

Longitudinal Target-Spin Effects in SIDIS with CLAS12

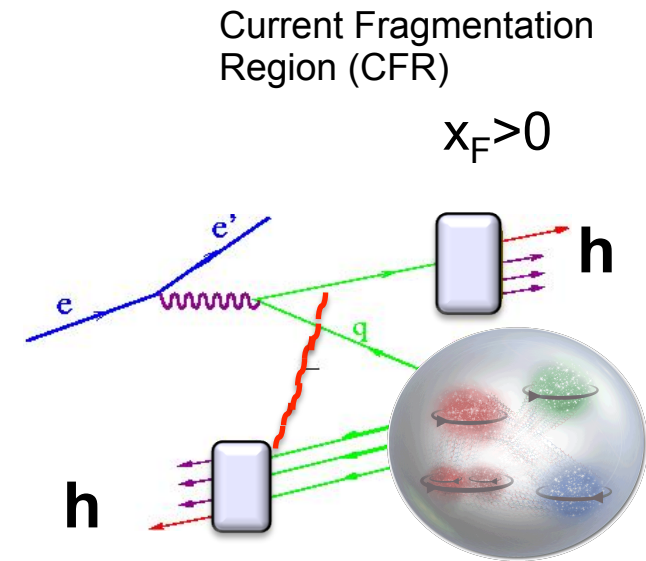
Tensor SIDIS workshop and b1/Azz Collaboration meeting

Harut Avakian (JLab)

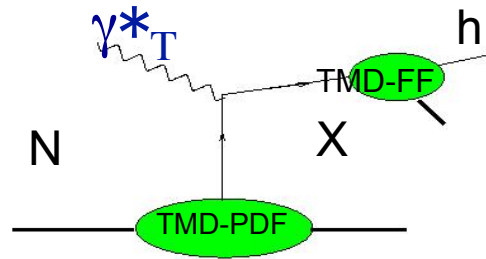
June 5, 2026

- Interconnections of Semi-Inclusive and Exclusive DIS
- Final states (π^0 , π^+ , $\pi^+\pi^-$, ...)
- What we can learn from longitudinal target measurements
- Dissecting SIDIS
- Evolution studies as validation test
- Comparing ALU with AUL
- Summary

3D PDFs: Electroproduction of hadrons



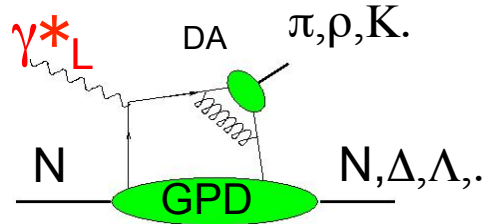
$x_F < 0$
Target Fragmentation Region (TFR)



Study

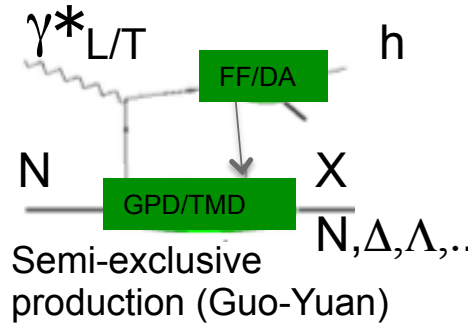
$x, Q^2, z, P_T, \phi, \phi_S \sim 1/Q^4$

Flavor and polarization dependence of transverse momentum distributions



$x, Q^2, t, \phi, \phi_S + \phi, \theta \sim 1/Q^6$

Flavor and polarization dependence of transverse space distributions



correlations and entanglement of CFR and TFR, controlling CFR, allowing access to GPDs and GTMDs

- Different non-perturbative objects may be involved with several independent variables involved
- Cross contributions make studies based on a given set of assumptions challenging

From electron cross sections to $\gamma^*p \rightarrow hX$

hep-ph/0611265

$$\frac{d\sigma}{dx_B dQ^2 d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{x_B Q^4} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left[F_{UU,T} + \varepsilon F_{UU,L} + \dots \right]$$

subprocess $\gamma^* N \rightarrow hX$

helicity structure functions

$$F_{mn}^{ij}(x_B, Q^2, z, P_{h\perp}^2) = \frac{Q^2(1-x)}{4\pi^3\alpha} \left(1 + \frac{\gamma^2}{2x_B}\right)^{-1} \frac{d\sigma_{mn}^{ij}}{dz dP_{h\perp}^2}$$

$$F_{UU,T} = \frac{1}{2}(F_{++}^{++} + F_{++}^{--}),$$

$$F_{UU,L} = F_{00}^{++},$$

(v+M)/v

hep-ph/0503023

$$\left[\frac{\alpha_{em}}{8\pi^3} \frac{y^2}{1-\varepsilon} \frac{1-x_B}{x_B} \frac{1}{Q^2} \right]^{-1} \frac{d\sigma}{dx_B dQ^2 d\phi d\psi} \left[\frac{1}{2}(\sigma_{++}^{++} + \sigma_{++}^{--}) + \varepsilon\sigma_{00}^{++} - \varepsilon \cos(2\phi) + \dots \right]$$

$$\sigma_T = \frac{1}{2}(\sigma_{++}^{++} + \sigma_{++}^{--}), \quad \sigma_L = \sigma_{00}^{++}$$

$$\Gamma = \frac{4\pi^3\alpha_{em}}{Q^2} \frac{x_B}{1-x_B} \frac{1}{2} \left[\frac{d\sigma_{++}^{++}}{dz dP_{hT}^2} + \frac{d\sigma_{++}^{--}}{dz dP_{hT}^2} \right] = \Gamma \mathcal{F}[f_1 D_1] \quad \leftarrow Q^2\text{-dependence in evolution}$$

What happens to Q^2 -dependences of $F_{UU,T}$ and $F_{UU,L}$ in exclusive limit of $z \rightarrow 1$?

Exclusive limit of SIDIS cross sections $ep \rightarrow e'hX$

hep-ph/0611265

$$\frac{d\sigma}{dx_B dQ^2 d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{x_B Q^4} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left[F_{UU,T} + \epsilon F_{UU,L} + \dots \right]$$

subprocess $\gamma^* N \rightarrow hX$

helicity structure functions

$$F_{mn}^{ij}(x_B, Q^2, z, P_{h\perp}^2) = \frac{Q^2(1-x)}{4\pi^3\alpha} \left(1 + \frac{\gamma^2}{2x_B}\right)^{-1} \frac{d\sigma_{mn}^{ij}}{dz dP_{h\perp}^2}, \quad \begin{aligned} F_{UU,T} &= \frac{1}{2}(F_{++}^{++} + F_{++}^{--}), \\ F_{UU,L} &= F_{00}^{++}, \end{aligned}$$

hep-ph/050617

$$z = 1 + \frac{x_B(M_P^2 - M_X^2)}{Q^2} + x_B t / Q^2 \quad \rightarrow \quad z_{\text{excl}} = 1 + \frac{x_B t}{Q^2}$$

$$\frac{d\sigma}{dx_B dQ^2 d\psi dt d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{Q^6} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left[F_{UU,T} + \epsilon F_{UU,L} + \dots \right]$$

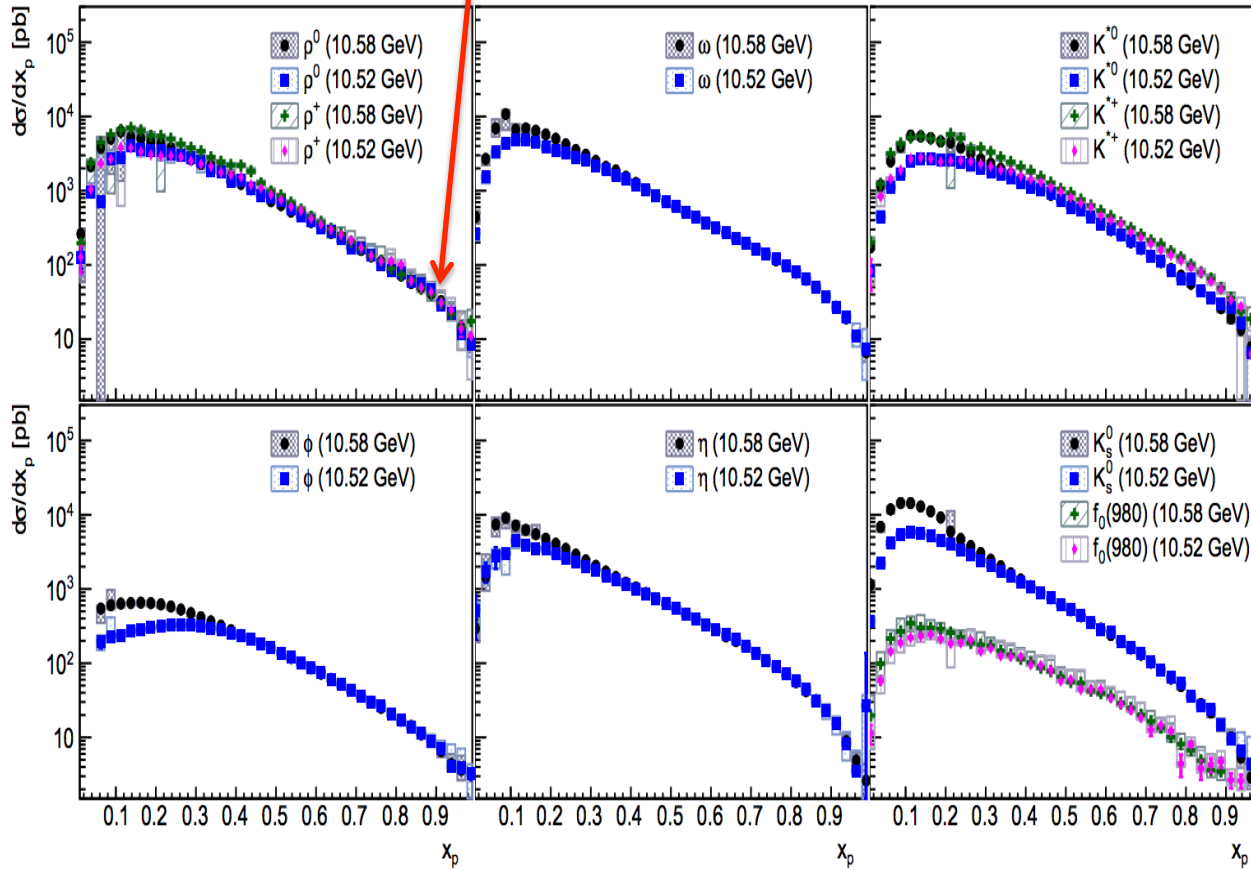
$$\frac{d\sigma}{dP_T^2} \propto \exp\left(-\frac{P_T^2}{2\sigma^2}\right) \quad \text{small } t \rightarrow \quad \frac{d\sigma}{d|t|} \propto (1-x_B) \exp\left[-\frac{(1-x_B)|t|}{2\sigma^2}\right]$$

exponential fall consistent with exclusive production

cross sections in the $z \rightarrow 1$ limit from e^+e^-

2411.12216

what is the $z^\alpha (1-z)^\beta$



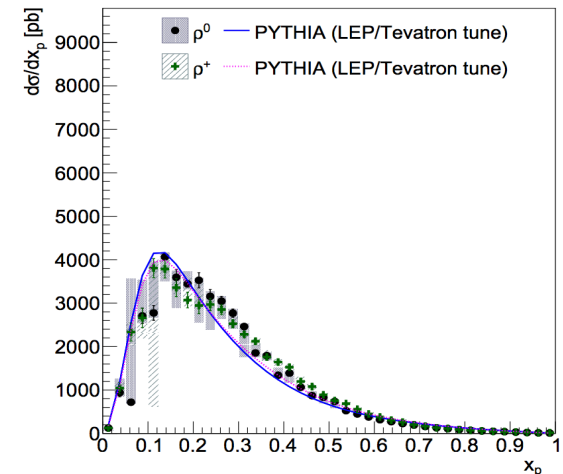
hadron momentum in e^+e^- CM

$$x_p = \frac{2|\vec{p}_h|}{\sqrt{s}} \quad z_h = \frac{E_h}{\nu}$$

$$z_p = \frac{\text{hadron light-cone momentum}}{\text{fragmenting parton light-cone momentum}}$$

$$z_h \approx z_p \left[1 + \frac{M_h^2 + P_T^2}{z_p^2 Q^2} \right]^{-1}$$

$$z_p \approx \frac{1}{2} \left[x_p + \sqrt{x_p^2 + \frac{4m_h^2}{s}} \right]$$



slightly more rho+!

Belle: production cross sections as a function of x_p

Can we use FFs in $z \rightarrow 1$ limit to estimate the σ_T ?

Theory-Experiment Dialogue

$$\frac{d\sigma^{lN \rightarrow l' h X}}{dx_B dQ^2 dz dP_{h\perp}^2 d\phi_h} = \frac{\pi\alpha^2 y}{x_B y Q^2 (1-\epsilon)} [F_{UU,T} + \dots]$$

$$\left. \begin{array}{l} lN \rightarrow l' \pi^+ X \\ lN \rightarrow l' \rho^0 X \\ \dots \end{array} \right\} lN \rightarrow l' \pi^+ X$$

Fragmentation Function
 → probability to produce π^+

$$F_{XY}^h(x, z, P_T, Q^2) \propto \sum H^q \times f^q(x, k_T, \dots) \otimes D^{q \rightarrow h}(z, p_T, \dots) + Y(Q^2, P_T) + \mathcal{O}(M/Q)$$

$$\gamma_{Tp}^* \rightarrow \pi^+ X(\pi^+ n, \pi^+ \Delta, \pi^+ \pi^- p, \pi^+ \pi^0 \pi^- \dots)$$

.....

$$\gamma_{Lp}^* \rightarrow \pi^+ X(\pi^+ n, \pi^+ \Delta, p\rho^0, \pi^+ \pi^0 \pi^- \dots)$$

experiment

$$\gamma_{Lp}^* \rightarrow p\rho_L^0 \rightarrow \text{most significant}$$

→ increases at higher energies

What type of exclusive processes should we cut out from experiment to have an adequate comparison with theory which doesn't have longitudinal photon contributions?

Observables with longitudinally pol. target

$$\sigma^{\lambda\Lambda} = \sigma_{UU} + \lambda\sigma_{LU} \sin \phi + \Lambda\sigma_{LU} \sin \phi + \lambda\Lambda(\sigma_{LL} + \sigma_{LL}^{\cos} \cos \phi)$$

λ and $\Lambda \rightarrow$ helicities of e- and proton (normalizing lumi of positive and negative targets)

$N^{++}+N^{-+}$ = sum of events (with +/- helicities of e-) for positive target polarization

$N^{+-}+N^{-}$ = sum of events (with +/- helicities of e-) for negative target polarization

$N^{++}+N^{+-}$ = sum of events (with +/- helicities of p) for positive e- helicity

$N^{+-}+N^{-}$ = sum of events (with +/- helicities of p) for negative e- helicity

Observables

beam SSA $(N^{++} + N^{+-} - N^{+-} - N^{-}) / (N^{++} + N^{+-} + N^{+-} + N^{-}) = (a_{lu} \sin \phi) / (1 + b_{uu} \cos \phi)$

use the $(1 + b_{uu} \cos \phi)$ containing cos from acceptance and Cahn for others

target SSA

$(N^{++} + N^{+-} - N^{+-} - N^{-}) / (N^{++} + N^{+-} + N^{+-} + N^{-}) = (a_{ul} \sin \phi + b_{ul} \sin 2\phi) / (1 + b_{uu} \cos \phi)$

Target double spin asymmetries

1) $(N^{++} - N^{+-}) / (N^{++} + N^{+-}) = (a_{ul} \sin \phi + b_{ul} \sin 2\phi + a_{LL} + b_{LL} \cos \phi) / (1 + b_{uu} \cos \phi)$

2) $(N^{-} - N^{+-}) / (N^{-} + N^{+-}) = (-a_{ul} \sin \phi - b_{ul} \sin 2\phi + a_{LL} + b_{LL} \cos \phi) / (1 + b_{uu} \cos \phi)$

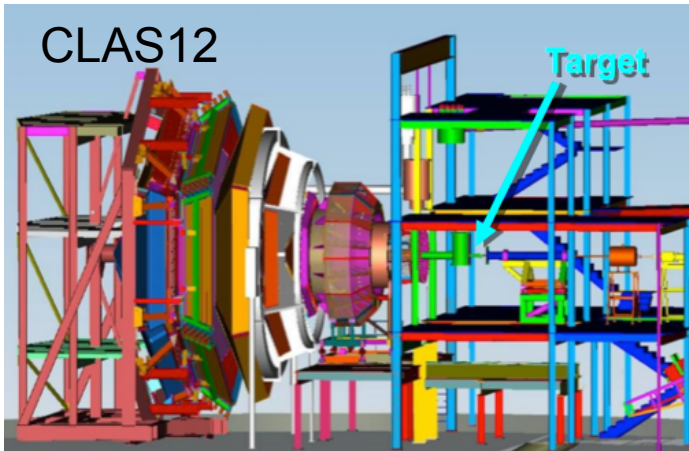
use the same helicity

1) $(N^{++} - N^{+-}) / (N^{++} + N^{+-}) = (a_{lu} \sin \phi + a_{LL} + b_{LL} \cos \phi) / (1 + b_{uu} \cos \phi)$

2) $(N^{-} - N^{+-}) / (N^{-} + N^{+-}) = (-a_{lu} \sin \phi + a_{LL} + b_{LL} \cos \phi) / (1 + b_{uu} \cos \phi)$

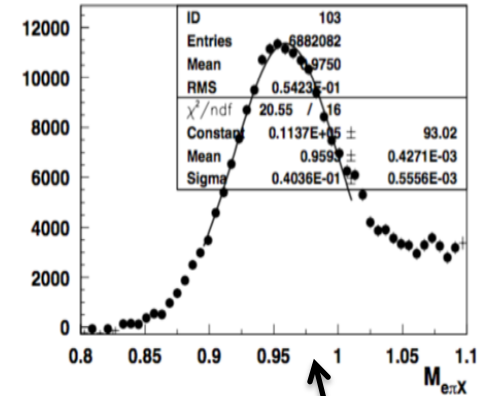
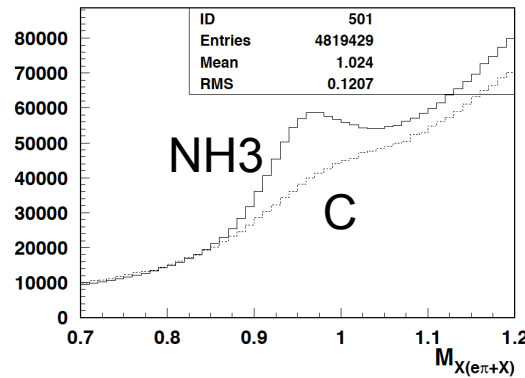
Longitudinally polarized target offers several observables critical for test

CLAS12 RGC experiment with longitudinally polarized target

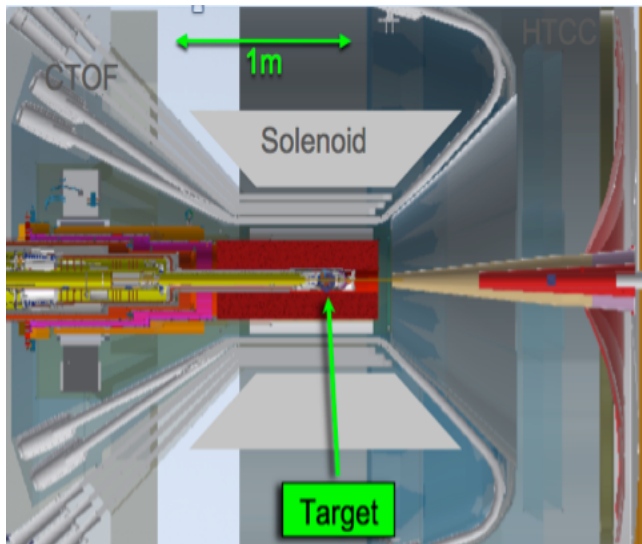


E12-06-109, E12-06-119, E12-07-107, E12-09-009

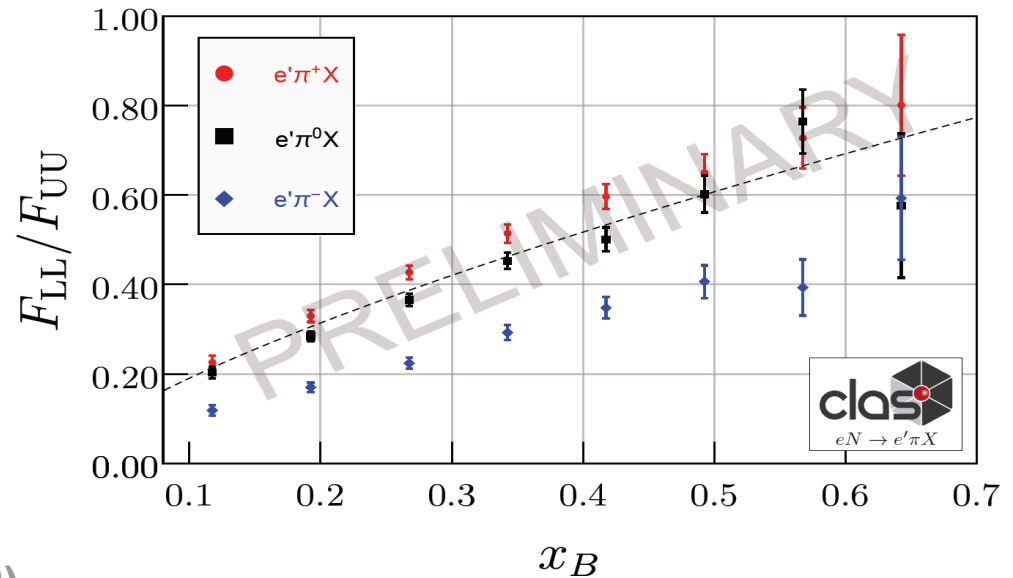
Electroproduction on longitudinally polarized NH₃ and ND₃



Subtracting carbon data from NH₃ (nice neutron peak)

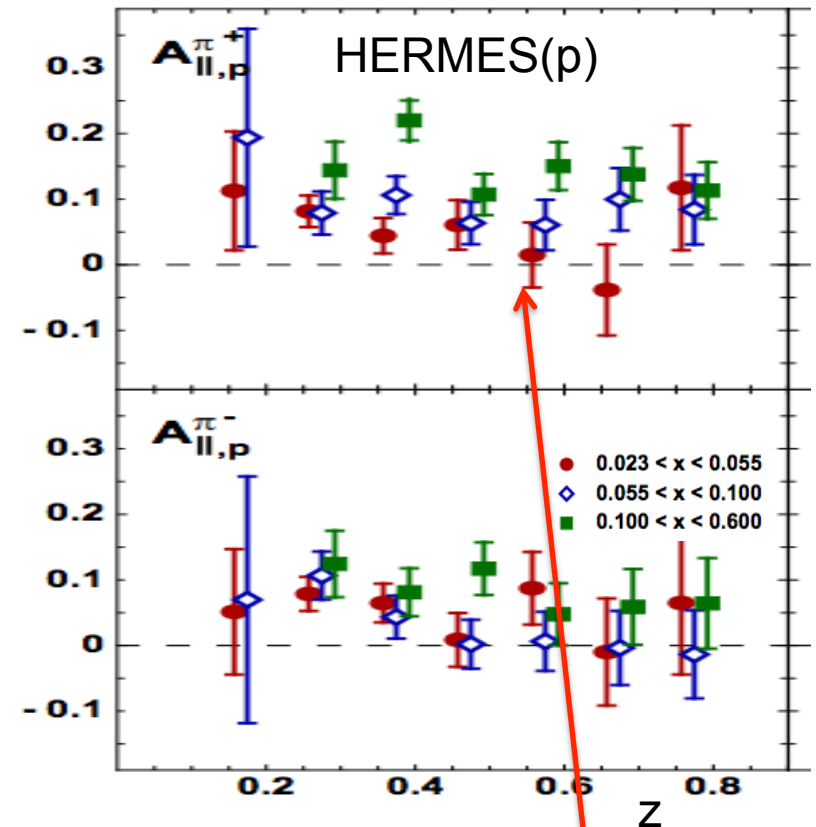
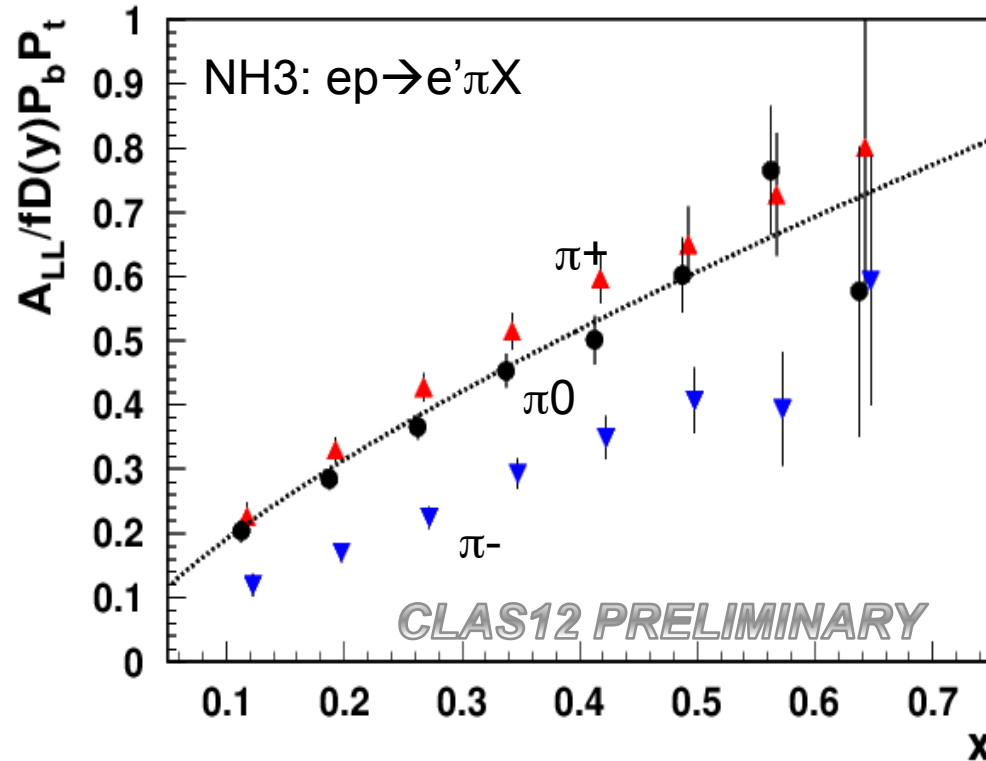


Dynamic Nuclear Polarization (DNP)



Single pion DSAs

1810.07054

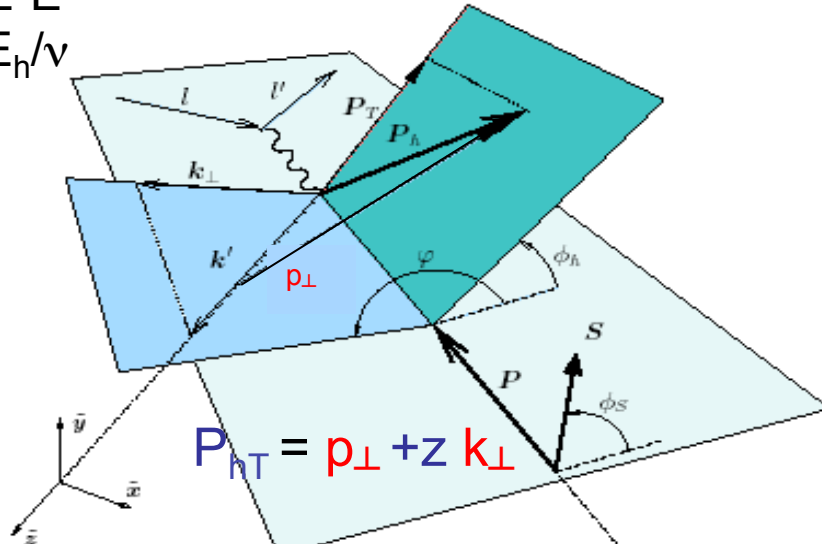


- Double spin asymmetries for $ep \rightarrow e\pi+X$ seem to decrease at large z and effect more significant at low x
- The $ep \rightarrow e\pi+X$ drops faster at low x than $ep \rightarrow e\pi^0X$ (consistent with DIS fit)
- Note: \rightarrow exclusive rho contributions more significant at large z and low x

DIS kinematical coverage and observables

$$v = E - E'$$

$$z = E_h / v$$



$$\frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2}$$

$$= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right.$$

$$+ \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} + S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \epsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right.$$

$$\left. \left. - S_L \lambda_e \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right] \right.$$

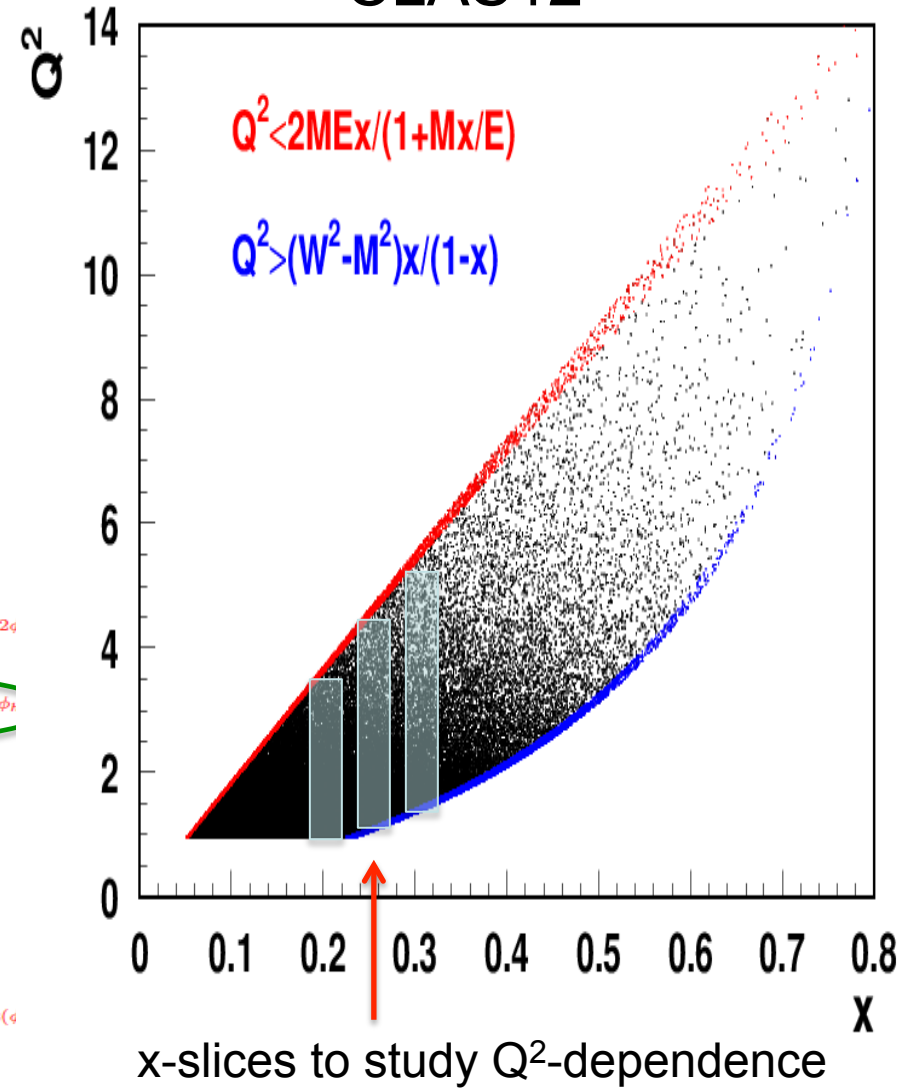
$$+ S_T \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \epsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \epsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right.$$

$$+ \epsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} + \sqrt{2\epsilon(1+\epsilon)} \sin \phi_S F_{UT}^{\sin \phi_S}$$

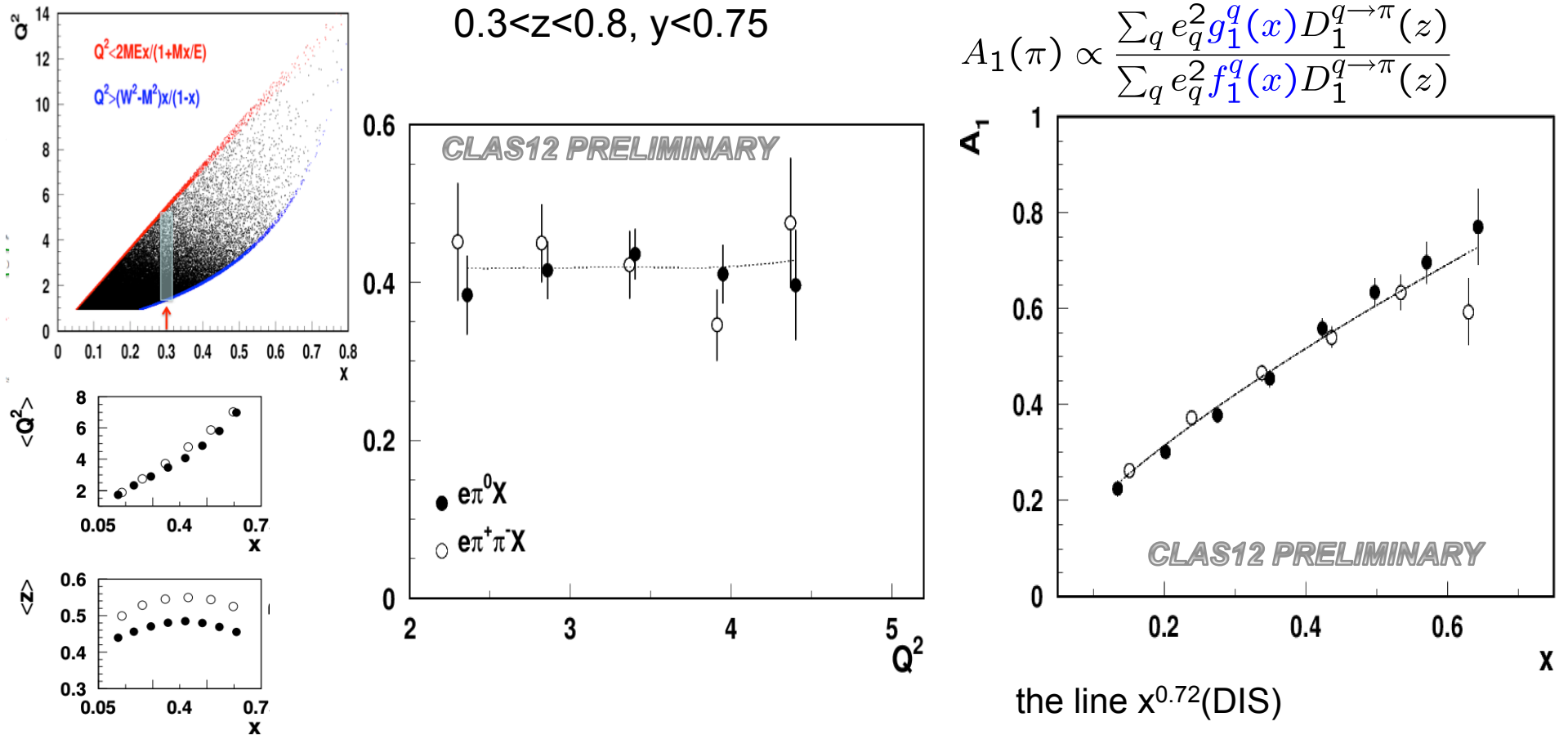
$$+ \left. \left. \left. \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] + S_T \lambda_e \left[\sqrt{1-\epsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right. \right.$$

$$\left. \left. \left. + \sqrt{2\epsilon(1-\epsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\}$$

CLAS12



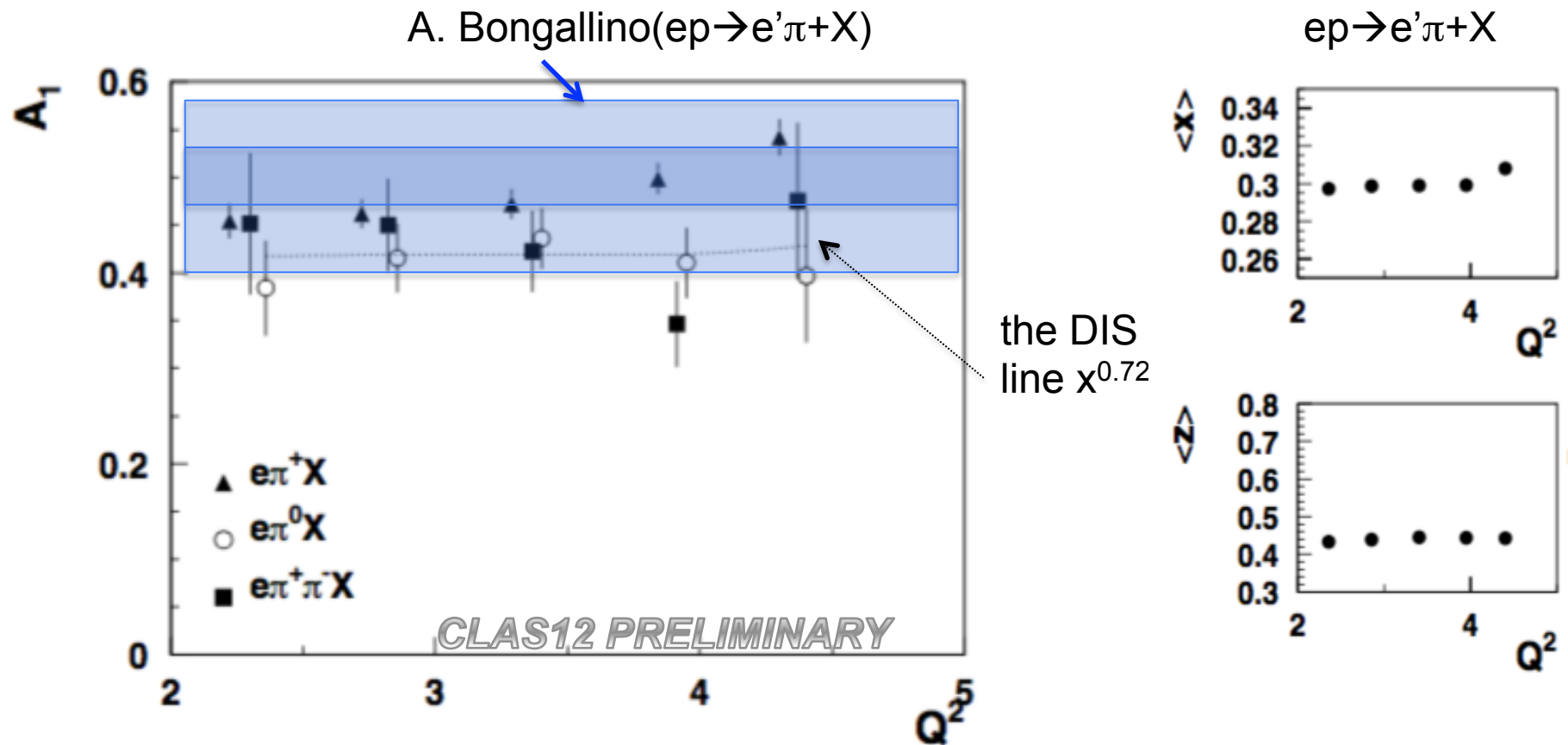
A_1 x-dependence for $ep \rightarrow e' \pi^0 X$ vs $ep \rightarrow e' \pi^+ \pi^- X$



- DSA extracted for $ep \rightarrow e' \pi^0 X$ (filled) and $ep \rightarrow e' \pi^+ \pi^- X$ for $0.3 < z < 0.8$ (empty circles) consistent
- No contributions from exclusive $ep \rightarrow e' \rho^0 X$
- Consistent with simple fit to world data (no major Q^2 -dependence)

DSAs: comparing different processes

$0.28 < x < 0.32$, $0.3 < z < 0.8$, $y < 0.75$

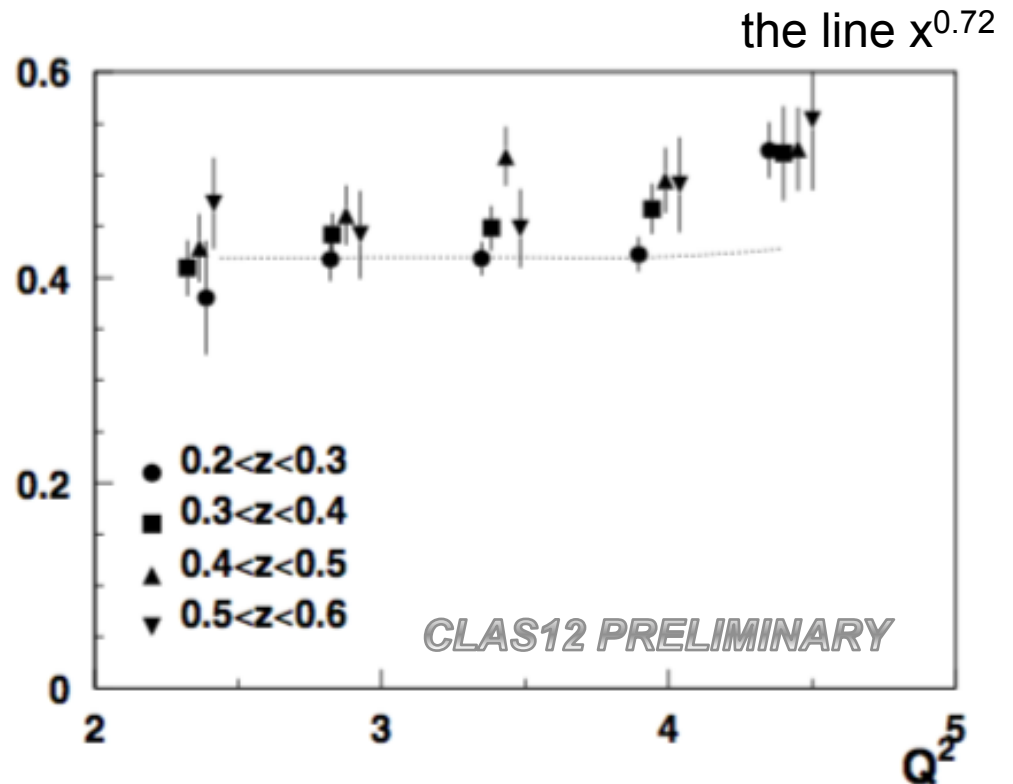
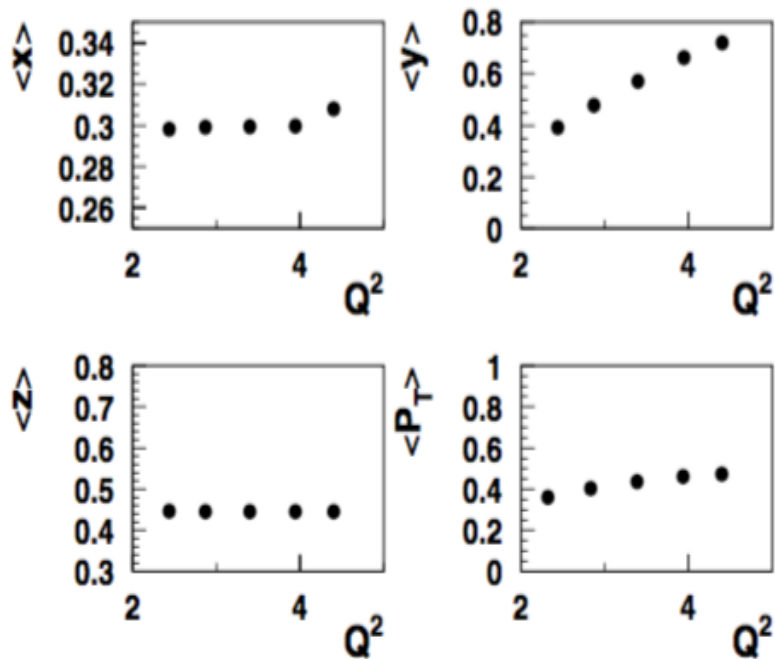


- DSA for $ep \rightarrow e'\pi + X$ vs $ep \rightarrow e'\pi^0 X$ and $ep \rightarrow e'\pi^-\pi^+ X$ consistent
- No major Q^2 -dependence apart from for $ep \rightarrow e'\pi + X$

DSAs: Q^2 -dependence in z -bins

$0.28 < x < 0.32, y < 0.75$

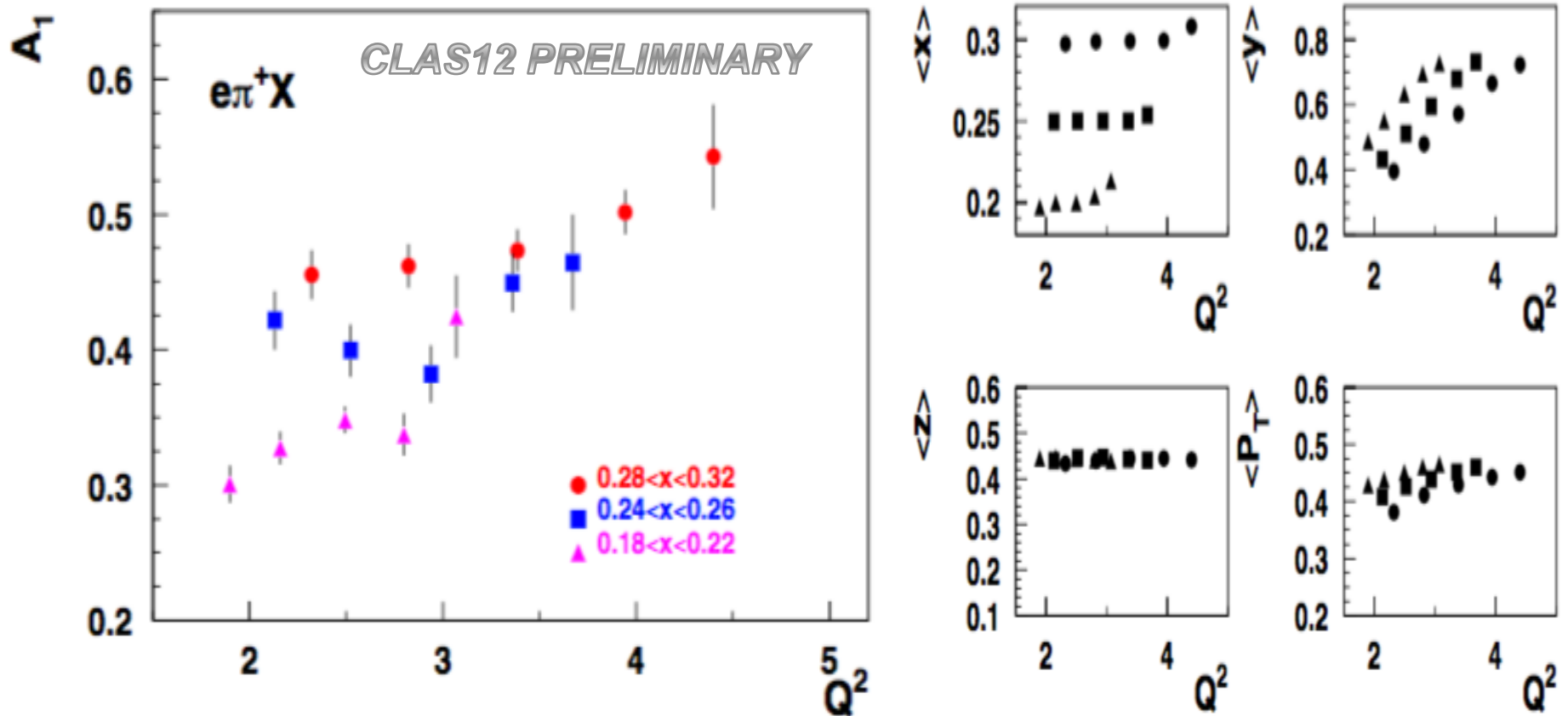
$ep \rightarrow e\pi + X$



- DSA for $ep \rightarrow e'\pi + X$ for z -bins
- Tendency to increase with Q^2 stays for bins in z

DSA $ep \rightarrow e' \pi^+ X$: more bins in x

$0.28 < x < 0.32$, $0.3 < z < 0.8$, $y < 0.75$

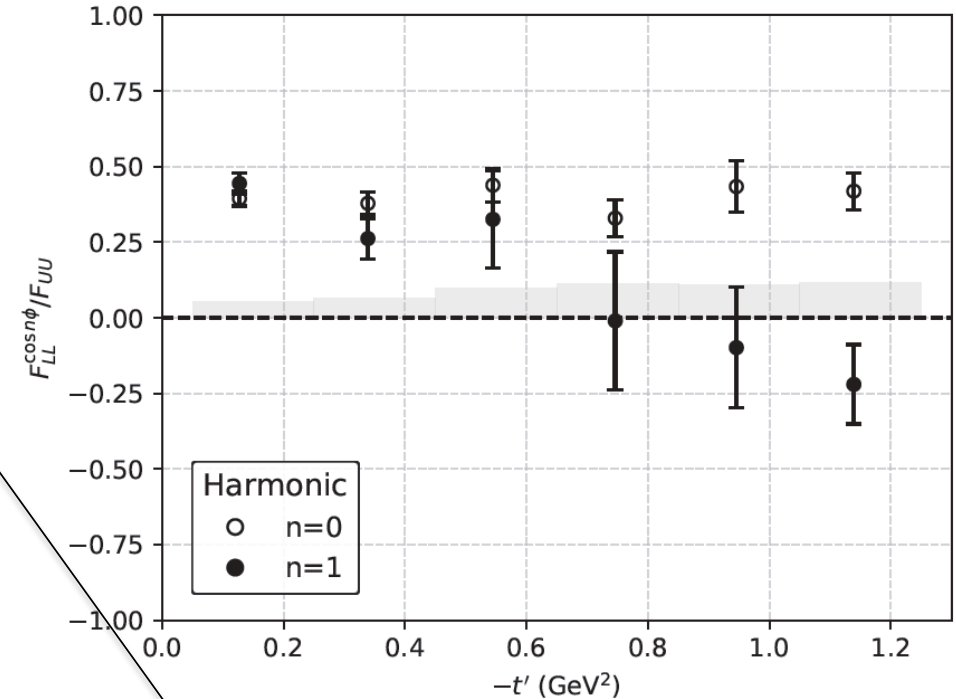
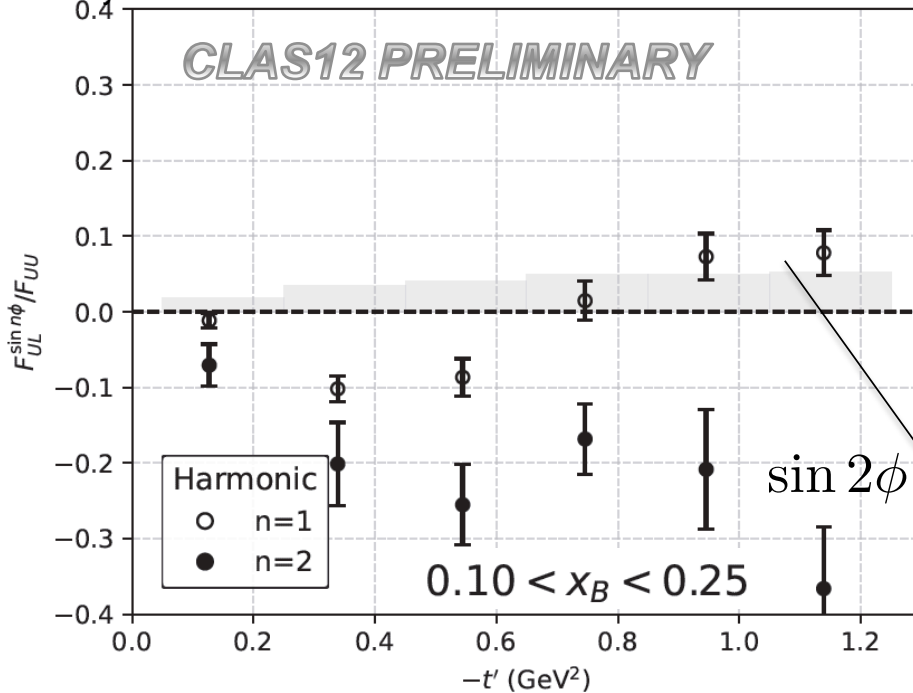


Inclusive (in progress) and π^+ samples may have significant contributions from longitudinal photons (VMs)

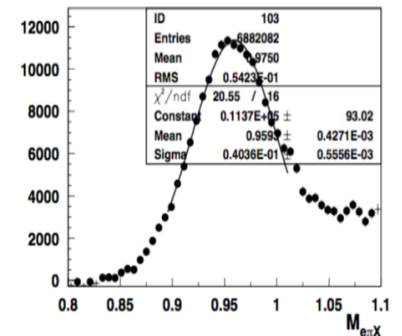
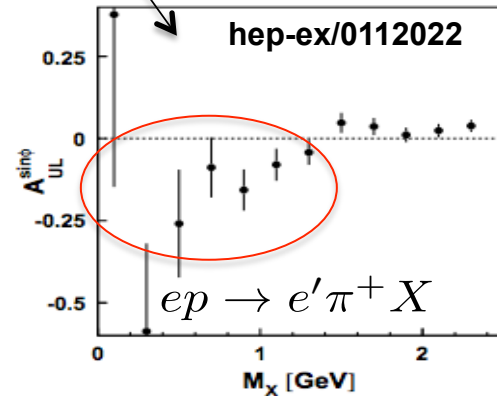
Behavior of the double spin asymmetry for π^+ is consistent with increase with Q^2

$ep \rightarrow e' \pi + X$: exclusive limit for SSA and DSA

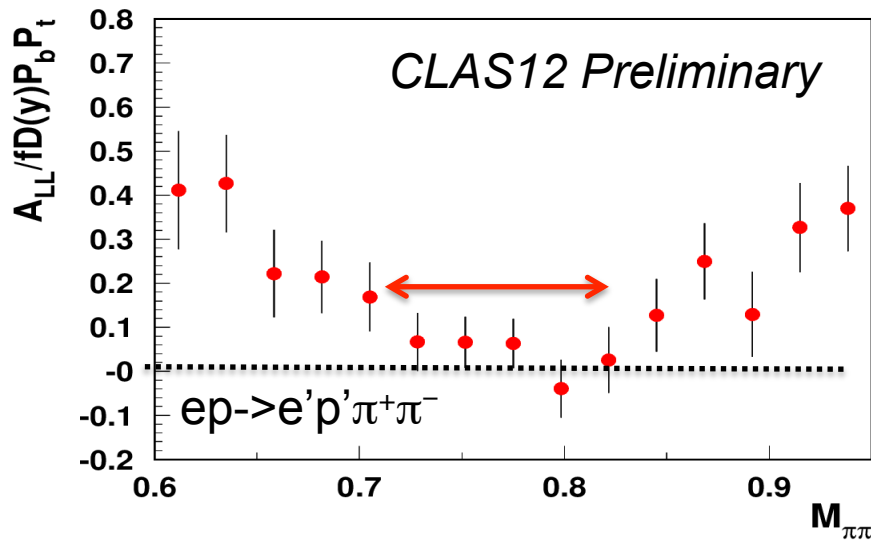
T. Hayward et al



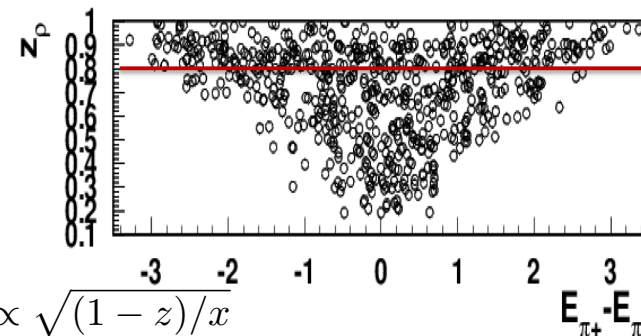
At low x (*low t*) CLAS12 observes negative $\langle \sin \phi \rangle$ consistent with HERMES
 The $\langle \sin 2\phi \rangle$ observed by CLAS12 may provide direct access to GTMDs
 (S. Bhattacharya et al hep-ph: 2312.01309)



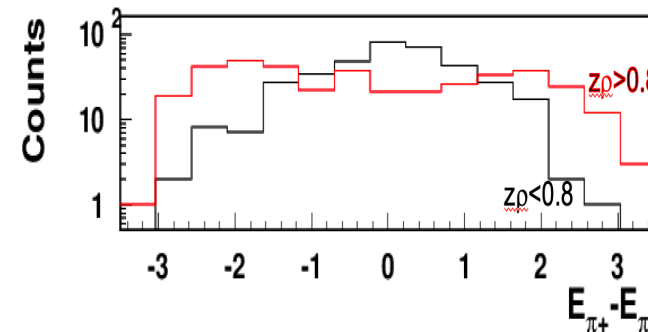
Studies of ρ^0 impact with longitudinally polarized NH_3 target



Polarization of rho



$$\gamma_T^* \rightarrow \rho_L \propto \sqrt{(1-z)/x}$$

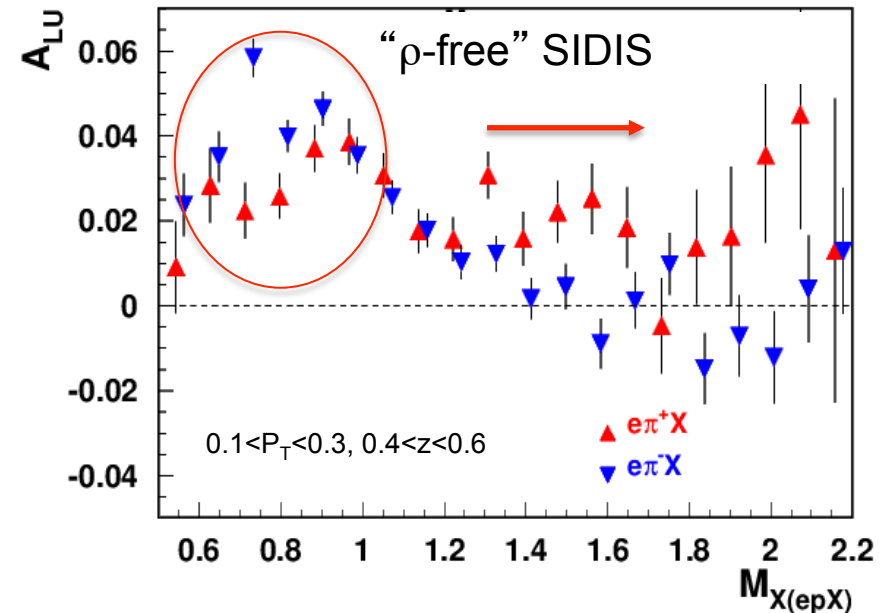
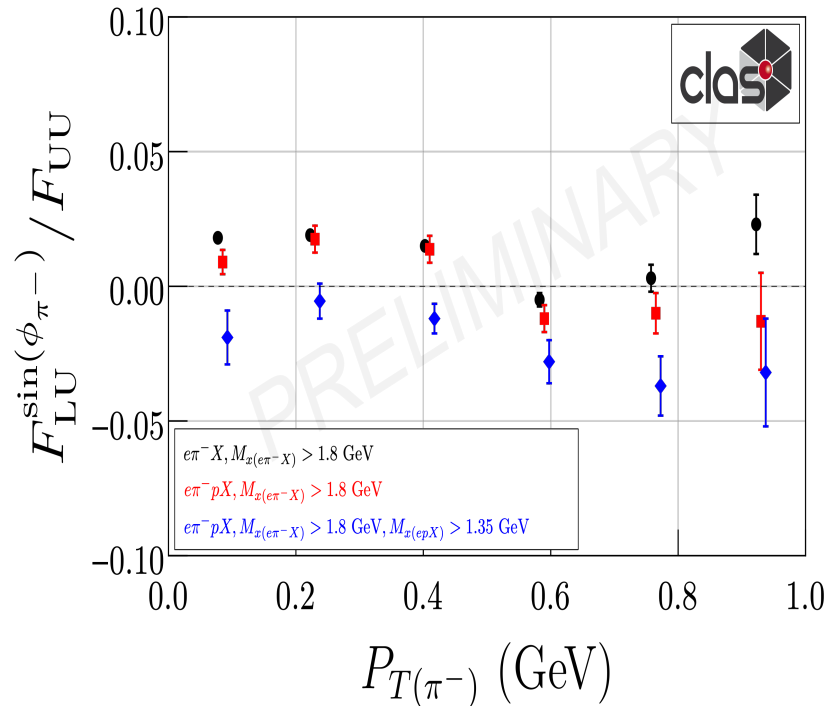


Need clear separation of hydrogen from NH_3 and “diffractive” exclusive ρ^0 s from exclusive $\pi^+\pi^-$

- DSA is P-even, SSA is P-odd
- longitudinal photon cross section is P-odd
 \rightarrow contribution appears only in the SSA, a P-odd observable, and does not appear in DSA (\rightarrow significant dilution in DSA)

At large z (small t) the shapes of distributions (getting asymmetric) clearly indicate dominance of longitudinal rho

Exclusive ρ contributions to π : P_T -dependence



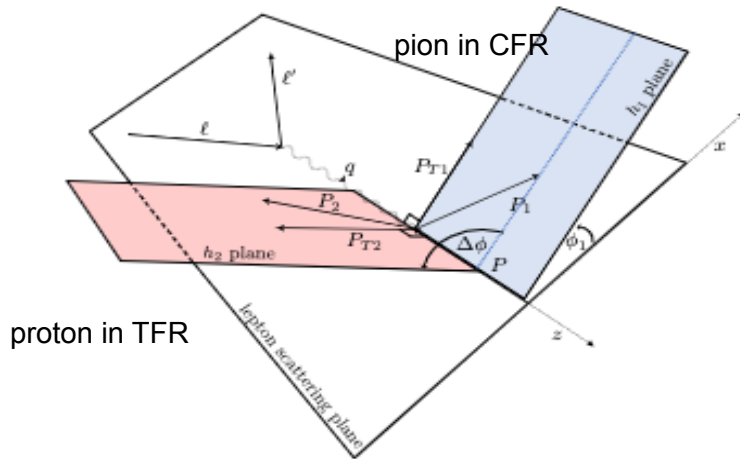
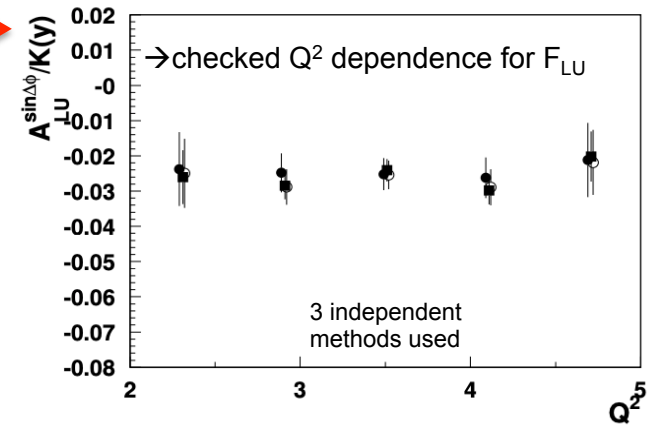
- Can change the pion SSAs, in particular at small P_T
- The same sign and size of π^+ and π^- SSA indicates the ρ^0 may not be properly subtracted (require detailed MC studies, which require proper SDMEs)
- While VM contributions are $\sim 20\%$ in multiplicities **in SSA they can be $>100\%$**
- Detection of the target proton introduces **much smaller bias on the inclusive charged pion SSA, than the exclusive ρ contributions**

Azimuthal modulations in B2B production

N/q	U	L	T
U	\hat{u}_1	$\hat{l}_1^{\perp h}$	$\hat{t}_1^h, \hat{t}_1^{\perp}$
L	$\hat{u}_{1L}^{\perp h}$	\hat{l}_{1L}	$\hat{t}_{1L}^h, \hat{t}_{1L}^{\perp}$
T	$\hat{u}_{1T}^h, \hat{u}_{1T}^{\perp}$	$\hat{l}_{1T}^h, \hat{l}_{1T}^{\perp}$	$\hat{t}_{1T}^h, \hat{t}_{1T}^{hh}, \hat{t}_{1T}^{\perp\perp}, \hat{t}_{1T}^{\perp h}$

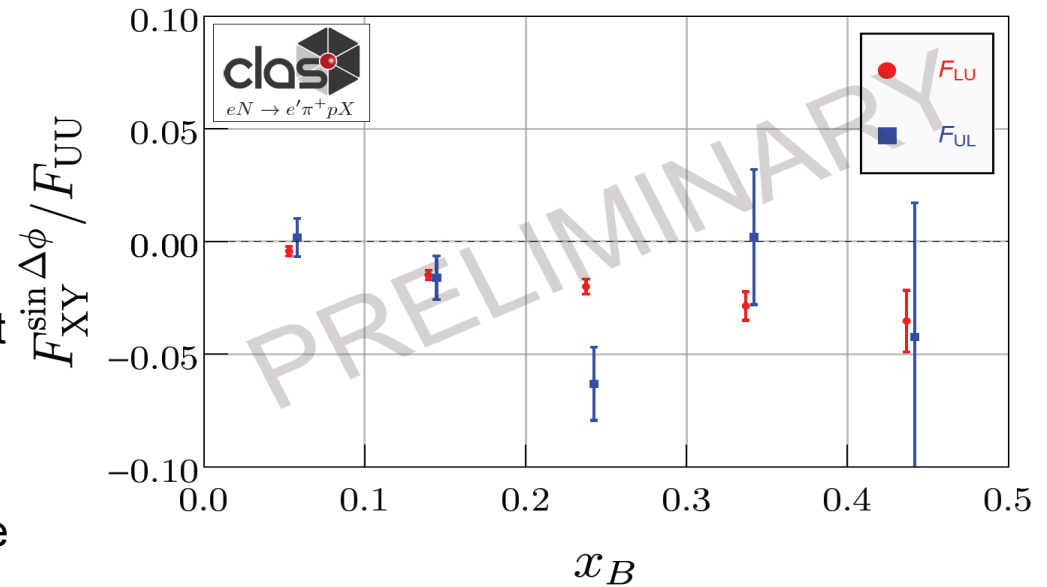
$$\sigma_{LU} = -\frac{P_{T1}P_{T2}}{m_N m_2} F_{k1}^{l^{\perp h} \cdot D_1} \sin(\Delta\phi),$$

$$\sigma_{UL} = -\frac{P_{T1}P_{T2}}{m_N m_2} F_{k1}^{\hat{u}_{1L}^{\perp h} \cdot D_1} \sin(\Delta\phi)$$



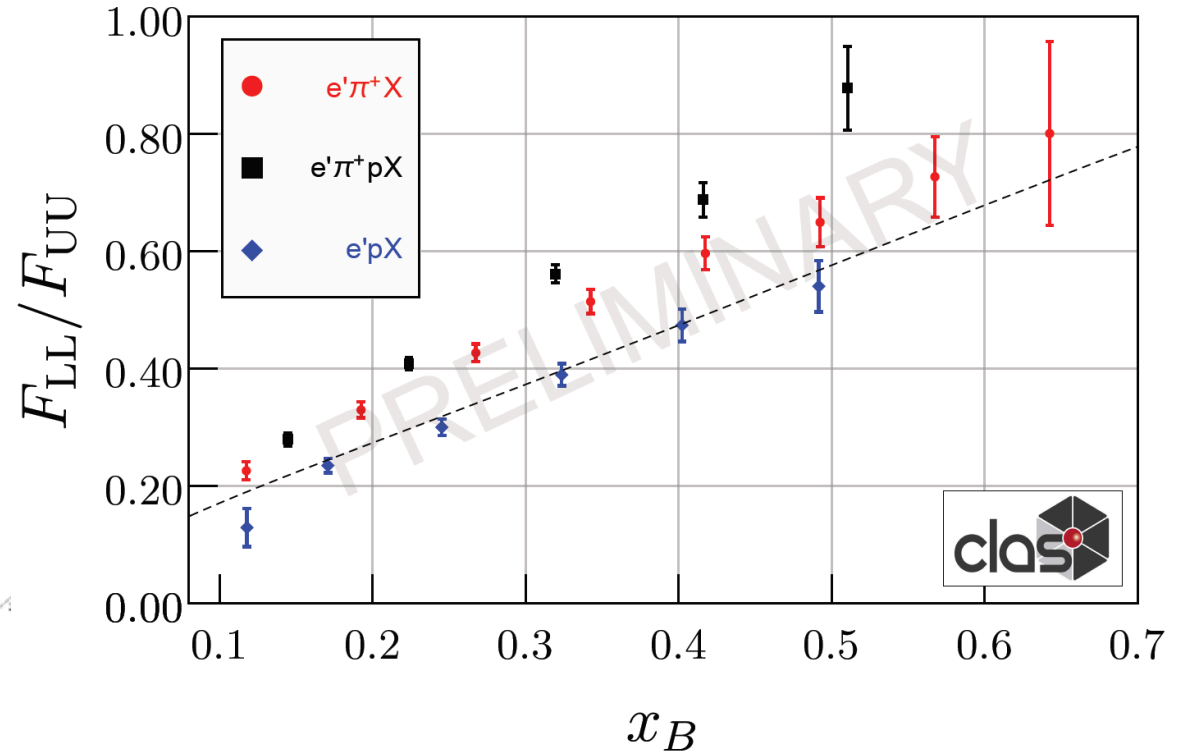
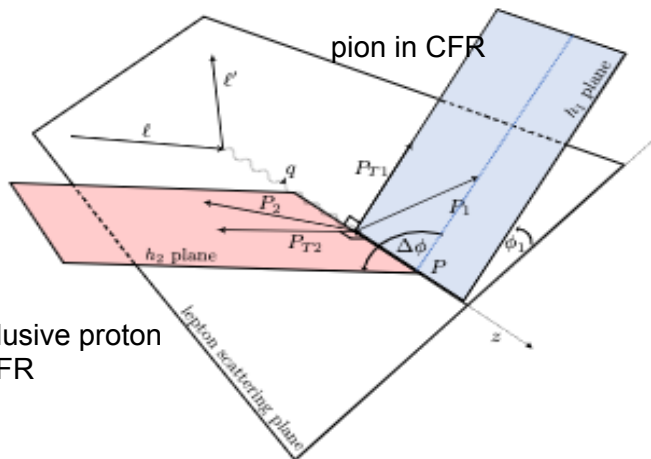
- F_{UL} and F_{LU} comparable (consistent with epX)
- No suppression at higher energies for F_{UL}

Full CLAS12 longitudinally polarized target set (x4) will provide a significant measurement of the target single spin asymmetry $A_{UL}^{\sin\Delta\phi}$, which has no suppression at higher energies and can be measured at colliders!



B2B production: exclusive baryon in TFR

N/q	U	L	T
U	\hat{u}_1	$\hat{l}_1^{\perp h}$	$\hat{t}_1^h, \hat{t}_1^\perp$
L	$\hat{u}_{1L}^{\perp h}$	\hat{l}_{1L}	$\hat{t}_{1L}^h, \hat{t}_{1L}^\perp$
T	$\hat{u}_{1T}^h, \hat{u}_{1T}^\perp$	$\hat{l}_{1T}^h, \hat{l}_{1T}^\perp$	$\hat{t}_{1T}^h, \hat{t}_{1T}^{hh}, \hat{t}_{1T}^{\perp\perp}, \hat{t}_{1T}^{\perp h}$



Detection of proton allows implementation of the “rho free” SIDIS. The same DSA $ep \rightarrow e\pi^+X$ with detection of proton, allowing to cut out the exclusive rho is higher.

- Semi-exclusive processes, involving GPDs/ GTMDs on proton side (TFR) and FFs on pion side (CFR) Yuan and Guo

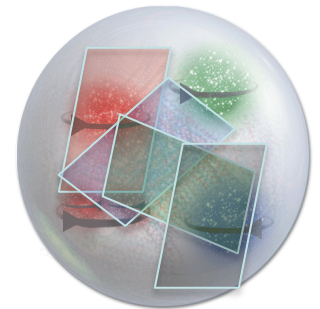
theory



Theory-Experiment Dialogue: How to proceed

1. Keeping the formalism the same, including the input data where it works well, and try to get a better description using more sophisticated TMD models for TMD PDFs, and TMD FFs.
2. Try to extend the theory adding contributions assumed irrelevant in existing phenomenology, including also accounting of NLO terms. Note that all kinds of perturbative calculations for azimuthal moments ($\sin, \cos, F_{UU,L}, \dots$) in perturbative approaches were order of magnitude less than non-perturbative quantities (ex. Cahn)
3. Try to extend the theory coverage by eliminating from the input data set the contributions that are not accounted for in the phenomenology, most importantly the longitudinal photon contributions

Measurements of Q^2 -dependence of observables is key for validation!!!



summary

Huge amount of semi-inclusive and exclusive hadron production data accumulated by CLAS12 allowing detailed studies of variety of contributions, critical for providing adequate data for QCD phenomenology for 3D studies (TMDs and GPDs/GTMDs?)

- First data from longitudinally polarized target, confirms importance of sorting out longitudinal photon contributions in general, and longitudinal ρ 0s, in particular
- Studies of evolution properties of all relevant observables has been shown to be a critical validation test
- *SIDIS in exclusive limit, may provide important info on transverse photon contributions in exclusive processes, the neutral pions (both exclusive and semi-inclusive), ready for phenomenological studies!!!*

Support slides

Connecting M_X , t , P_T and z

$$ep \rightarrow e' \pi^0 X \quad (M_X = M_P, t = (\gamma^* - p_{\pi 0})^2)$$

exclusive limit $M_X = M_P$

$$z(t) = z_0 + at, \quad a = \frac{x_B}{Q^2}, \quad z_0 = 1 + \frac{x_B(M_P^2 - M_X^2)}{Q^2}$$

$$P_T^2(t) = z^2 \nu^2 - m_\pi^2 - \frac{(t + Q^2 - m_\pi^2 + 2z\nu^2)^2}{4(\nu^2 + Q^2)}$$

$$P_T^2(t) = \nu^2 \left(1 + \frac{x_B t}{Q^2}\right)^2 - m_\pi^2 - \frac{\left[Q^2 - m_\pi^2 + 2\nu^2 + t \left(1 + \frac{2\nu^2 x_B}{Q^2}\right)\right]^2}{4(\nu^2 + Q^2)}$$

In the small- $|t|/Q^2$ limit and neglecting m_π^2 ,

$$P_T^2(t) \simeq -(1 - x_B)t = (1 - x_B)|t| \quad \rightarrow \quad \frac{d\sigma}{d|t|} \propto (1 - x_B) \exp\left[-\frac{(1 - x_B)|t|}{2\sigma^2}\right]$$

$$\frac{d^5 \sigma^{\ell p \rightarrow \ell h X}}{dx_B dQ^2 dz_h d^2 P_T} = \frac{2\pi\alpha^2}{Q^4} \frac{y^2}{1 - \epsilon} \sum_q e_q^2 f_q(x_B) D_q^h(z_h) \frac{1}{\pi \langle P_T^2 \rangle} e^{-P_T^2 / \langle P_T^2 \rangle}$$

$$\langle P_T^2 \rangle = \langle p_\perp^2 \rangle + z_h^2 \langle k_\perp^2 \rangle = 2\sigma^2,$$

Correlated slopes in P_T and t

$$ep \rightarrow e' \pi^0 X \quad (M_X = M_P, \quad t = (\gamma^* - p_{\pi^0})^2)$$

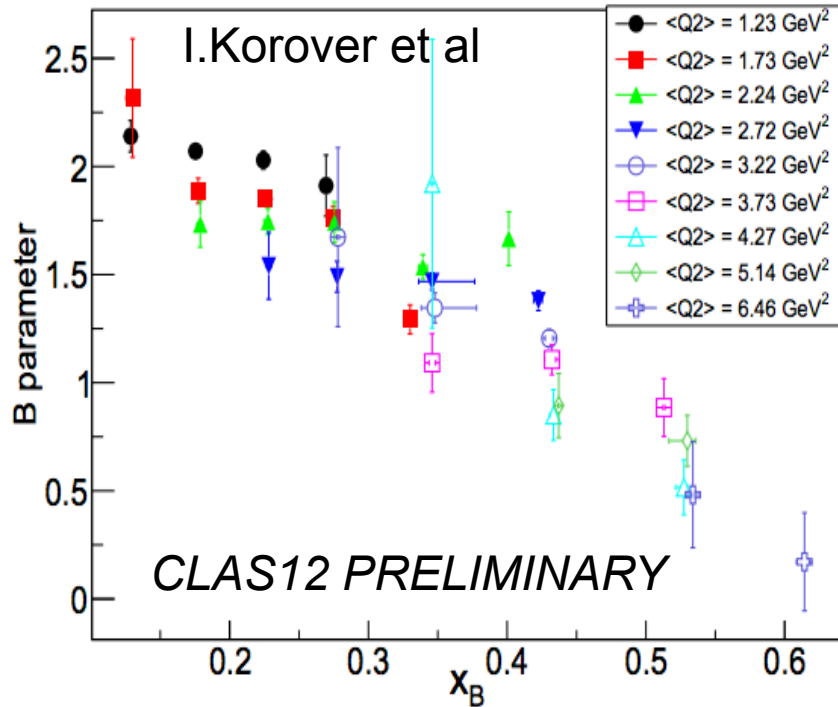
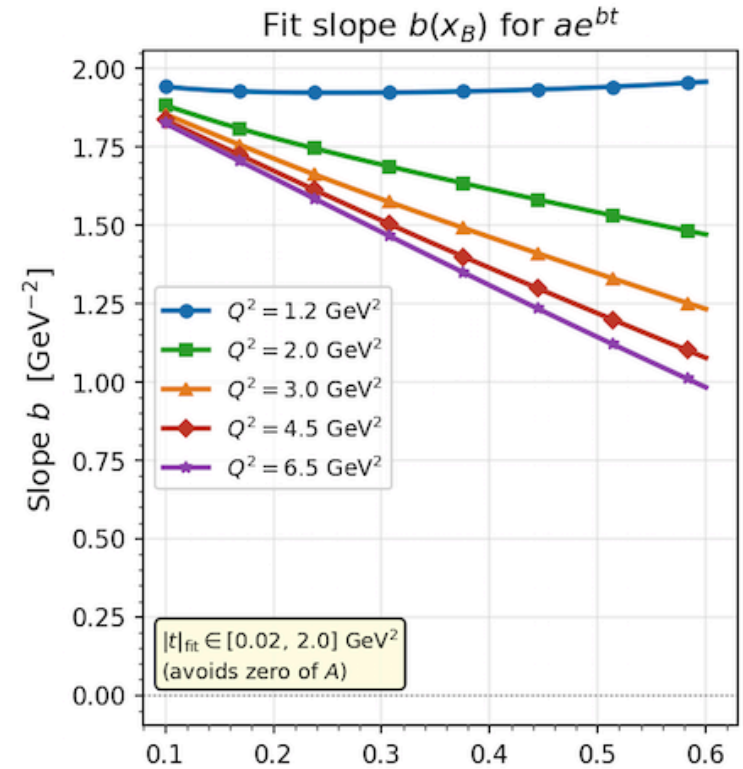


Figure 68: The extracted B parameters for multiple Q^2 bins as function of x_B . The Q^2 value is average value of the Q^2 value that was used to extract the structure function at the relevant bin.



$$\frac{d\sigma}{d^2P_T} \propto \exp \left[-\frac{P_T^2}{2\sigma^2} \right] x_B$$

$$\frac{d\sigma}{dt} \propto \left| \frac{dP_T^2}{dt} \right| \exp \left[\frac{z_{\text{excl}} t + z_{\text{excl}}(1 - z_{\text{excl}}) Q^2 + (1 - z_{\text{excl}}) m_\pi^2}{2\sigma^2} \right]$$

$$z_{\text{excl}} = 1 + \frac{x_B t}{Q^2}$$