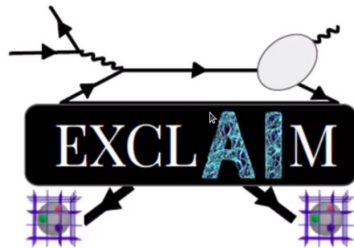


# Generalized Parton Distributions of Composite Light Nuclei



Matthew D. Sievert  
& Antonio Garcia Vallejo



*Tensor SIDIS Workshop*  
*Jefferson Lab*

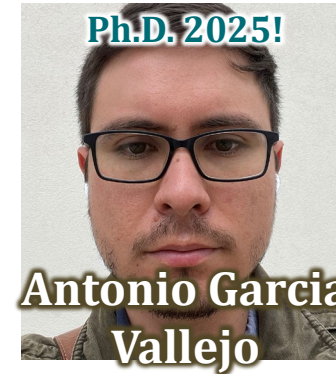
*6/4/2026*

# Important Information

**For more details:**

[arXiv: 2510.15838](https://arxiv.org/abs/2510.15838)

- To appear in PRD
- Editor's Suggestion



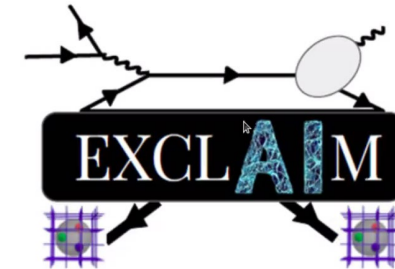
❖ **Next talk!**

[Thurs. 6/4,](#)  
[11:25am](#)

**This work supported by:**



DOE Office of Science,  
Award #DE-SC0024560



EXCLAIM Collaboration: DOE Office of Science,  
Award #DE-SC0024644

# Perturbation Theory: The Textbook Story

$$d\sigma = d\sigma^{[0]} + \alpha d\sigma^{[1]} + \alpha^2 d\sigma^{[2]} + \alpha^3 d\sigma^{[3]} + \dots$$

- **Perturbation theory:**

Taylor expansion in **powers of the coupling**  $\alpha_s$

- **Successes:**

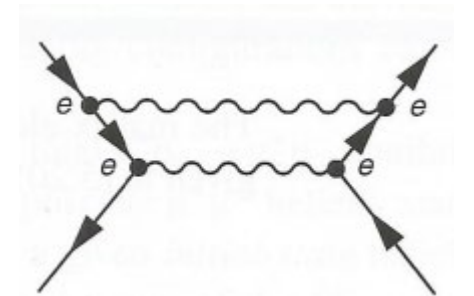
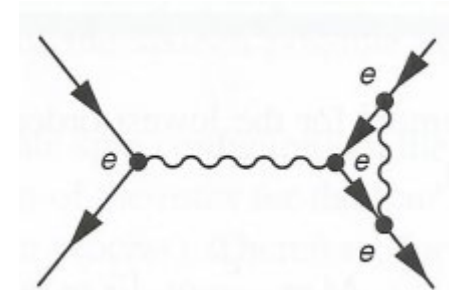
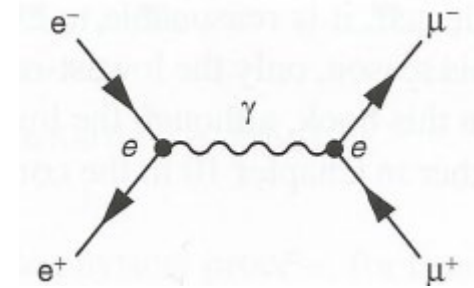
Weak coupling  $\alpha_s(Q) \ll 1$  at  $Q^2 \gg \Lambda_{QCD}^2$

- **Limitations:**

Slow convergence

Asymptotic series

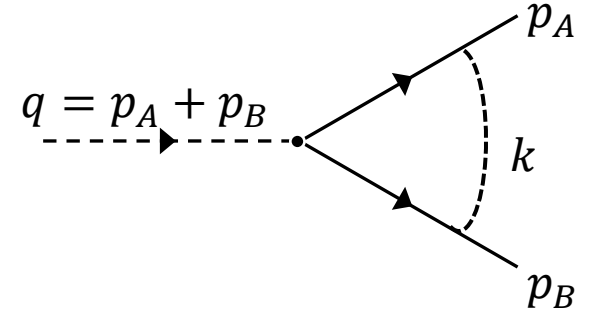
Nonperturbative effects



# Factorization is a More Powerful Statement

$$I \equiv g^3 \mu^{3(3-d/2)} \int \frac{d^d k}{(2\pi)^d} \frac{1}{(k^2 - m^2)((p_A - k)^2 - m^2)((p_B + k)^2 - m^2)}$$

$$= I_{A, coll} + I_{B, coll} + I_{soft} + I_{A, soft-coll} + I_{B, soft-coll}$$



- **Collinear factorization:**

**Dimensional analysis** of  $Q^2 \rightarrow \infty$  asymptotics

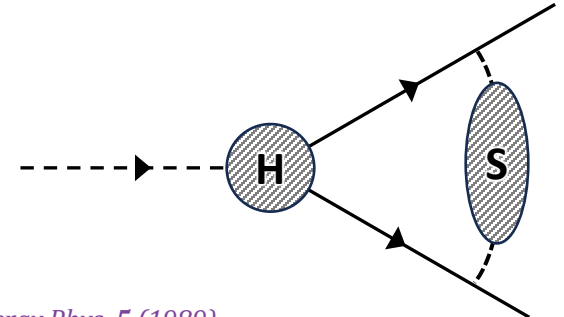
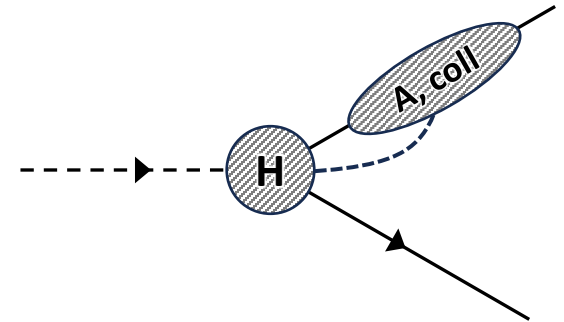
- **Superficially:**

Scale all units by  $Q$ , then drop other scales  $\frac{m^2}{Q^2} \rightarrow 0$

- **Subtlety:**

Setting  $\frac{m^2}{Q^2} \rightarrow 0$  can create **IR divergences**.

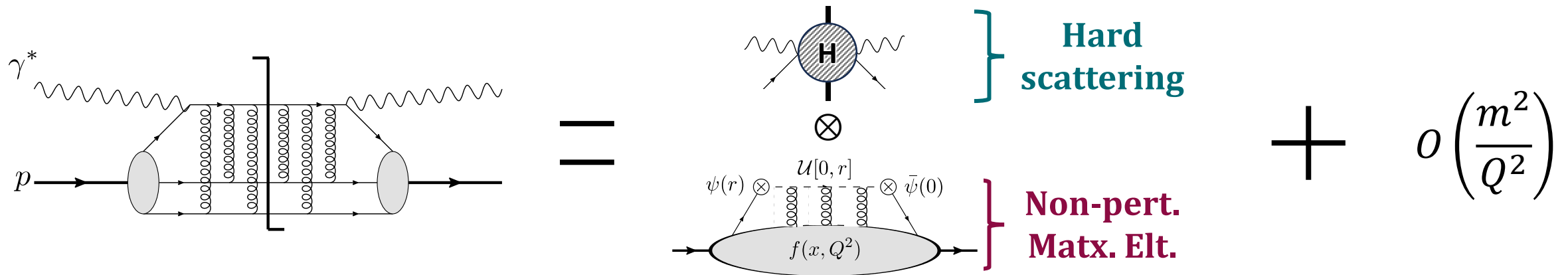
Anomalous power enhancements in momentum space



*"Foundations of Perturbative QCD," J. C. Collins, (1989), Cambridge Univ. Press, 2011*

*Collins, Soper, Sterman, Adv. Ser. Direct. High Energy Phys. 5 (1989)*

# Factorization Theorems, to All Orders in pQCD



- **Factorization theorem:**

Nonperturbative physics is quarantined into specific, universal matrix elements

- **Kinematic expansion:**

Hadron structure as seen by an infinitely hard probe  $Q^2 \rightarrow \infty$  (“**infinite momentum frame**”)

- **Predictive power:**

The same universal matrix elements appear in multiple reactions

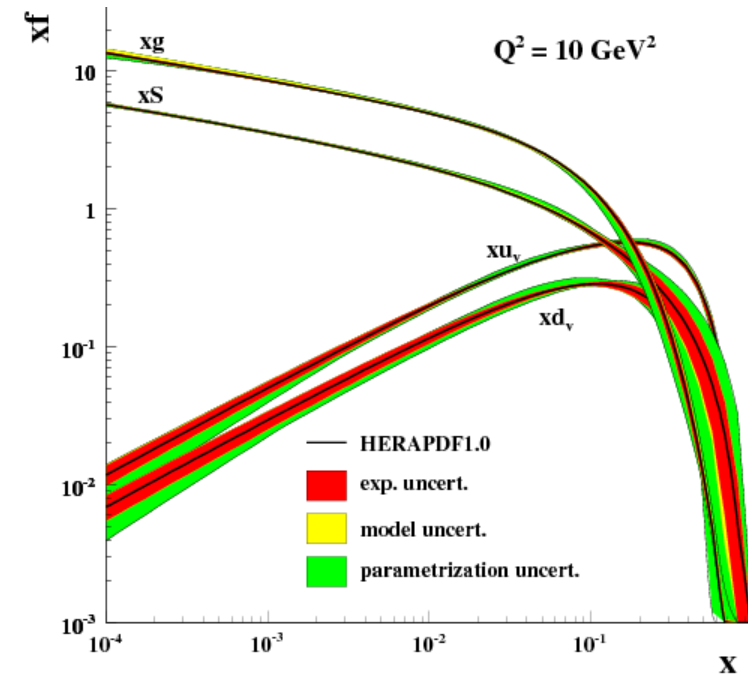
# 1D Structure: PDFs

$$\phi_{\alpha\beta}(x) = \int \frac{dr^-}{2\pi} e^{ixp^+r^-} \langle p, S | \bar{\psi}_\beta(0) \mathcal{U}[0, r^-] \psi_\alpha(r^-) | p, S \rangle$$

- **Collinear Factorization:**  
**Inclusive** processes with a **single scale**  $Q^2 \rightarrow \infty$

- **Parton Distribution Functions (PDFs):**  
Gauge-invariant operators which correspond to **parton densities**  $\frac{dN}{dx}$  in light-front gauge  $A^+ = 0$ .

Differential only in the **longitudinal momentum fraction  $x$**



*H1 and ZEUS Collaborations, JHEP 01 (2010) 109*

*Collins, Soper, Sterman, Adv. Ser. Direct. High Energy Phys. 5 (1989)*

# 3D Structure: TMDs

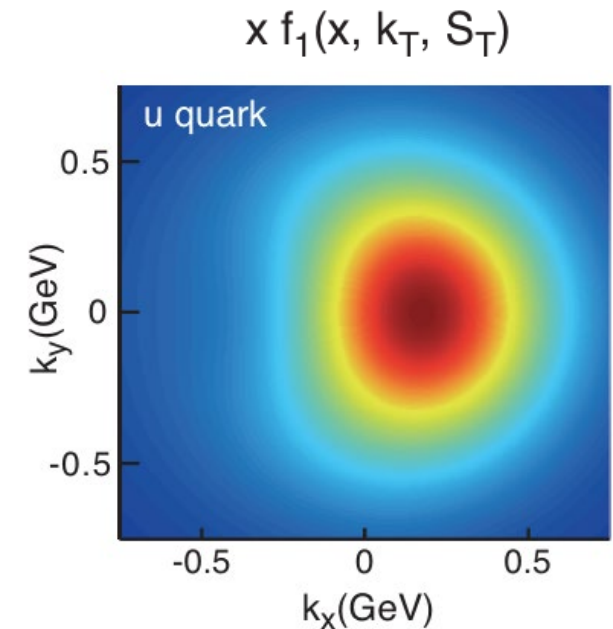
$$\phi_{\alpha\beta}(x, \vec{k}_{\perp}) = \int \frac{d^2 r_{\perp} dr^{-}}{(2\pi)^3} e^{ixp^{+}r^{-} - i\vec{k}_{\perp} \cdot \vec{r}_{\perp}} \langle p, S | \bar{\psi}_{\beta}(0) \mathcal{U}[0, r] \psi_{\alpha}(r) | p, S \rangle$$

- **Transverse-Momentum-Dependent (TMD) Factorization:**  
Semi-inclusive processes with **two scales**:  $Q^2 \rightarrow \infty$  and  $k_{\perp}^2 \ll Q^2$

“**Fragile**” factorization holds only for select processes, with modified universality

- **TMD Parton Distribution Functions (TMDs):**  
Gauge-invariant operators differential in both longitudinal momentum fraction  $x$  and **transverse momentum**  $\vec{k}_{\perp}$ .

Not simply parton densities: irreducible physics of **QCD lensing**



# 3D Structure: GPDs

$$\phi_{\alpha\beta}(x, \xi, \vec{\Delta}_{\perp}) = \int \frac{dr^{-}}{2\pi} e^{ixp^{+}r^{-}} \text{out} \langle p', S' | \bar{\psi}_{\beta}(0) \mathcal{U}[0, r^{-}] \psi_{\alpha}(r^{-}) | p, S \rangle_{\text{in}}$$

- **Exclusive Factorization:**

Exclusive final state provides **two scales**:  $Q^2 \rightarrow \infty$  and  $|t| \ll Q^2$

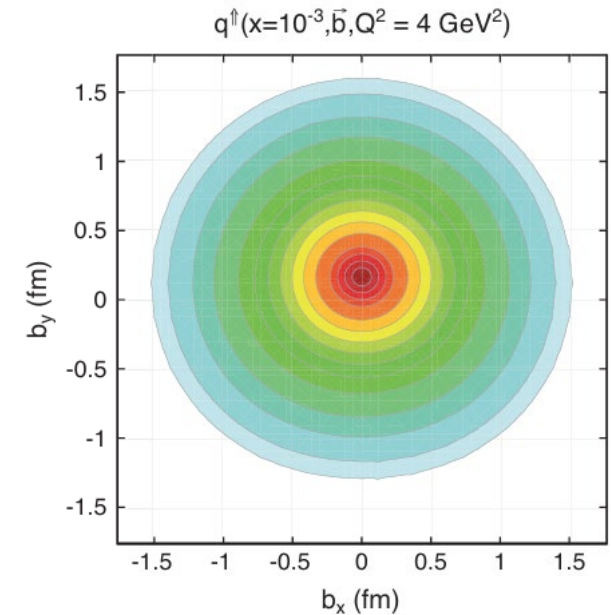
Rarer statistics, but greater sensitivity (amplitude level)

- **Generalized Parton Distribution Functions (GPDs):**

Gauge-invariant operators differential in longitudinal momentum fraction  $x$ , longitudinal skewness  $\xi$ , and **momentum transfer  $\vec{\Delta}_{\perp}$** .

**Fourier transform  $\vec{\Delta}_{\perp} \rightarrow \vec{b}_{\perp}$**  at  $\xi = 0$  gives parton densities

$\frac{dN}{dx d^2b_{\perp}}$  in **impact parameter space**.



*Muller et al., Fortschritte der Physik, 42 (1994)*

*Radyushkin, Phys. Lett. B 380 (1996)*

*Ji, Phys. Rev. D 55 (1997)*

*Collins, Freund, Phys. Rev. D, 59 (1999)*

*A. Accardi, et al., Eur. Phys. J. A 52 (2016)*

# 5D Structure: Wigner Distributions

$$\phi_{\alpha\beta}(x, \xi, \vec{\Delta}_\perp, \vec{k}_\perp) = \int \frac{d^2 r_\perp dr^-}{(2\pi)^3} e^{ixp^+ r^- - \vec{k}_\perp \cdot \vec{r}_\perp} \text{out} \langle p', S' | \bar{\psi}_\beta(-\frac{1}{2}r) \mathcal{U}[0, r] \psi_\alpha(\frac{1}{2}r) | p, S \rangle_{\text{in}}$$

- **Generalized TMD (GTMD) Factorization:**

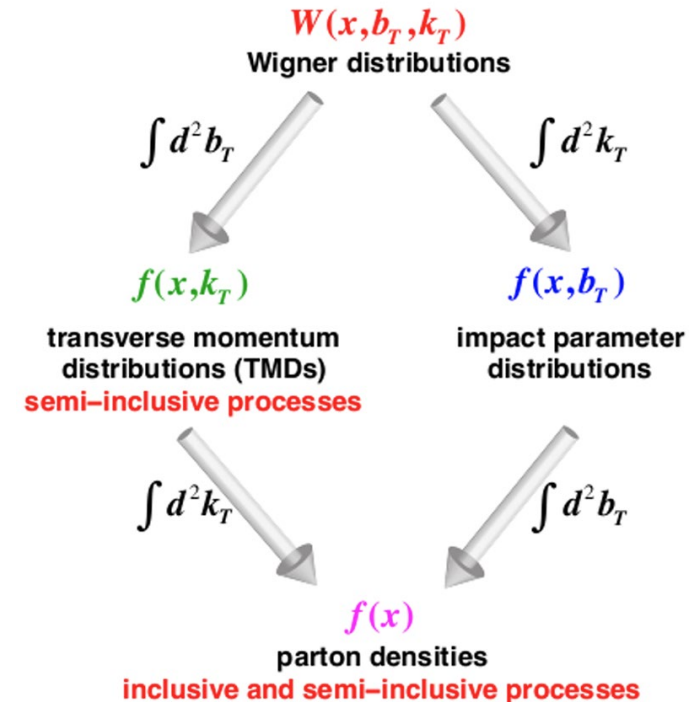
Rare processes with both a diffractive component and a momentum imbalance (e.g., diffractive dijets in pA)

- **Wigner Functions (GTMDs):**

Gauge-invariant operators differential  $x$ ,  $\vec{k}_\perp$ , and  $\vec{b}_\perp$

Simultaneously differential in **position and momentum**, without violating the **Uncertainty Principle**

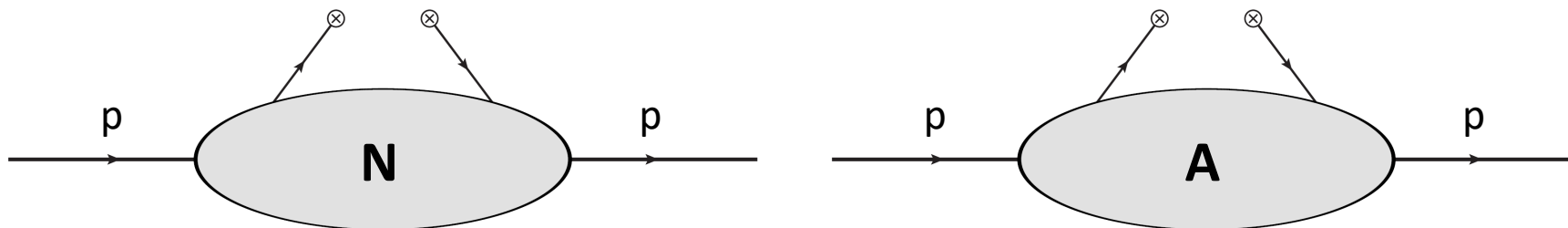
Quantum-mechanical “master functions” with well-defined **TMD, GPD, and classical limits**



Meissner, Metz, Goeke, *Phys. Rev. D*, **80** (2009)

A. Accardi, et al., *Eur. Phys. J. A* **52** (2016)

# Partonic Structure of Nuclei



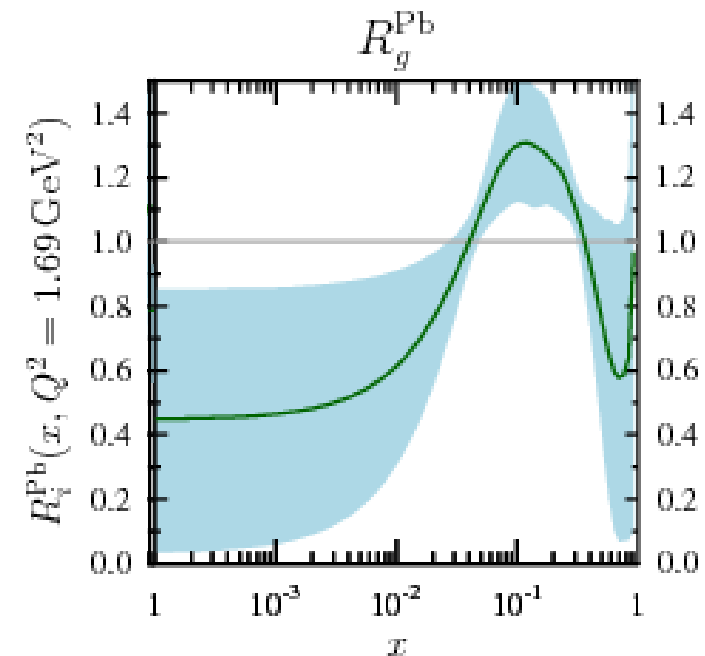
- **Factorization works the same way for nuclei:**  
**Same factorization formula** and matrix elements

Dependence on target species through mass number  $A$

- **Nuclear Modification Factor for PDFs:**  
Compares the ratio of nuclear PDF to nucleon PDF

Modification of partonic structure of a nucleon due to nuclear environment

Reveals fascinating nuclear modification associated with the **EMC effect**.



*Helenius et al., JHEP 07 (2012)*

# Impulse Approximation: The One-Body Sector

$$\langle A' | \bar{\psi}_\beta \psi_\alpha | A \rangle = (\Psi_{N'}^* \Psi_N) \otimes \langle N' | \bar{\psi}_\beta \psi_\alpha | N \rangle + \text{correlations}$$

- **A composite system can be decomposed into its constituents:**

Nuclear state is expressed as **many-body wave function** of its constituents (**spectral function**)

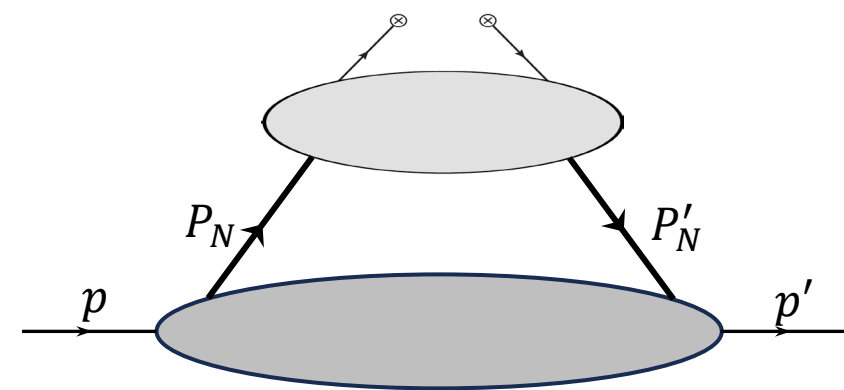
Only a single active constituent is treated dynamically (**mean-field approximation**), but **systematically improvable**

- **Multiple variations on implementation**

Instant-form wave functions (nonrelativistic)

Light-front wave functions (relativistic)

[**Virtual Nucleon Approximation**]



*Geesaman, Saito, Thomas., Ann.Rev.Nucl.Part.Sci. 45 (1995)*

*Ericson, Kumano. Phys. Rev. C 67 (2003)*

*Hirai, Kumano, Saito, Watanabe. Phys. Rev. C 83 (2011)*

*Cosyn, Dong, Kumano, Sargsian. Phys. Rev. D 95 (2017)*

# Composite Structure Mixing

- **Orbital motion of constituents mixes 3D partonic structure:**

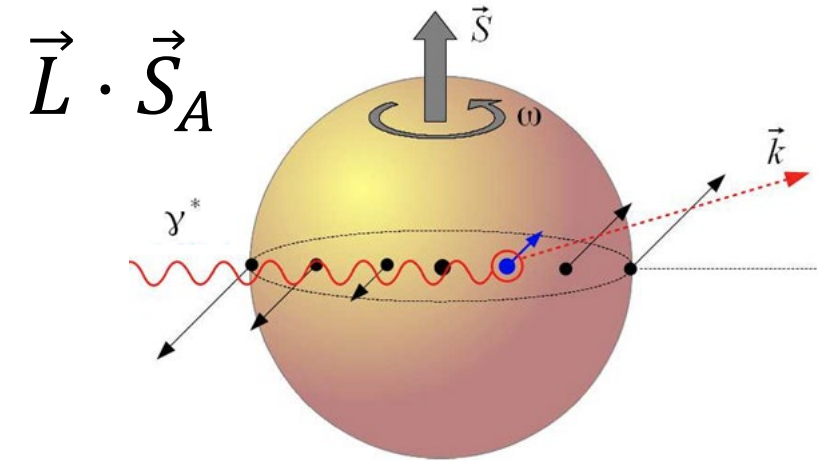
A static nucleus simply smears the partonic structure of the nucleon

Nontrivial **orbital motion of the nucleons mixes 3D structure** for, e.g., the Sivers TMD and Boer-Mulders TMD

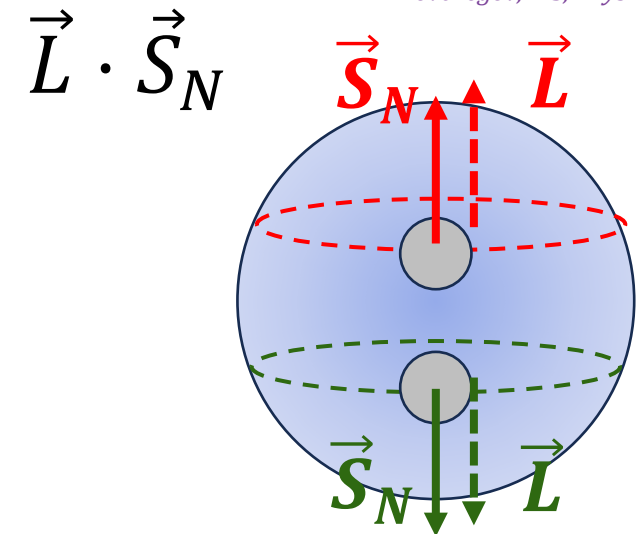
**QCD lensing** effects are essential to some mixing channels

- **An overdetermined problem:**

A small number of nuclear correlations (e.g.,  $\vec{L} \cdot \vec{S}$ ) are responsible for **several mixing channels**



*Kovchegov, MS, Phys. Rev. D, 89 (2014)*



*Kovchegov, MS, Nucl. Phys. B, 903 (2016)*

# An Application: $^4\text{He}$ and ALERT

- **Jlab experiment with CLAS12 + ALERT:**  
Spectator-tagged DVCS and  $\phi$  production

Will access the **quark and gluon GPDs of  $^4\text{He}$**   
and study the relation to the EMC effect

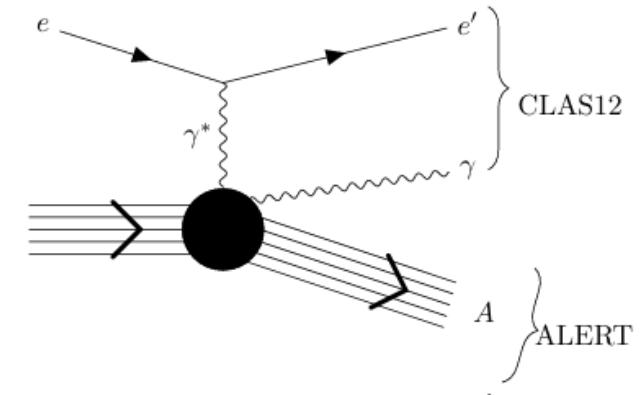
$^4\text{He}$  is a simple spin-0 composite nucleus

Recently completed data collection with ongoing analysis;  
leadership of **NMSU colleague M. Paolone**.

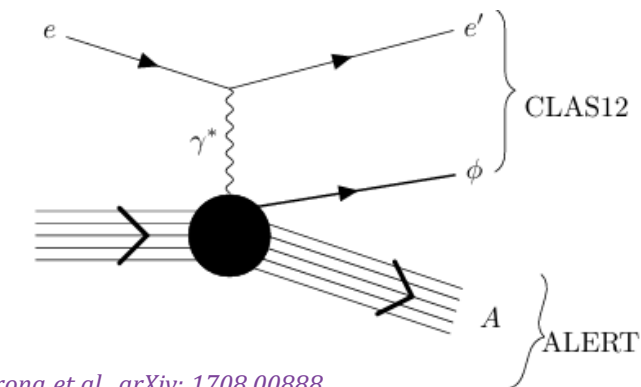
- **This work:**  
Application of a **light-front impulse approximation**  
to study the GPDs of  $^4\text{He}$

**Wigner representation** to make symmetries manifest.

$$e + A \rightarrow e' + \gamma + A'$$



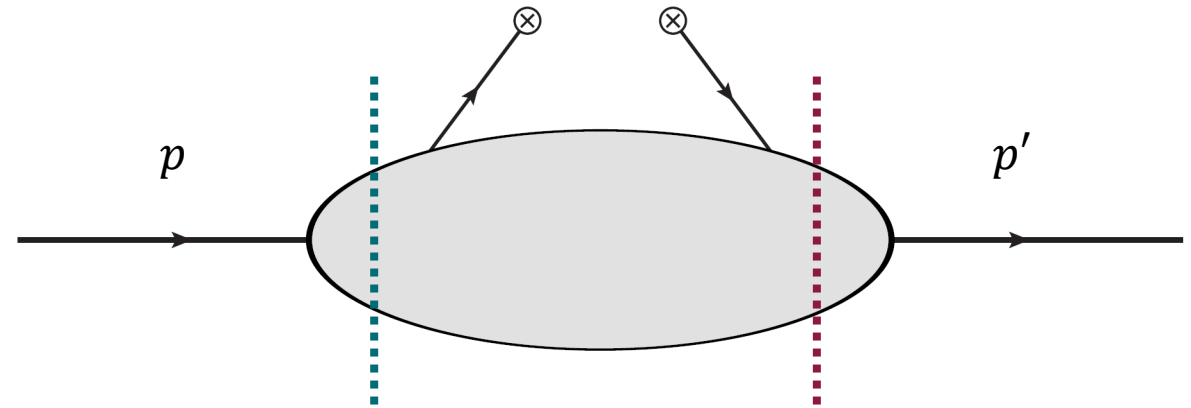
$$e + A \rightarrow e' + \phi + A'$$



*Armstrong et al., arXiv: 1708.00888*

# Derivation: Completeness

$$F_{q/\phi}^{[\Gamma]} = \frac{1}{4\pi} \int dr^- e^{ixP^+r^-} (\Gamma)_{JI} \\ \times \text{out} \langle p' | \bar{\psi}_J(-r^-/2) \psi_I(r^-/2) | p \rangle \text{in}$$



1. Insert **complete sets** of free, on-shell **constituent Fock states**
- Expresses in/out states as wave packets of constituents

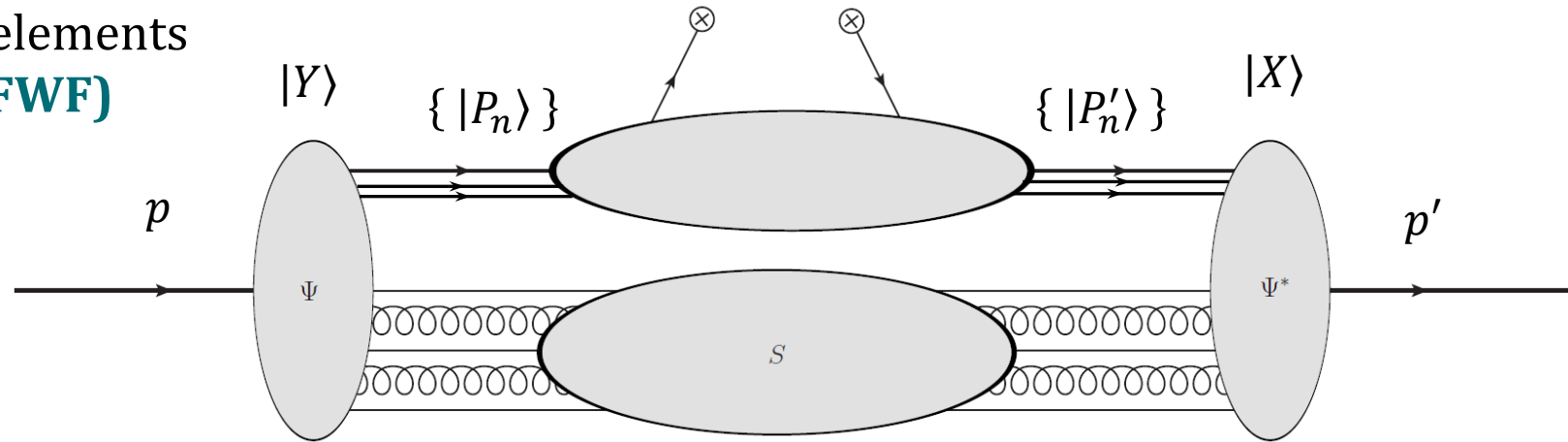
$$\hat{\mathbb{1}} = \int_X |X\rangle \langle X| \\ = \sum_n \frac{1}{S_n} \int \frac{d^2 p_{1\perp} dp_1^+}{(2\pi)^3 2p_1^+} \dots \frac{d^2 p_{n\perp} dp_n^+}{(2\pi)^3 2p_n^+} |p_1 \dots p_n\rangle \langle p_1 \dots p_n|$$

$$\text{out} \langle p' | \bar{\psi}_J\left(\frac{-r^-}{2}\right) \psi_I\left(\frac{r^-}{2}\right) | p \rangle \text{in} = \int_{\{X,Y\}} \boxed{\text{out} \langle p' | X \rangle \text{out}} \text{out} \langle X | \bar{\psi}_J(-r^-/2) \psi_I(r^-/2) | Y \rangle \text{in} \boxed{\text{in} \langle Y | p \rangle \text{in}}$$

# Derivation: Light Front Wave Functions

2. Relate **in/in** and **out/out** matrix elements to **light-front wave functions (LFWF)**

- LFWF are **boost invariant**
- Integrate out **disconnected spectators**
- Inclusive LFWF remain



$$\text{in} \langle Y | p \rangle_{\text{in}} \equiv (2\pi)^3 2p^+ \delta^2 \left( \sum \vec{p}_{Yi\perp} - \vec{p}_\perp \right) \delta \left( \sum_i p_{Yi}^+ - p^+ \right) \\ \times \Psi(\{p_{Yi}^+\}; \{\vec{p}_{Yi\perp}\})$$

$$\Psi(\{p_{Yi}^+\}; \{\vec{p}_{Yi\perp}\}) = \Psi \left( \left\{ \frac{p_{Yi}^+}{p^+} \right\}; \{\vec{p}_{Yi\perp}\} \right)$$

*Brodsky, Pauli, Pinsky, Phys. Rept. 301 (1998)*

# Derivation: Wigner Distribution

3) Re-express the **off-forward product of LFWF** in terms of a **Wigner distribution**

$$\tilde{\Psi}_s(b^-, \vec{b}_\perp) = \int \frac{d^2 k_\perp dk^+}{(2\pi)^3} e^{-ik^+ b^- + i\vec{k}_\perp \cdot \vec{b}_\perp} \frac{\tilde{\Psi}_s(k^+, \vec{k}_\perp)}{\sqrt{2k^+}}$$

- The **Fourier transform** of the LFWF defines a **spacetime position**
- A Wigner distribution is a **mixed Fourier transform** that fixes the **average momentum and impact parameter**
- Fully **quantum**, but **semi-classical correspondence**

$$W_{s's}(p^+, \vec{p}_\perp; b^-, \vec{b}_\perp) =$$

$$= \int \frac{d^2 q_\perp dq^+}{(2\pi)^3} e^{-iq^+ b^- + i\vec{q}_\perp \cdot \vec{b}_\perp} \frac{\tilde{\Psi}_{s'}^*(p - \frac{1}{2}q)}{\sqrt{2(p - \frac{1}{2}q)^+}} \frac{\tilde{\Psi}_s(p + \frac{1}{2}q)}{\sqrt{2(p + \frac{1}{2}q)^+}}$$

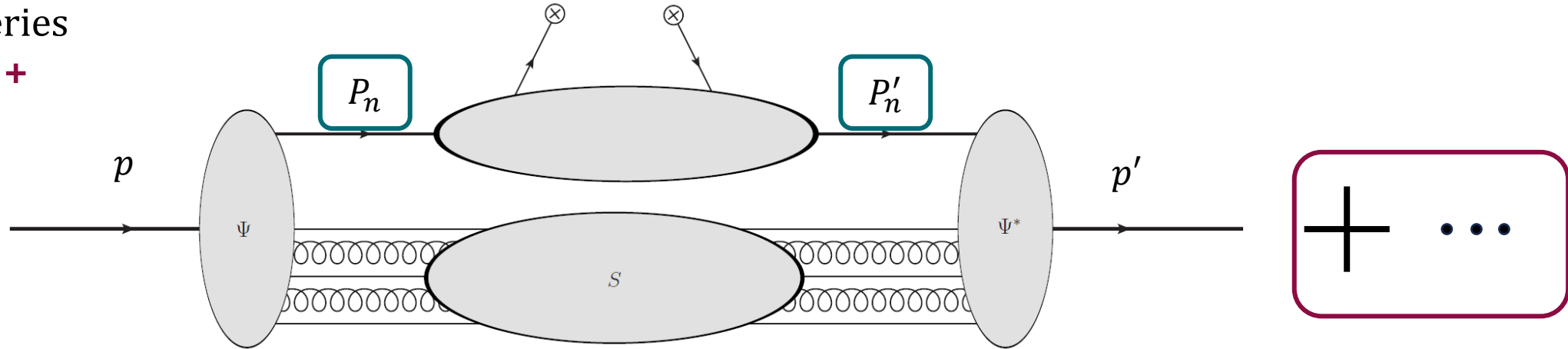
$$= \int d^2 r_\perp dr^- e^{+ip^- r^- - i\vec{p}_\perp \cdot \vec{r}_\perp} \tilde{\Psi}_{s'}^*(b - \frac{1}{2}r) \tilde{\Psi}_s(b + \frac{1}{2}r)$$

$$\frac{\tilde{\Psi}_{s'}^*(k')}{\sqrt{2k'^+}} \frac{\tilde{\Psi}_s(k)}{\sqrt{2k^+}} = \int d^2 b_\perp db^- e^{+i(k-k')^+ b^- - i(\vec{k} - \vec{k}')_\perp \cdot \vec{b}_\perp}$$

$$\times W_{s's}\left(\frac{1}{2}(k^+ + k'^+), \frac{1}{2}(\vec{k}_\perp + \vec{k}'_\perp); b^-, \vec{b}_\perp\right)$$

# Derivation: Mean Field + Correlations

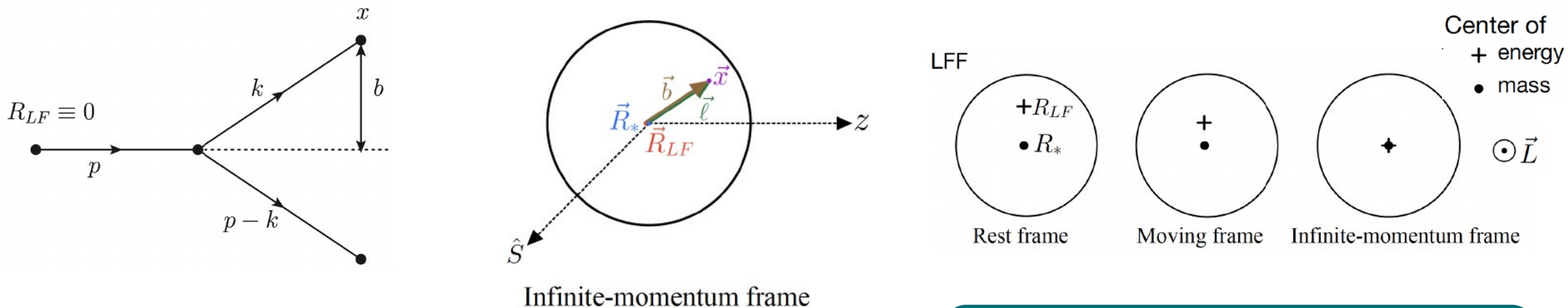
- 4) Expand in a series of **mean field + correlations**



$$\text{out } \langle p' | \bar{\psi}_J(\frac{-r^-}{2}) \psi_I(\frac{r^-}{2}) | p \rangle_{\text{in}} = \frac{1}{2} \sum_{ss'} \int d^2 P_{1\perp} dP_1^+ \int d^2 b_\perp db^- e^{-i\Delta^+ b^- + i\bar{\Delta}_\perp \cdot \bar{b}_\perp} \left( \frac{1}{\sqrt{P_1^+}} \frac{p'^+}{\sqrt{P_1^+ + \Delta^+}} \frac{p^+}{P^+} \frac{p^+ - P_1^+}{P^+} \right) \\ \times W_{s's}(P_1 + \frac{1}{2}\Delta, b; P, \Delta) \langle (P_1 + \Delta) s' | \bar{\psi}_J(-r^-/2) \psi_I(r^-/2) | P_1 s \rangle + \text{correlations}$$

- In a **large nucleus**, dominance of the **mean field** is guaranteed by  $A \gg 1$
- In a **small nucleus**, must be considered just the **first term in a series**
  - Start with the mean field, but **correlations may not be small** (e.g. SRC)

# Derivation: Light Front / Rest Frame Dictionary



5) Exploit **boost invariance** to **relate IMF Wigner function to RF**

- Since  **$W$  is boost invariant**, only its arguments change
- Use **boost-invariant products** to map to Rest Frame

❖ **Caveat: relativistic CoM**

$$\alpha_{IMF} = \alpha_{LF} \quad (P^+ b^-)_{IMF} = (P^+ b^-)_{LF}$$

$$\xi_{IMF} = \xi_{LF}$$

$$\begin{aligned} (P_{N,z})^{R.F.} &\equiv \sqrt{\frac{\Lambda^2}{4(1-\xi^2)}} \left[ \alpha - \left( \frac{1-\xi^2}{1-(\xi/\alpha)^2} \right) \frac{(\vec{P}_{N\perp} + \frac{1}{2}\vec{\Delta}_\perp)^2 - (1-\xi/\alpha)(\vec{P}_{N\perp} \cdot \vec{\Delta}_\perp) + m^2}{\alpha\Lambda^2} \right] \\ (\Delta_z)^{R.F.} &\equiv -2\xi \sqrt{\frac{\Lambda^2}{1-\xi^2}} \\ (b_z)^{R.F.} &\equiv -\sqrt{\frac{1-\xi^2}{\Lambda^2}} (b^- P^+). \end{aligned} \quad \Lambda^2 \equiv \frac{1}{4} \vec{\Delta}_\perp^2 + M^2$$

# Derivation: Intermediate Spin States

6) Use a **Pauli matrix basis** to change from spin projection to **spin vector**

$$W(P_N, b, S; P, \Delta) = W_{unp} - \vec{W}_{pol} \cdot \vec{S}$$

- Decomposes polarized quantities with **explicit linear dependence on  $\vec{S}$**

$$W_{s's}(P_N, b; P, \Delta) = W_\nu(P_N, b; P, \Delta) [\sigma^\nu]_{s's} \\ \equiv W_{unp} [\mathbb{1}]_{s's} - \vec{W}_{pol}^i [\vec{\sigma}^i]_{s's}$$

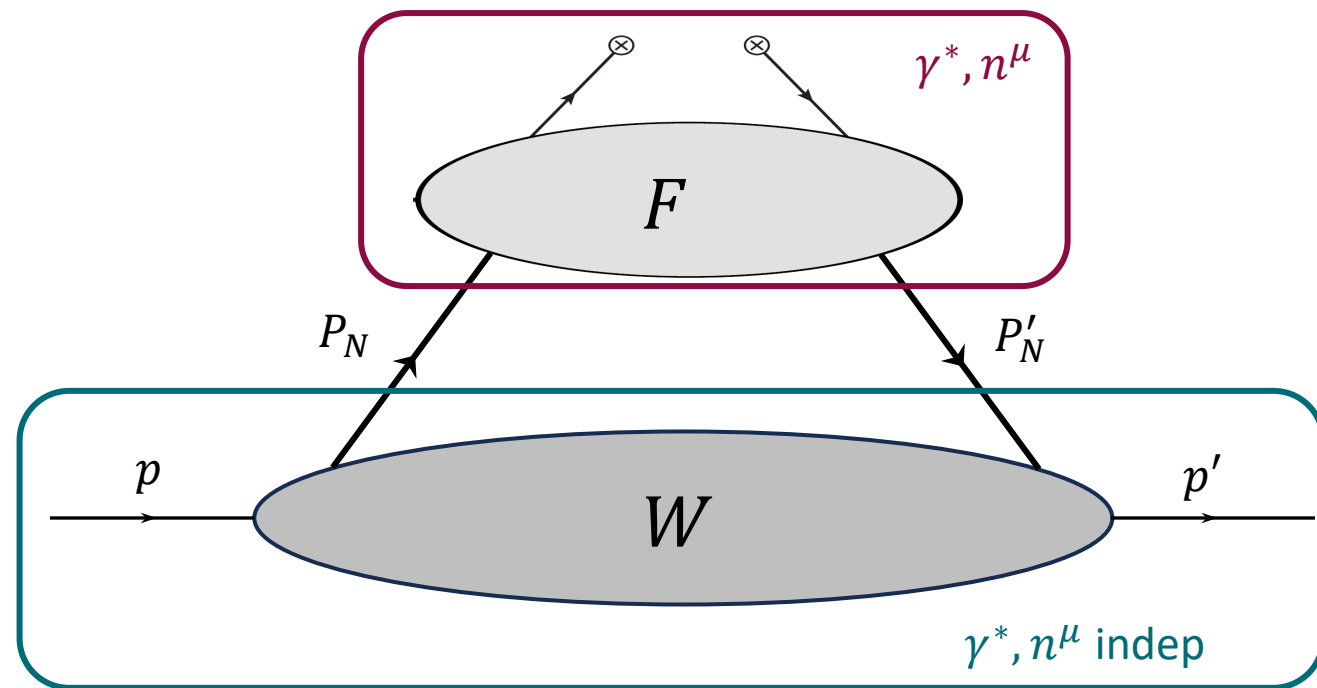
- Decomposes the nuclear GPD as a **sum over unpolarized, longitudinally-, and transversely-polarized channels**

$$F_{q/N}^{[\Gamma]}(x'; P_N, \Delta; s', s) = F_{q,\mu}^{[\Gamma]}(x'; P_N, \Delta; s', s) [\sigma^\mu]_{ss'} \\ \equiv F_{q,unp}^{[\Gamma]} [\mathbb{1}]_{ss'} - \vec{F}_{q,pol}^{[\Gamma],j} [\vec{\sigma}^j]_{ss'}$$

$$F_{q/\phi}^{[\Gamma]} = (1 - \xi^2) \int \frac{db^- dP_N^+}{\sqrt{1 - \xi_N^2}} \left( \frac{1 - \alpha}{\alpha} \right) \int d^2b_\perp d^2P_{N\perp} e^{-i[b^- \Delta^+ - \vec{b}_\perp \cdot \vec{\Delta}_\perp]} [W_{unp} F_{q,unp}^{[\Gamma]} + \vec{W}_{pol} \cdot \vec{F}_{q,pol}^{[\Gamma]}]$$

# Derivation: Symmetry Constraints

- 7) Impose **symmetry constraints** on the **Wigner function**
- The GPD is a property of the **high-energy cross section**
    - **2D rotational symmetry** about the collision axis  $n^\mu$
  - LFWF / Wigner distribution are properties of the **target only**
    - **3D rotational symmetry** in the RF
    - Unbroken  **$T, P$  symmetry**
  - Only  $(\vec{L} \cdot \vec{S})$  and  $(\vec{\Delta L} \cdot \vec{S})$  correlations survive



$$W_{unp}(\vec{\Delta}, \vec{P}_N, \vec{b}) \equiv W_{unp}(\vec{b}^2, \vec{\Delta}^2, \vec{P}_N^2, (\vec{\Delta} \cdot \vec{P}_N), (\vec{b} \cdot \vec{\Delta}), (\vec{b} \cdot \vec{P}_N), \vec{\Delta} \cdot (\vec{b} \times \vec{P}_N))$$

$$\vec{W}_{pol}^i \equiv (\vec{b} \times \vec{P}_N)^i \omega_1 + (\vec{b} \times \vec{\Delta})^i \omega_2 \equiv \omega_1 \vec{L}_{P_N}^i + \omega_2 (\Delta \vec{L}^i)$$

# Derivation: Master Formula for ${}^4\text{He}$

8) Combine with constituent GPDs to obtain nucleon / nucleus “master formula”

$$F_{q/N}^{[\gamma^+]}(p', s'; p, s) = \frac{1}{2P^+} \bar{u}(p', s') \left[ H^q \gamma^+ + E^q \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} \right] u(p, s)$$

$$F_{q/\phi}^{[\gamma^+]}(x, \xi, t) = (1 - \xi^2) \int \frac{db^- dP_N^+}{\sqrt{1 - \xi_N^2}} \left( \frac{1 - \alpha}{\alpha} \right) \int d^2b_\perp d^2P_{N\perp} e^{-i[b^- \Delta^+ - \vec{b}_\perp \cdot \vec{\Delta}_\perp]}$$

$$\text{Unp} \times \left\{ \omega_0 \sqrt{1 - \xi_N^2} \left[ H_q(x', \xi_N, t) - \frac{\xi_N^2}{1 - \xi_N^2} E_q(x', \xi_N, t) \right] \right\}$$

$$(\vec{L} \cdot \vec{S}) + \frac{i\omega_1}{2m\sqrt{1 - \xi_N^2}} \left\{ (b_z)^{R.F.} [(\vec{\Delta}_\perp \cdot \vec{P}_{N\perp}) + 2\xi_N \vec{P}_{N\perp}^2] - (P_{N,z})^{R.F.} [(\vec{\Delta}_\perp \cdot \vec{b}_\perp) + 2\xi_N (\vec{P}_{N\perp} \cdot \vec{b}_\perp)] \right\} E_q(x', \xi_N, t)$$

$$(\vec{\Delta L} \cdot \vec{S}) + \frac{i\omega_2}{2m\sqrt{1 - \xi_N^2}} \left\{ (b_z)^{R.F.} [\vec{\Delta}_\perp^2 + 2\xi_N (\vec{P}_{N\perp} \cdot \vec{\Delta}_\perp)] - (\Delta_z)^{R.F.} [(\vec{\Delta}_\perp \cdot \vec{b}_\perp) + 2\xi_N (\vec{P}_{N\perp} \cdot \vec{b}_\perp)] \right\} E_q(x', \xi_N, t)$$

# Illustration: A Simple Model for ${}^4\text{He}$

- **Static, isotropic nucleus**

$$\omega_0(\vec{P}_N, \vec{b}) \stackrel{R.F.}{=} A_0 \theta(R - |\vec{b}|) \theta(P_N^{max} - |\vec{P}_N|)$$

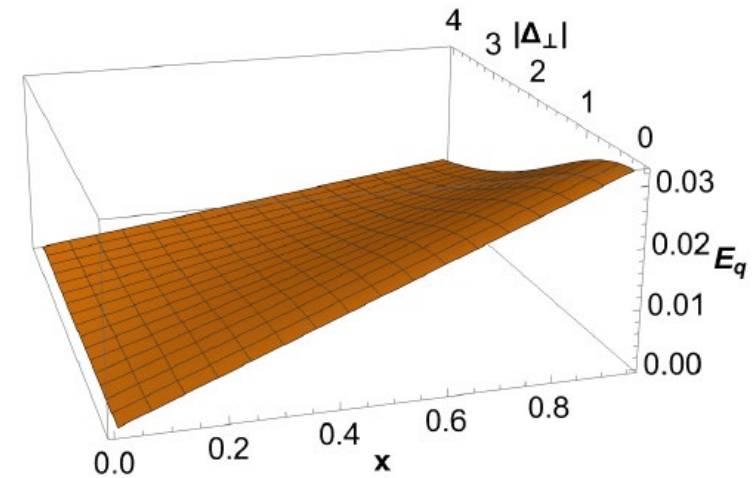
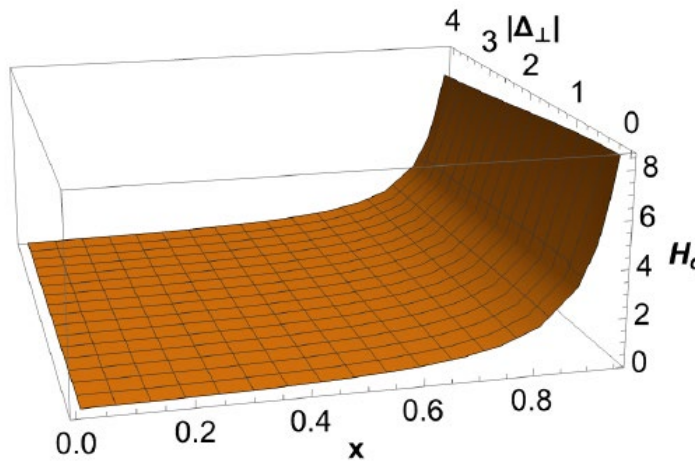
- **Ballpark  ${}^4\text{He}$  parameters**

$$R = 1.7 \text{ fm} \quad m = 1.0 \text{ GeV}$$

$$P_N^{max} = 0.12 \text{ GeV} \quad M = 4.0 \text{ GeV}$$

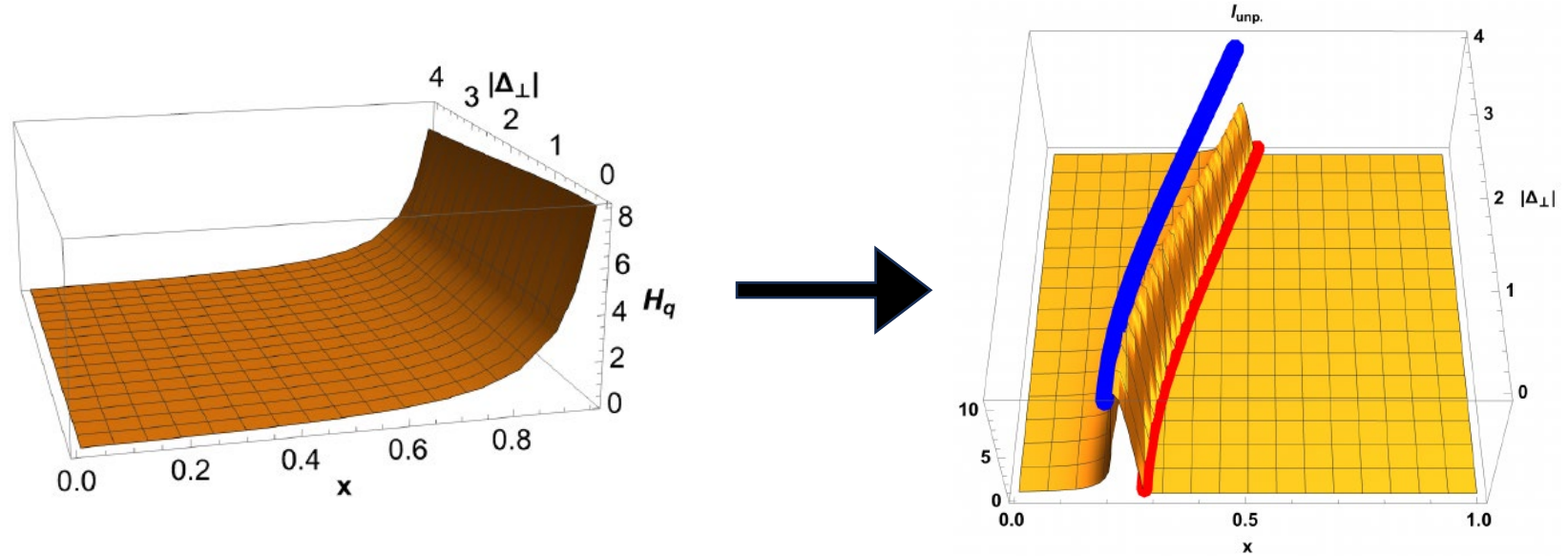
- **Quark Target Model GPDs at  $\xi = 0$**

*Meissner, Metz, Goeke, Phys. Rev. D 76 (2007)*



# Signatures of Nuclear Effects: Longitudinal Smearing

$$F_{q/\phi}^{[\gamma^+],unp} = A_0[\pi R^3][\pi(P_N^{max})^3] \\ \times \Phi_{unp}(|\vec{\Delta}_\perp|) \times \mathcal{I}_{unp}(x, |\vec{\Delta}_\perp|)$$



$$\Phi_{unp}(|\vec{\Delta}_\perp|) = \frac{4\Lambda}{|\vec{\Delta}_\perp|^3 R^3} [\sin(|\vec{\Delta}_\perp|R) - |\vec{\Delta}_\perp|R \cos(|\vec{\Delta}_\perp|R)]$$

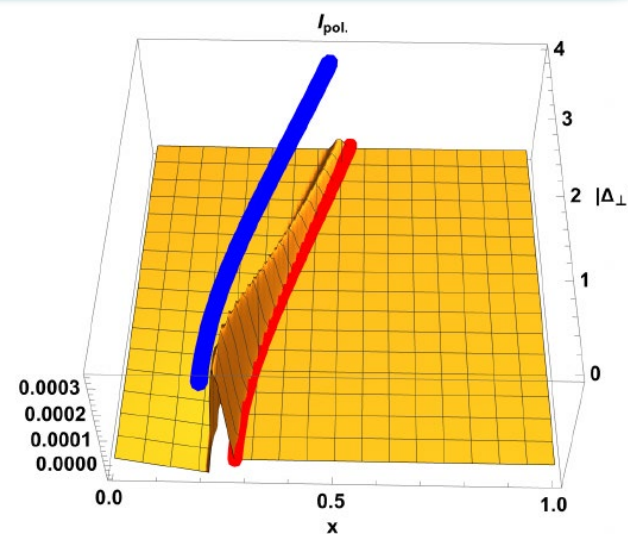
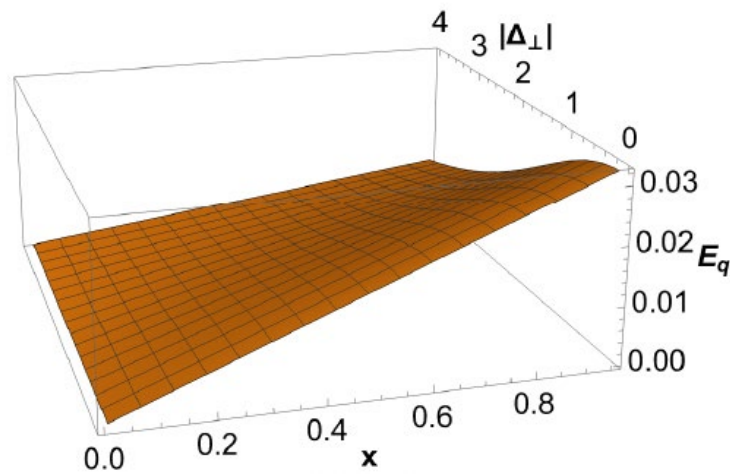
$$\mathcal{I}_{unp}(x, |\vec{\Delta}_\perp|) \equiv \frac{2}{(P_N^{max})^3} \int_0^{P_N^{max}} dP_{N\perp} P_{N\perp} \int_{\alpha_{min}}^{\alpha_{max}} d\alpha \left( \frac{1-\alpha}{\alpha} \right) H_q \left( \frac{x}{\alpha}, 0, -\vec{\Delta}_\perp^2 \right)$$

- Nuclear GPD is a **product of 2 factors** (reflects **factorized form of W**)
  - **Fourier Transform of spatial profile:**  $R \rightarrow \Delta$  dependence
  - **Longitudinal downshift and smearing:**  $P_z \rightarrow x$  dependence

$$\Delta \mathbf{x} = 2\sqrt{\frac{P_N^{max 2} + \lambda^2}{\Lambda^2}}$$

# Signatures of Nuclear Effects: Intermediate Polarization

$$F_{q/\phi}^{[\gamma^+],pol} = A_0[\pi R^3][\pi(P_N^{max})^3] \times \Phi_{pol}(|\vec{\Delta}_\perp|) \times \mathcal{I}_{pol}(x, |\vec{\Delta}_\perp|)$$



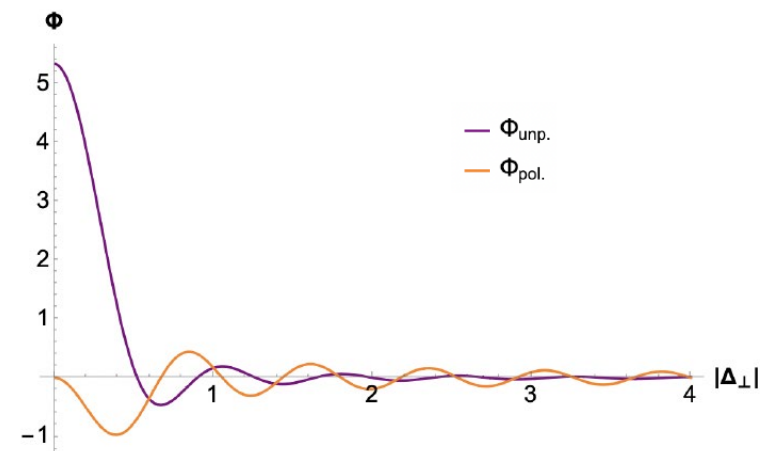
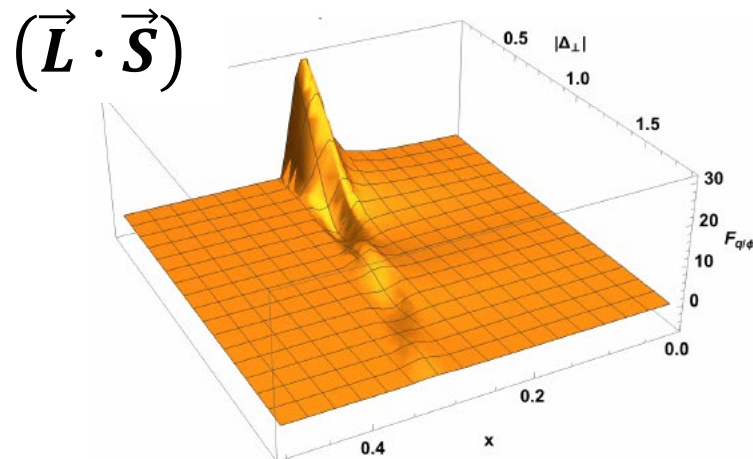
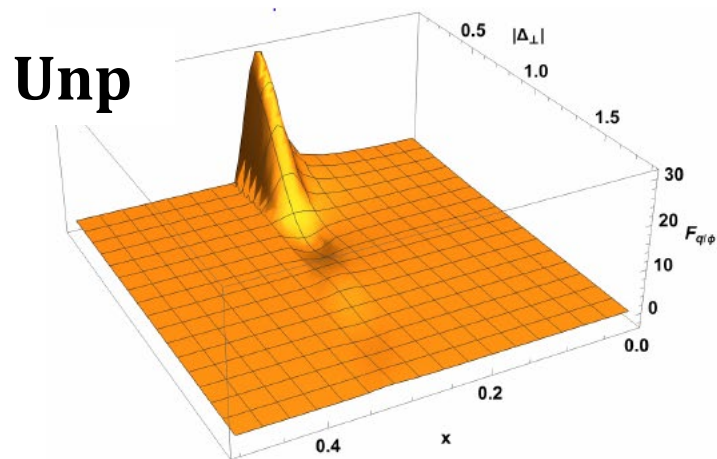
$$\Phi_{pol}(|\vec{\Delta}_\perp|) = \frac{4\Lambda}{|\vec{\Delta}_\perp|^3 R^3} \left[ 3R|\vec{\Delta}_\perp| \cos(R|\vec{\Delta}_\perp|) + (R^2|\vec{\Delta}_\perp|^2 - 3) \sin(R|\vec{\Delta}_\perp|) \right]$$

$$\mathcal{I}_{pol}(x, |\vec{\Delta}_\perp|) \equiv \frac{2}{P_N^{max3}} \int_0^{P_N^{max}} dP_{N\perp} P_{N\perp} \int_{\alpha_{min}}^{\alpha_{max}} d\alpha \left( \frac{1-\alpha}{\alpha} \right) E_q \left( \frac{x}{\alpha}, 0, -\vec{\Delta}_\perp^2 \right) \times \left\{ \beta_1 \frac{\Lambda}{4m\alpha} \left[ \alpha^2 - \frac{\vec{P}_{N\perp}^2 + \lambda^2}{\Lambda^2} \right] \right\}$$

- If  $(\vec{L} \cdot \vec{S})$  correlation is present, it couples to GPD E to generate mixing
  - Different spatial Fourier transform
  - Longitudinal downshift and smearing

QTM:  $E \propto m \ll H$

# Unpolarized vs. Polarized Channels



- Artificially scale up  $E \sim H$  and compare shapes:
  - **Qualitatively similar:** Fourier Transform, downshift, smearing
  - Spin-orbit correlations **change the  $\Delta$  dependence** and **shift the nodes**
- First steps toward theory guidance and interpretation for ALERT

# Conclusion

- **This Work:**

Further theoretical developments on **light-front impulse approximation** in **Wigner representation**

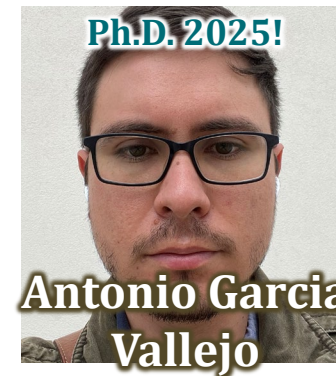
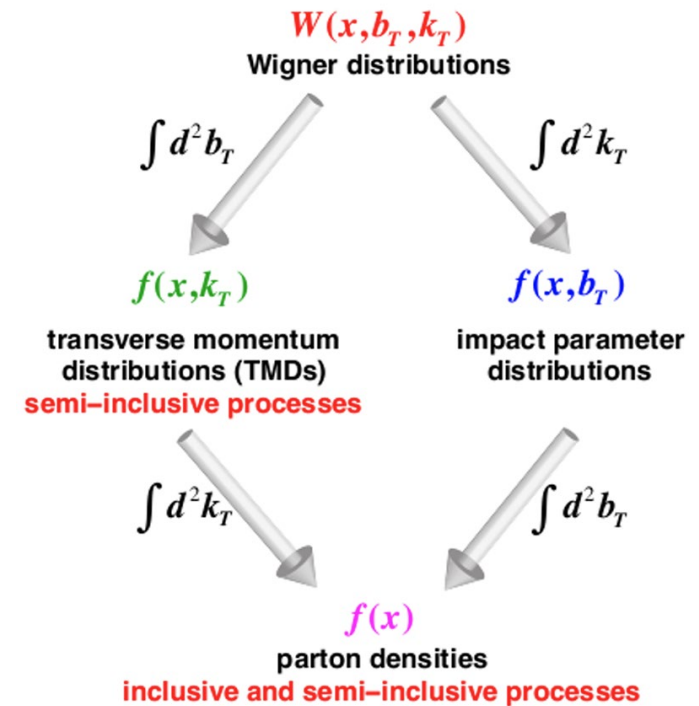
General formalism applies to **full family of matrix elements**

**First application to GPDs**, revealing **novel  $\overline{\Delta L} \cdot \vec{S}$  mixing channels** in exclusive processes

Illustrative **toy phenomenology for  $^4\text{He}$**

- **Next Steps:**

Application to a **TMDs of a composite spin-1 target** for SIDIS on tensor-polarized deuterium



❖ **Next talk!**

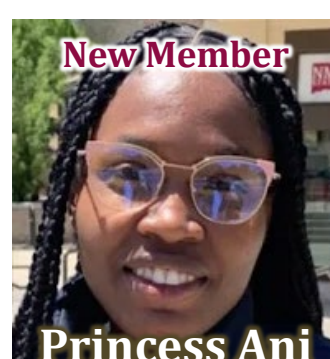
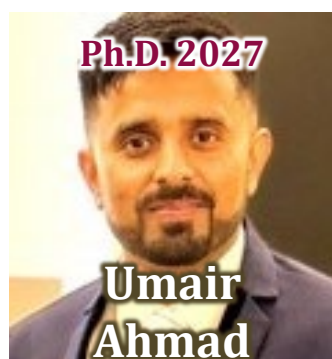
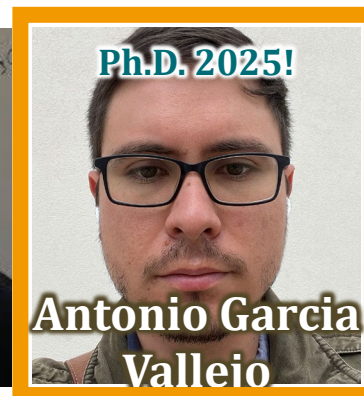
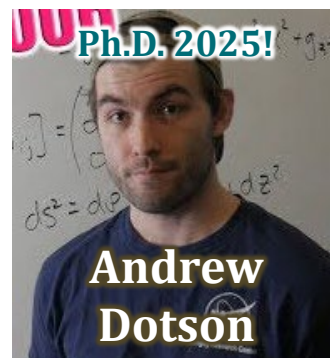
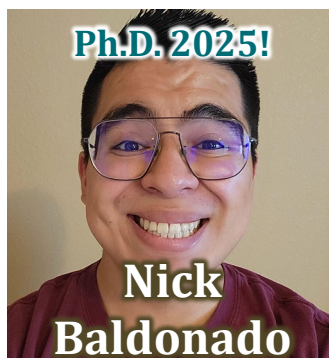
**Thurs. 6/4,**  
**11:25am**

Thank You!

# The Sievert Group(s) at NMSU

## Hot QCD

## Cold QCD



## This Work



Physics Education Research

# Backup Slides

# Center of Momentum of a Relativistic System

$$R_E^\mu \equiv \frac{1}{p^0} \int d^3x x^\mu T^{00}(x)$$

$$R_*^\mu \equiv R_E^\mu \text{ if } \vec{p} = 0$$

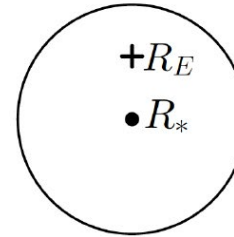
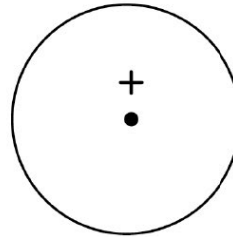
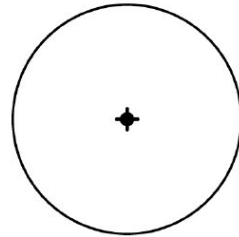
(rest frame)

$$R_{LF}^\mu \equiv \frac{1}{p^+} \int d^2x_\perp dx^- x^\mu T^{++}(x)$$

$$\vec{R}_E - \vec{R}_* = \frac{\vec{p} \times \vec{W}}{p^0 m^2}$$

$$R_{LF}^\mu - R_*^\mu = -\frac{\varepsilon^{\mu\alpha\beta+} W_\alpha p_\beta}{m^2 p^+}$$

IFF

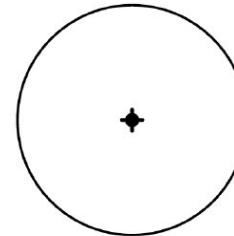
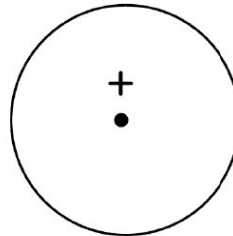
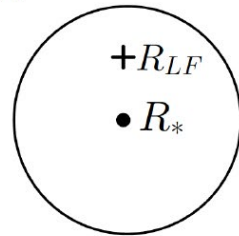


$\odot \vec{L}$

• Text

Center of  
+ energy  
• mass

LFF



Rest frame

Moving frame

Infinite-momentum frame

# Center of Momentum of a Relativistic System

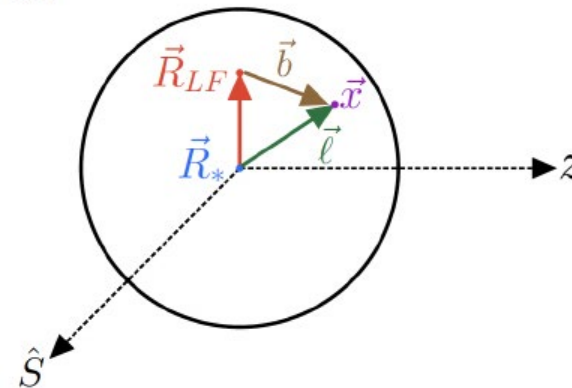
$$b^\mu \equiv x^\mu - R_{LF}^\mu,$$

$$\ell^\mu \equiv x^\mu - R_*^\mu,$$

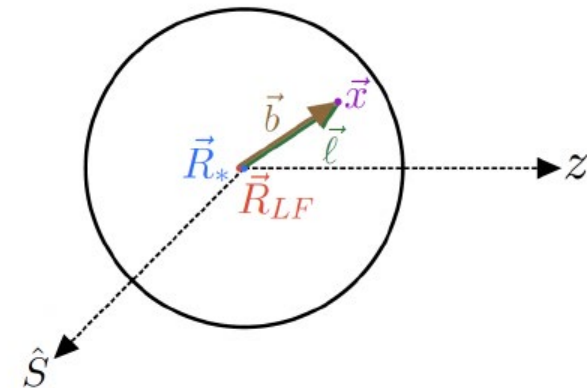
$$b^\mu = \ell^\mu - (R_{LF}^\mu - R_*^\mu)$$

$$P^+ b^- \stackrel{IMF}{=} P^+ \ell^- = -\sqrt{\frac{\Lambda^2}{1-\xi^2}} (\ell_z)^{RF}$$

LFF



Rest frame



Infinite-momentum frame