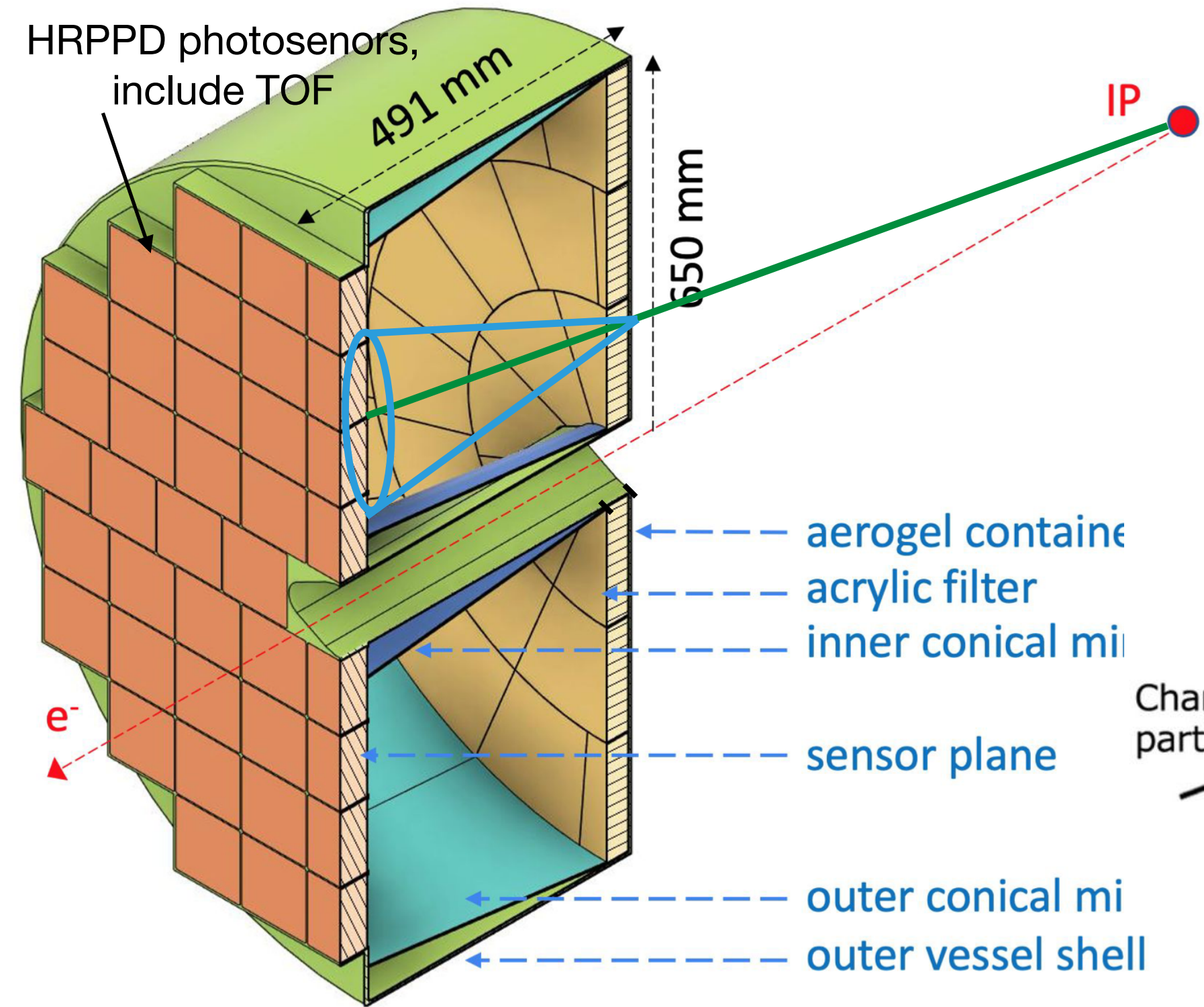
ePIC particle identification

Particle identification: Cherenkov detectors



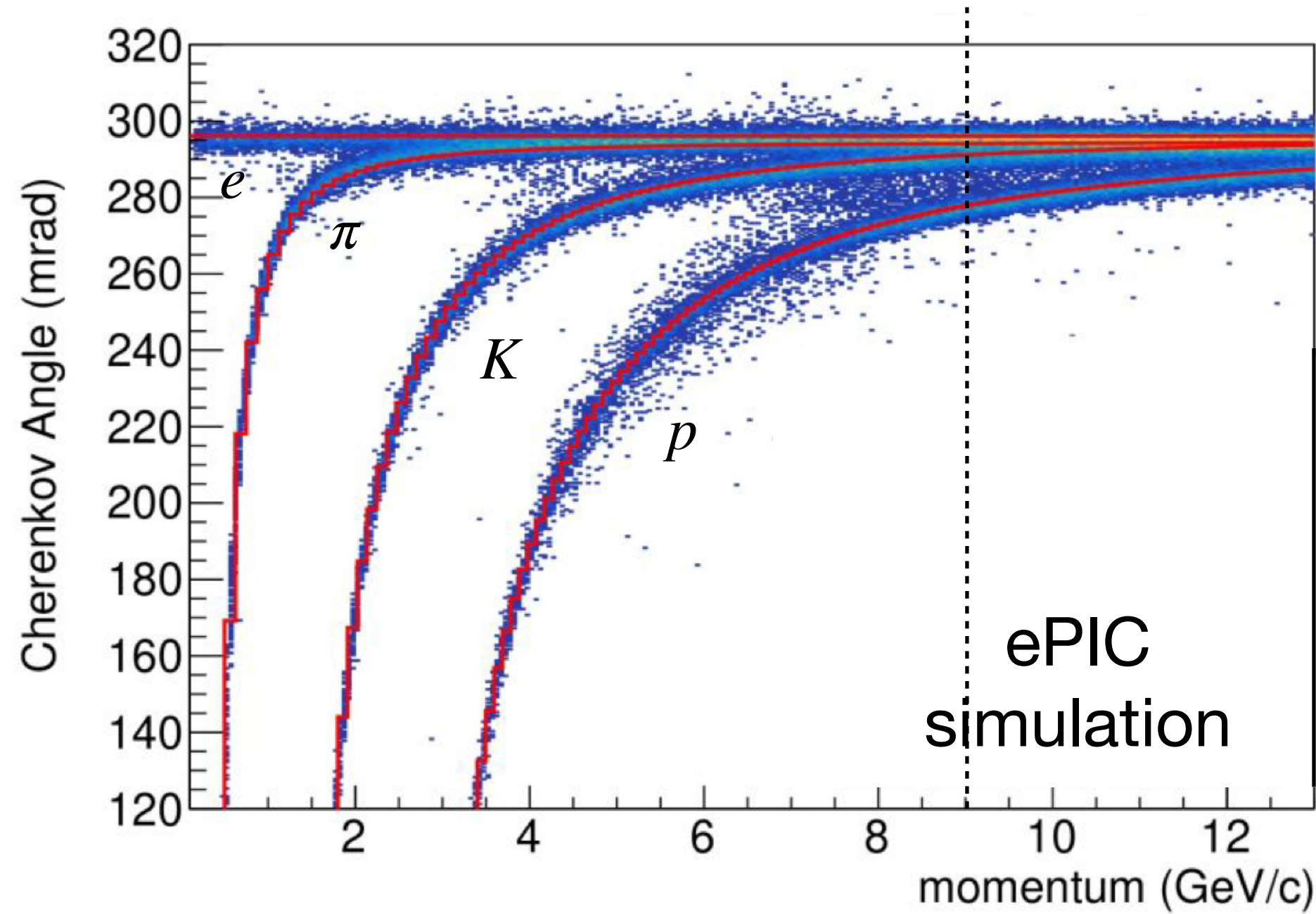
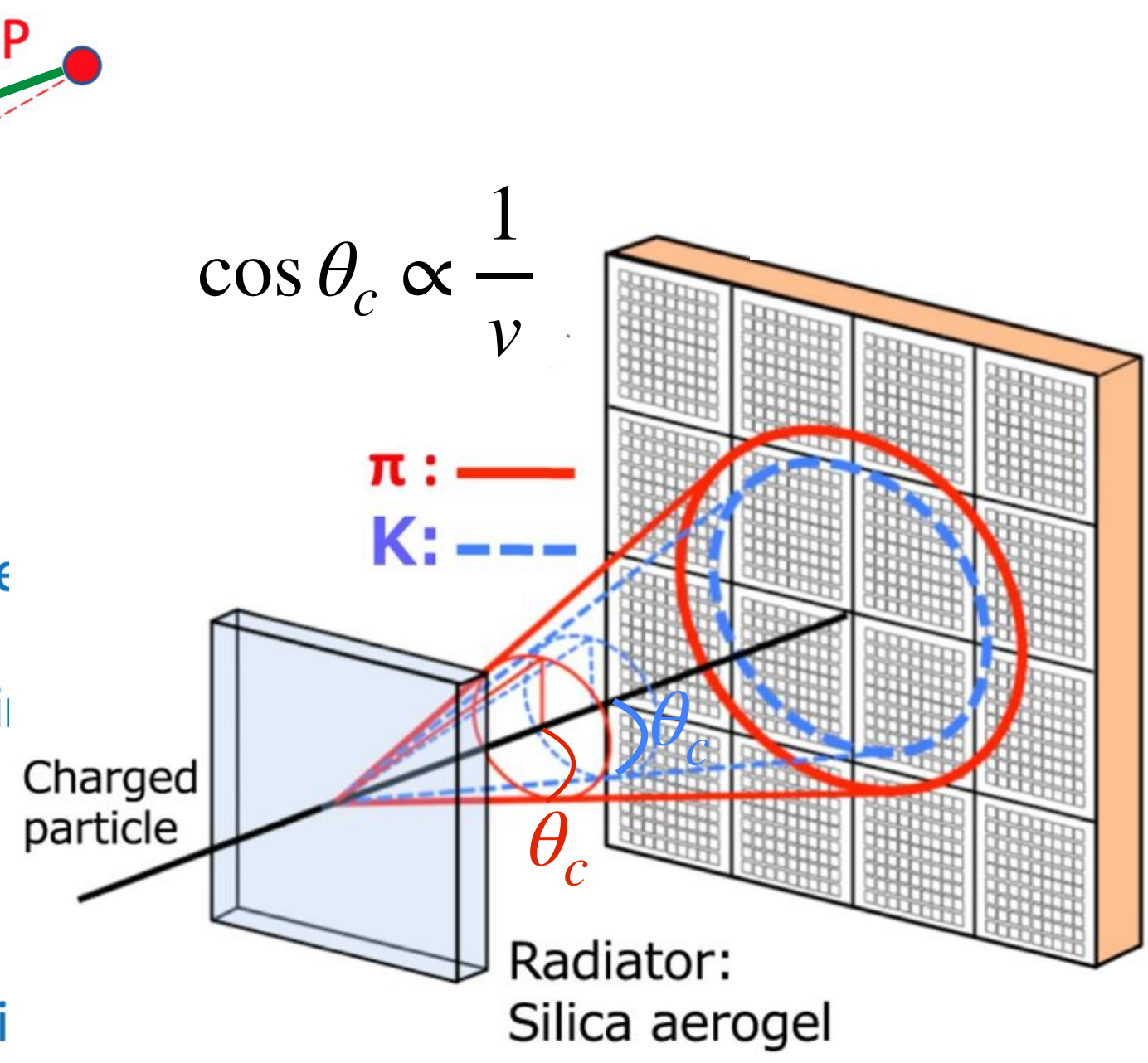
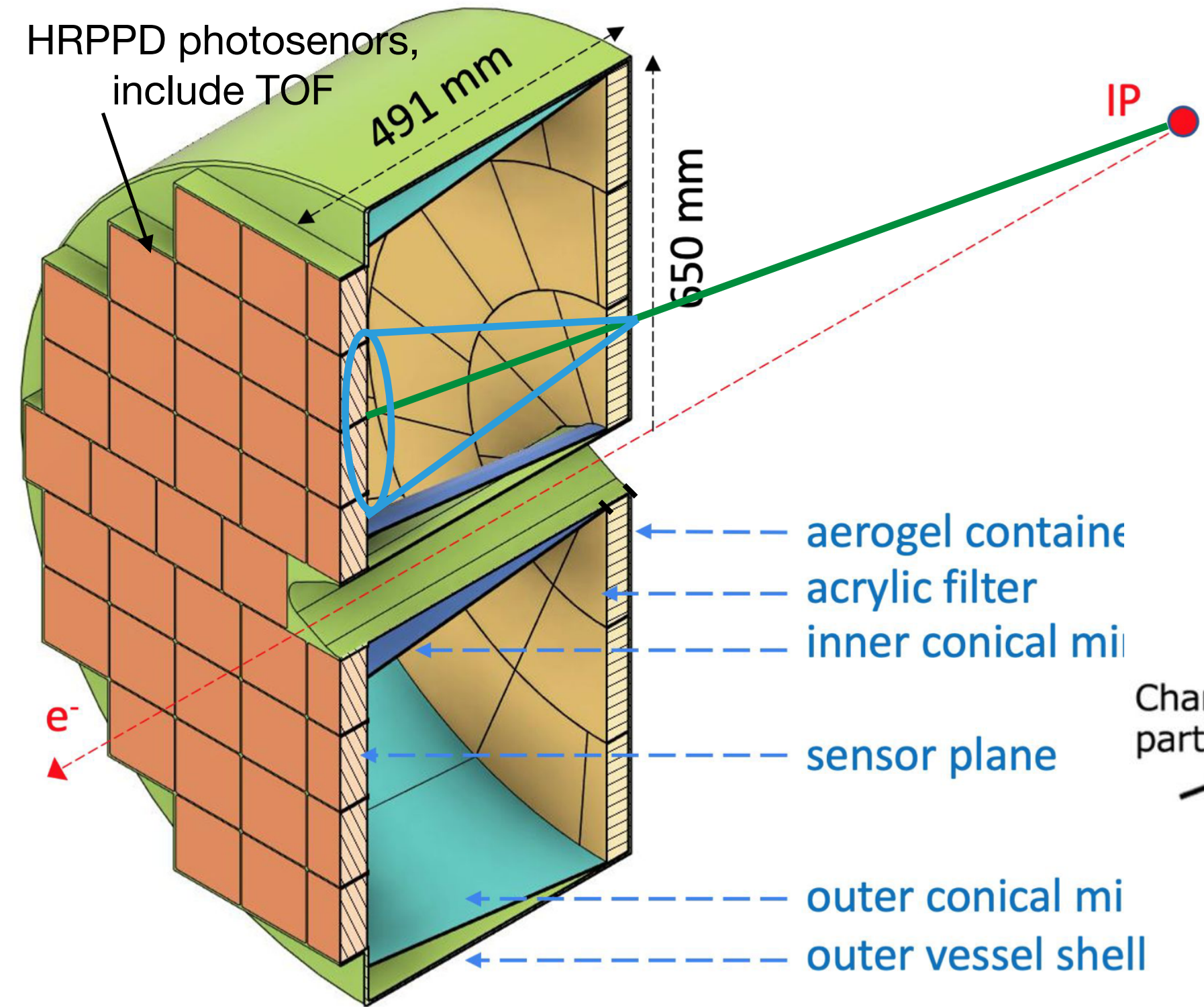
ePIC particle identification

Particle identification: Cherenkov detectors



ePIC particle identification

Particle identification: Cherenkov detectors

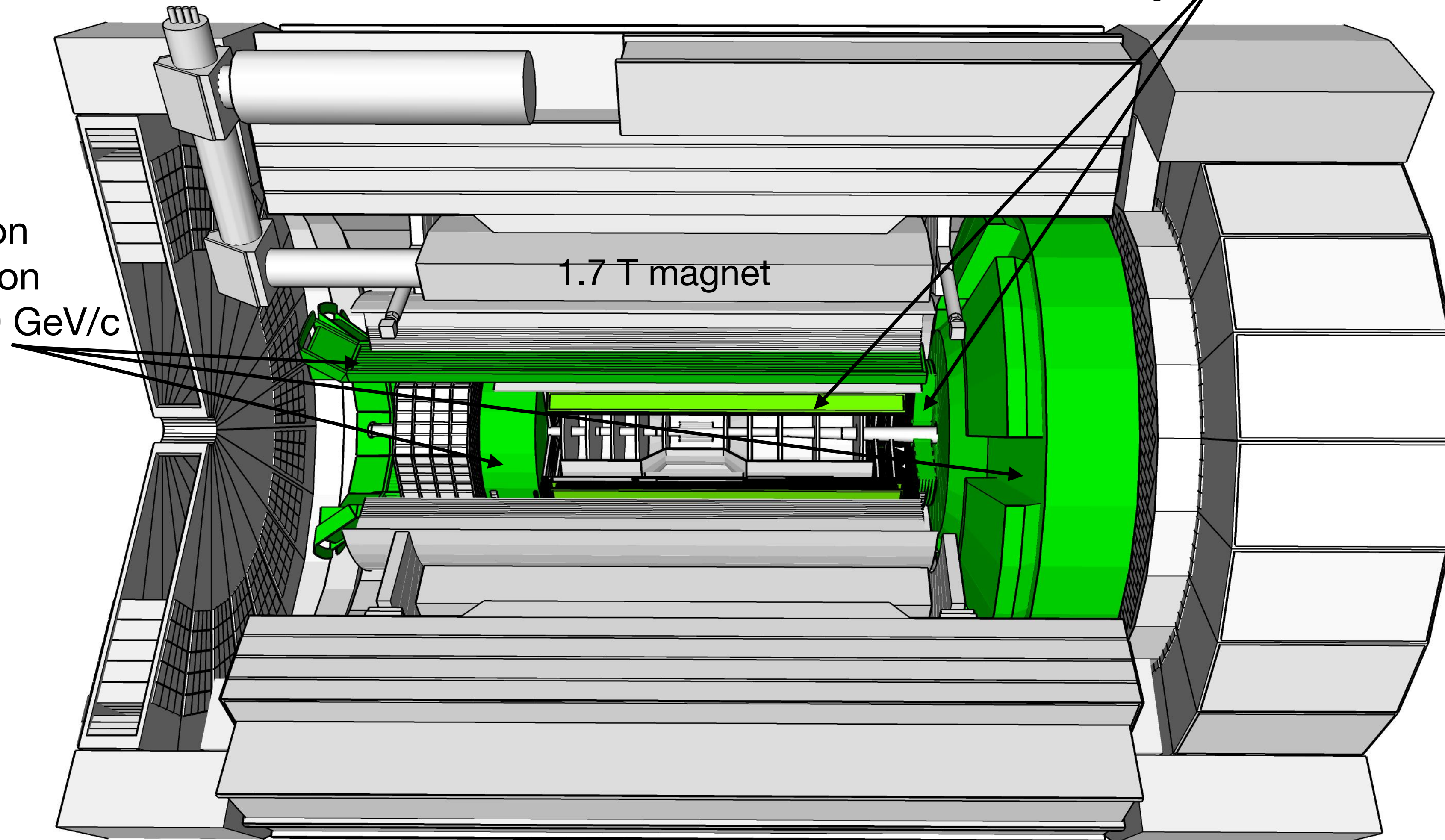


ePIC particle identification

AC-LGAD based TOF, for $p < 0.5 - 3 \text{ GeV}/c$

$$v = \frac{L}{t_{stop} - t_{start}}$$

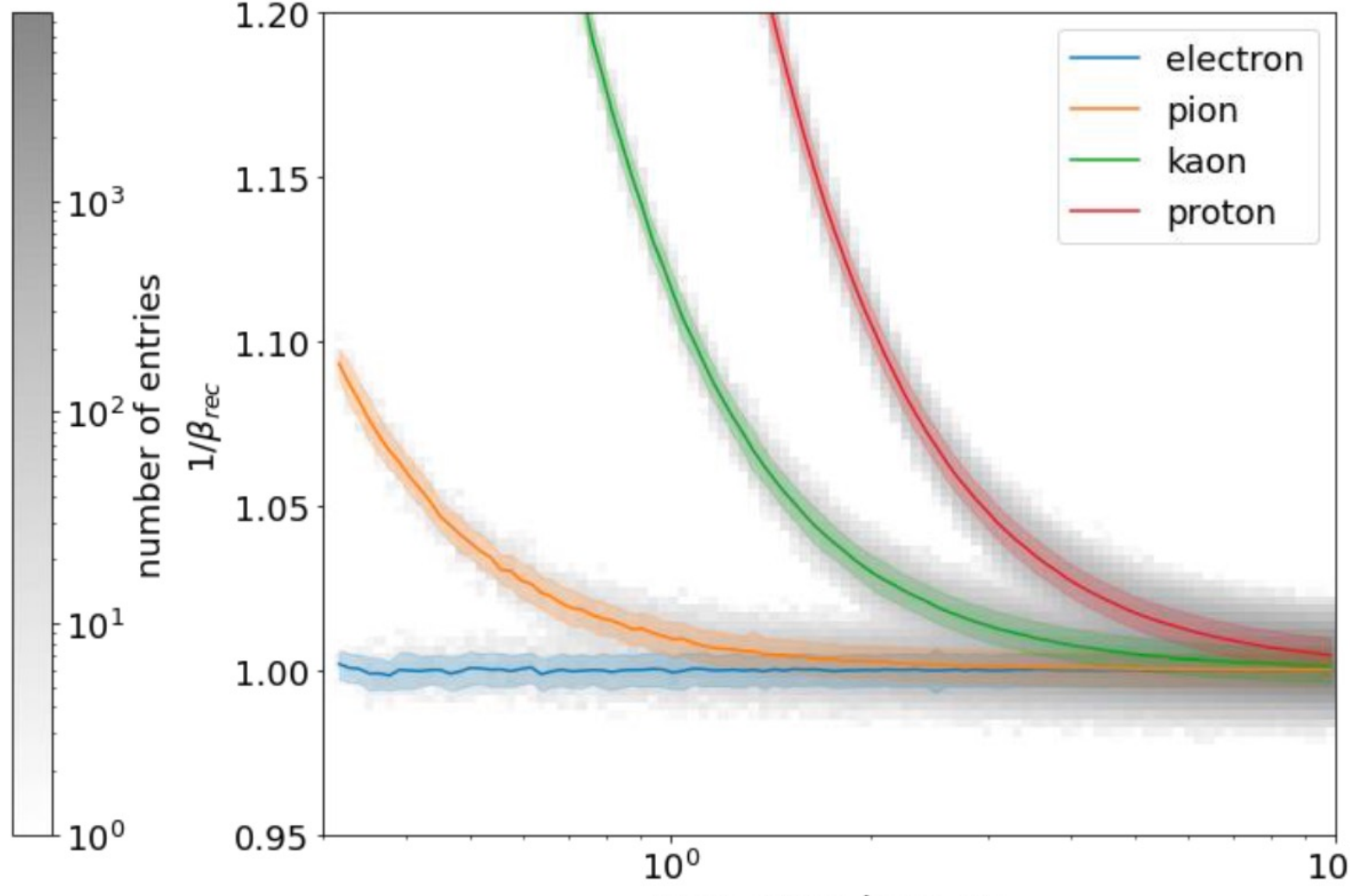
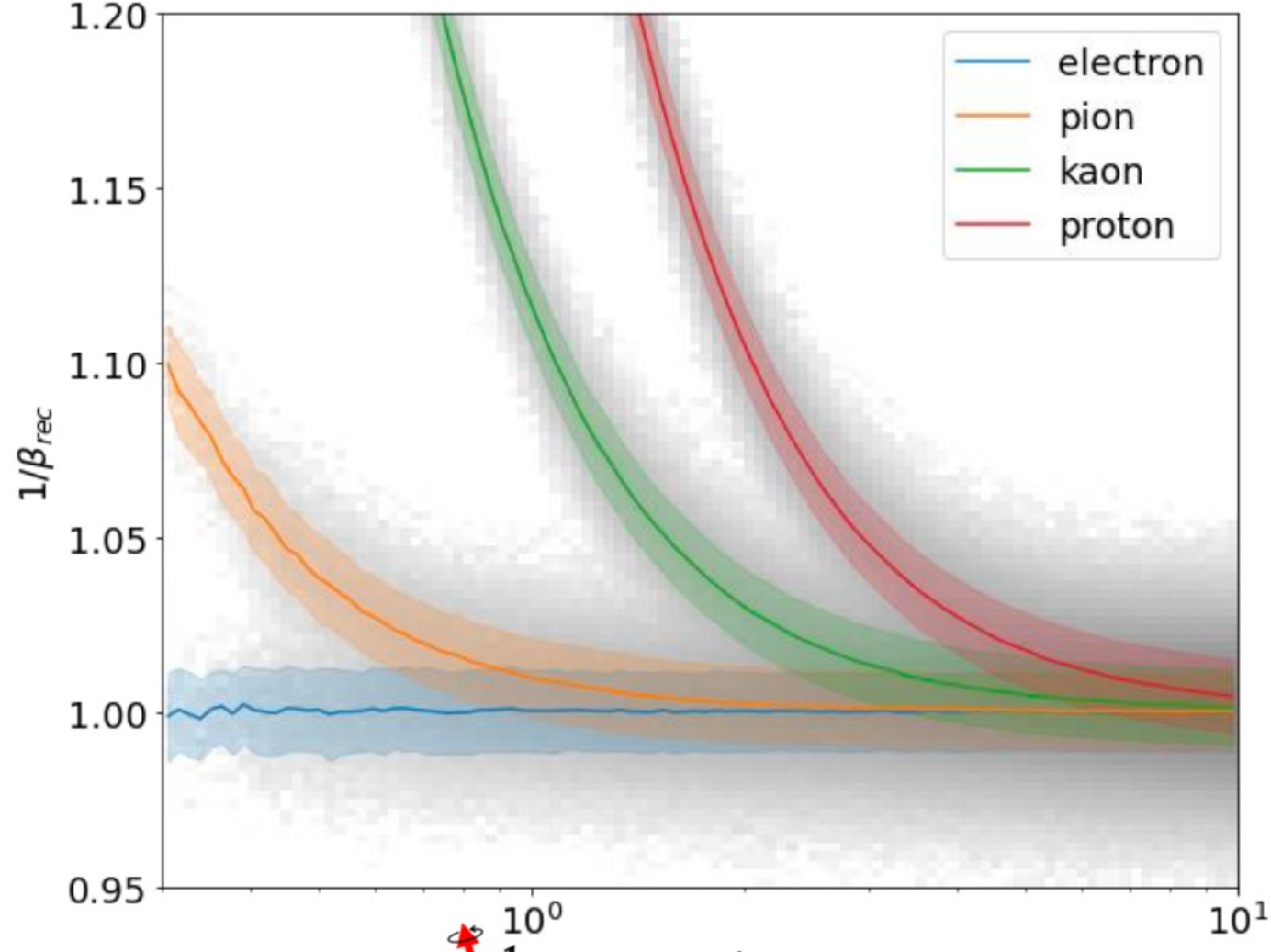
detectors based on Cherenkov radiation for $1 \text{ GeV}/c < p < 50 \text{ GeV}/c$



ePIC particle identification

Particle identification: time of flight

- Barrel Region**
- e/pi up to 0.5 GeV/c
 - pi/K up to 1.9 GeV/c
 - K/p up to 3.1 GeV/c

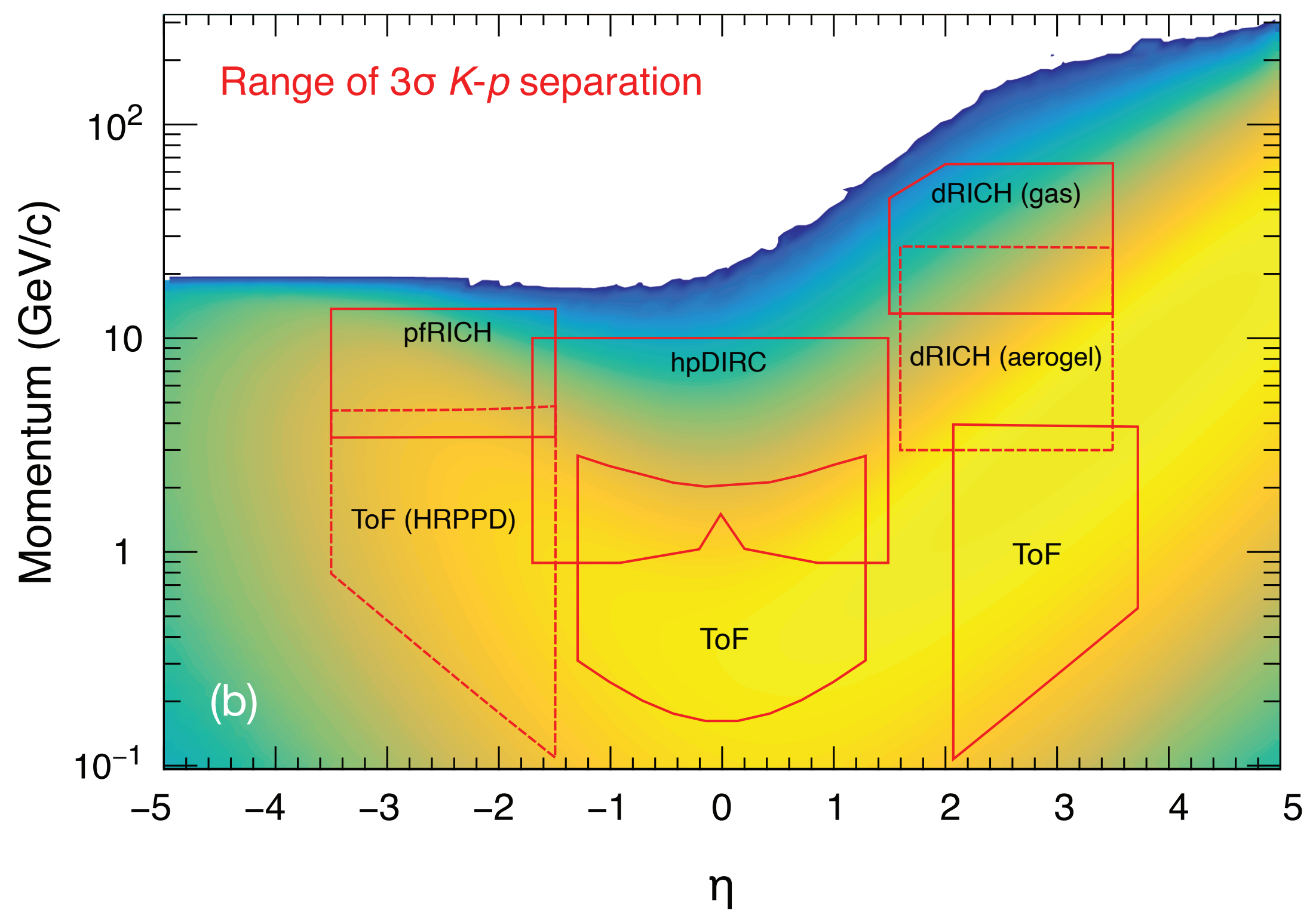
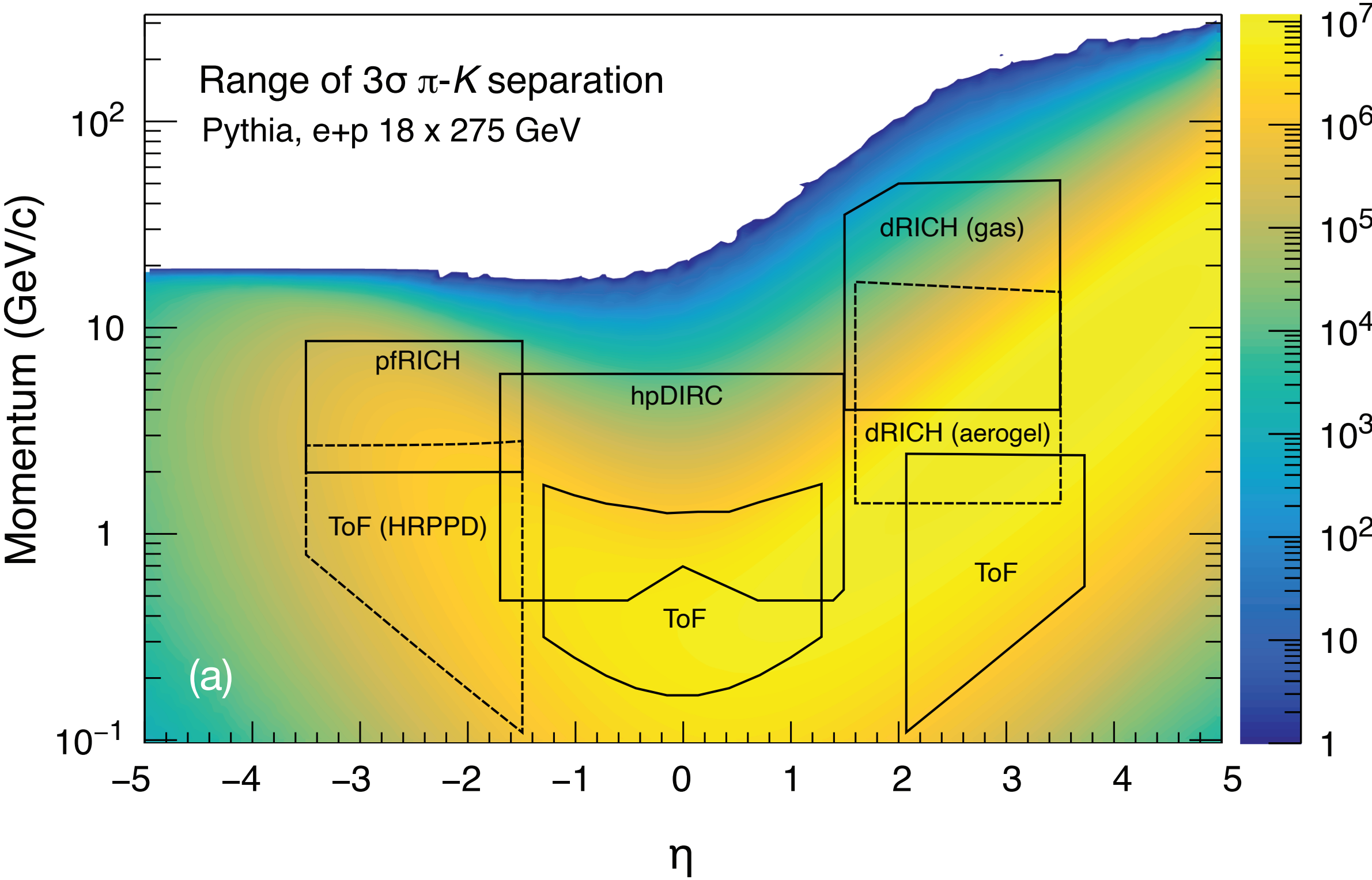


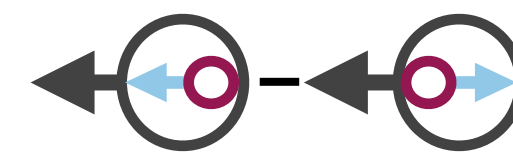
TOF Simulations in ePIC

- Endcap Region**
- e/pi up to 0.8 GeV/c
 - pi/K up to 2.7 GeV/c
 - K/p up to 4.6 GeV/c

ePIC particle identification

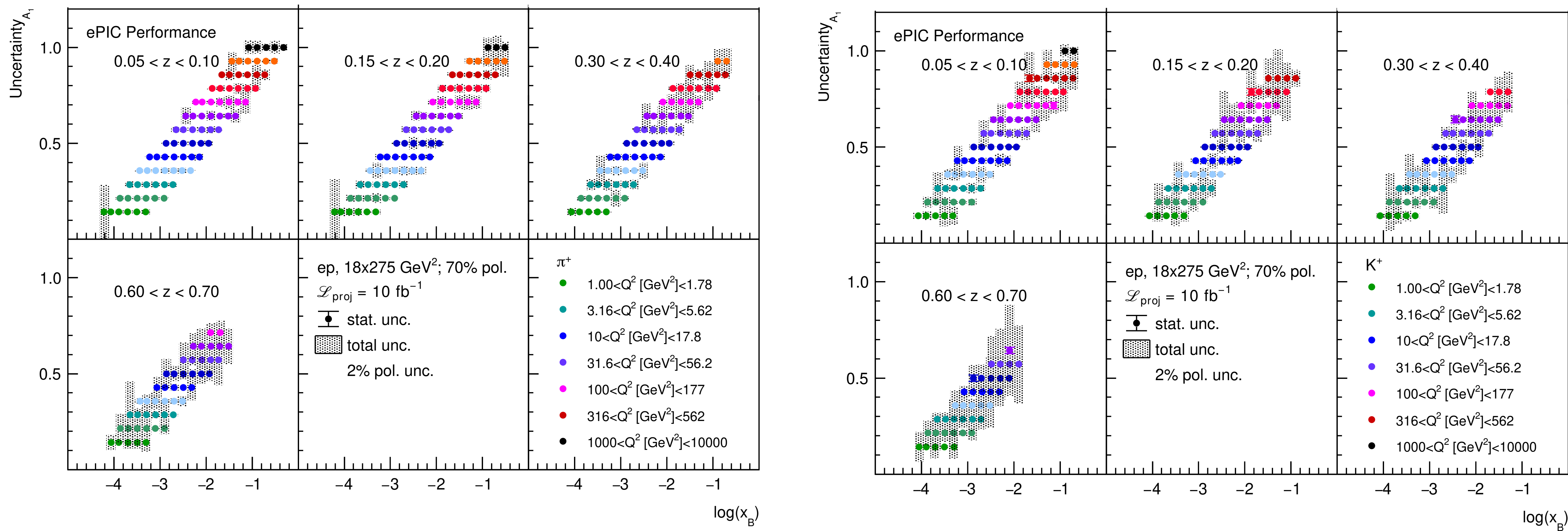
Particle identification: coverage

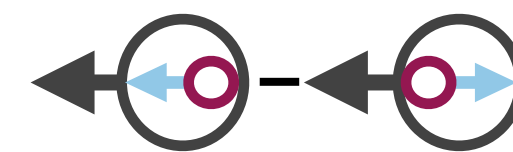




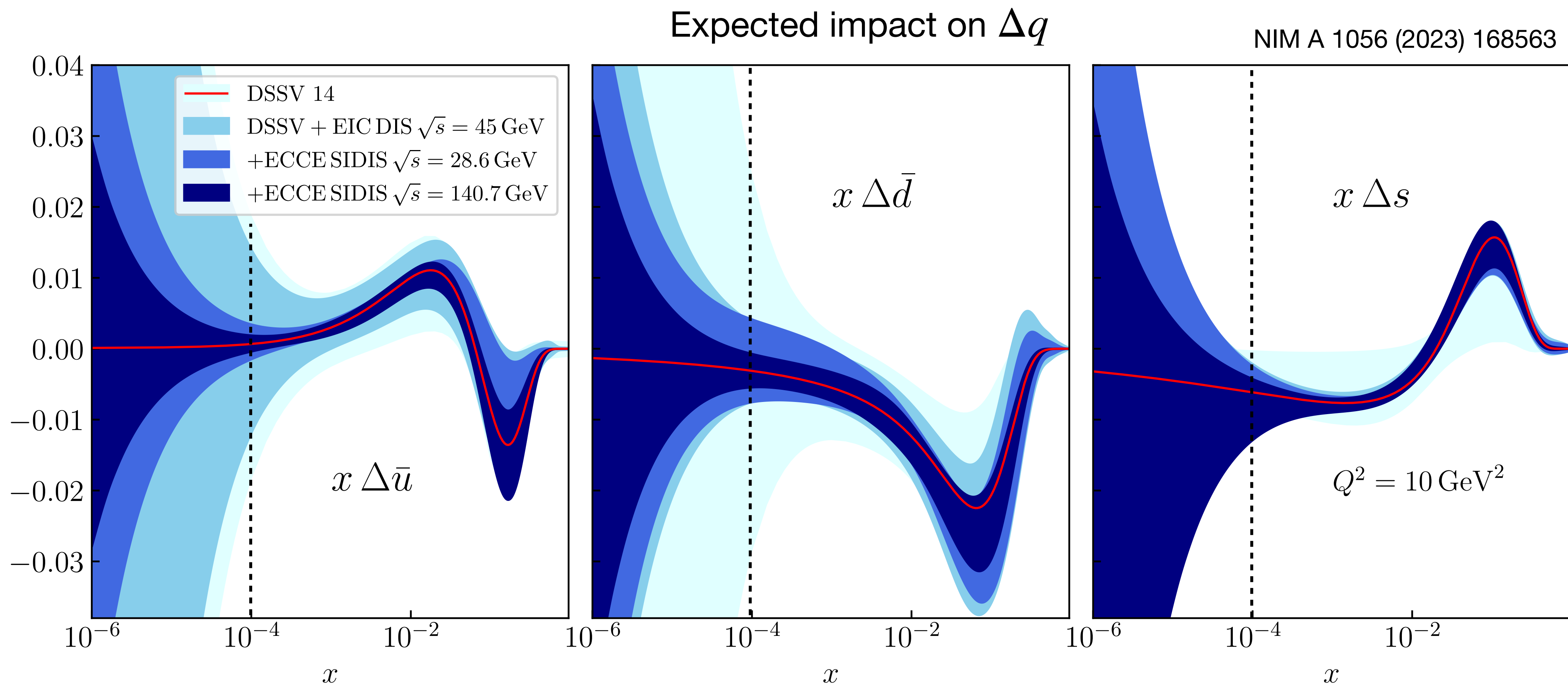
Quark helicity distributions of the proton

Kinematic coverage

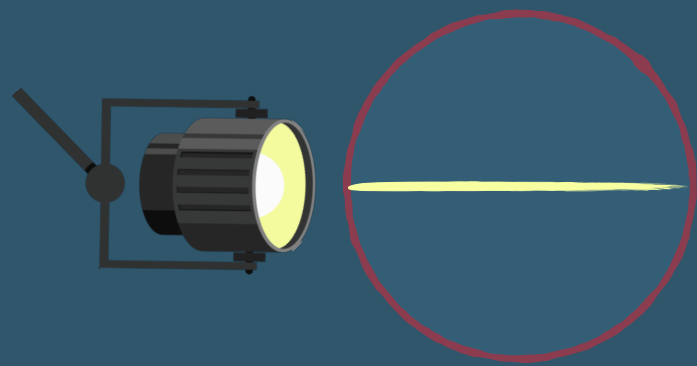




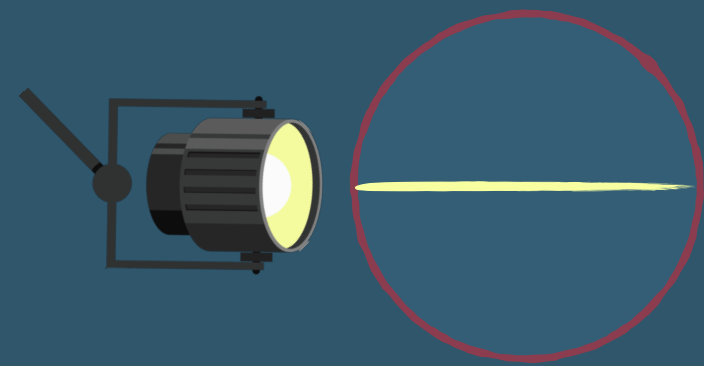
Quark helicity distributions of the proton



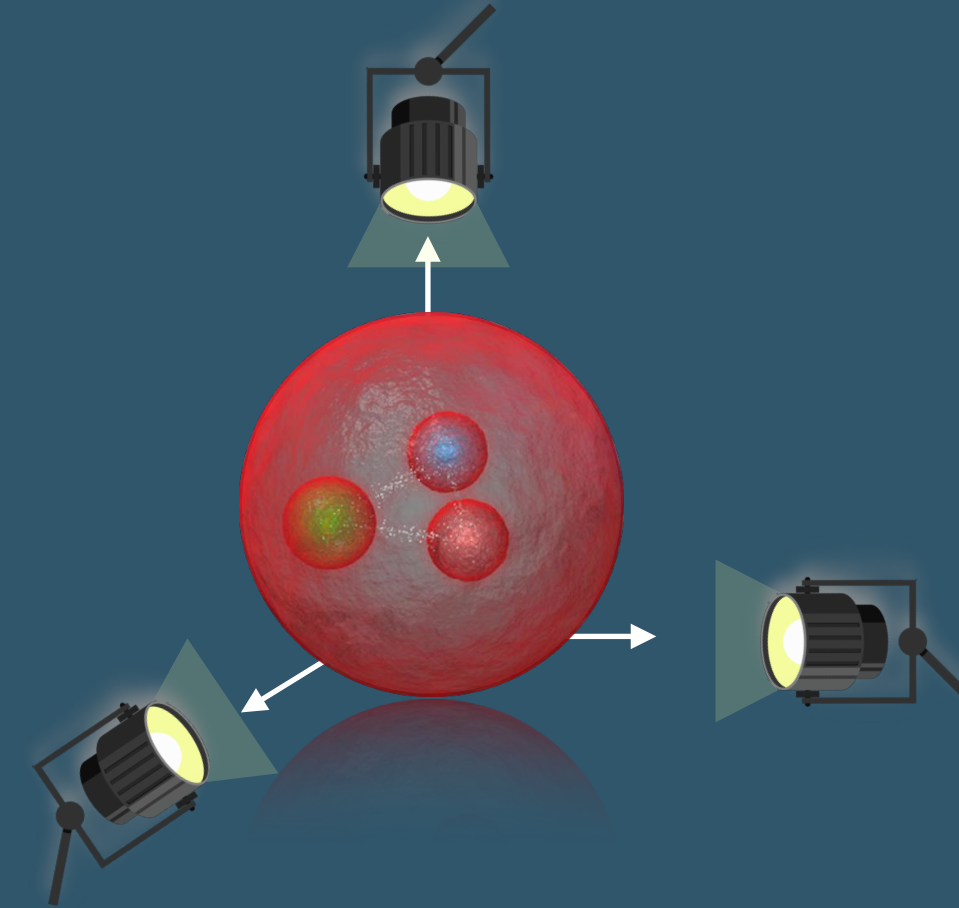
1D image



1D image

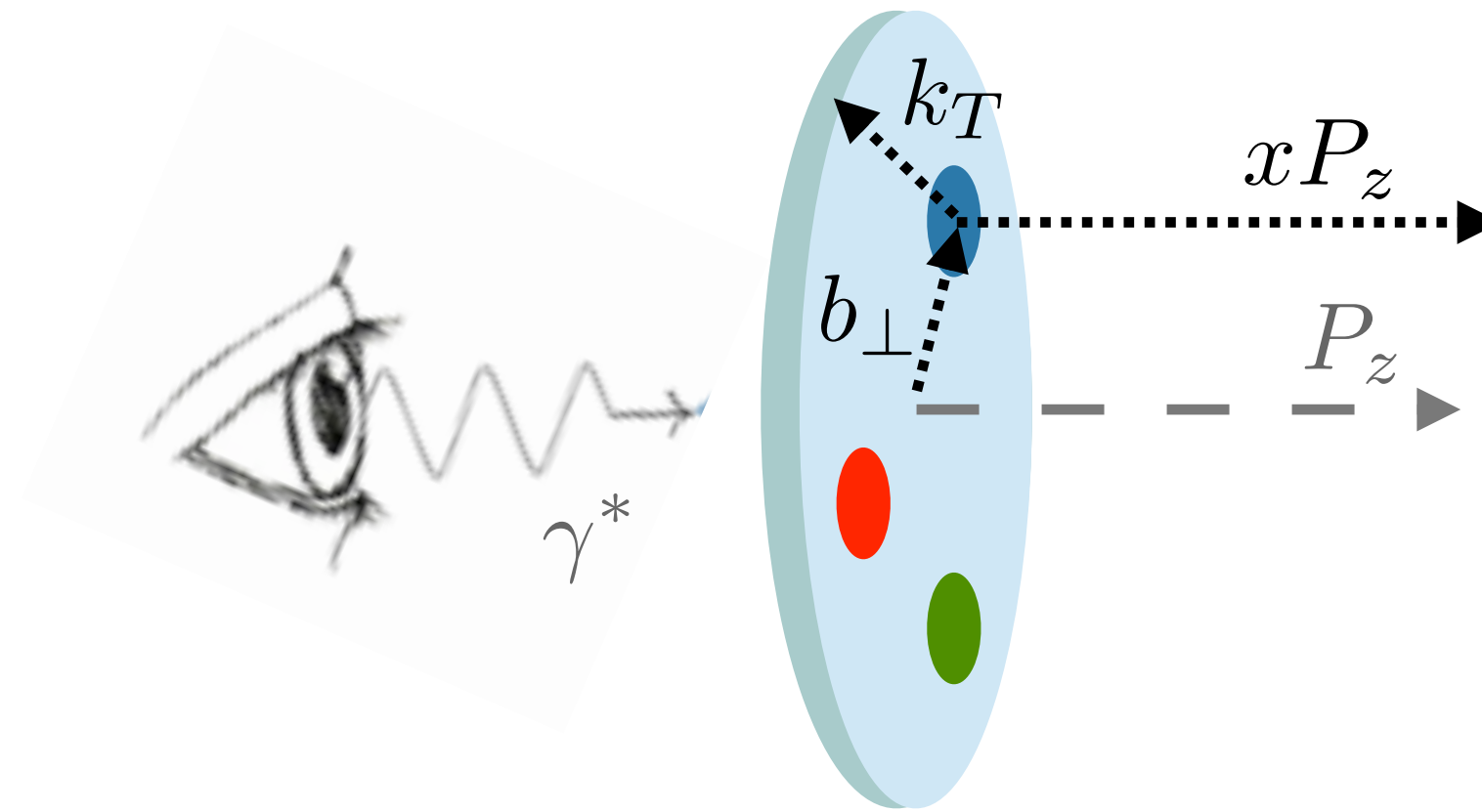


3D tomographies of the nucleon

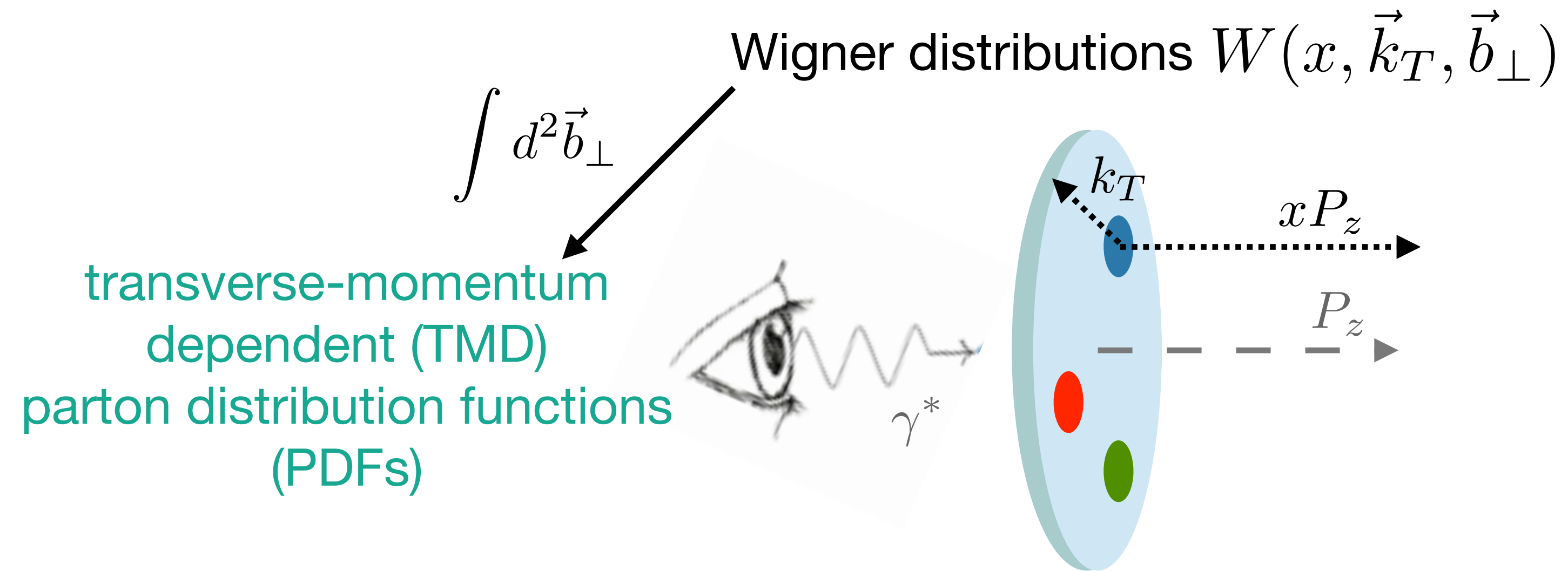


The various dimensions of the nucleon

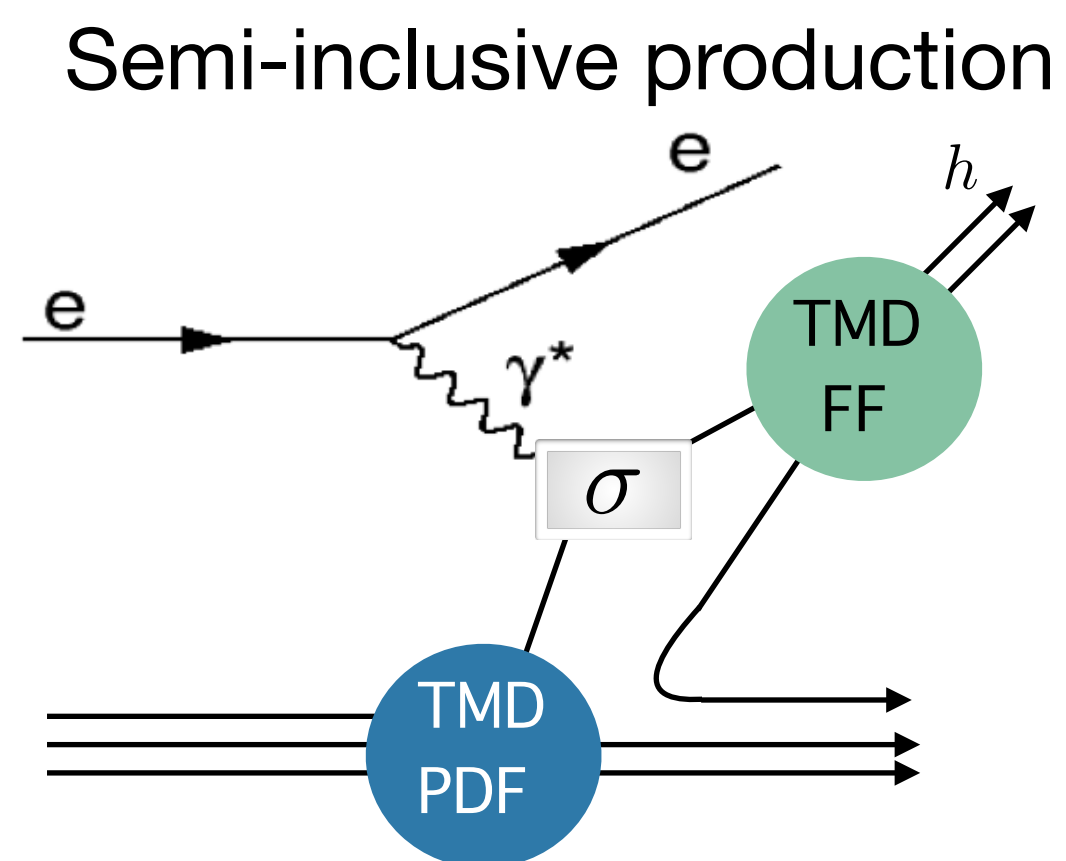
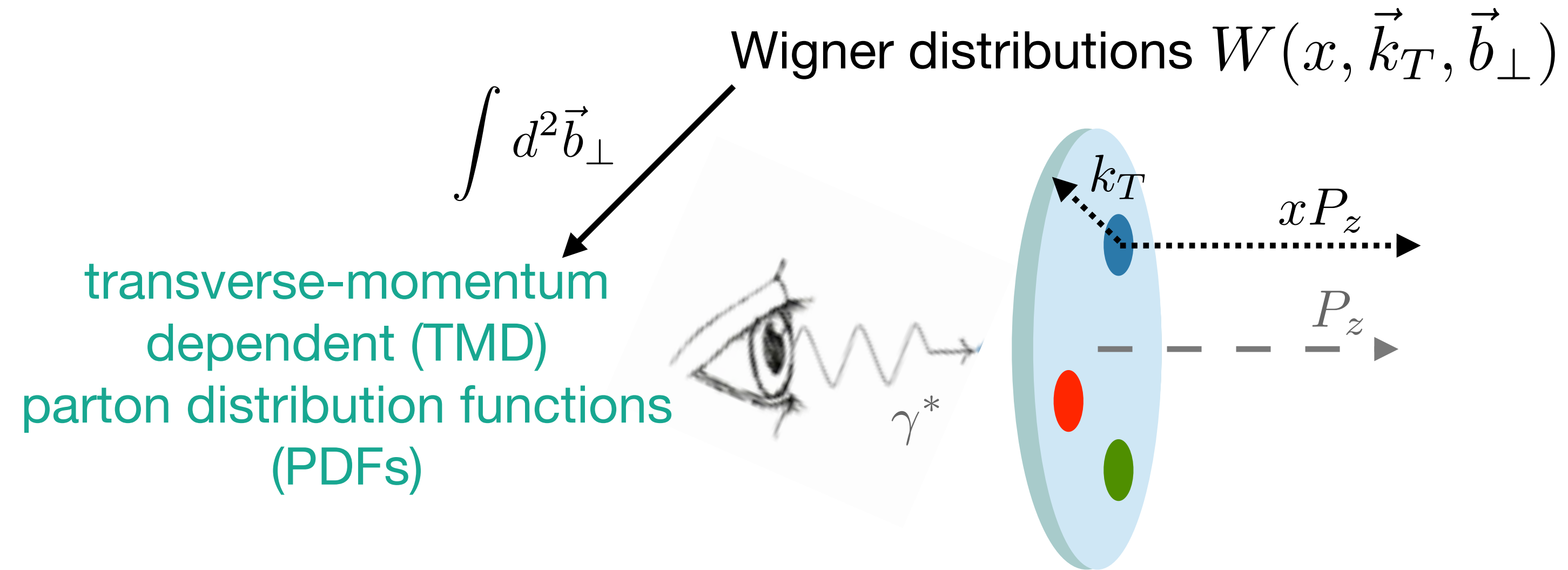
Wigner distributions $W(x, \vec{k}_T, \vec{b}_\perp)$



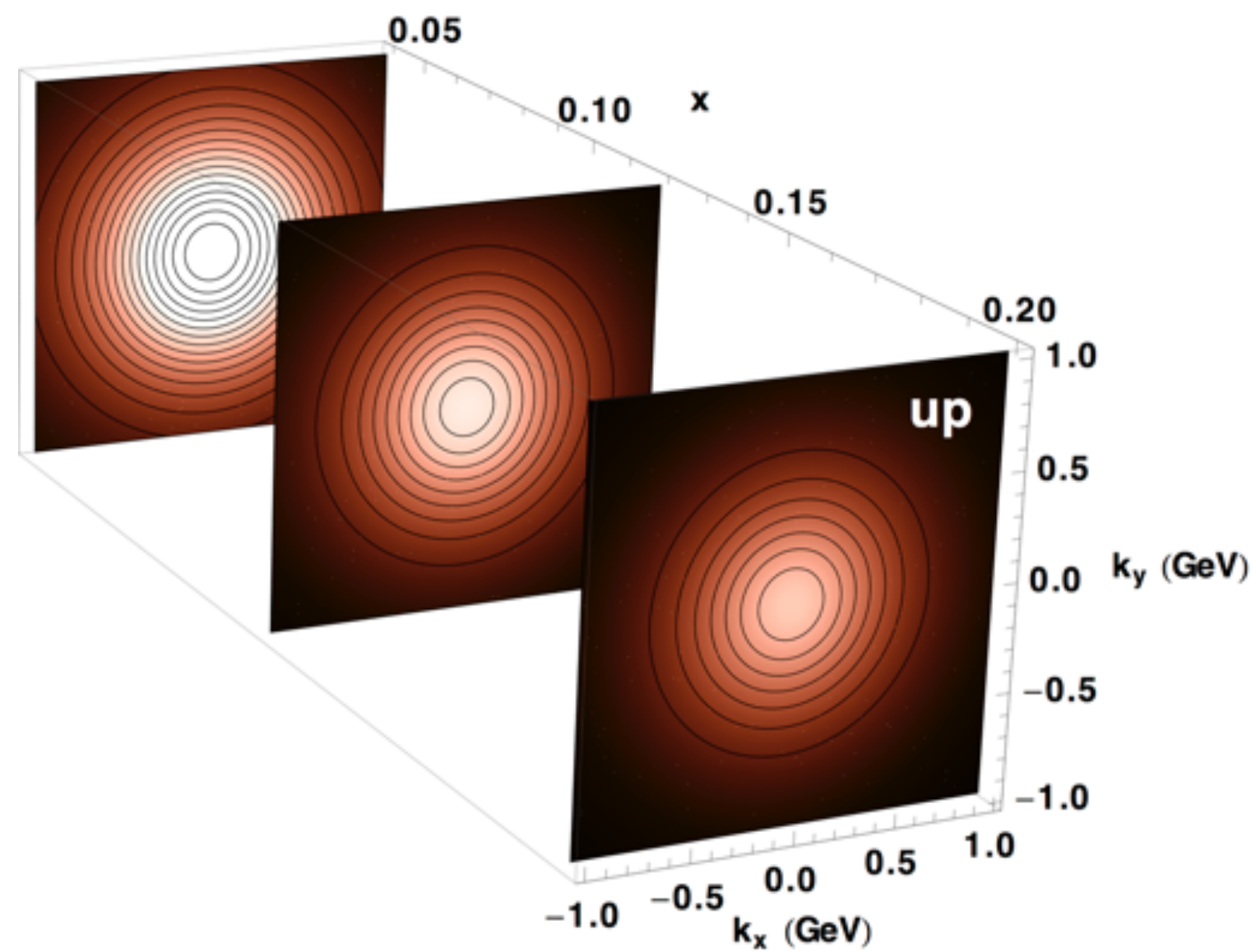
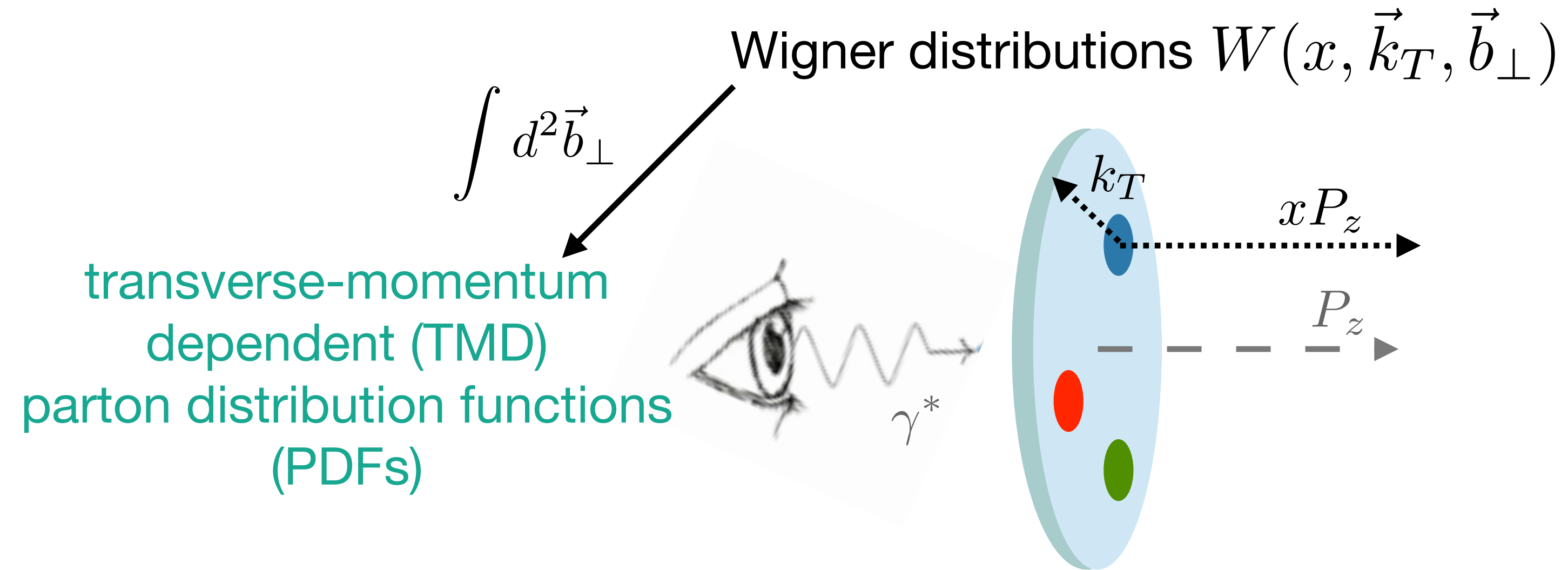
The various dimensions of the nucleon



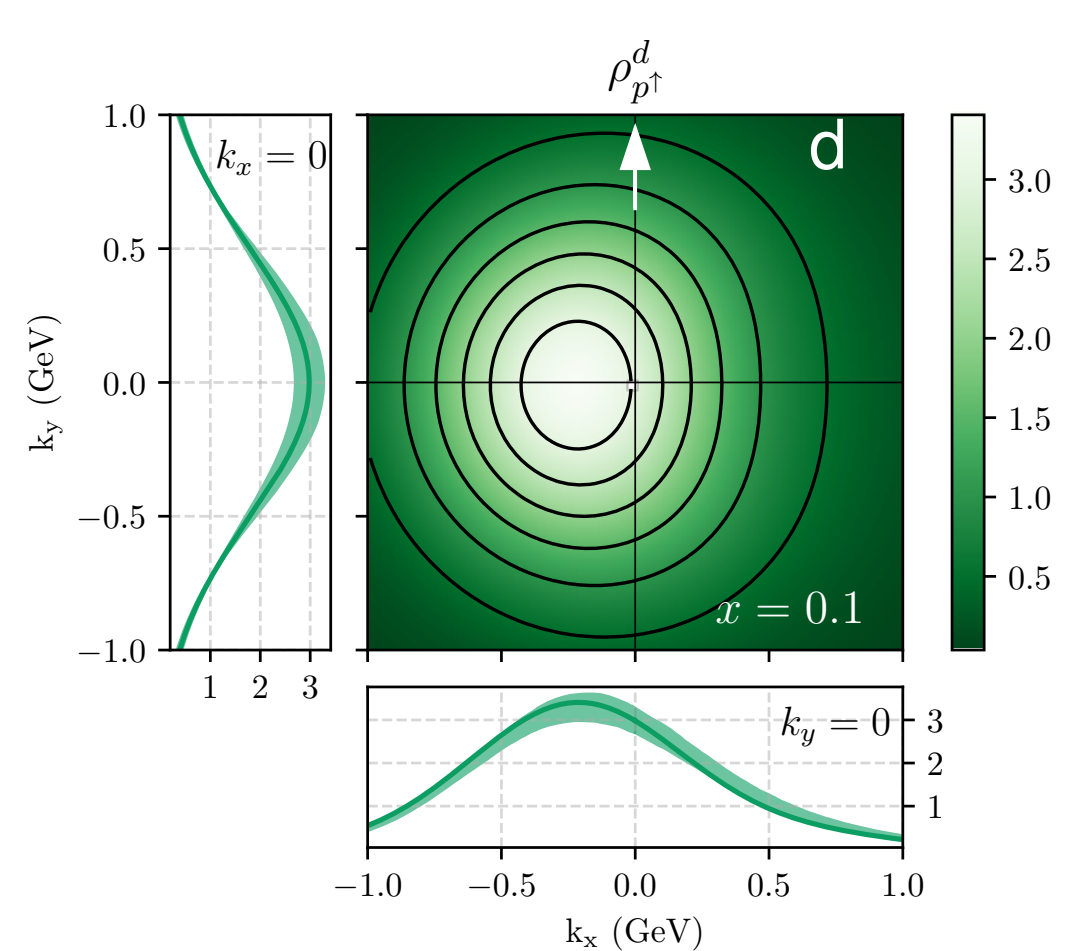
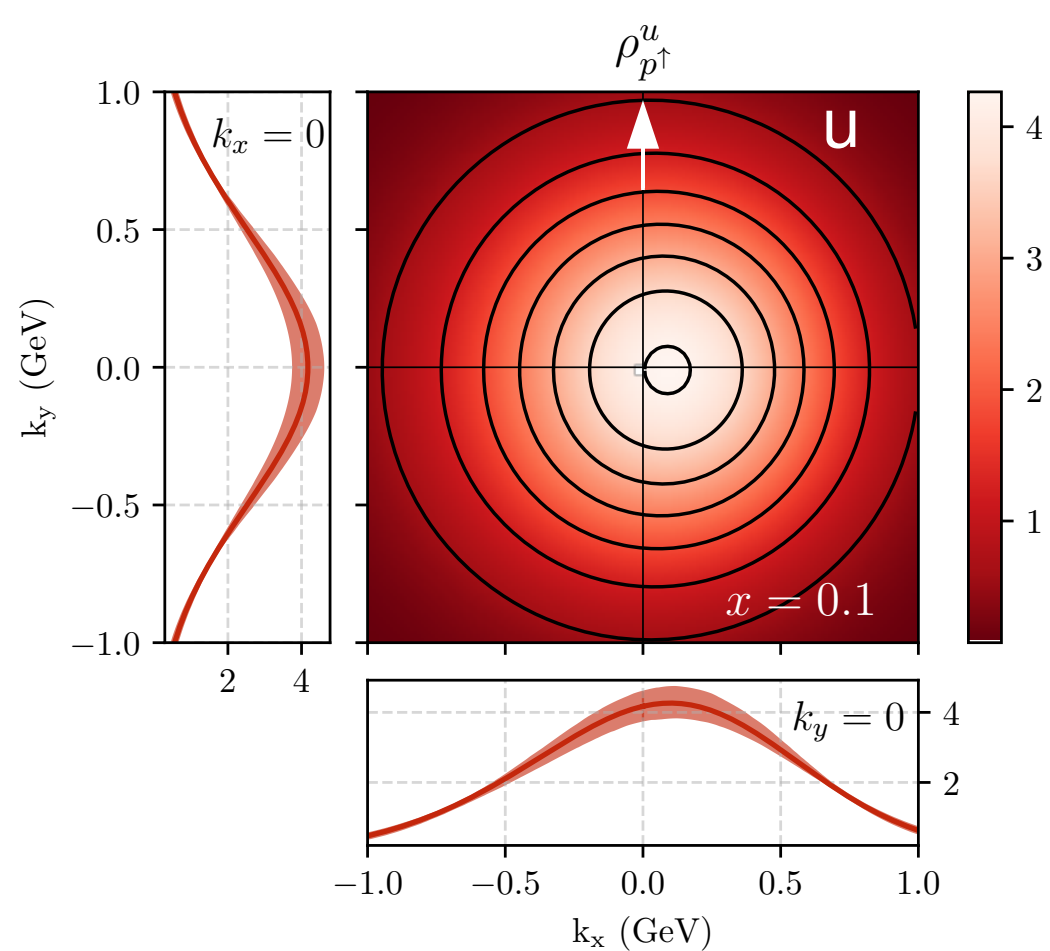
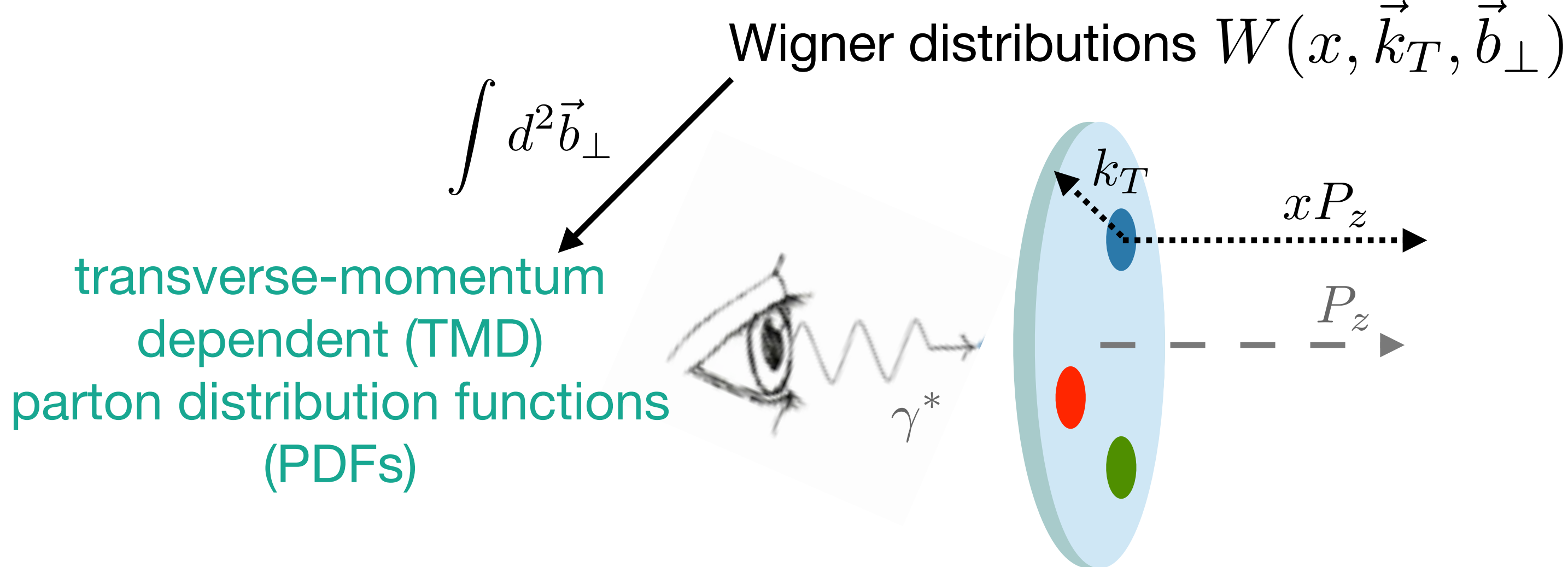
The various dimensions of the nucleon



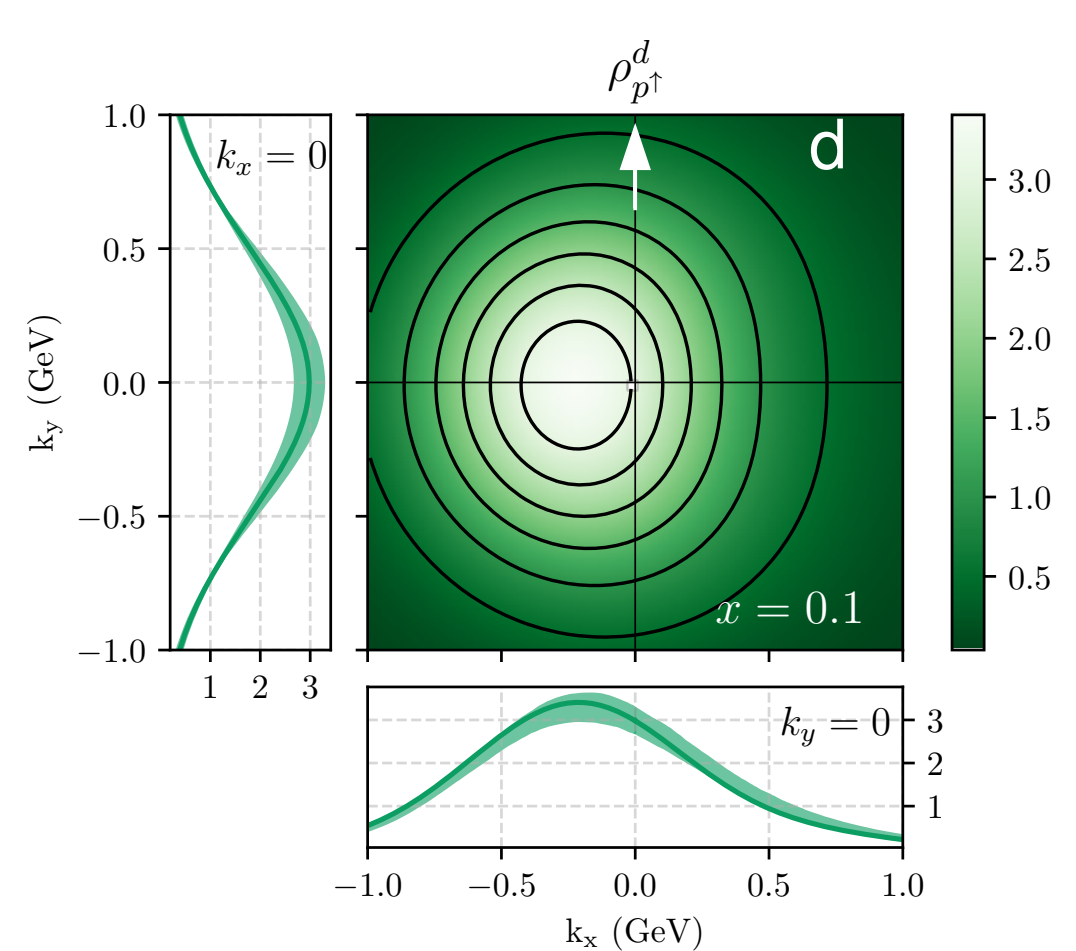
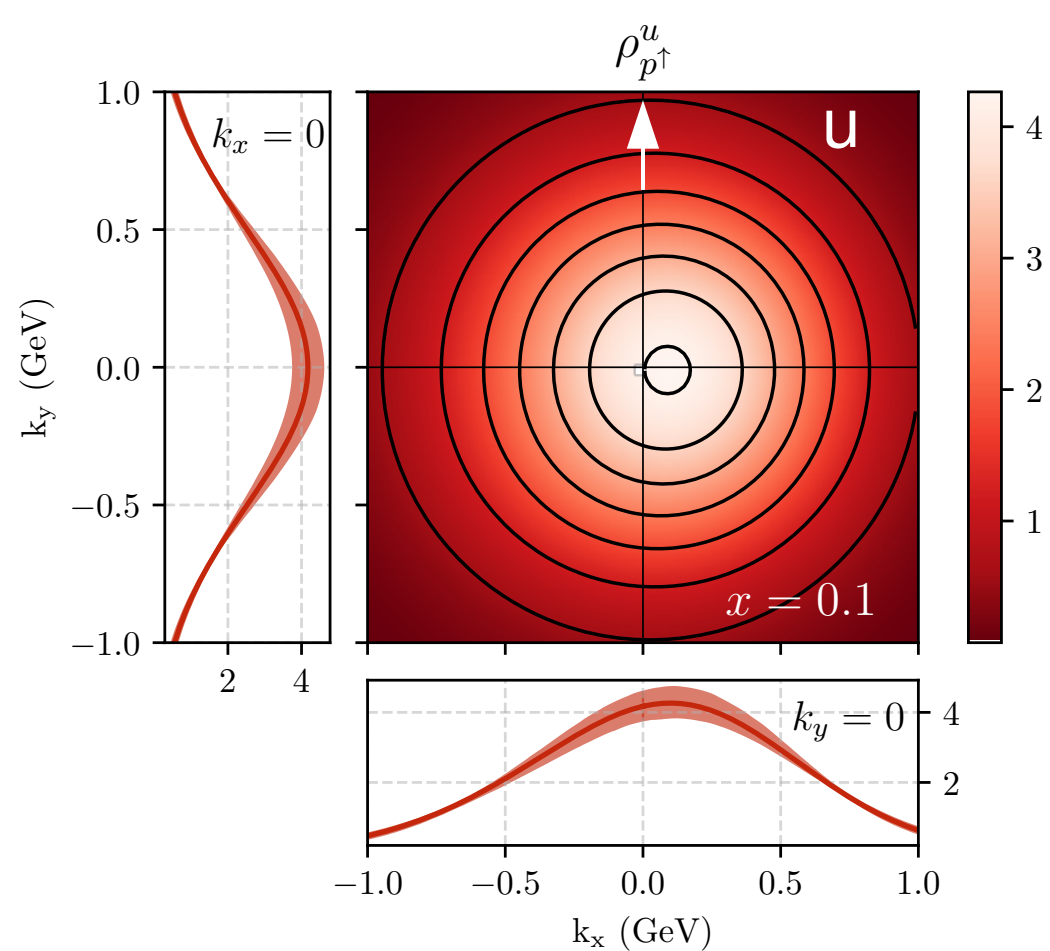
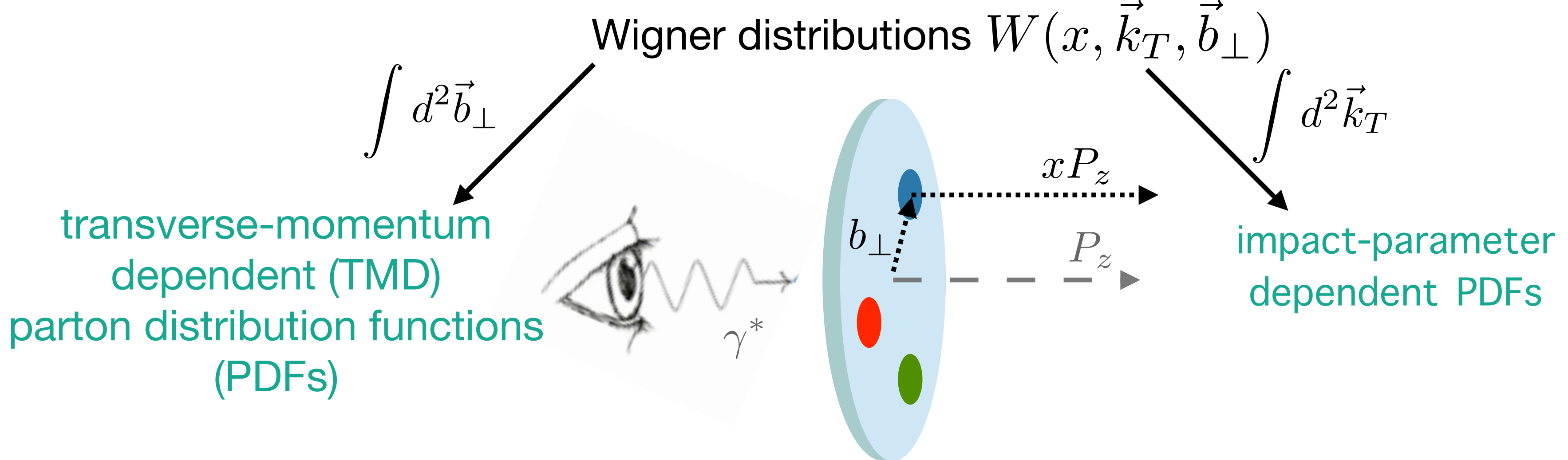
The various dimensions of the nucleon



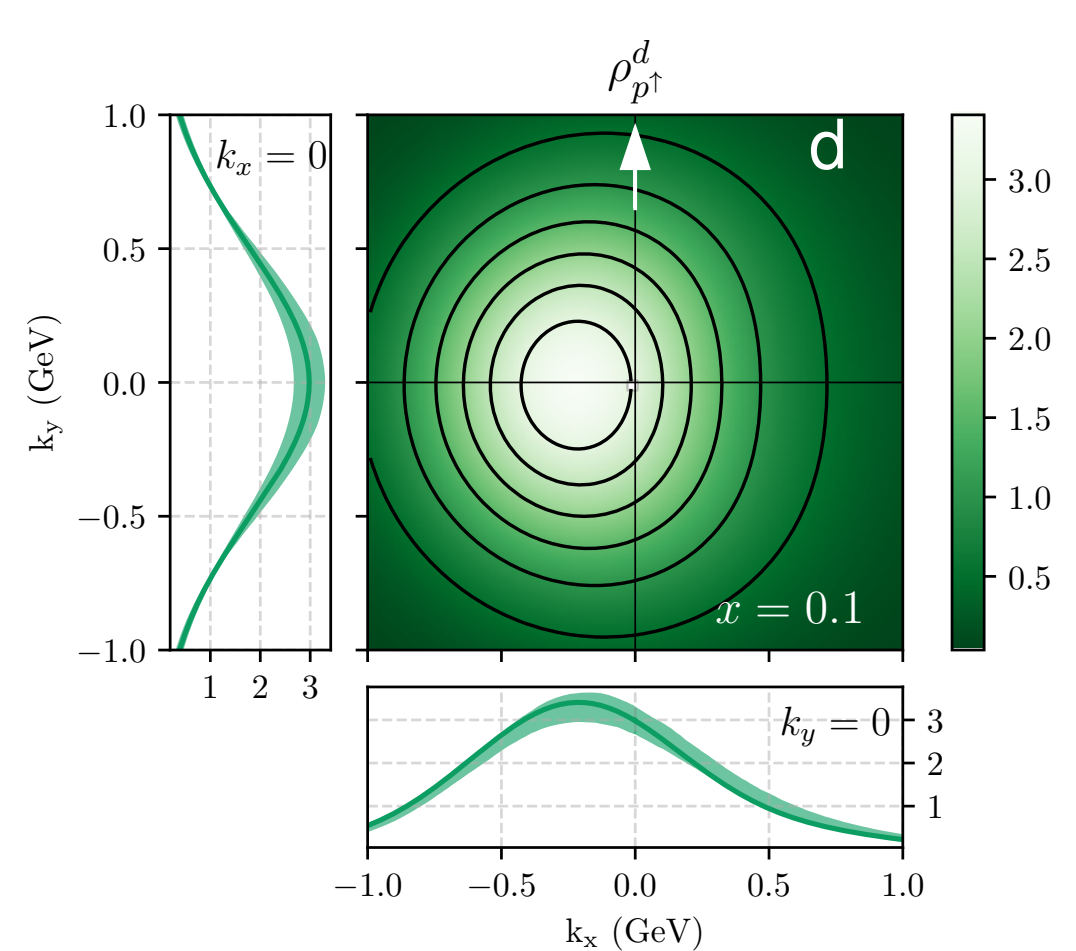
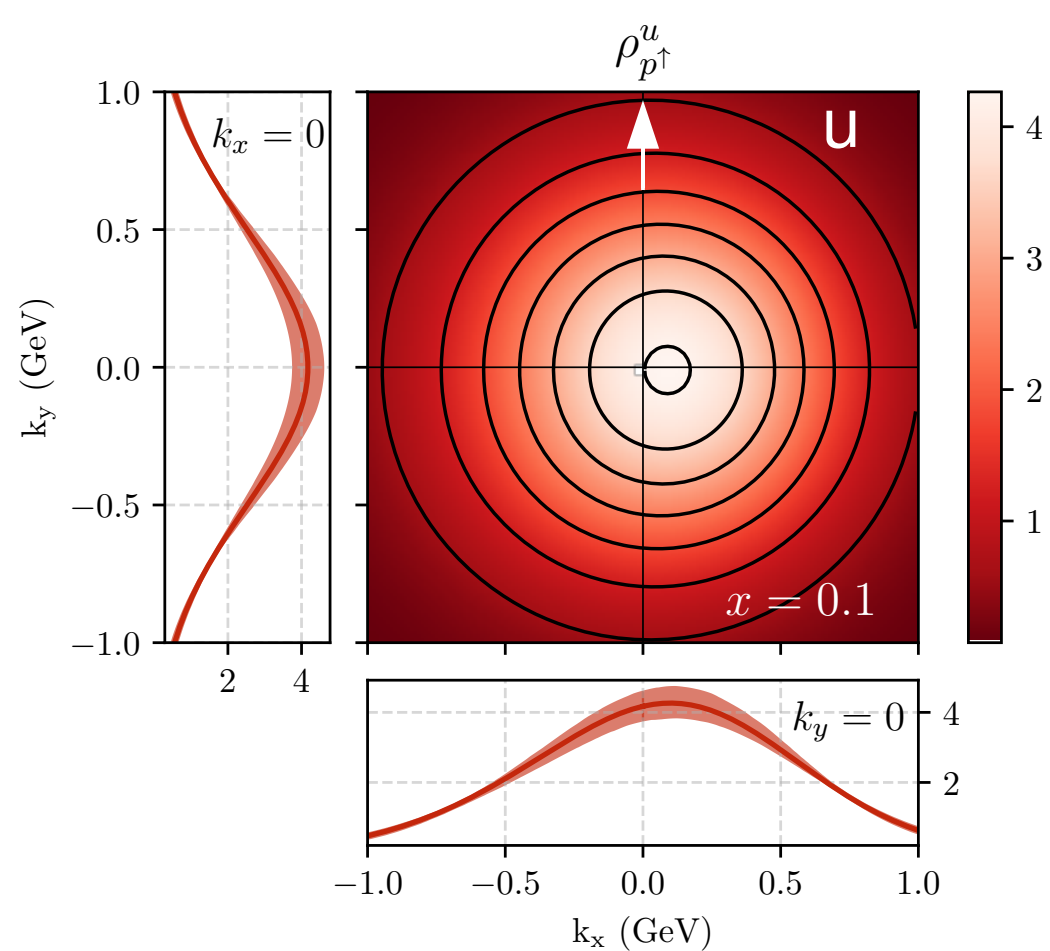
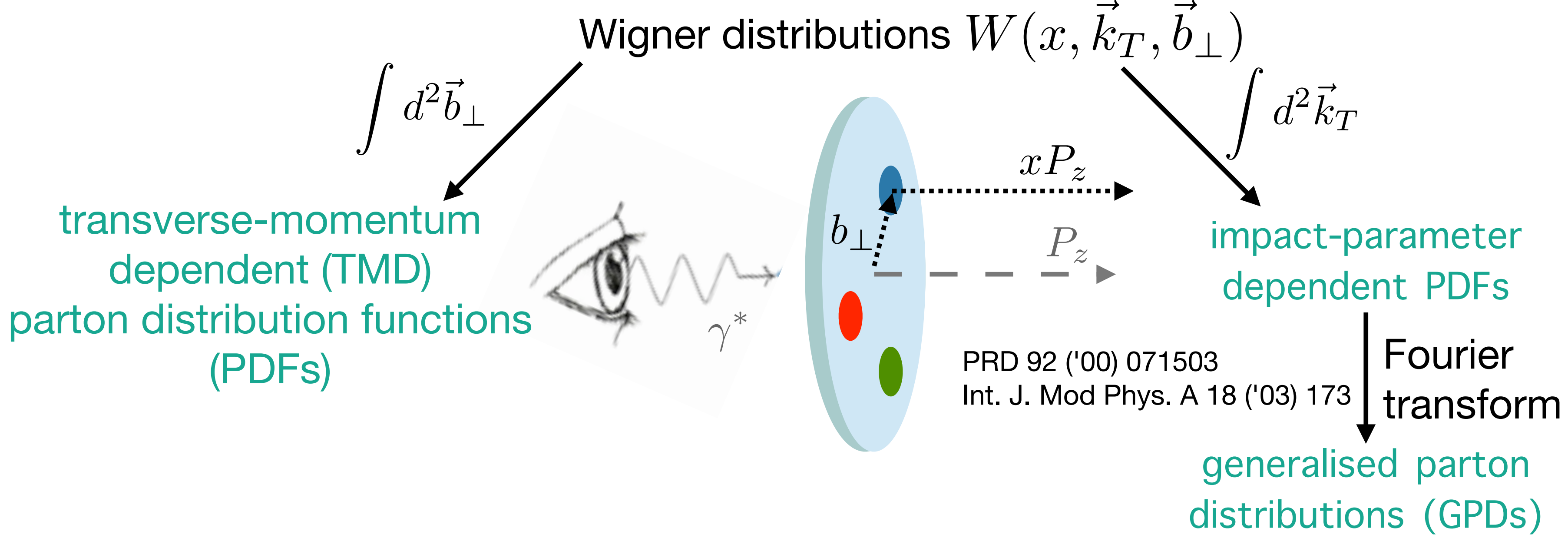
The various dimensions of the nucleon



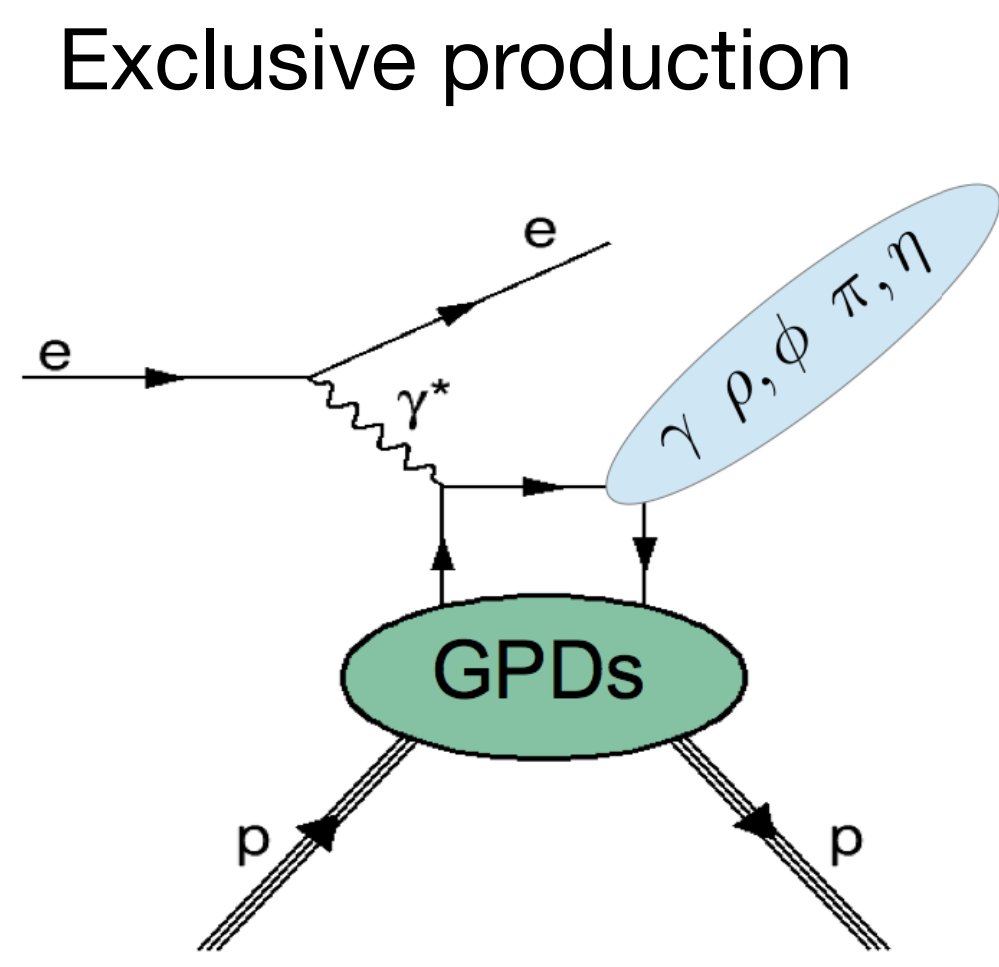
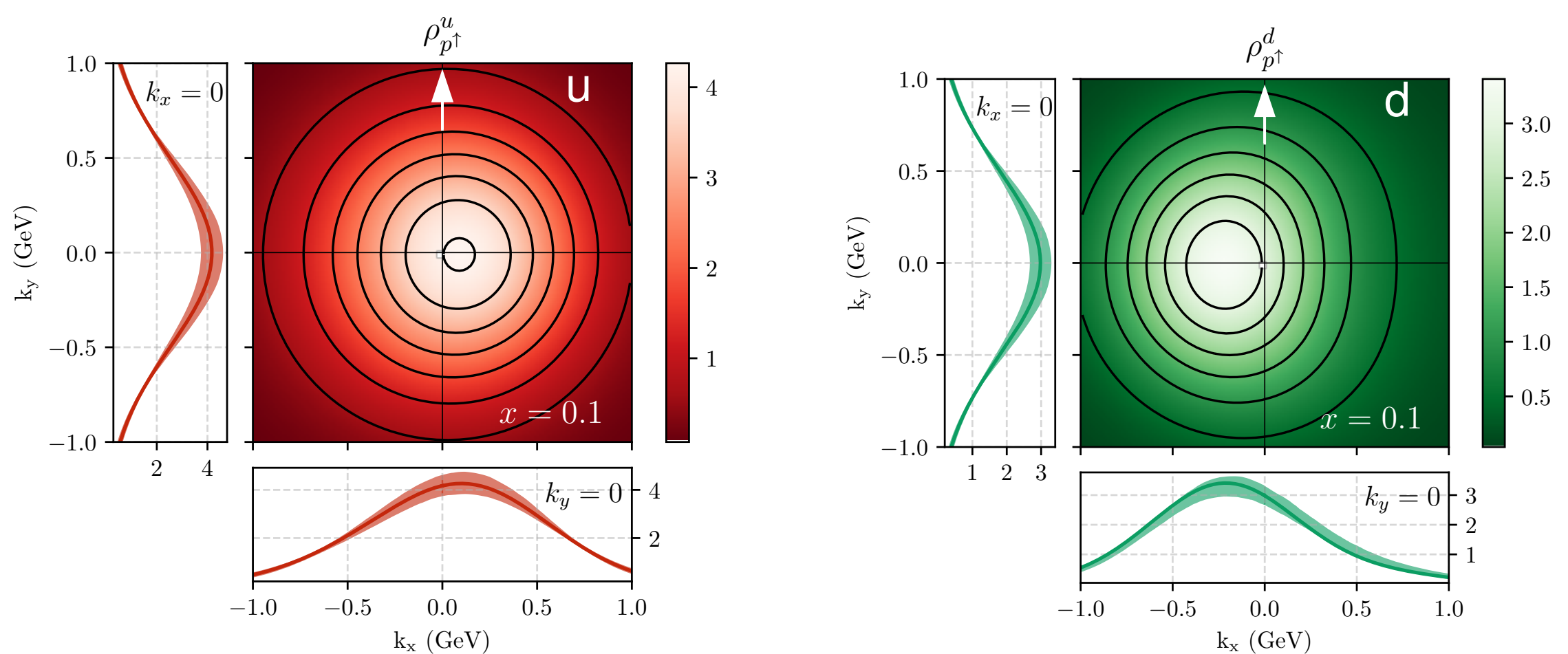
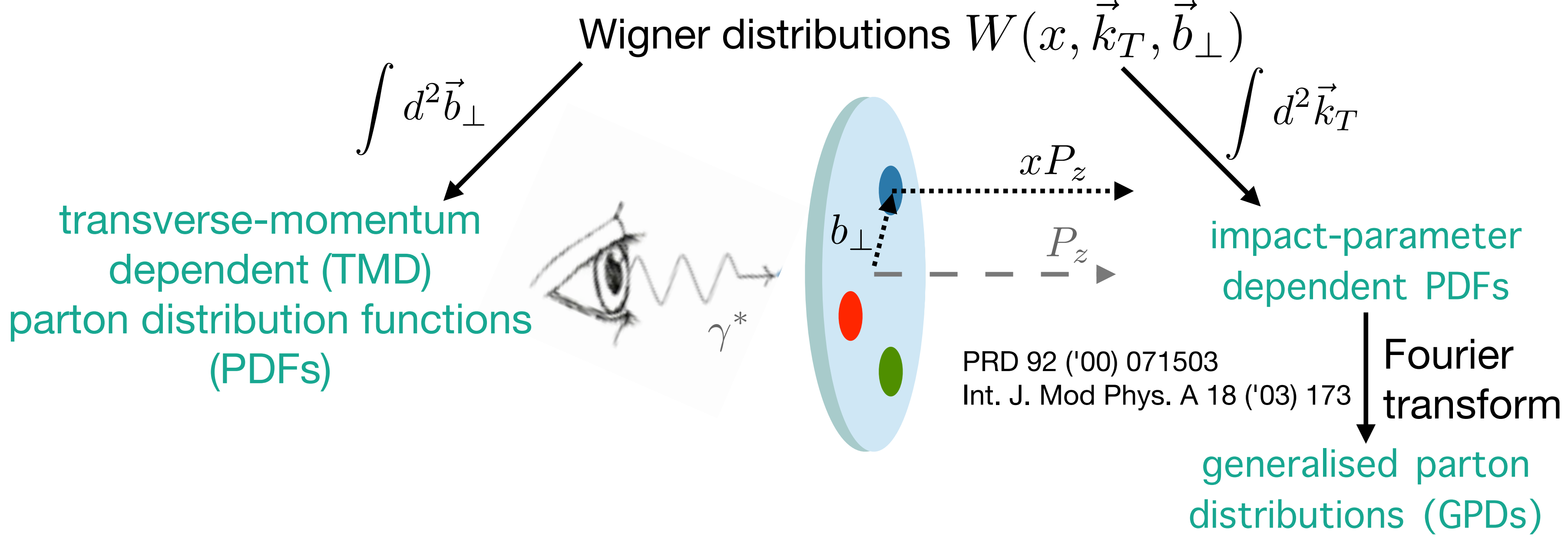
The various dimensions of the nucleon



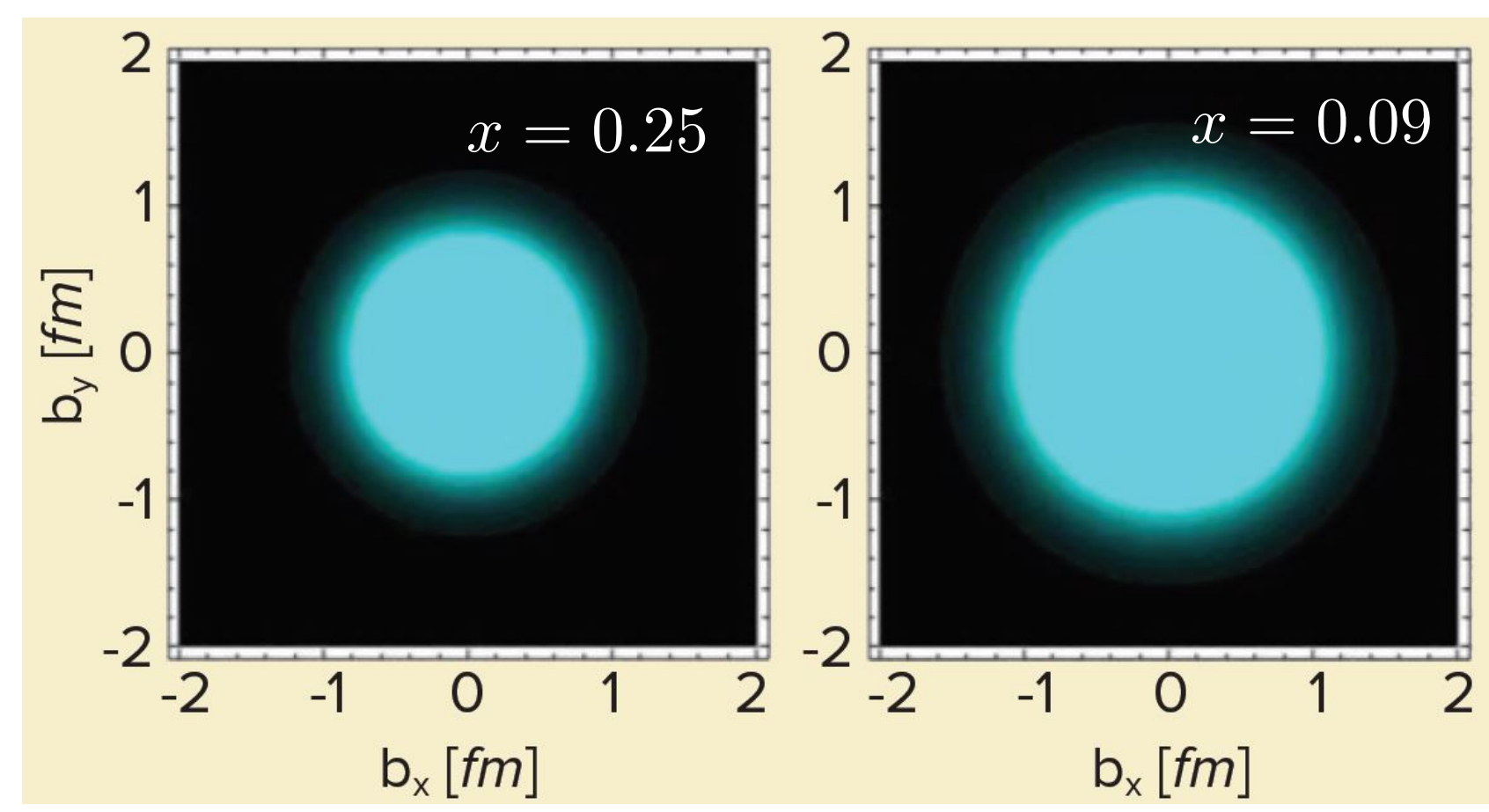
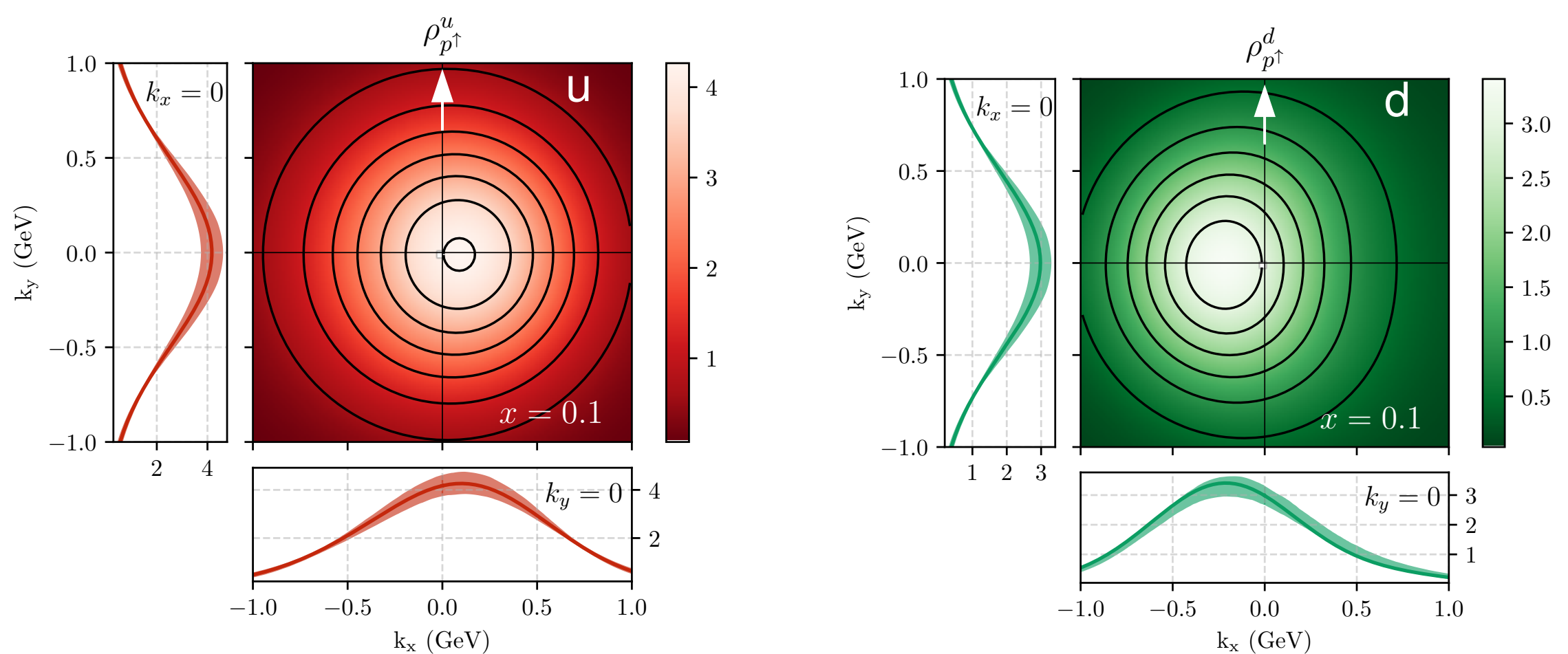
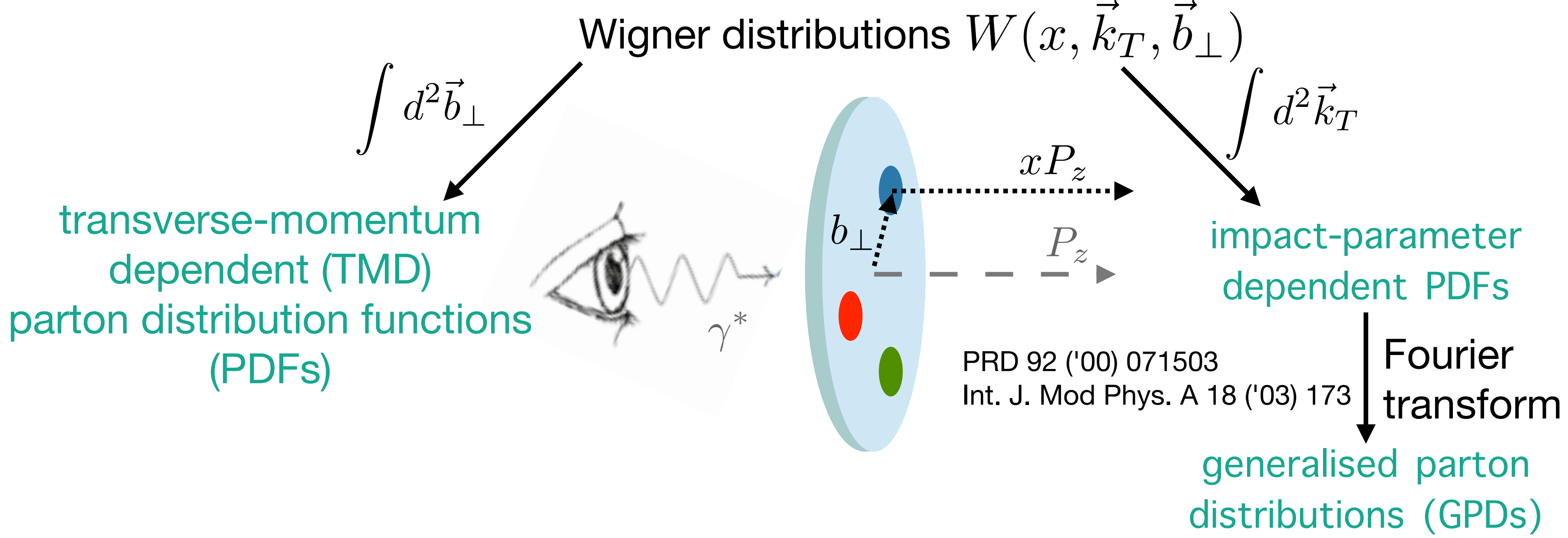
The various dimensions of the nucleon



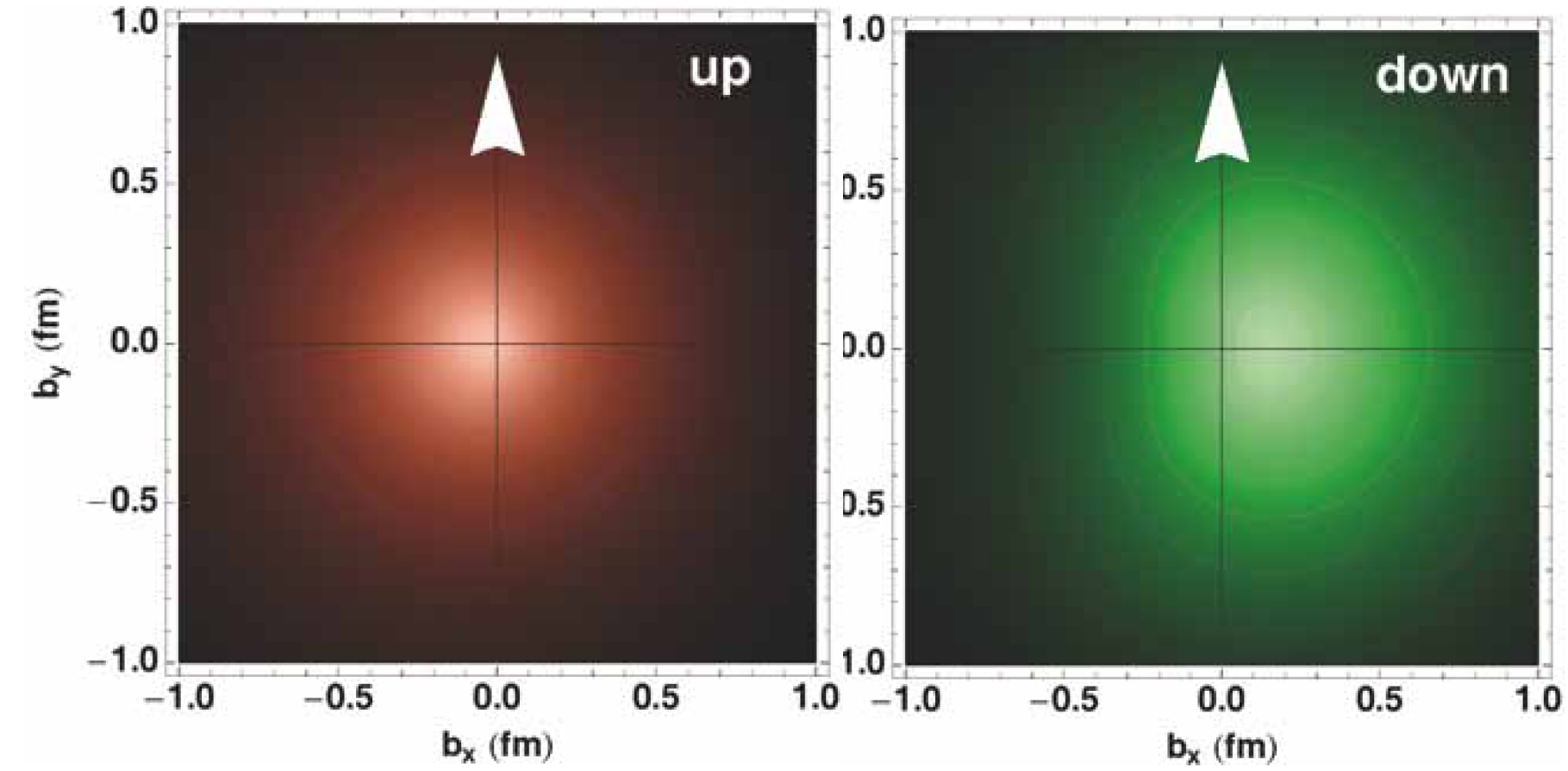
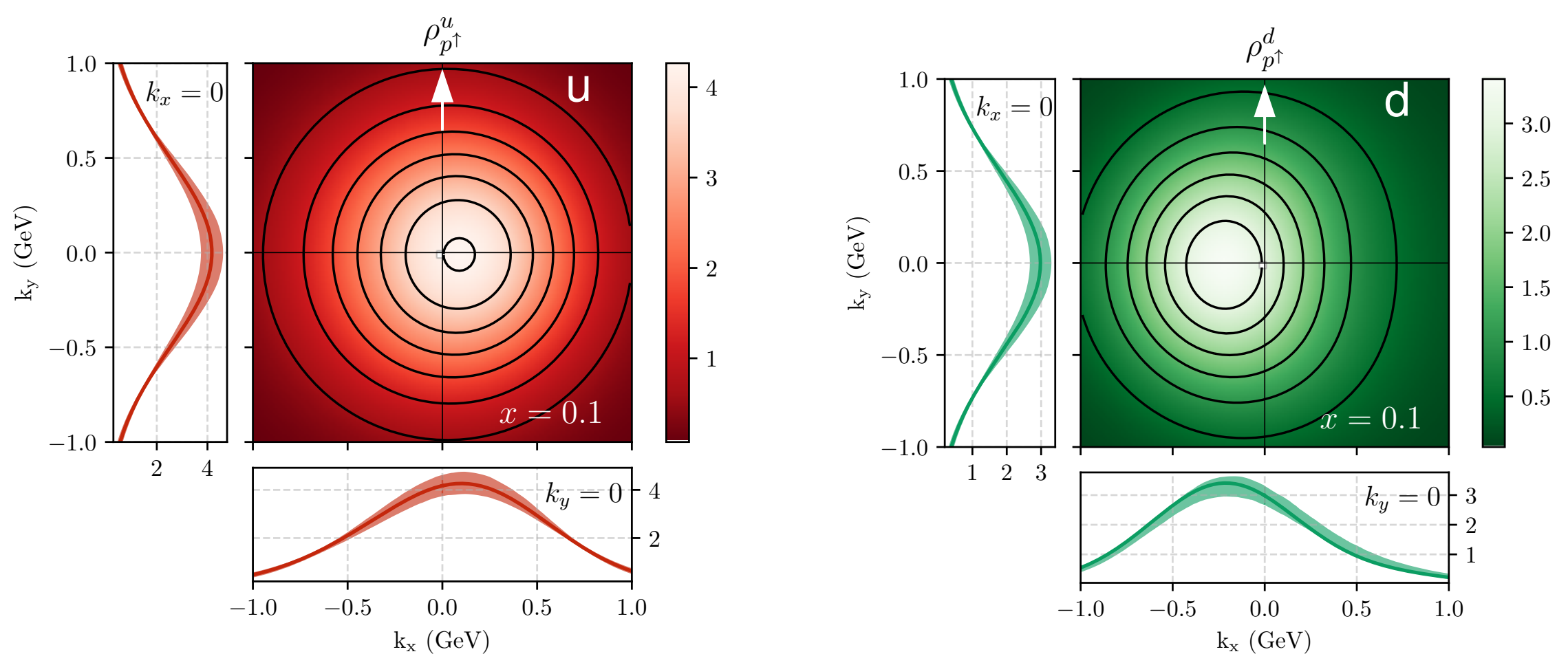
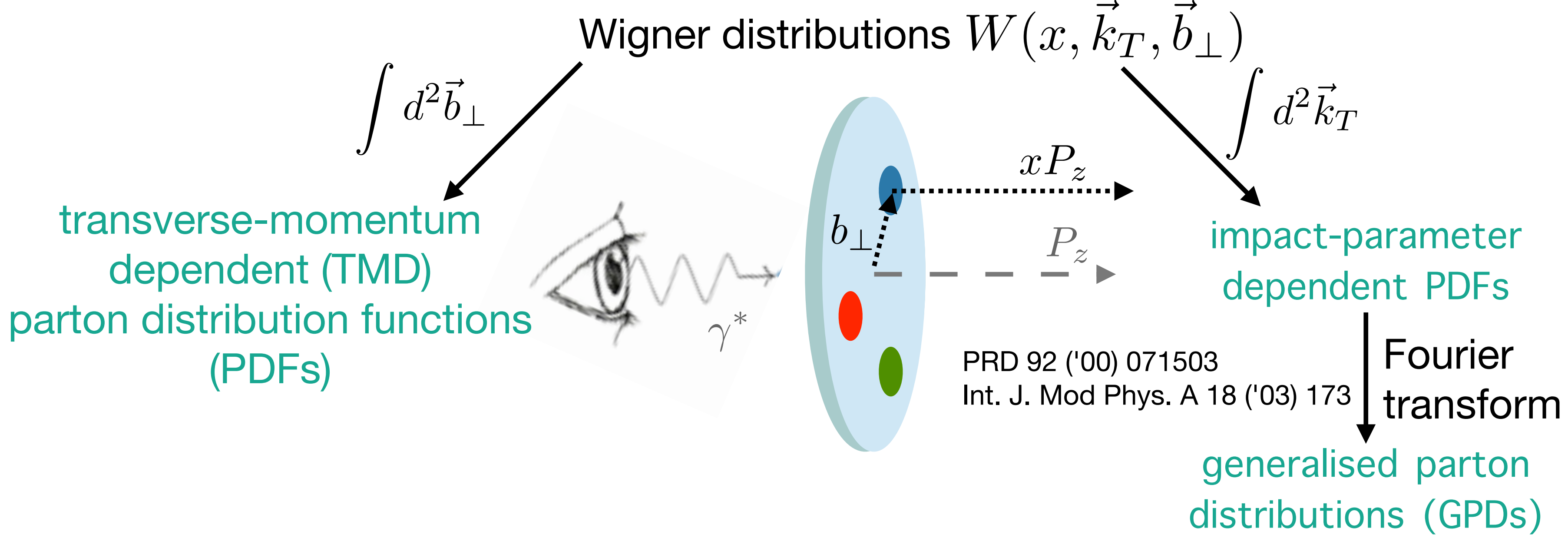
The various dimensions of the nucleon



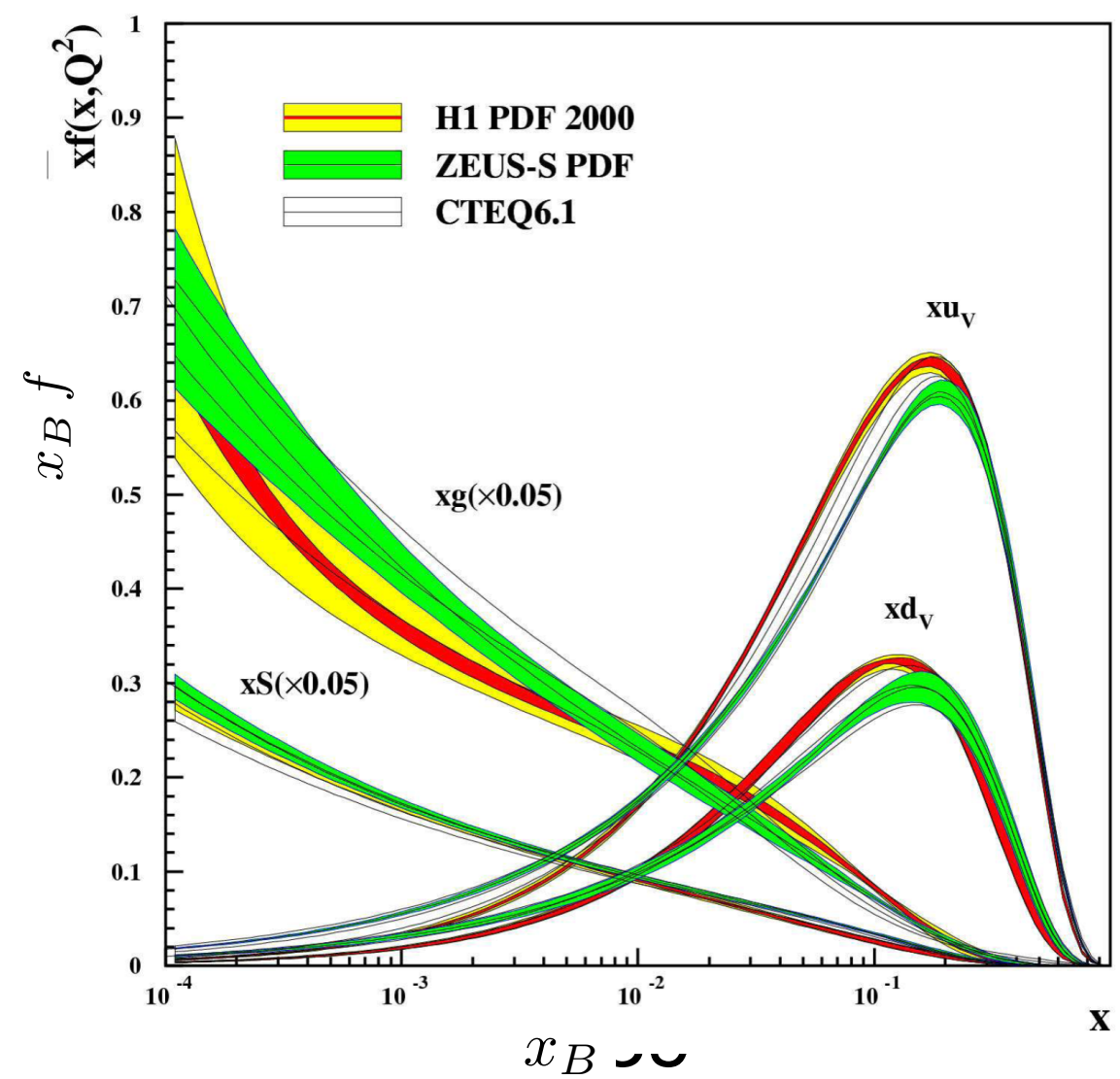
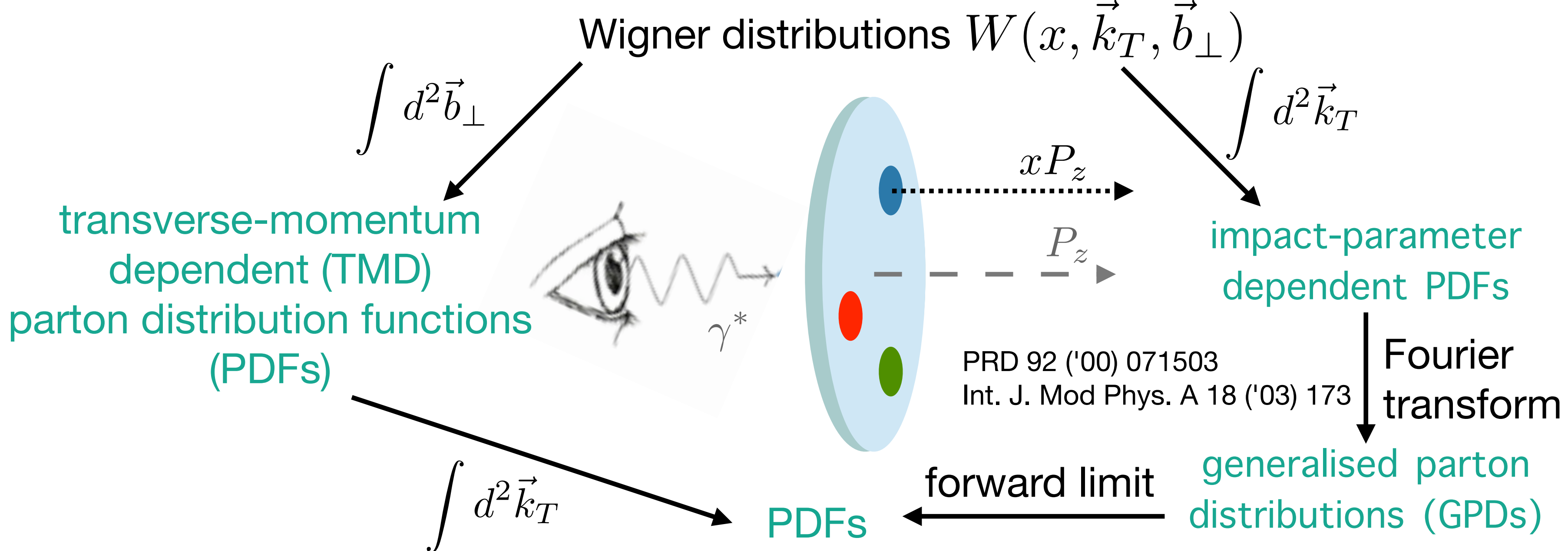
The various dimensions of the nucleon



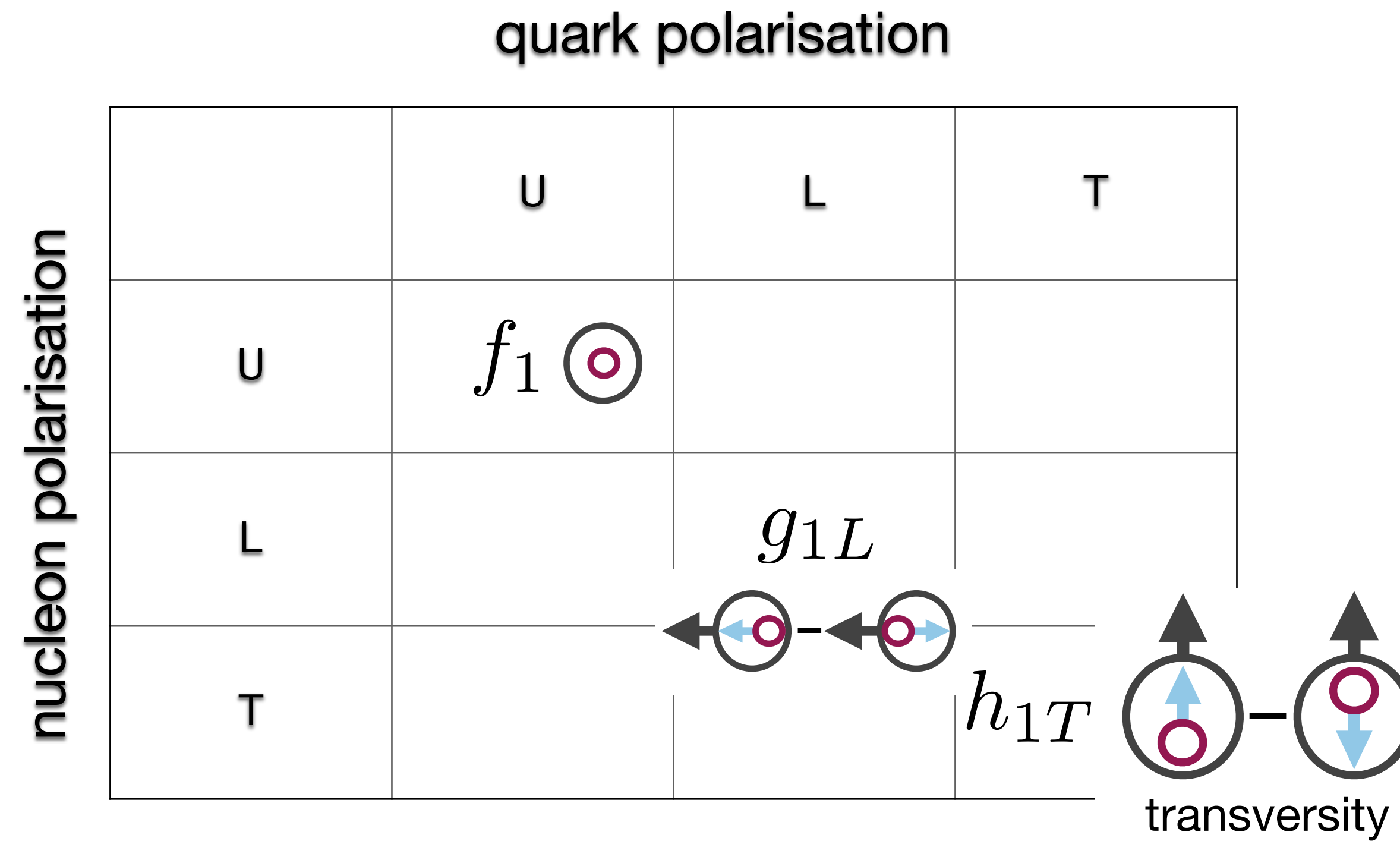
The various dimensions of the nucleon



The various dimensions of the nucleon



Transverse-momentum-dependent PDFs (TMD PDFs)



survive integration of parton
transverse momentum

Transverse-momentum-dependent PDFs (TMD PDFs)

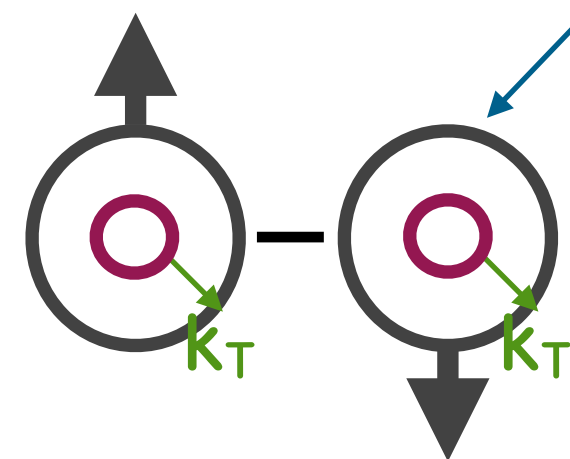
quark polarisation

	U	L	T
nucleon polarisation	U	f_1	h_1^\perp
	L		g_{1L}
	T	f_{1T}^\perp	g_{1T}^\perp
			$h_{1T} h_{1T}^\perp$

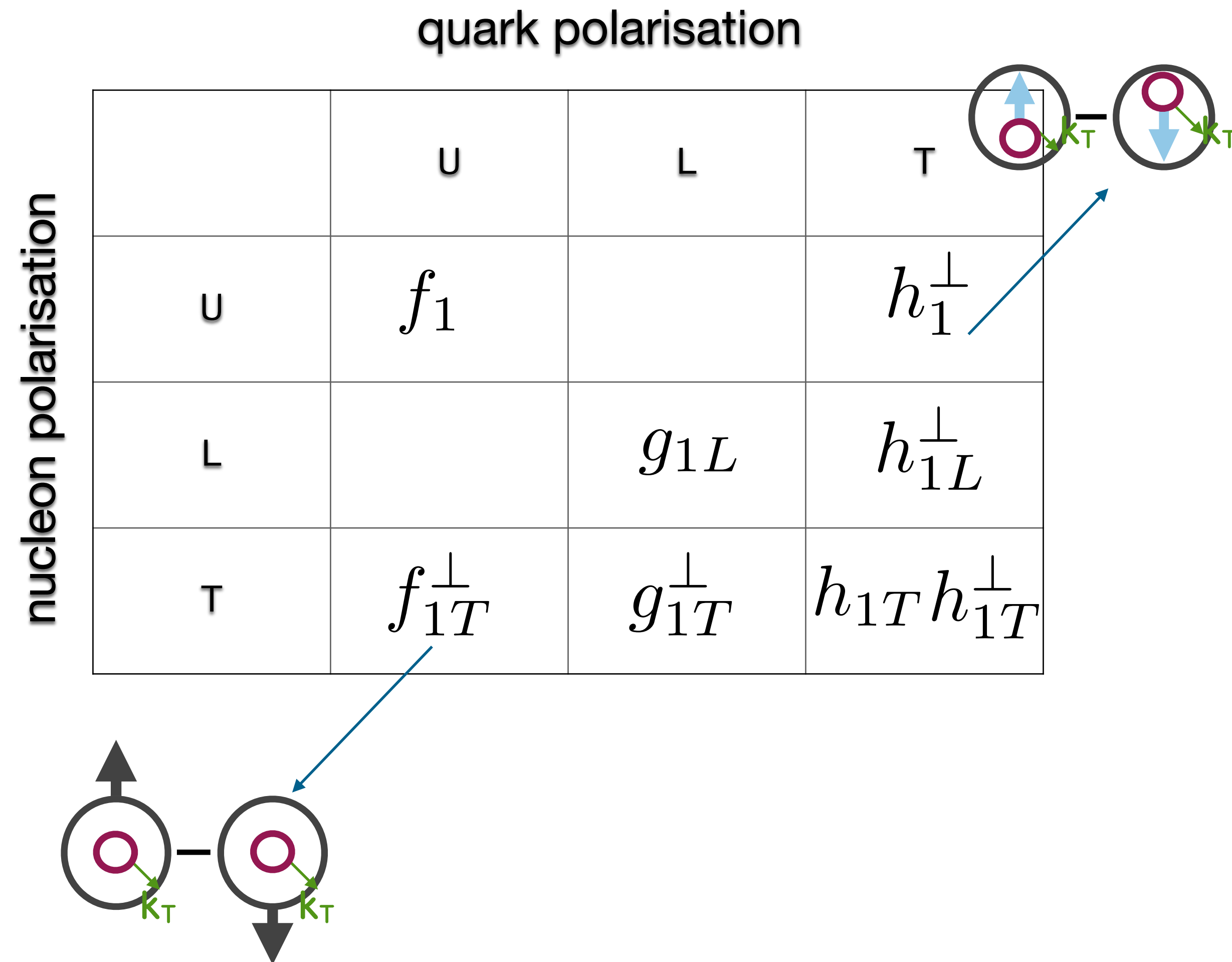
Transverse-momentum-dependent PDFs (TMD PDFs)

quark polarisation

		quark polarisation		
		U	L	T
nucleon polarisation	U	f_1		h_1^\perp
	L		g_{1L}	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	$h_{1T} h_{1T}^\perp$



Transverse-momentum-dependent PDFs (TMD PDFs)



Transverse-momentum-dependent PDFs (TMD PDFs)

quark polarisation

		U	L	T
nucleon polarisation	U	f_1		h_1^\perp
	L		g_{1L}	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp

Chiral odd

Transverse-momentum-dependent PDFs (TMD PDFs)

quark polarisation

		U	L	T
nucleon polarisation	U	f_1		h_1^\perp
	L		g_{1L}	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	$h_{1T} h_{1T}^\perp$

Chiral odd

Naive T-odd

TMD PDFs: correlations

Unpolarized

$$f_1 = \text{[Yellow circle with blue center]}$$

Spin-spin correlations

$$g_1 = \text{[Yellow circle with blue center and right arrow]} - \text{[Yellow circle with blue center and left arrow]}$$

$$h_1 = \text{[Yellow circle with blue center and up arrow]} - \text{[Yellow circle with blue center and down arrow]}$$

$$g_{1T} = \text{[Yellow circle with blue center, right arrow, and up arrow]} - \text{[Yellow circle with blue center, left arrow, and up arrow]}$$

Spin-momentum correlations

$$f_{1T}^\perp = \text{[Yellow circle with blue center and up arrow]} - \text{[Yellow circle with blue center and down arrow]}$$

$$h_1^\perp = \text{[Yellow circle with blue center and down arrow]} - \text{[Yellow circle with blue center and up arrow]}$$

$$h_{1L}^\perp = \text{[Yellow circle with blue center, right arrow, and diagonal arrow]} - \text{[Yellow circle with blue center, right arrow, and diagonal arrow]}$$

Sivers

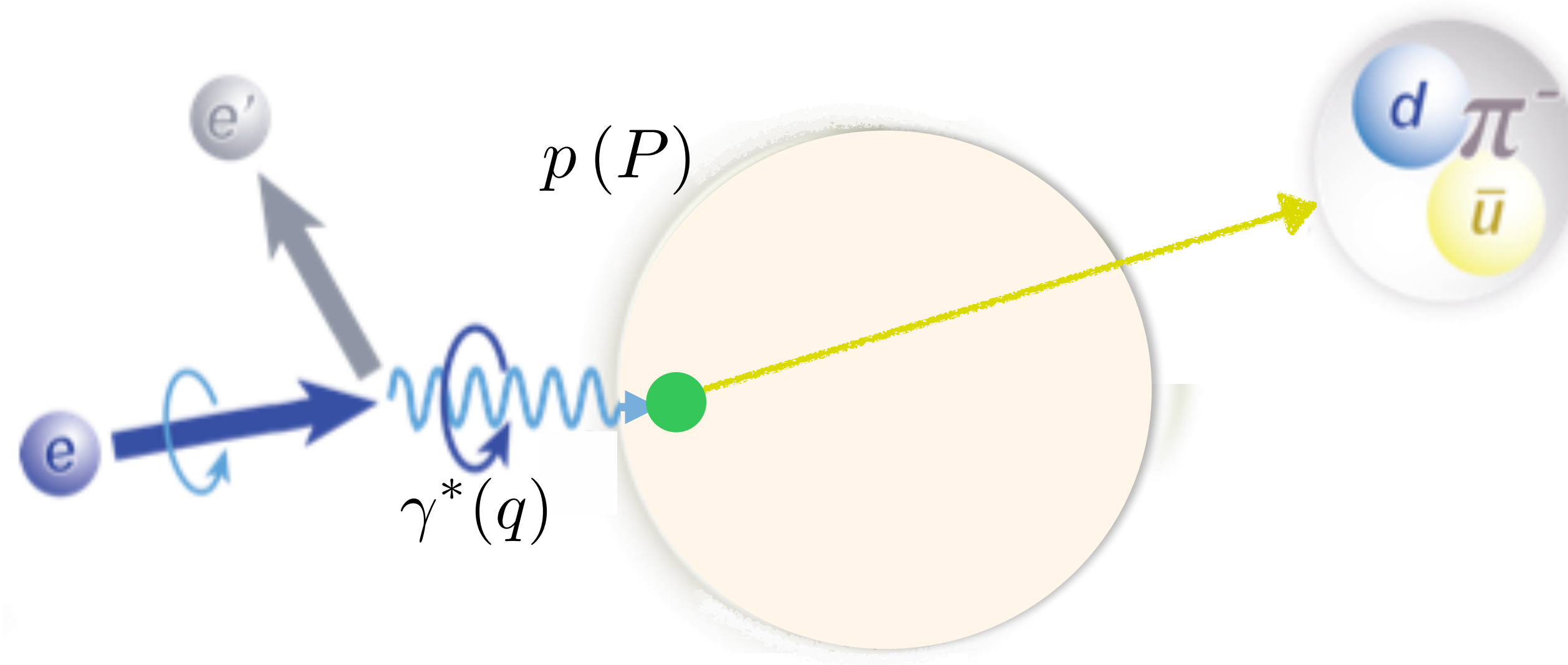
Boer-Mulders

$$h_{1T}^\perp = \text{[Yellow circle with blue center, up arrow, and diagonal arrow]} - \text{[Yellow circle with blue center, up arrow, and diagonal arrow]}$$

TMD semi-inclusive DIS

$$Q^2 = -q^2$$

$$x_B = \frac{Q^2}{2P \cdot q}$$



Highly virtual photon:

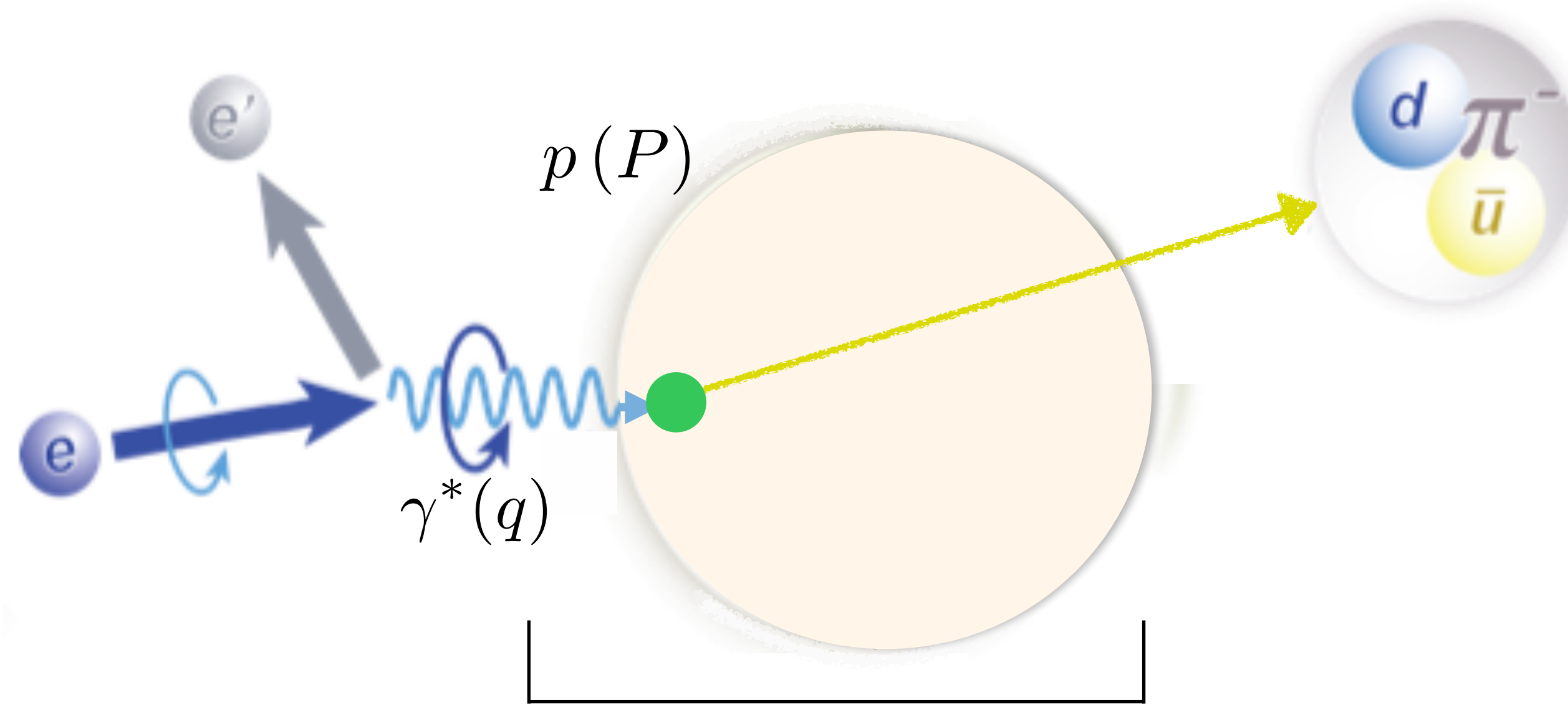
$$Q^2 \gg 1 \text{ GeV}^2$$

provides hard
scale of process

TMD semi-inclusive DIS

$$Q^2 = -q^2$$

$$x_B = \frac{Q^2}{2P \cdot q}$$



Highly virtual photon:

$$Q^2 \gg 1 \text{ GeV}^2$$

provides hard
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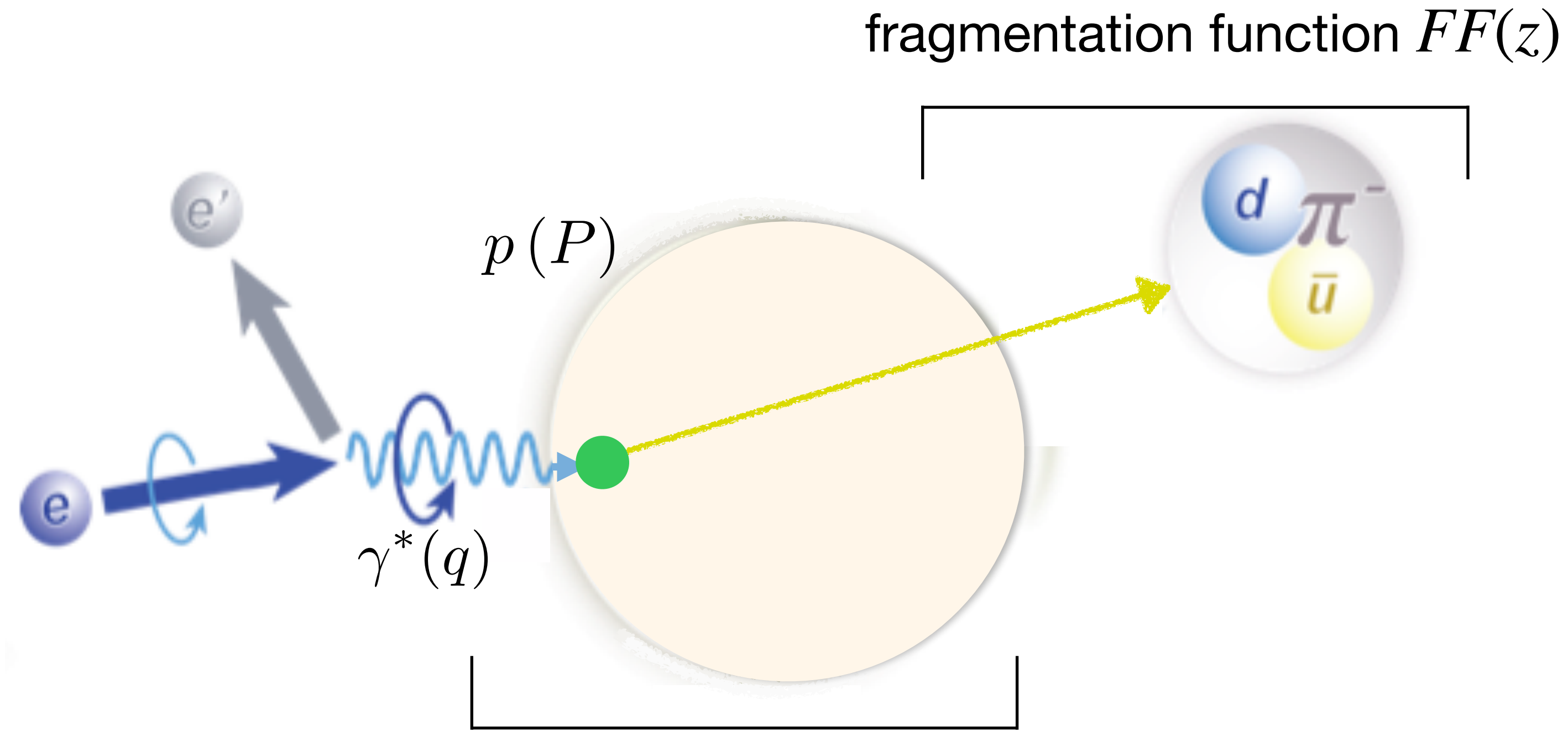
parton distribution function $PDF(x_B)$

TMD semi-inclusive DIS

$$Q^2 = -q^2$$

$$x_B = \frac{Q^2}{2P \cdot q}$$

$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$



Highly virtual photon:

$$Q^2 \gg 1 \text{ GeV}^2$$

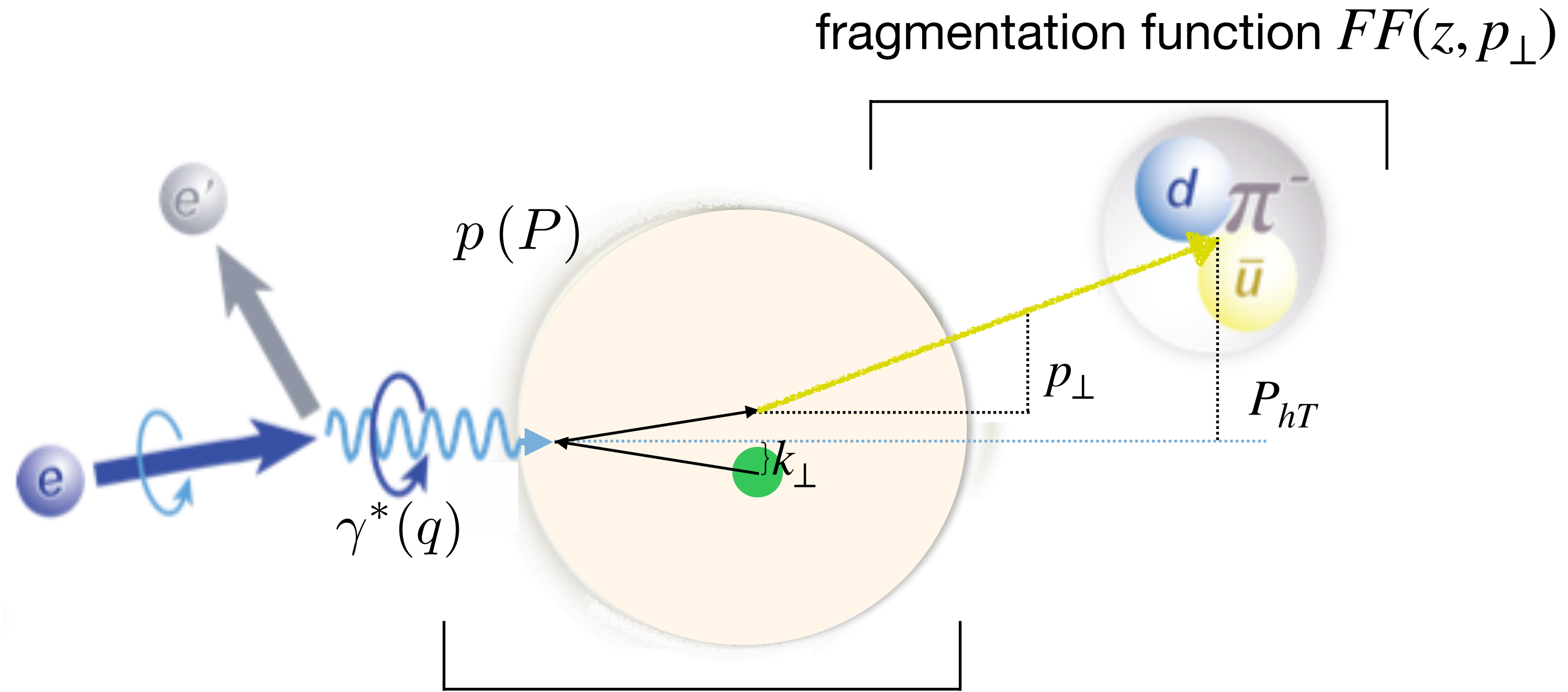
provides hard
scale of process

TMD semi-inclusive DIS

$$Q^2 = -q^2$$

$$x_B = \frac{Q^2}{2P \cdot q}$$

$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$



Transverse-momentum-dependent (TMD)
parton distribution function $PDF(x_B, k_{\perp})$

Highly virtual photon:
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provides hard
scale of process

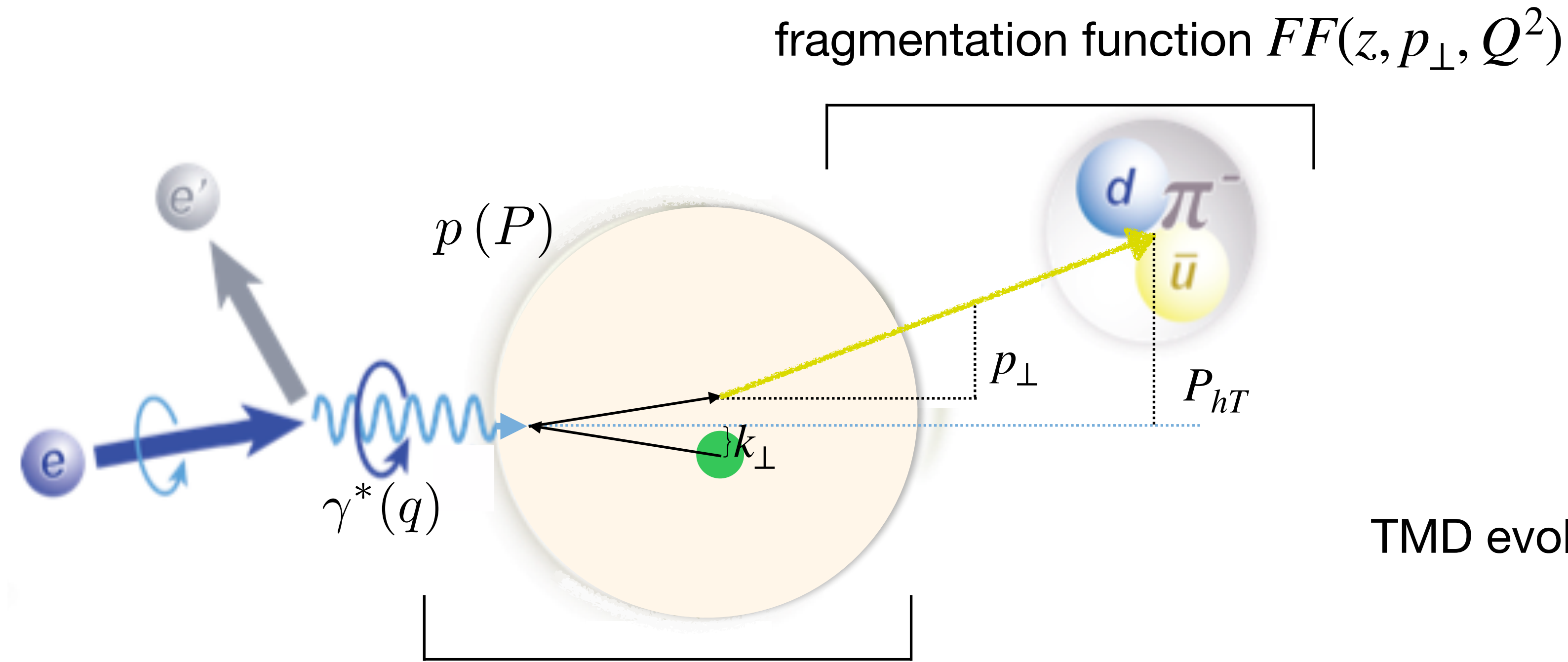
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TMD evolution

Transverse-momentum-dependent (TMD)
 parton distribution function $PDF(x_B, k_{\perp}, Q^2)$



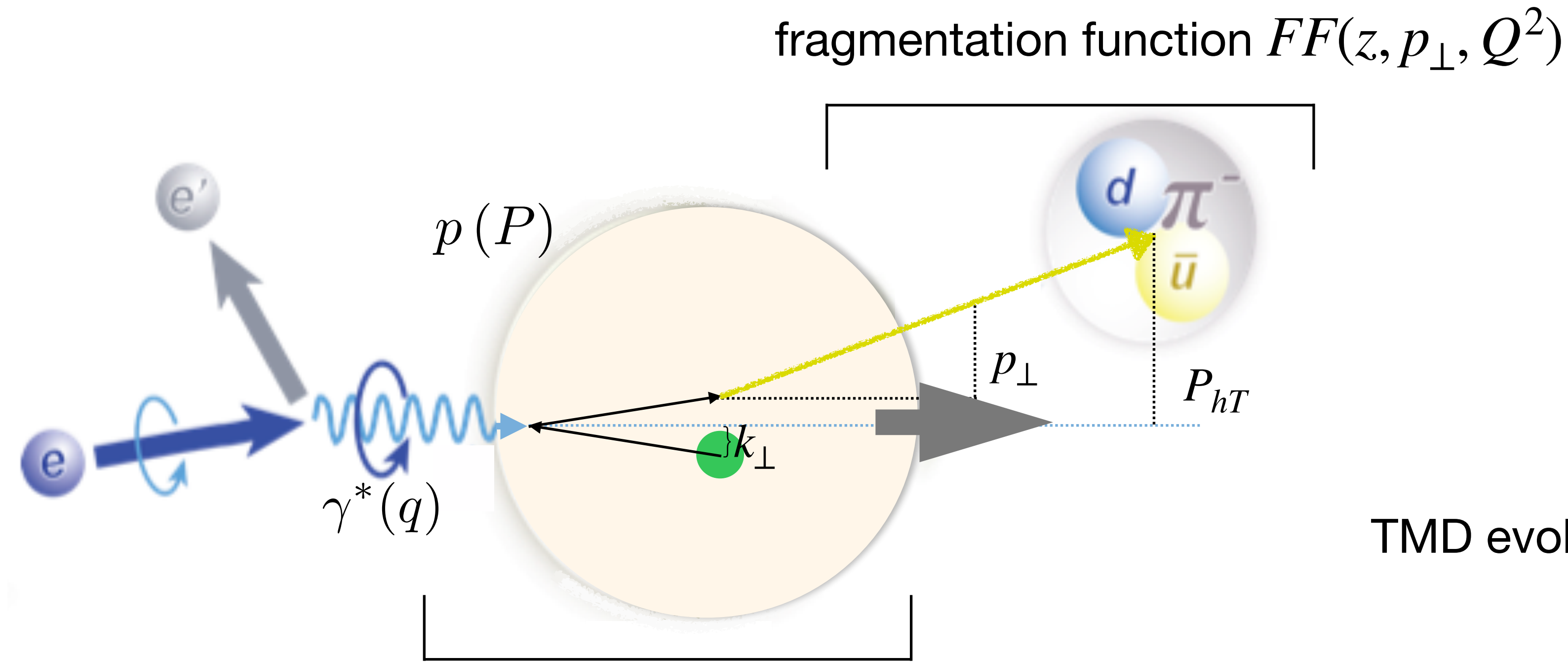
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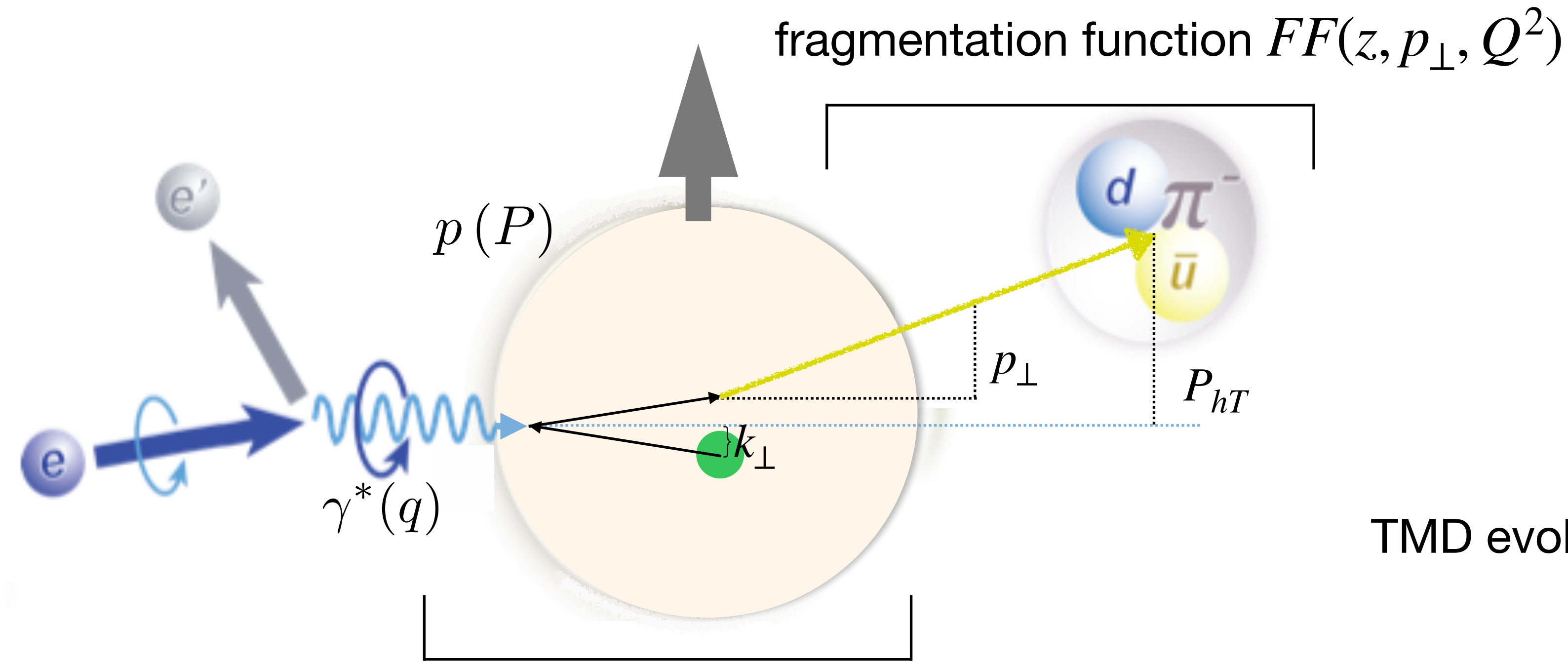
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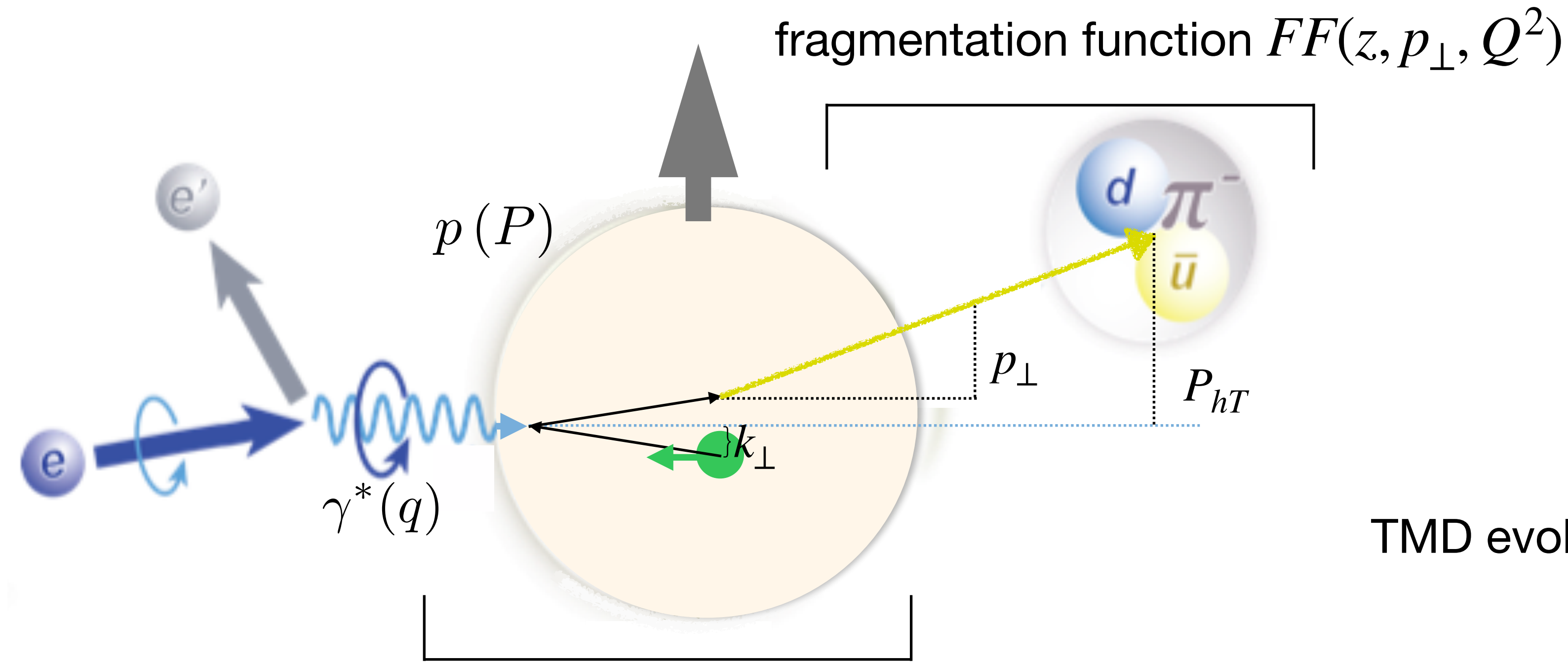
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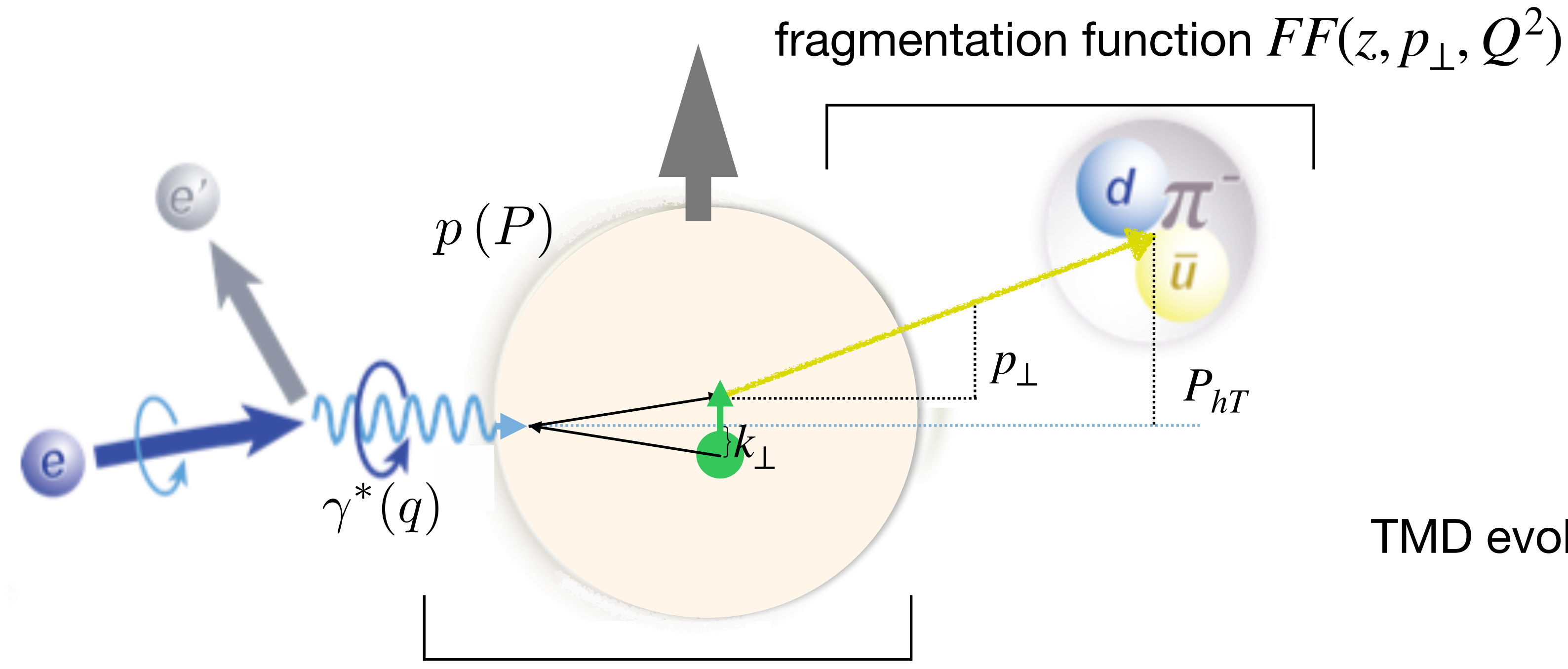
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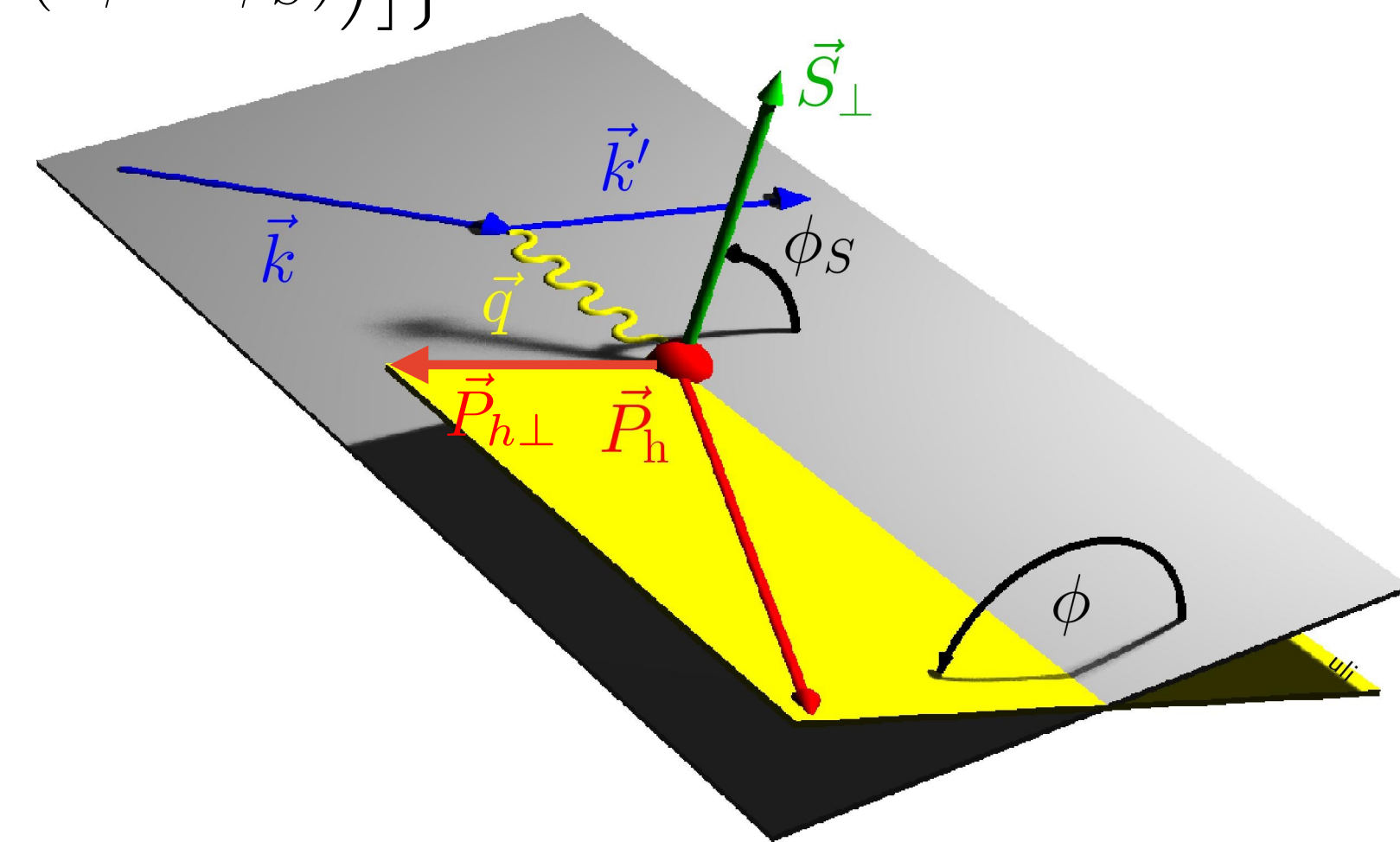
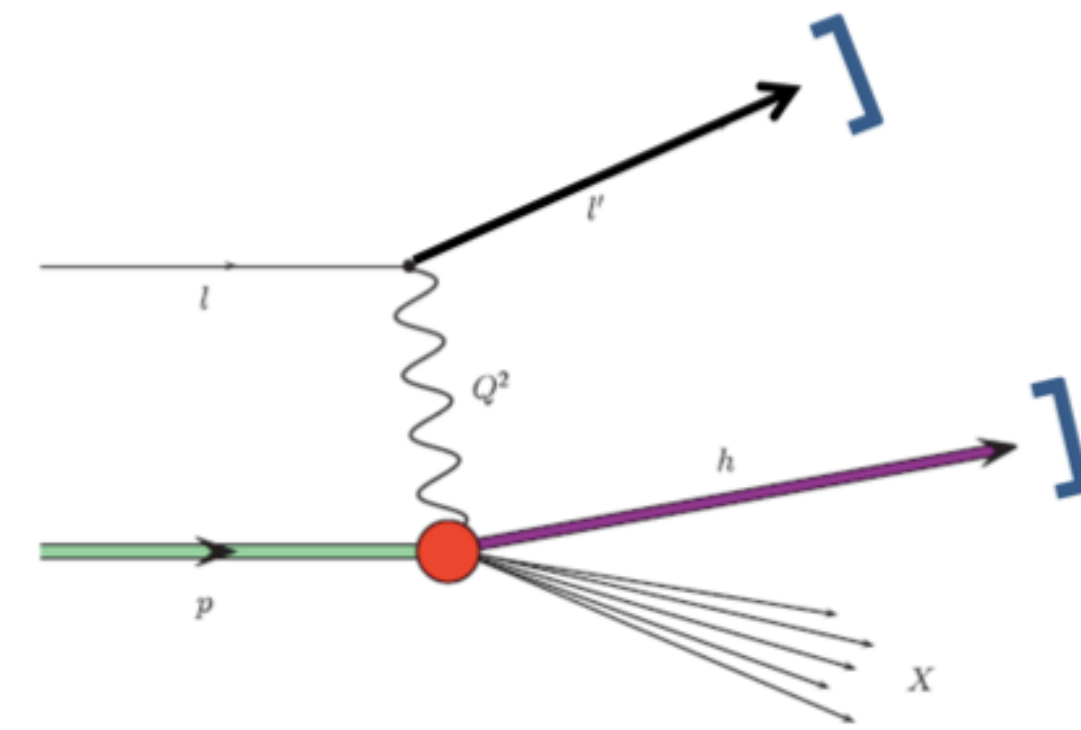
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TMD evolution

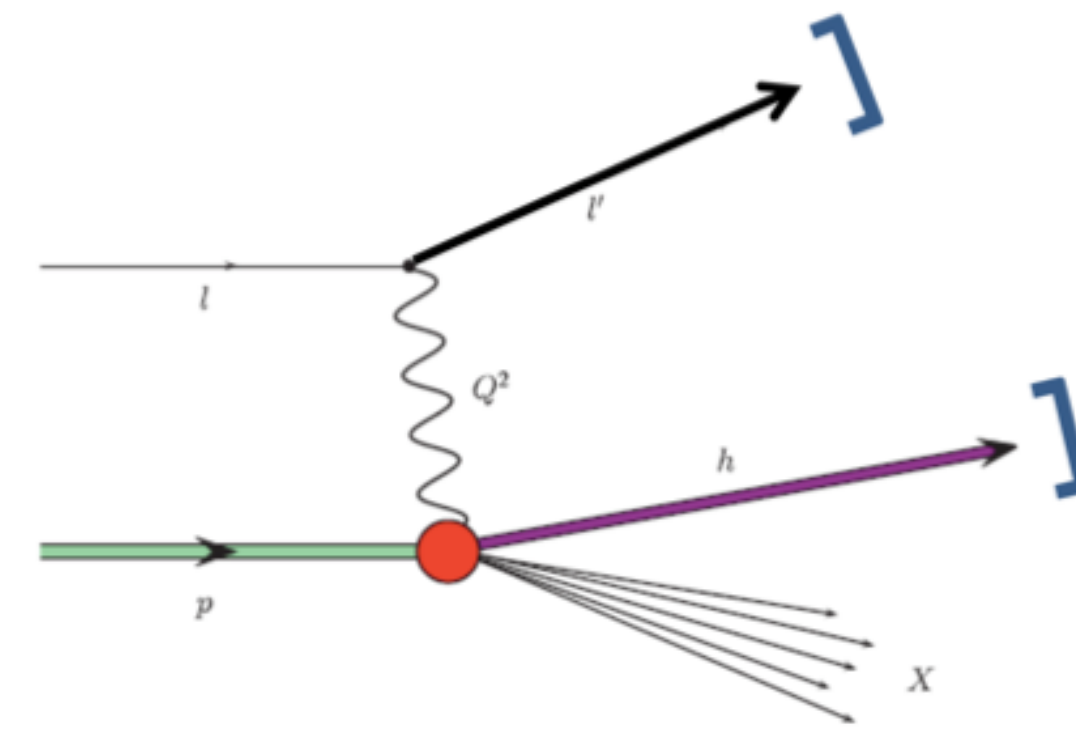


Semi-inclusive DIS cross section

$$\begin{aligned}
 \sigma^h(\phi, \phi_S) = & \sigma_{UU}^h \left\{ 1 + 2\langle \cos(\phi) \rangle_{UU}^h \cos(\phi) + 2\langle \cos(2\phi) \rangle_{UU}^h \cos(2\phi) \right. \\
 & + \lambda_l 2\langle \sin(\phi) \rangle_{LU}^h \sin(\phi) \\
 & + S_L \left[2\langle \sin(\phi) \rangle_{UL}^h \sin(\phi) + 2\langle \sin(2\phi) \rangle_{UL}^h \sin(2\phi) \right. \\
 & + \lambda_l \left(2\langle \cos(0\phi) \rangle_{LL}^h \cos(0\phi) + 2\langle \cos(\phi) \rangle_{LL}^h \cos(\phi) \right) \left. \right] \\
 & + S_T \left[2\langle \sin(\phi - \phi_S) \rangle_{UT}^h \sin(\phi - \phi_S) + 2\langle \sin(\phi + \phi_S) \rangle_{UT}^h \sin(\phi + \phi_S) \right. \\
 & + 2\langle \sin(3\phi - \phi_S) \rangle_{UT}^h \sin(3\phi - \phi_S) + 2\langle \sin(\phi_S) \rangle_{UT}^h \sin(\phi_S) \\
 & + 2\langle \sin(2\phi - \phi_S) \rangle_{UT}^h \sin(2\phi - \phi_S) \\
 & + \lambda_l \left(2\langle \cos(\phi - \phi_S) \rangle_{LT}^h \cos(\phi - \phi_S) \right. \\
 & \left. \left. + 2\langle \cos(\phi_S) \rangle_{LT}^h \cos(\phi_S) + 2\langle \cos(2\phi - \phi_S) \rangle_{LT}^h \cos(2\phi - \phi_S) \right) \right] \left. \right\}
 \end{aligned}$$

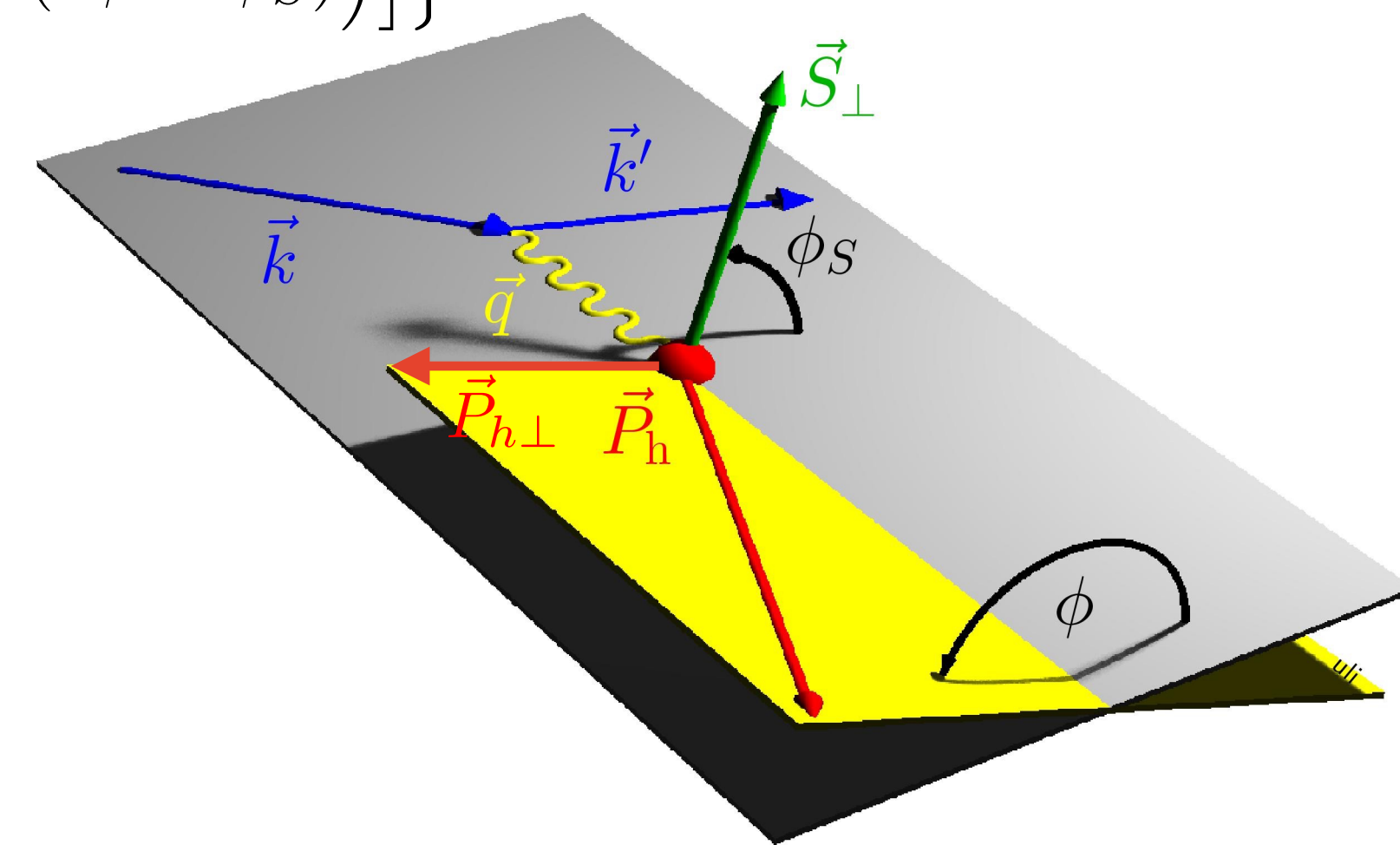


Semi-inclusive DIS cross section



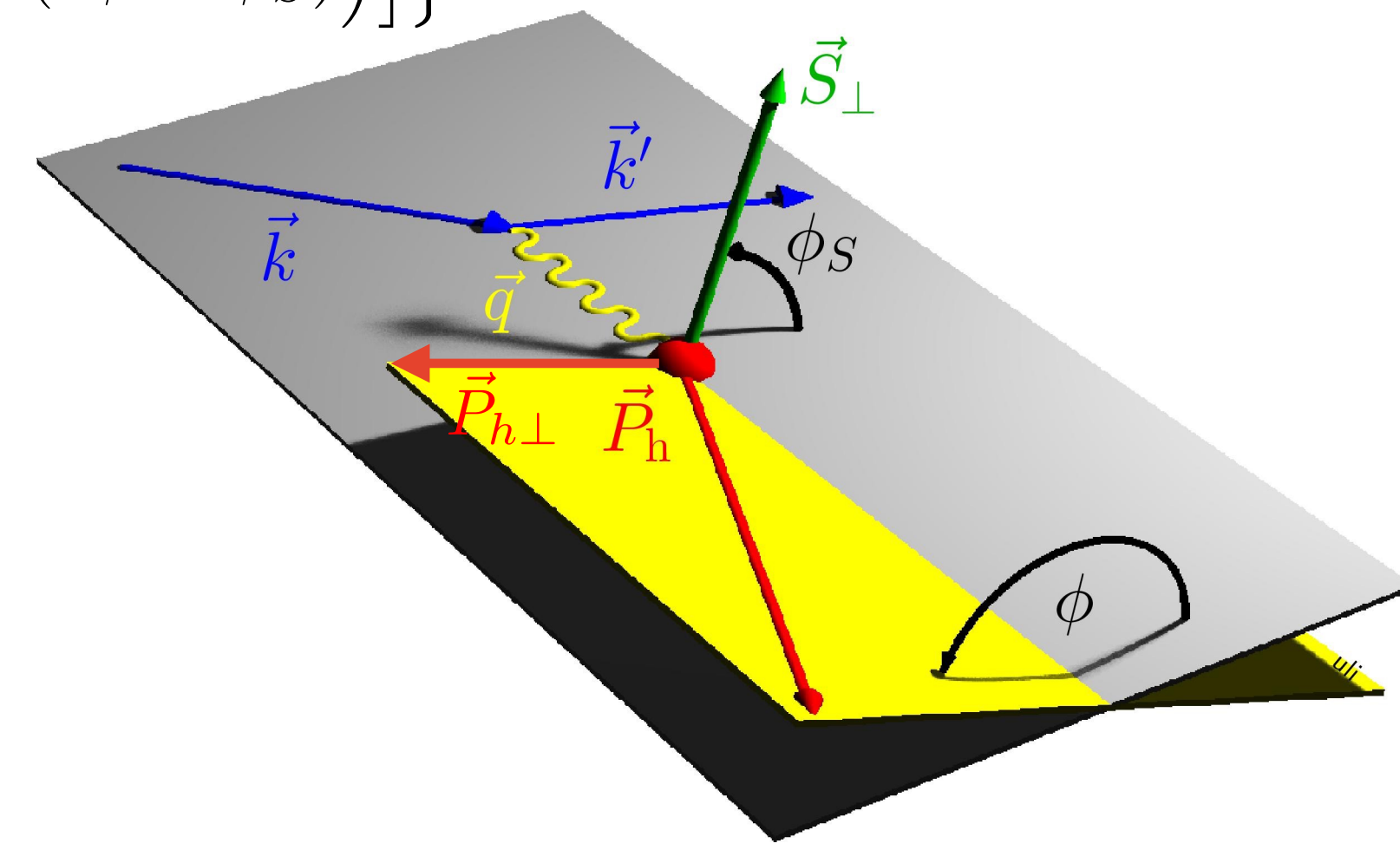
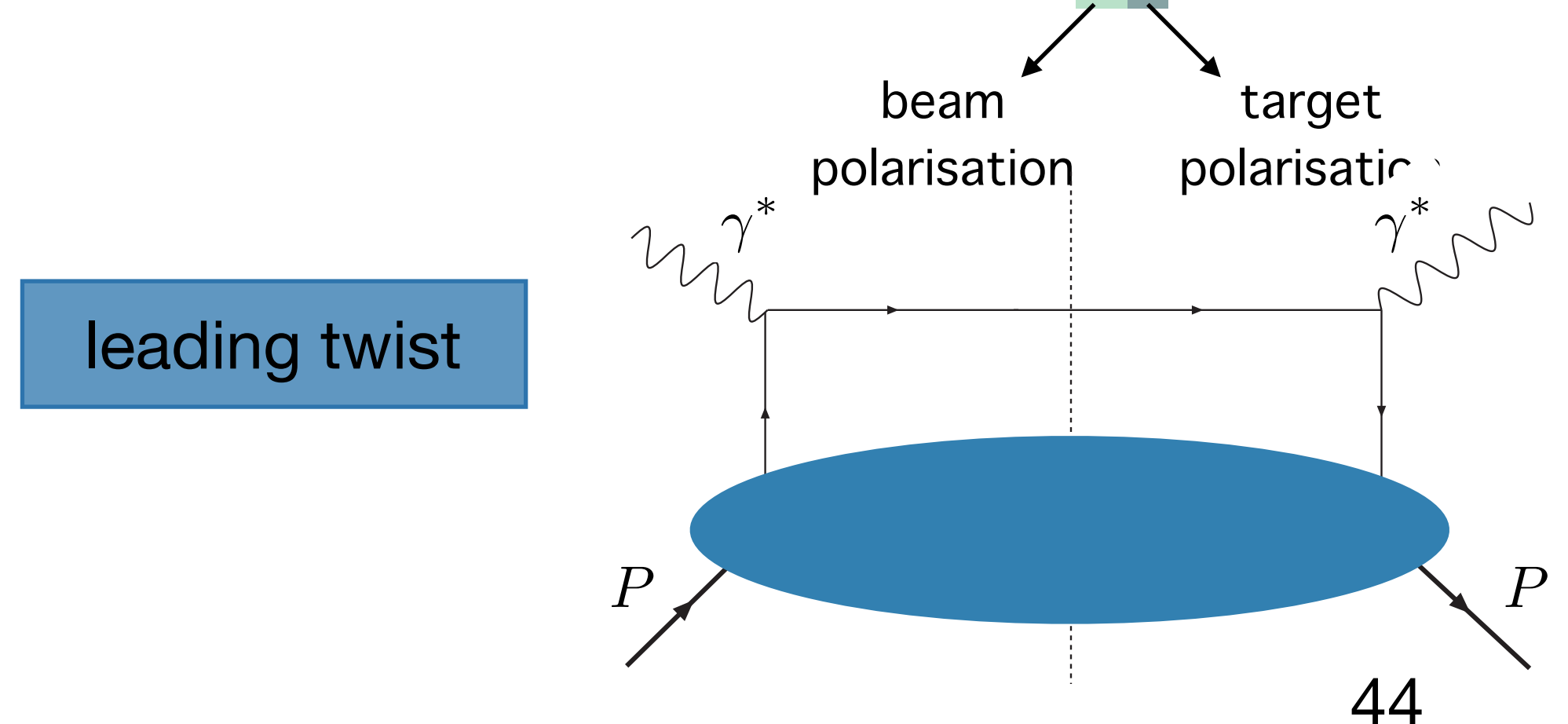
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 & + \lambda_l 2\langle \sin(\phi) \rangle_{LU}^h \sin(\phi) \\
 \text{longitudinal target} & \leftarrow S_L \left[2\langle \sin(\phi) \rangle_{UL}^h \sin(\phi) + 2\langle \sin(2\phi) \rangle_{UL}^h \sin(2\phi) \right. \\
 \text{polarisation} & \left. + \lambda_l \left(2\langle \cos(0\phi) \rangle_{LL}^h \cos(0\phi) + 2\langle \cos(\phi) \rangle_{LL}^h \cos(\phi) \right) \right] \\
 \text{transverse target} & \leftarrow S_T \left[2\langle \sin(\phi - \phi_S) \rangle_{UT}^h \sin(\phi - \phi_S) + 2\langle \sin(\phi + \phi_S) \rangle_{UT}^h \sin(\phi + \phi_S) \right. \\
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 & + 2\langle \sin(2\phi - \phi_S) \rangle_{UT}^h \sin(2\phi - \phi_S) \\
 \text{beam} & \leftarrow \lambda_l \left(2\langle \cos(\phi - \phi_S) \rangle_{LT}^h \cos(\phi - \phi_S) \right. \\
 \text{polarisation} & \left. + 2\langle \cos(\phi_S) \rangle_{LT}^h \cos(\phi_S) + 2\langle \cos(2\phi - \phi_S) \rangle_{LT}^h \cos(2\phi - \phi_S) \right) \left. \right\}
 \end{aligned}$$

beam polarisation
target polarisation



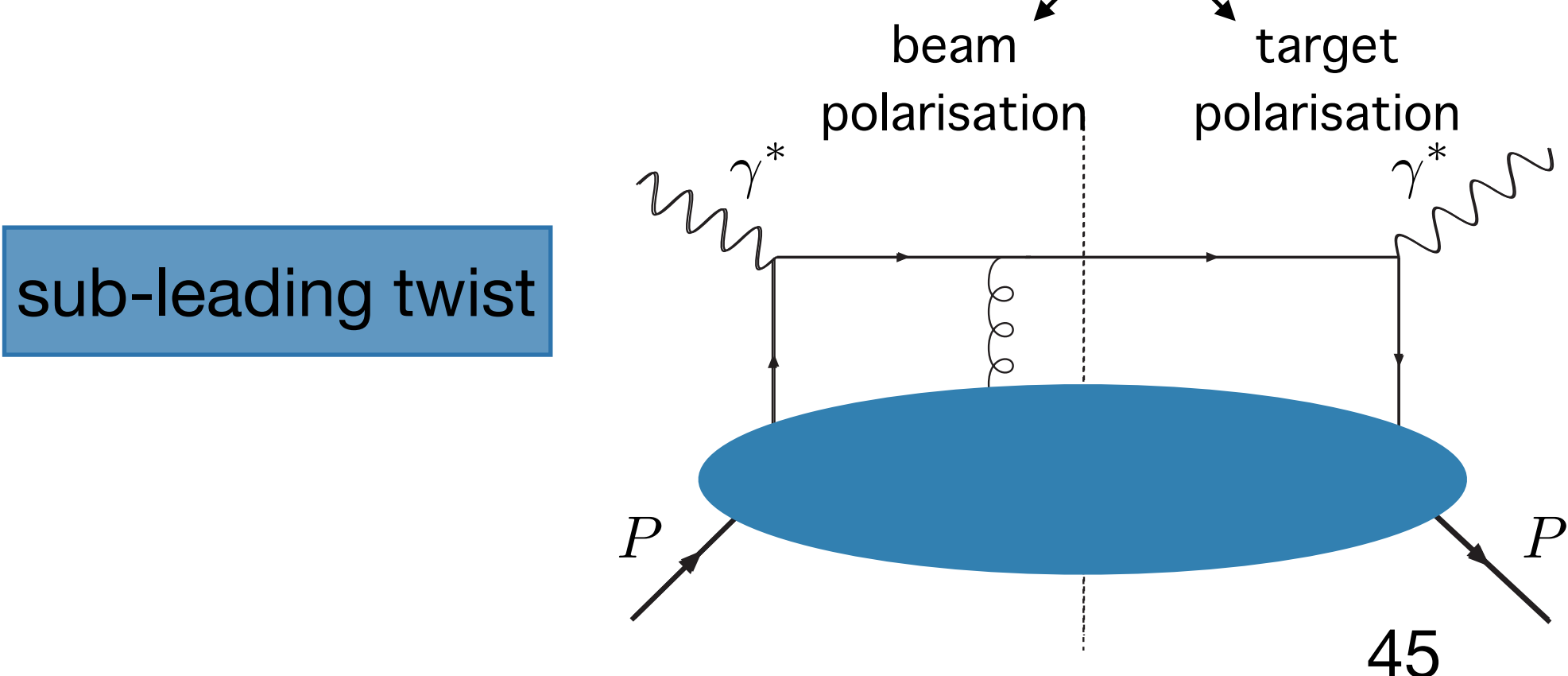
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 & + \lambda_l 2\langle \sin(\phi) \rangle_{LU}^h \sin(\phi) \\
 \text{longitudinal target polarisation} \leftarrow & + S_L \left[2\langle \sin(\phi) \rangle_{UL}^h \sin(\phi) + 2\langle \sin(2\phi) \rangle_{UL}^h \sin(2\phi) \right. \\
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 \text{beam polarisation} \leftarrow & + \lambda_l \left(2\langle \cos(\phi - \phi_S) \rangle_{LT}^h \cos(\phi - \phi_S) \right. \\
 & \left. + 2\langle \cos(\phi_S) \rangle_{LT}^h \cos(\phi_S) + 2\langle \cos(2\phi - \phi_S) \rangle_{LT}^h \cos(2\phi - \phi_S) \right) \left. \right\}
 \end{aligned}$$

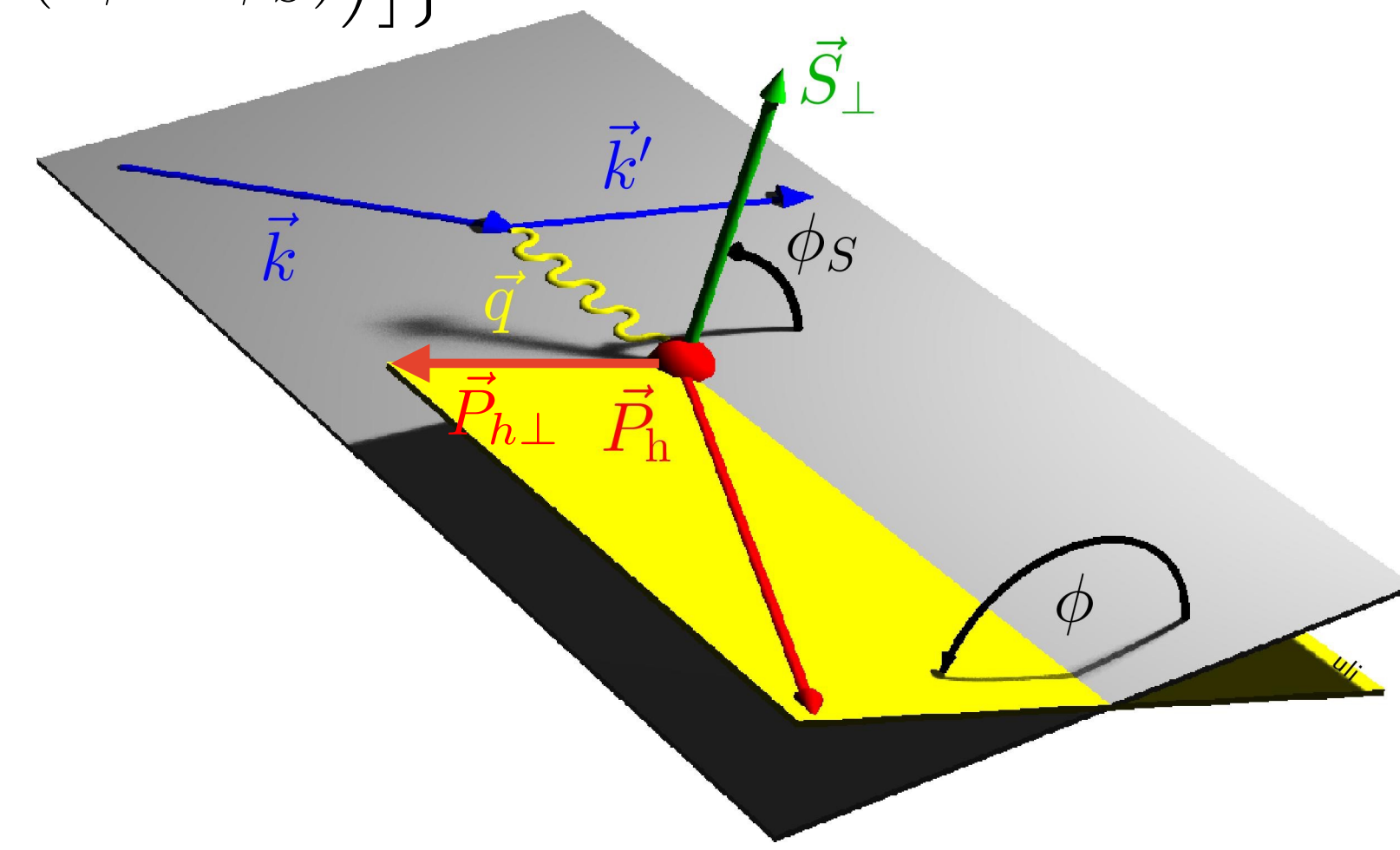


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 & + 2\langle \sin(2\phi - \phi_S) \rangle_{UT}^h \sin(2\phi - \phi_S) \\
 \text{beam polarisation} \leftarrow & + \lambda_l \left(2\langle \cos(\phi - \phi_S) \rangle_{LT}^h \cos(\phi - \phi_S) \right. \\
 & + \left. \left. 2\langle \cos(\phi_S) \rangle_{LT}^h \cos(\phi_S) + 2\langle \cos(2\phi - \phi_S) \rangle_{LT}^h \cos(2\phi - \phi_S) \right) \right] \left. \right\}
 \end{aligned}$$



sub-leading twist



TMD PDFs and TMD fragmentation functions

Azimuthal amplitudes related to structure functions F_{XY} :

$$2\langle \sin(\phi + \phi_S) \rangle_{UT}^h = \epsilon F_{UT}^{\sin(\phi + \phi_S)}$$

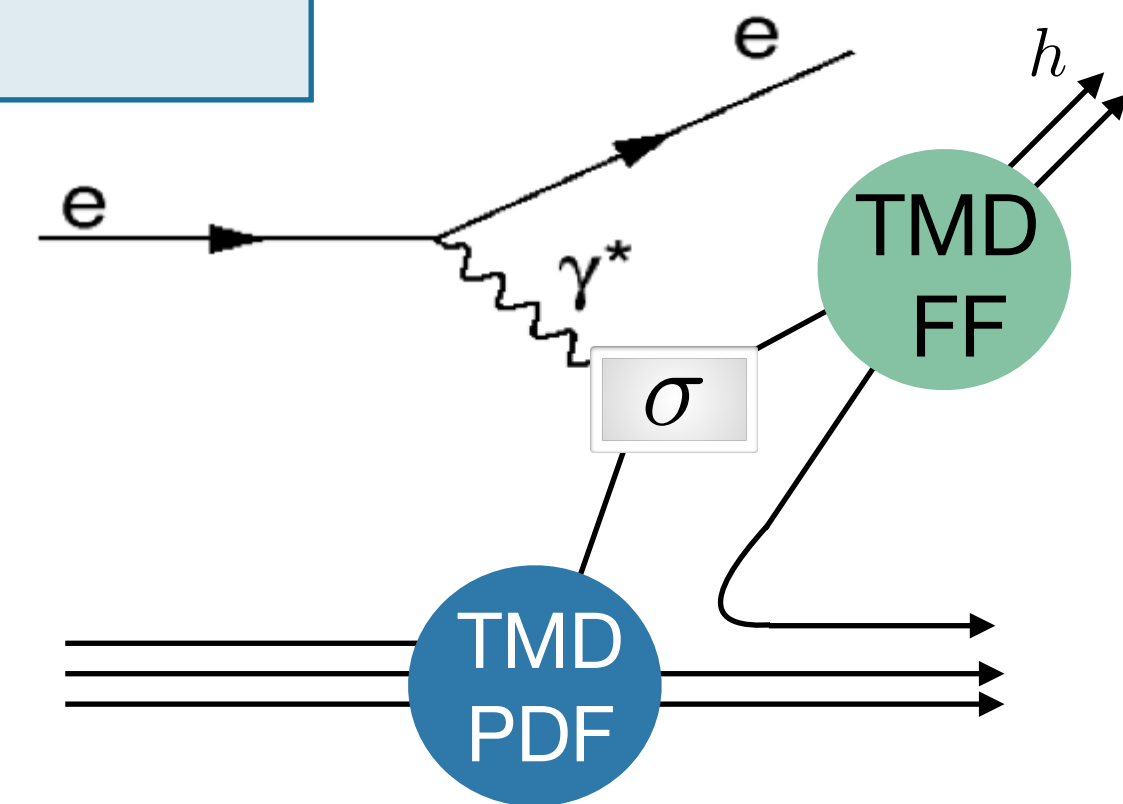
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$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$



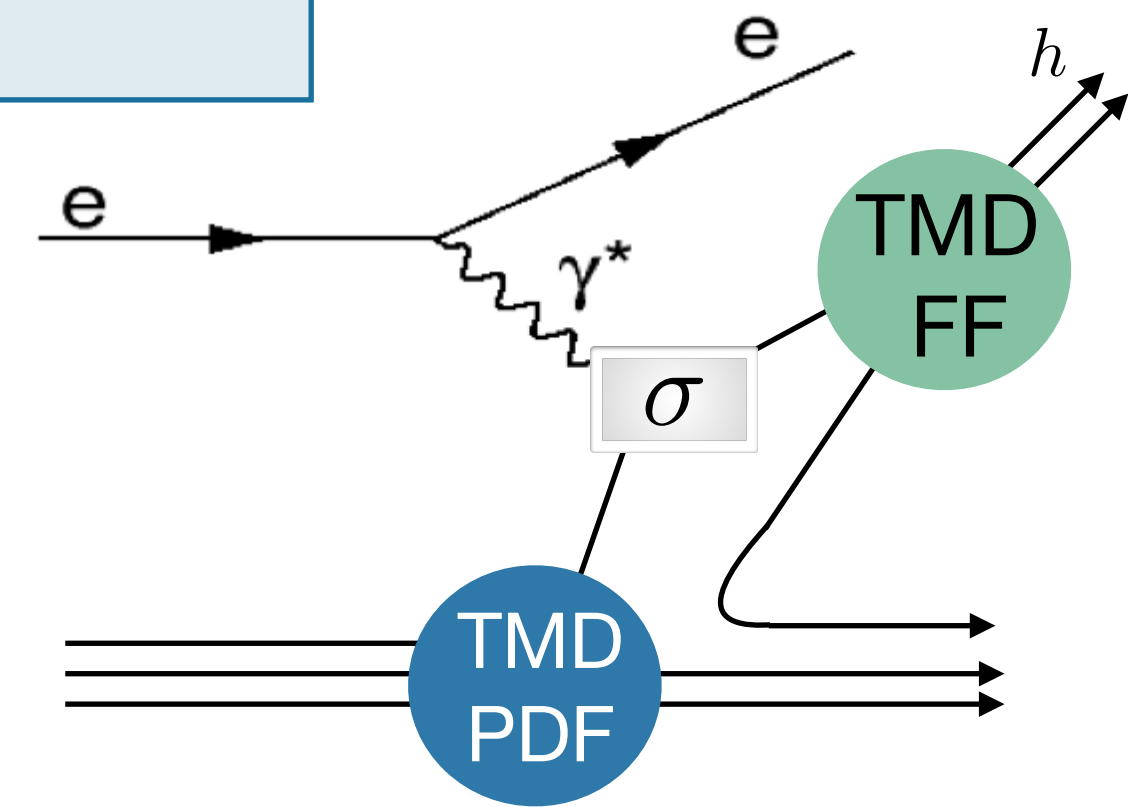
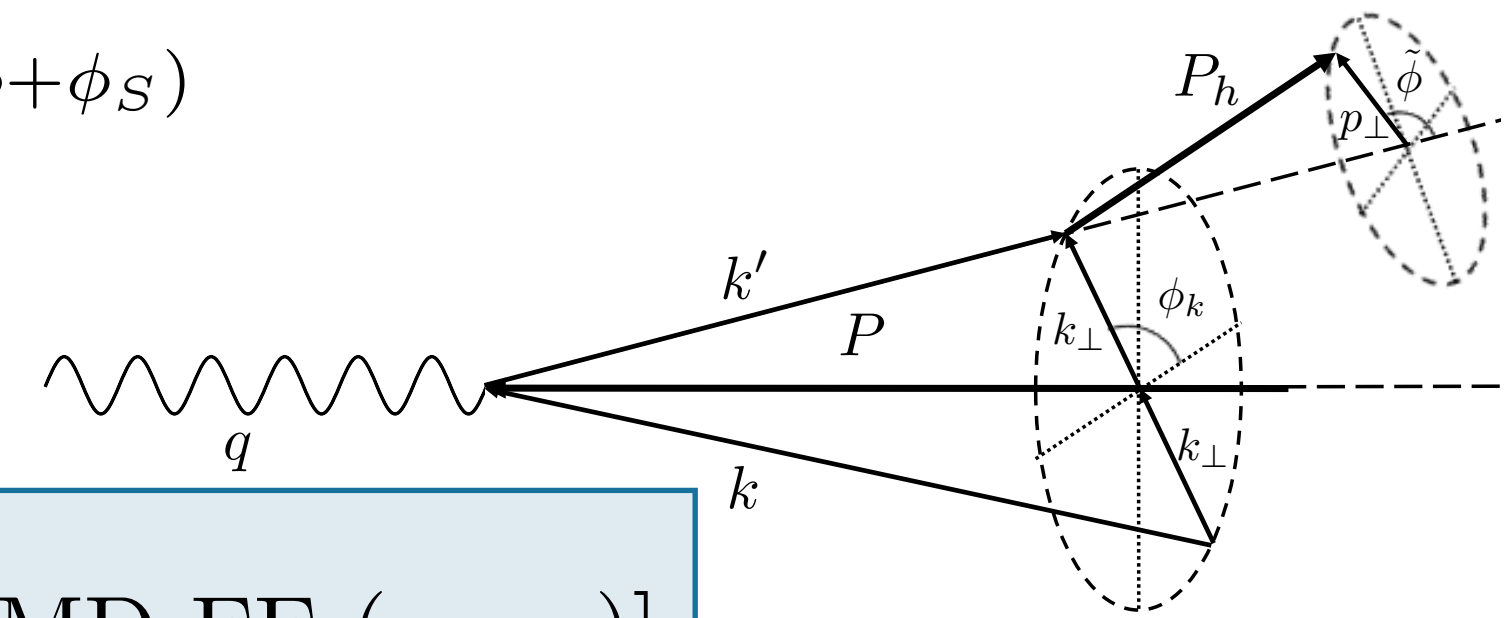
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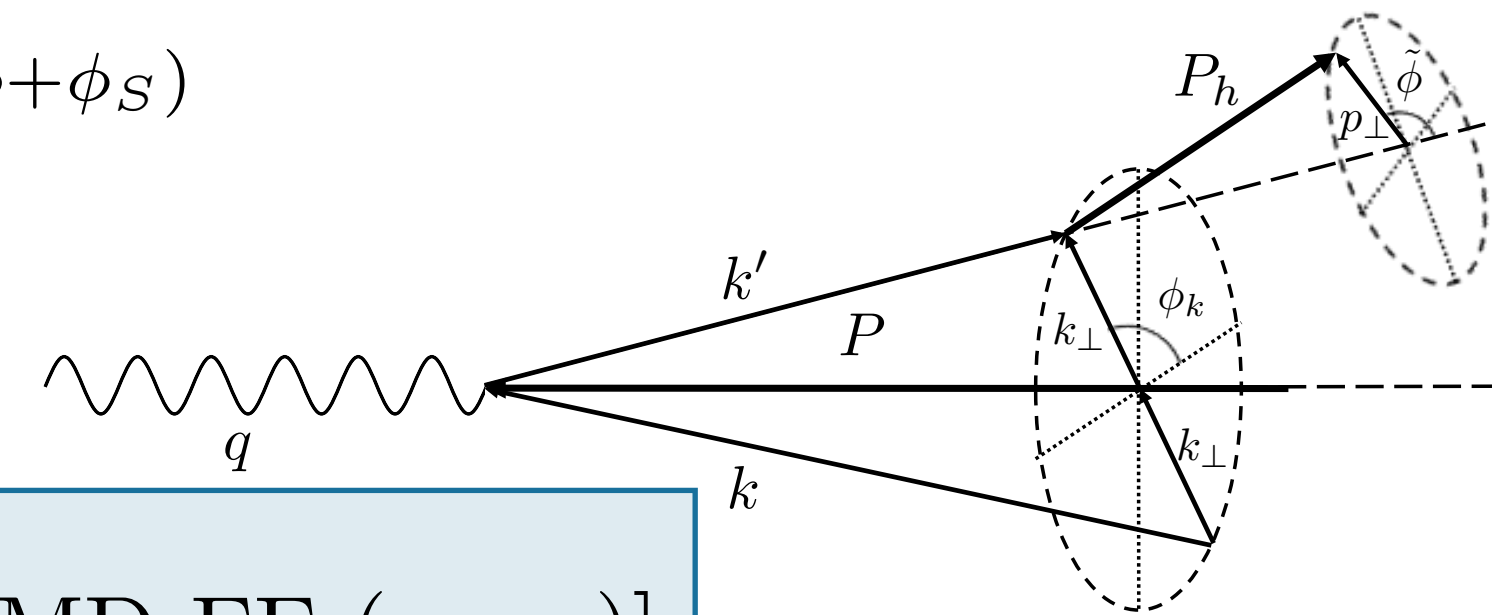


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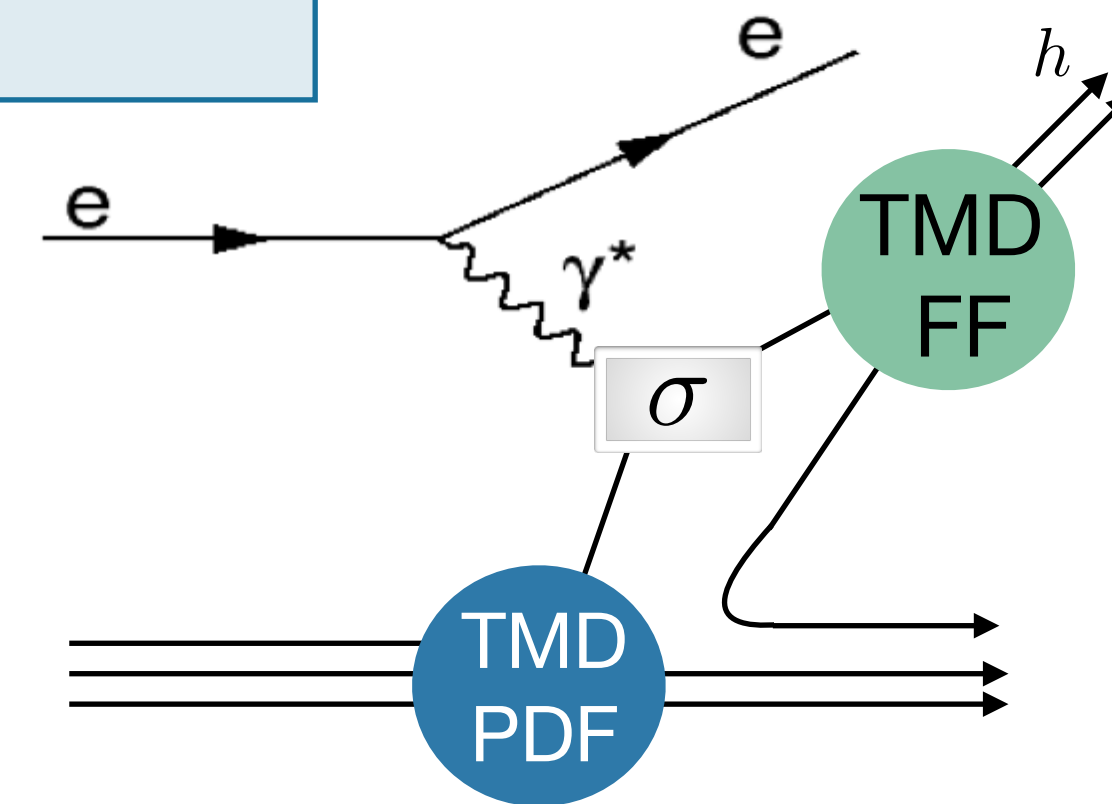


nucleon polarisation

quark polarisation

	U	L	T
U	f_1		h_1^{\perp}
L		g_{1L}	h_{1L}^{\perp}
T	f_{1T}^{\perp}	g_{1T}^{\perp}	$h_{1T} h_{1T}^{\perp}$

$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$

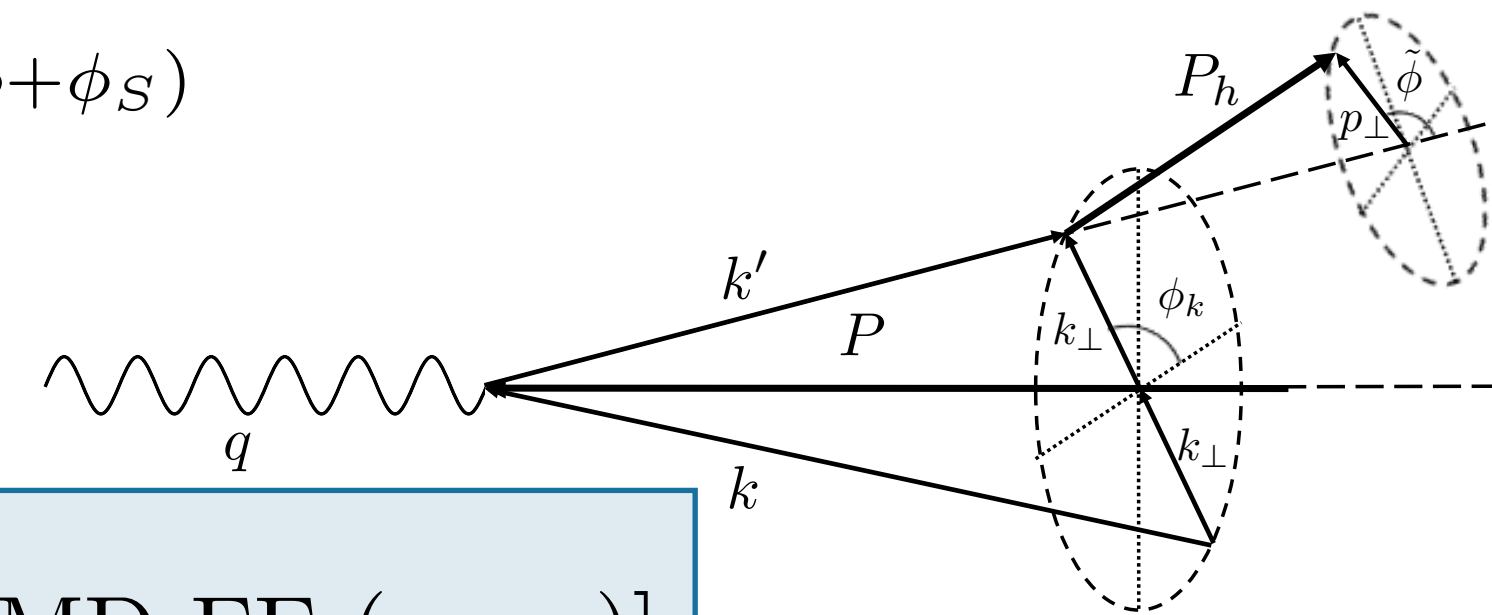


TMD PDFs and TMD fragmentation functions

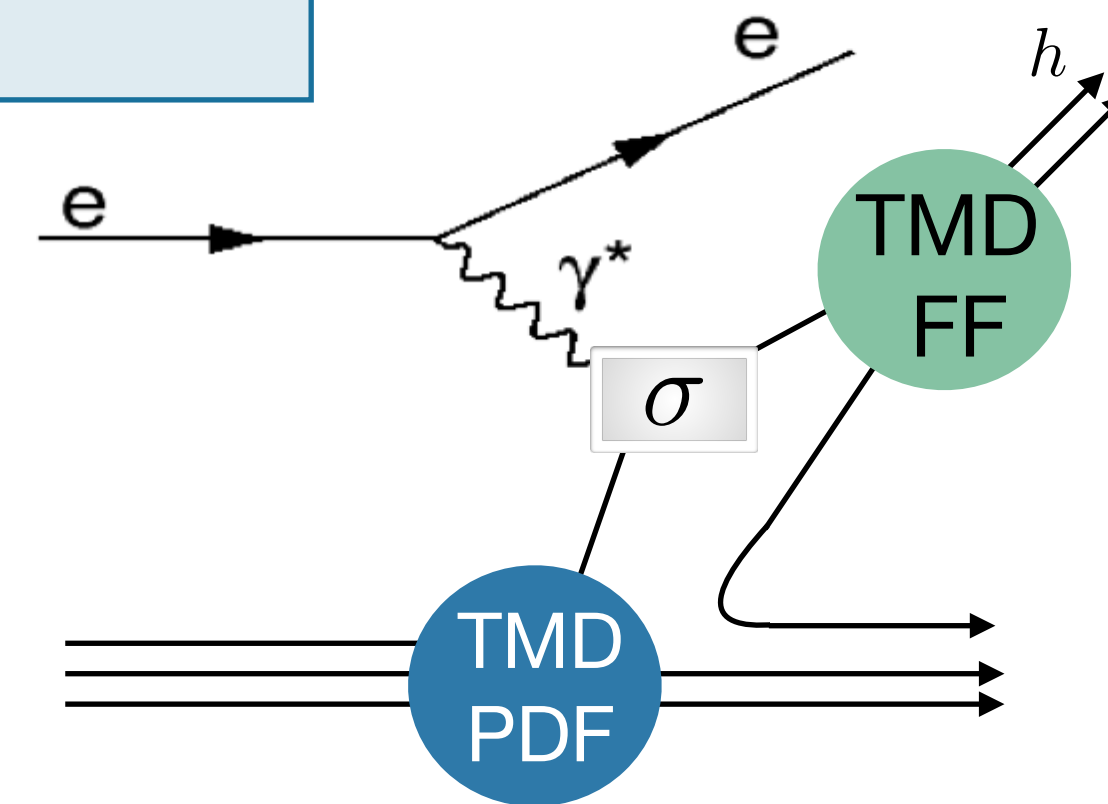
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$$z \stackrel{\text{lab}}{=} \frac{E_h}{E_{\gamma^*}}$$



quark polarisation

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nucleon polarisation

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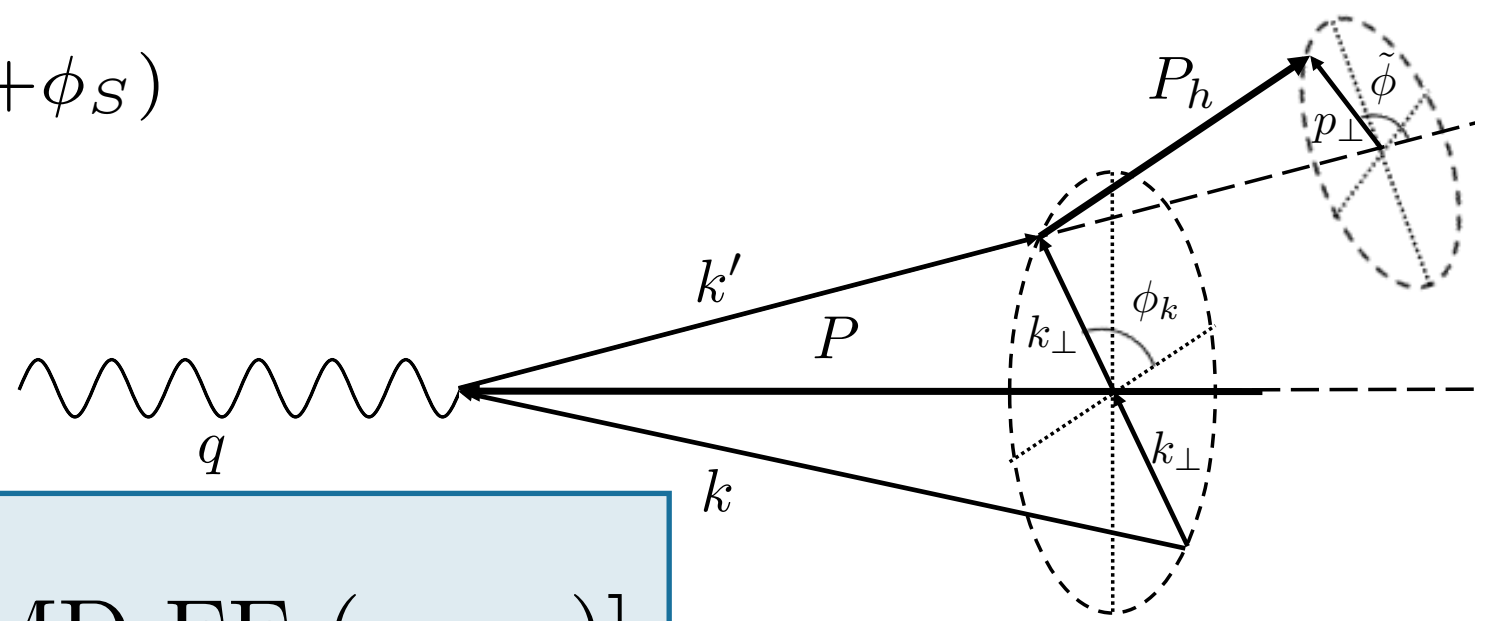
hadron polarisation

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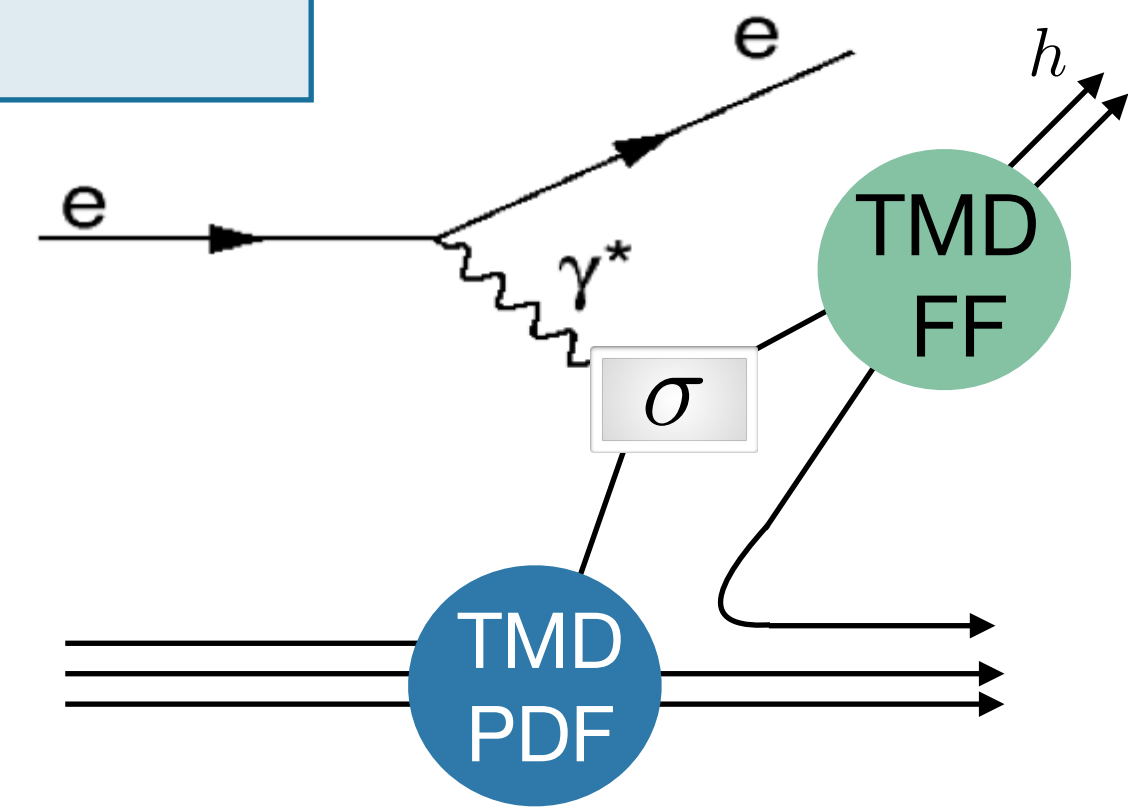


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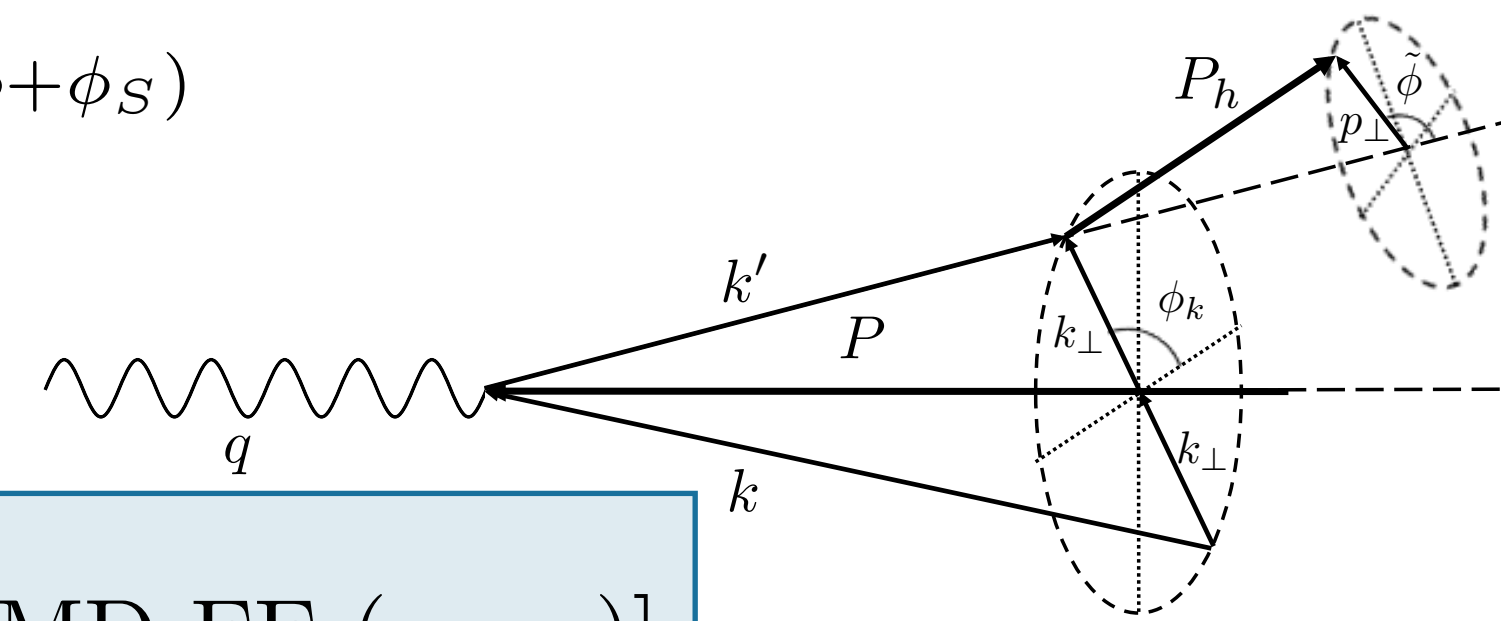
Chiral odd

TMD PDFs and TMD fragmentation functions

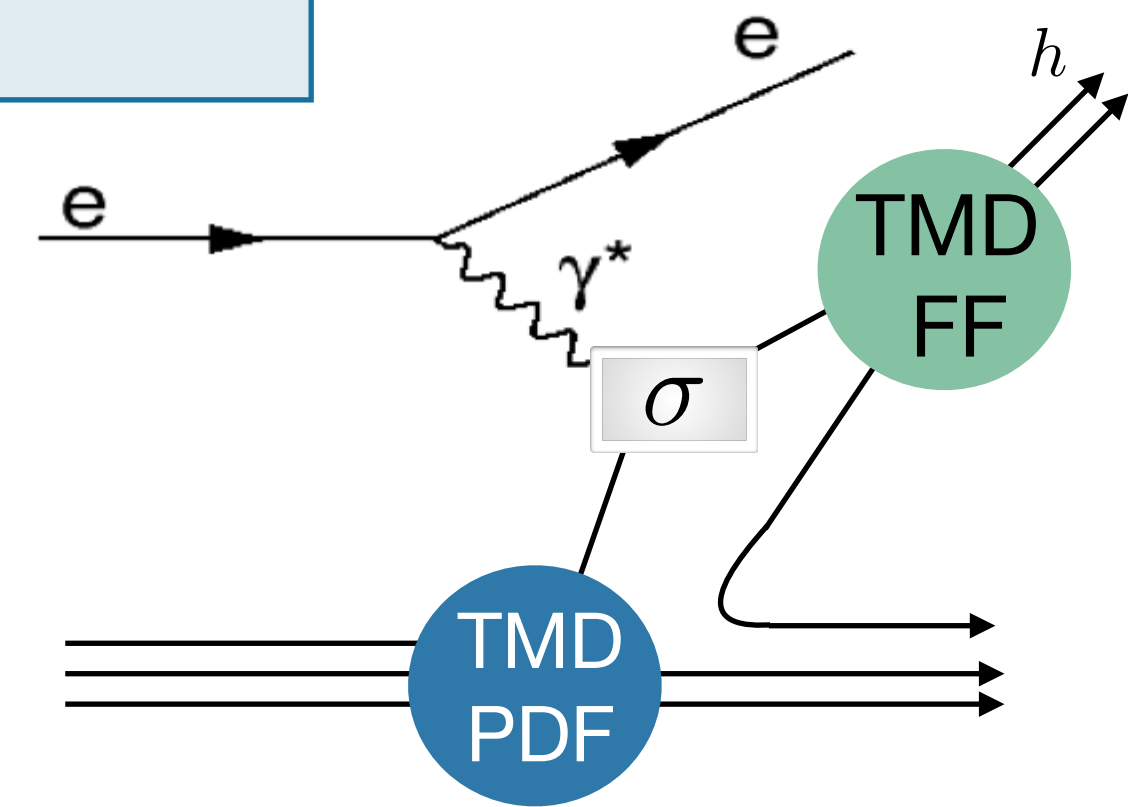
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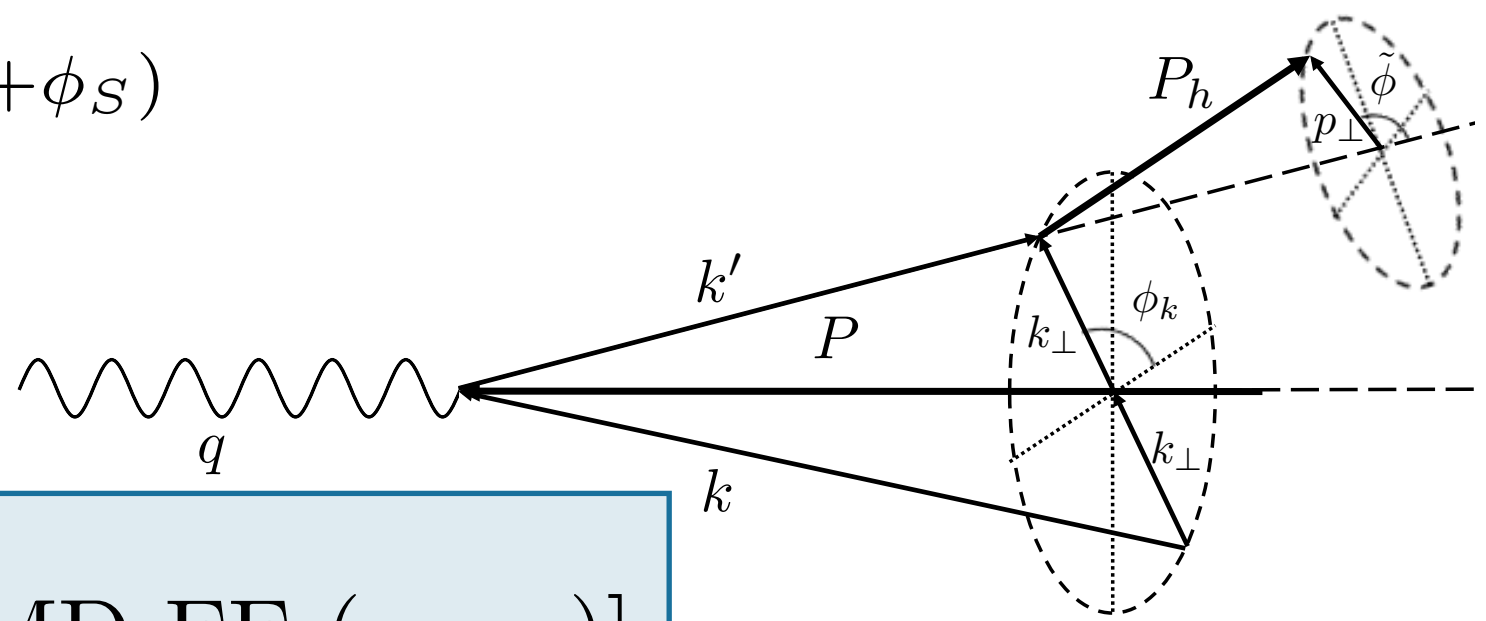
Chiral odd
Naive T-odd

TMD PDFs and TMD fragmentation functions

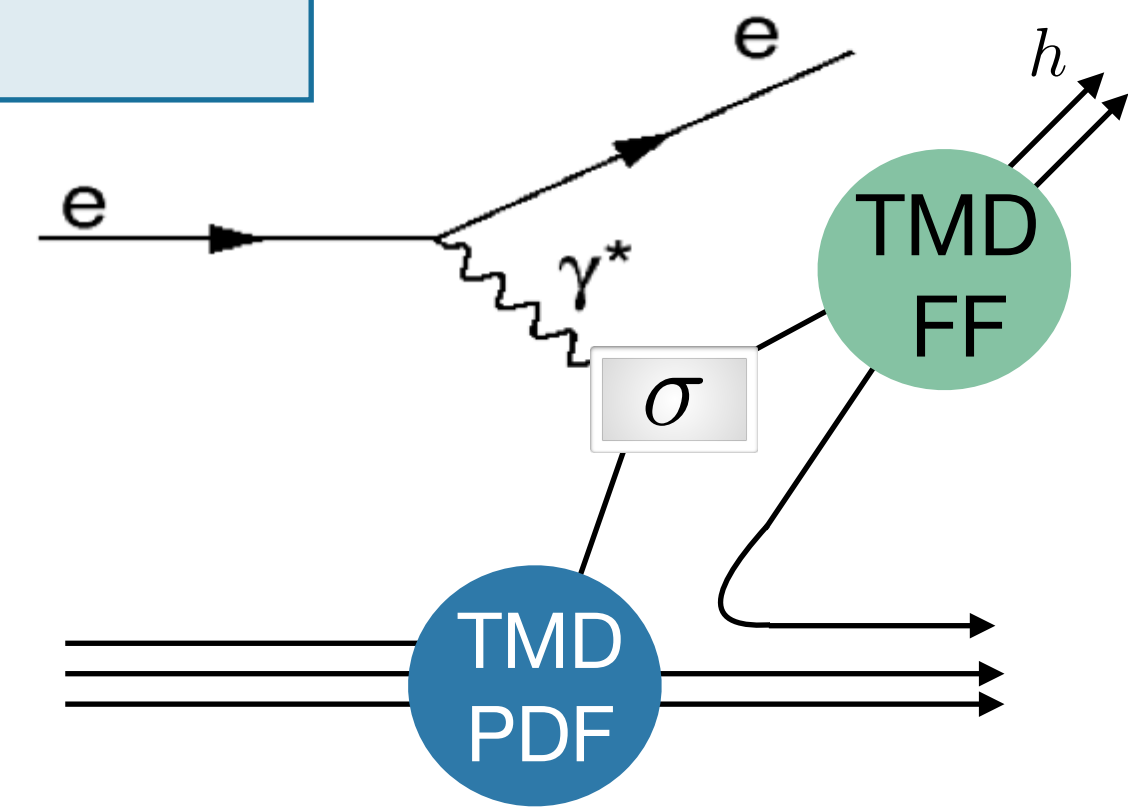
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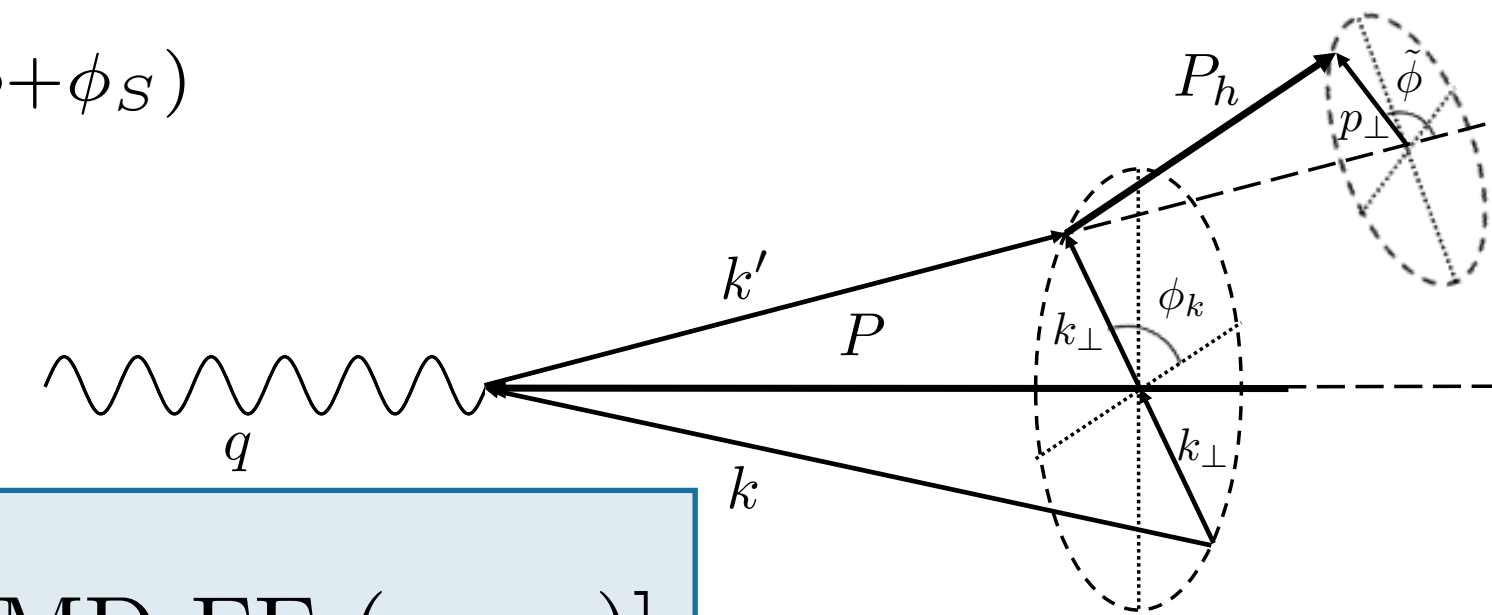
Chiral odd
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TMD PDFs and TMD fragmentation functions

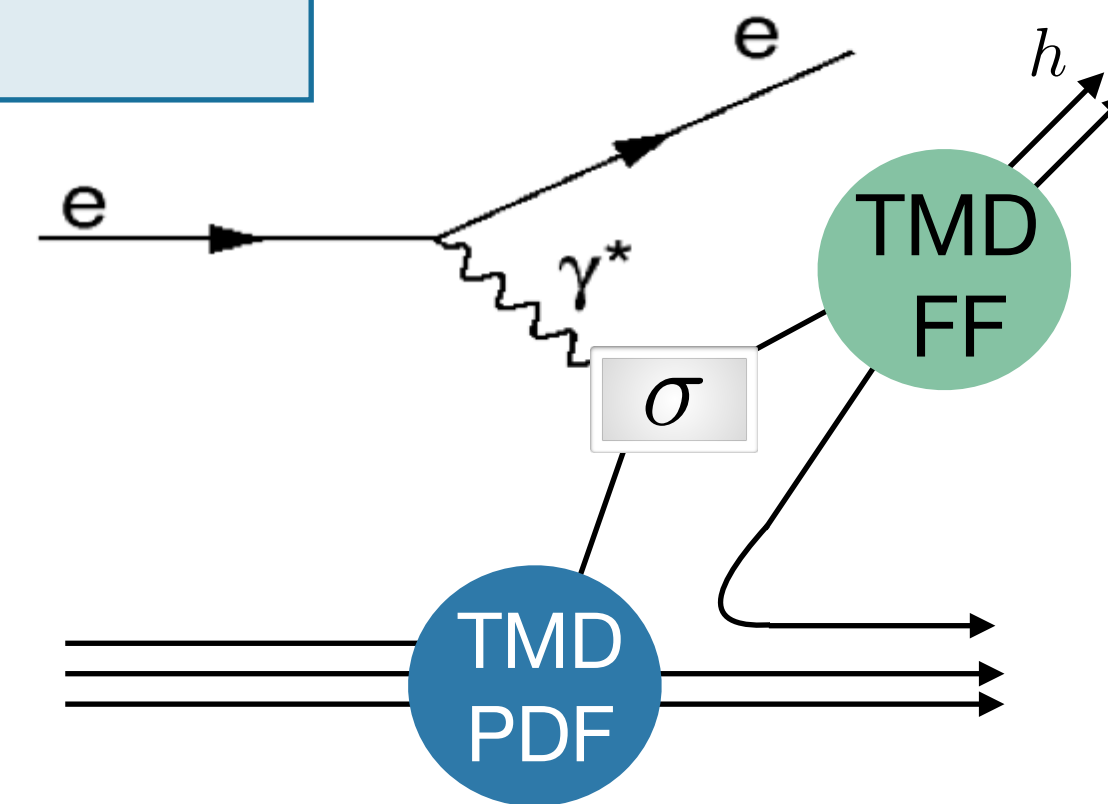
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nucleon polarisation

quark polarisation

	U	L	T
U	D_1		H_1^{\perp}

hadron polarisation

Chiral odd

Naive T-odd

TMD FFs

Unpolarized

Spin-spin
correlations

Spin-momentum
correlations

$$D_1 = \text{⊙}$$

$$G_1 = \text{⊙} \rightarrow \text{---} \text{⊙} \rightarrow$$

$$H_1 = \text{⊙} \uparrow \text{---} \text{⊙} \uparrow$$

$$G_{1T} = \text{⊙} \uparrow \text{---} \text{⊙} \uparrow$$

$$D_{1T}^\perp = \text{⊙} \uparrow \text{---} \text{⊙} \downarrow$$

$$H_1^\perp = \text{⊙} \uparrow \text{---} \text{⊙} \downarrow$$

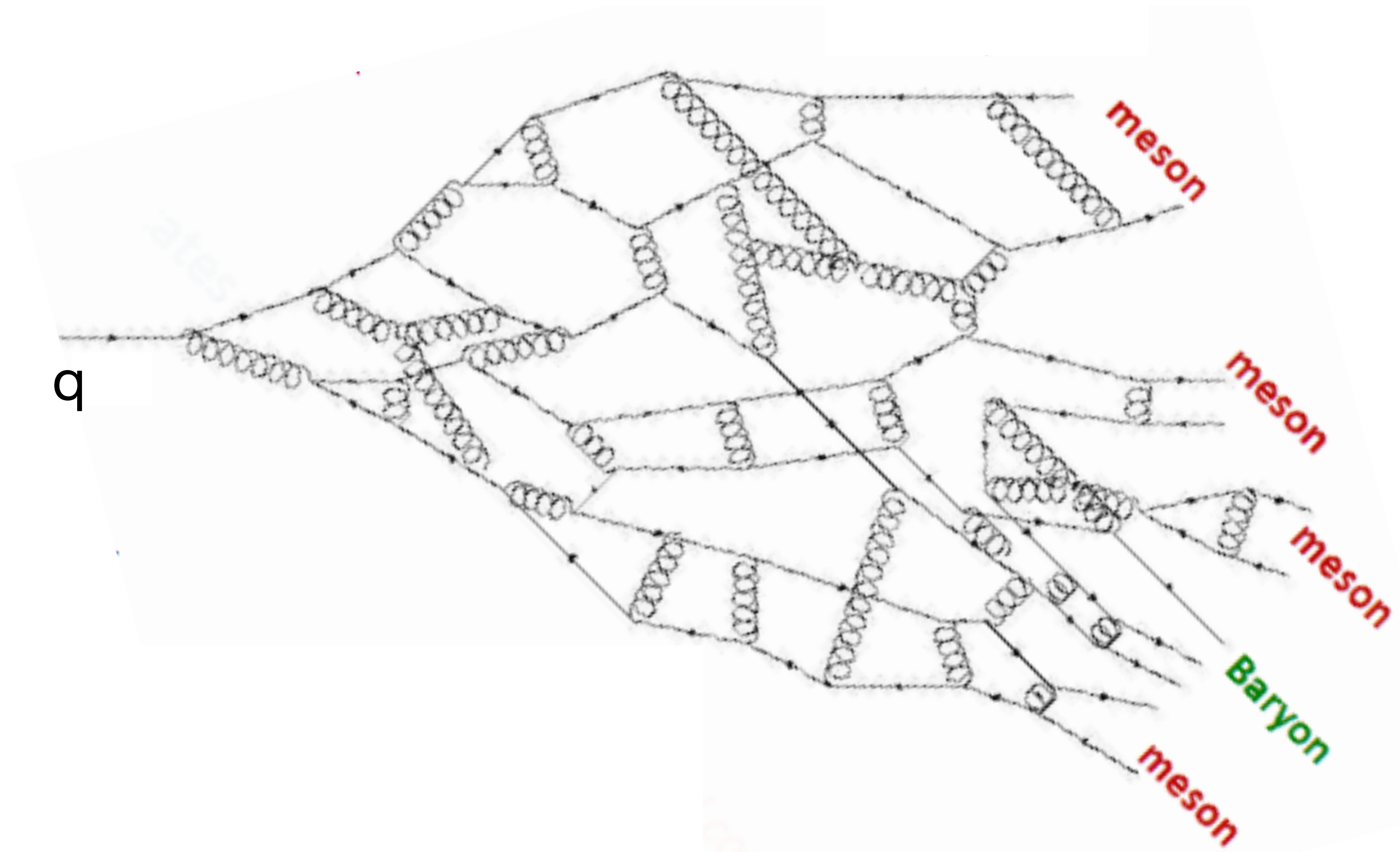
$$H_{1L}^\perp = \text{⊙} \rightarrow \text{---} \text{⊙} \rightarrow$$

Polarizing FF

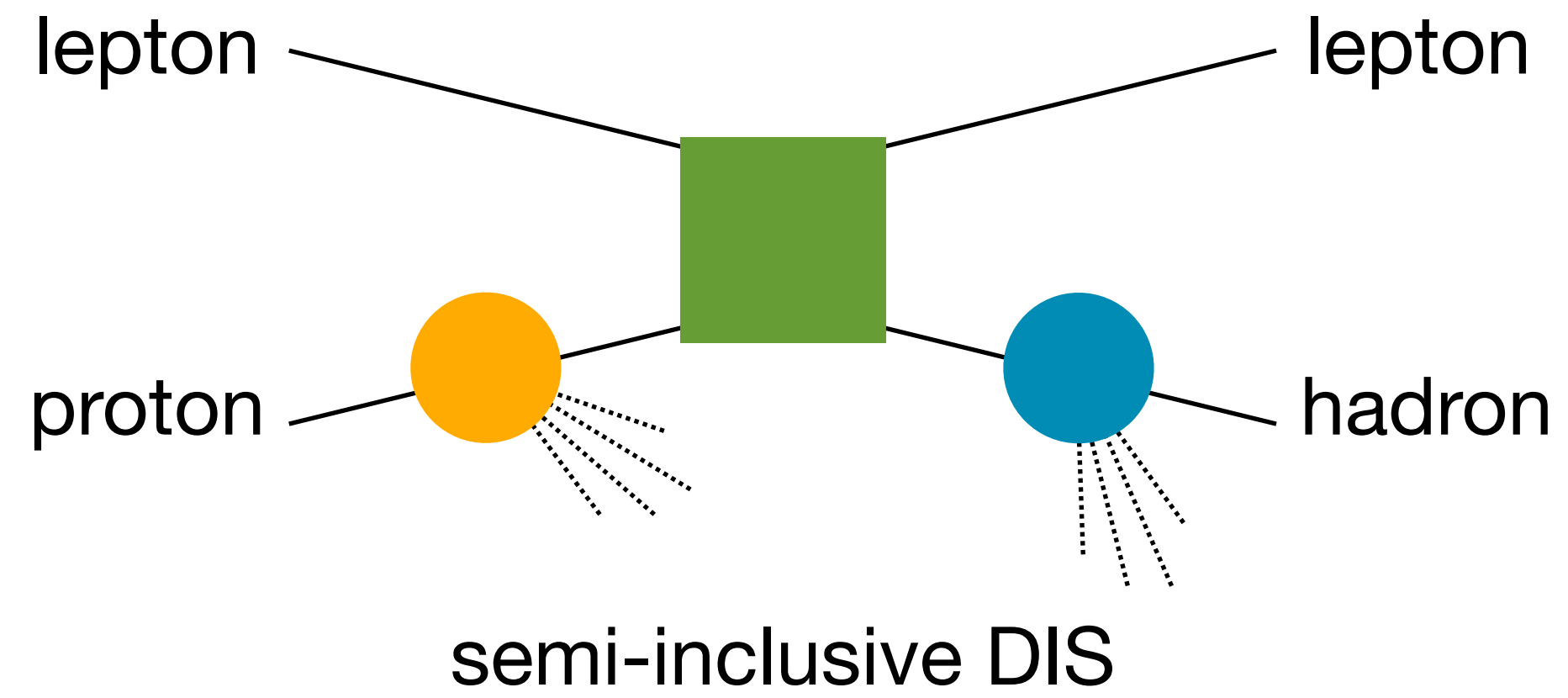
Collins

$$H_{1T}^\perp = \text{⊙} \uparrow \text{---} \text{⊙} \uparrow$$

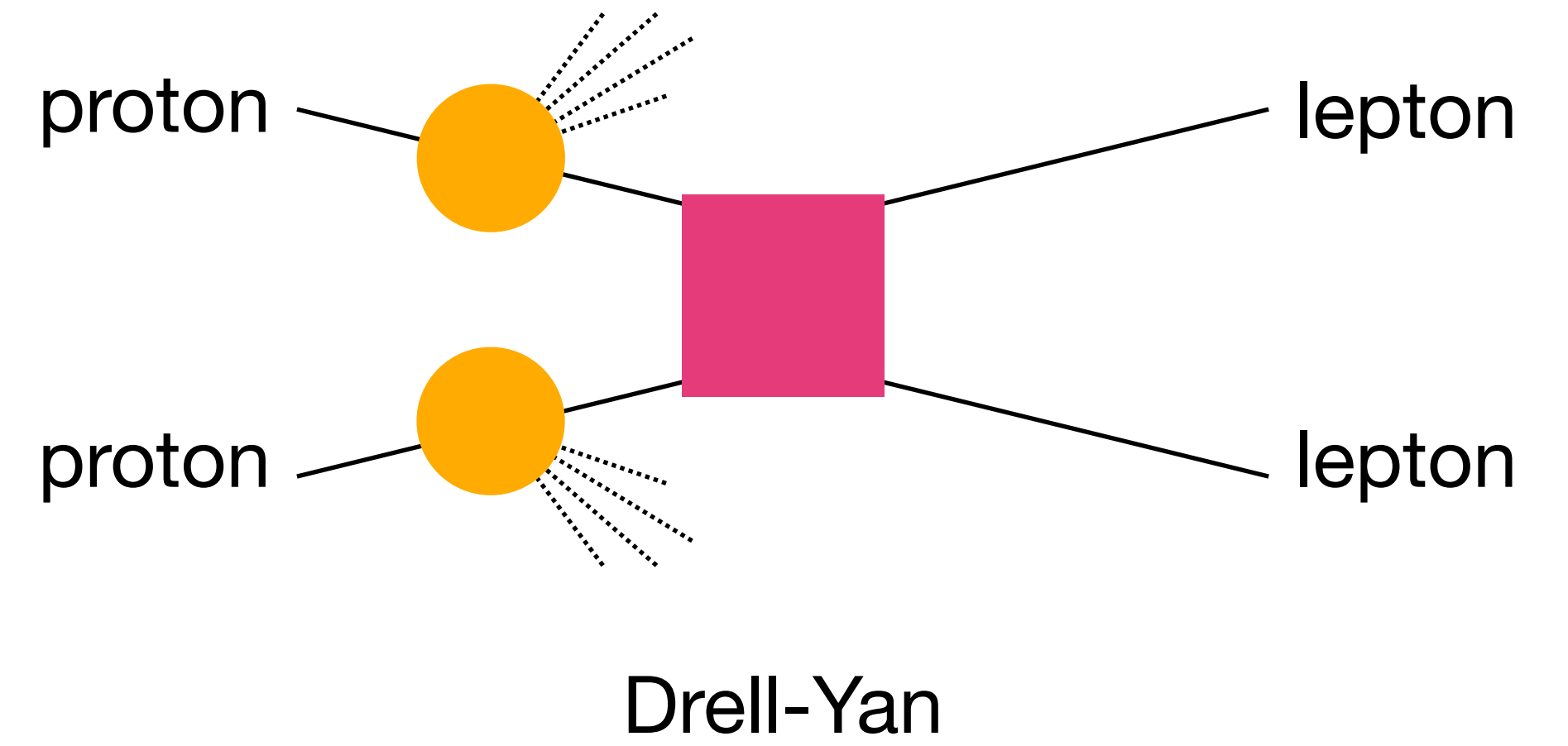
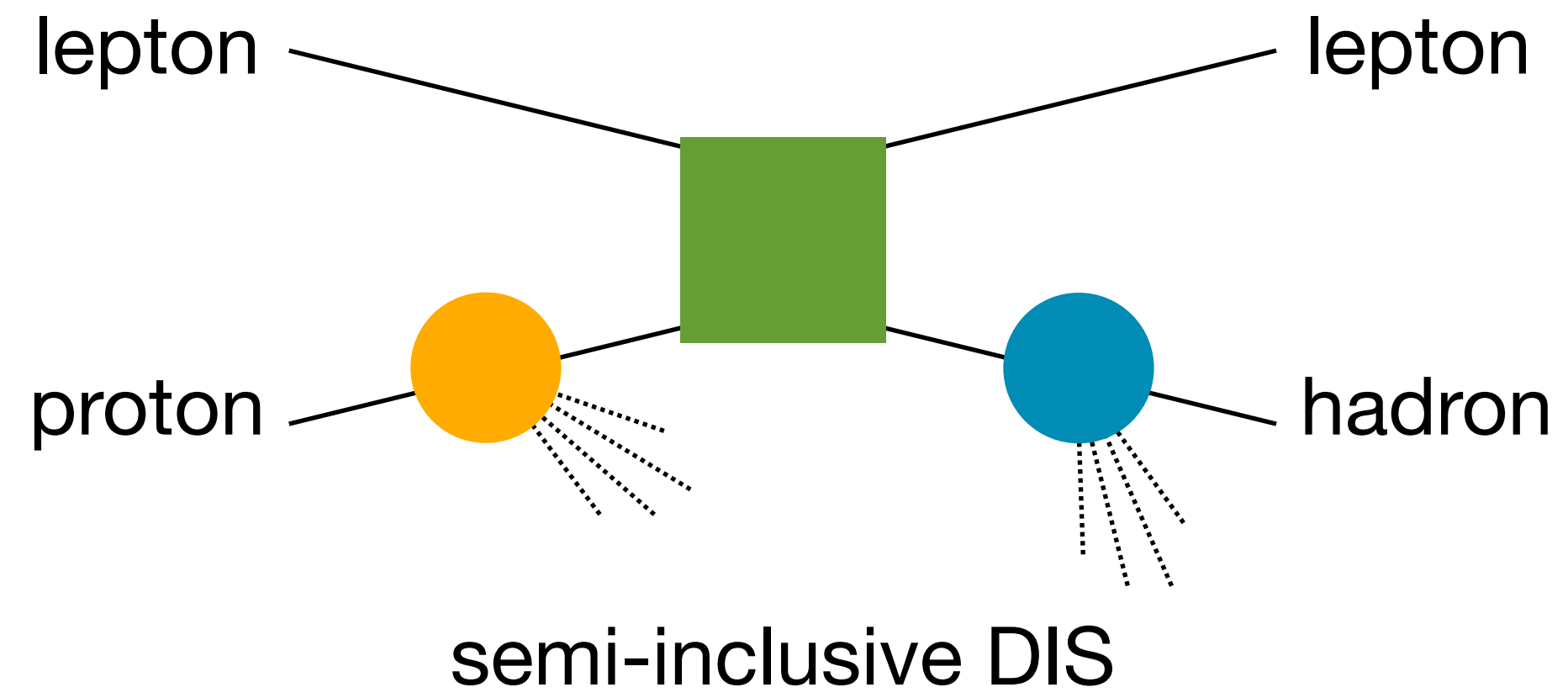
Fragmentation



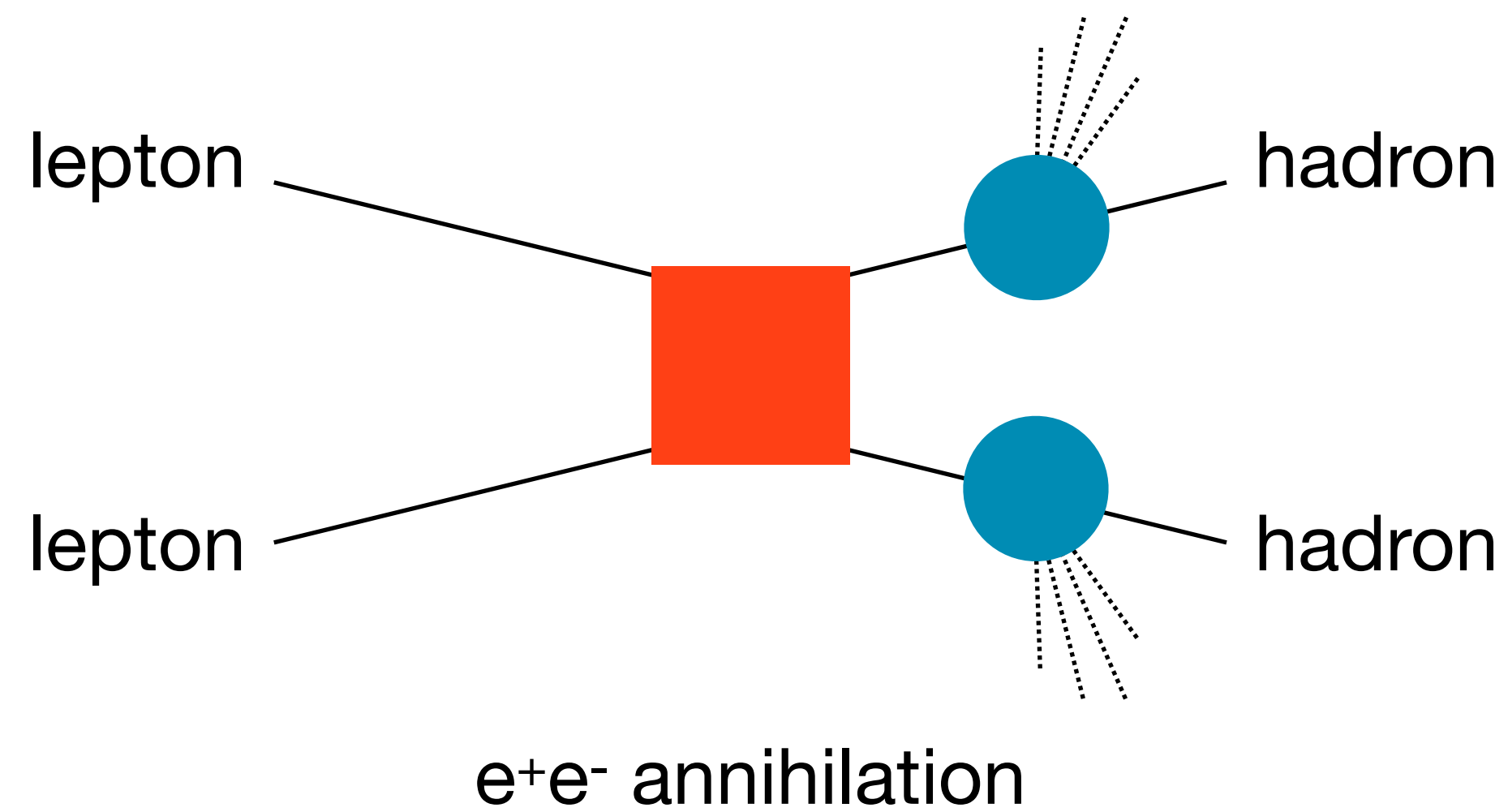
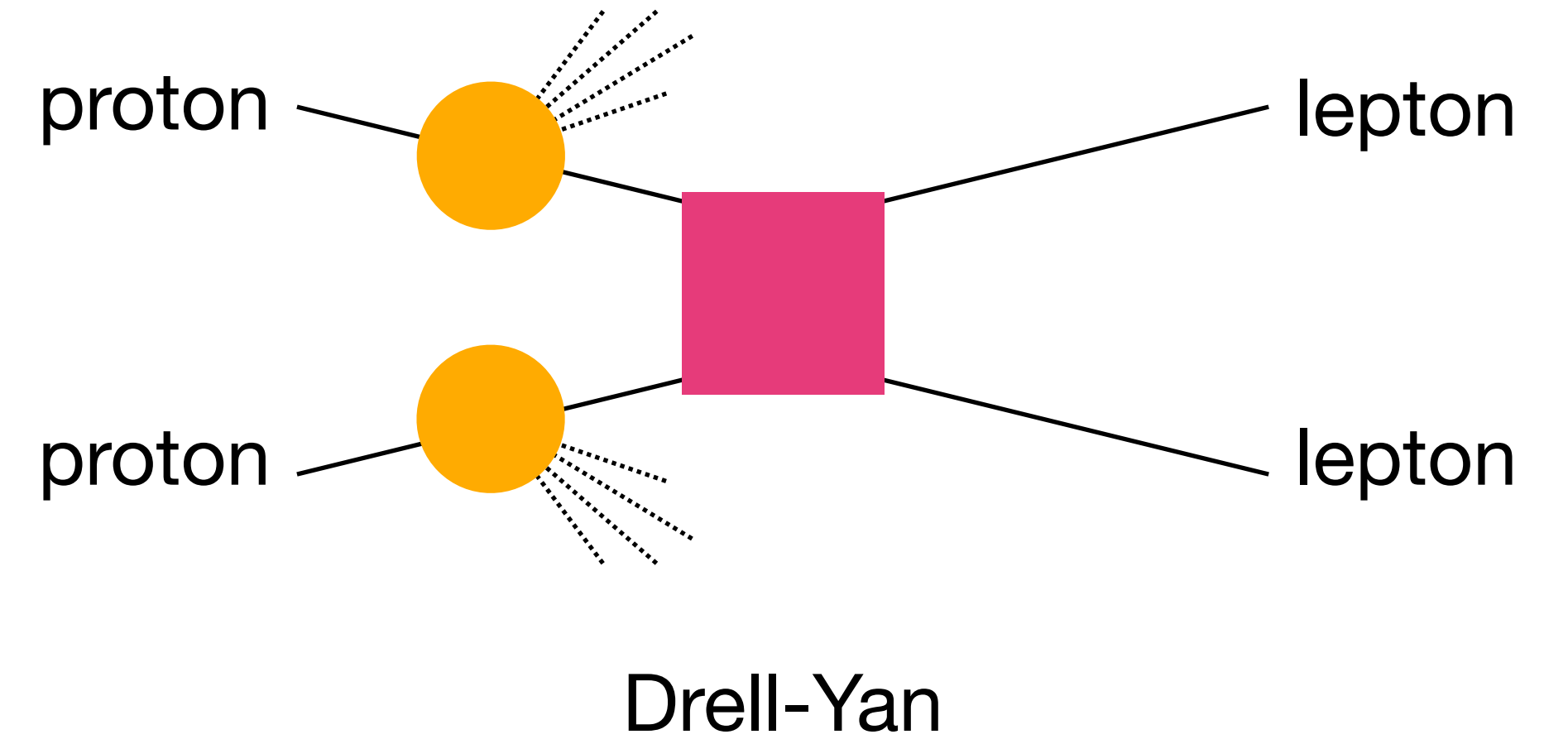
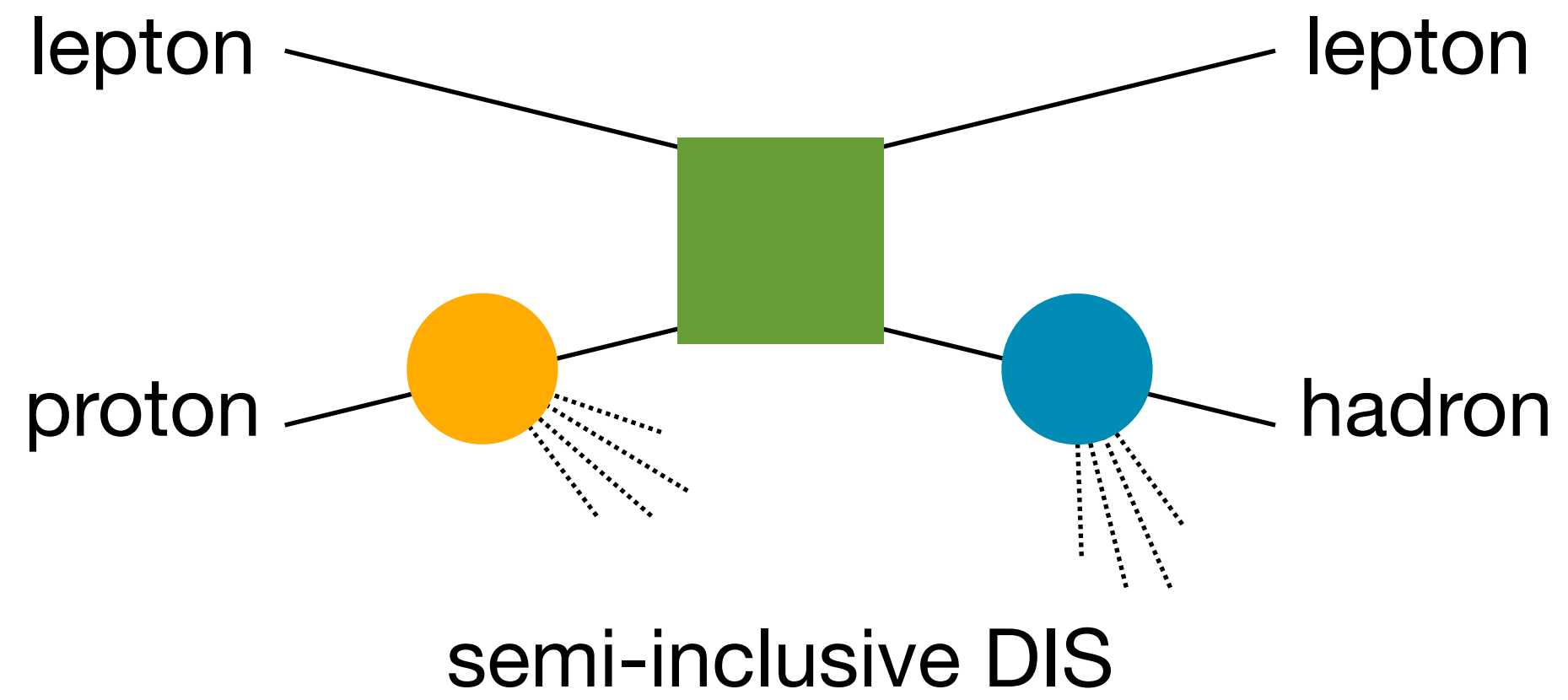
TMDs: factorisation and universality



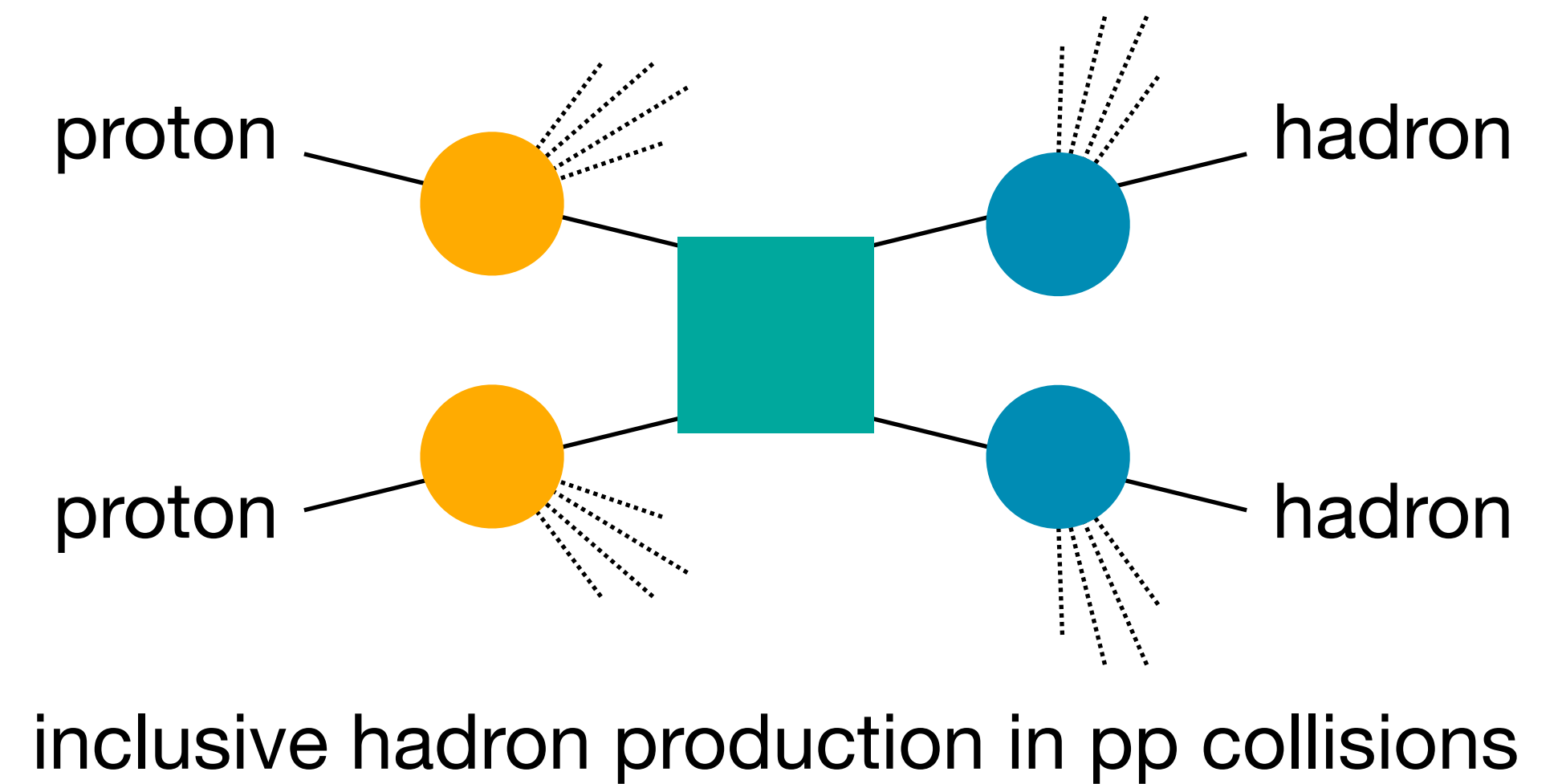
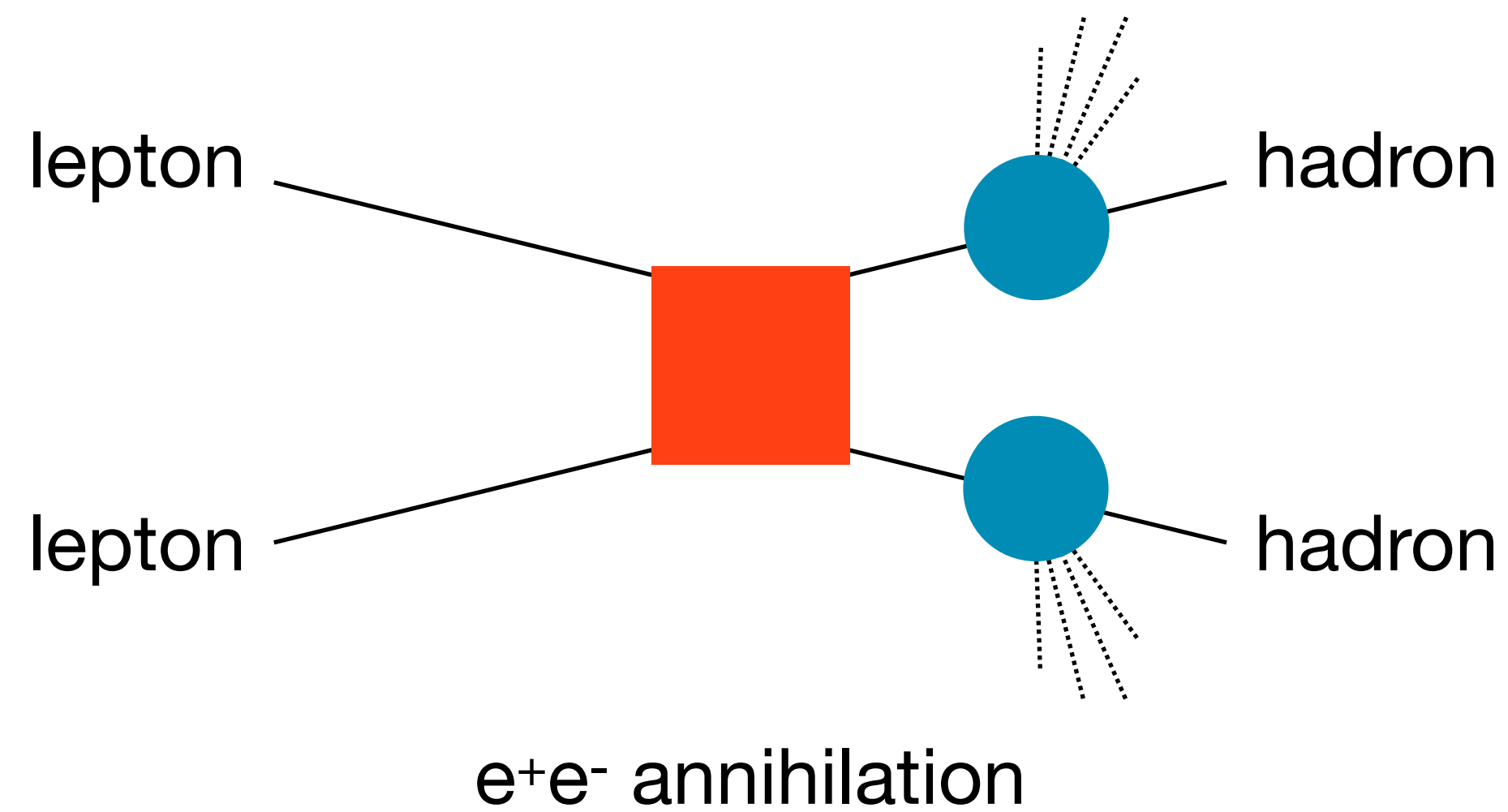
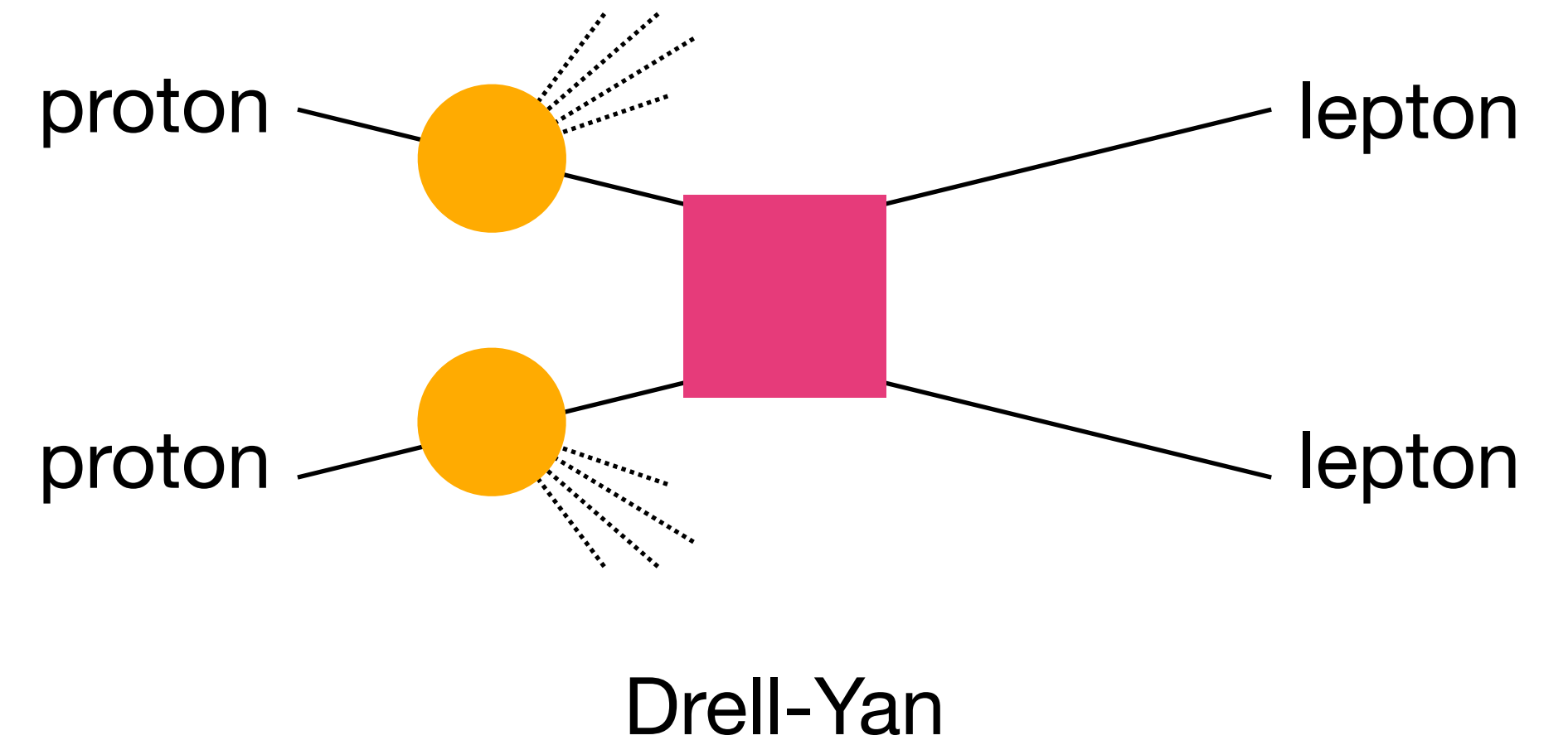
TMDs: factorisation and universality



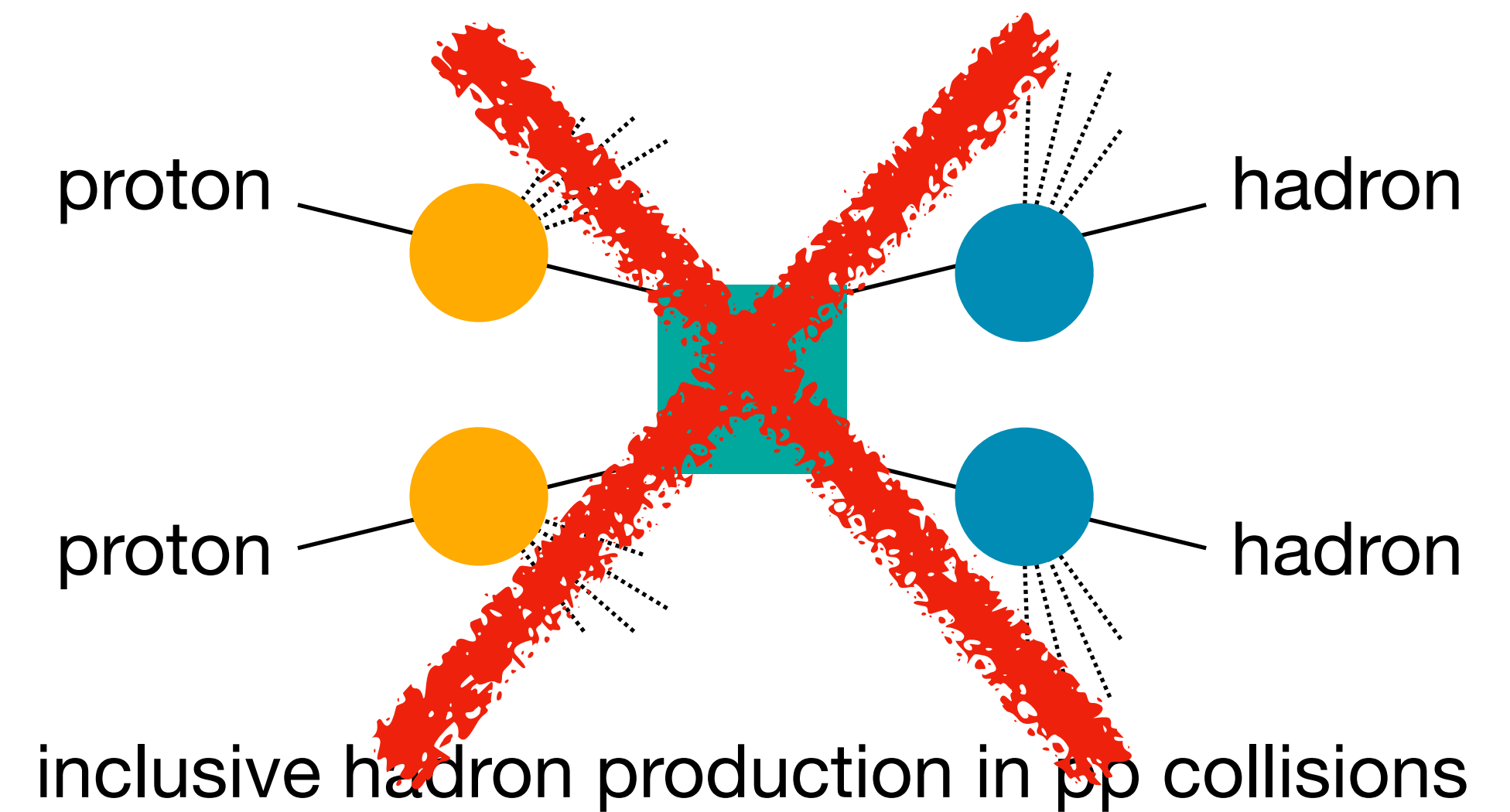
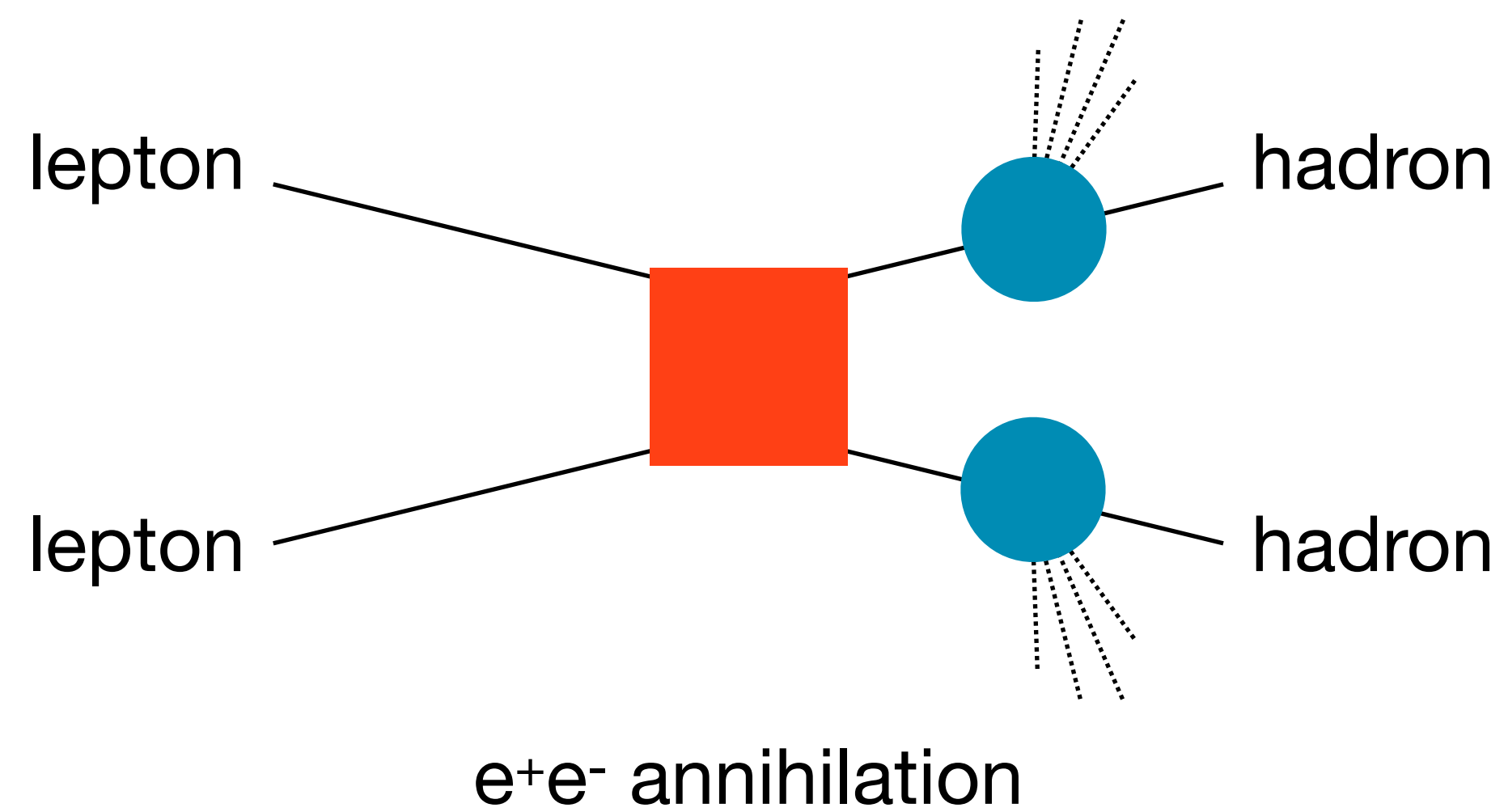
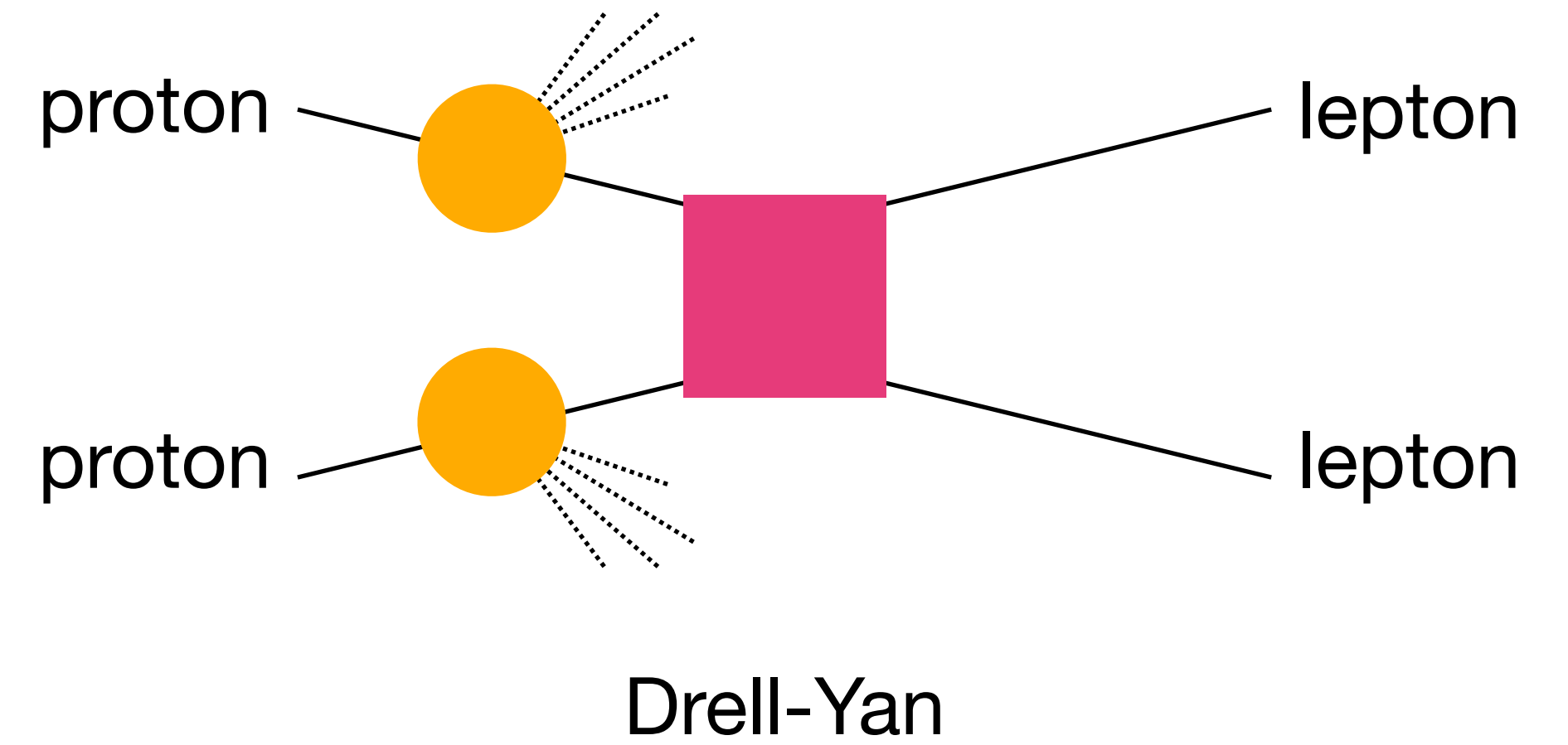
TMDs: factorisation and universality



TMDs: factorisation and universality

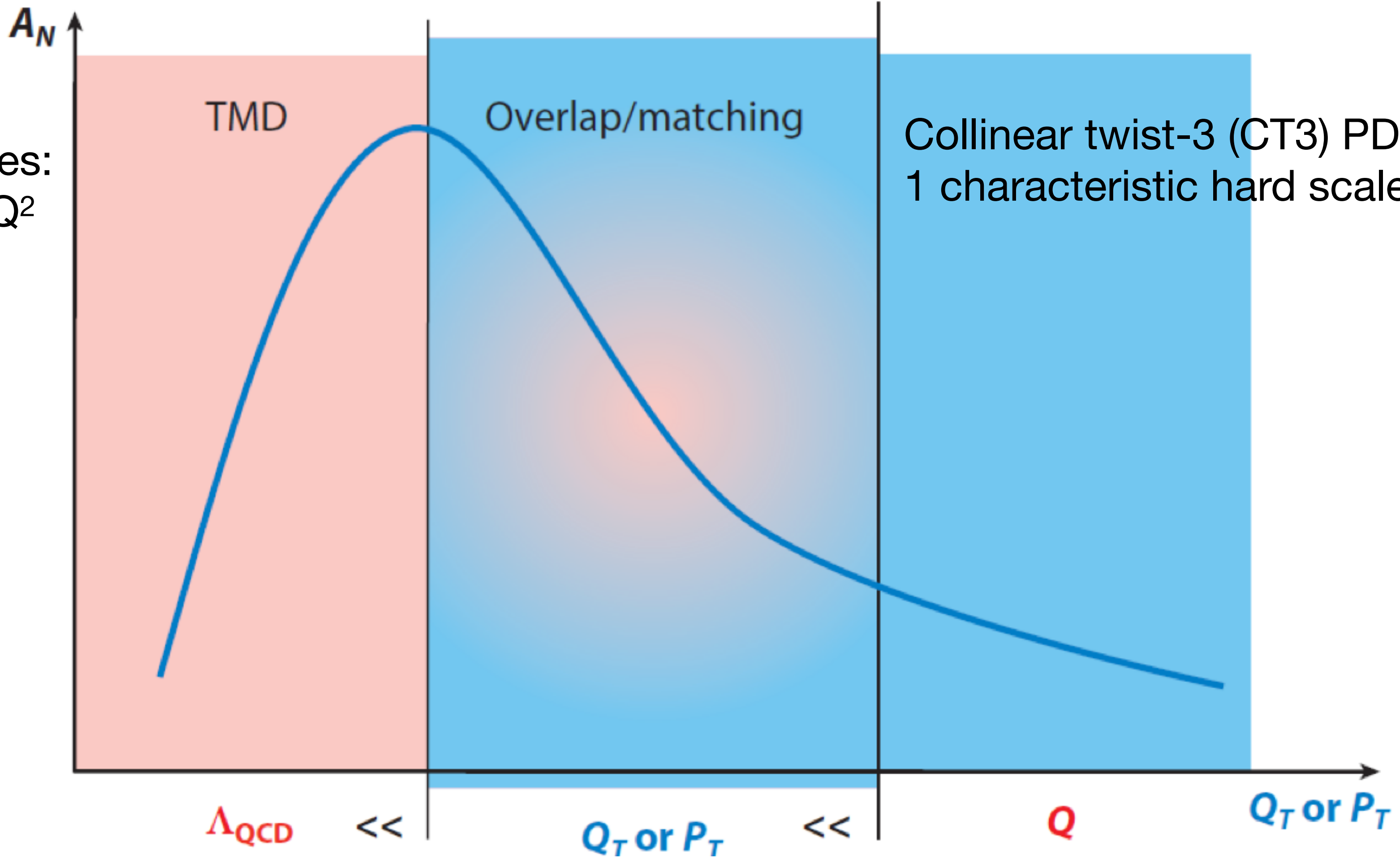


TMDs: factorisation and universality



Validity of TMD description

2 characteristic scales:
small P_{hT} and large Q^2



Collinear twist-3 (CT3) PDFs.
1 characteristic hard scale, e.g., P_{hT}

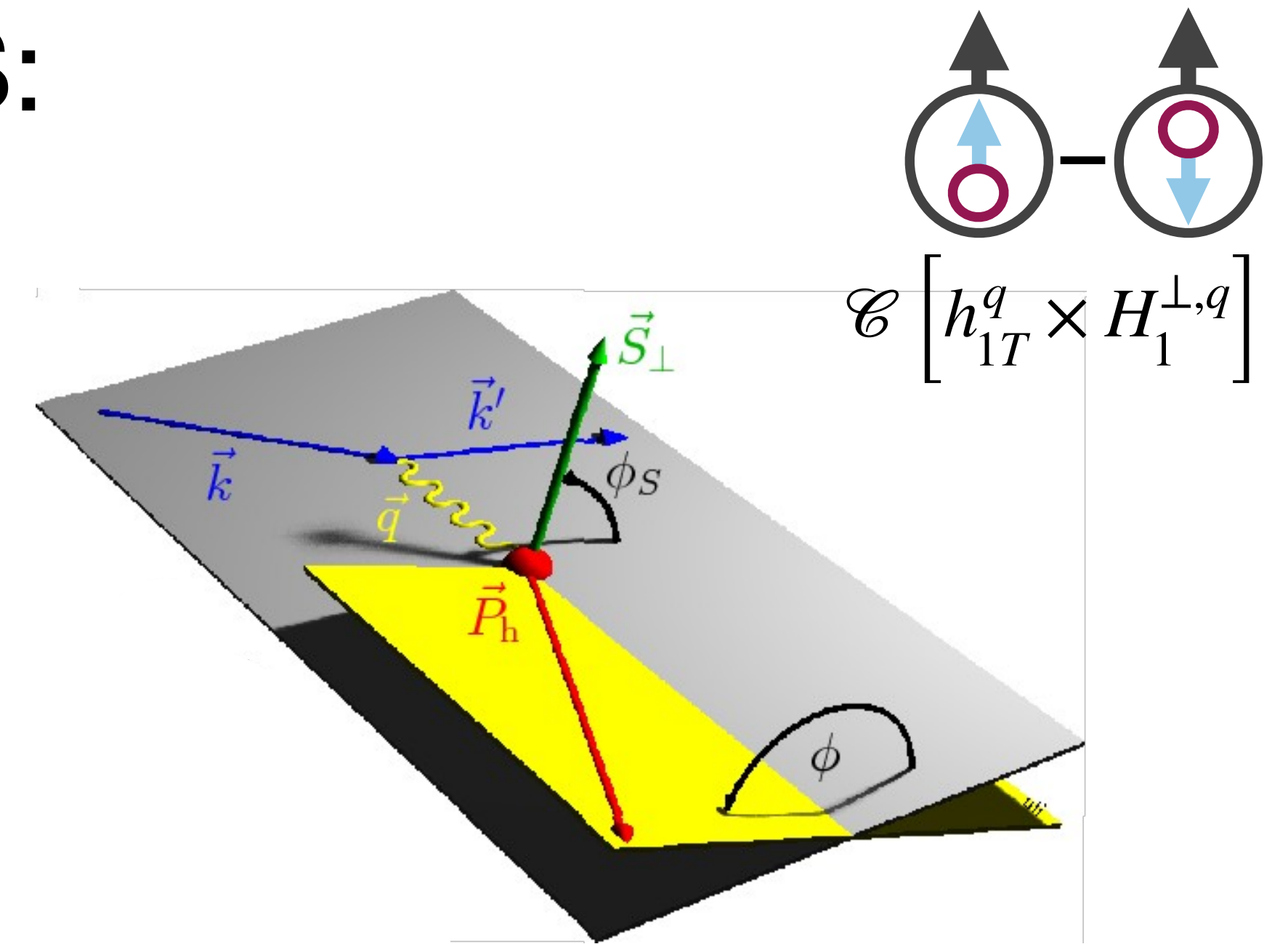
Consistent results for TMD
and CT3 in overlap region

Experiments investigating TMD PDFs and TMD FFs



Access to transversity in semi-inclusive DIS: Collins amplitude

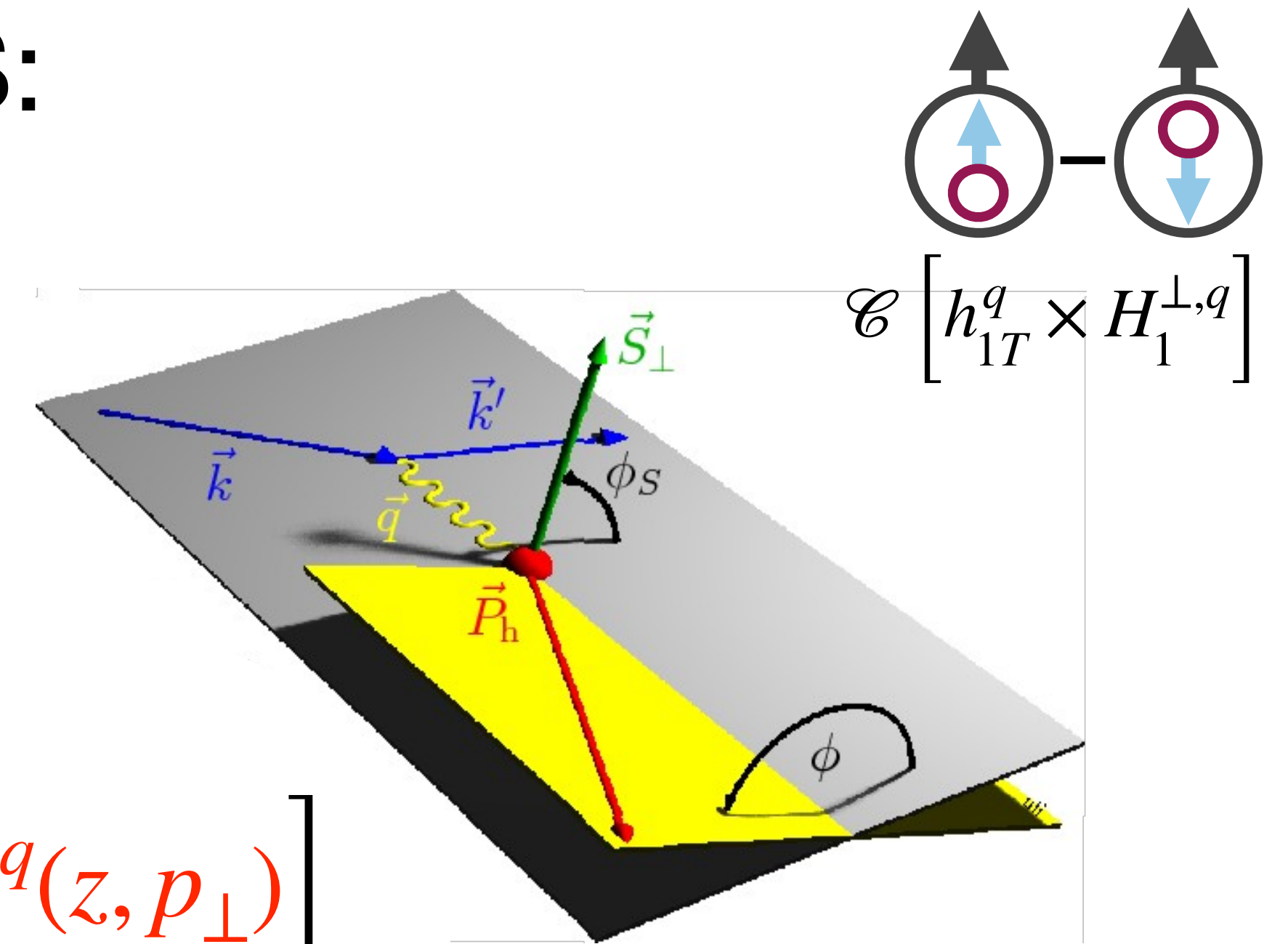
$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$



Access to transversity in semi-inclusive DIS: Collins amplitude

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

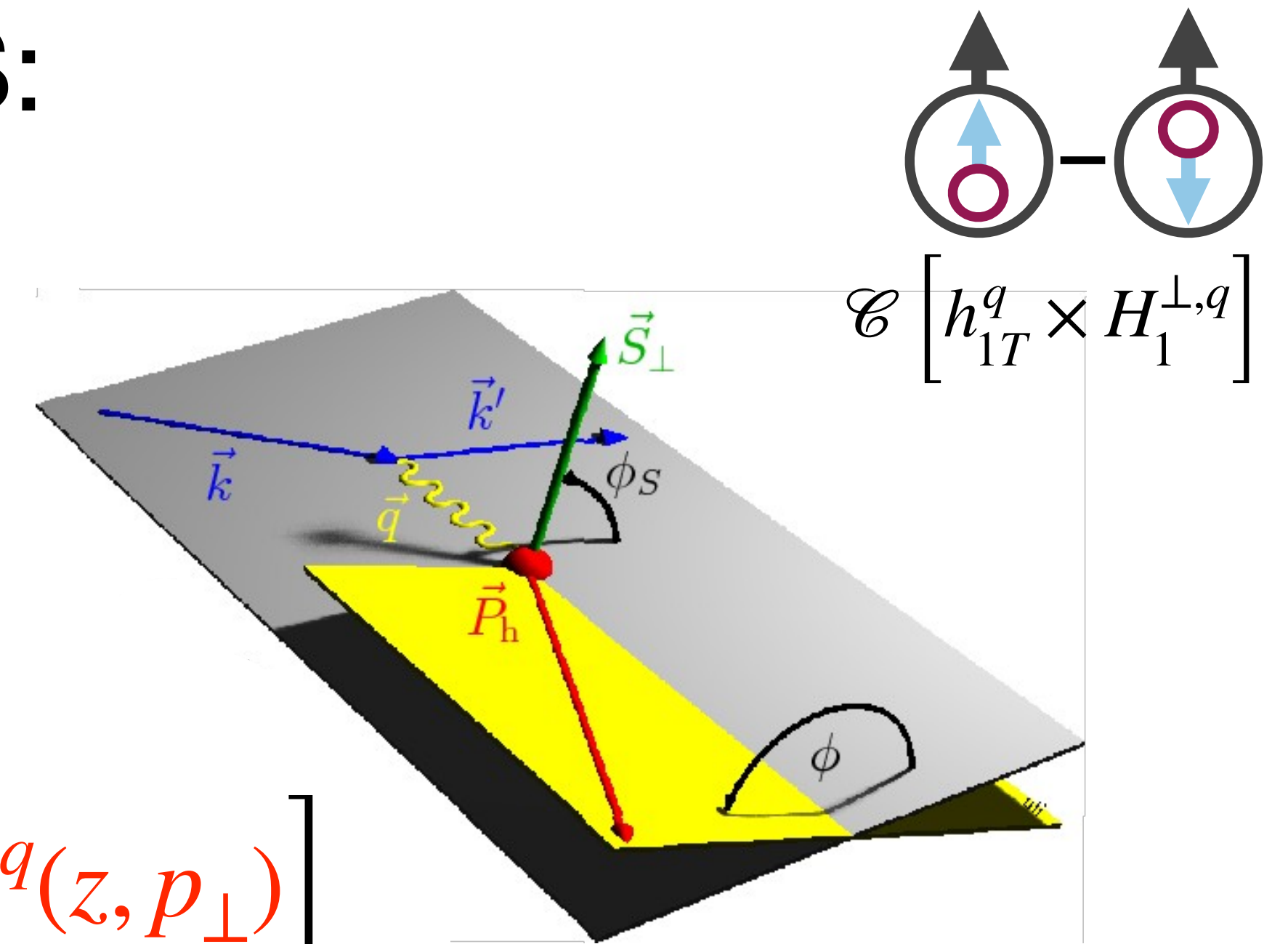
$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 C \left[h_{1T}^q(x, k_\perp) \times H_1^{\perp, q}(z, p_\perp) \right]$$



Access to transversity in semi-inclusive DIS: Collins amplitude

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

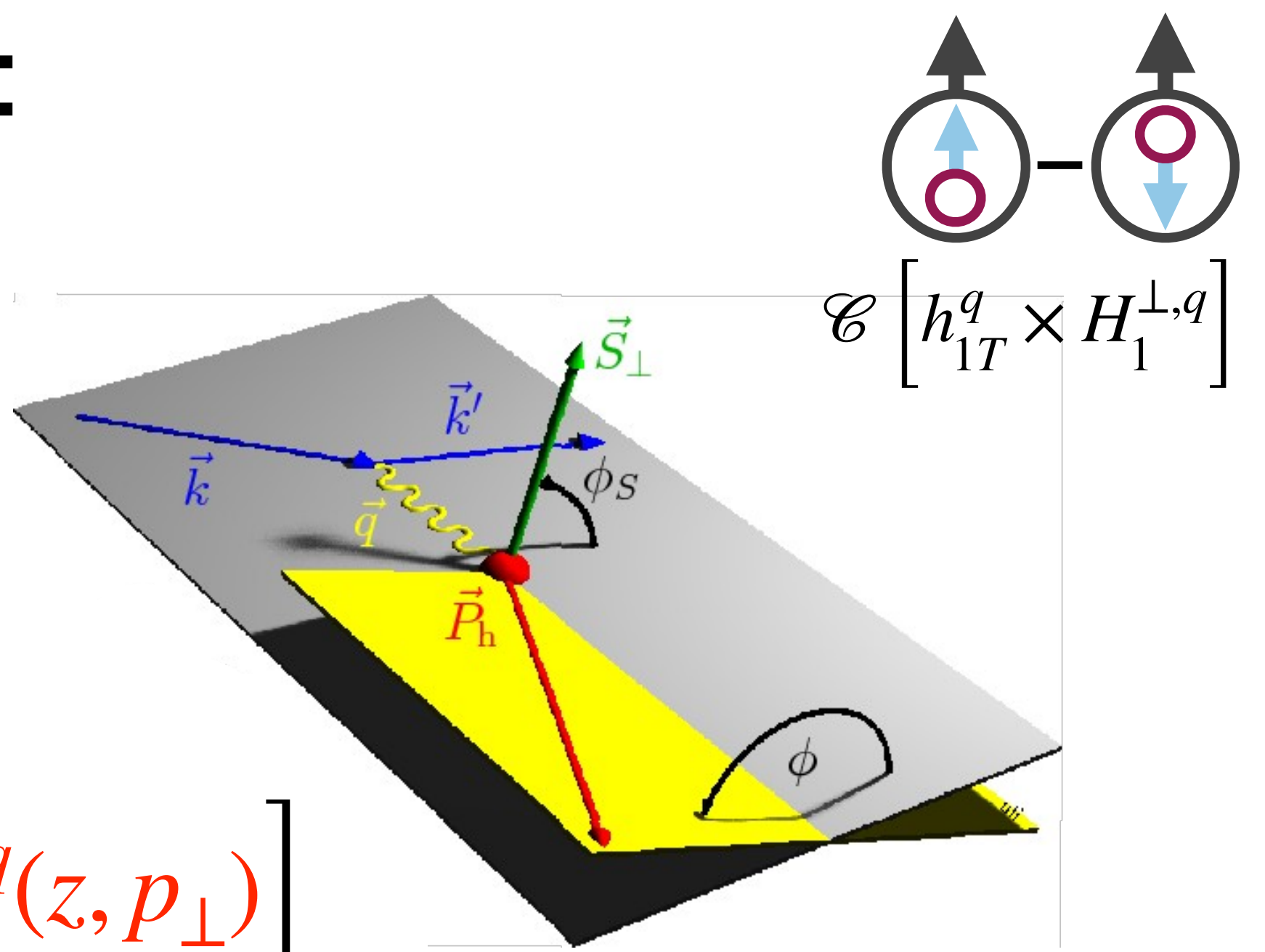
$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 C \left[h_{1T}^q(x, k_\perp) \times H_1^{\perp, q}(z, p_\perp) \right]$$



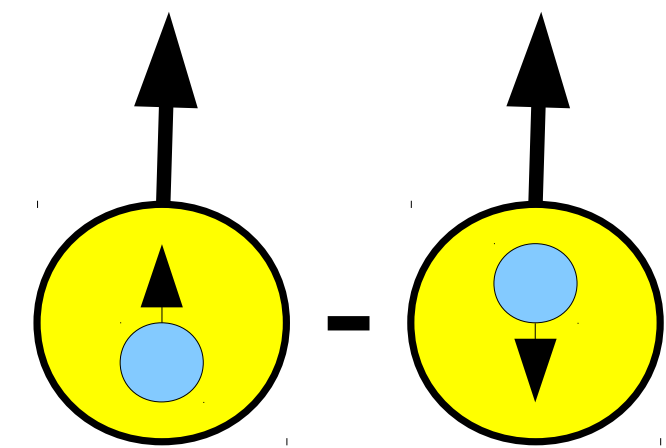
Access to transversity in semi-inclusive DIS: Collins amplitude

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

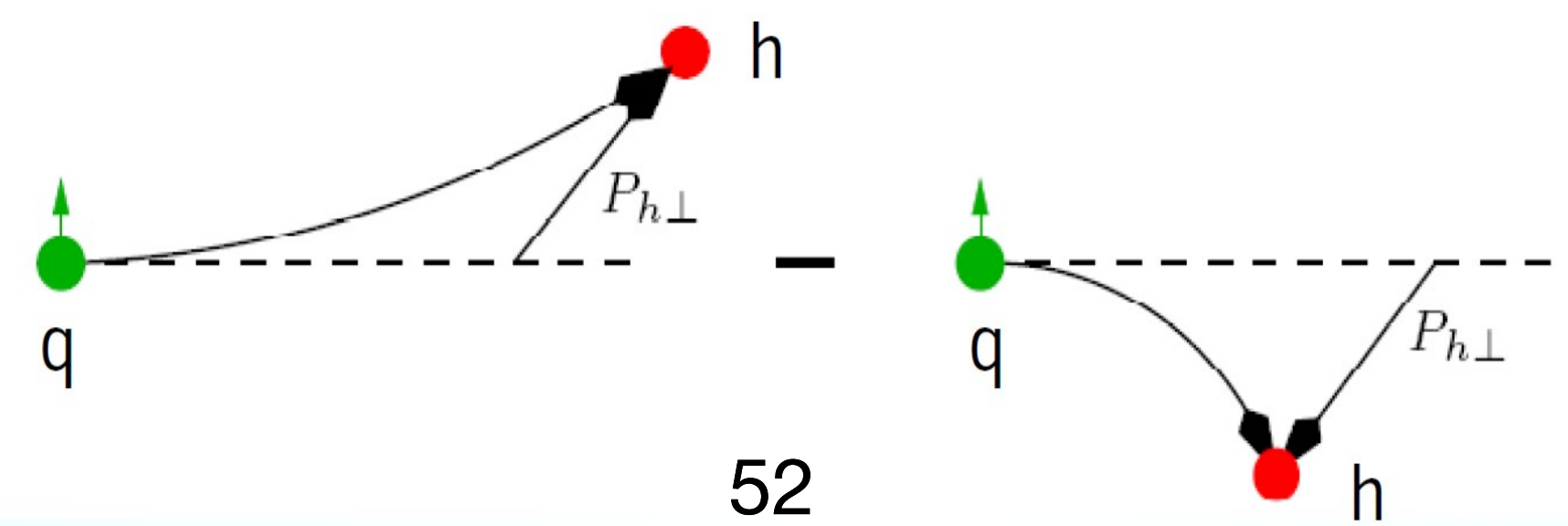
$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 C \left[h_{1T}^q(x, k_\perp) \times H_1^{\perp,q}(z, p_\perp) \right]$$



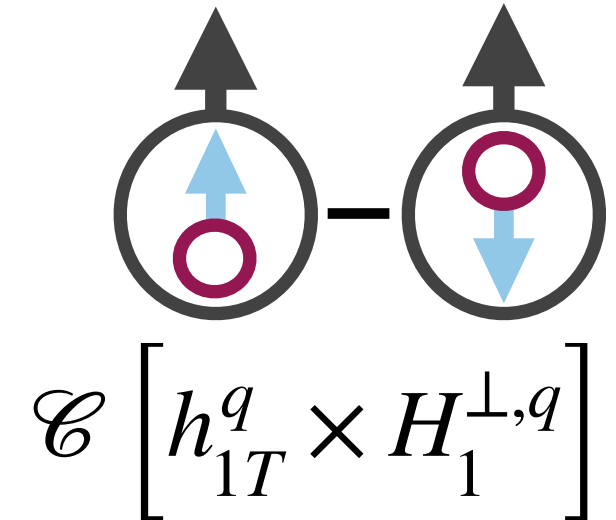
$h_{1T}^q(x, k_\perp)$: transversity



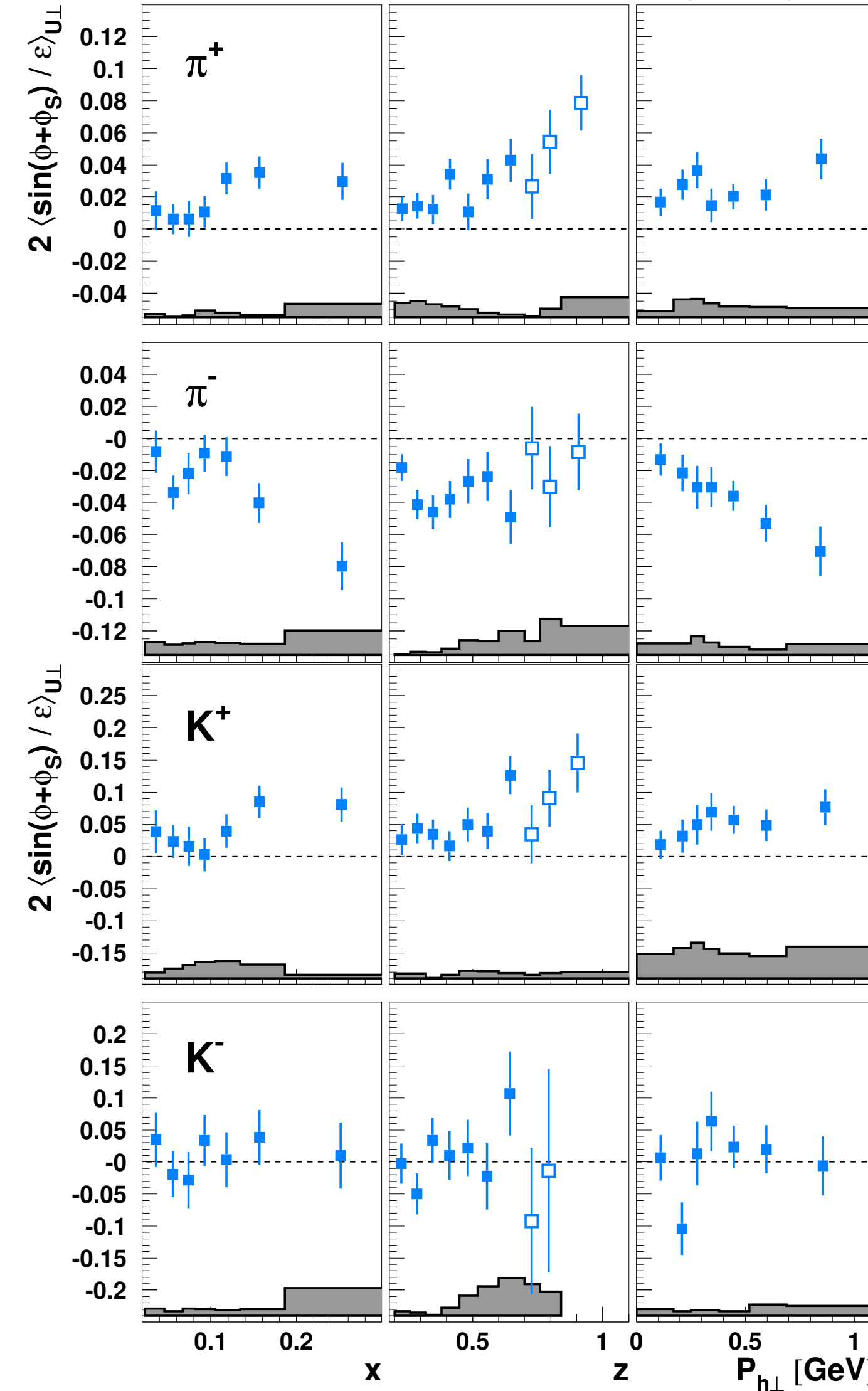
$H_1^{\perp,q}(z, p_\perp)$: Collins fragmentation function



Collins amplitudes



HERMES, JHEP 12(2020)010



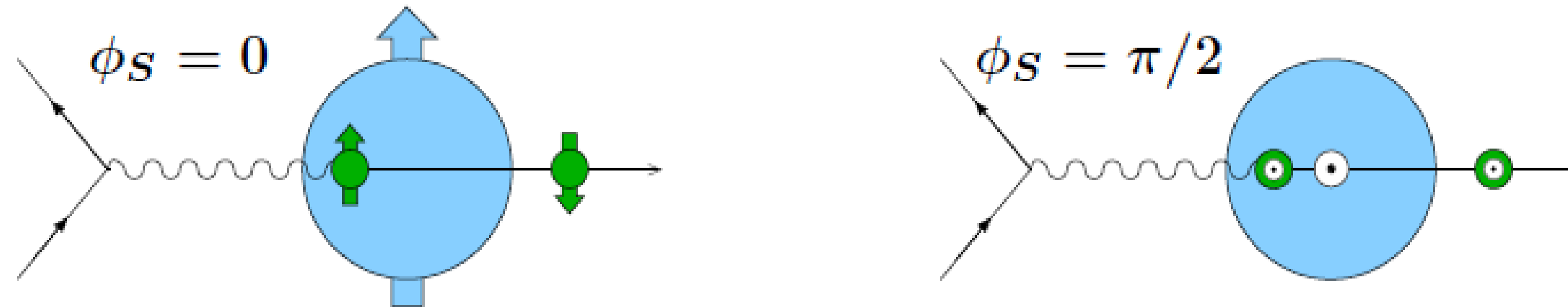
- Oppositely signed amplitudes for π^+ and π^- :

$$H_1^\perp, u \rightarrow \pi^+ \approx -H_1^\perp, u \rightarrow \pi^-$$

Artru model

X. Artru et al., Z. Phys. C73 (1997) 527

polarisation component in lepton scattering plane reversed by photoabsorption:



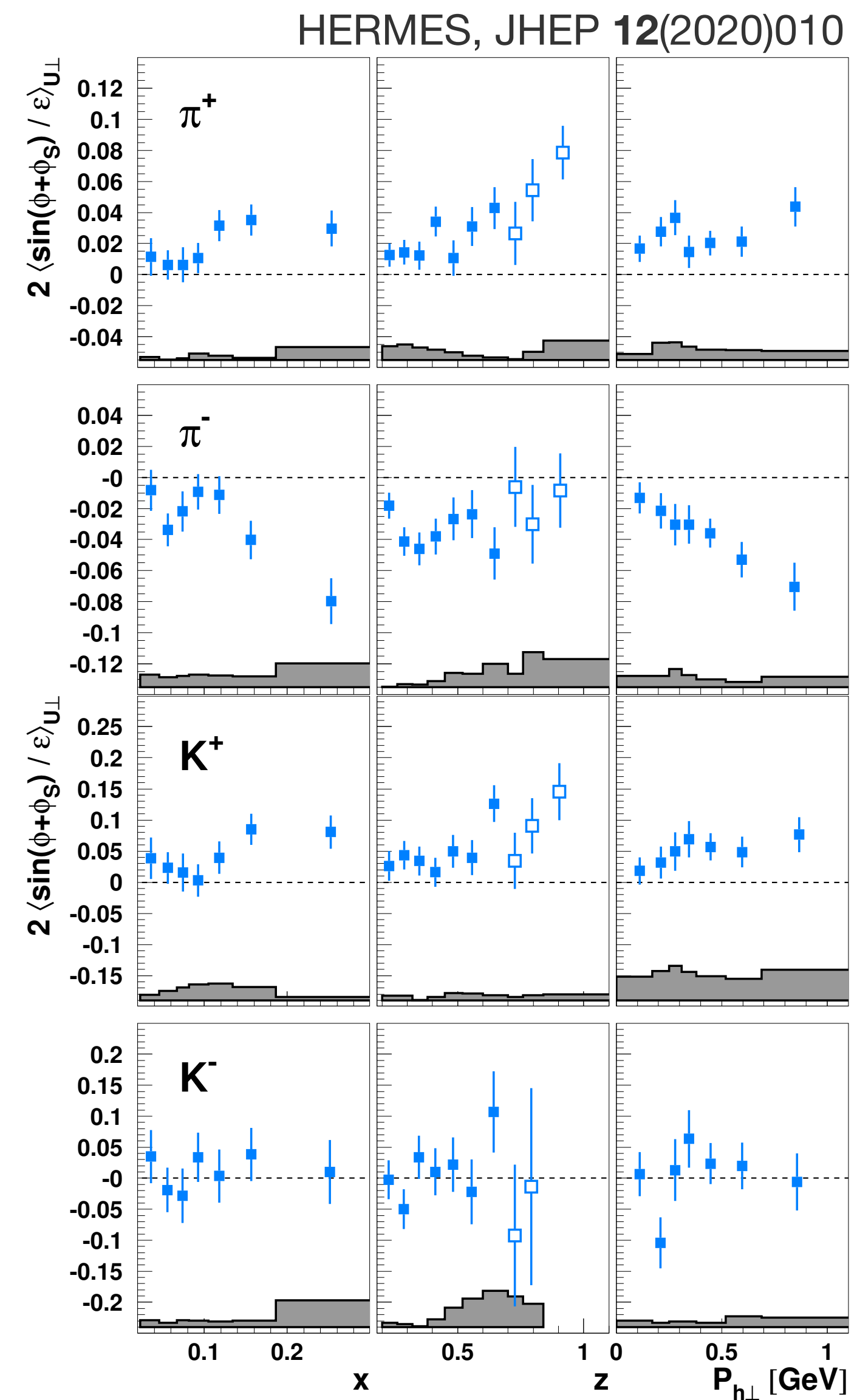
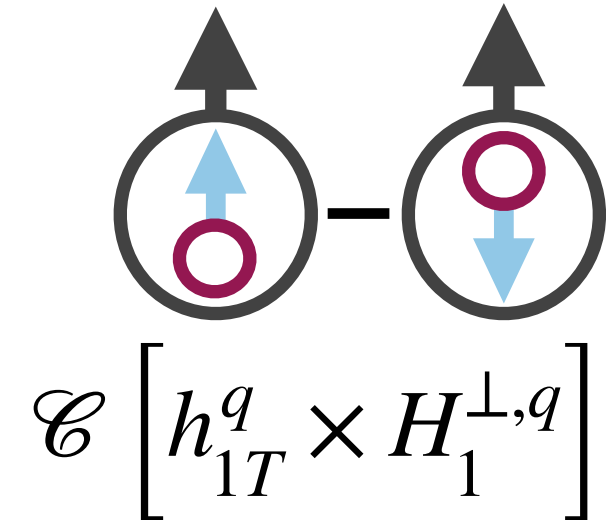
string break, quark-antiquark pair with vacuum numbers:



orbital angular momentum creates transverse momentum:



Collins amplitudes



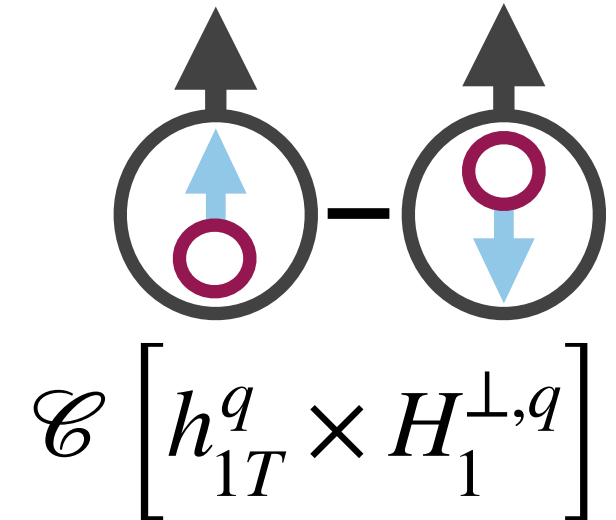
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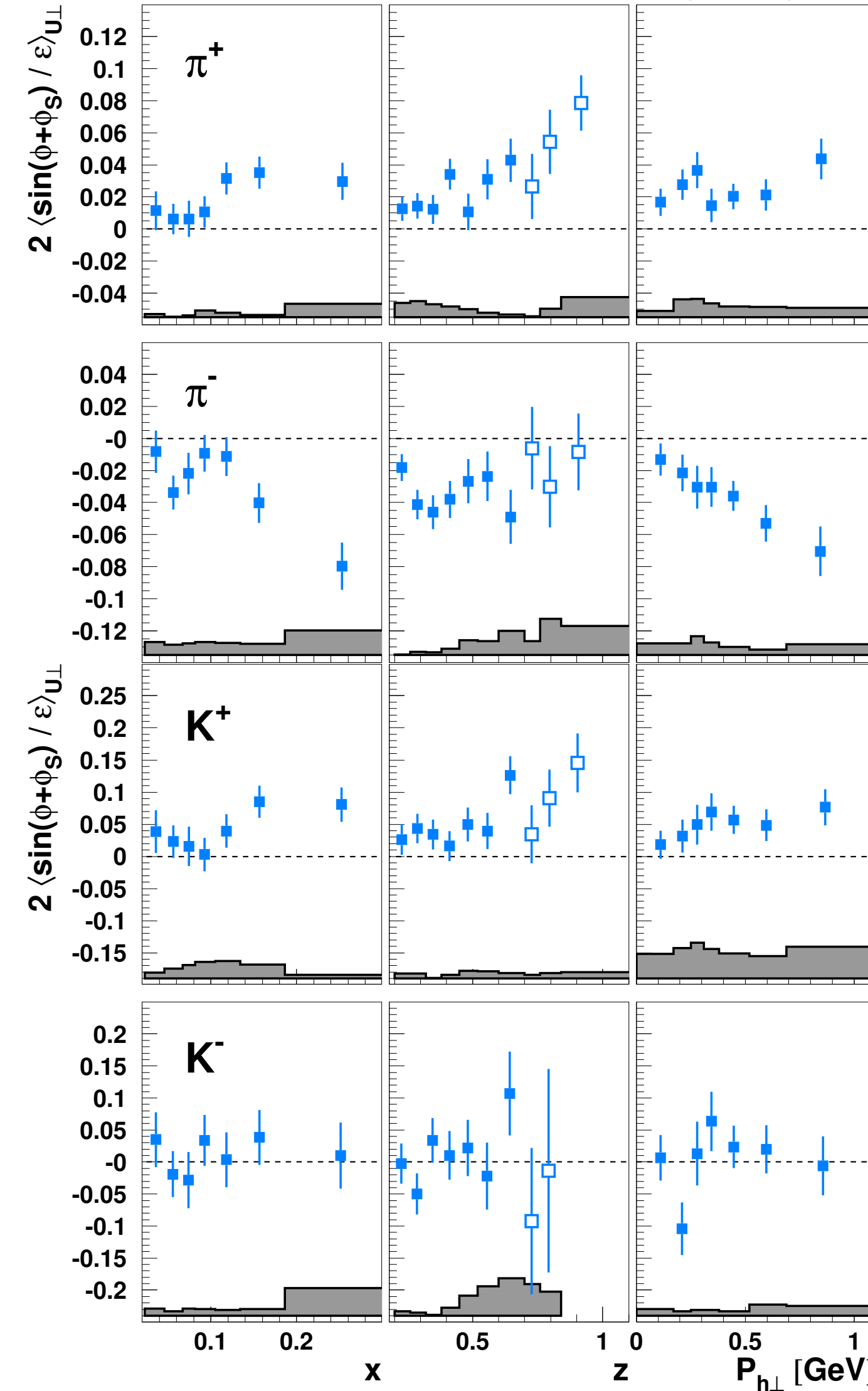
- Amplitudes for K^+ larger than for π^+ :

$$H_1^{\perp, u \rightarrow K^+} > H_1^{\perp, u \rightarrow \pi^+}$$

Collins amplitudes



HERMES, JHEP 12(2020)010



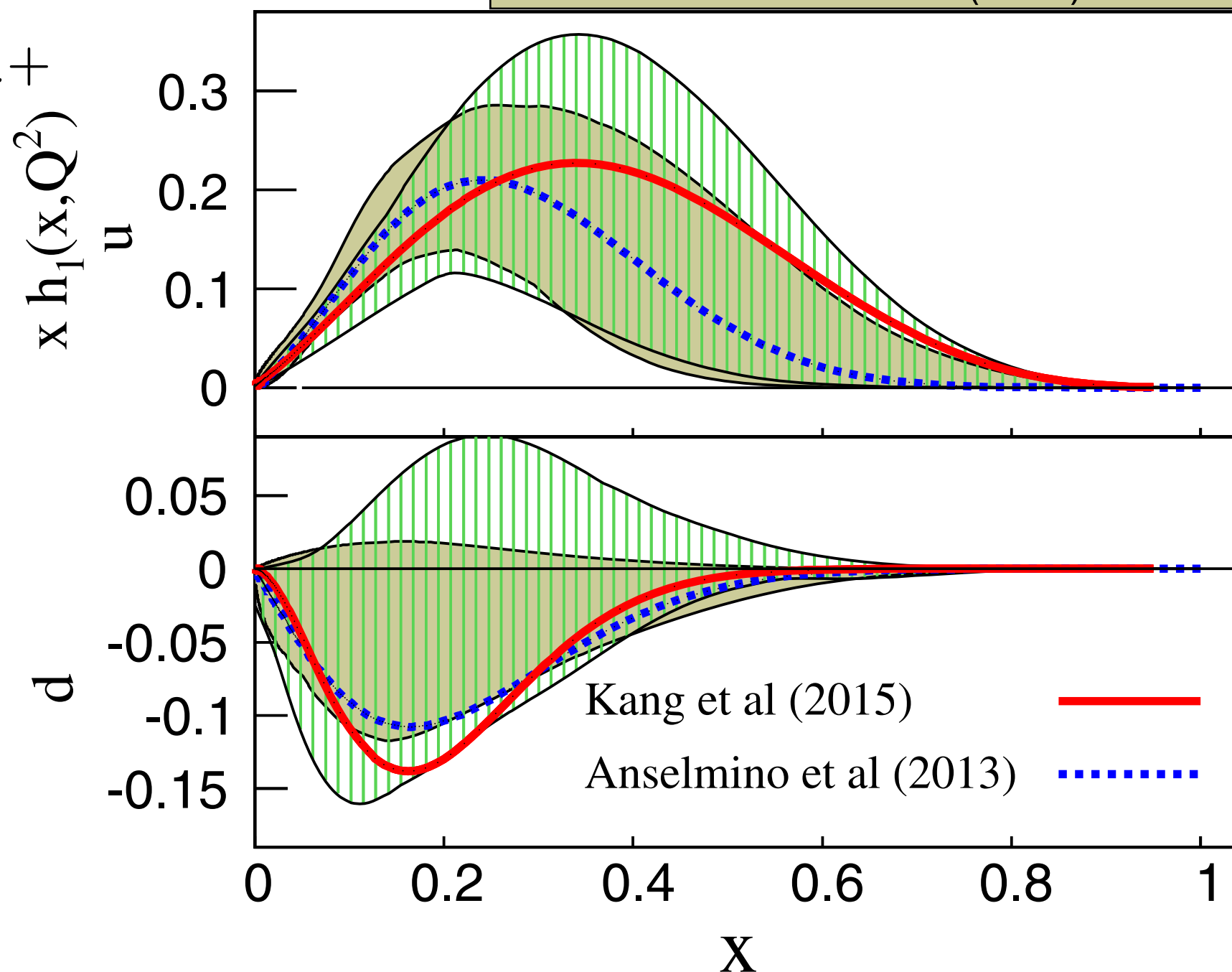
- Oppositely signed amplitudes for π^+ and π^- :

$$H_1^{\perp, u \rightarrow \pi^+} \approx -H_1^{\perp, u \rightarrow \pi^-}$$

- Amplitudes for K^+ larger than for π^+ :

$$H_1^{\perp, u \rightarrow K^+} > H_1^{\perp, u \rightarrow \pi^+}$$

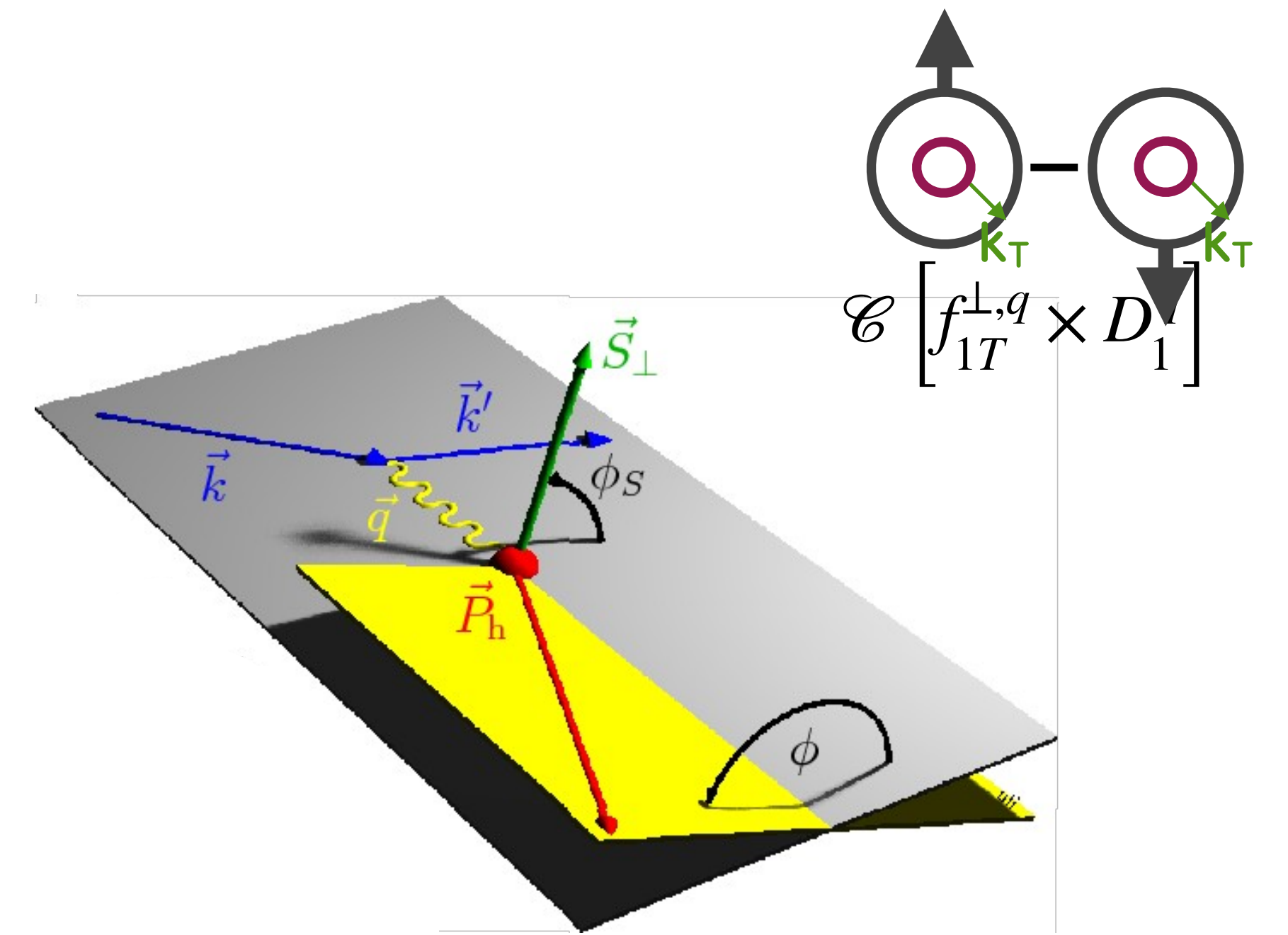
Kang et al., PRD 93 (2016) 014009
 Anselmino et al. PRD 87 (2013) 094019



data from Belle, Babar, COMPASS, HERMES, Jefferson Lab Hall A

Access to Sivers in semi-inclusive DIS

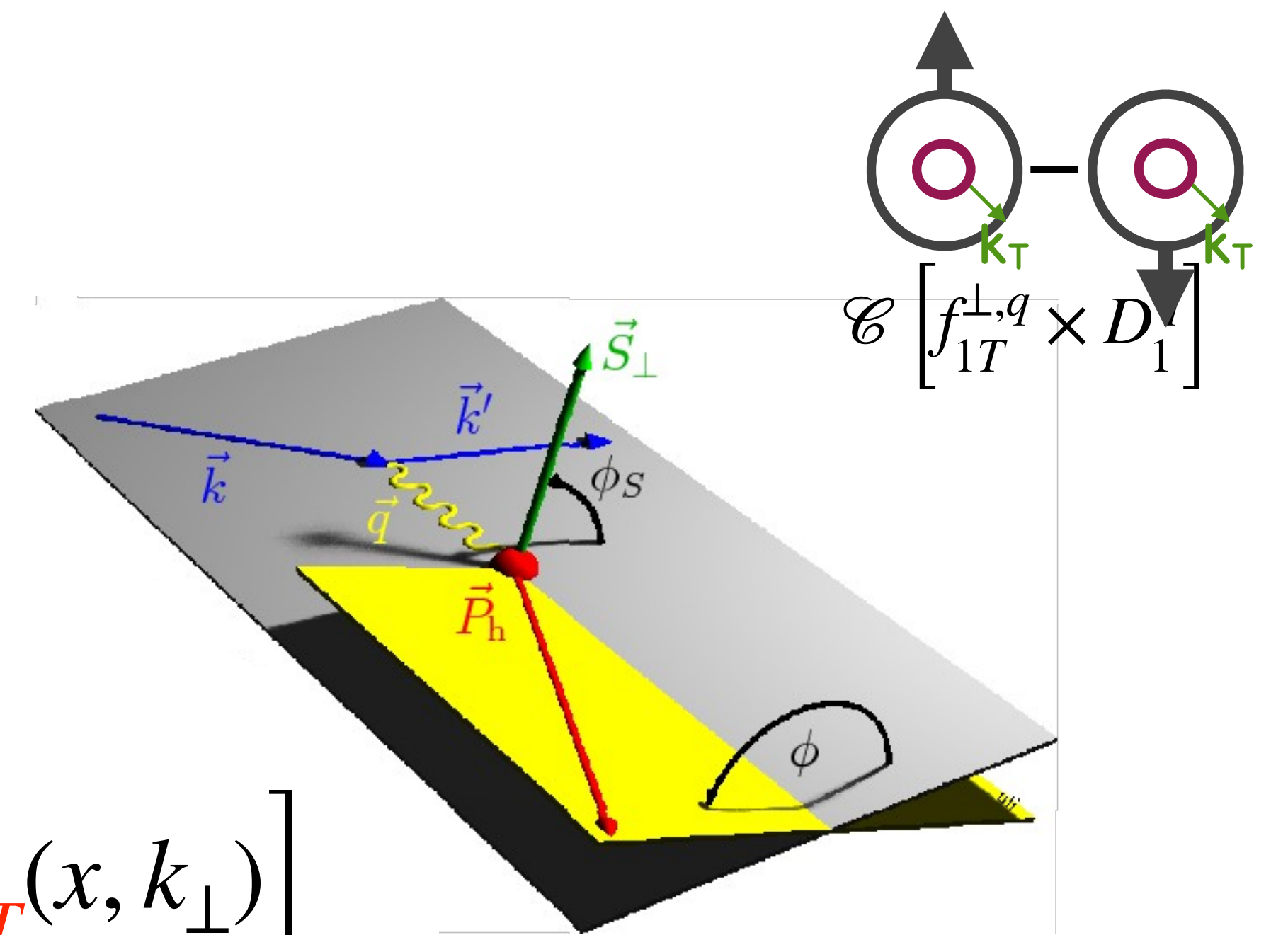
$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$



Access to Sivers in semi-inclusive DIS

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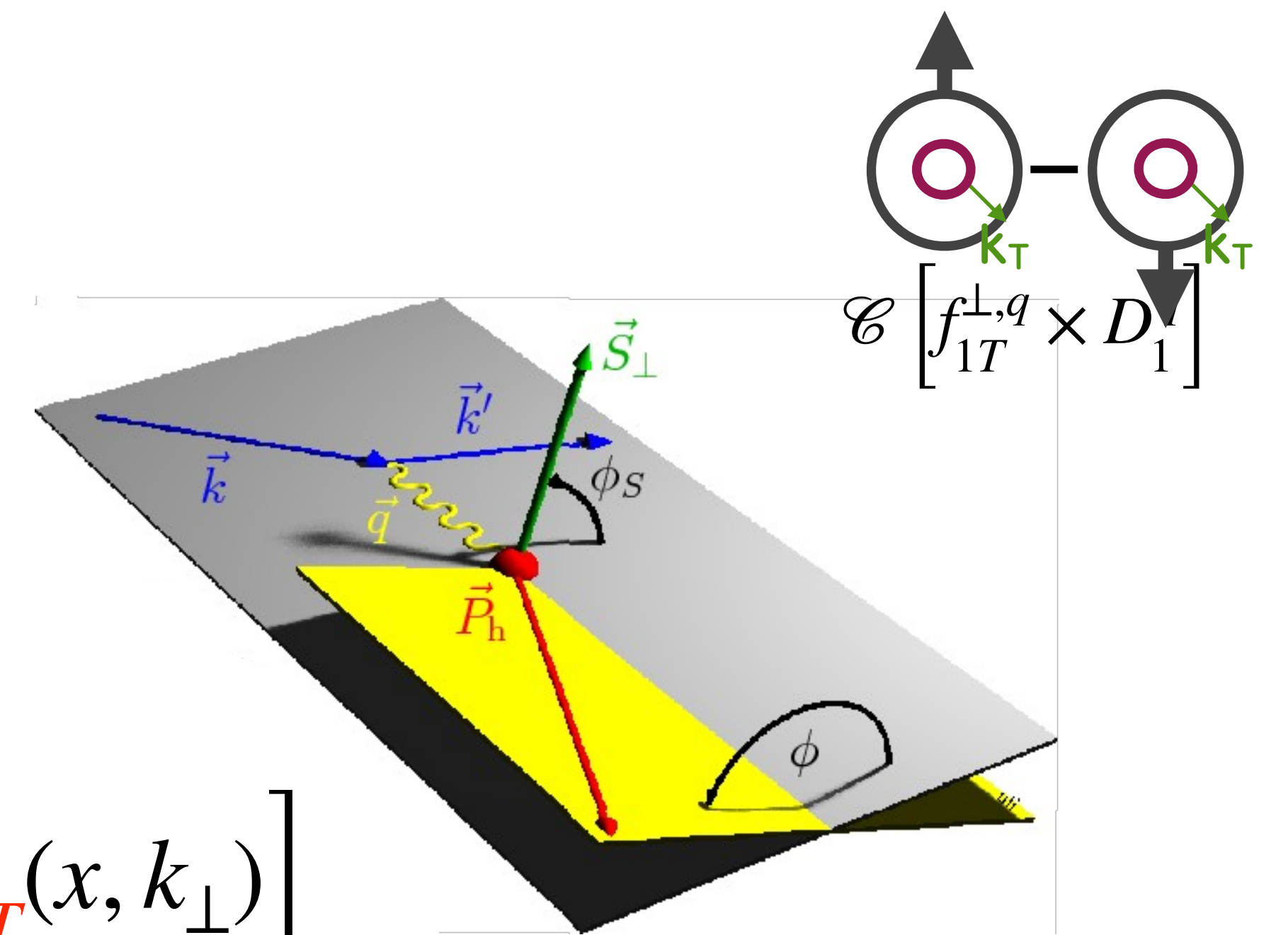
$$\sim \sin(\phi - \phi_S) \sum_q e_q^2 C \left[f_{1T}^{\perp,q}(x, k_\perp) \times D_{1T}^q(x, k_\perp) \right]$$



Access to Sivers in semi-inclusive DIS

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

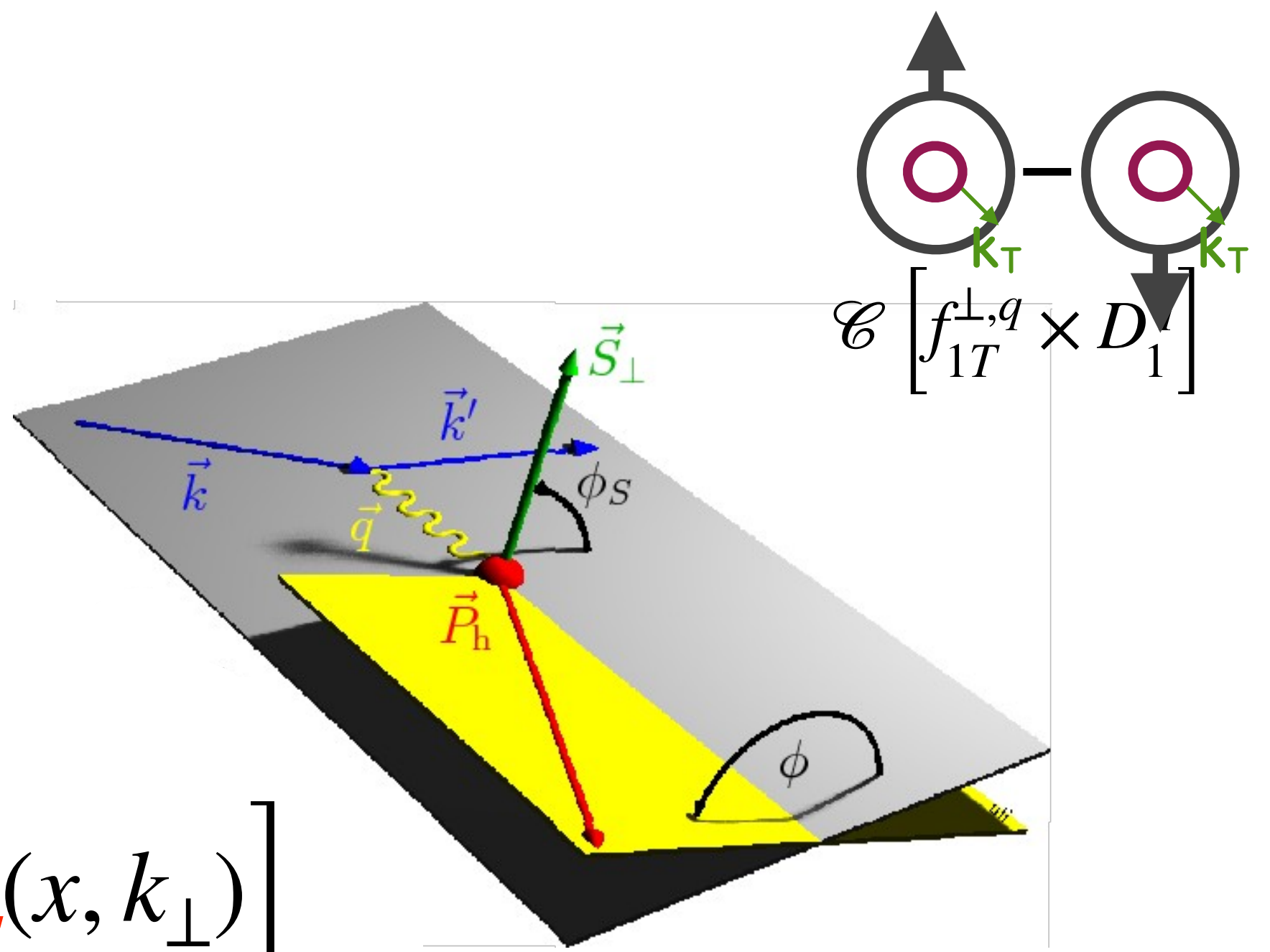
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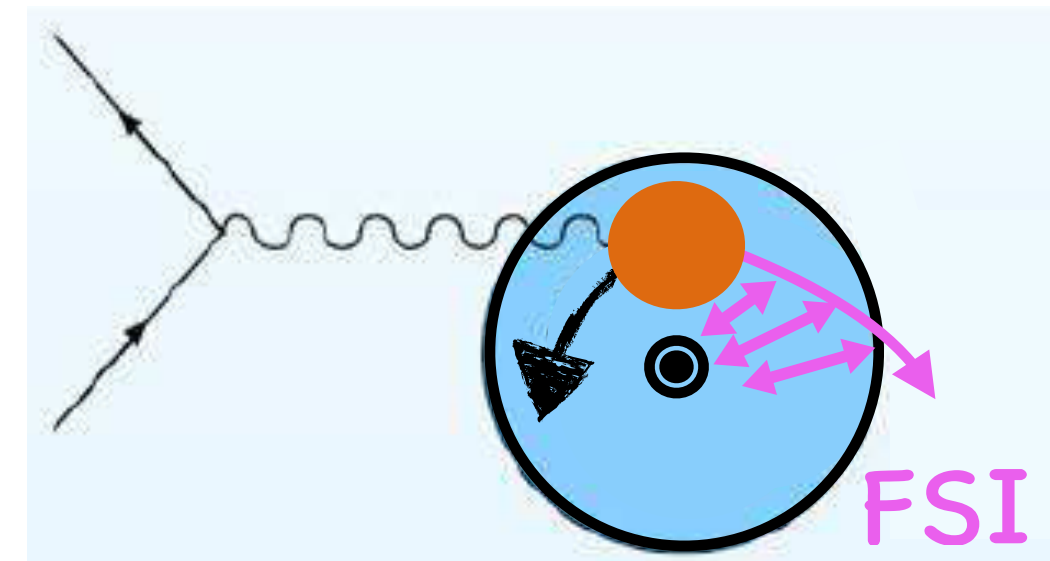
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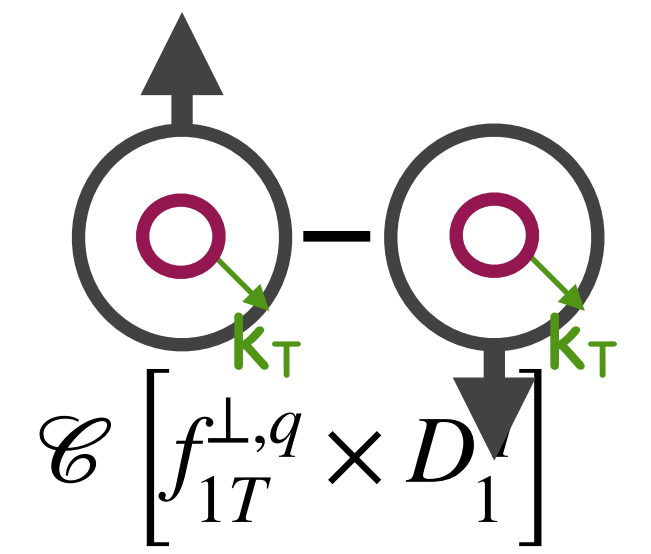
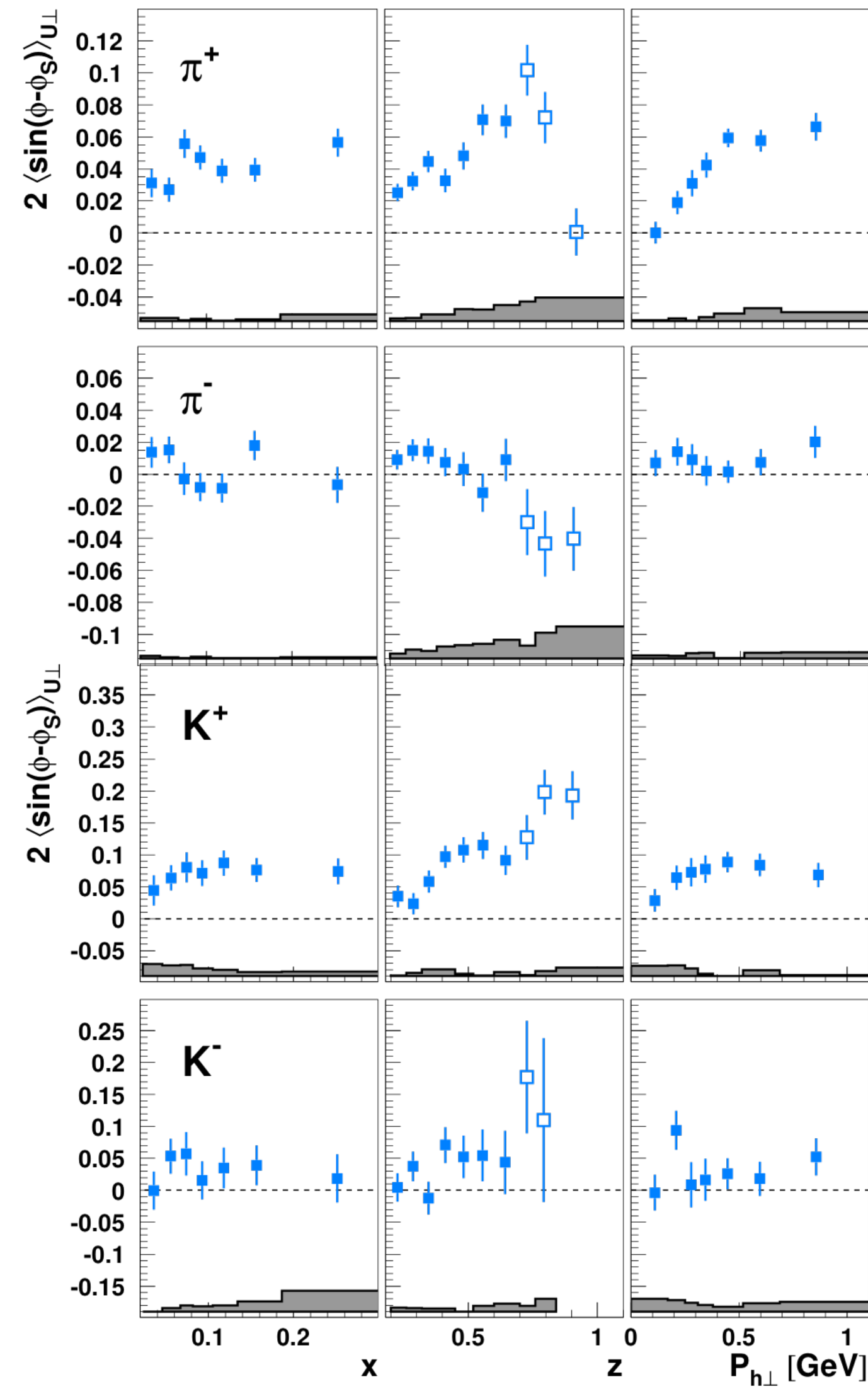


- Sivers function:
 - requires non-zero orbital angular momentum
 - final-state interactions → azimuthal asymmetries

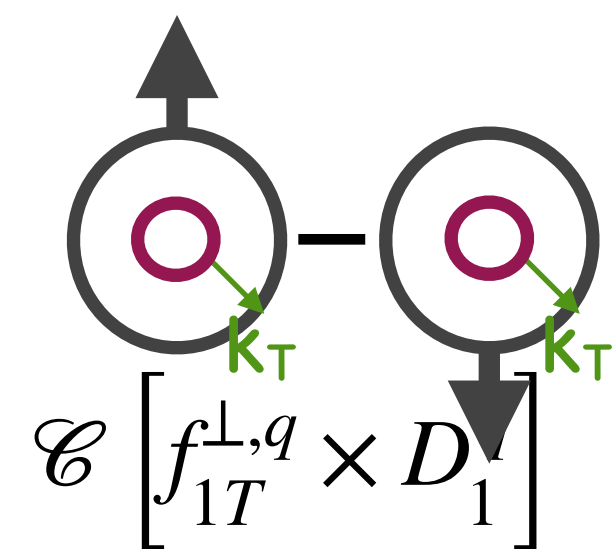


Sivers amplitudes

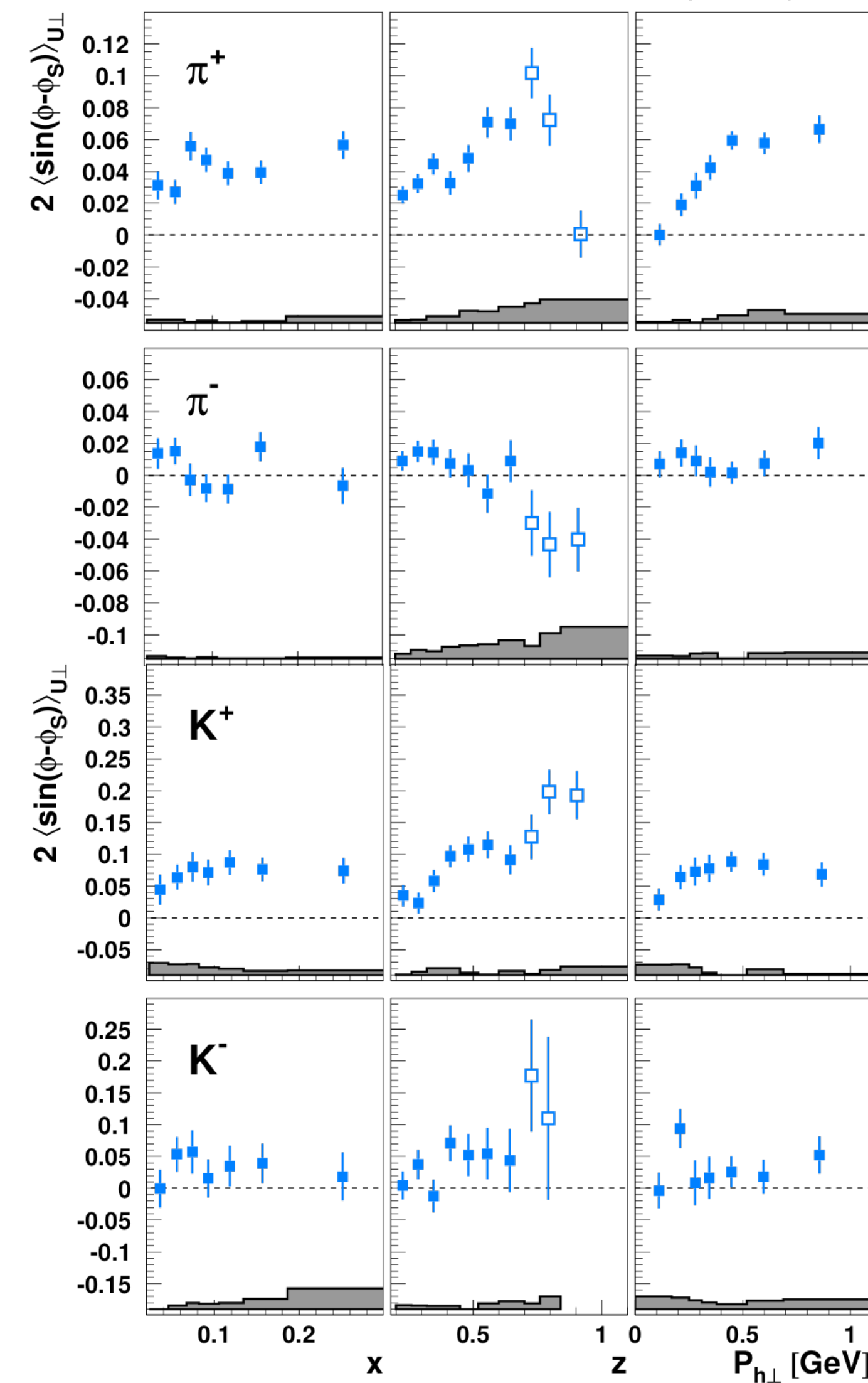
HERMES, JHEP **12**(2020)010



Sivers amplitudes

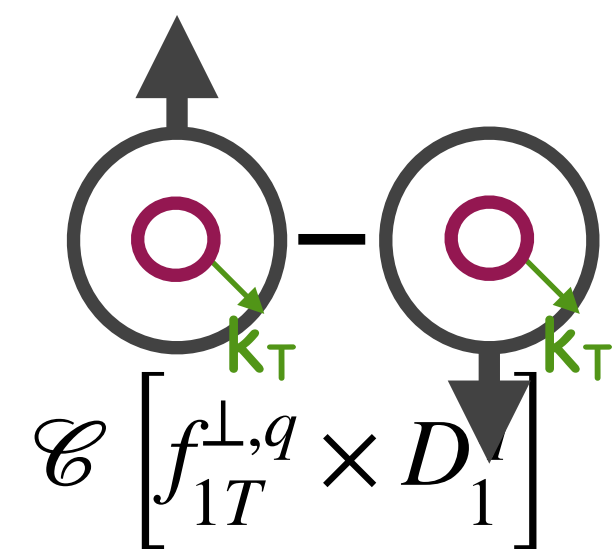


HERMES, JHEP 12(2020)010

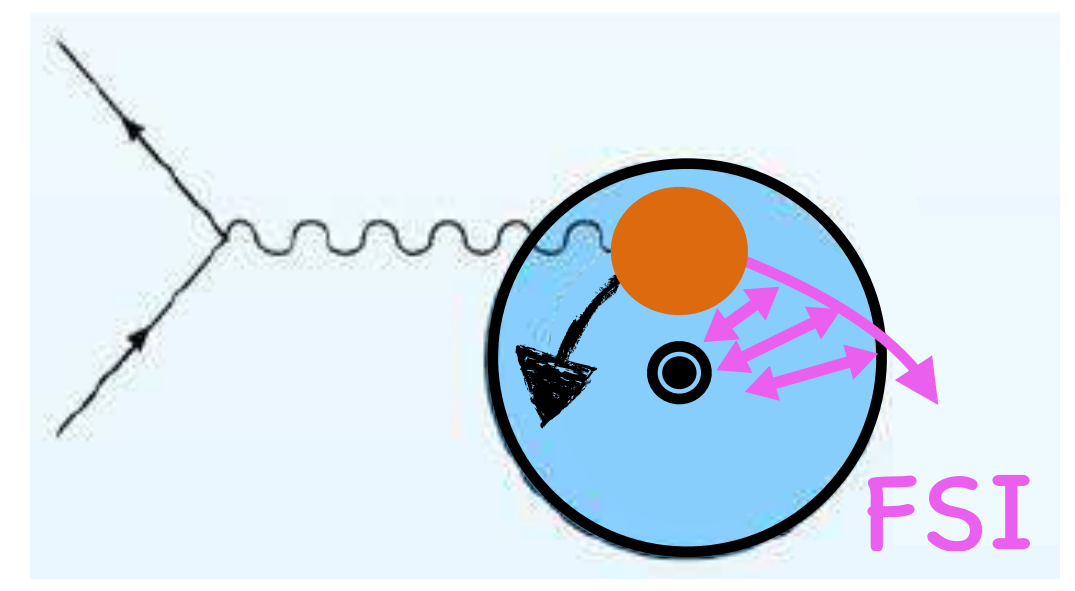
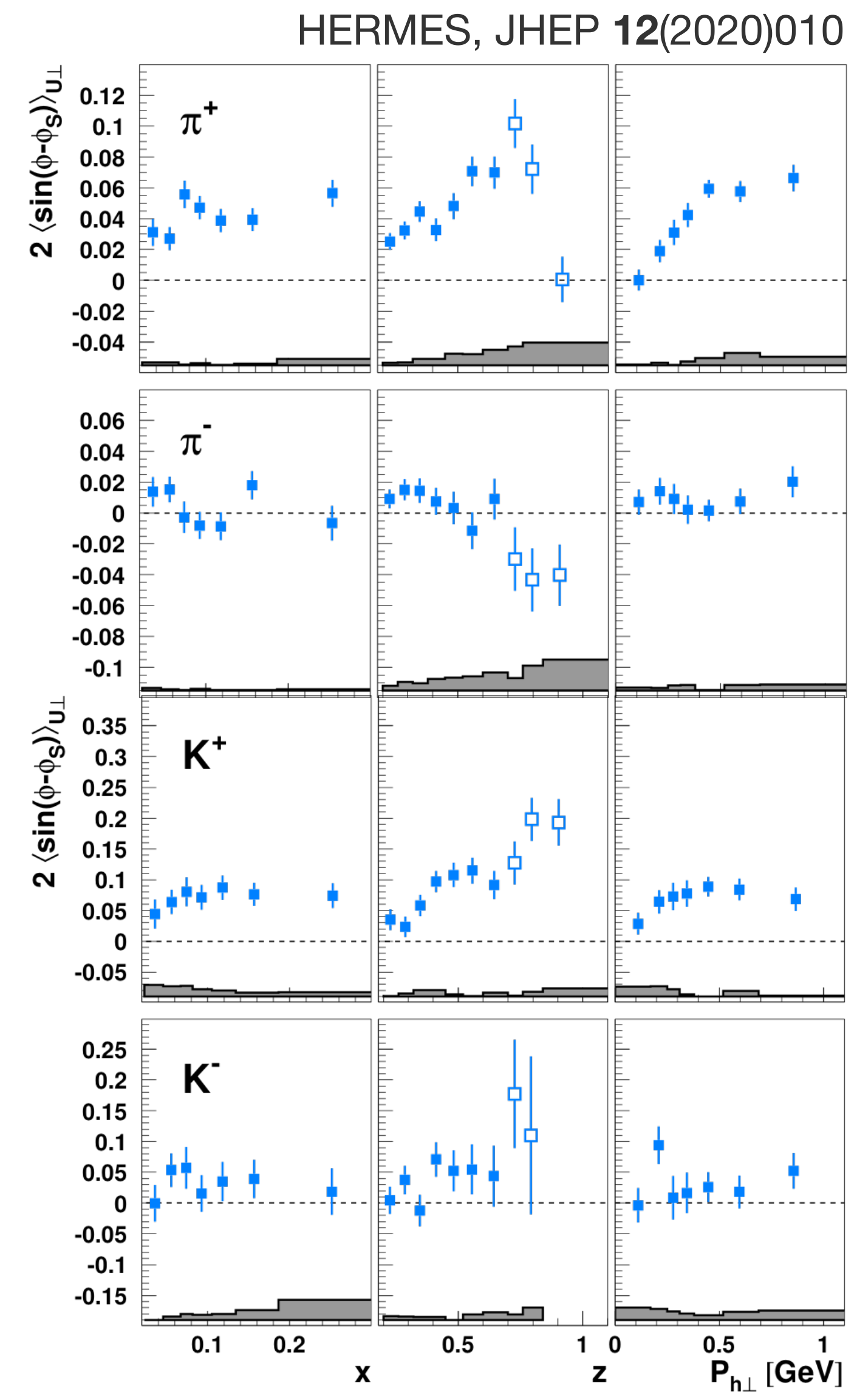


- π^+ :
 - positive \rightarrow non-zero orbital angular momentum
- π^- :
 - consistent with zero $\rightarrow u$ and d quark cancelation

Sivers amplitudes

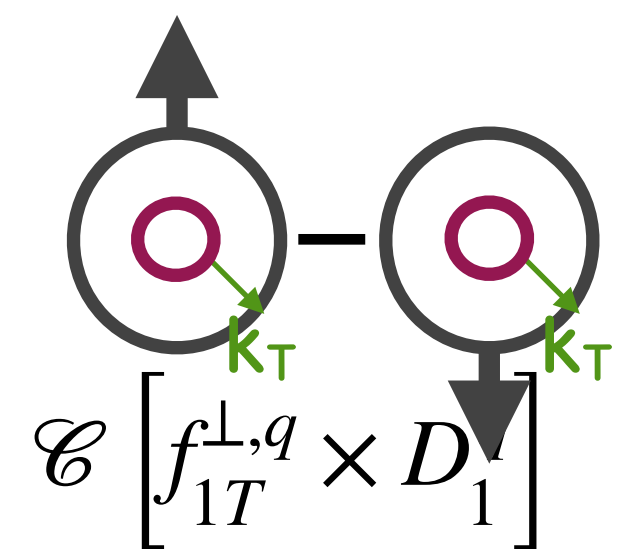
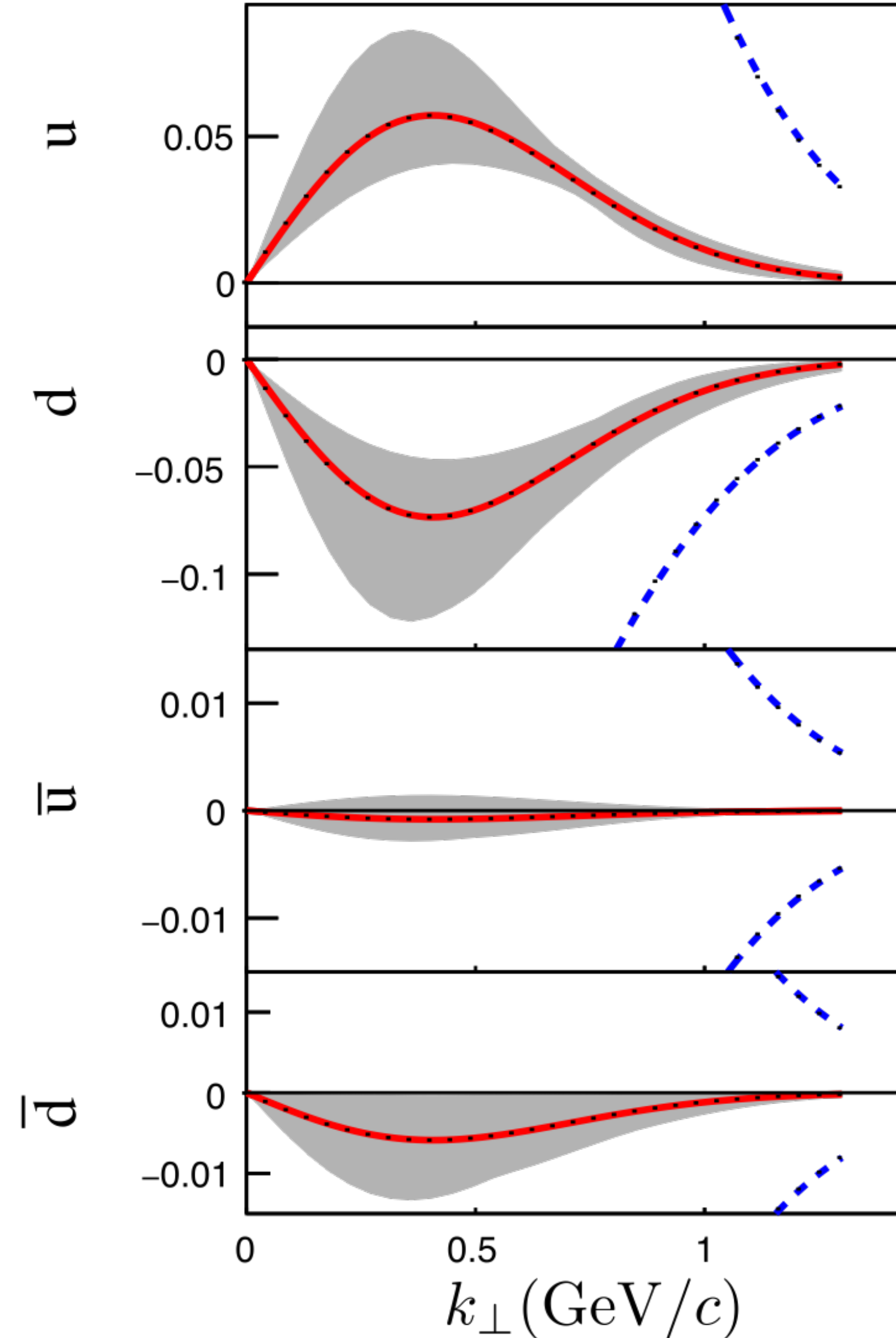


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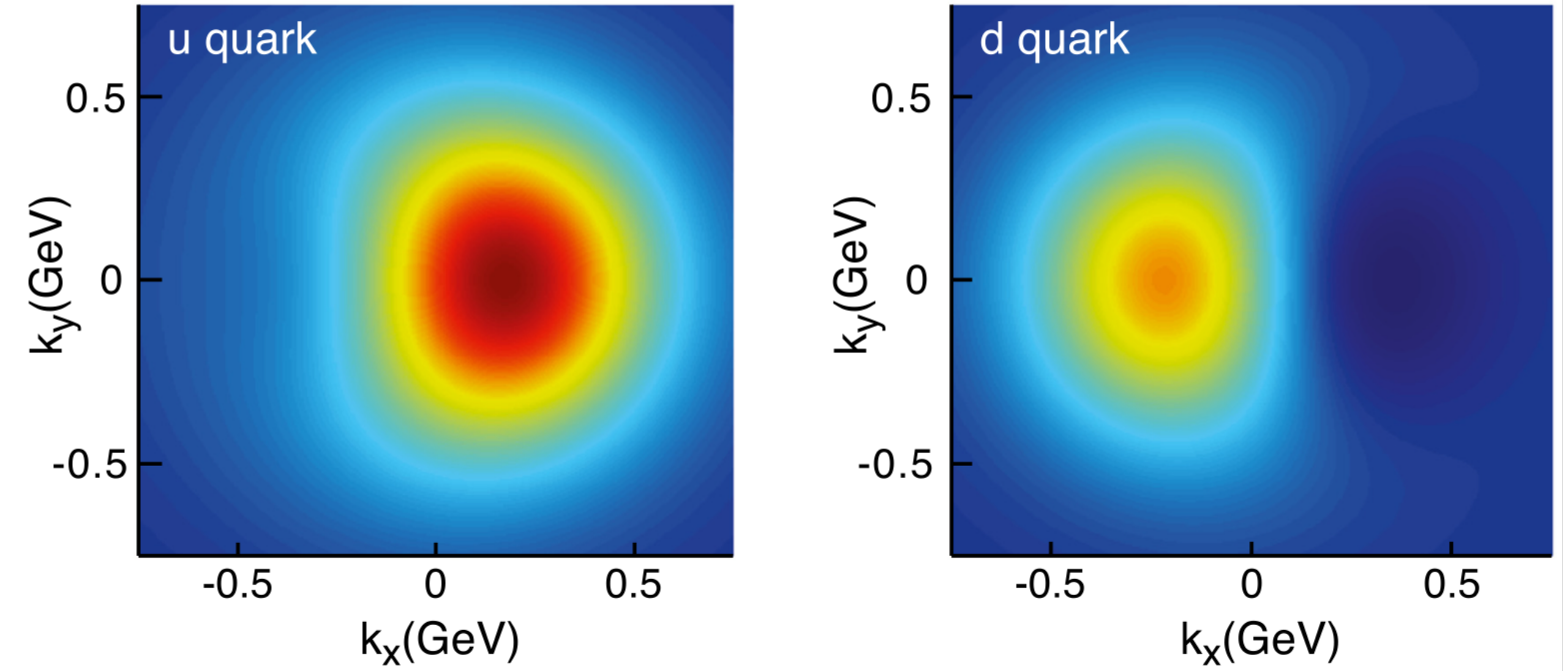
Sivers function

M. Anselmino et al., JHEP **04** (2017) 046



$x f_1(x, k_T, S_T)$

A. Accardi et al.,
Eur. Phys. J. A **52** (2016) 268



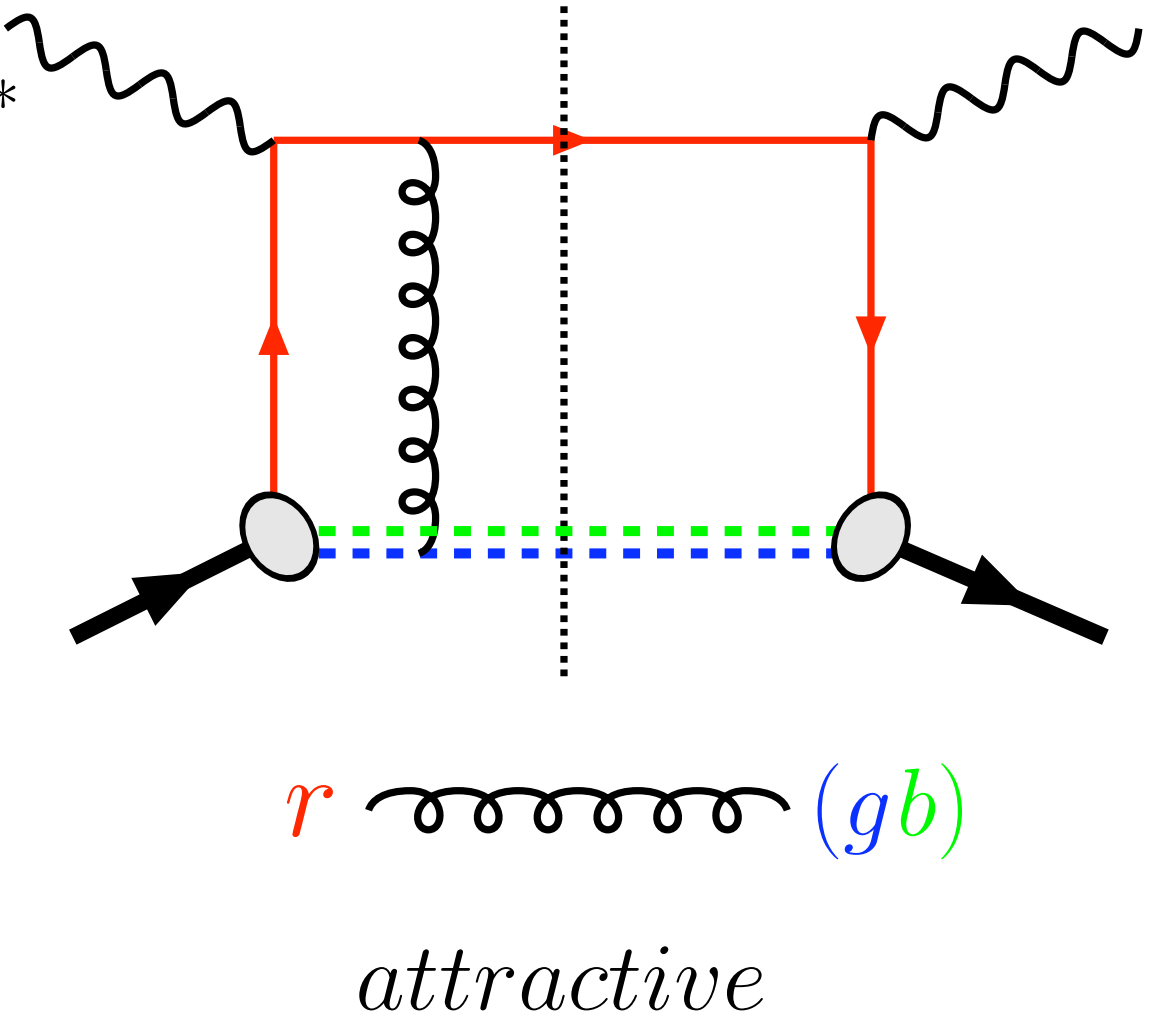
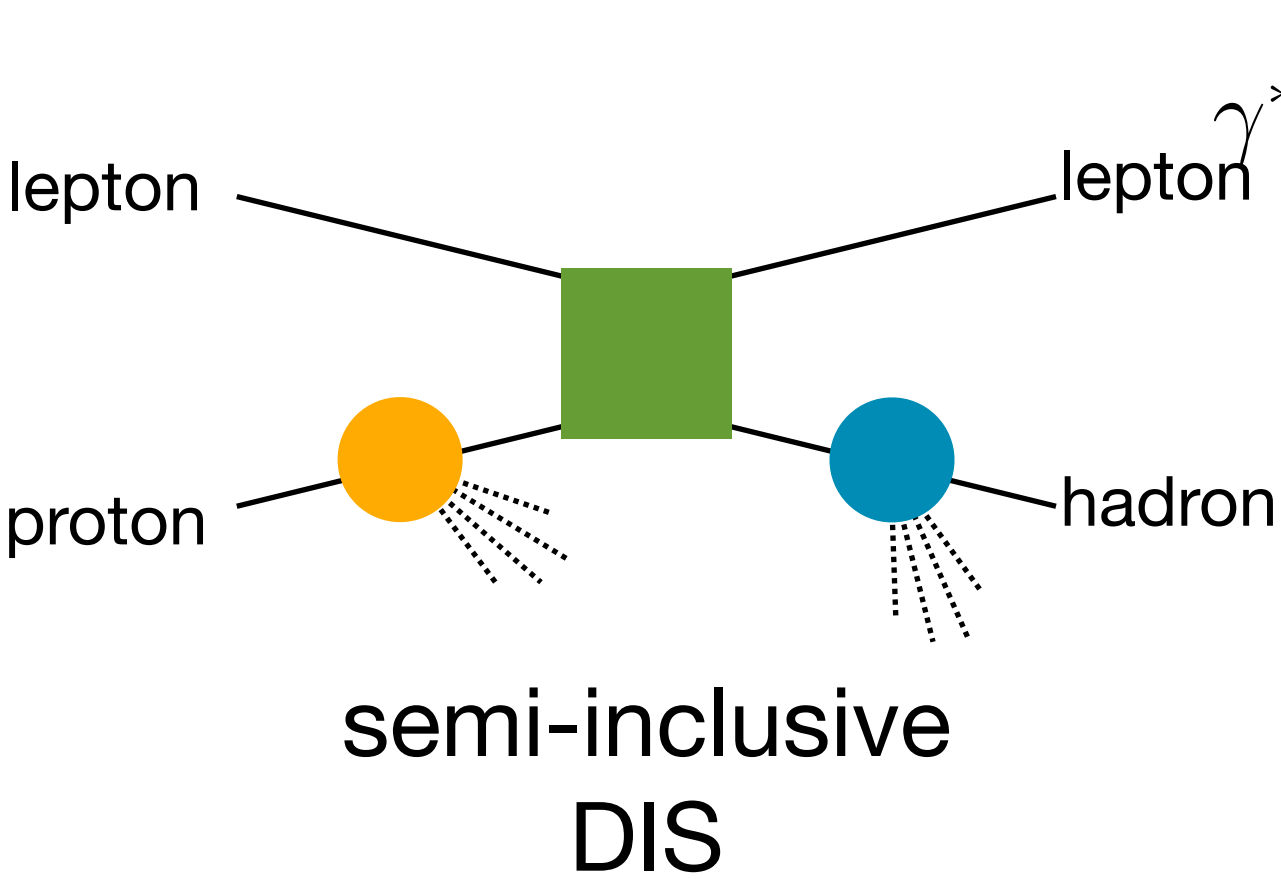
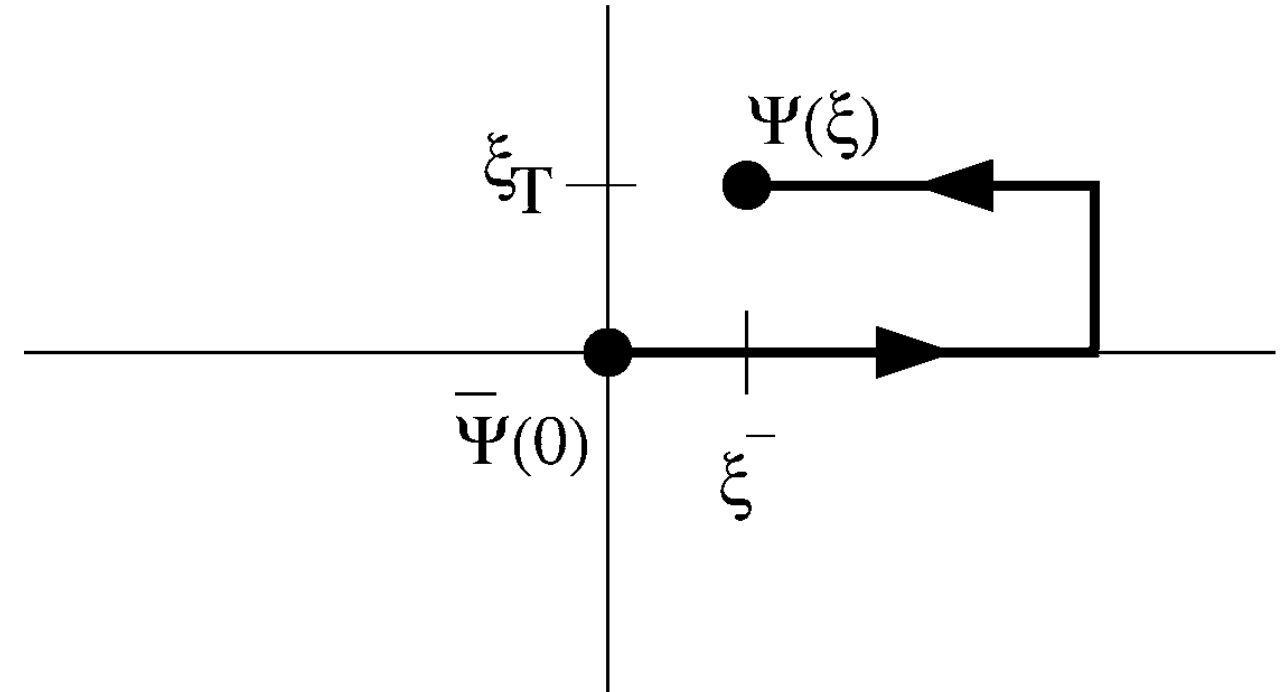
nucleon polarised along \hat{y}

Sivers: predicted sign change

$$\Phi_{ij}(p, P, S) = \frac{1}{(2\pi)^4} \int d^4\xi e^{ip \cdot \xi} \langle P, S | \bar{\psi}_j(0) U_{[0,\xi]} \psi_i(\xi) | P, S \rangle$$

J. C. Collins, Phys. Lett. B 536 (2002) 43

$W[0, \xi, \text{SIDIS}]$

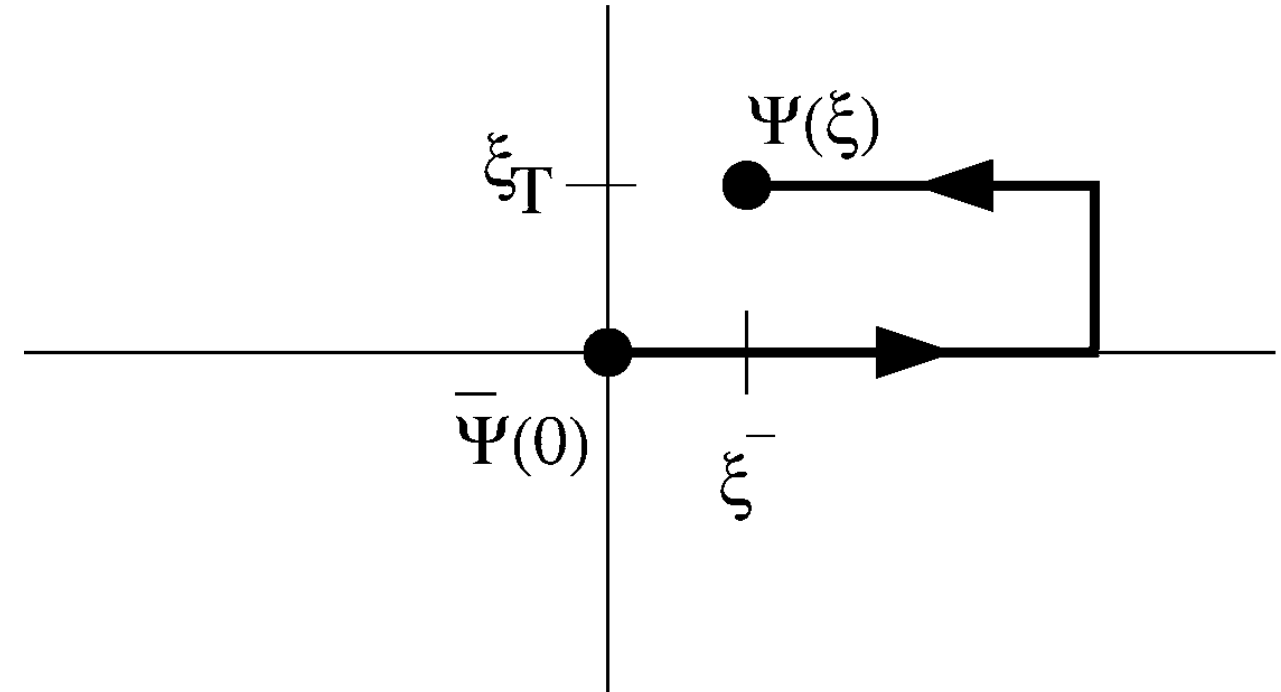


Sivers: predicted sign change

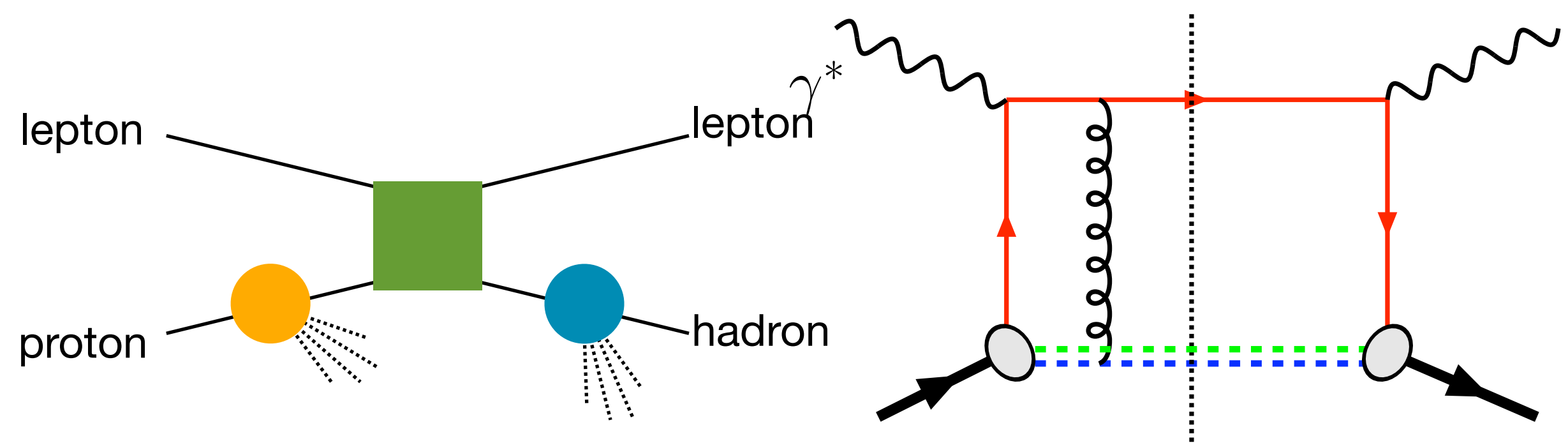
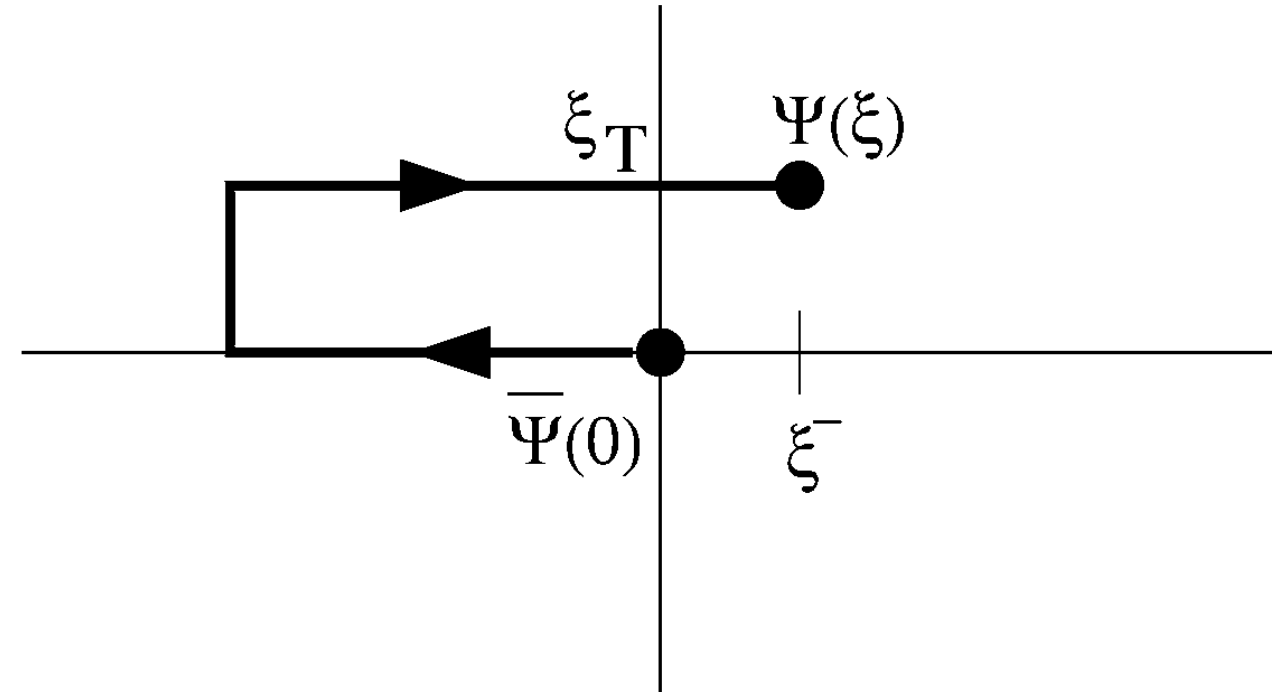
J. C. Collins, Phys. Lett. B 536 (2002) 43

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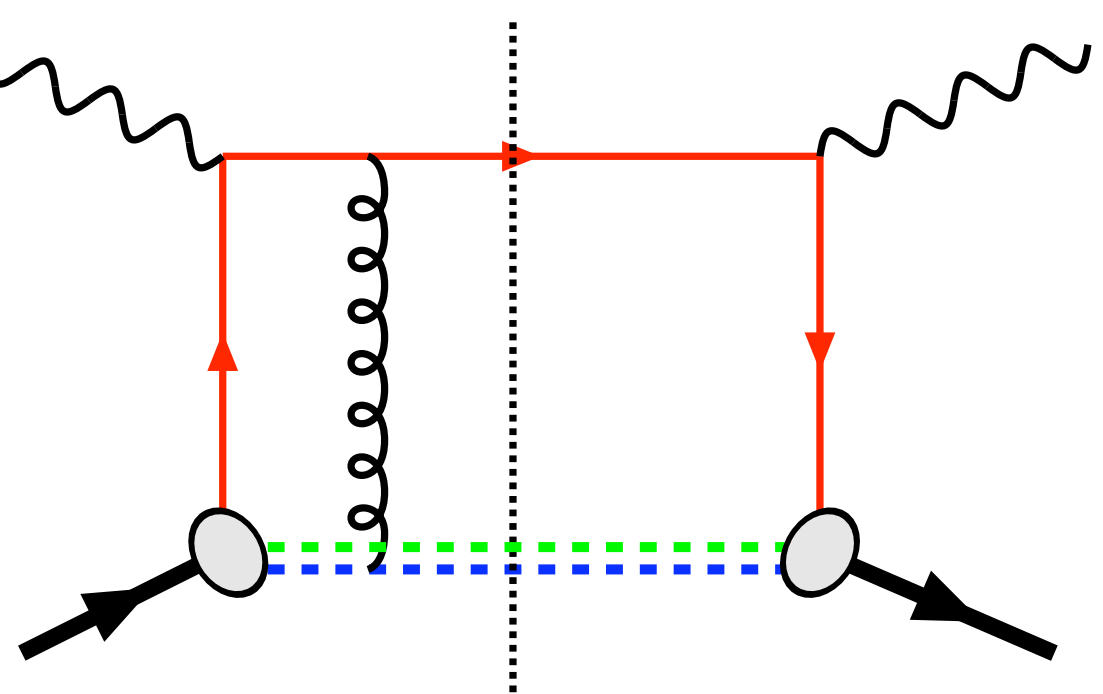
$W [0, \xi, \text{SIDIS}]$



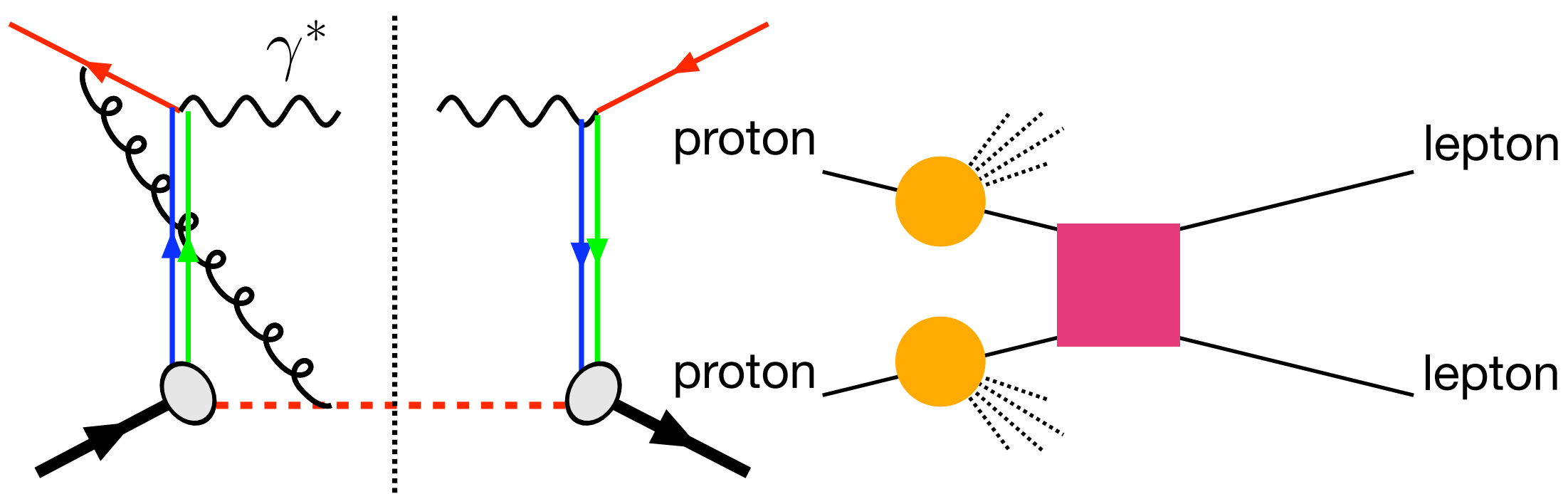
$U [\xi, \text{DY}]$



semi-inclusive DIS



r (gb)
attractive



r r
repulsive

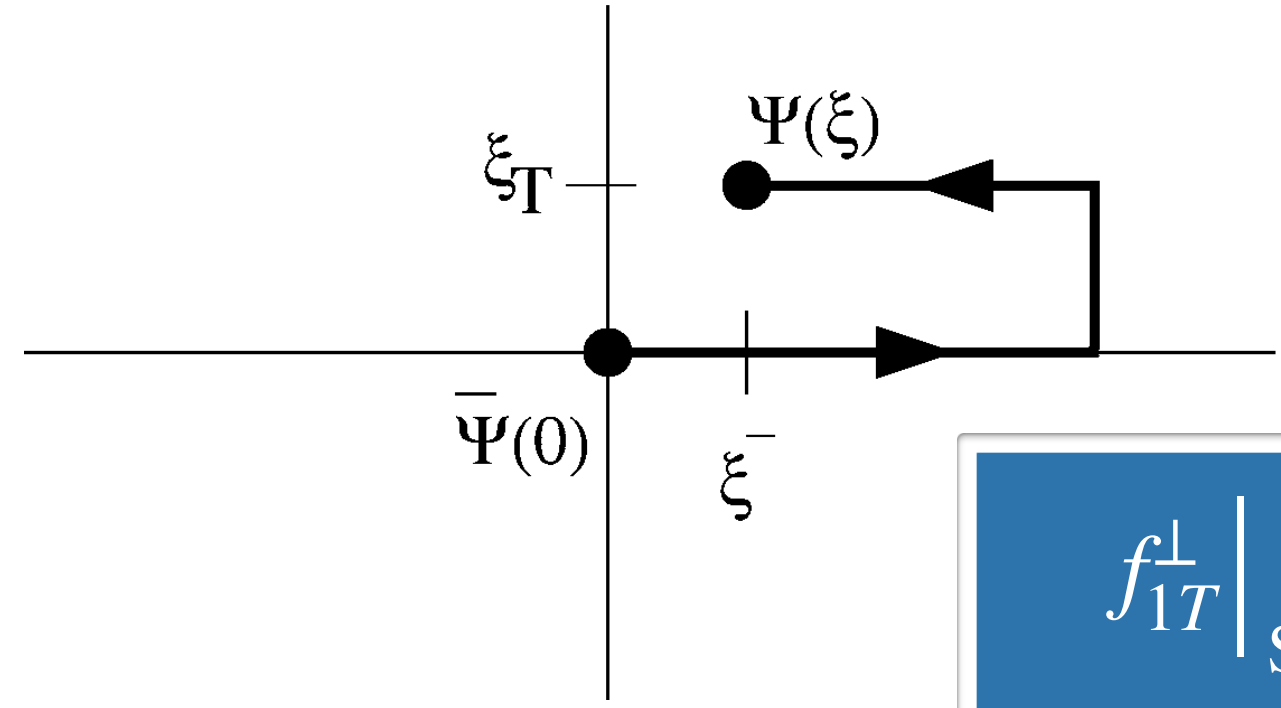
Drell-Yan

Sivers: predicted sign change

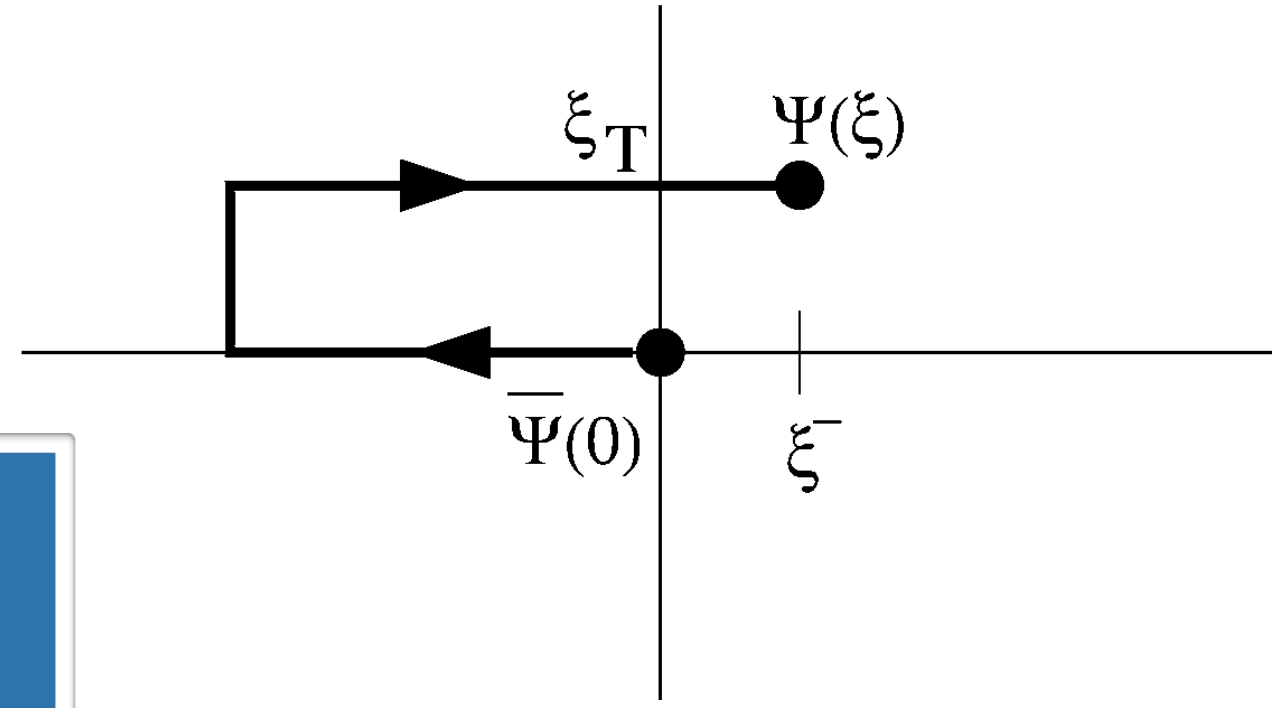
J. C. Collins, Phys. Lett. B 536 (2002) 43

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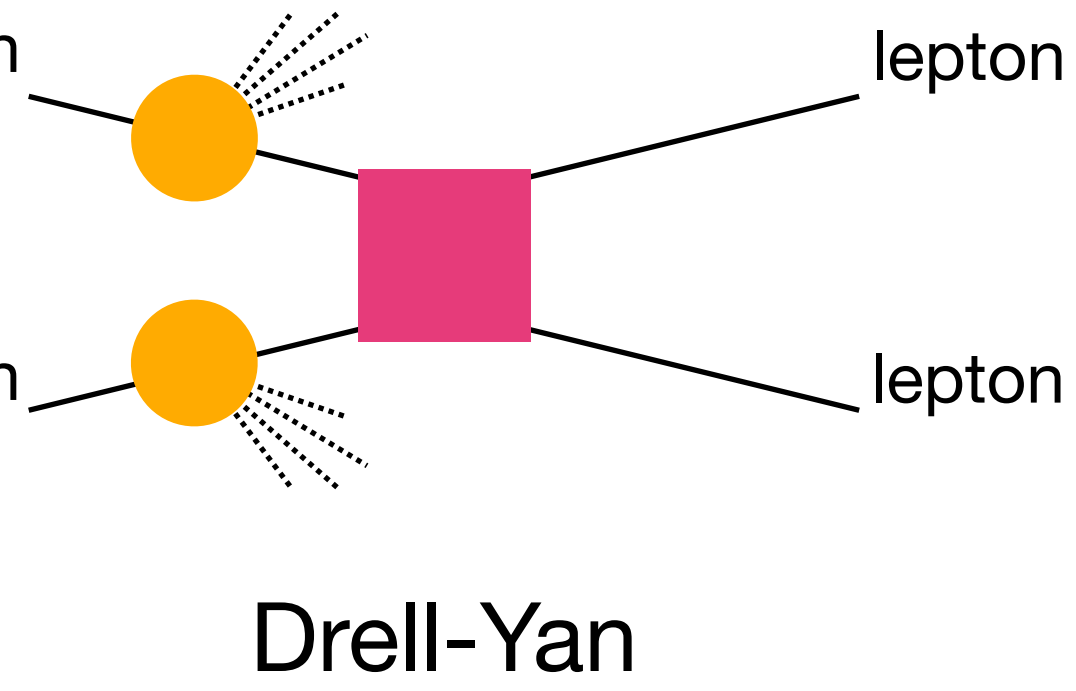
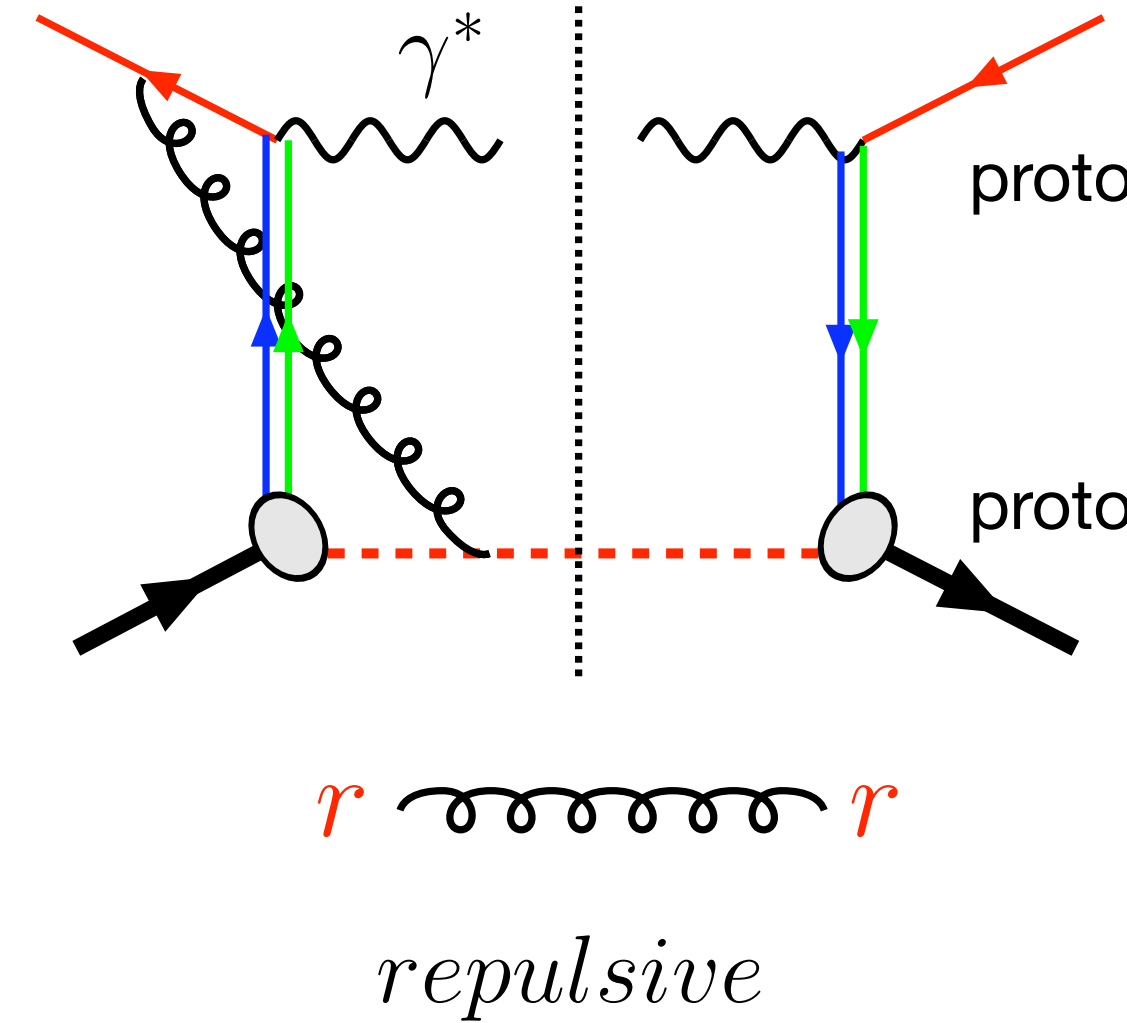
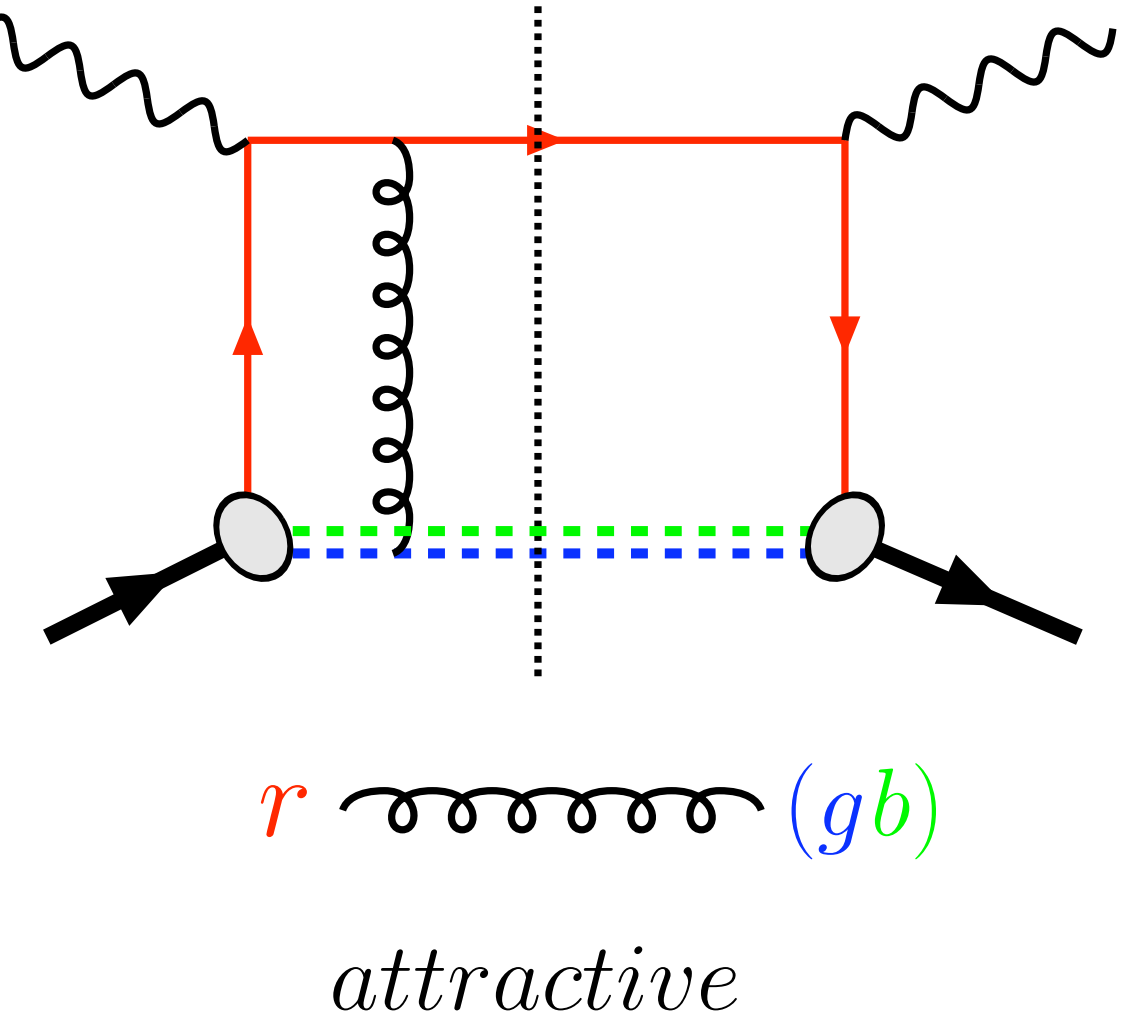
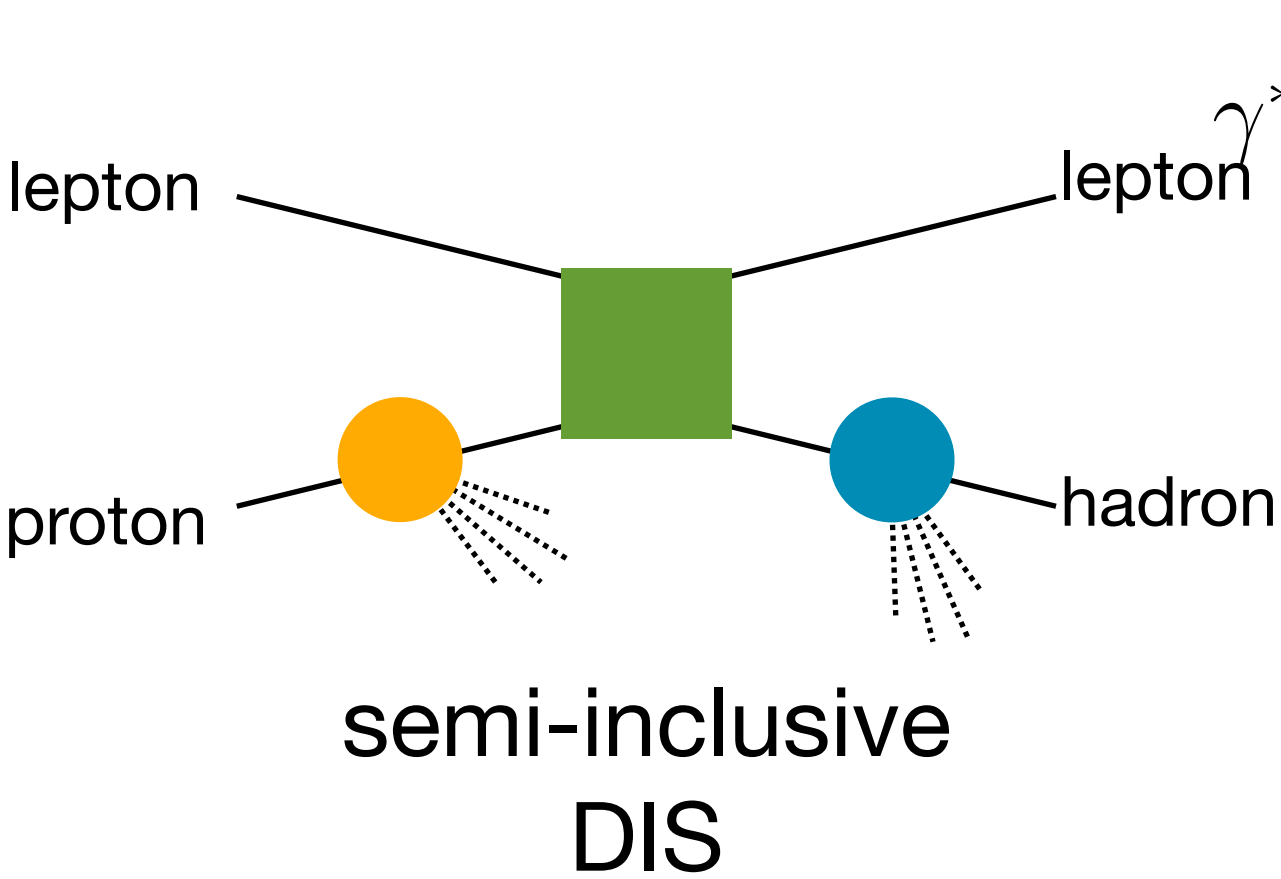
$W [0, \xi, \text{SIDIS}]$



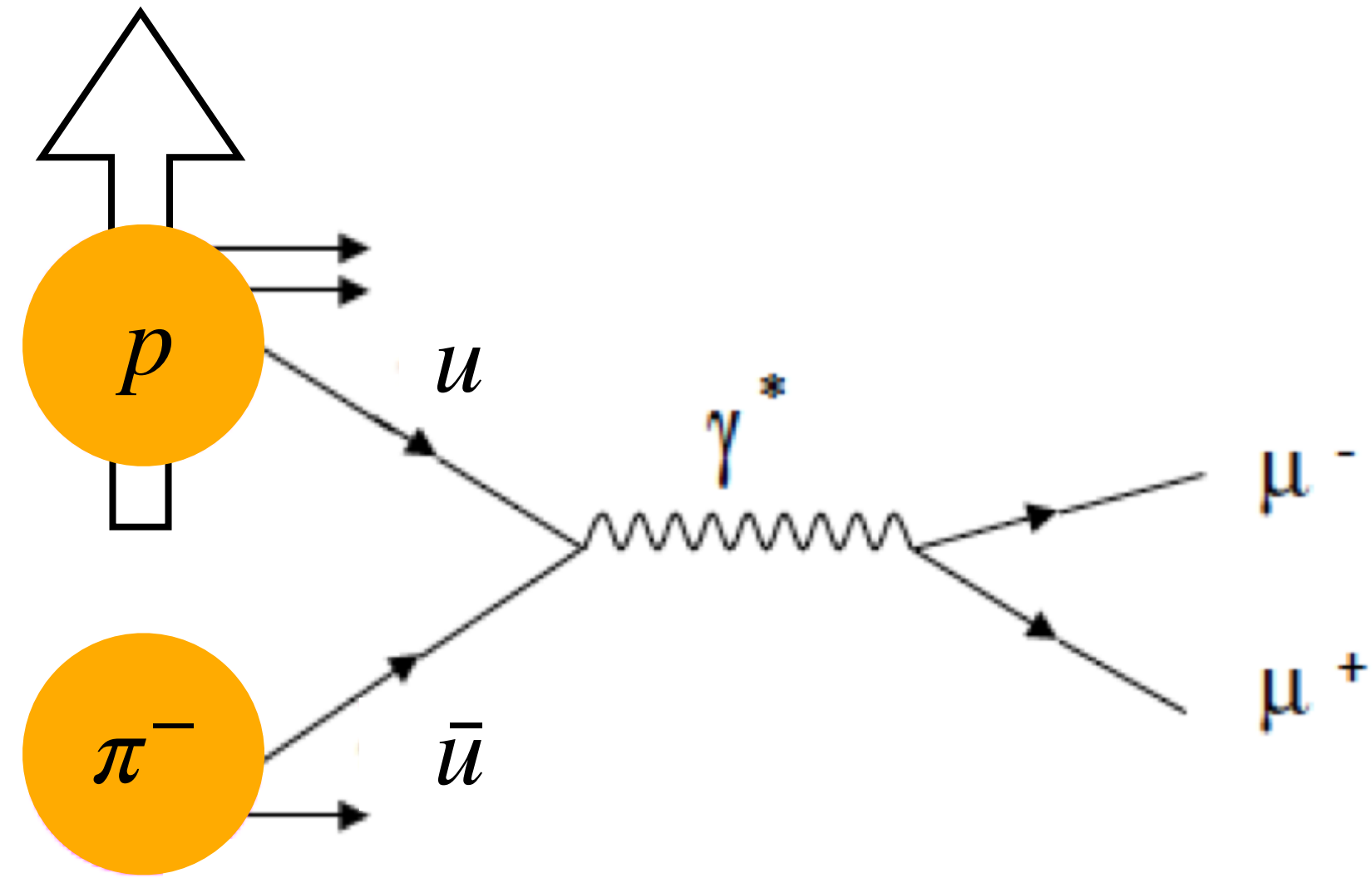
$U_{\xi, \text{DY}}$



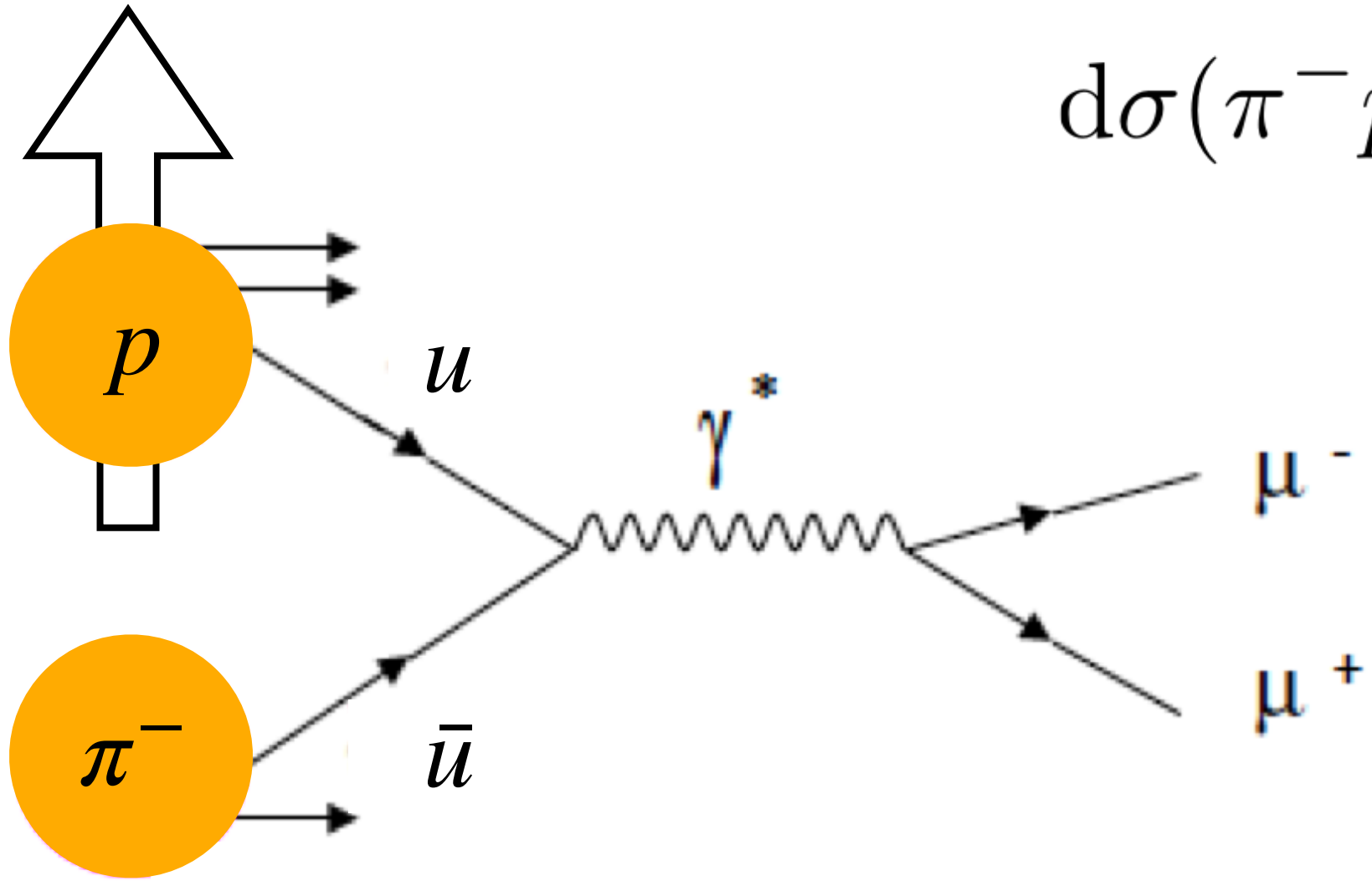
$$f_{1T}^\perp |_{\text{SIDIS}} = -f_{1T}^\perp |_{\text{DY}}$$



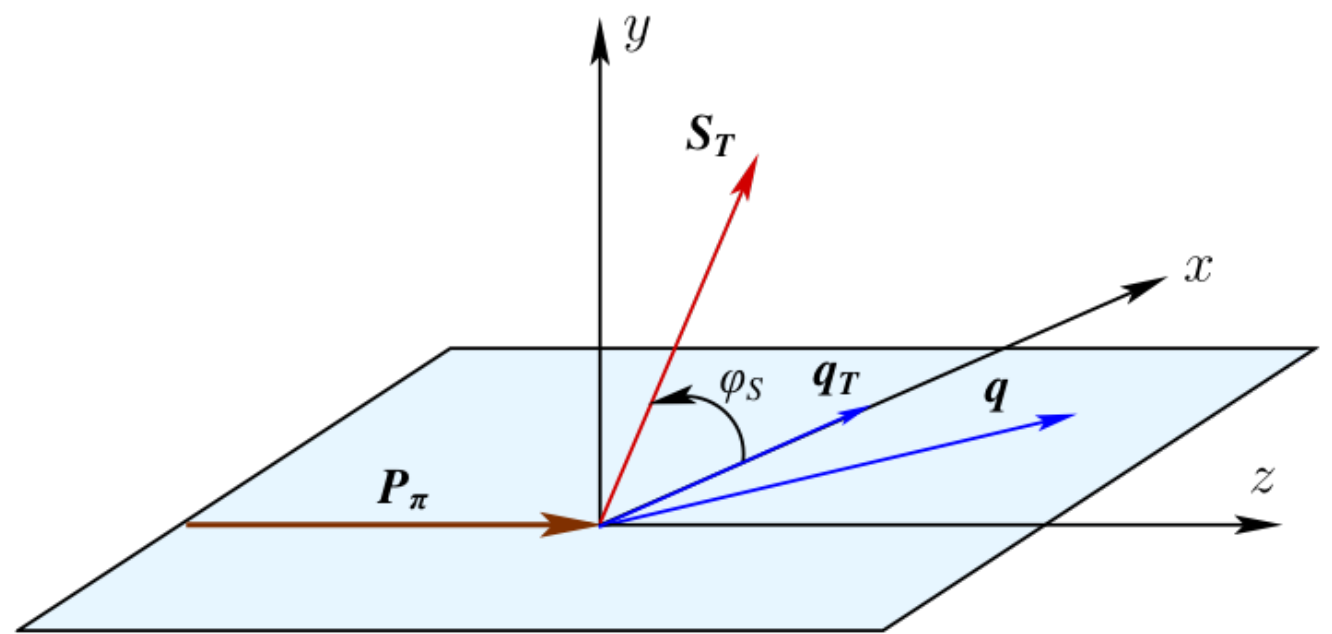
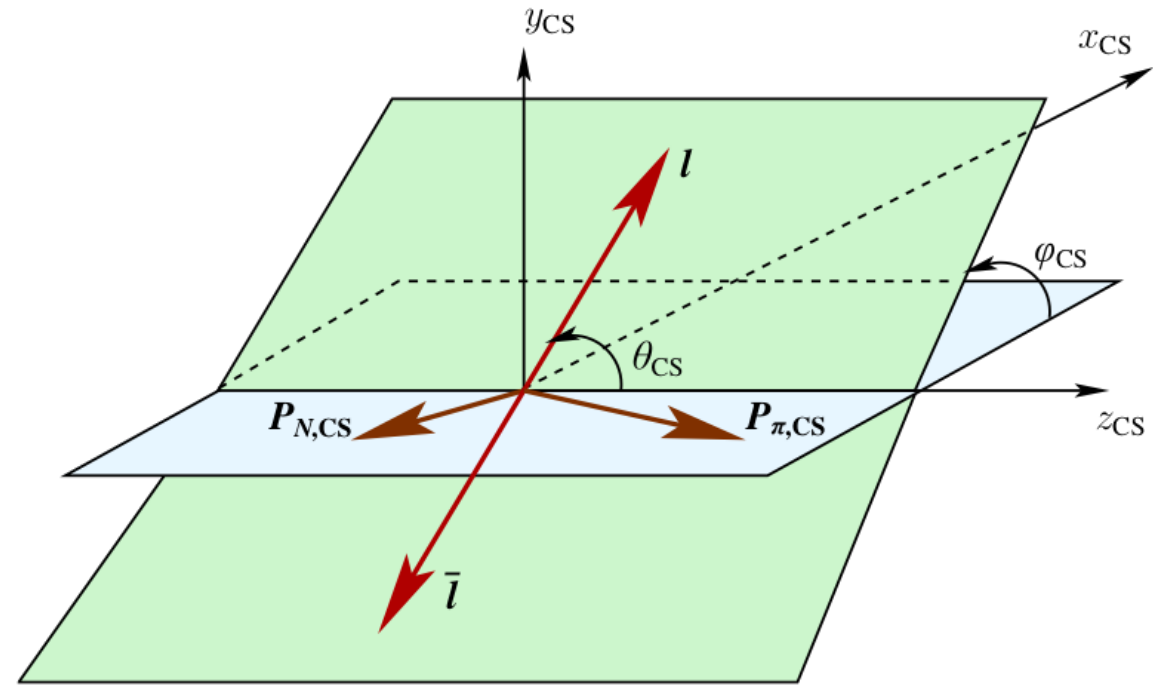
Experimental access to Sivers in Drell Yan



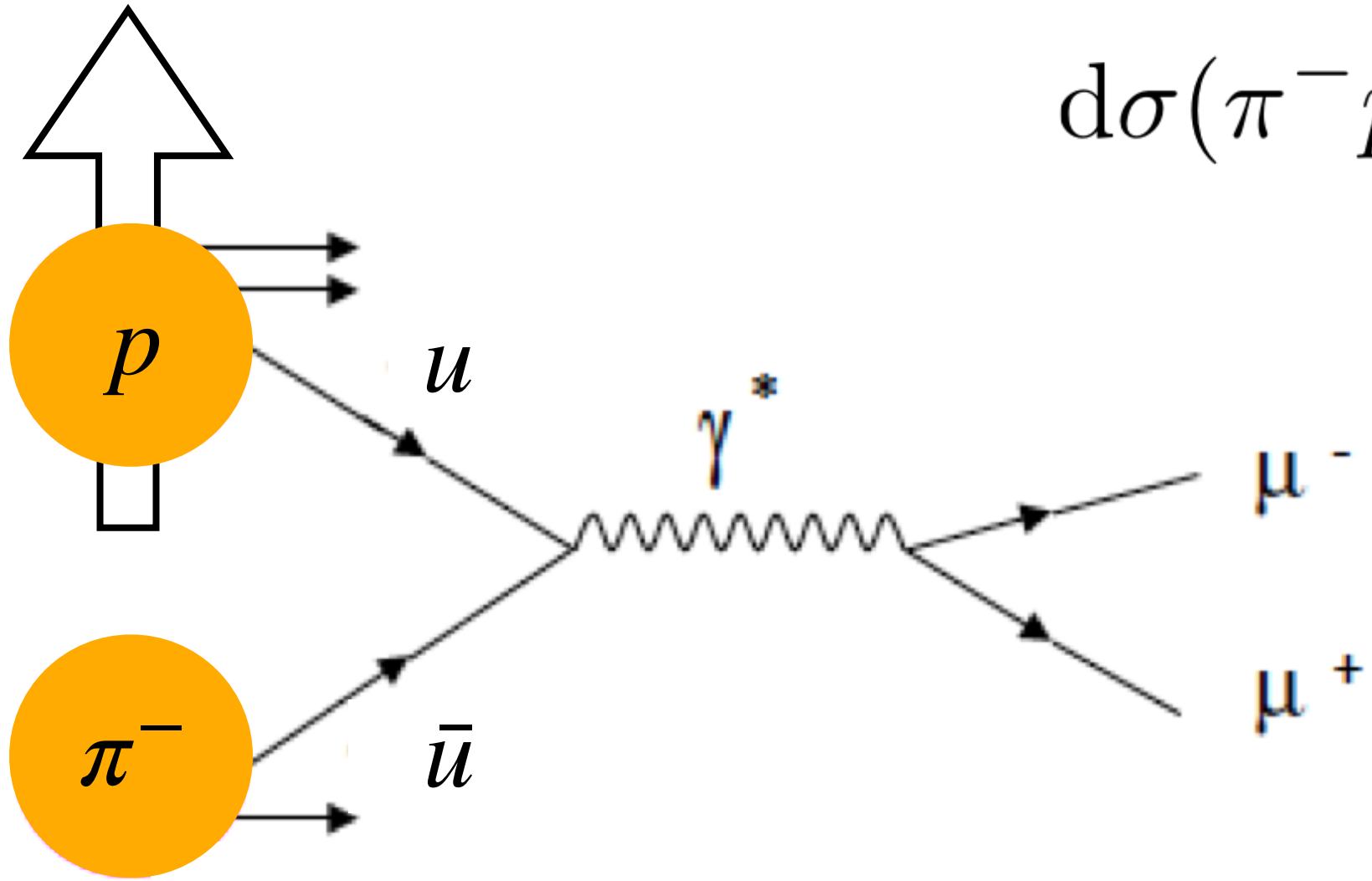
Experimental access to Sivers in Drell Yan



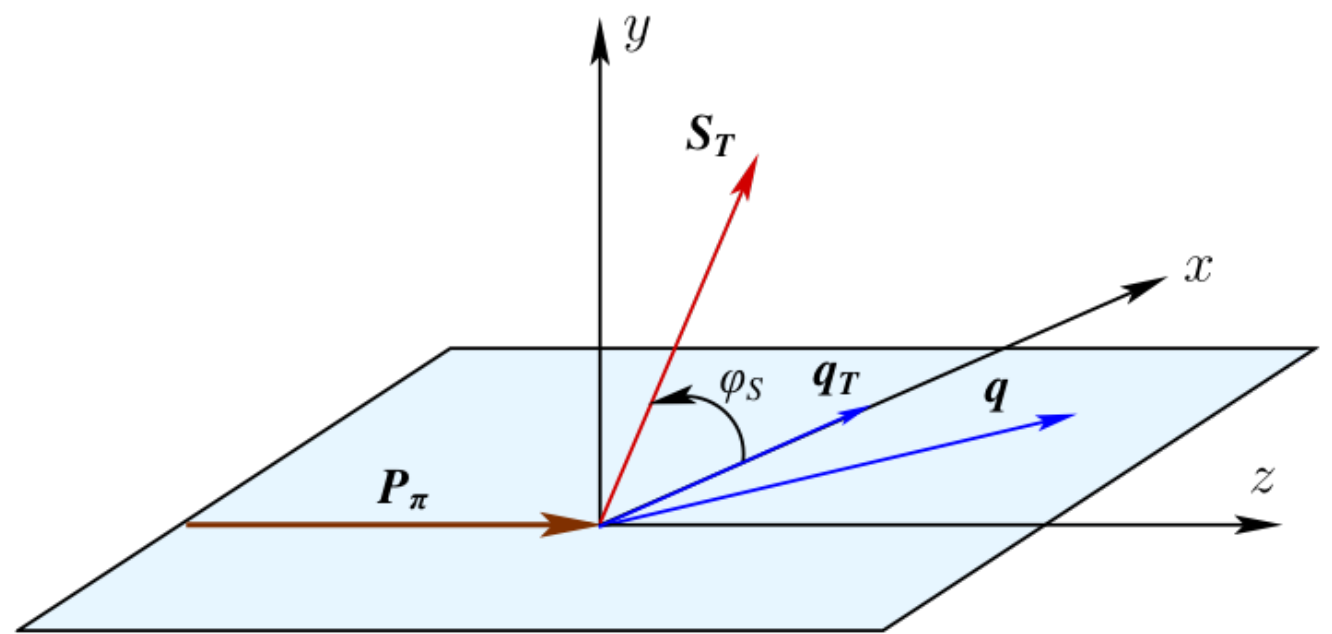
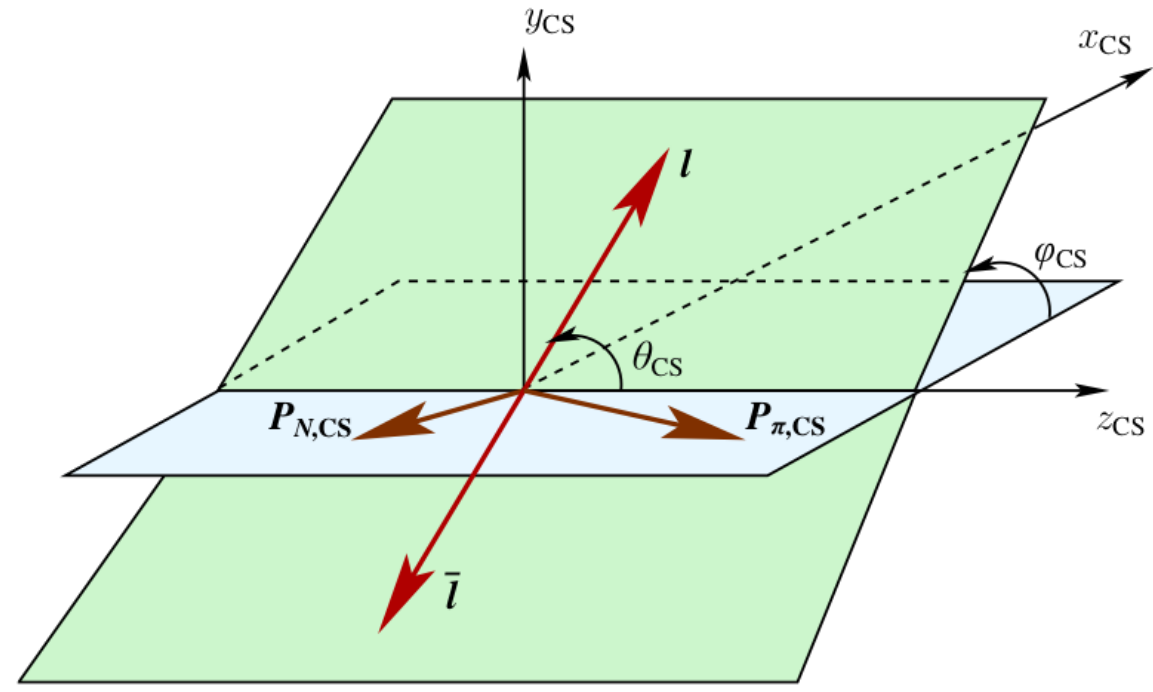
$$\begin{aligned}
 d\sigma(\pi^- p^\uparrow \rightarrow \mu^+ \mu^- X) \sim & 1 + \bar{h}_1^\perp \otimes h_1^\perp \cos(2\phi) \\
 & + |S_T| \bar{f}_1 \otimes f_{1T}^\perp \sin \phi_S \\
 & + |S_T| \bar{h}_1^\perp \otimes h_{1T}^\perp \sin(2\phi + \phi_S) \\
 & + |S_T| \bar{h}_1^\perp \otimes h_{1T} \sin(2\phi - \phi_S)
 \end{aligned}$$



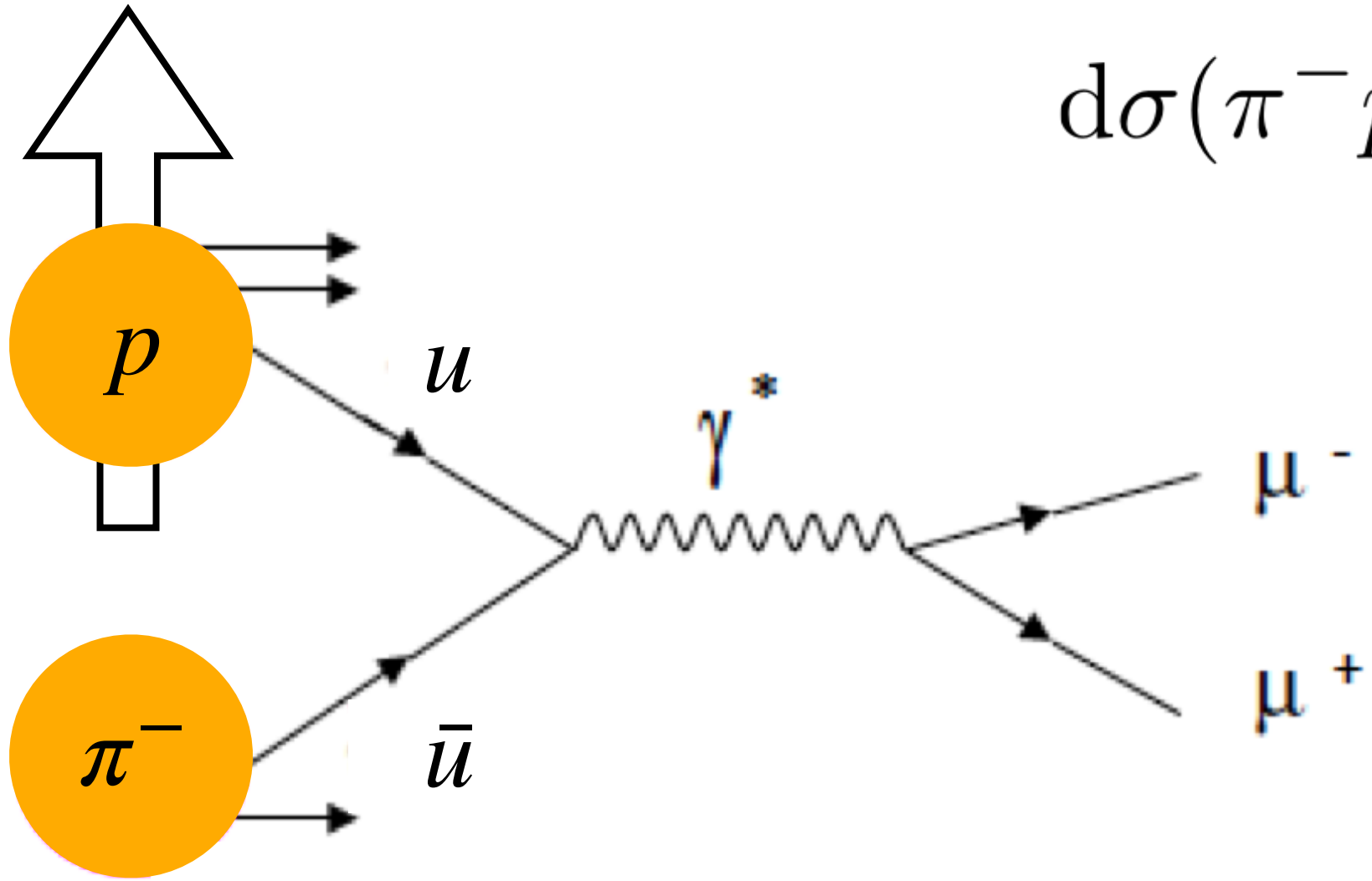
Experimental access to Sivers in Drell Yan



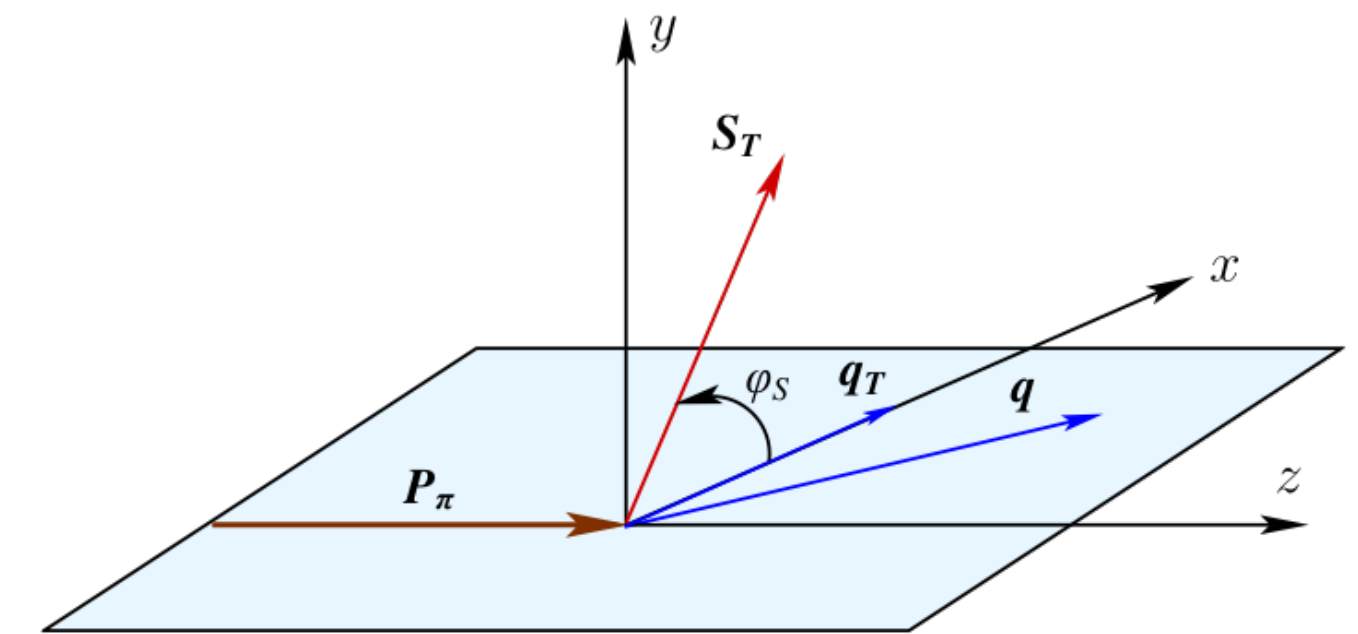
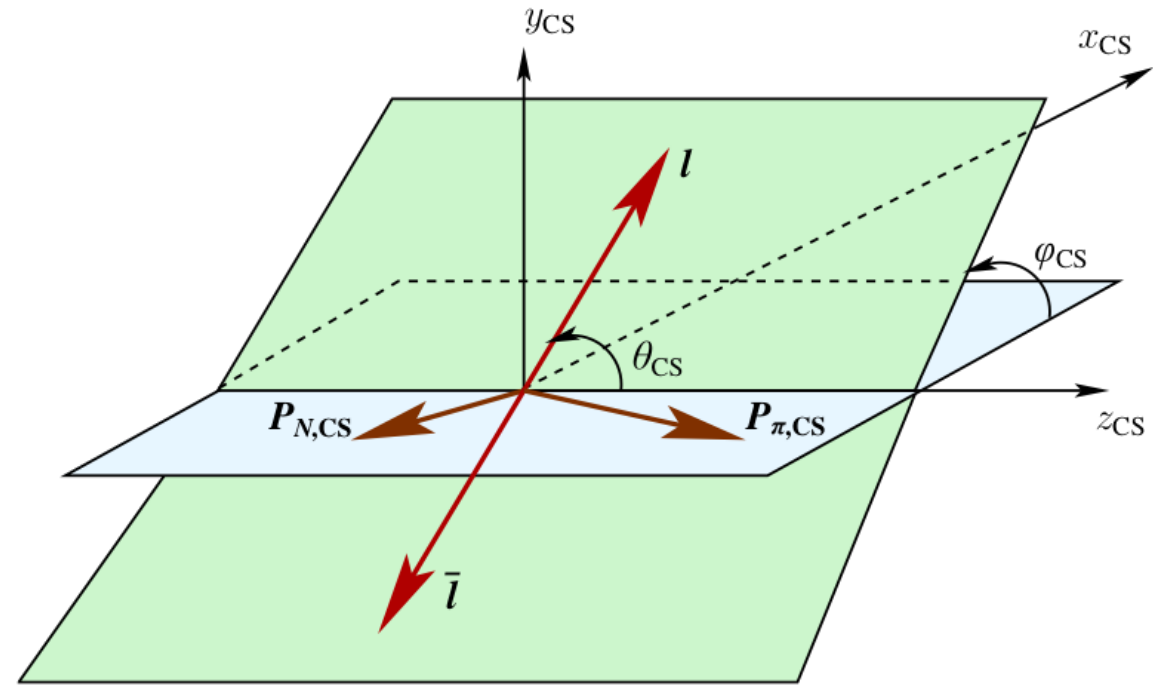
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 & + |S_T| \underbrace{\bar{h}_1^\perp}_{\pi^-} \otimes \underbrace{h_{1T}^\perp}_p \sin(2\phi - \phi_S)
 \end{aligned}$$



Experimental access to Sivers in Drell Yan



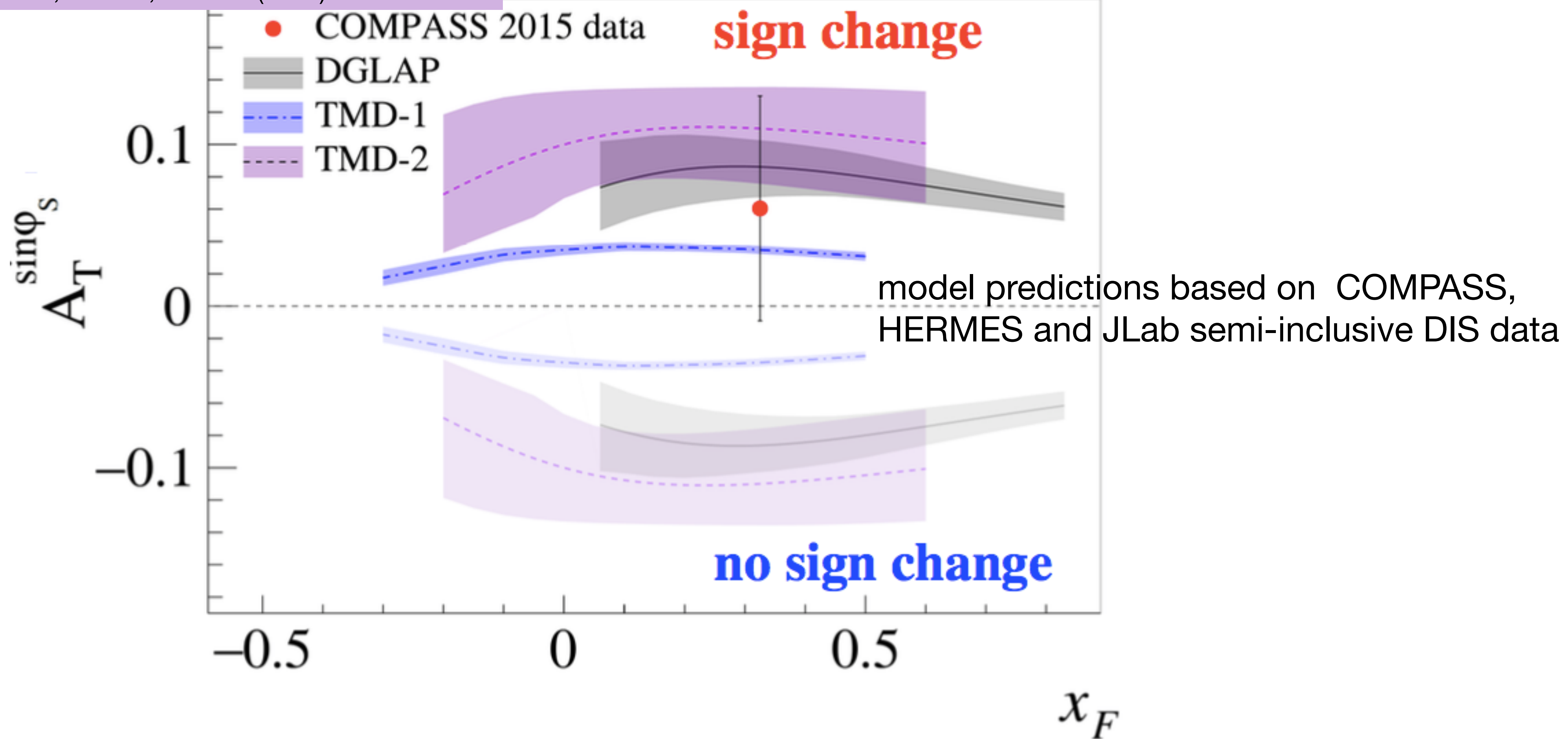
$$\begin{aligned}
 d\sigma(\pi^- p^\uparrow \rightarrow \mu^+ \mu^- X) \sim & 1 + \bar{h}_1^\perp \otimes h_1^\perp \cos(2\phi) \\
 & + |S_T| \bar{f}_1 \otimes \bar{f}_{1T} \sin \phi_S \\
 & + |S_T| \bar{h}_1^\perp \otimes h_{1T}^\perp \sin(2\phi + \phi_S) \\
 & + |S_T| \underbrace{\bar{h}_1^\perp}_{\pi^-} \otimes \underbrace{h_{1T}^\perp}_p \sin(2\phi - \phi_S)
 \end{aligned}$$



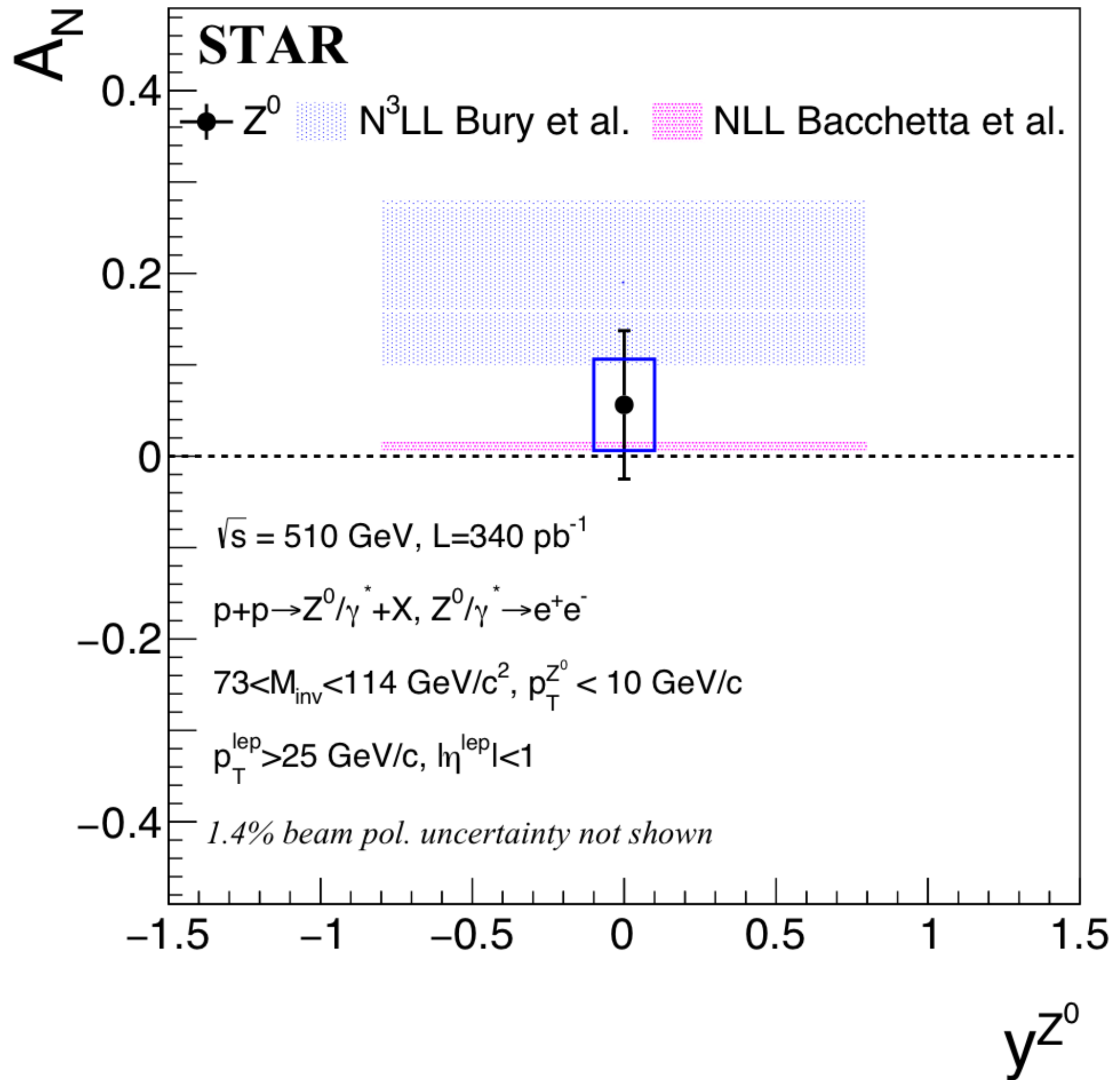
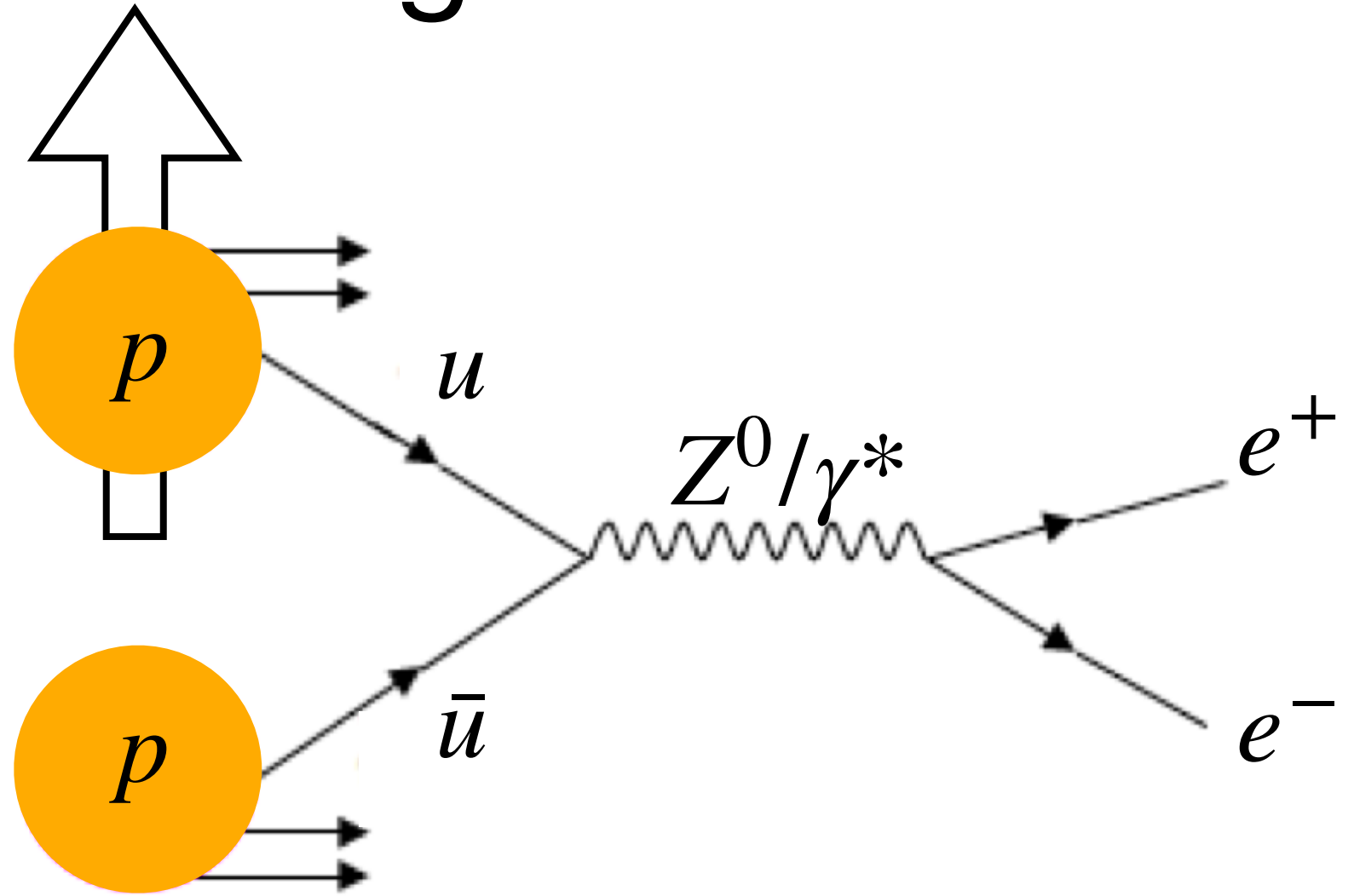
Investigation of the Sivers sign change in $p^\uparrow\pi$ collisions

M. Anselmino et al., JHEP **04** (2017) 046
M. G. Echevarria et al. PRD **89** (2014)074013
P. Sun, F. Yuan, PRD **88** (2013) 114012

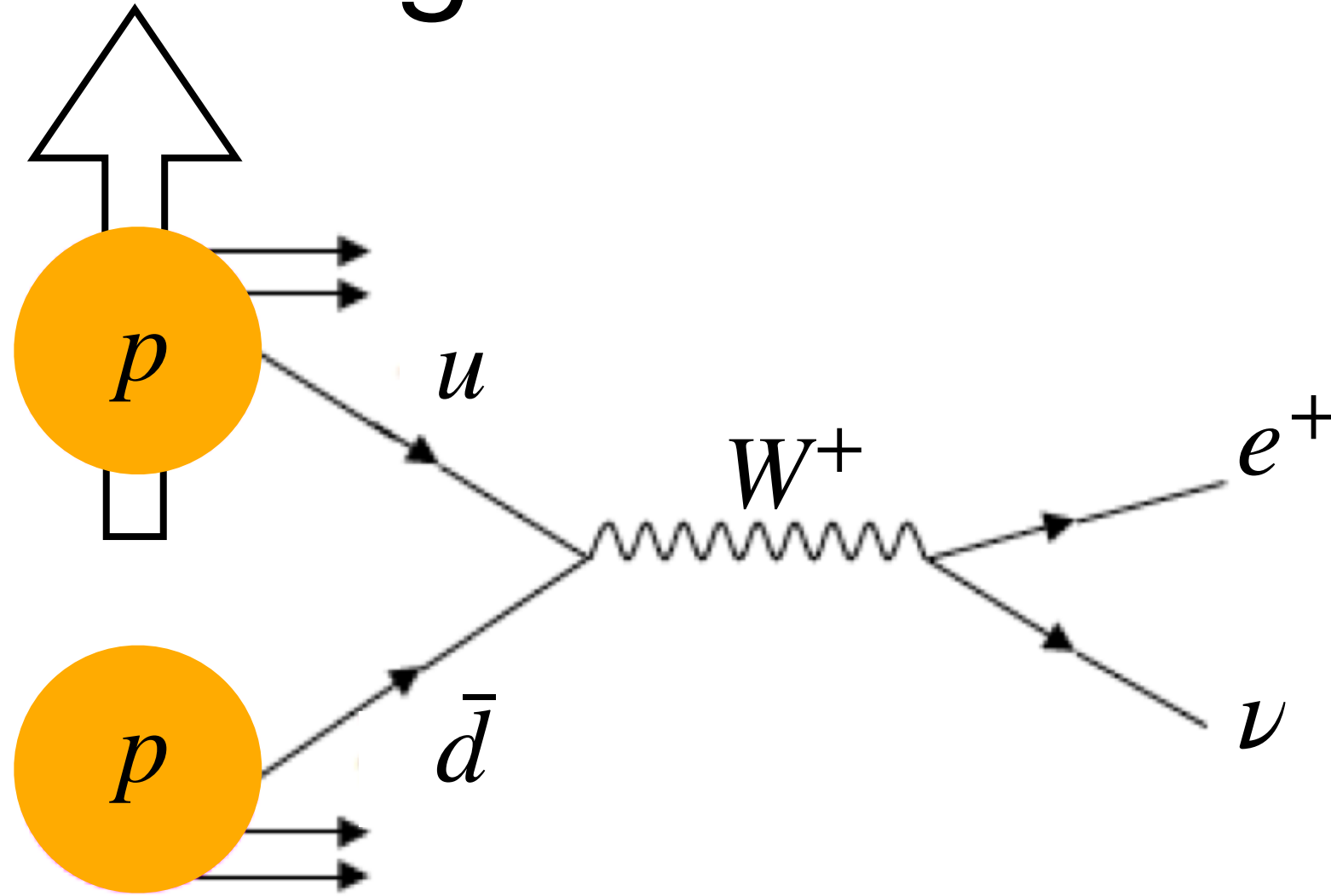
COMPASS, PRL **119** (2017) 112002



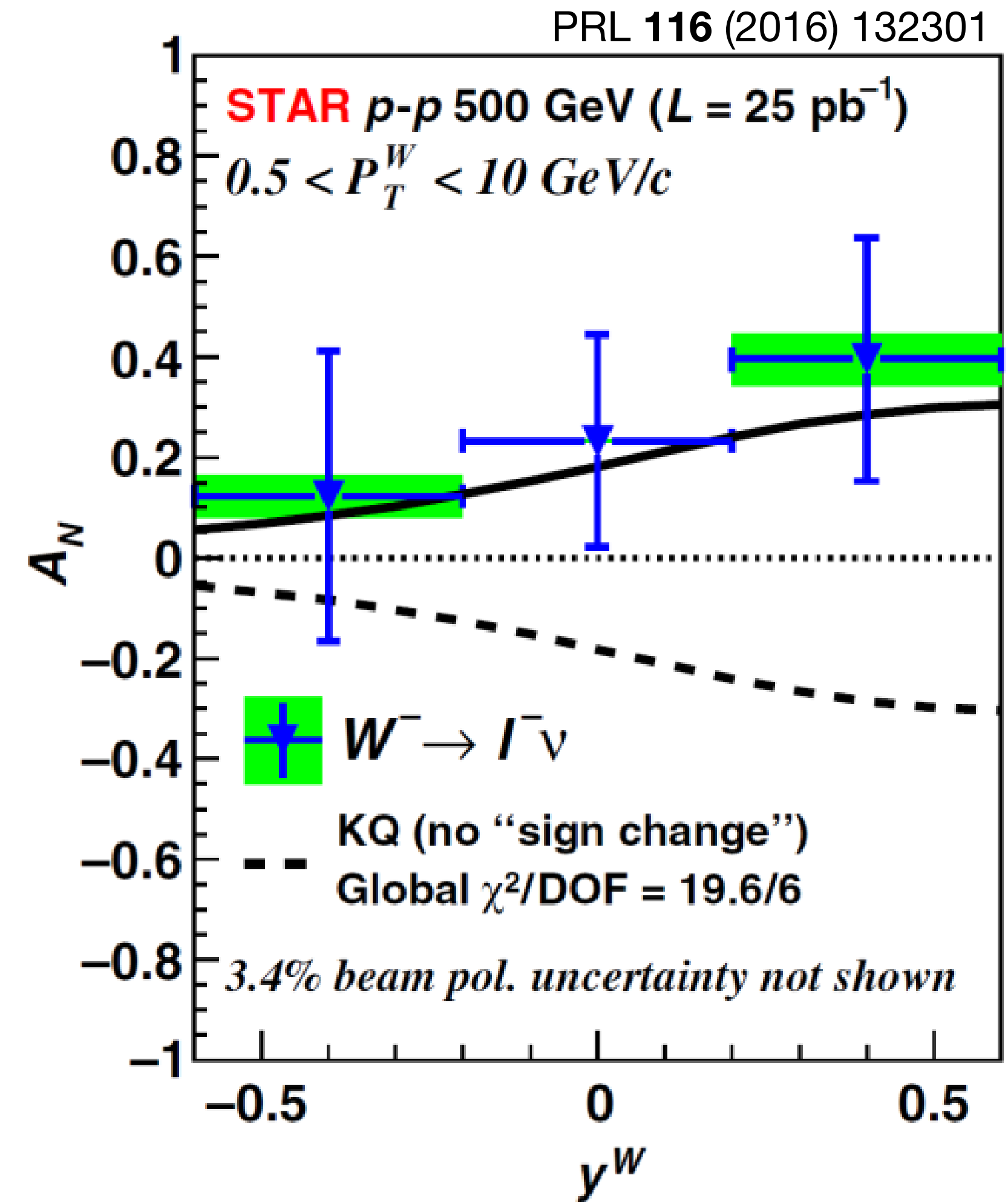
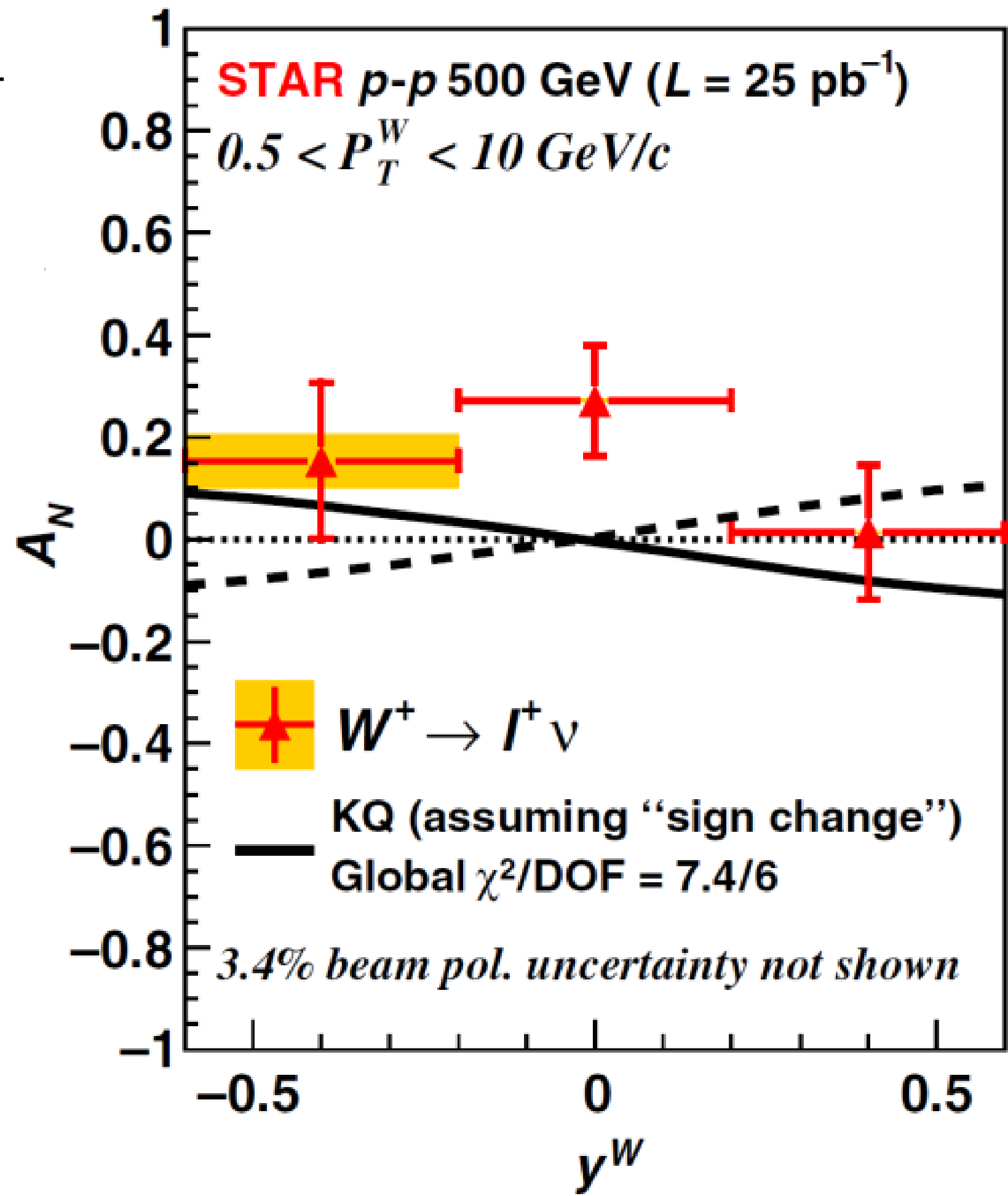
Investigation of the Sivers sign change in $p^\uparrow p$ collisions



Investigation of the Sivers sign change in $p^\uparrow p$ collisions

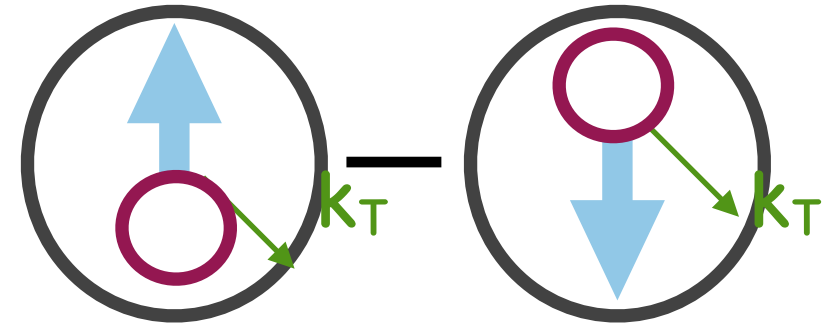


$$x_{1,2} = \frac{Q}{\sqrt{s}} e^{\pm y}$$



PRL 116 (2016) 132301

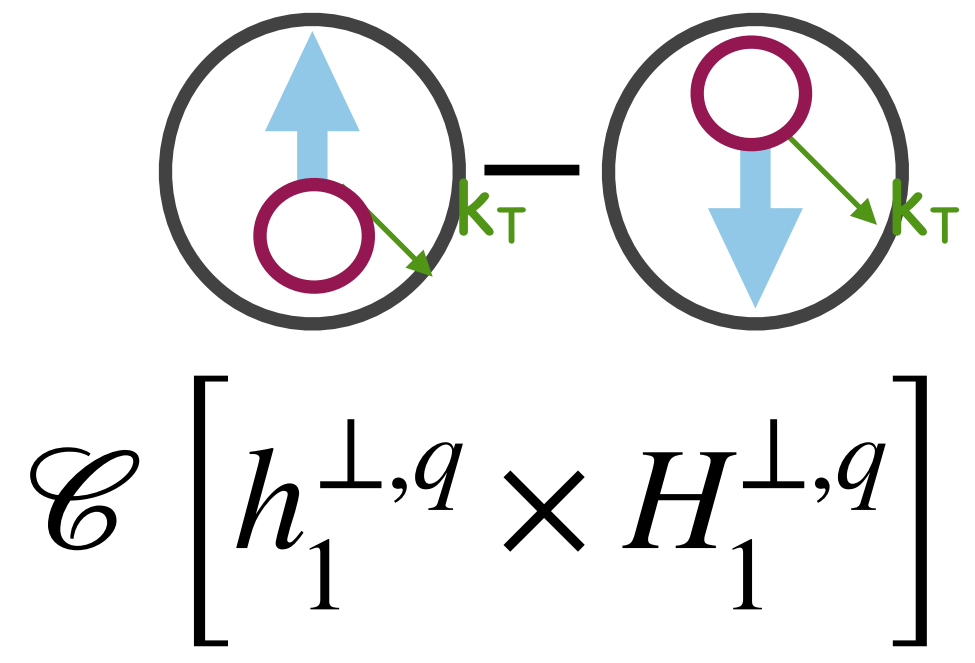
Boer-Mulders TMD PDF



Distribution of transversely polarised quarks in an unpolarised nucleon

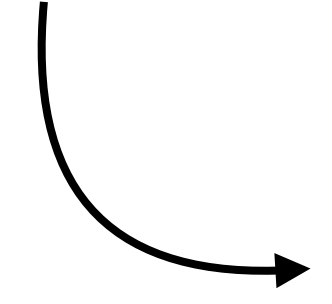
$$\mathcal{C} \left[h_1^{\perp,q} \times H_1^{\perp,q} \right]$$

Boer-Mulders TMD PDF



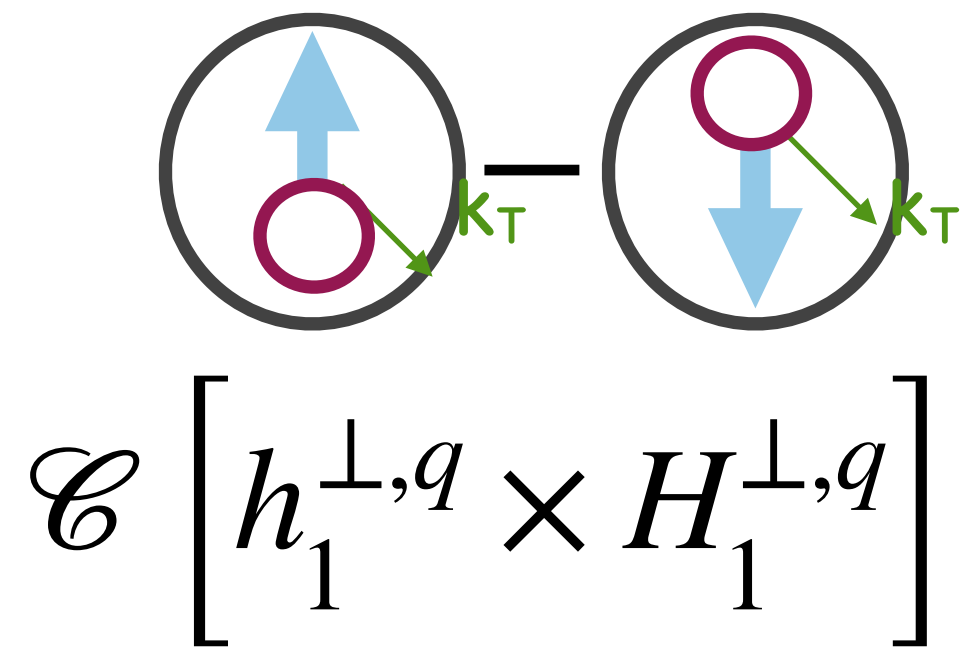
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Distribution of transversely polarised quarks in an unpolarised nucleon



spin physics with unpolarised hadrons!

Boer-Mulders TMD PDF



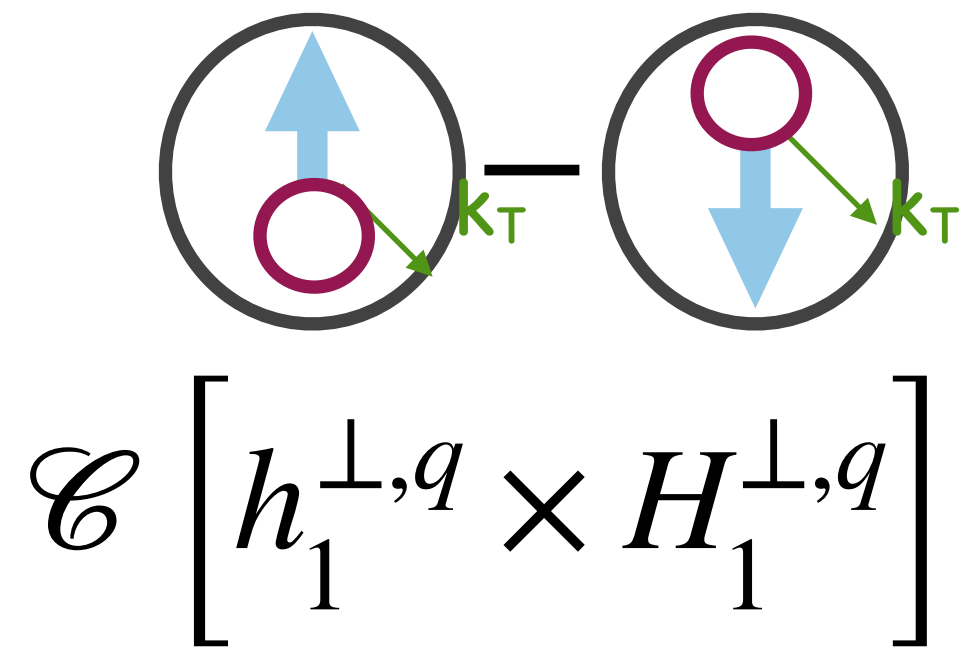
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Distribution of transversely polarised quarks in an unpolarised nucleon

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access at unpolarised facilities, such as the LHC!

Boer-Mulders TMD PDF

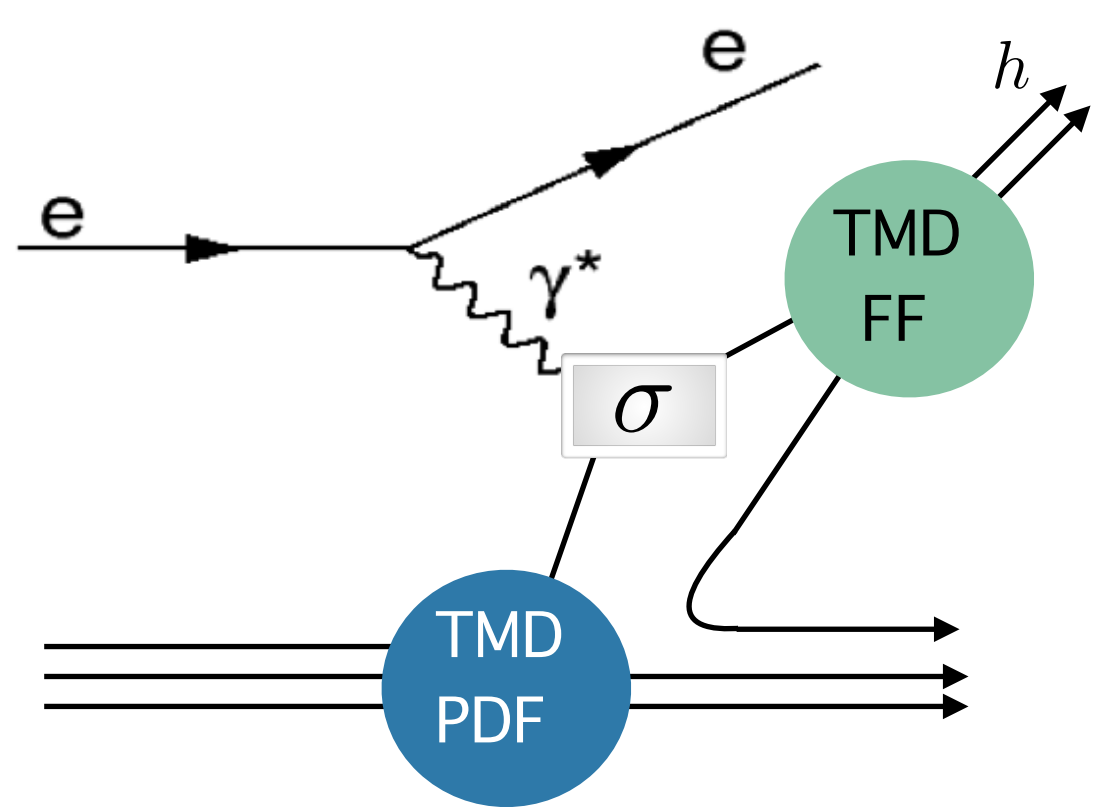


Distribution of transversely polarised quarks in an unpolarised nucleon

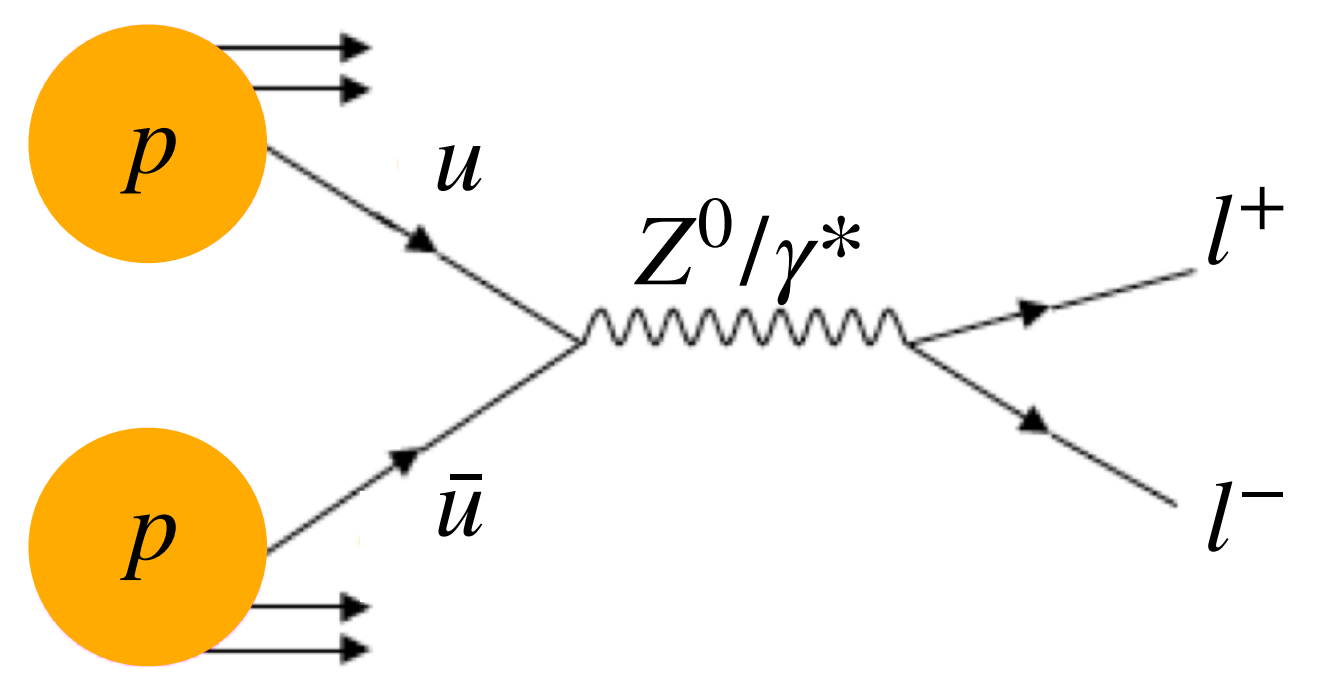
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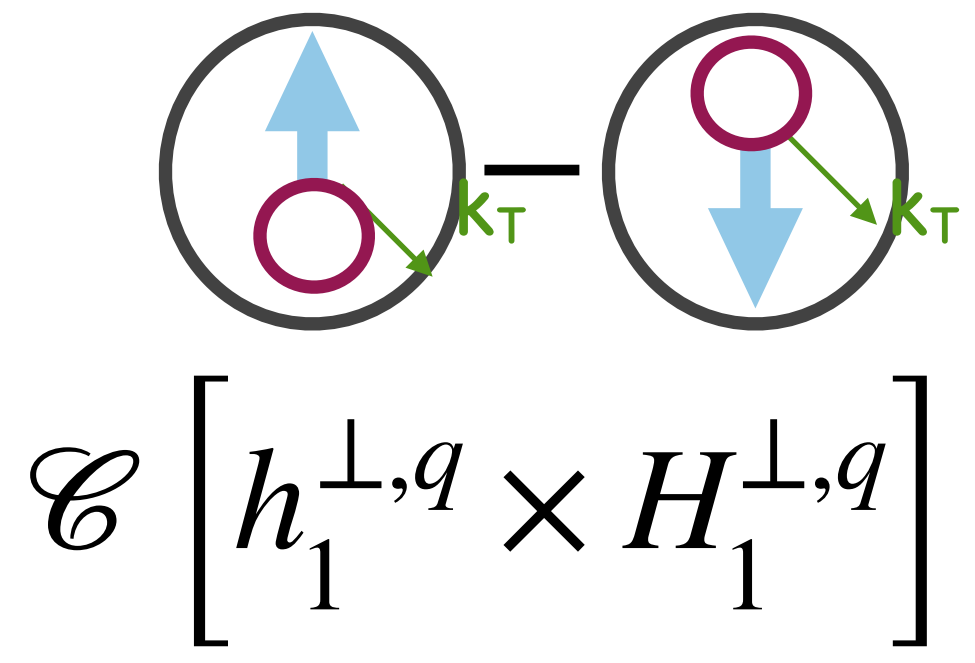


ep collisions: semi-inclusive DIS



hh collisions: Drell-Yan

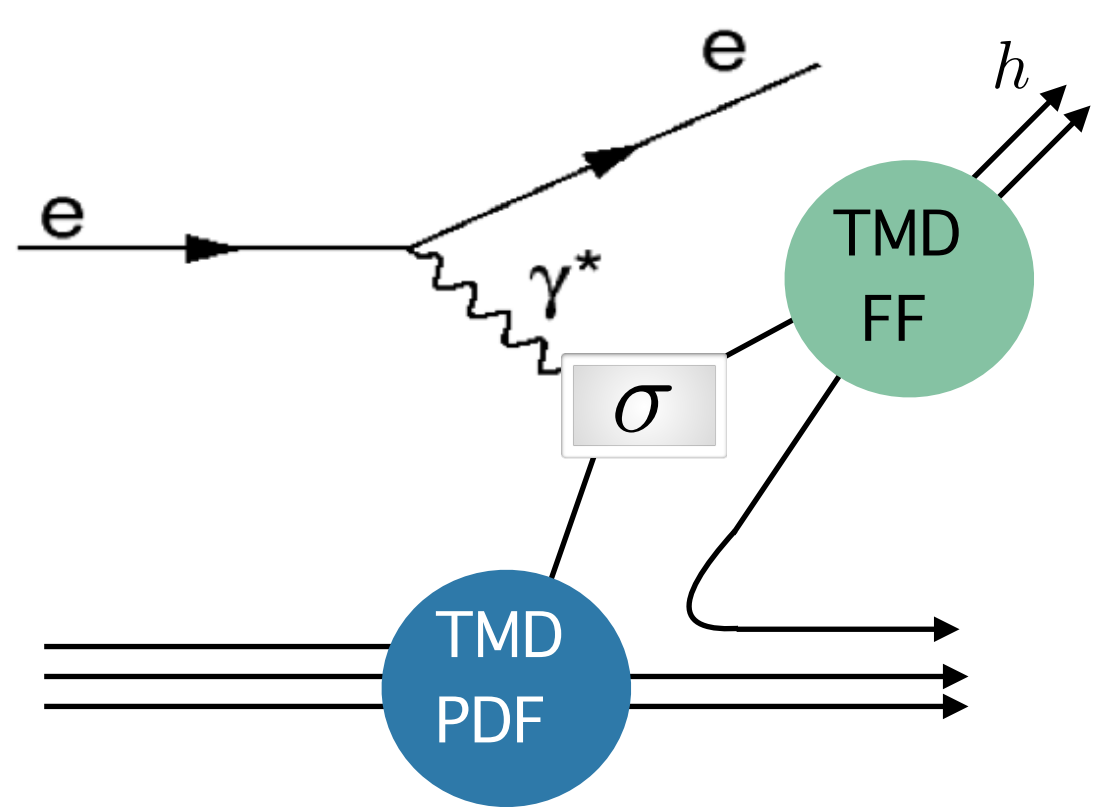
Boer-Mulders TMD PDF



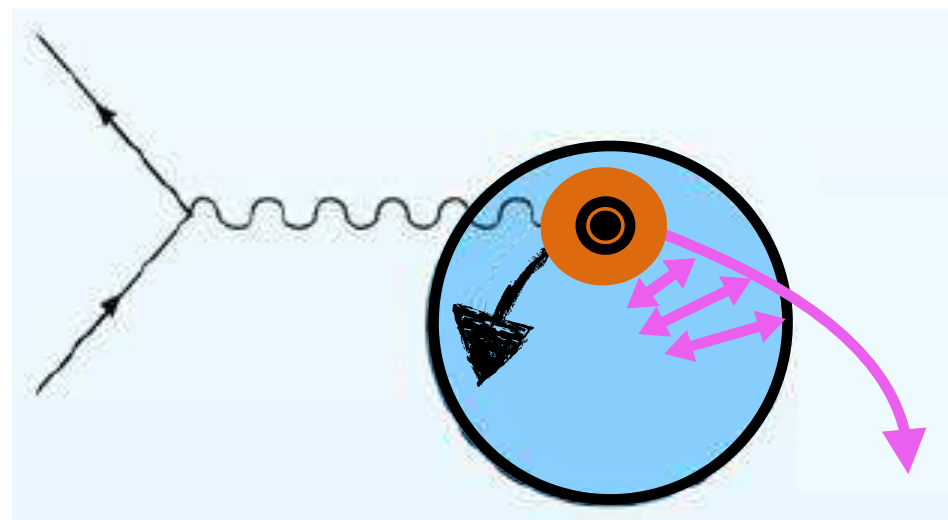
Distribution of transversely polarised quarks in an unpolarised nucleon

spin physics with unpolarised hadrons!

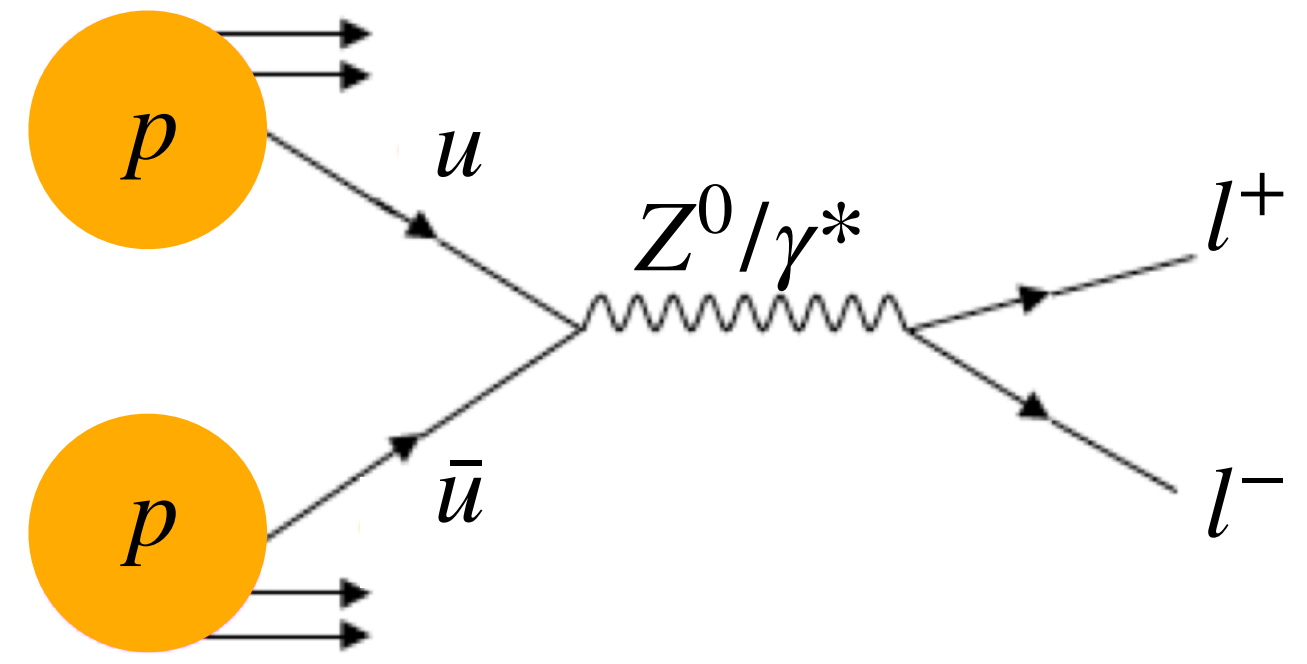
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ep collisions: semi-inclusive DIS

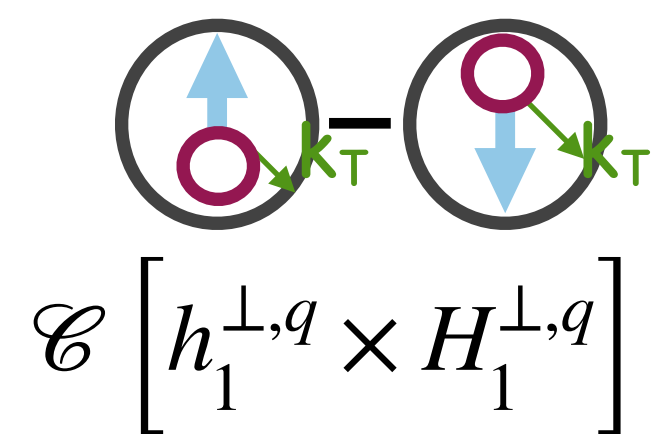


FSA vs. ISA \rightarrow sign change

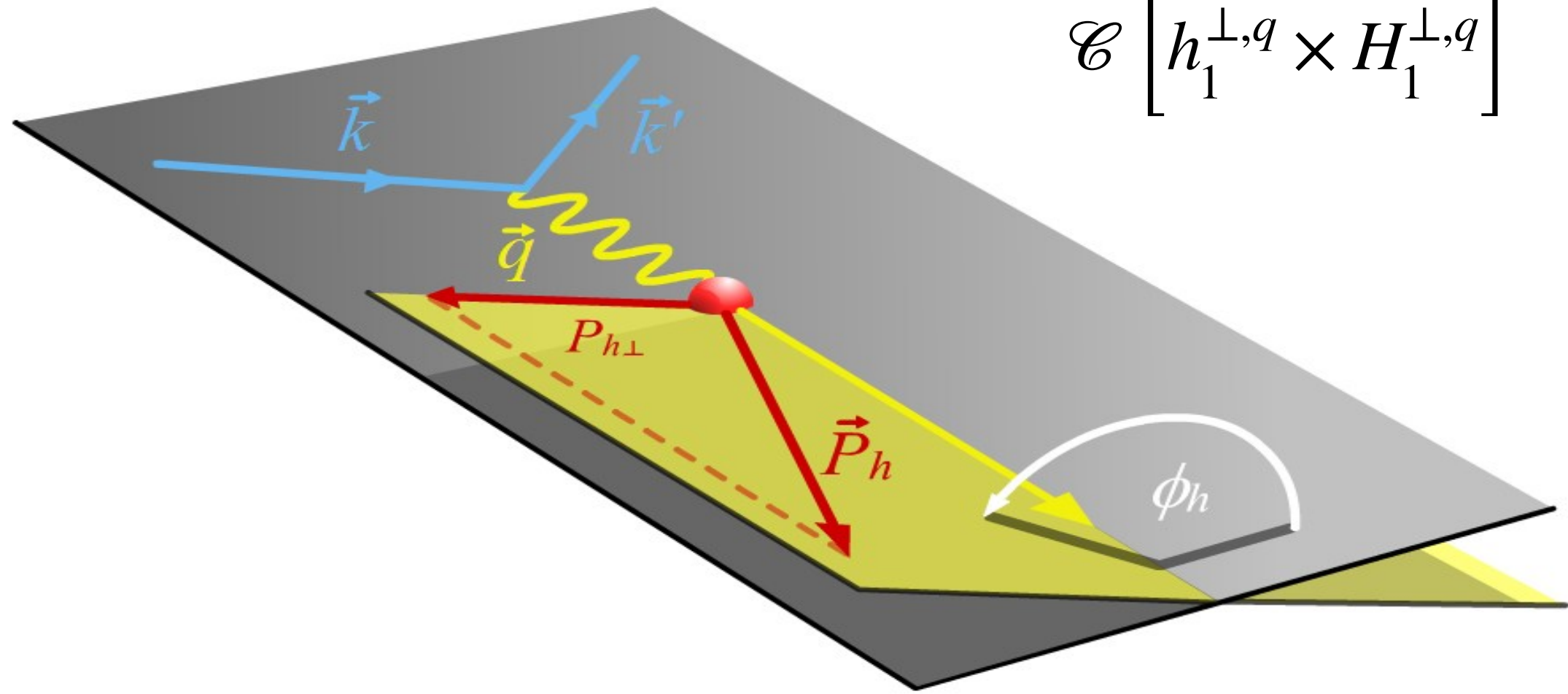


hh collisions: Drell-Yan

Boer-Mulders TMD PDF in semi-inclusive DIS

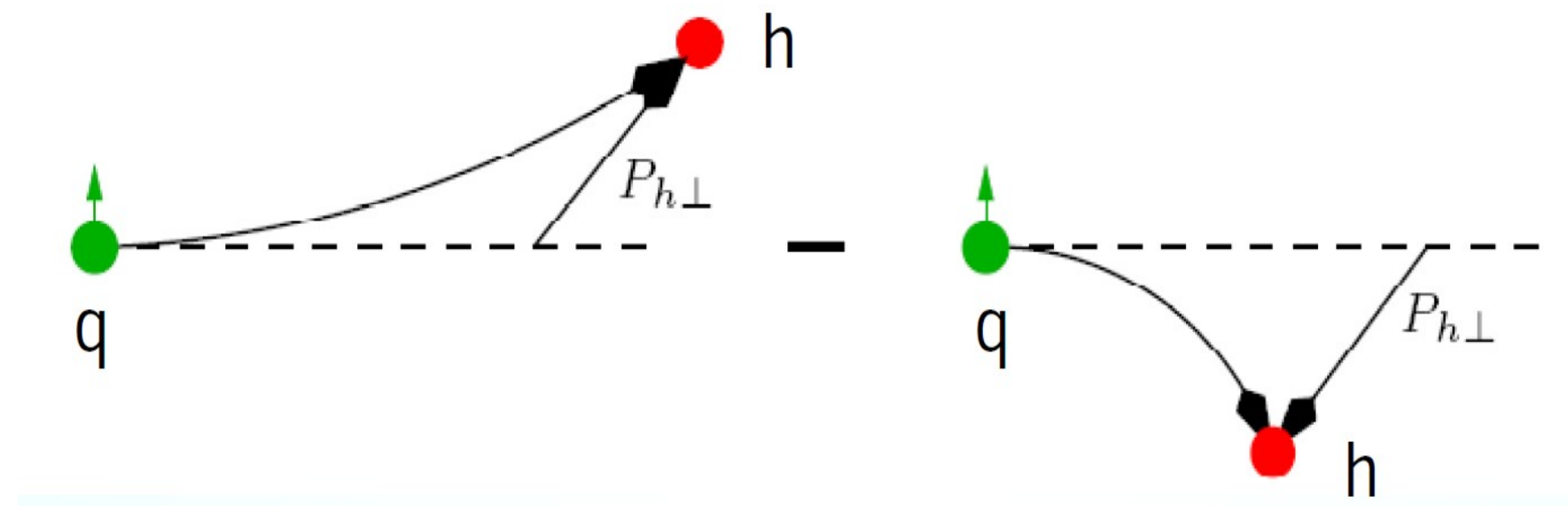


$$\sigma \sim \cos(2\phi_h) \sum_q e_q^2 C \left[h_1^q(x, k_{\perp}) \times H_1^{\perp,q}(z, p_{\perp}) \right]$$

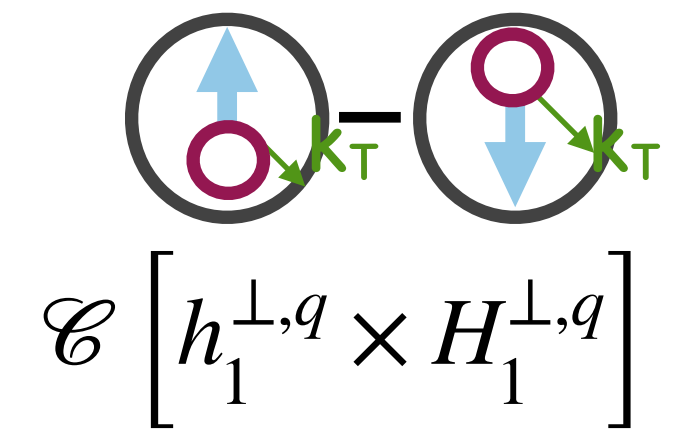


$h_1^q(x, k_{\perp})$: Boer Mulders

$H_1^{\perp,q}(z, p_{\perp})$: Collins fragmentation function



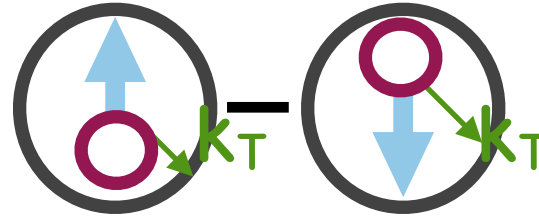
Boer-Mulders modulation: experimental access



Measurement in ep: $\langle \cos(2\phi_h) \rangle_{Born}(j)$ $\langle \cos(2\phi_h) \rangle_{meas}(i)$



Boer-Mulders modulation: experimental access

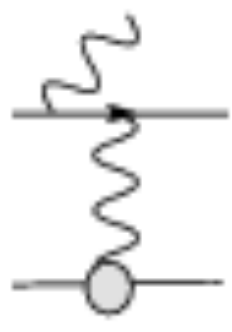


$$\mathcal{E} \left[h_1^{\perp,q} \times H_1^{\perp,q} \right]$$

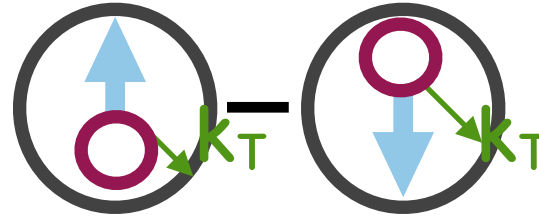
Measurement in ep: $\langle \cos(2\phi_h) \rangle_{Born}(j)$ $\langle \cos(2\phi_h) \rangle_{meas}(i)$



- QED radiate effects



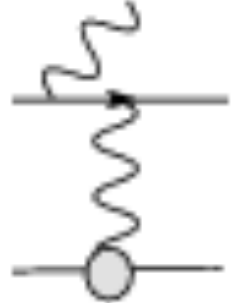
Boer-Mulders modulation: experimental access



$$\mathcal{C} \left[h_1^{\perp,q} \times H_1^{\perp,q} \right]$$

Measurement in ep: $\langle \cos(2\phi_h) \rangle_{Born}(j)$ $\langle \cos(2\phi_h) \rangle_{meas}(i)$



- QED radiate effects 
- limited geometric and kinematic acceptance of detector

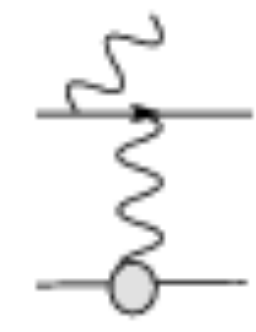
Boer-Mulders modulation: experimental access

$$\mathcal{C} \left[h_1^{\perp,q} \times H_1^{\perp,q} \right]$$

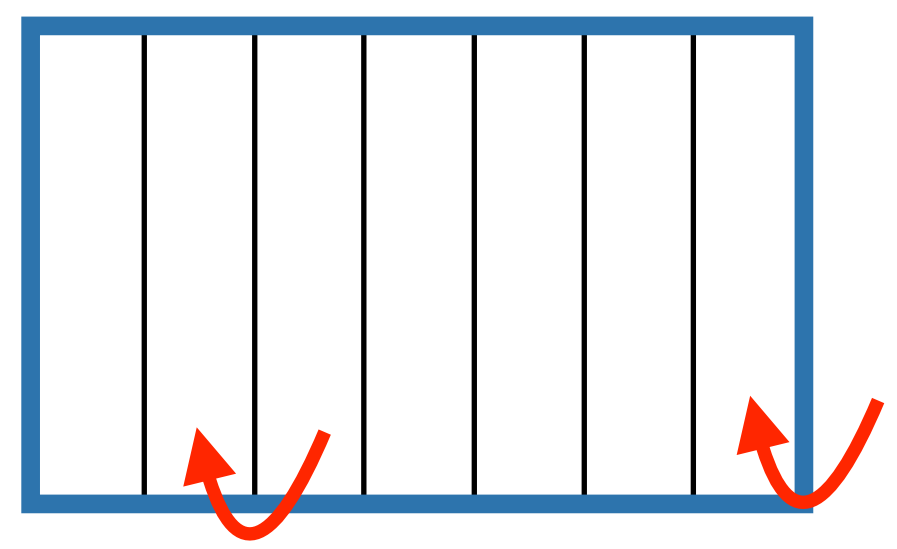
Measurement in ep: $\langle \cos(2\phi_h) \rangle_{Born}(j)$ $\langle \cos(2\phi_h) \rangle_{meas}(i)$



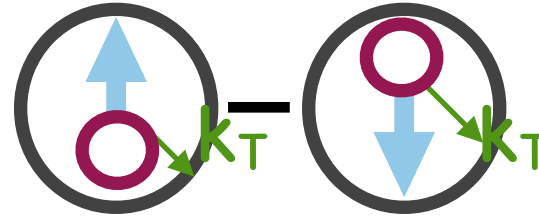
- QED radiate effects



- limited geometric and kinematic acceptance of detector
- limited detector resolution



Boer-Mulders modulation: experimental access

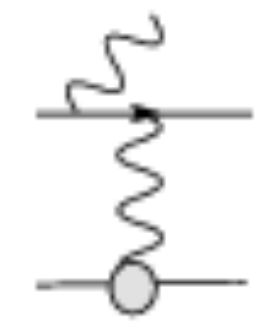


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Measurement in ep: $\langle \cos(2\phi_h) \rangle_{Born}(j)$ $\langle \cos(2\phi_h) \rangle_{meas}(i)$

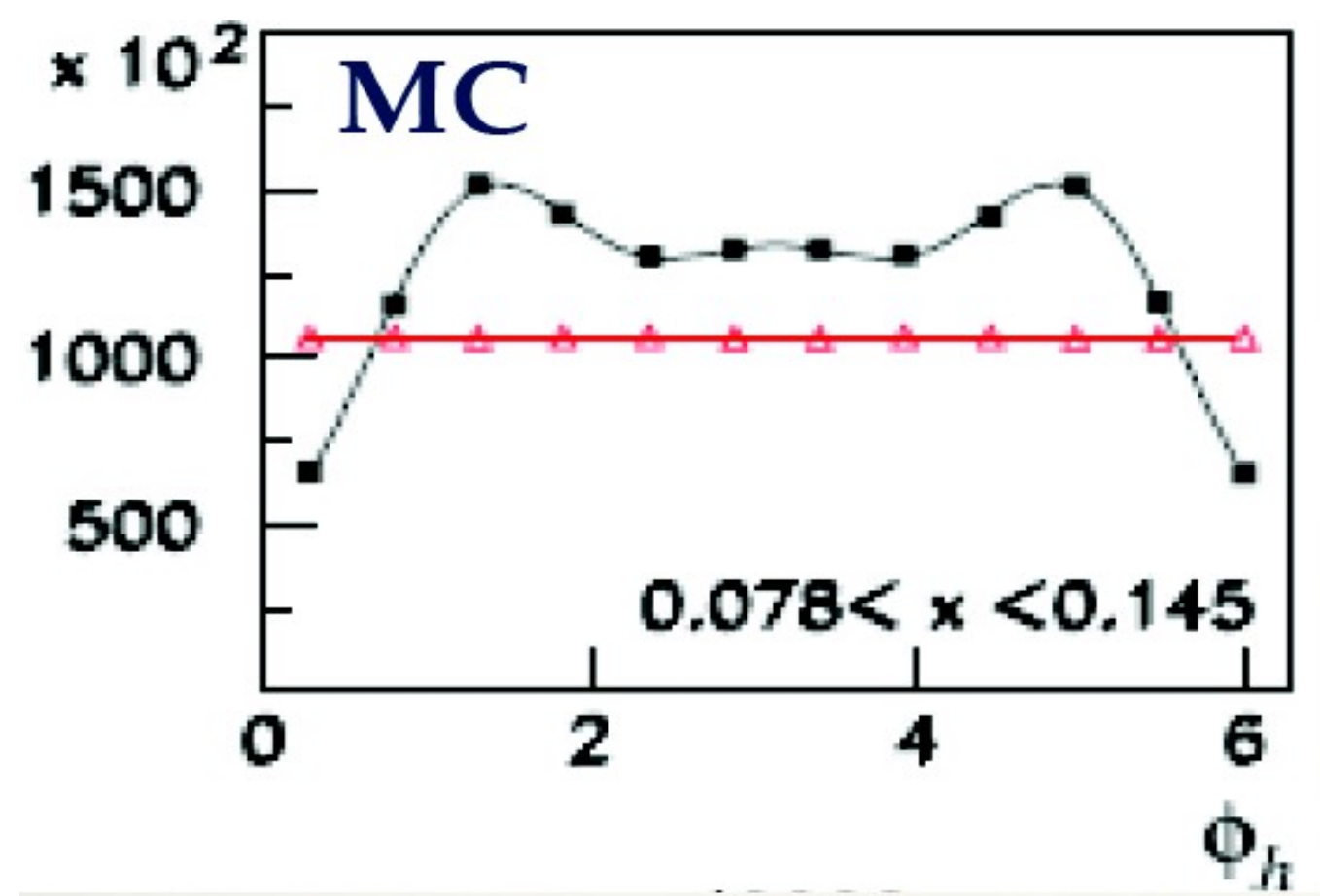
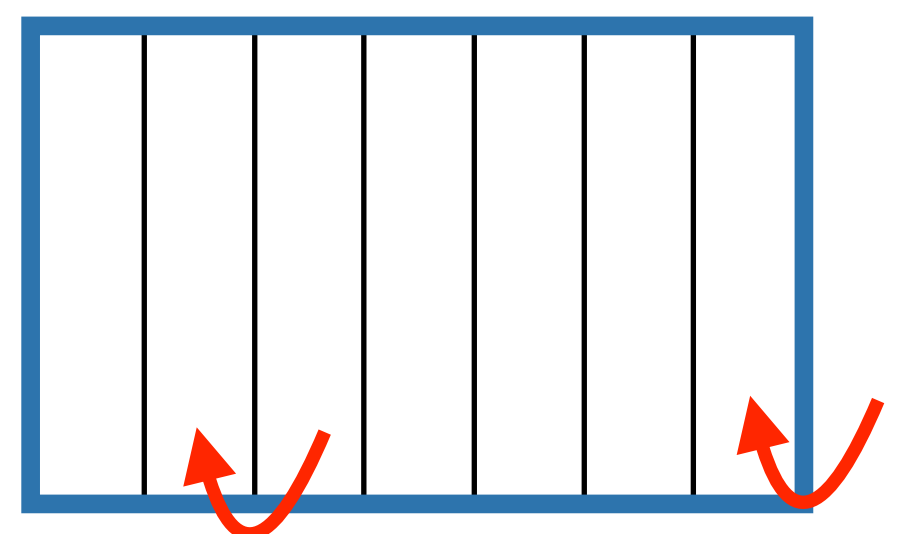




- QED radiate effects



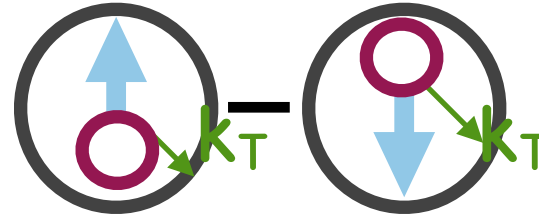
- limited geometric and kinematic acceptance of detector

- limited detector resolution



 generated in 4π
 inside acceptance

Boer-Mulders modulation: experimental access



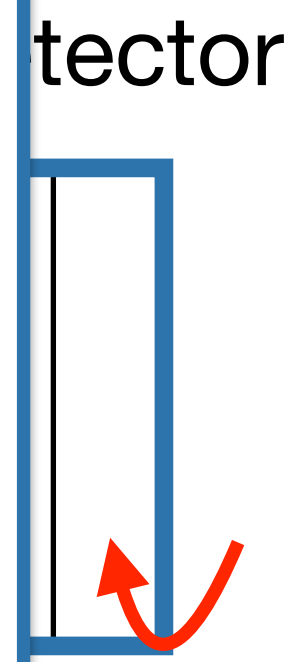
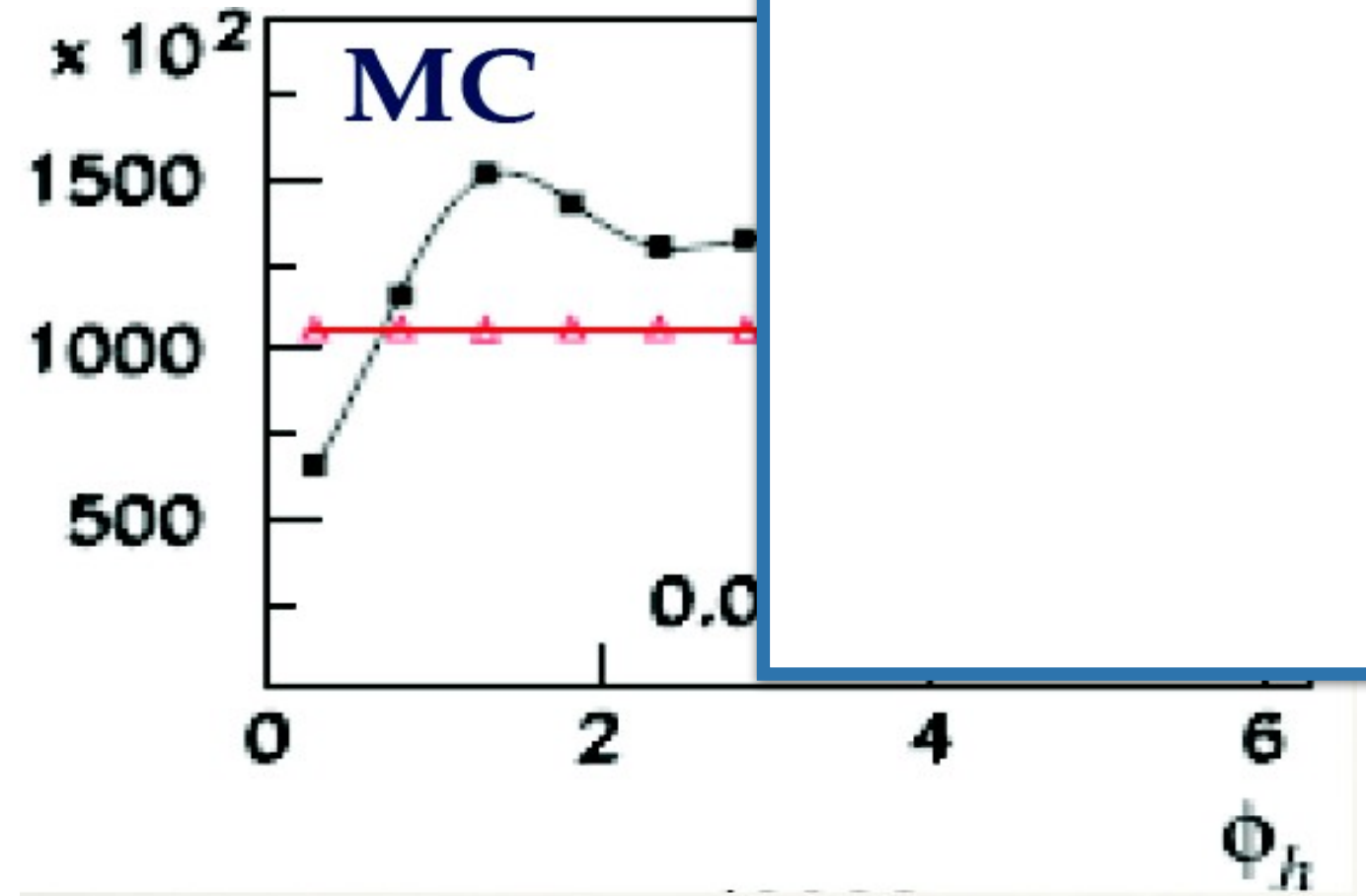
$$\mathcal{C} \left[h_1^{\perp,q} \times H_1^{\perp,q} \right]$$

Measurement in ep:

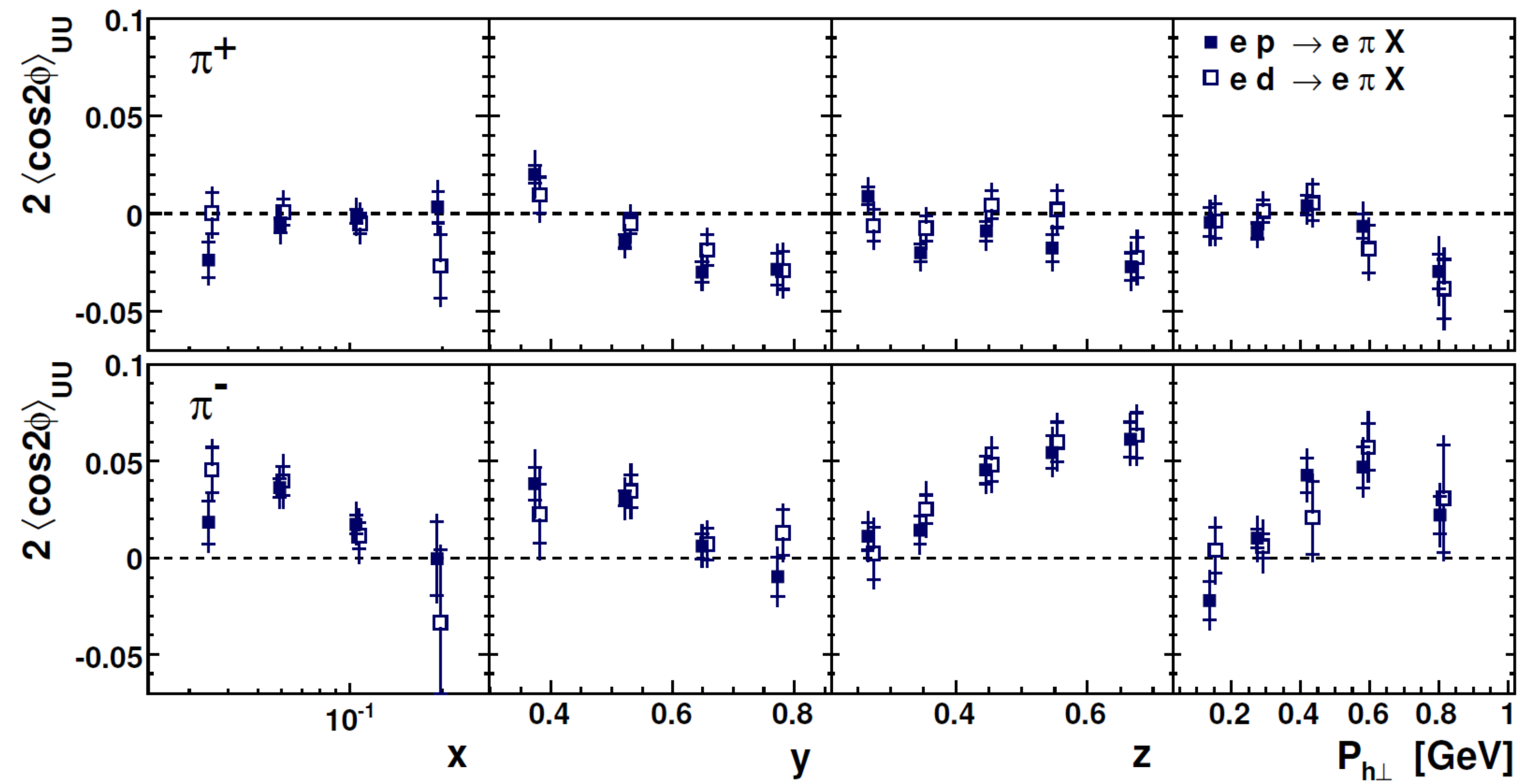
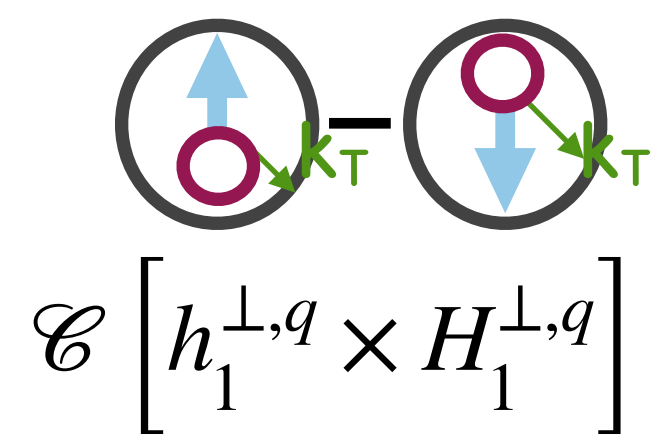
4D

Fully differential analysis
Unfolding in 400 x 12 bins

BINNING							
400 kinematic bins x 12 ϕ -bins							
Variable	Bin limits						#
x	0.023	0.042	0.078	0.145	0.27	1	5
y	0.3	0.45	0.6	0.7	0.85		4
z	0.2	0.3	0.45	0.6	0.75	1	5
P_{hT}	0.05	0.2	0.35	0.5	0.75		4



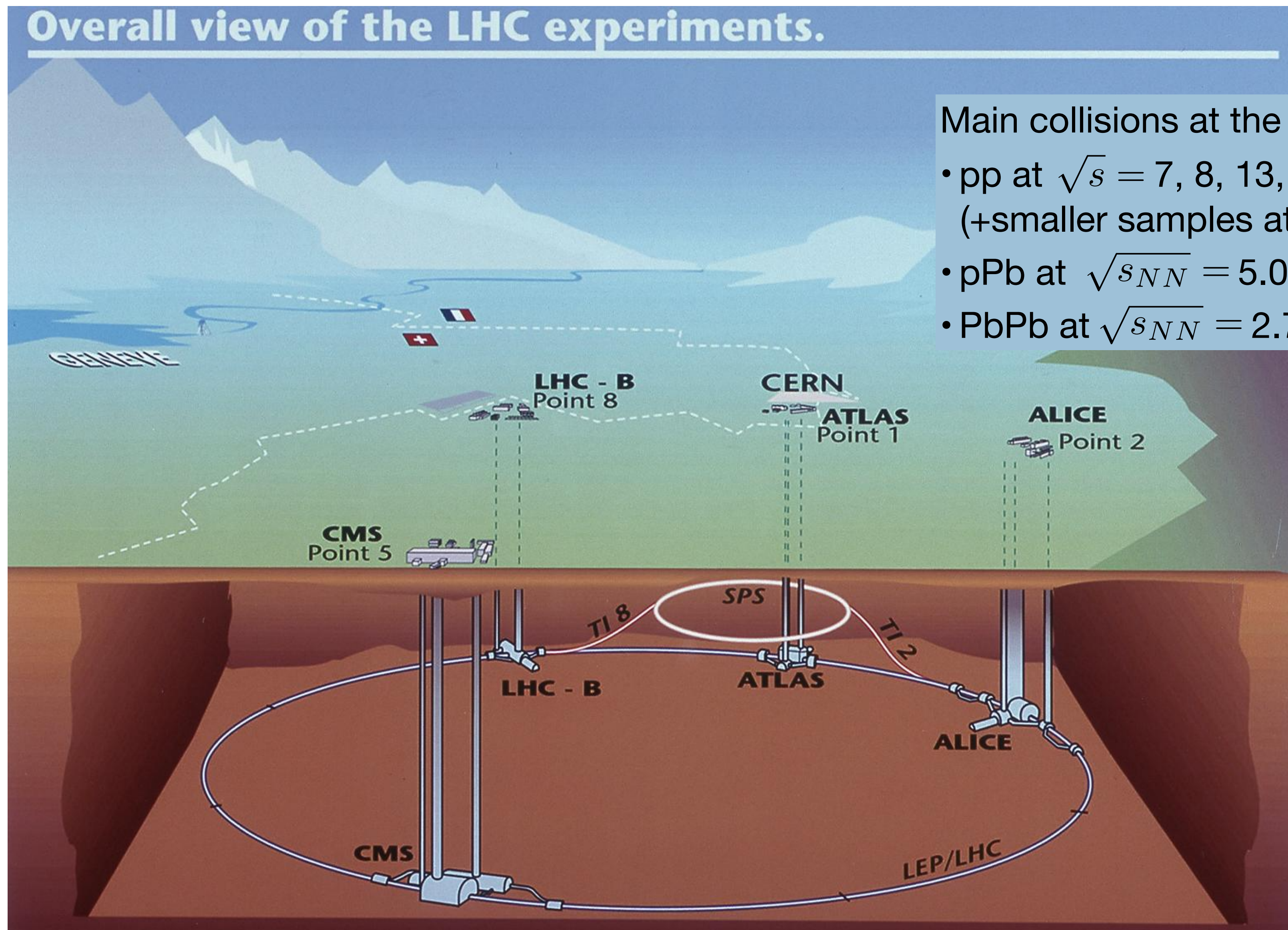
Boer-Mulders modulations



H-D comparison: $h_1^{\perp,u} \approx h_1^{\perp,d}$

Negative for π^+ ; positive for $\pi^- \rightarrow H_1^{\perp,u \rightarrow \pi^+} \approx -H_1^{\perp,u \rightarrow \pi^-}$

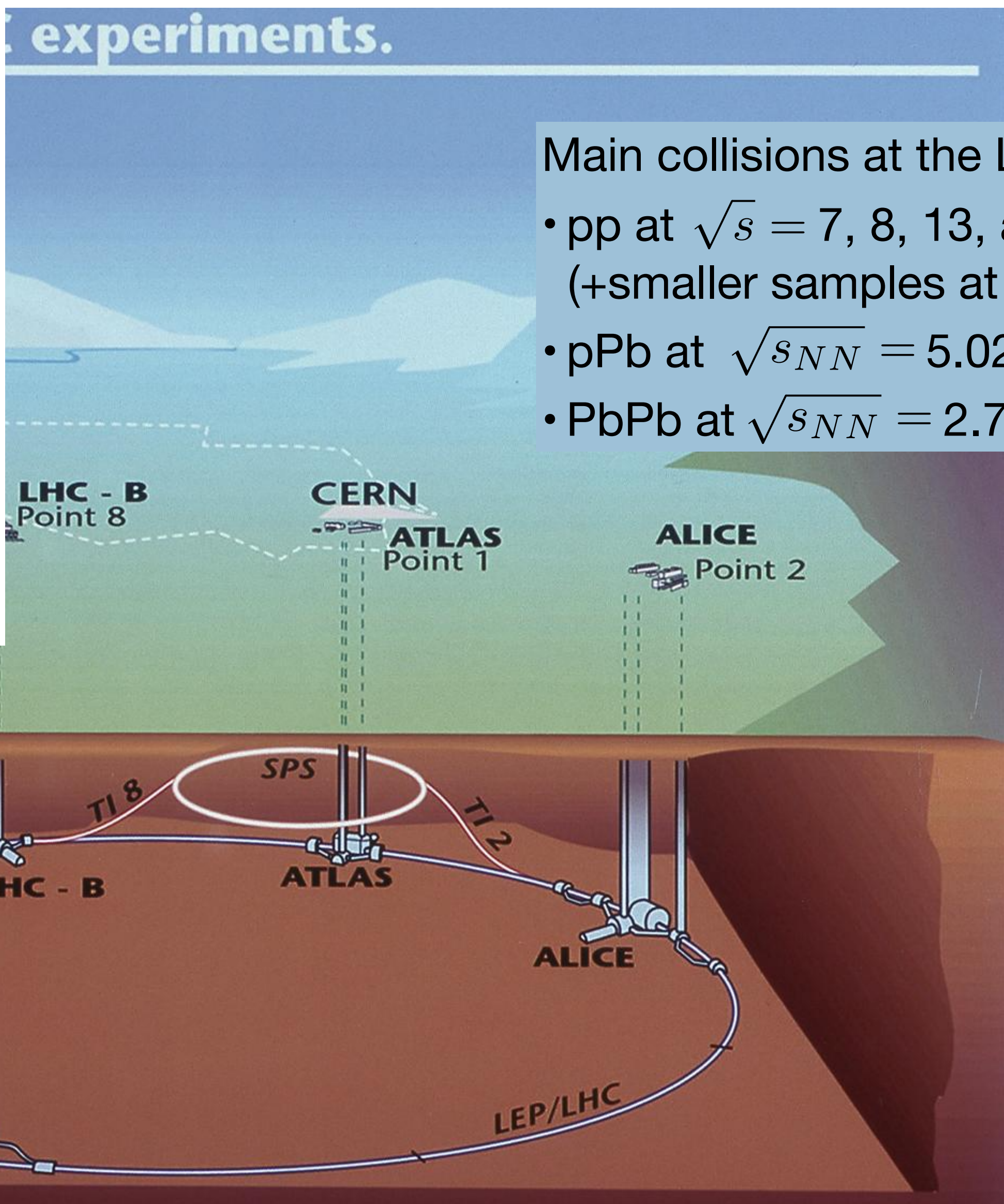
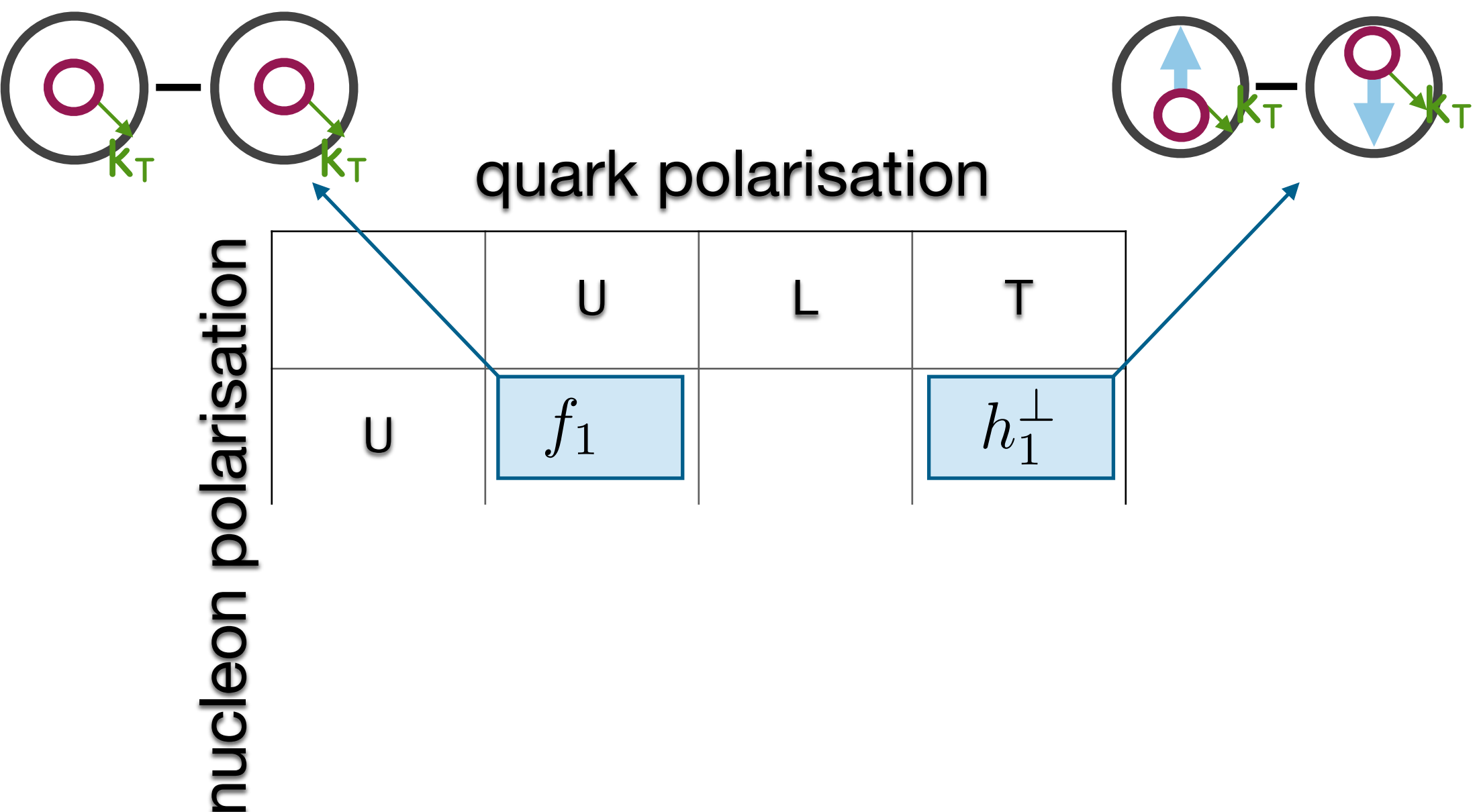
Study of quark TMD PDFs at the LHC



Main collisions at the LHC:

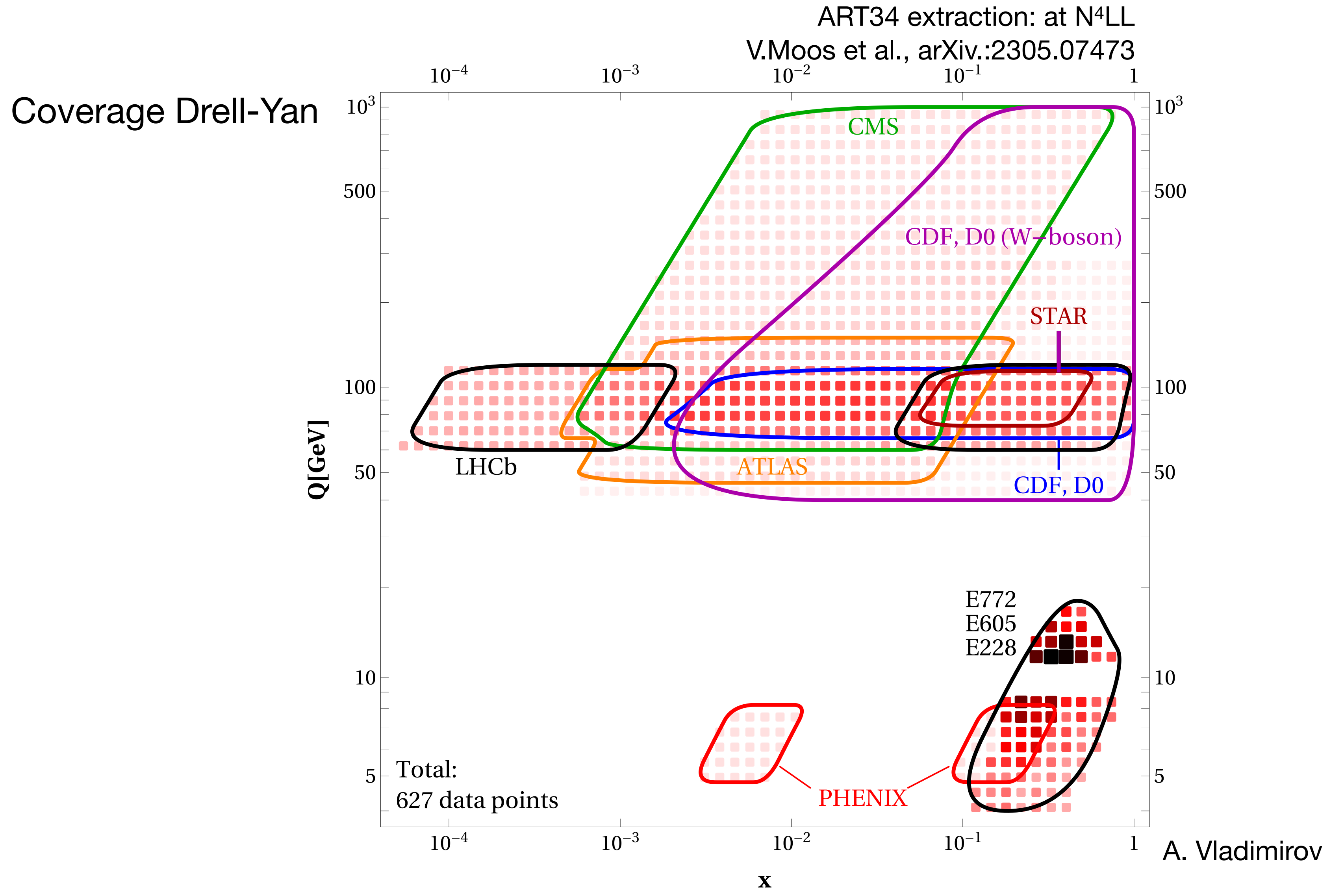
- pp at $\sqrt{s} = 7, 8, 13, \text{ and } 14 \text{ TeV}$
(+smaller samples at 2.76 and 5.02 TeV)
- pPb at $\sqrt{s_{NN}} = 5.02, 8.20, 8.80 \text{ TeV}$
- PbPb at $\sqrt{s_{NN}} = 2.76, 5.02, 5.44 \text{ TeV}$

Study of quark TMD PDFs at the LHC

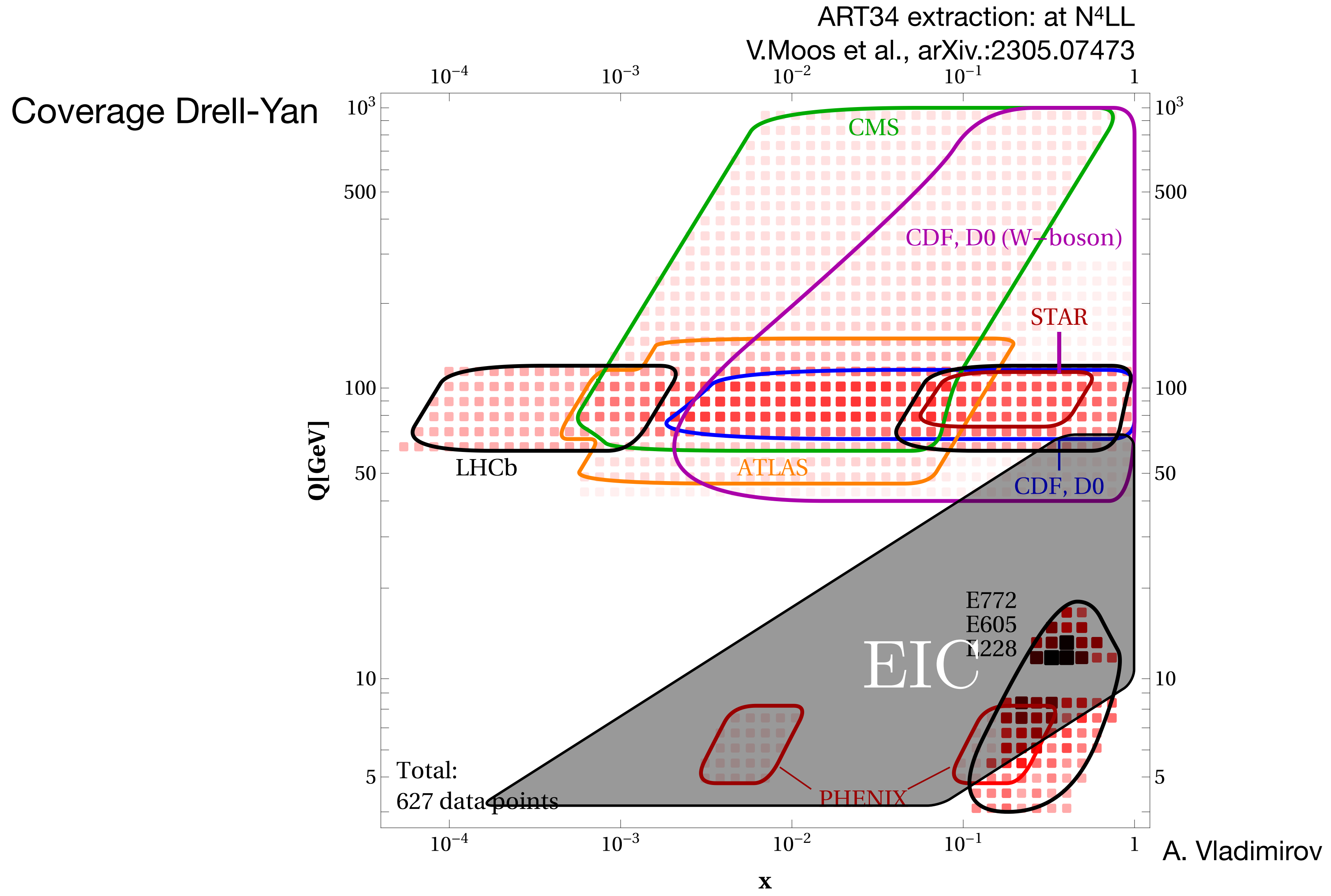


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- pp at $\sqrt{s} = 7, 8, 13, \text{ and } 14 \text{ TeV}$
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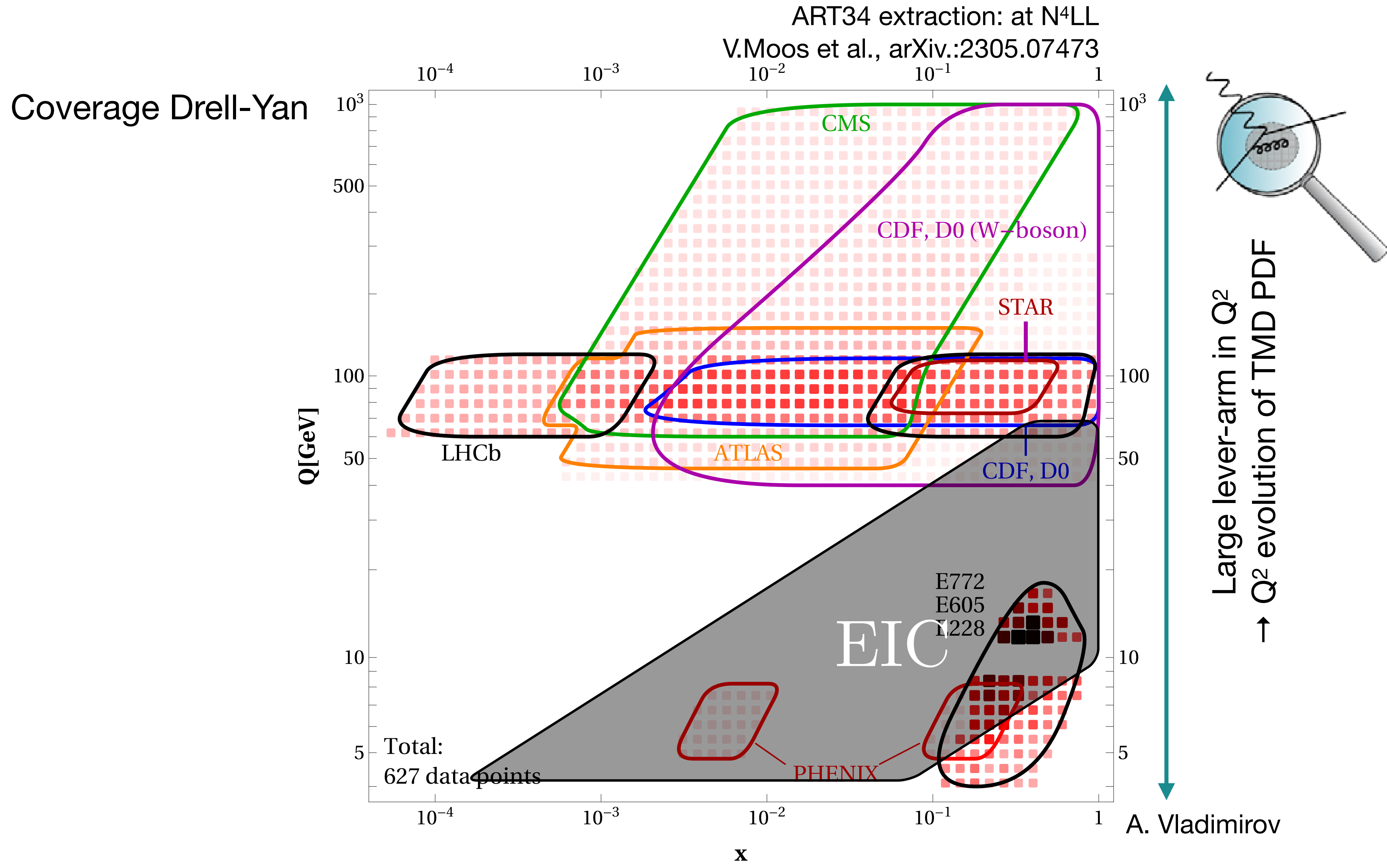
Study of spin-independent quark TMD PDFs at the LHC



Study of spin-independent quark TMD PDFs at the LHC



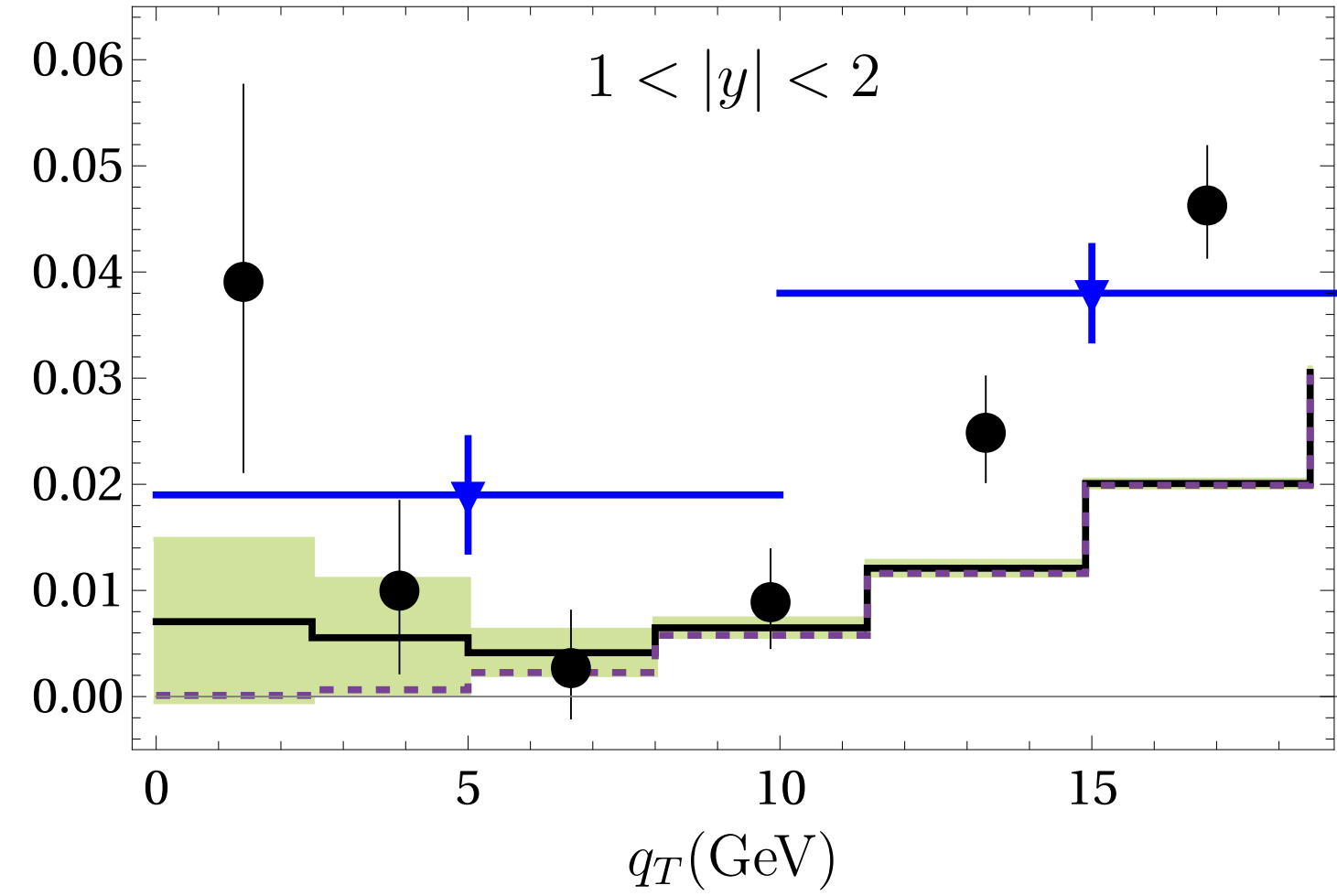
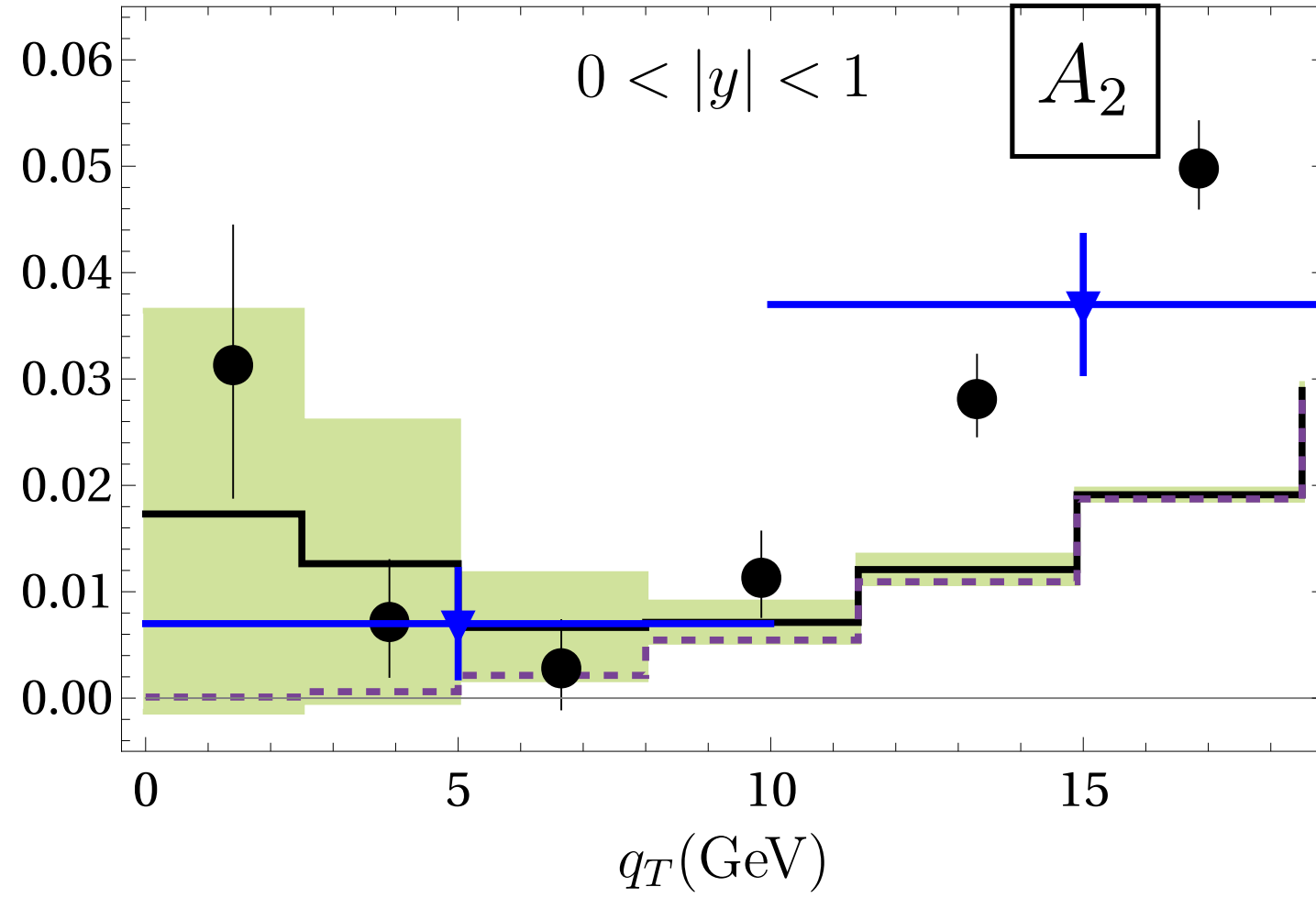
Study of spin-independent quark TMD PDFs at the LHC



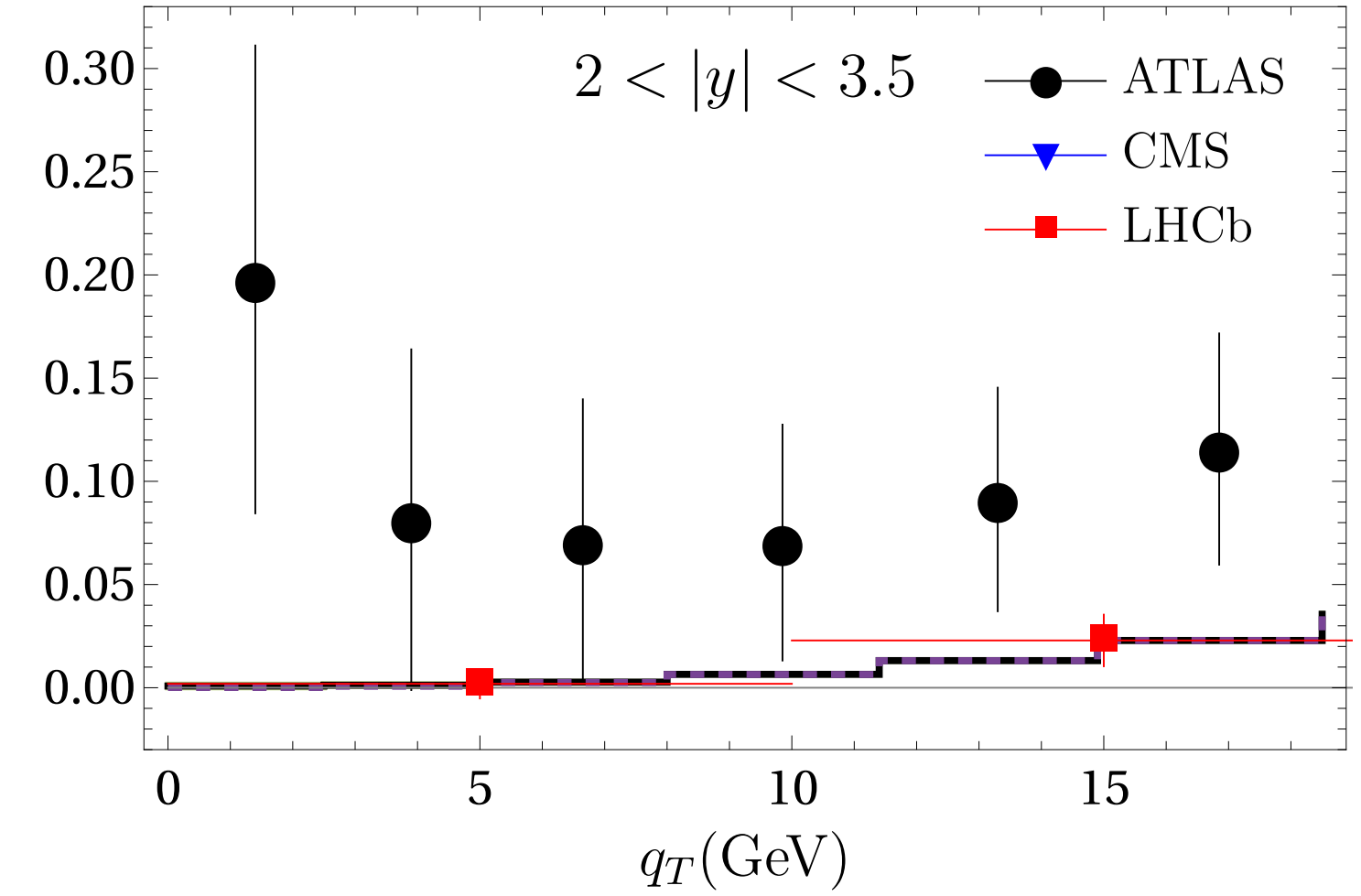
Quark Boer-Mulders TMD PDFs at the LHC

$A_2 \sim h_1^\perp h_1^\perp$ and $f_1 f_1$

Comparison data – fit:



S. Piloñeta, A. Vladimirov, JHEP **12** (2024) 059



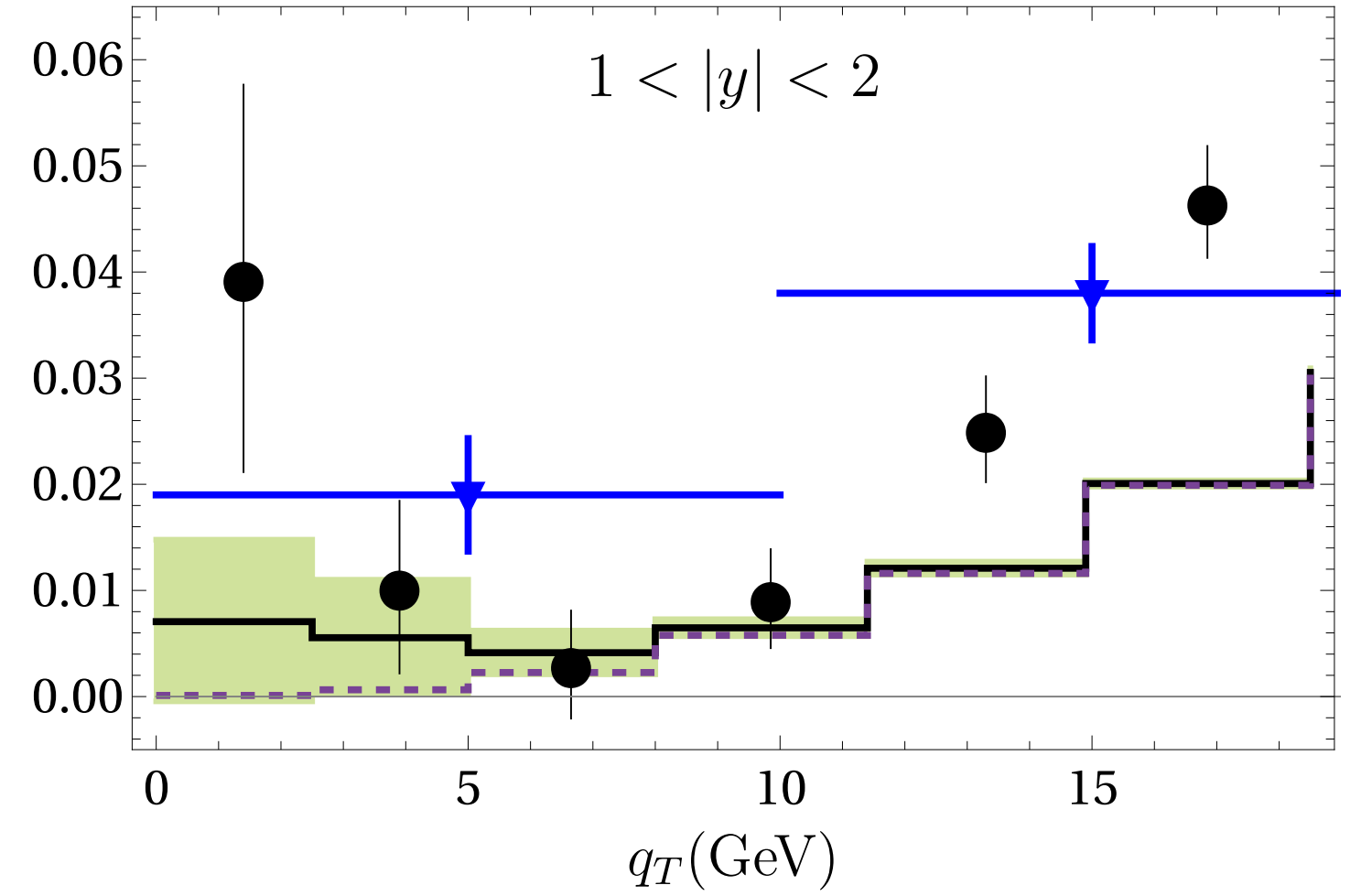
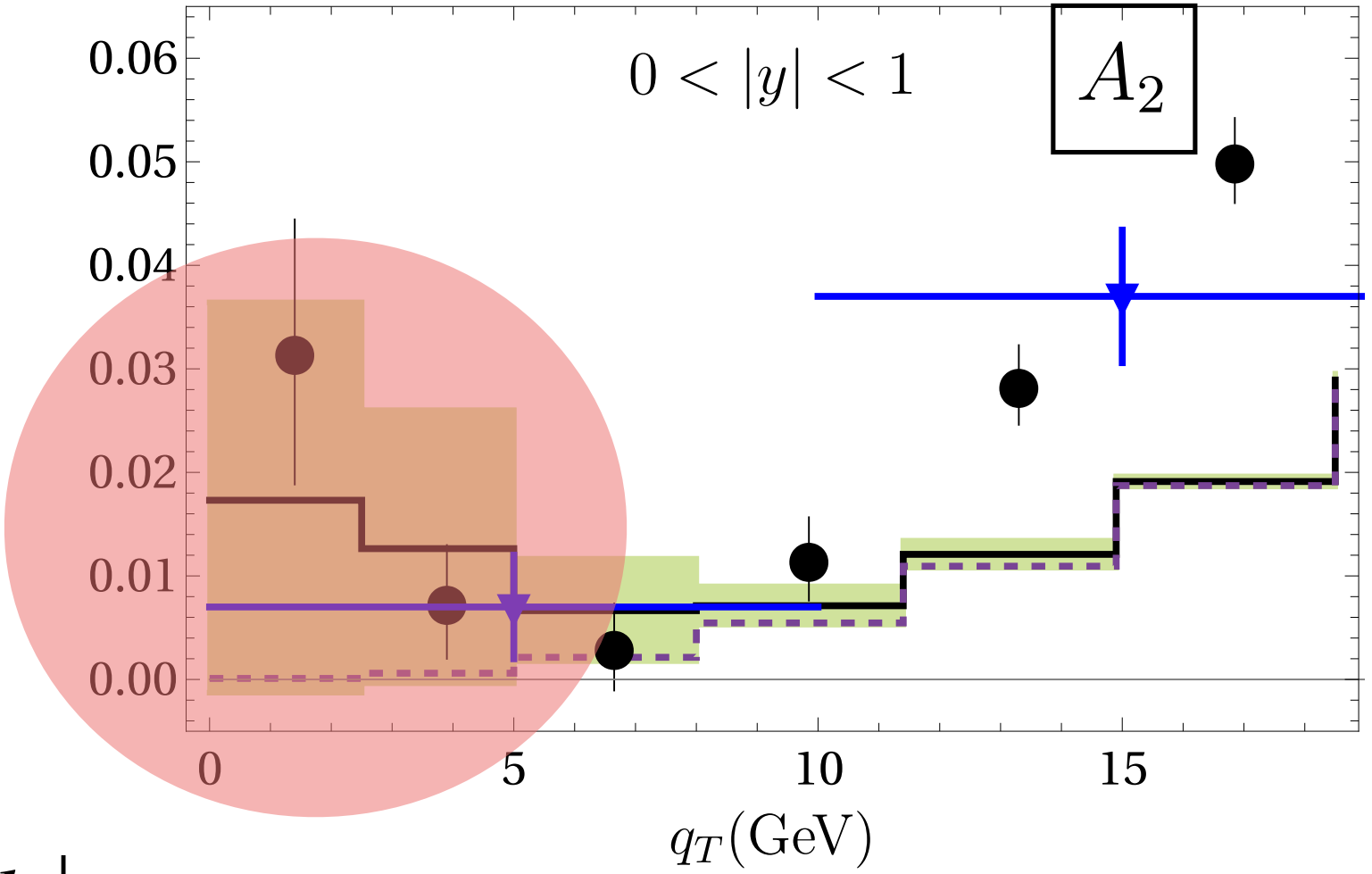
----- No Boer-Mulders

- ATLAS JHEP **08** (2016) 159.
- CMS, Phys. Lett. B **750** (2015) 154.
- LHCb, Phys. Rev. Lett. **129** (2022) 091801.

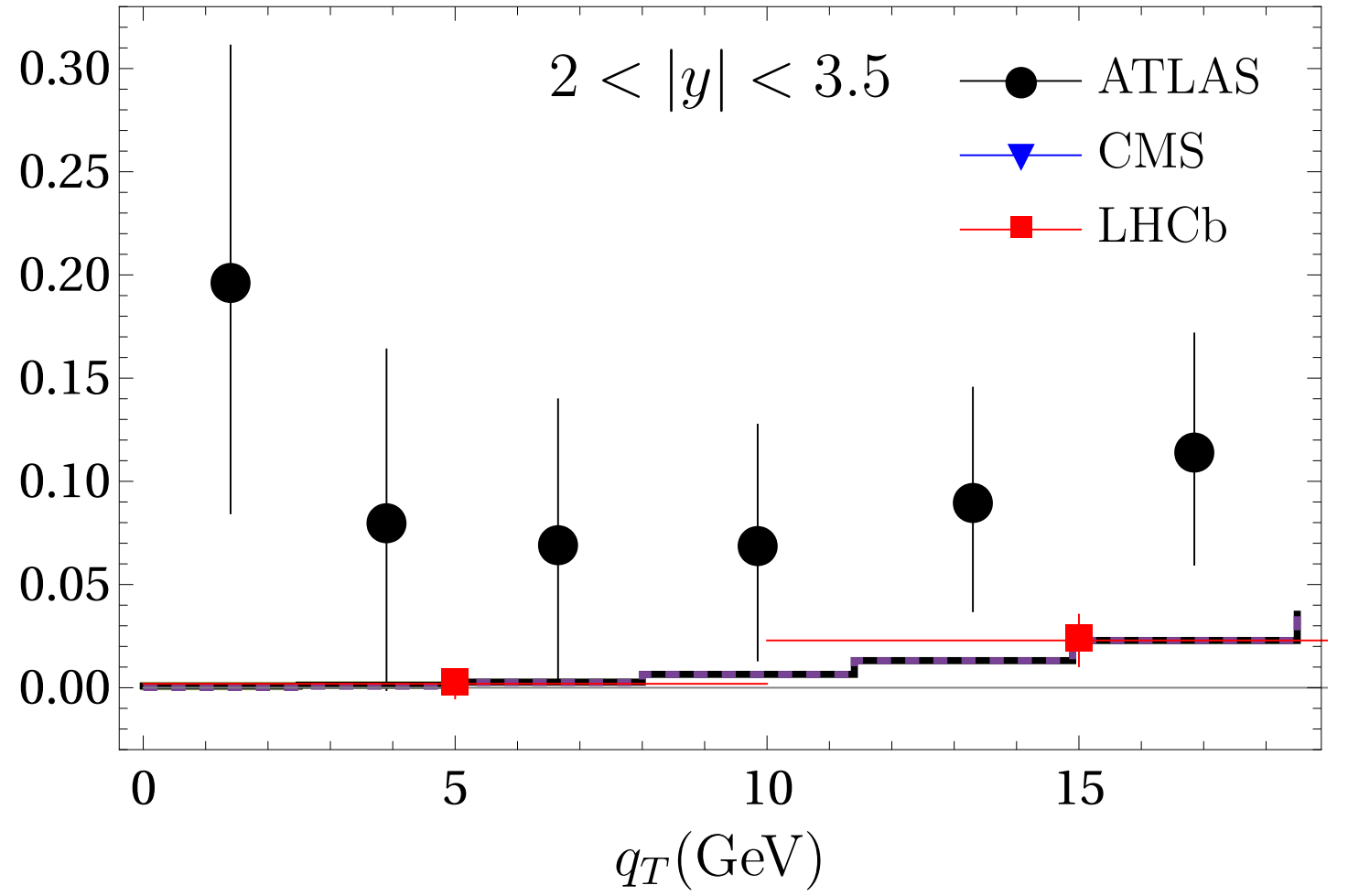
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$h_1^\perp h_1^\perp$ dominant

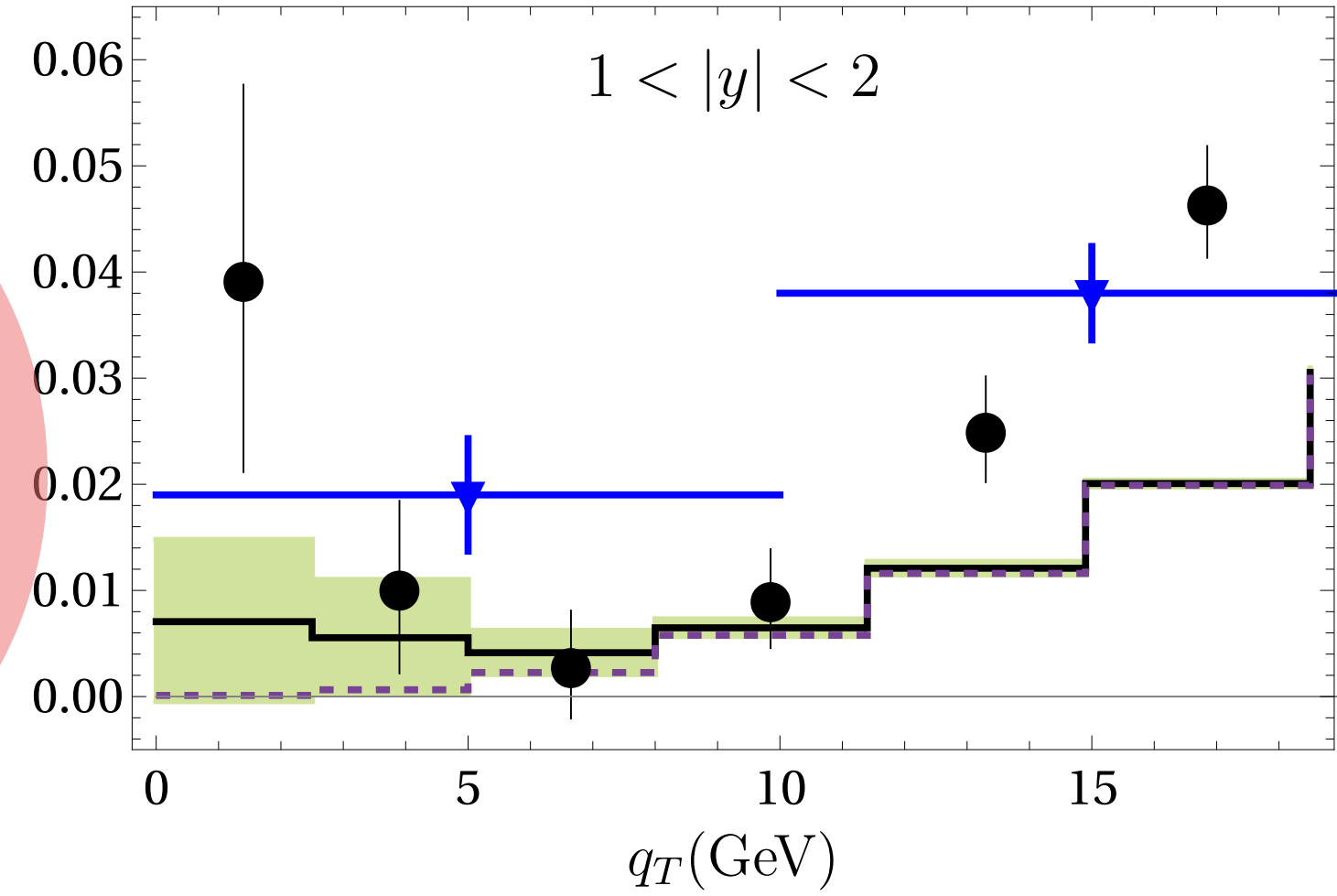
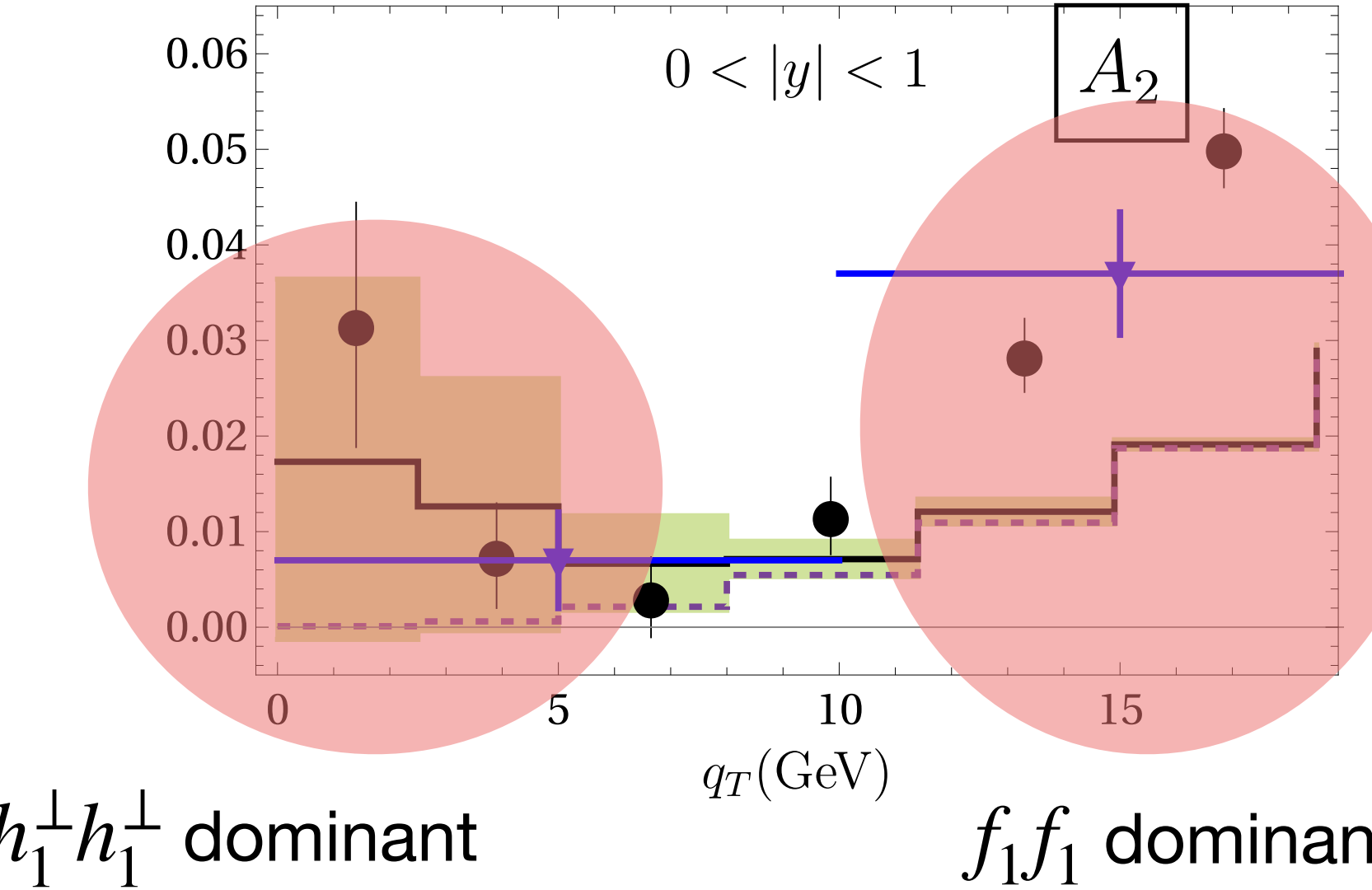
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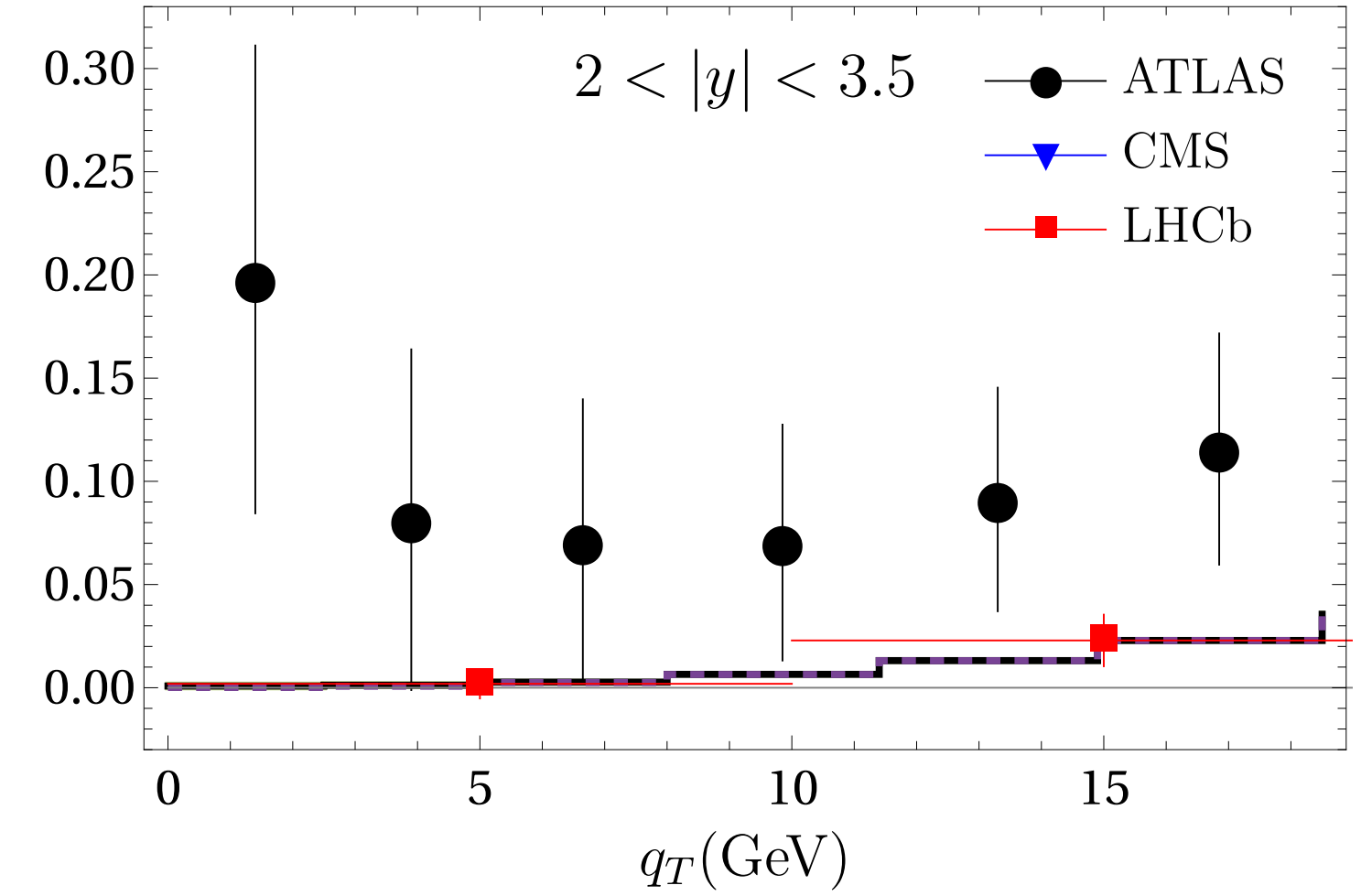
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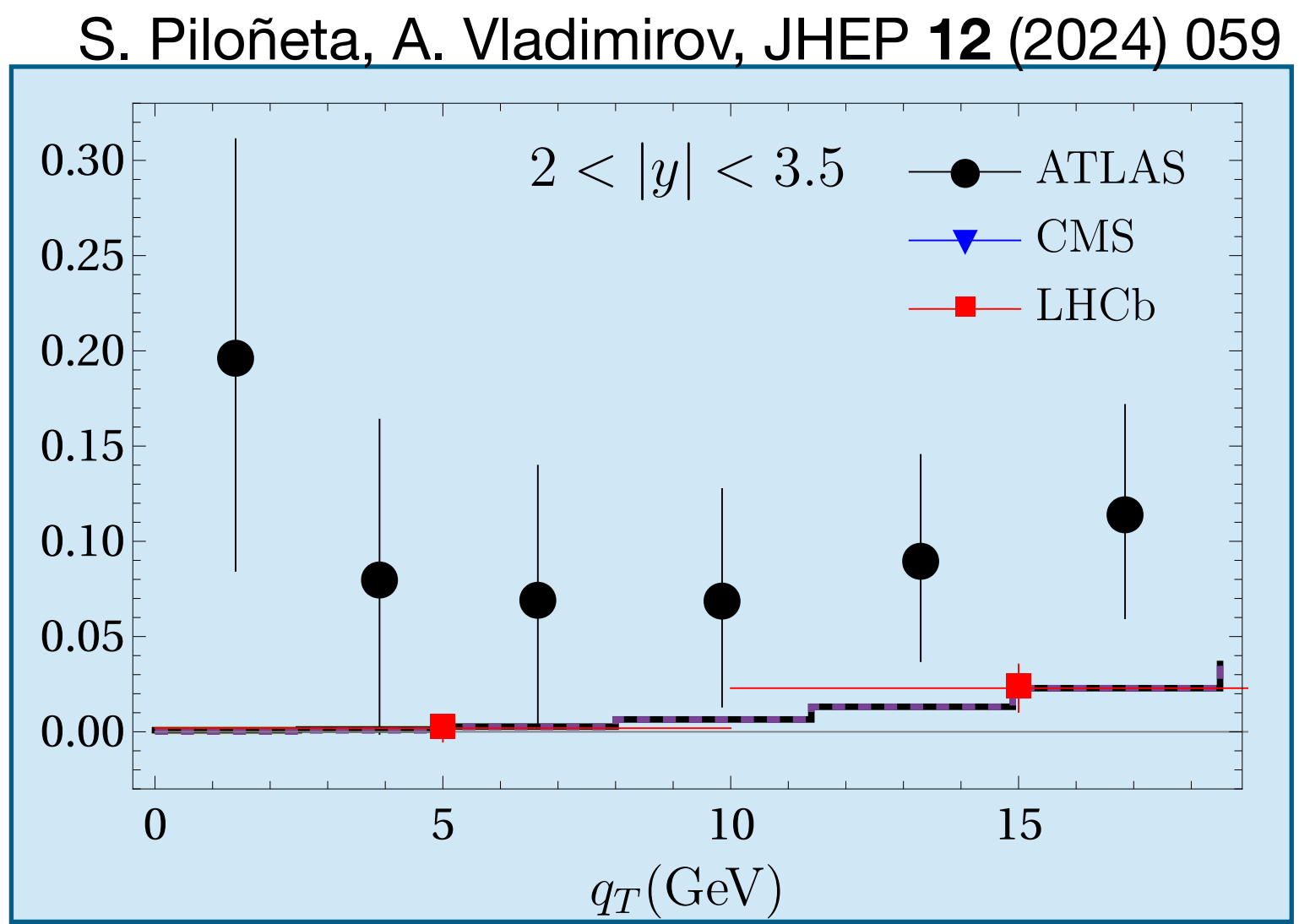
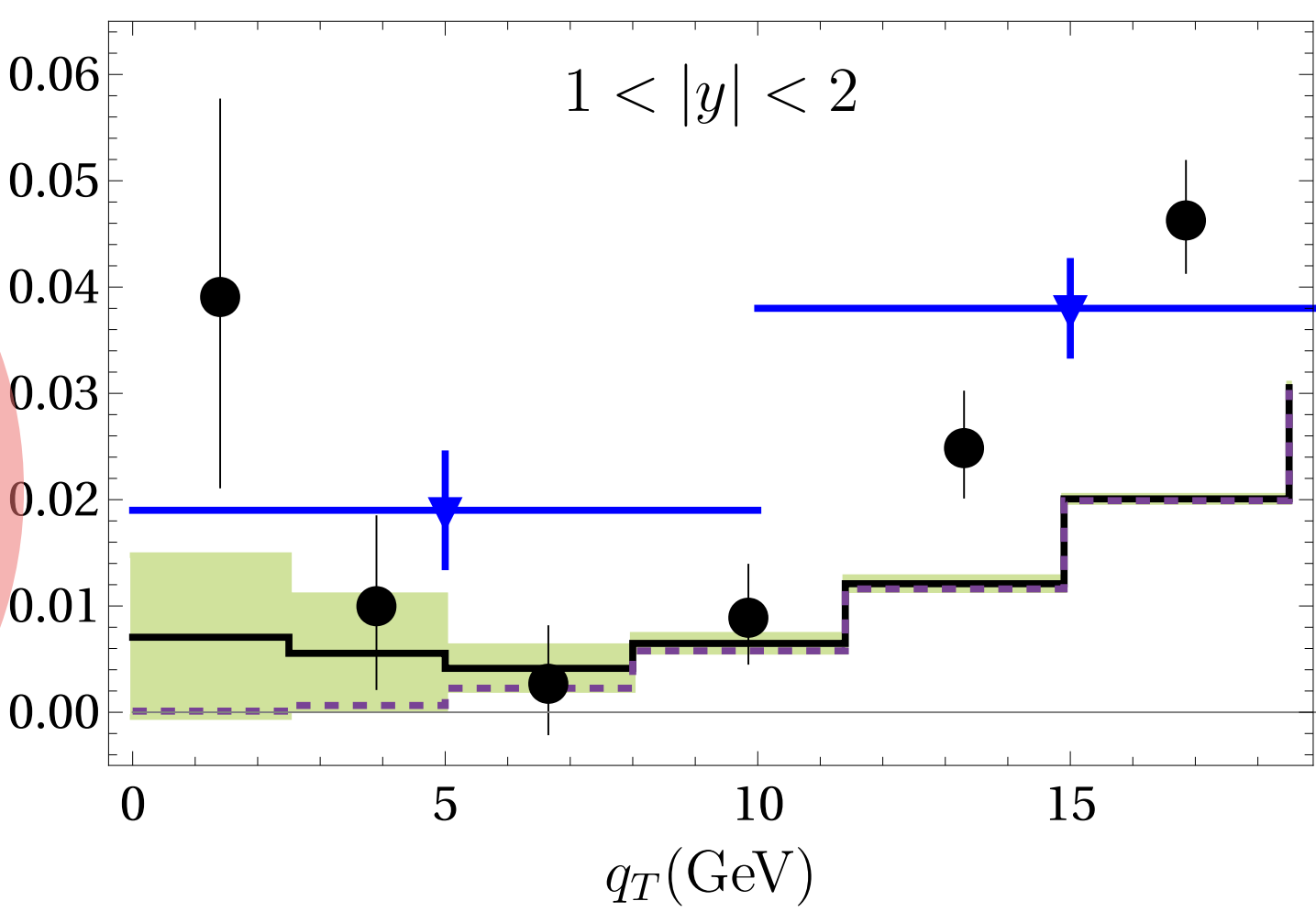
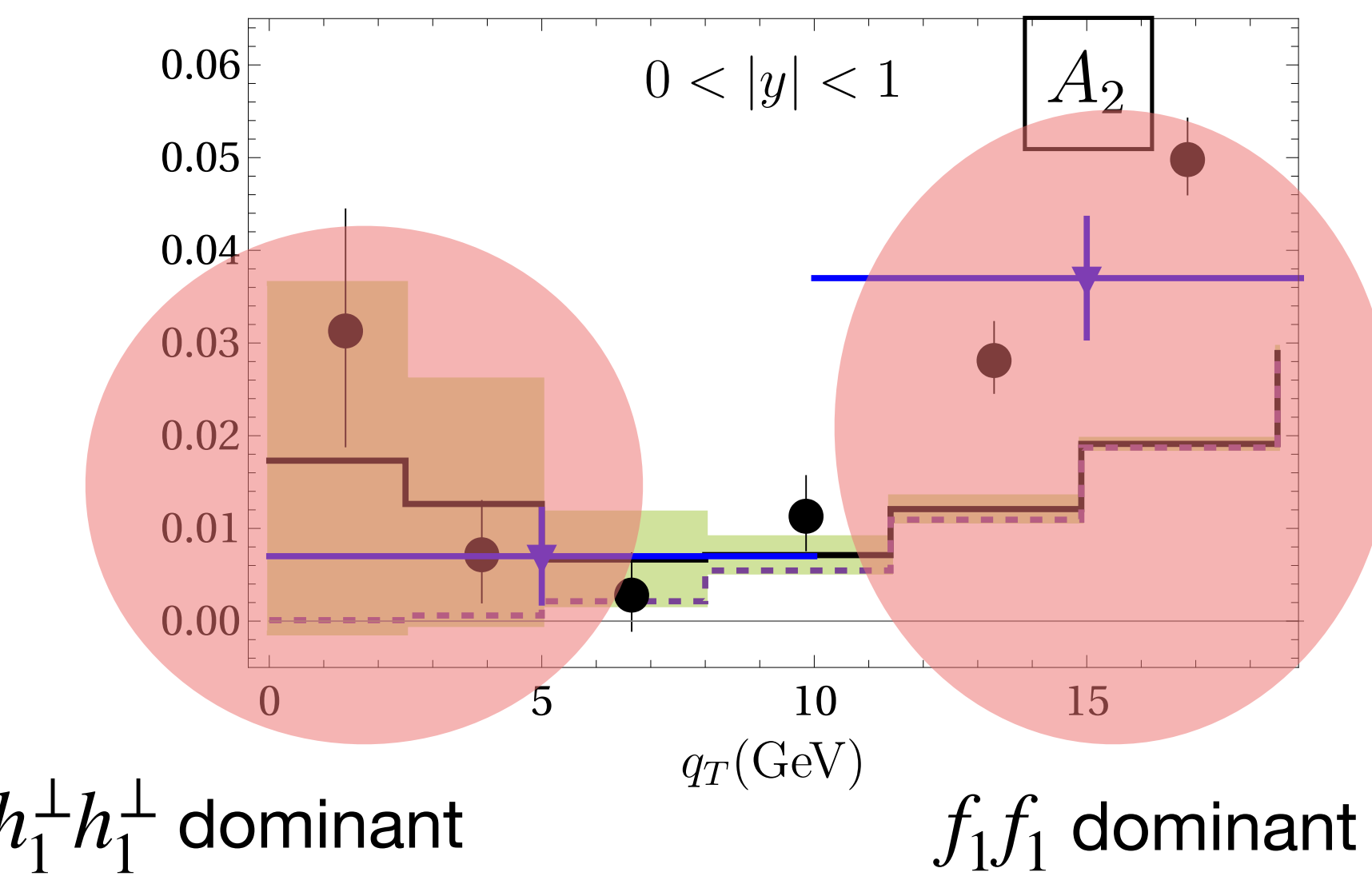
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Quark Boer-Mulders TMD PDFs at the LHC

$A_2 \sim h_1^\perp h_1^\perp$ and $f_1 f_1$

Comparison data – fit:



----- No Boer-Mulders

- ATLAS JHEP **08** (2016) 159.
- CMS, Phys. Lett. B **750** (2015) 154.
- LHCb, Phys. Rev. Lett. **129** (2022) 091801.

Problematic: inconsistent with ATLAS; consistent with LHCb.

Gluon TMD PDFs

gluon polarisation

nucleon polarisation

	U	circular	linear
U	f_1^g		$h_1^{\perp g}$
L		g_1^{gg}	$h_{1L}^{\perp g}$
T	$f_{1T}^{\perp g}$	g_{1T}^g	$h_1^g, h_{1T}^{\perp g}$

Gluon TMD PDFs

gluon polarisation

nucleon polarisation

	U	circular	linear
U	f_1^g		$h_1^{\perp g}$
L		g_1^{gg}	$h_{1L}^{\perp g}$
T	$f_{1T}^{\perp g}$	g_{1T}^g	$h_1^g, h_{1T}^{\perp g}$

- In contrast to quark TMDs, gluon TMDs are almost unknown

Gluon TMD PDFs

gluon polarisation

nucleon polarisation

	U	circular	linear
U	f_1^g		$h_1^{\perp g}$
L		g_1^{gg}	$h_{1L}^{\perp g}$
T	$f_{1T}^{\perp g}$	g_{1T}^g	$h_1^g, h_{1T}^{\perp g}$

- In contrast to quark TMDs, gluon TMDs are almost unknown
- Accessible through production of dijets, high- P_T hadron pairs, quarkonia

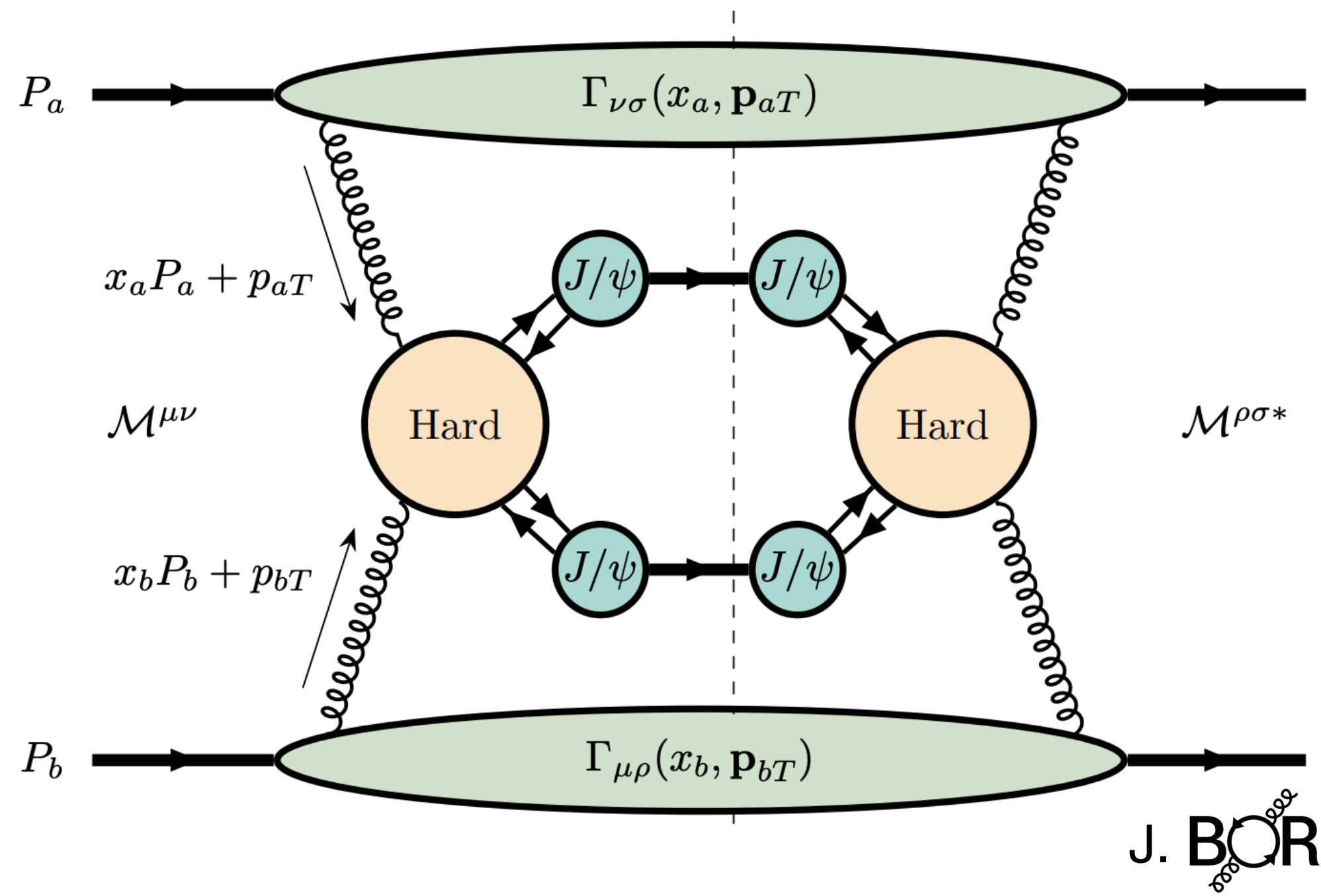
Access to gluon TMD PDFs

nucleon polarisation

gluon polarisation

	U	circular	linear
U	f_1^g		$h_1^{\perp g}$

Unpolarised experiments



No problem with factorisation if J/ψ in colour-singlet state

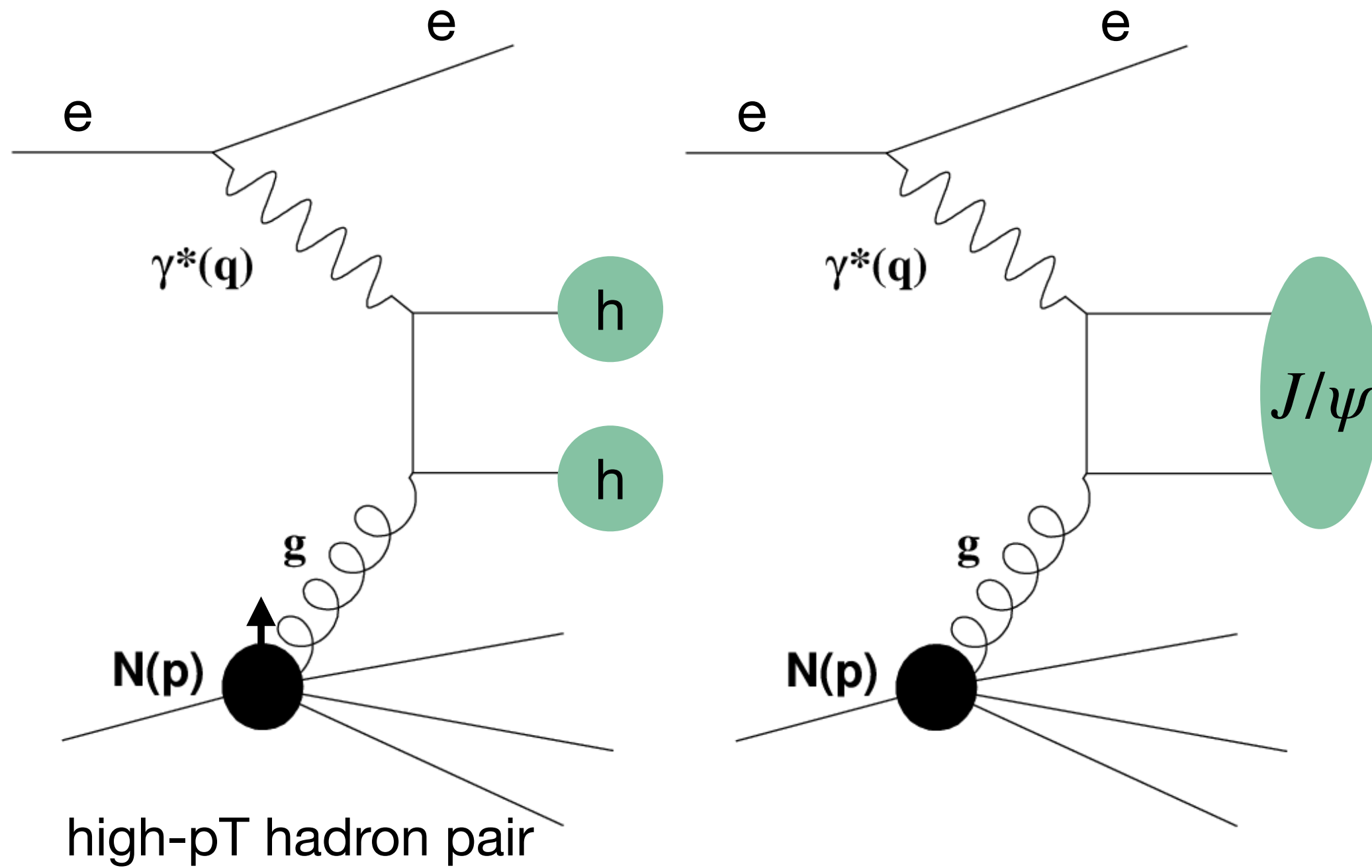
Access to gluon TMD PDFs

nucleon polarisation

gluon polarisation

	U	circular	linear
U	f_1^g		$h_1^{\perp g}$
L		g_1^{gg}	$h_{1L}^{\perp g}$
T	$f_{1T}^{\perp g}$	g_{1T}^g	$h_1^g, h_{1T}^{\perp g}$

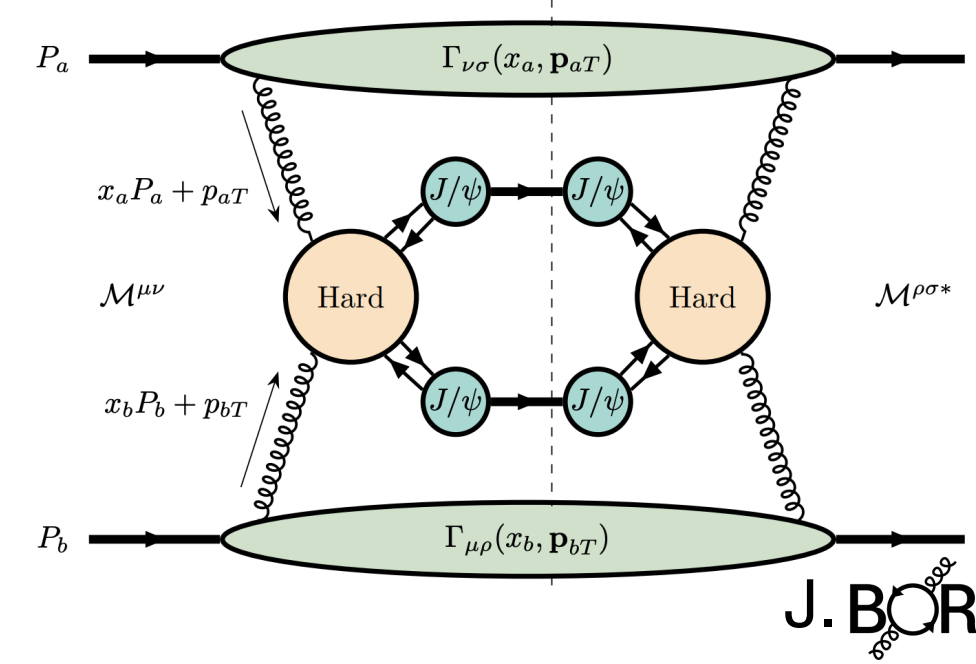
Polarised ep experiments



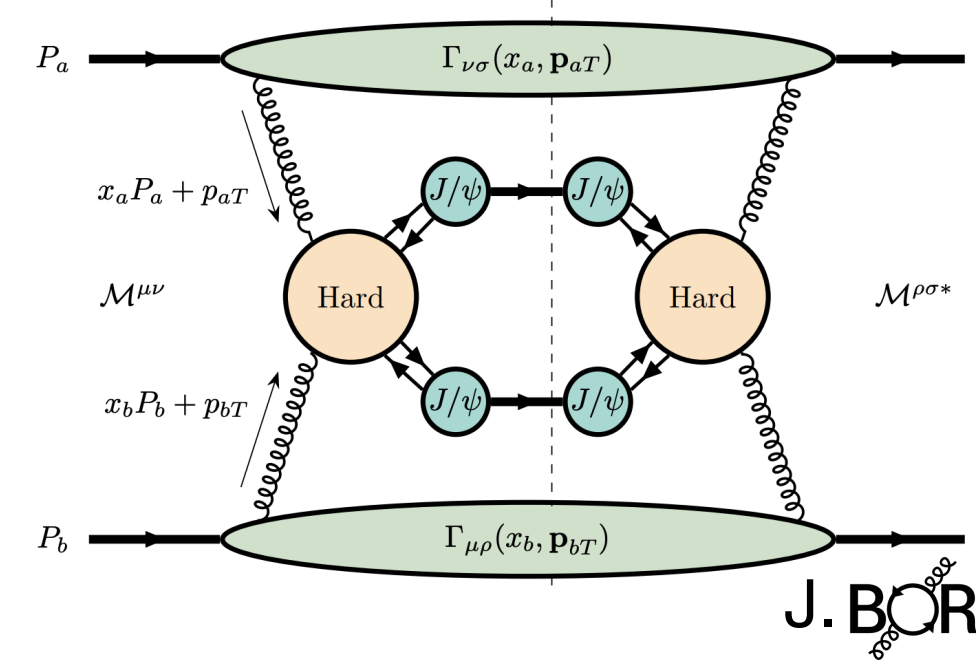
Linearly polarised gluon TMD PDF at LHCb

- $J/\psi J/\psi$ production largely dominated by gluon-induced processes

$$\sigma \propto F_1 \mathcal{C}[f_1^g f_1^g] + F_2 \mathcal{C}[w_2 h_1^{g\perp} h_1^{g\perp}] + \left(F_3 \mathcal{C}[w_3 f_1^g h_1^{g\perp}] + F'_3 \mathcal{C}[w'_3 f_1^g h_1^{g\perp}] \right) \cos(2\phi_{CS}) + \left(F_4 \mathcal{C}[w_4 h_1^{g\perp} h_1^{g\perp}] \right) \cos(4\phi_{CS})$$



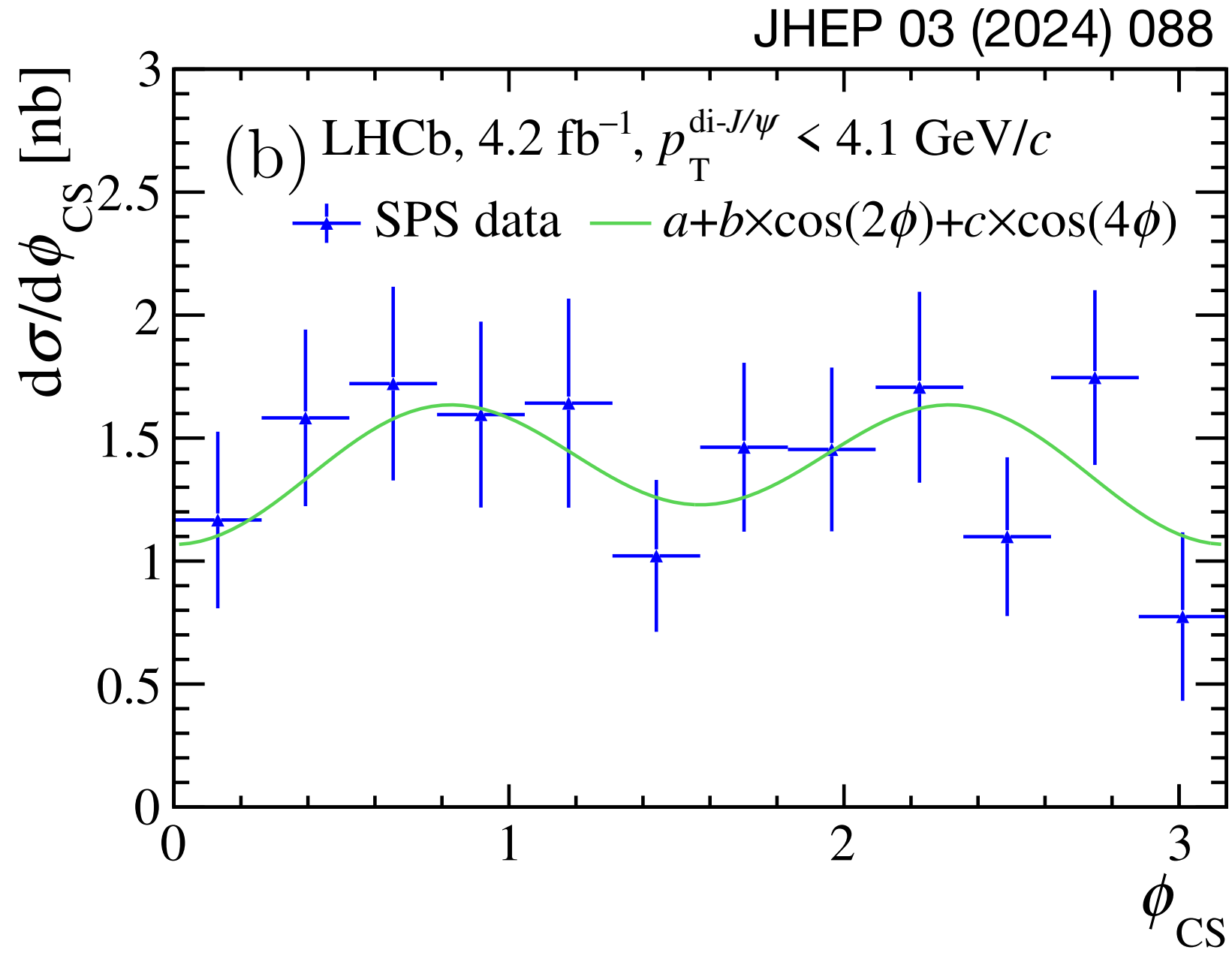
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After subtraction of the double-parton scattering contribution



$$p_T^{J/\psi J/\psi} < \frac{\langle M_{J/\psi J/\psi} \rangle}{2},$$

$$\langle M_{J/\psi J/\psi} \rangle = 8.2 \text{ GeV}/c^2$$

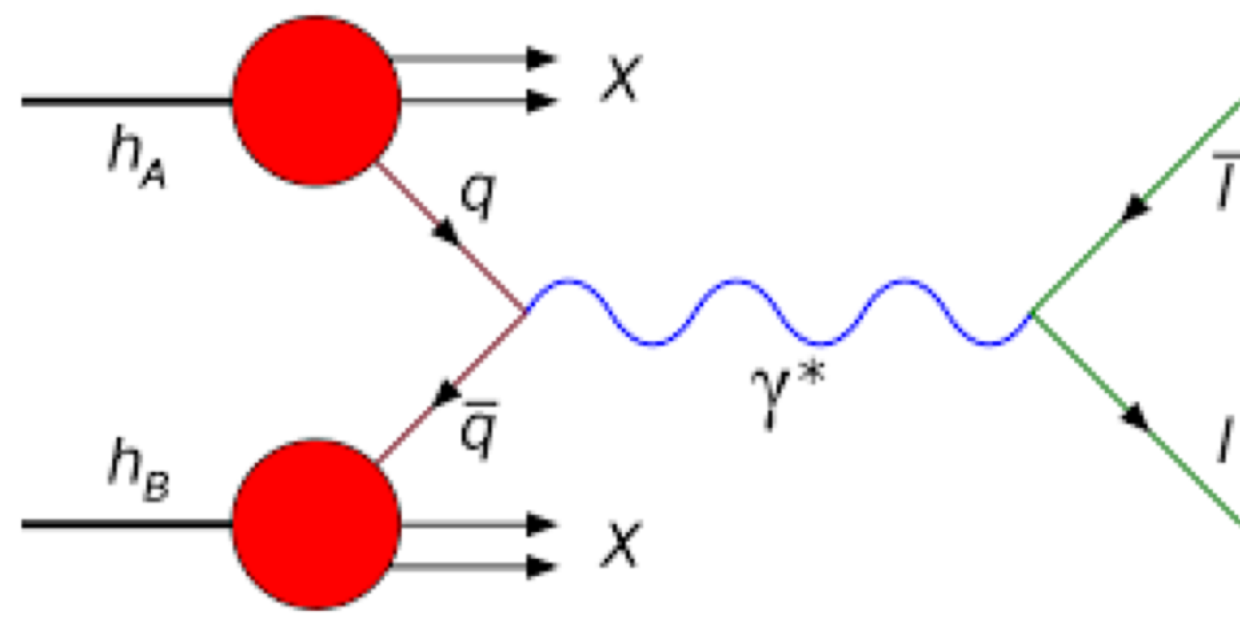
$$\langle \cos 2\phi_{CS} \rangle = -0.029 \pm 0.050 \text{ (stat)} \pm 0.009 \text{ (syst)}$$

$$\langle \cos 4\phi_{CS} \rangle = -0.087 \pm 0.052 \text{ (stat)} \pm 0.013 \text{ (syst)}$$

Upcoming

A000BER

Apparatus for Meson and Baryon
Experimental Research

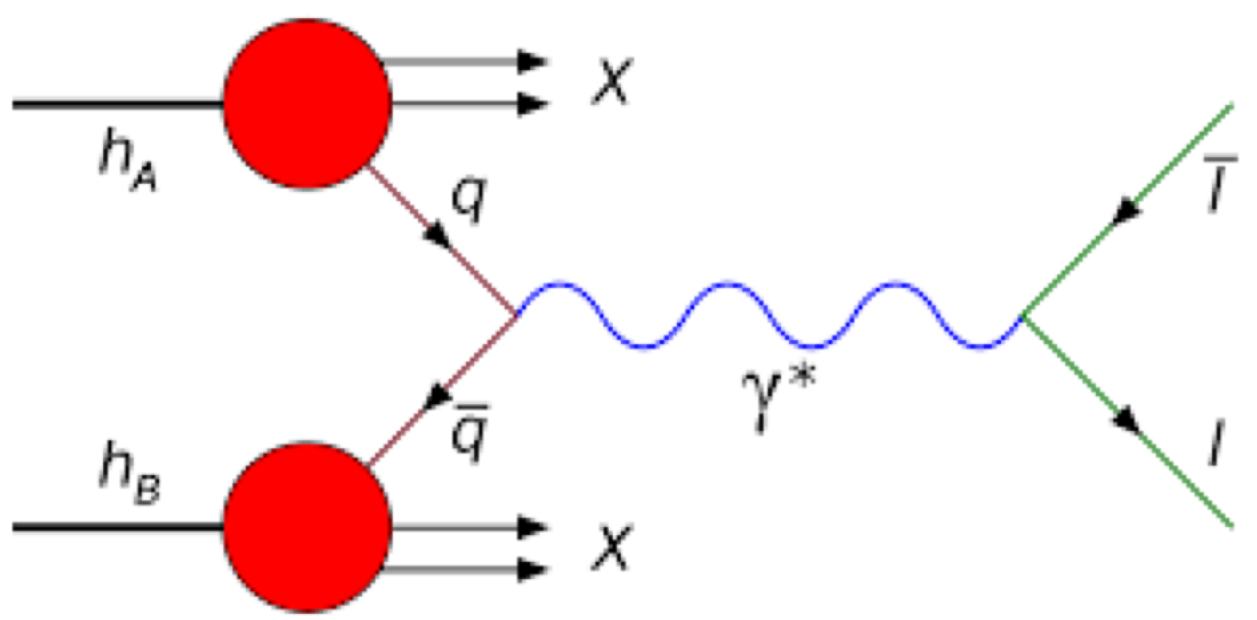


Meson structure

Upcoming

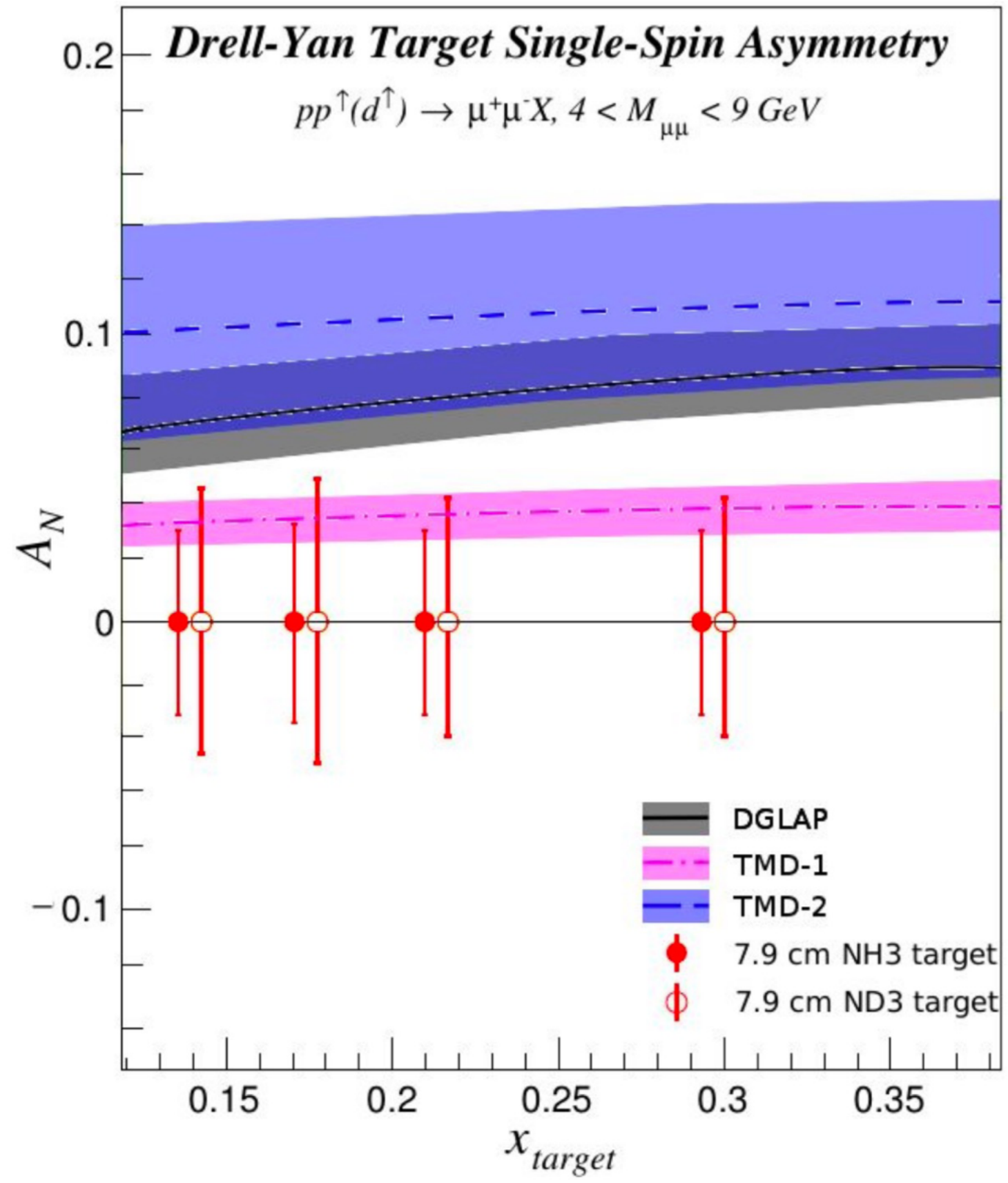


Apparatus for Meson and Baryon Experimental Research



Meson structure

SpinQuest

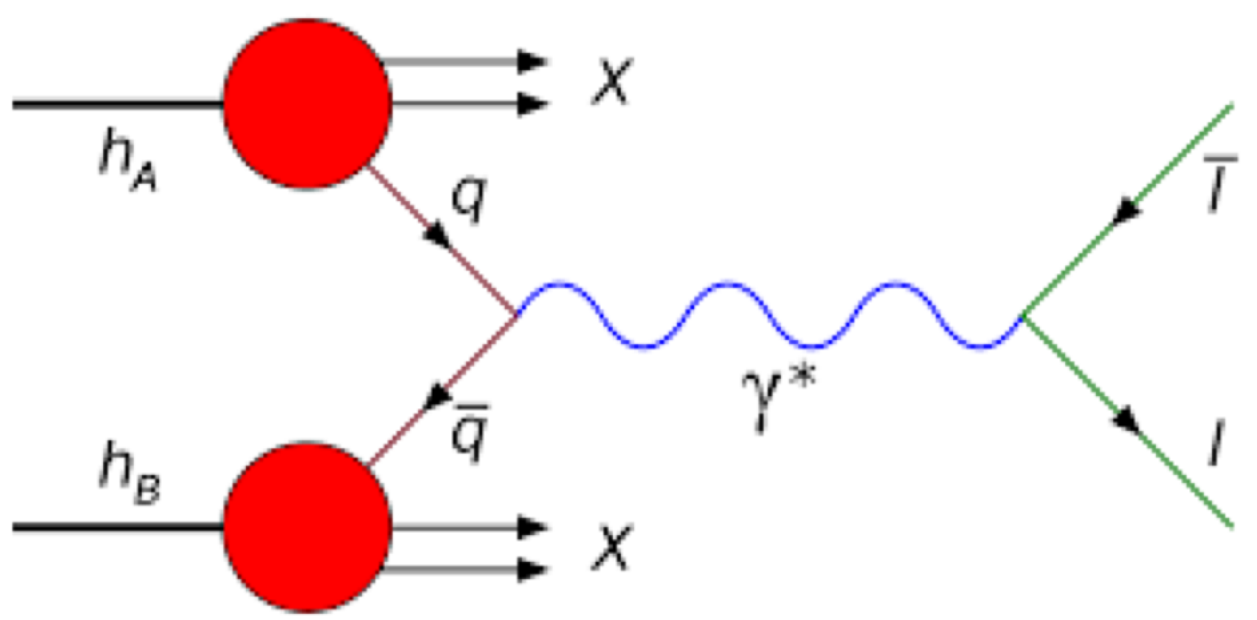


Study of \bar{u} and \bar{d} Siverson function

Upcoming

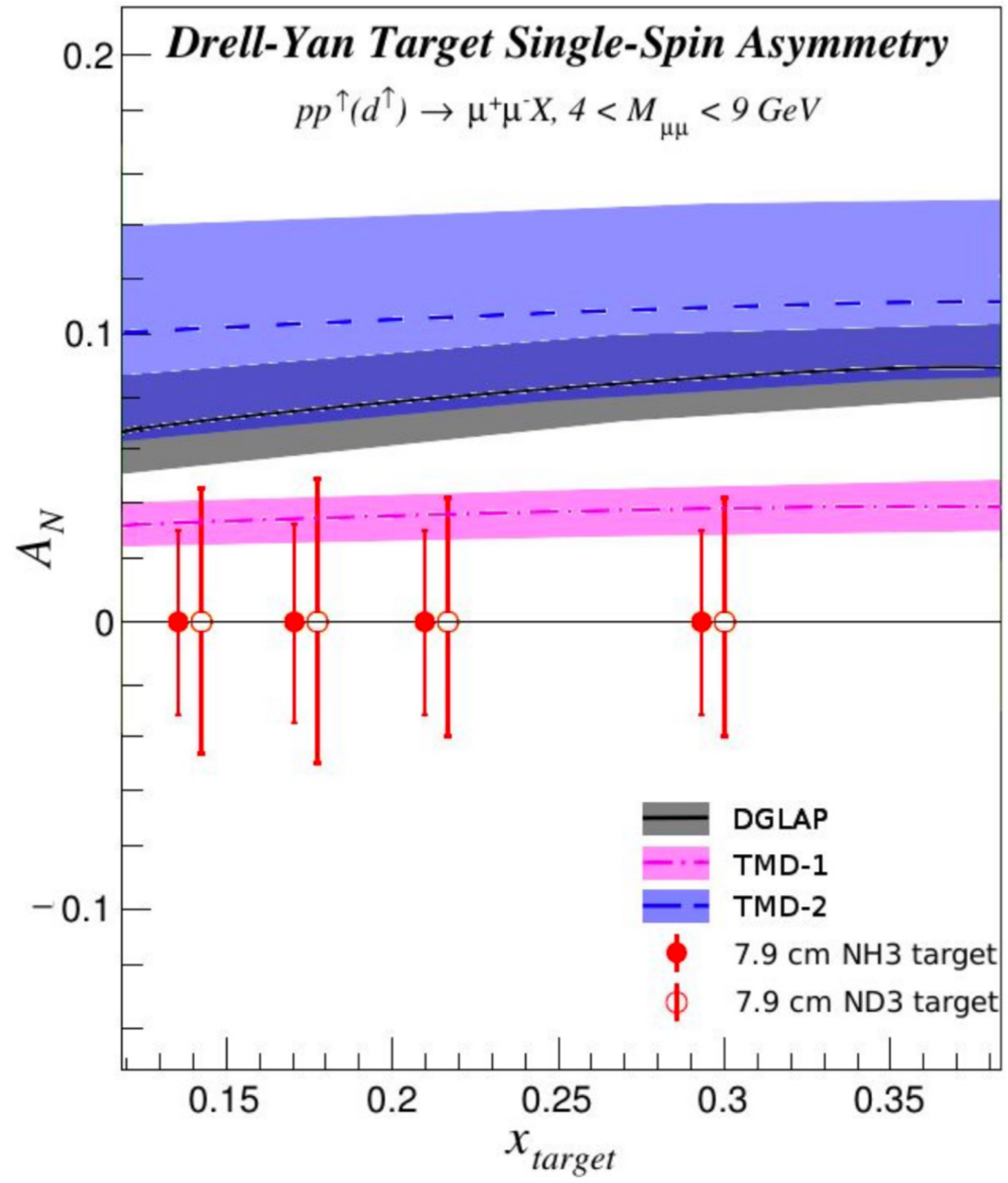
A000BER

Apparatus for Meson and Baryon Experimental Research

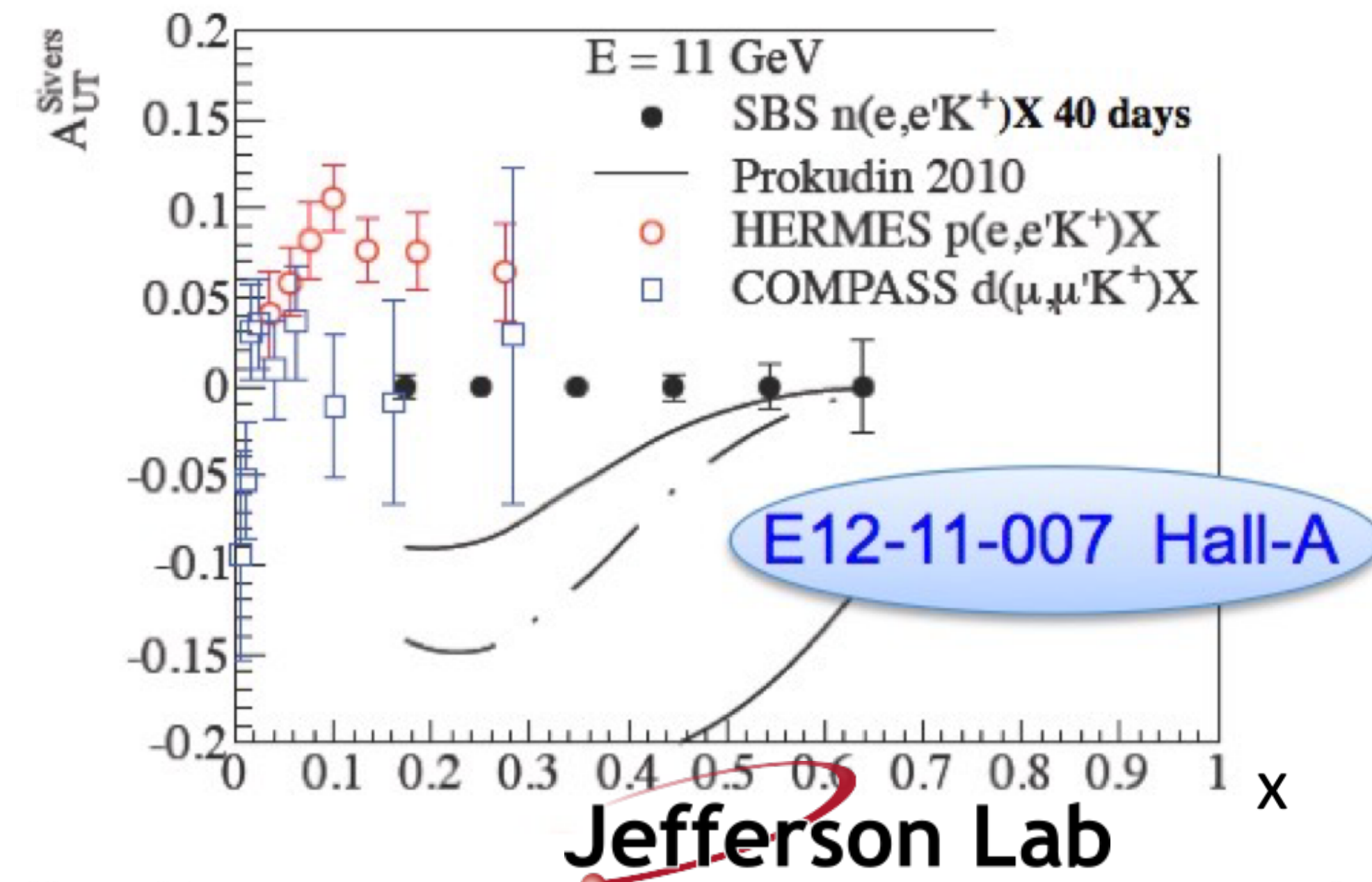


Meson structure

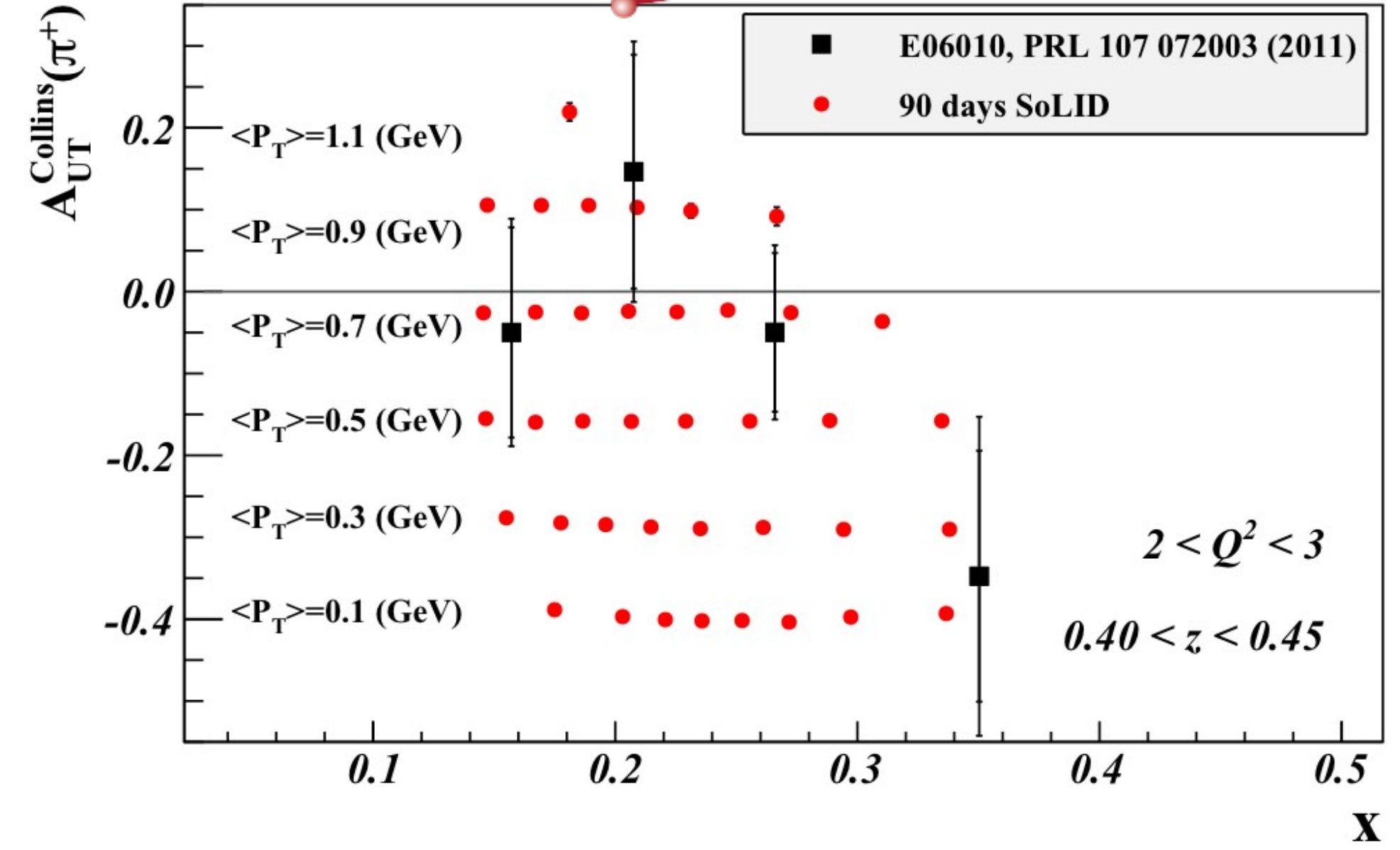
SpinQuest



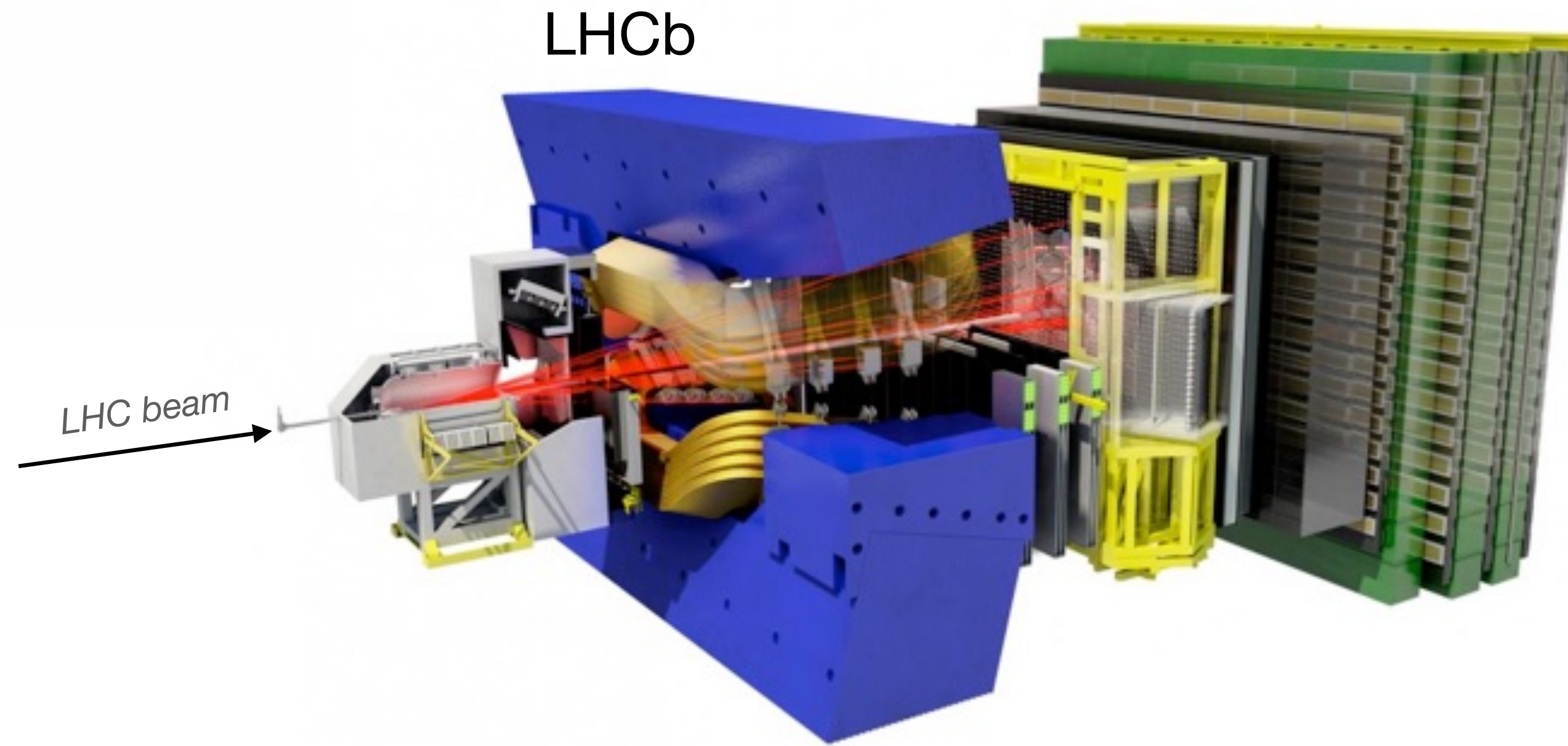
Study of \bar{u} and \bar{d} Sivens function



Jefferson Lab

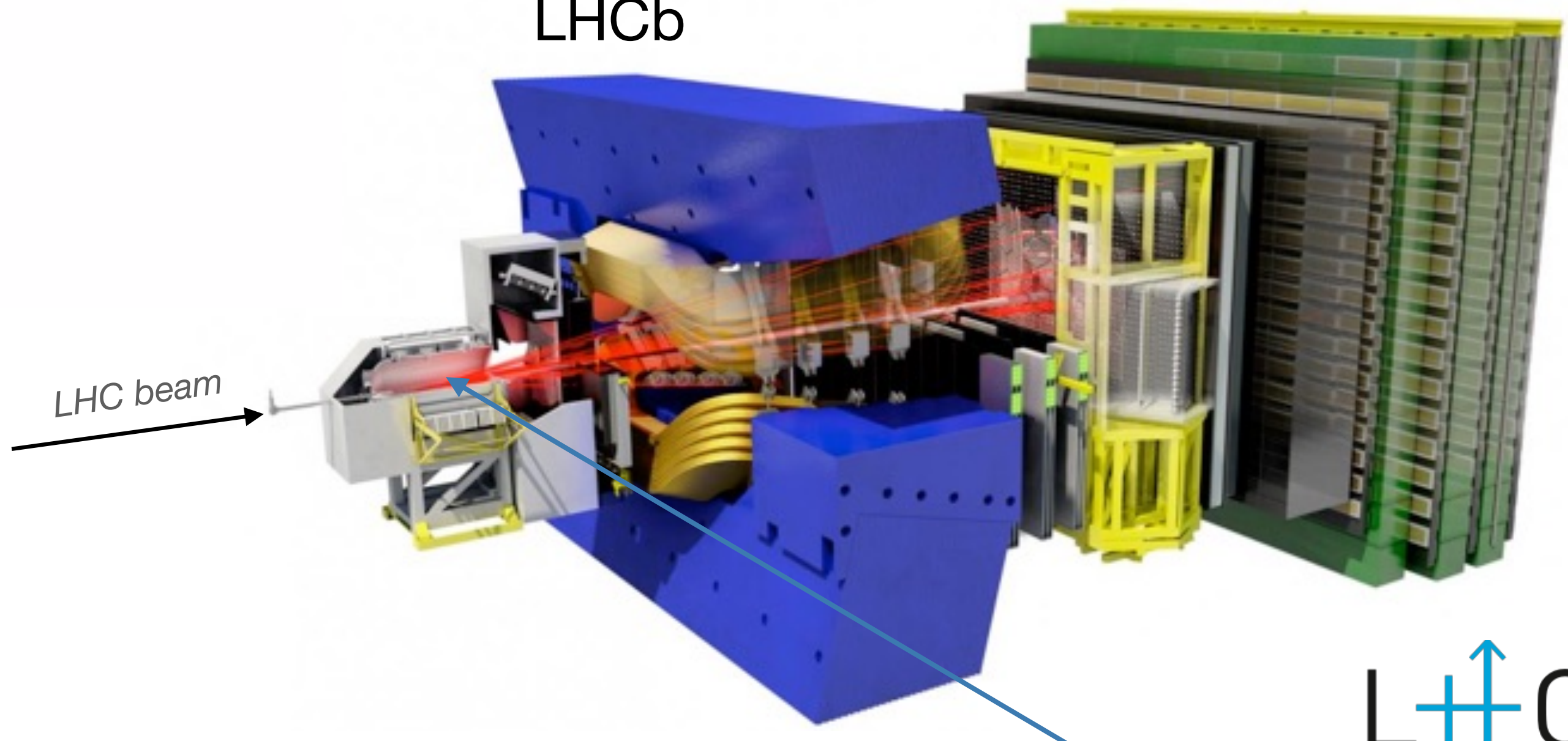


Future: LHCSpin

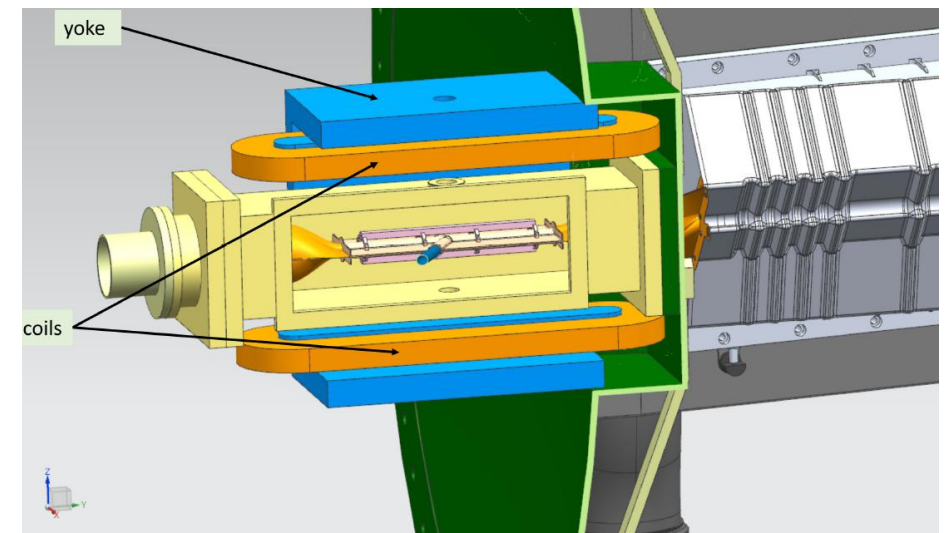
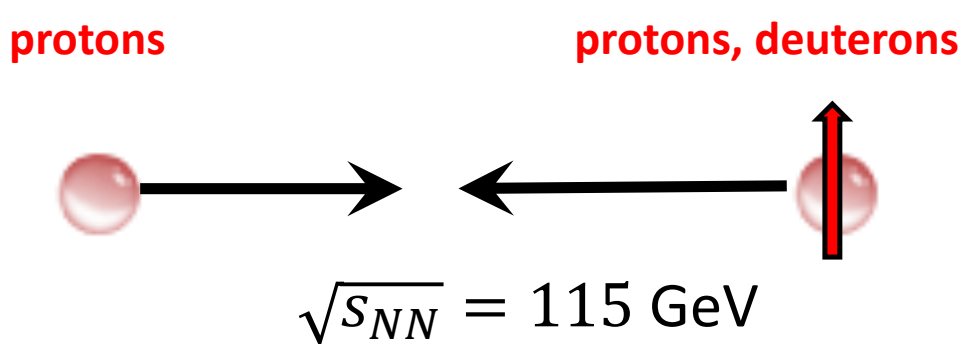


Future: LHCSpin

LHCb

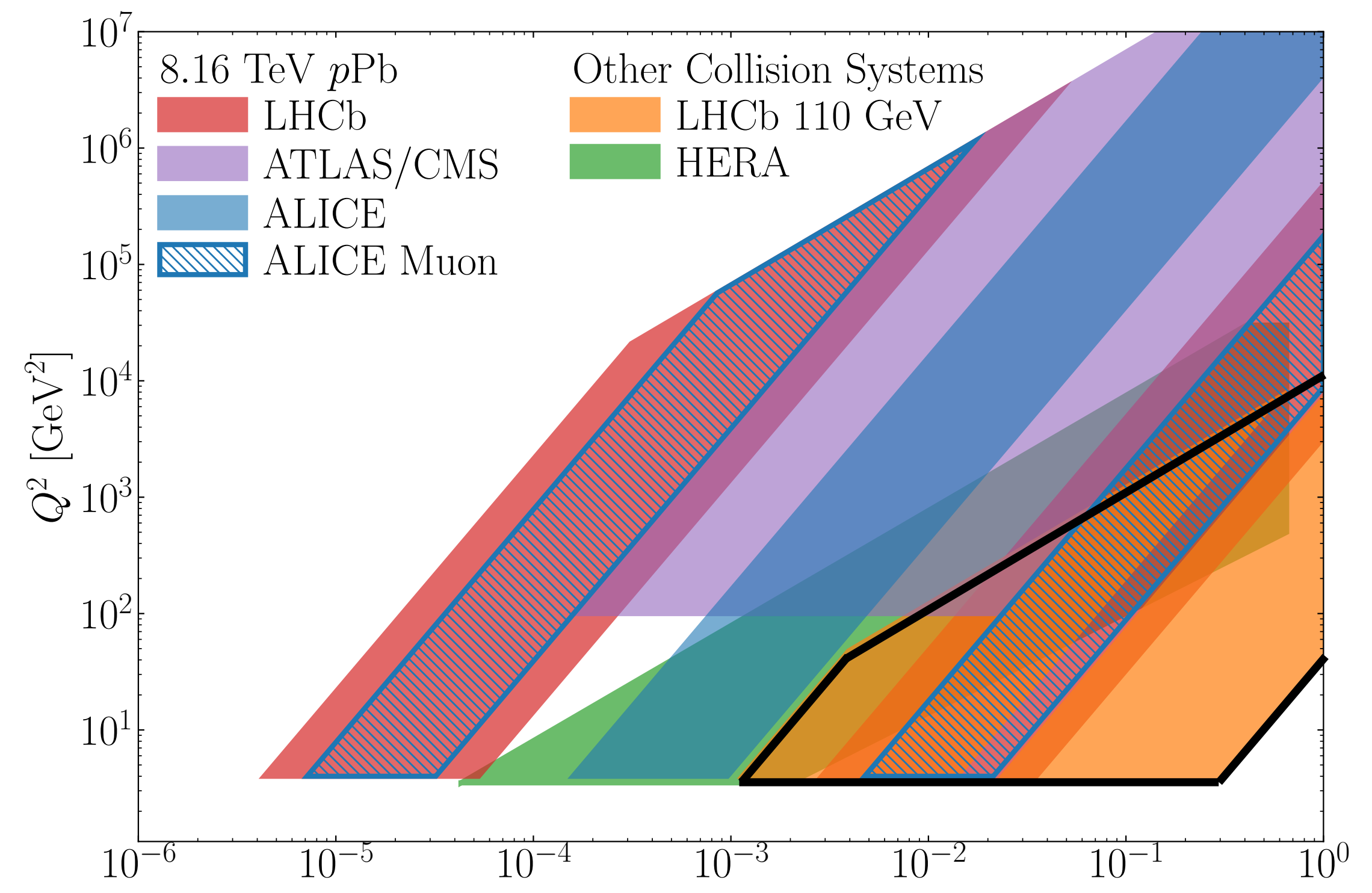
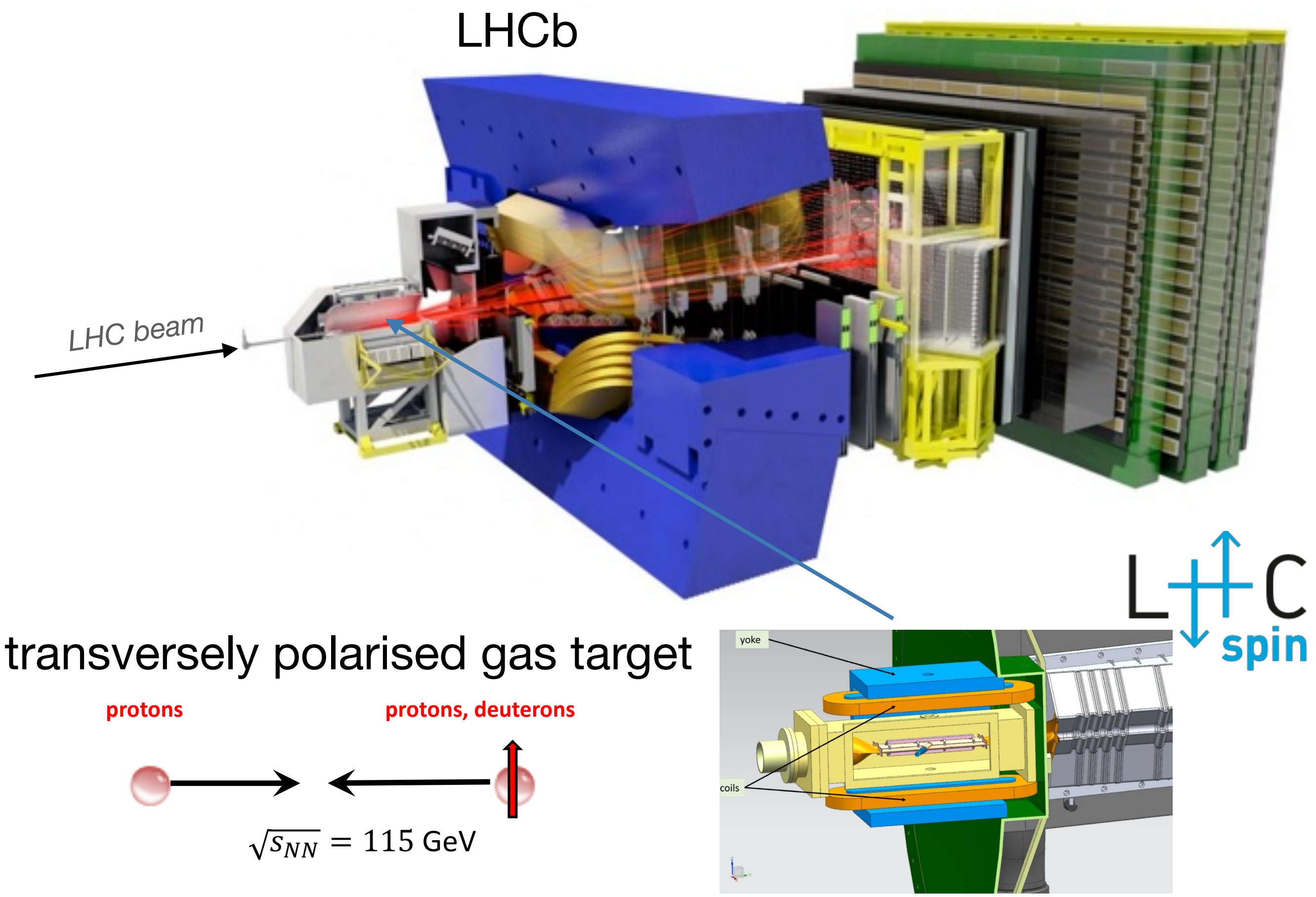


transversely polarised gas target



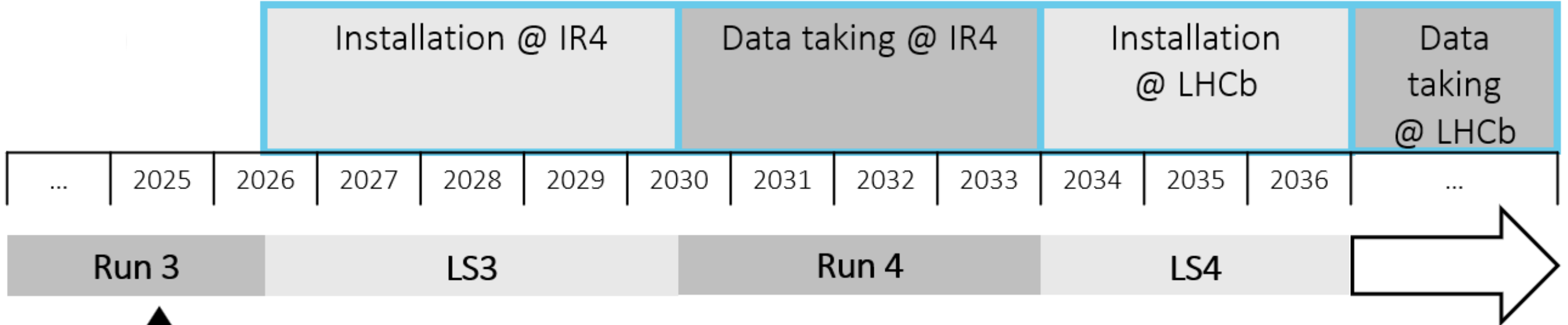
L C
↑ ↓
spin

Future: LHCSpin

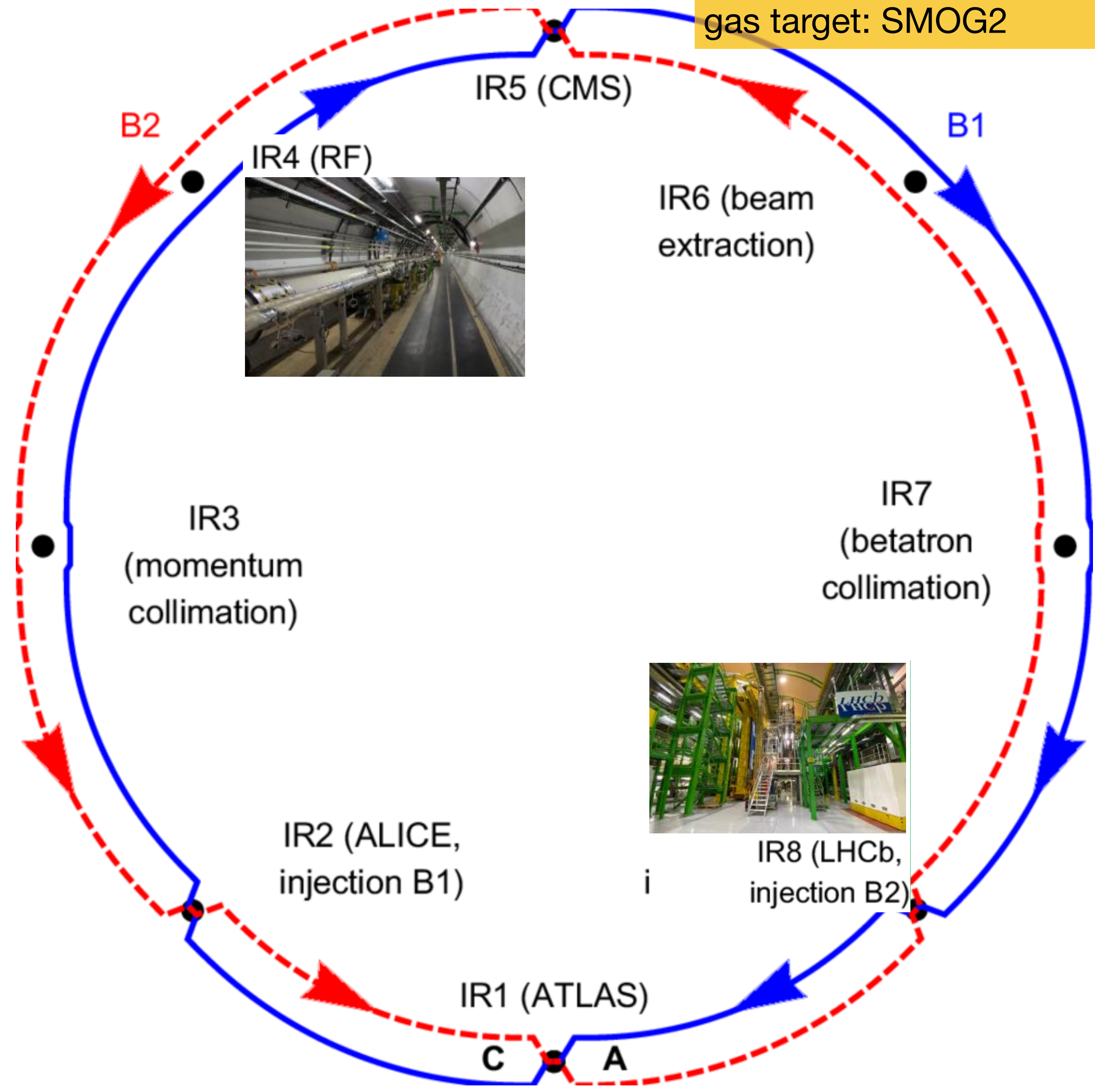


Study of quark and gluon TMDs in polarised proton, via Drell-Yan or quarkonium production at **high x**

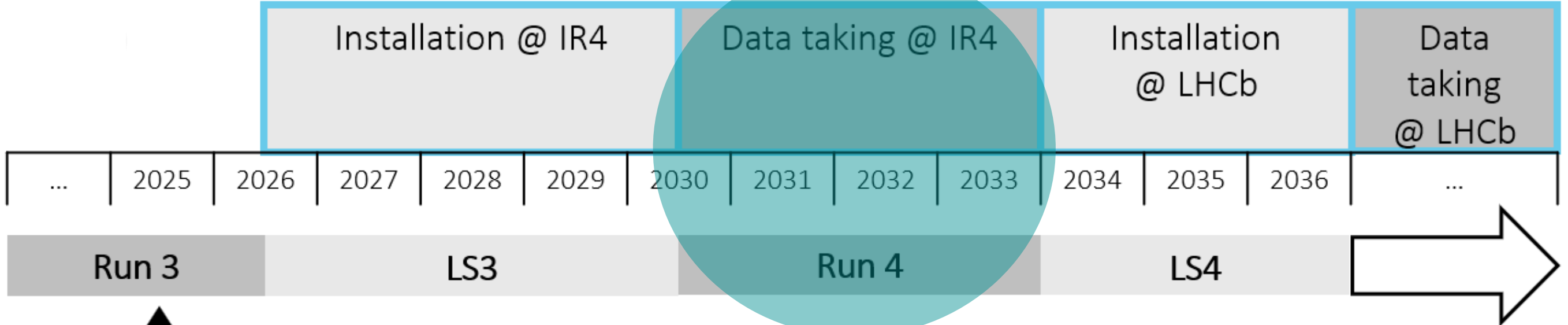
Future: LHCSpin



We are here: unpolarised gas target: SMOG2

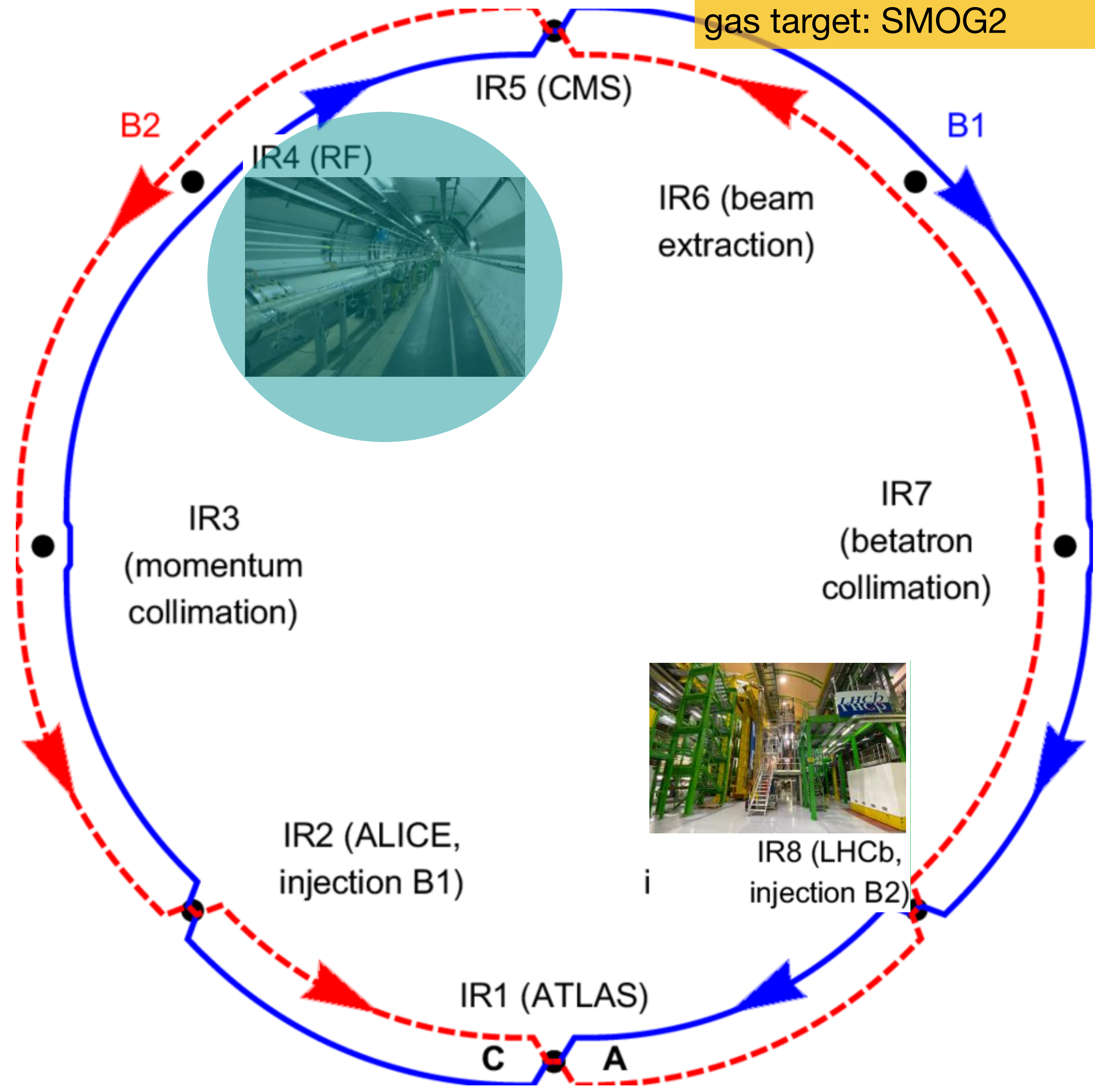


Future: LHCSpin

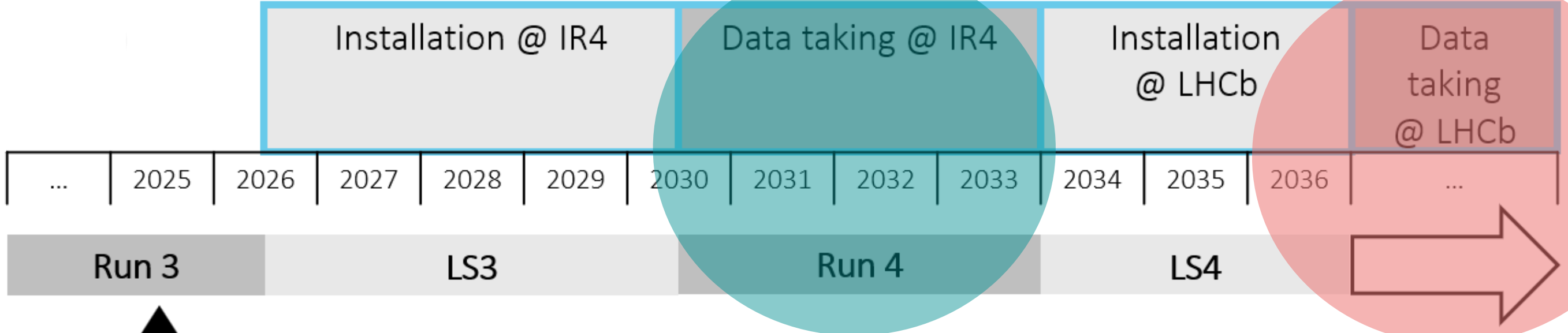


We are here: unpolarised gas target: SMOG2

phase I



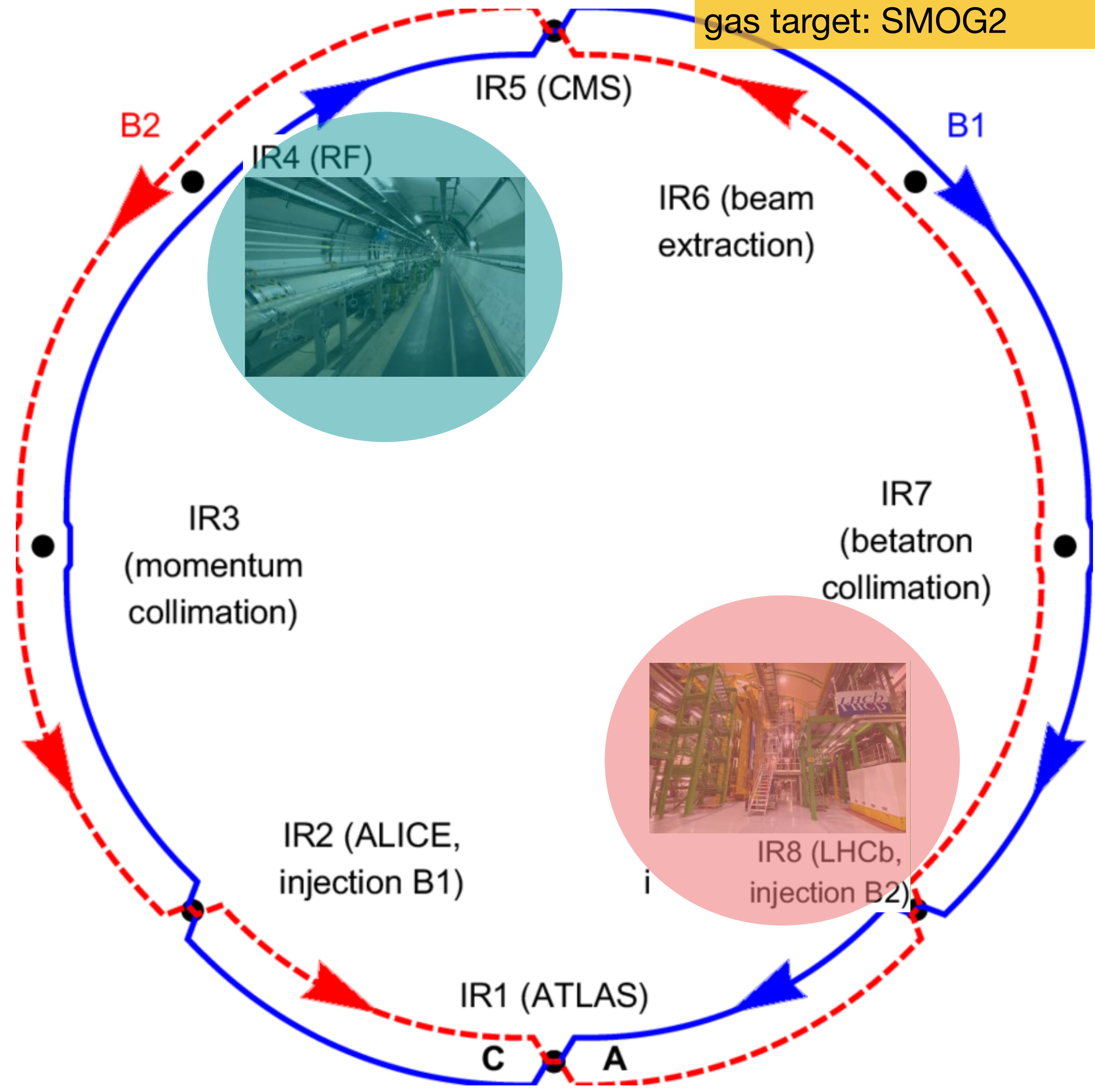
Future: LHCSpin



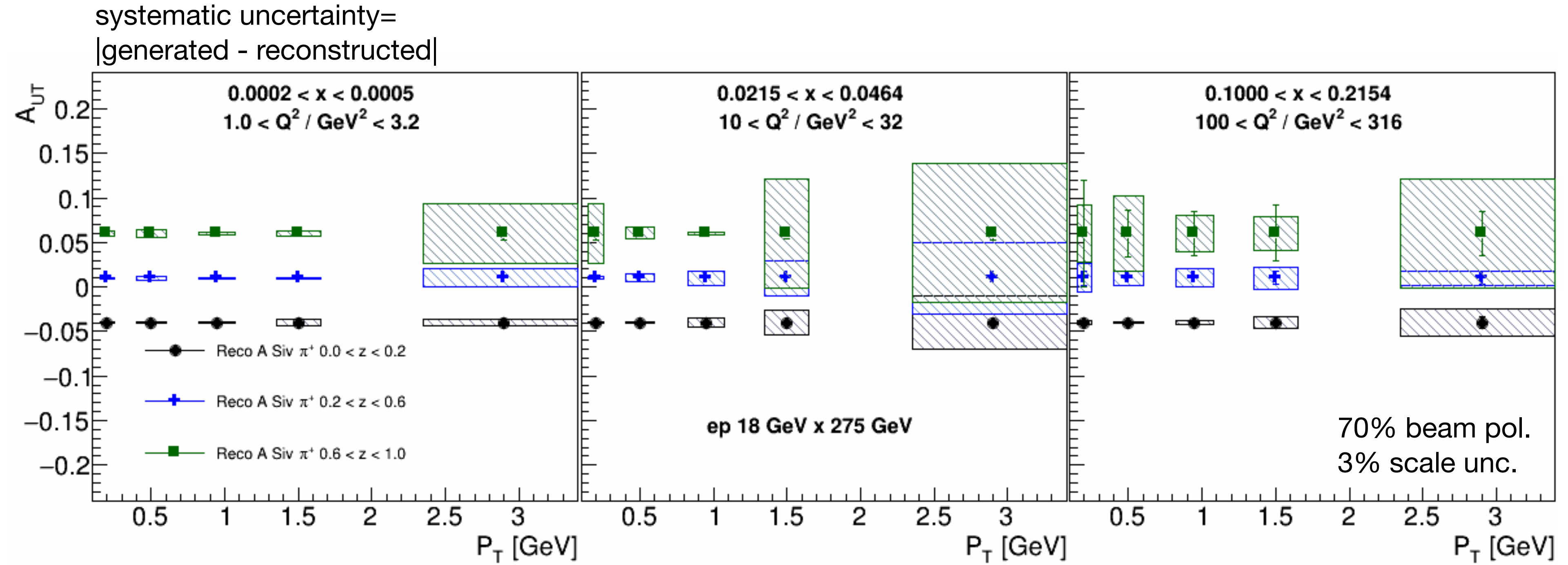
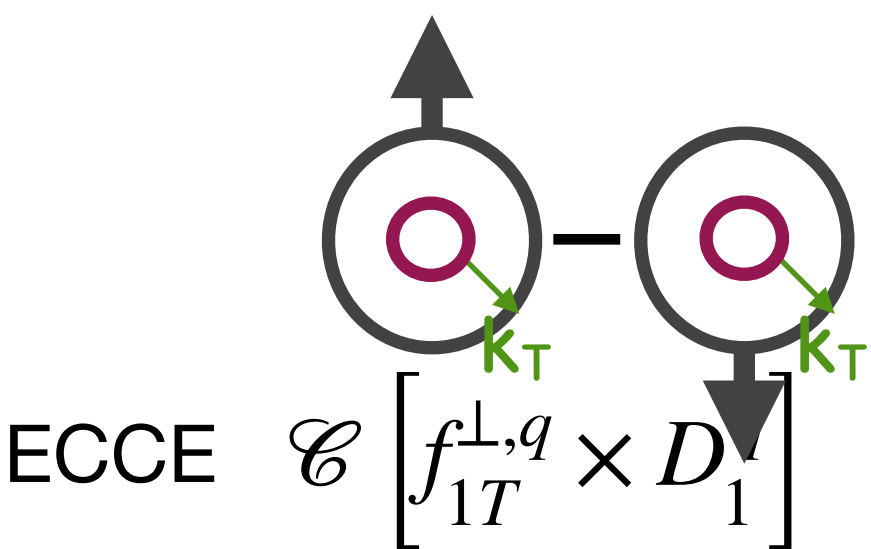
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phase I

phase II

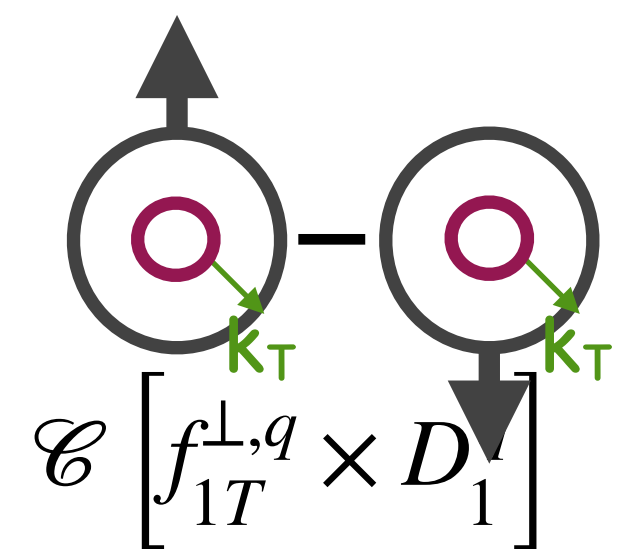


EIC: Sivers asymmetry

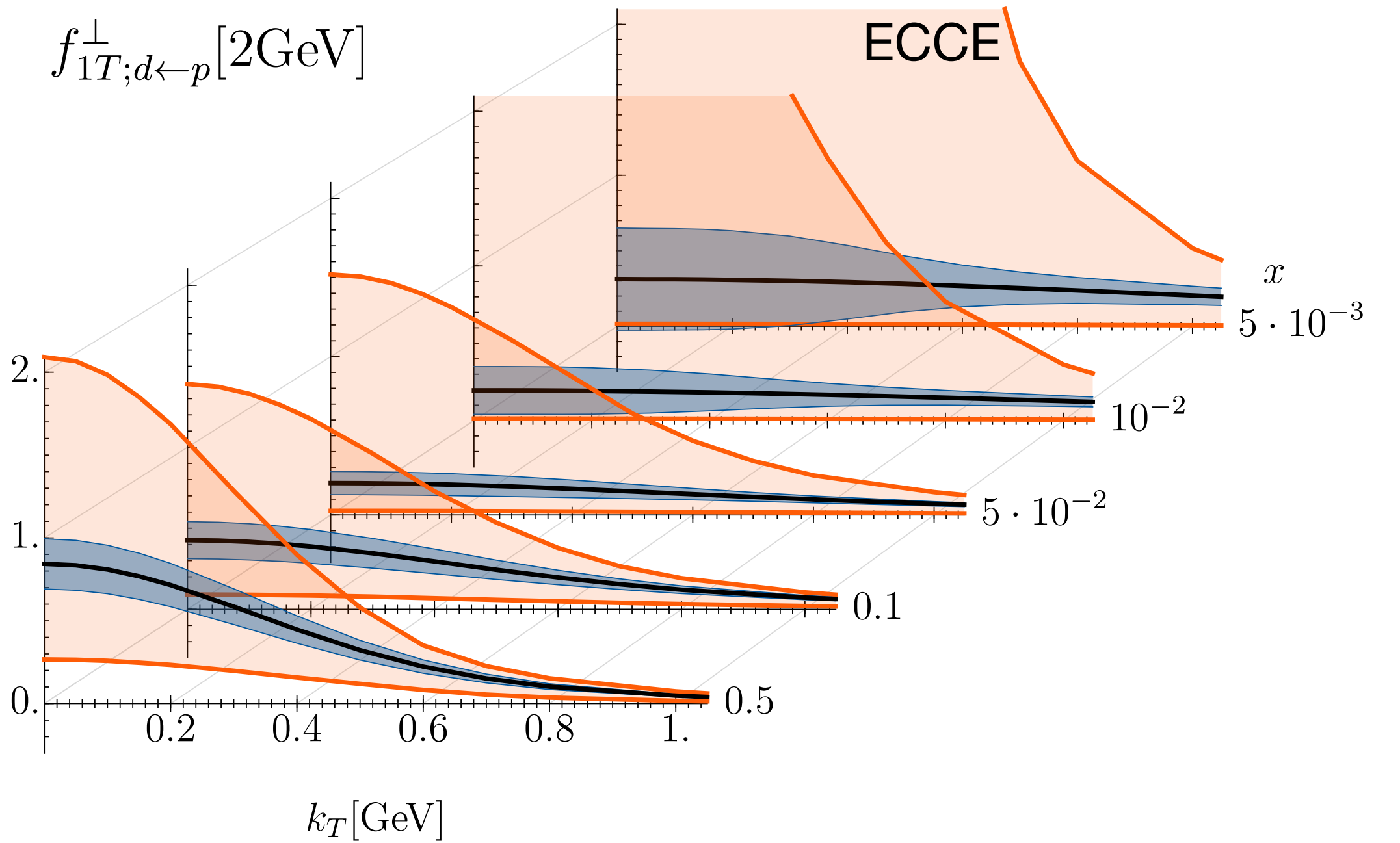
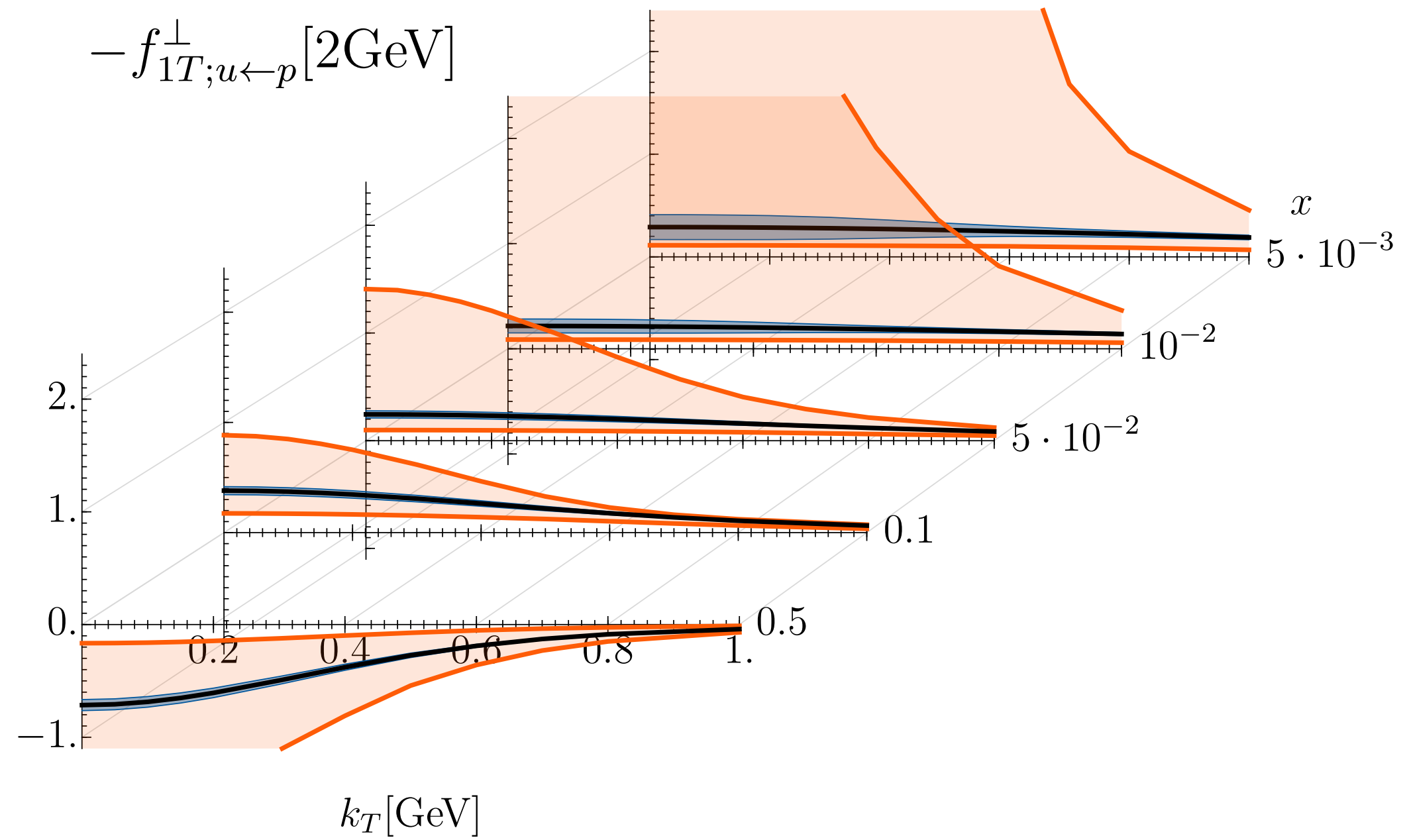


- Asymmetries at low x and low Q² well below 1% → need small uncertainties.
- Low x and Q²: small statistical uncertainty.
- For not too large z and P_T, statistical uncertainty well below 1%.
- Systematic uncertainties increase with z and P_T: likely because of higher smearing effects.

Sivers TMD: impact of the EIC



A. Vladimirov, R. Seidl et al., NIM A **1049** (2023) 168017
 Parametrisation from M. Bury et al., JHEP **05** (2021)151



DIS variables via scattered lepton

- $Q^2 > 1 \text{ GeV}^2$
- $0.01 < y < 0.95$
- $W^2 > 10 \text{ GeV}^2$
- $5 \times 41 \text{ GeV}^2$
- $10 \times 100 \text{ GeV}^2$
- $18 \times 100 \text{ GeV}^2$
- $18 \times 275 \text{ GeV}^2$

$\mathcal{L} = 10 \text{ fb}^{-1}$ for each collision energy