

# Measurement of the Generalized Polarizabilities of the Proton in Virtual Compton Scattering

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# Scalar Polarizabilities

Fundamental structure constants  
(such as mass, size, shape, ...)

Response of internal structure  
& dynamics to external EM field

Sensitive to the full excitation  
spectrum of the nucleon (contrary  
to the elastic FFs)

Accessed experimentally through  
Compton Scattering processes

Virtual Compton Scattering:

Virtuality of photon gives access to the  
Generalized Polarizabilities  $\alpha_E(Q^2)$  &  $\beta_M(Q^2)$

→ mapping out the spatial distribution of  
the polarization densities

Fourier transform of densities of electric charges and  
magnetization of a nucleon deformed by an applied EM field

PDG

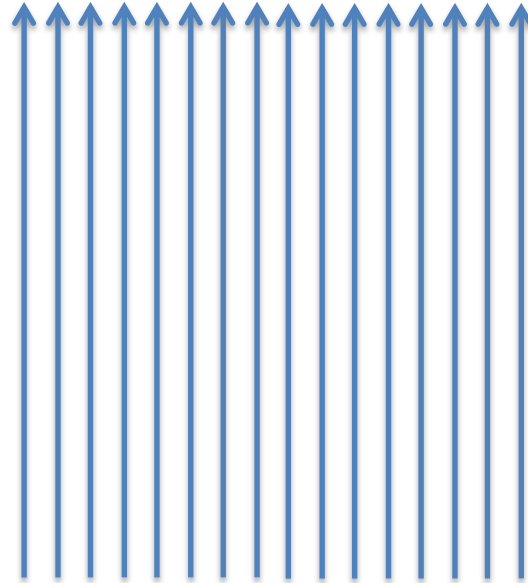
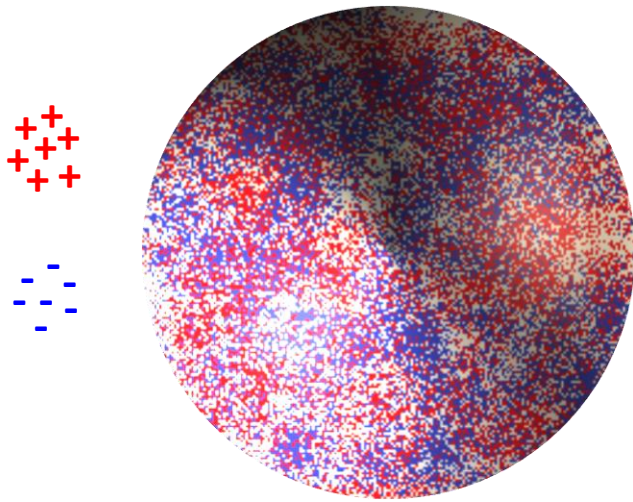
150 Baryon Summary Table

<b><math>N</math> BARYONS</b> <b><math>(S = 0, I = 1/2)</math></b> $p, N^+ = uud; \quad n, N^0 = udd$
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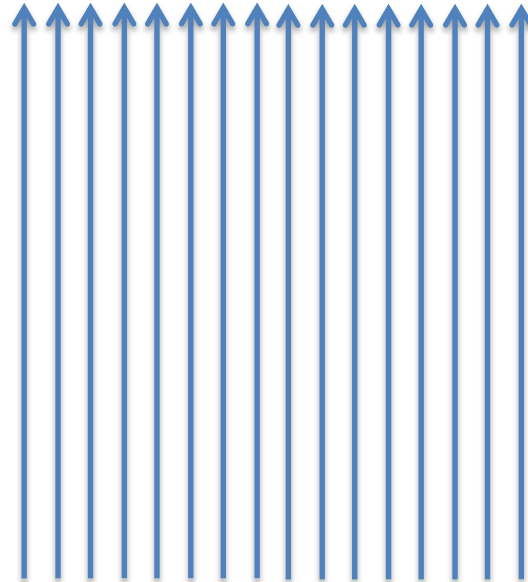
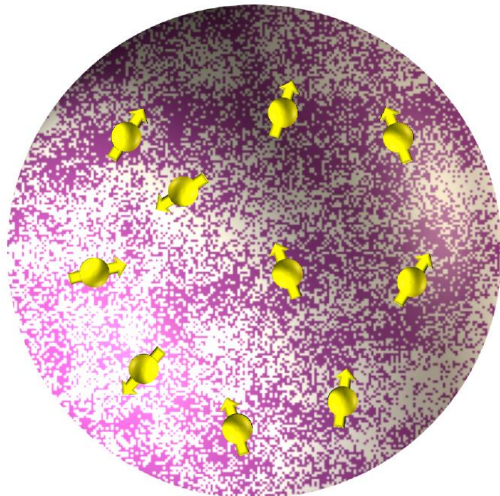
<b><math>p</math></b>	$I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$
Mass $m = 1.00727646681 \pm 0.00000000009$ u	
Mass $m = 938.272046 \pm 0.000021$ MeV [a]	
$ m_p - m_{\bar{p}} /m_p < 7 \times 10^{-10}$ , CL = 90% [b]	
$ \frac{q_p}{m_p} /(\frac{q_e}{m_e}) = 0.99999999991 \pm 0.00000000009$	
$ q_p + q_{\bar{p}} /e < 7 \times 10^{-10}$ , CL = 90% [b]	
$ q_p + q_e /e < 1 \times 10^{-21}$ [c]	
Magnetic moment $\mu = 2.792847356 \pm 0.000000023$ $\mu_N$	
$(\mu_p + \mu_{\bar{p}}) / \mu_p = (0 \pm 5) \times 10^{-6}$	
Electric dipole moment $d < 0.54 \times 10^{-23}$ e cm	
Electric polarizability $\alpha = (11.2 \pm 0.4) \times 10^{-4}$ fm <sup>3</sup>	
Magnetic polarizability $\beta = (2.5 \pm 0.4) \times 10^{-4}$ fm <sup>3</sup> ( $S = 1.2$ )	
Charge radius, $\mu p$ Lamb shift = $0.84087 \pm 0.00039$ fm [d]	
Charge radius, $e p$ CODATA value = $0.8775 \pm 0.0051$ fm [d]	
Magnetic radius = $0.777 \pm 0.016$ fm	
Mean life $\tau > 2.1 \times 10^{29}$ years, CL = 90% [e] ( $p \rightarrow$ invisible mode)	
Mean life $\tau > 10^{31}$ to $10^{33}$ years [e] (mode dependent)	

# Scalar Polarizabilities

Response of internal structure to an applied EM field



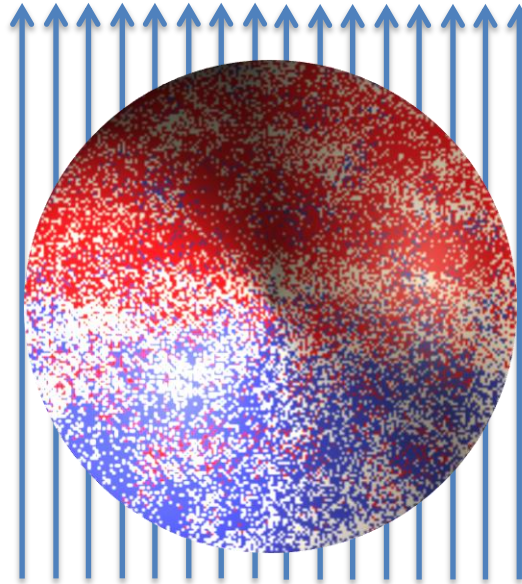
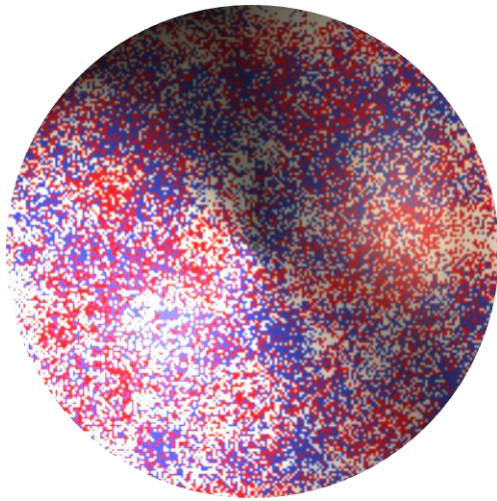
$\vec{E}$



$\vec{B}$

# Scalar Polarizabilities

Response of internal structure to an applied EM field

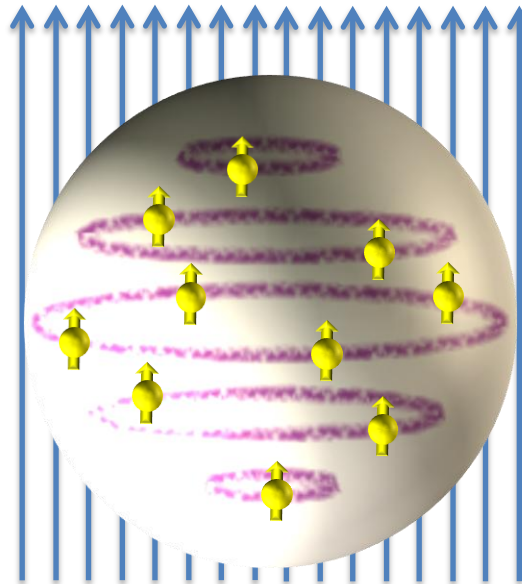
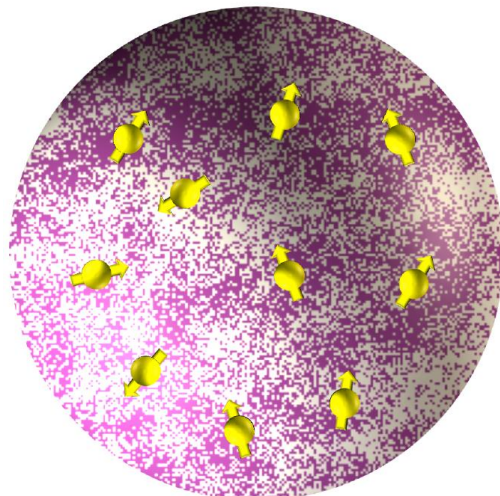


$\vec{E}$

“stretchability”

$$\vec{d}_{E \text{ induced}} \sim \alpha \vec{E}$$

External field deforms the charge distribution



$\vec{B}$

“alignability”

$$\vec{d}_{M \text{ induced}} \sim \beta \vec{B}$$

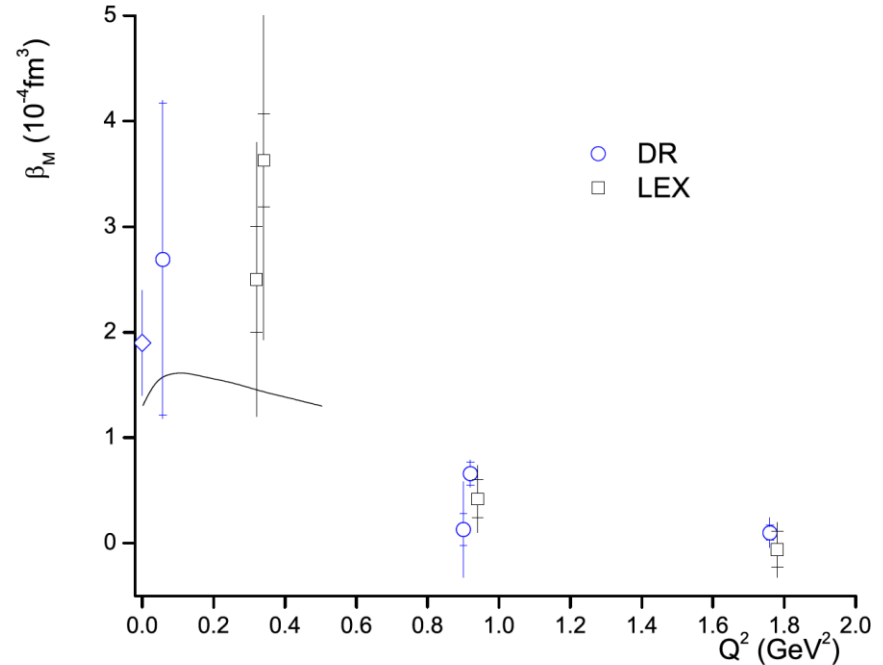
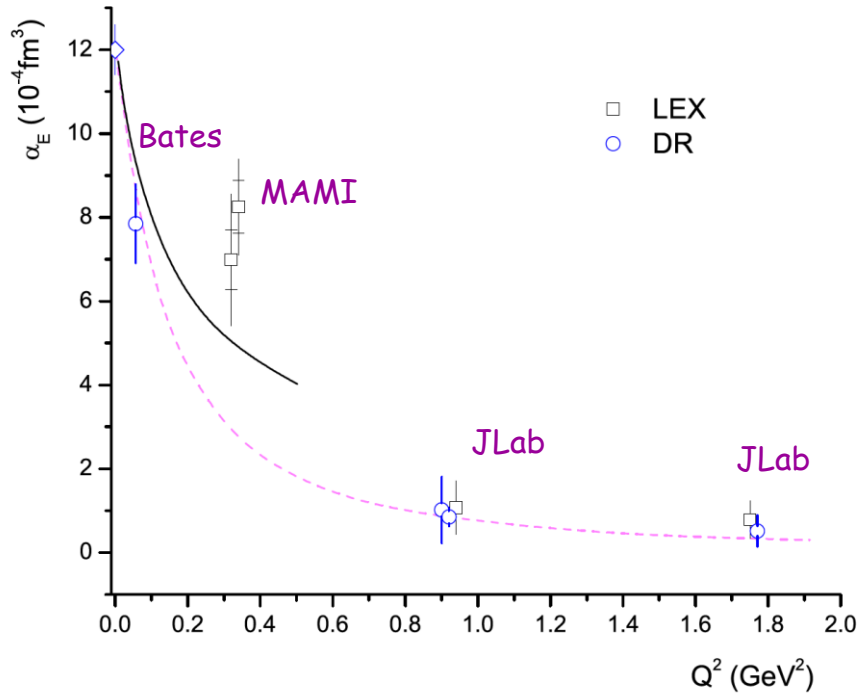
$$\beta_{\text{para}} > 0$$

$$\beta_{\text{diam}} < 0$$

Paramagnetic: proton spin aligns with the external magnetic field

Diamagnetic:  $\pi$ -cloud induction produces field counter to the external one

# Experimental Landscape



$a_E \approx 10^{-3} V_N$  (stiffness / relativistic character)

Data suggest non-trivial  $Q^2$  evolution of  $a_E$

Current theoretical calculations not able to describe the enhancement at low  $Q^2$

$Q^2 = 0.33 \text{ (GeV/c)}^2$  measured twice at MAMI:

- Phys. Rev. Lett 85, 708 (2000)
- Eur. Phys. J. A37, 1-8 (2008)

$\beta_M$  small  $\leftrightarrow$  cancellation of competing mechanisms

Large uncertainties

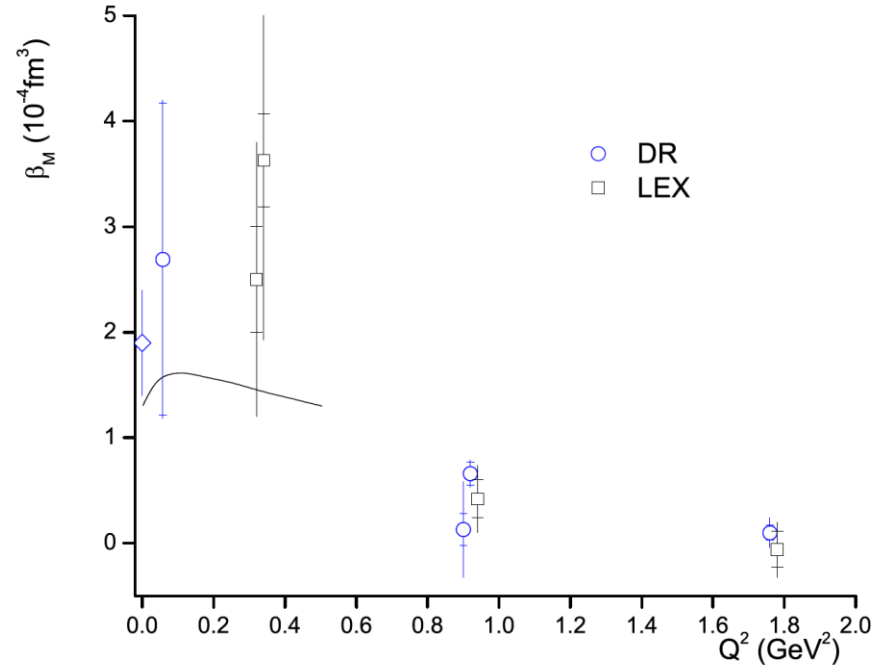
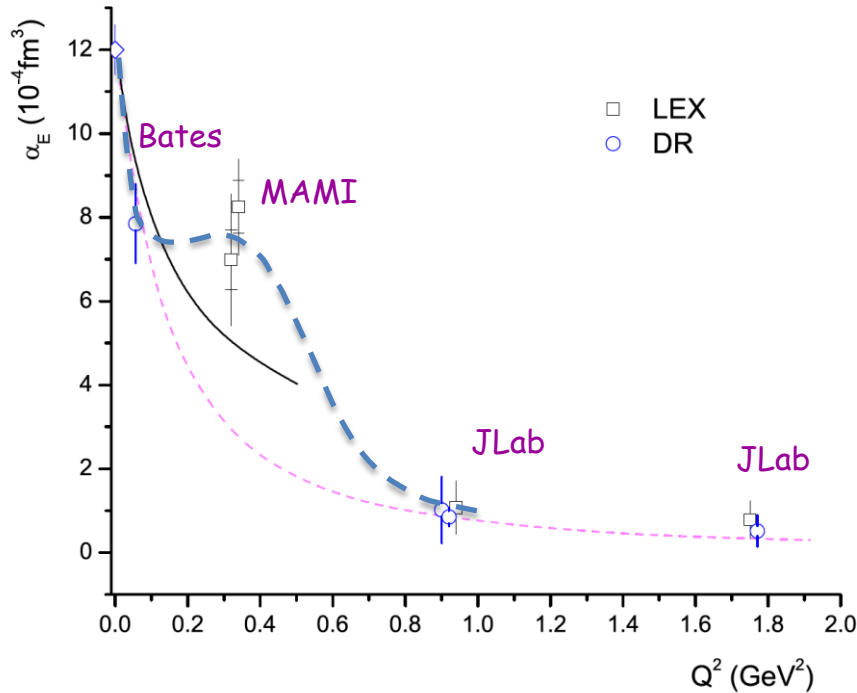
Higher precision measurements needed

$\rightarrow$  Quantify the balance between diamagnetism and paramagnetism

Current situation unsatisfactory:

- more measurements needed (vs  $Q^2$ )
- Higher precision measurements needed

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Current theoretical calculations not able to describe the enhancement at low  $Q^2$

$Q^2 = 0.33$  ( $\text{GeV}/c$ )<sup>2</sup> measured twice at MAMI:

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Large uncertainties

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→ Quantify the balance between diamagnetism and paramagnetism

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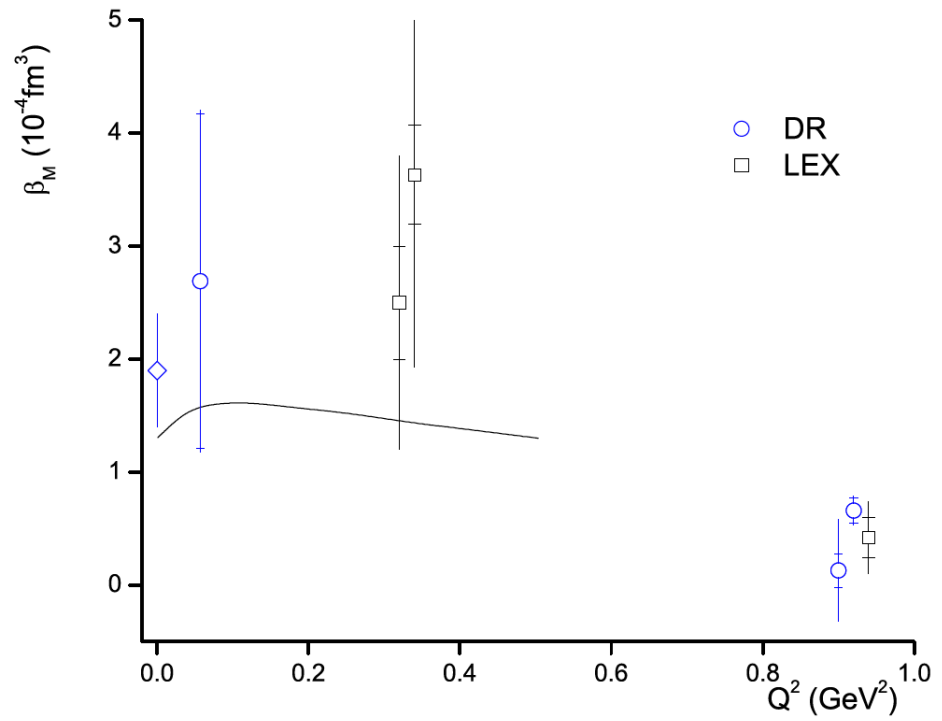
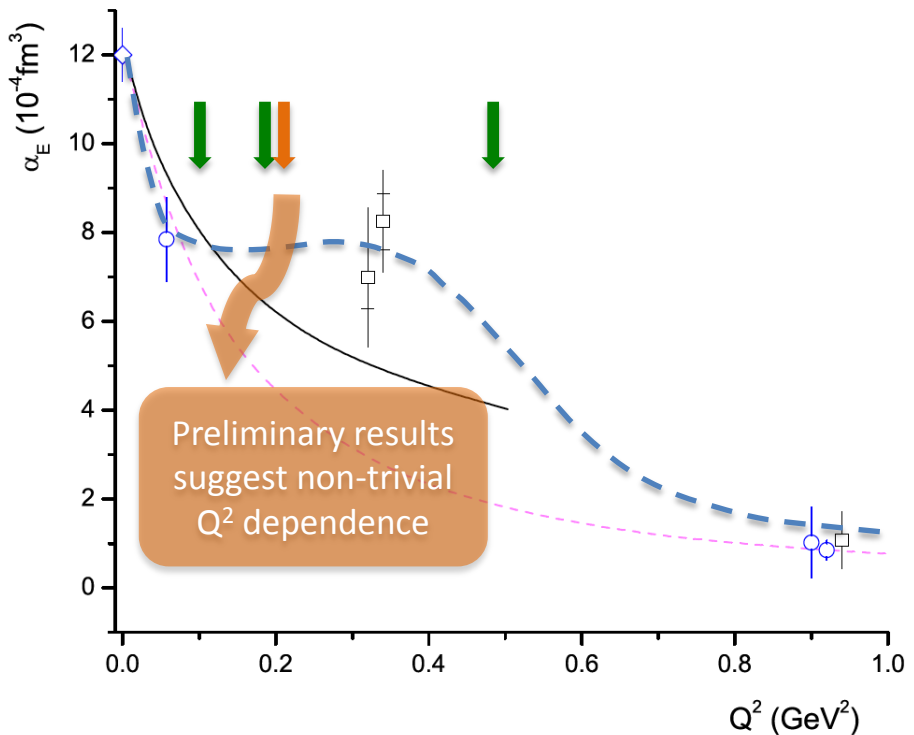
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# Ongoing Experiments

MAMI	A1/1-09	Fonvieille et al	VCS below threshold	data analysis ongoing
MAMI	A1/3-12	Sparveris et al	VCS above threshold	data analysis ongoing

new MAMI measurements competitive / comparable to the  $Q^2=0.33$  (GeV/c)<sup>2</sup> measurement

MAMI constraints  $Q^2 < 0.5$  (GeV/c)<sup>2</sup>



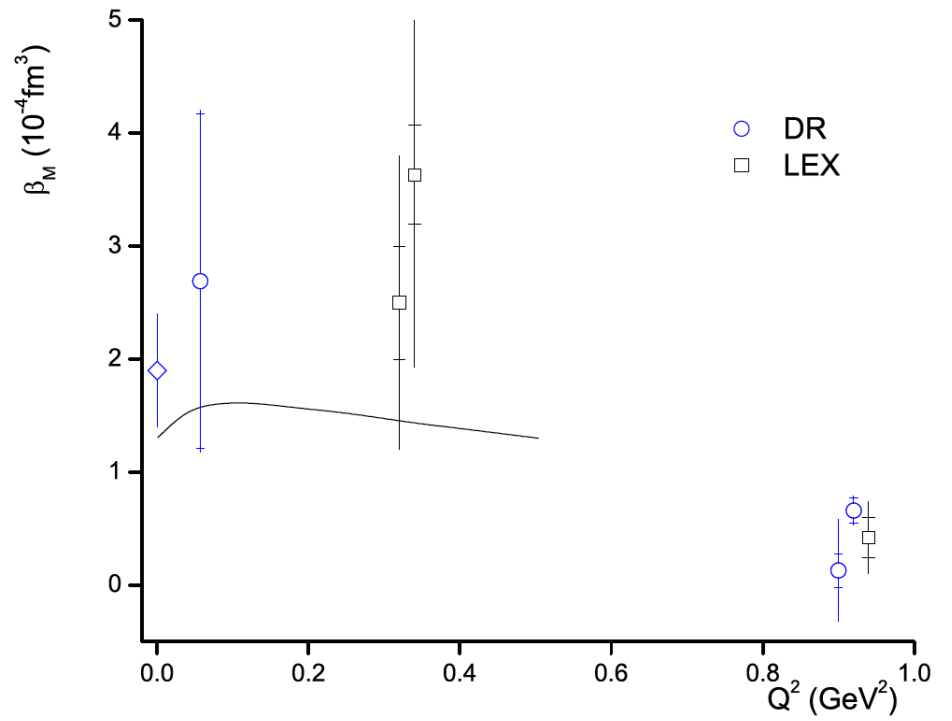
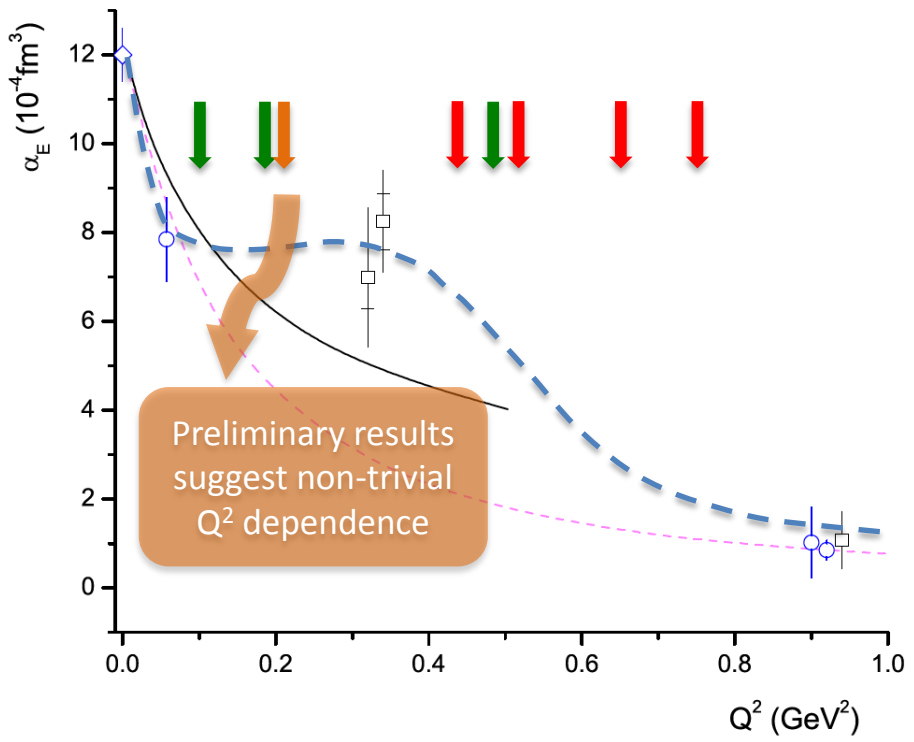
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Jlab This proposal





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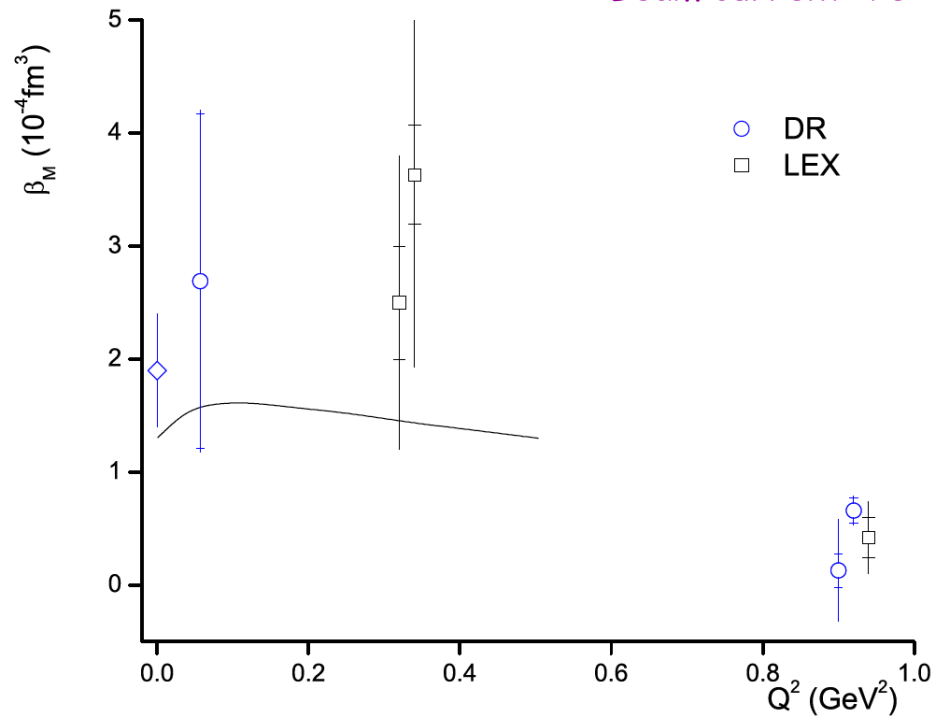
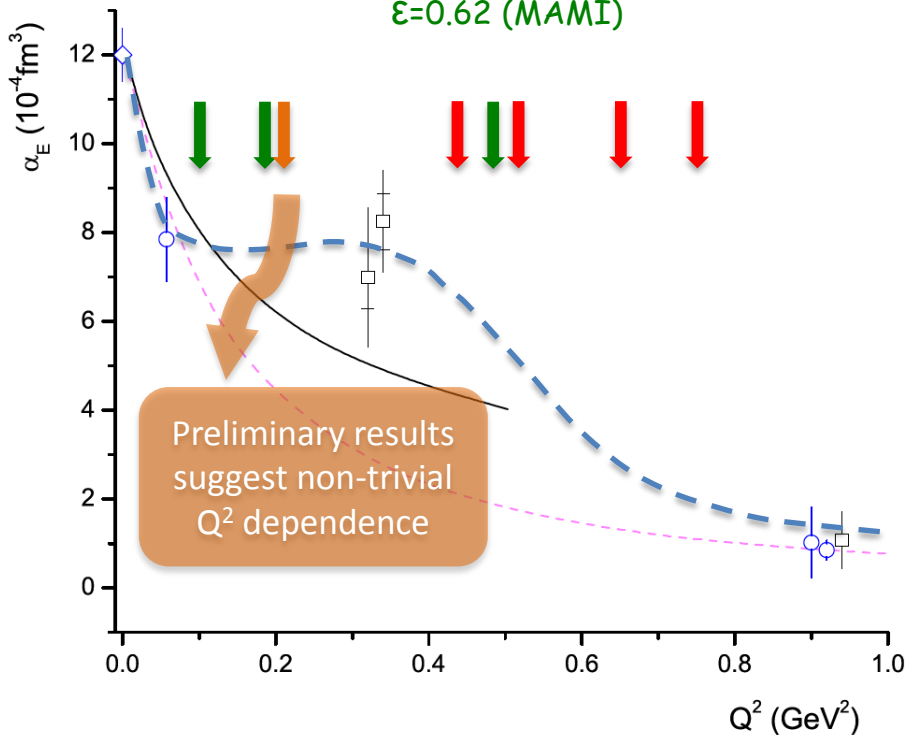
MAMI constraints  $Q^2 < 0.5$  (GeV/c)<sup>2</sup>

## Jlab This proposal

Going from  $\epsilon = 0.6 \rightarrow 0.9$  doubles the sensitivity to the GPs

$\epsilon=0.97$  (Jlab)  
 $\epsilon=0.62$  (MAMI)

additional + :  
 Beam energy x 4  
 Beam current x 5



# Theoretical Landscape

HBChPT

NRQCM

Effective Lagrangian Model

Linear Sigma Model

T.R. Hemmert et al

Phys. Rev. D 62, 014013 (2000)

B. Pasquini et al

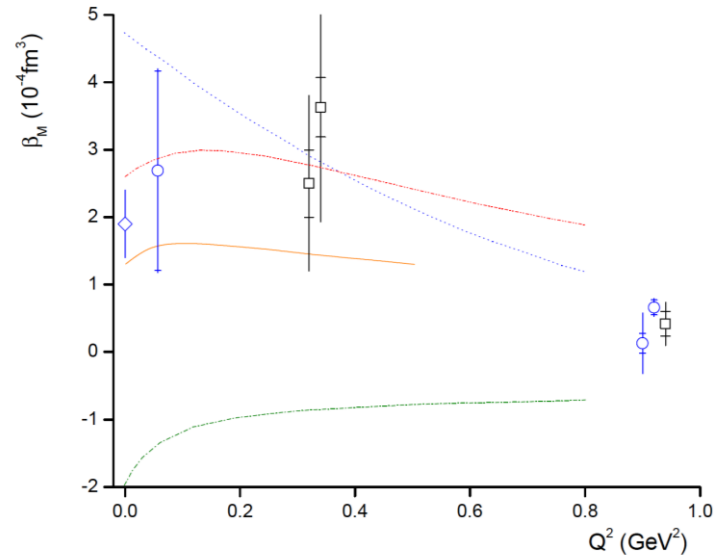
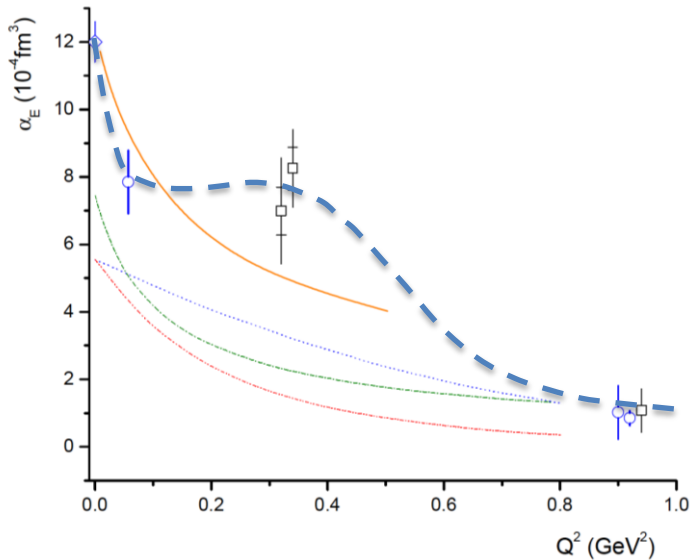
Phys. Rev. C 63, 025205 (2001)

A. Yu. Korchin and O. Scholten

Phys. Rev. C 58, 1098 (1998)

A. Metz and D. Drechsel

Z. Phys. A 356, 351 (1996)



All theoretical calculations predict a smooth fall off for  $\alpha_E$

None of the models can account for the non trivial structure of  $\alpha_E$  suggested by the data

**Lattice QCD**

Currently:

$Q^2=0$  calculations exist but at unphysical quark masses

Near Future:

calculations at the physical point for  $Q^2=0$

first calculations for  $Q^2 \neq 0$

# Spatial dependence of induced polarizations in an external EM field

Nucleon form factor data → light-front quark charge densities

Formalism extended to the deformation of these quark densities when applying an external e.m. field:

GPs → spatial deformation of charge & magnetization densities under an applied e.m. field

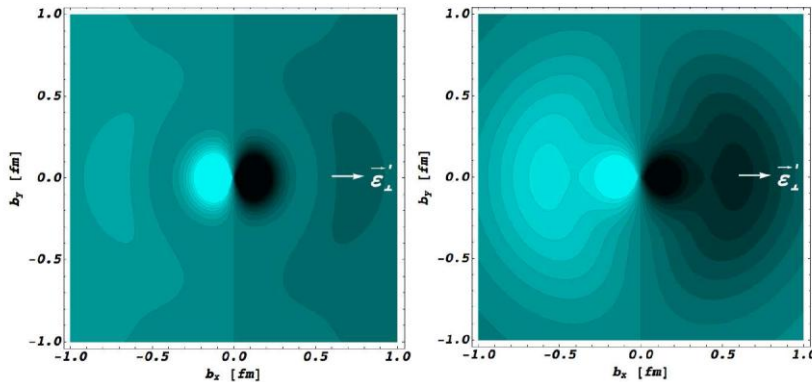
## Induced polarization in a proton when submitted to an e.m. field

Phys. Rev. Lett. 104, 112001 (2010)

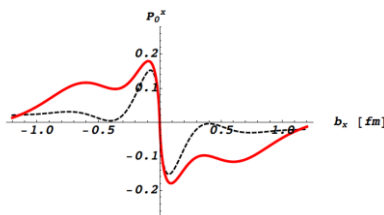
M. Gorchtein, C. Lorce, B. Pasquini, M. Vanderhaeghen

GP I

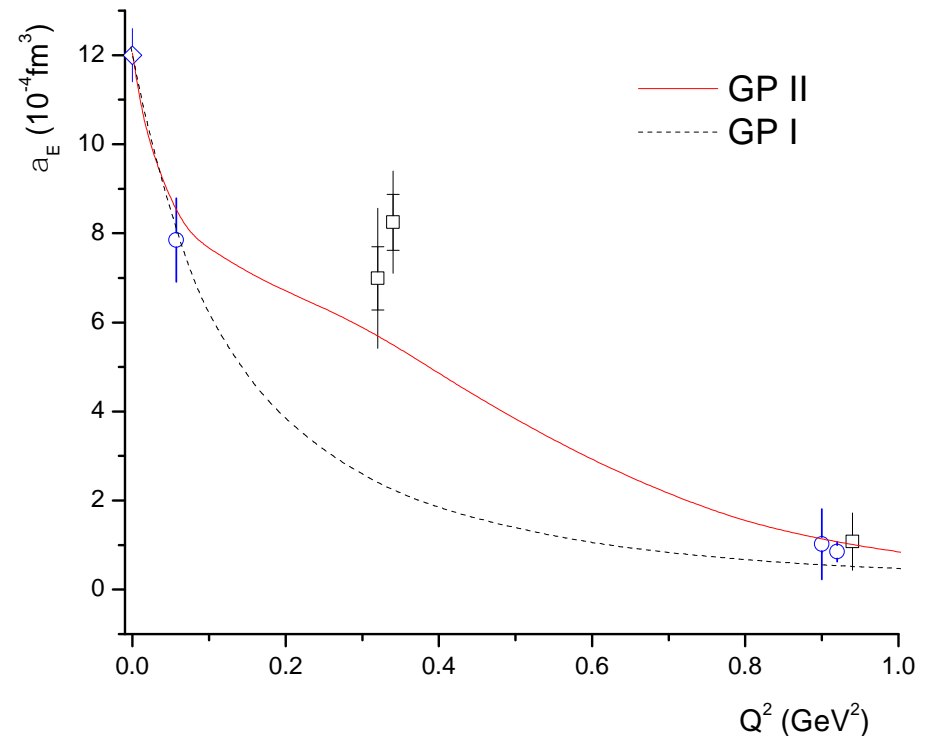
GP II



Light (dark) regions → largest (smaller) values  
(photon polarization along x-axis, as indicated)



Induced polarization along  $b_y=0$



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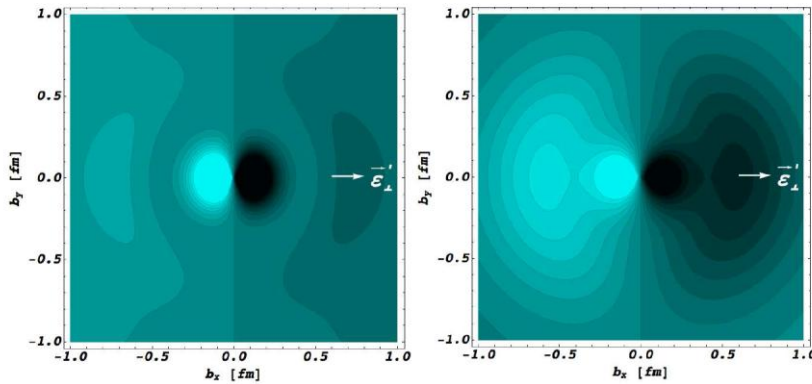
## Induced polarization in a proton when submitted to an e.m. field

Phys. Rev. Lett. 104, 112001 (2010)

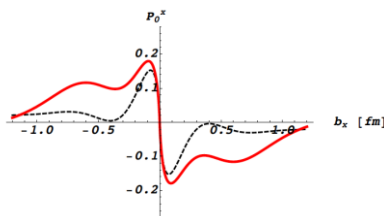
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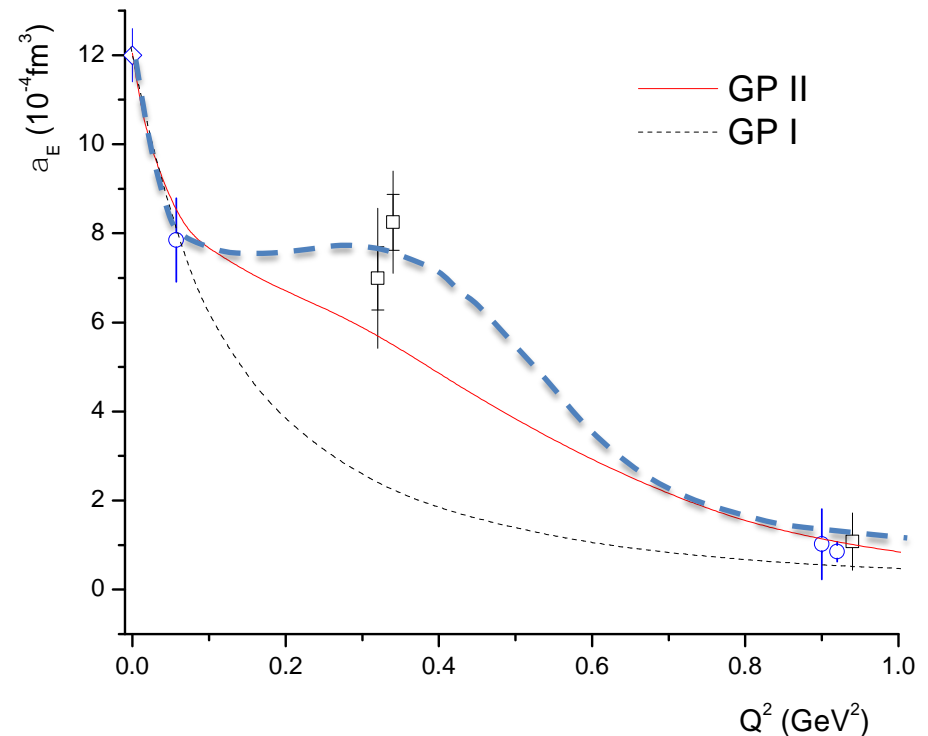
GP II



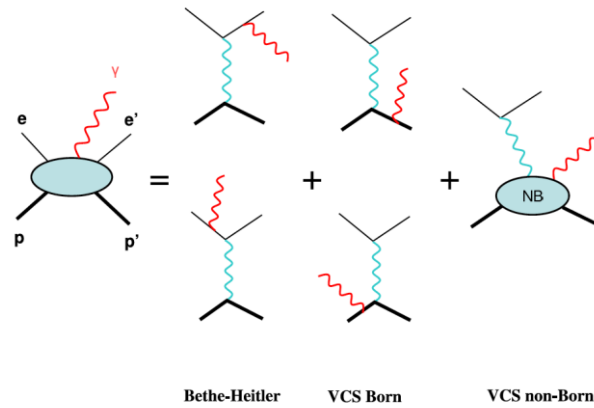
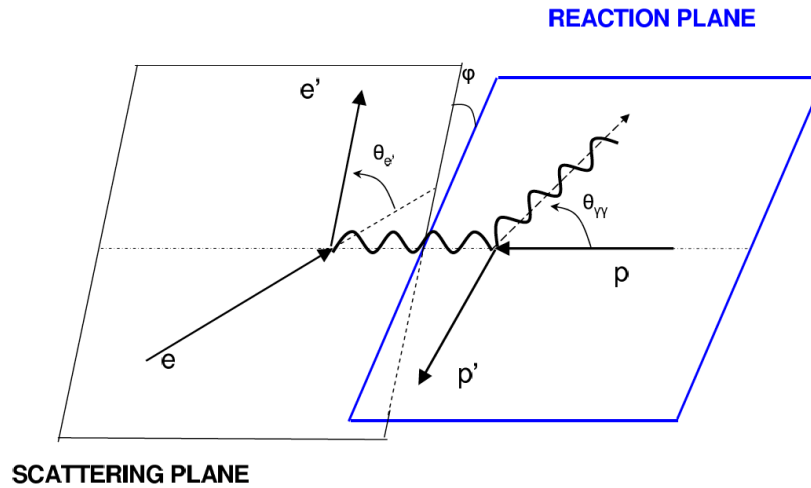
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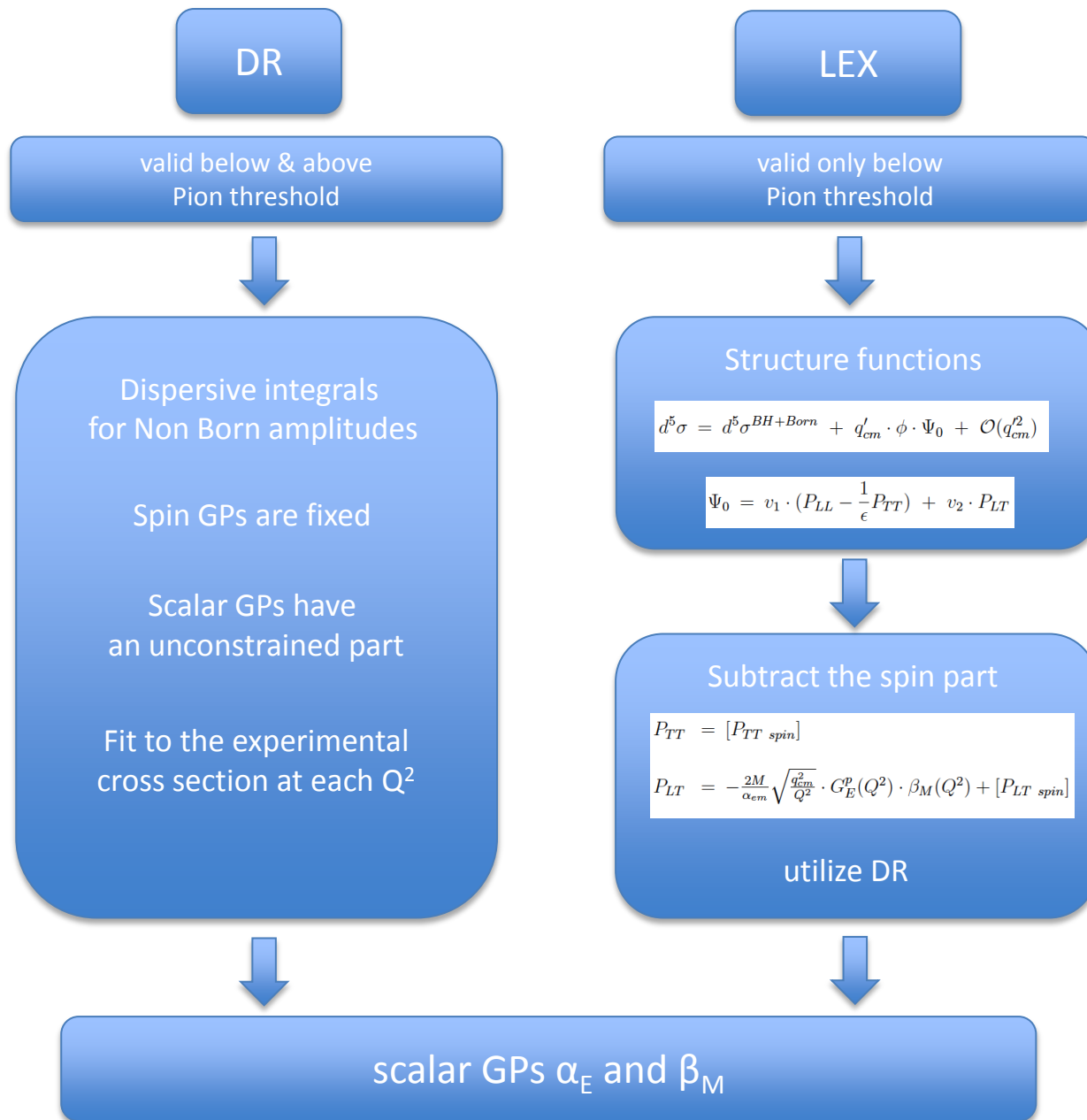
# Virtual Compton Scattering



Elastic FFs

GPs

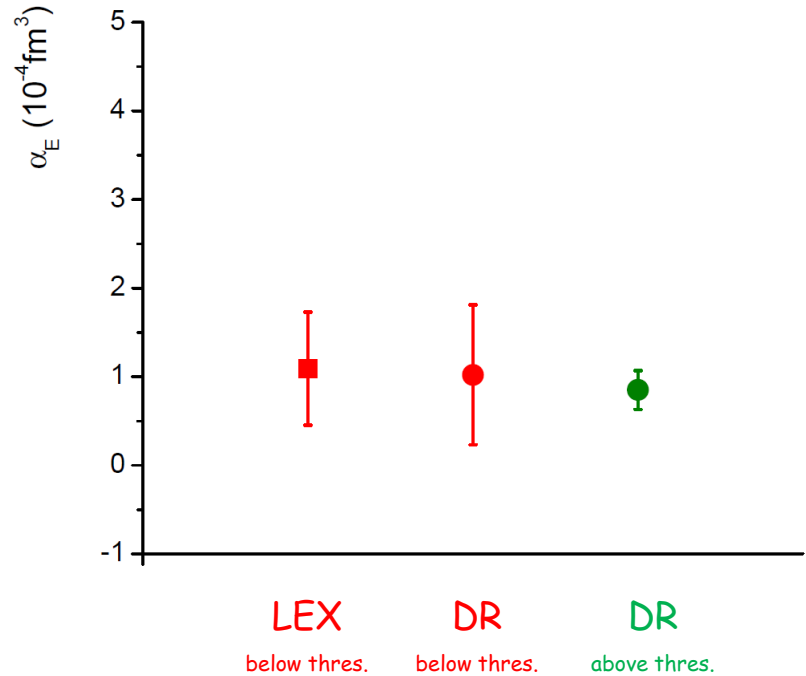
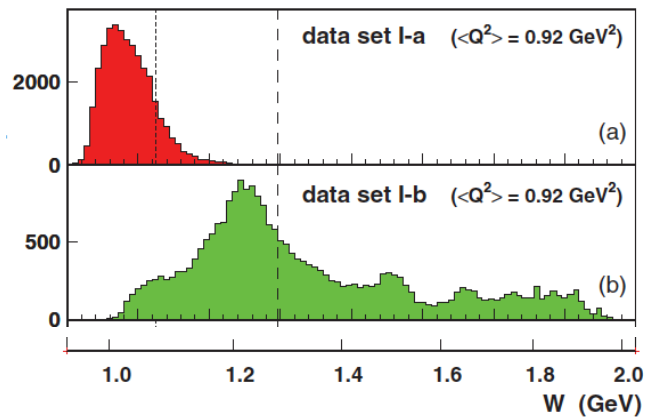
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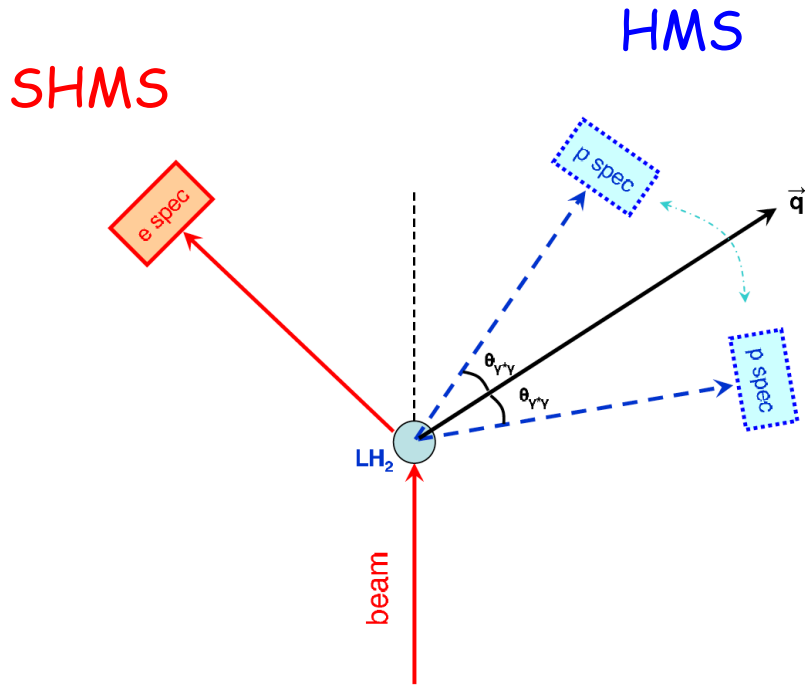
Phys. Rev C 86, 015210 (2012)

Phys. Rev Lett. 93, 122001 (2004)



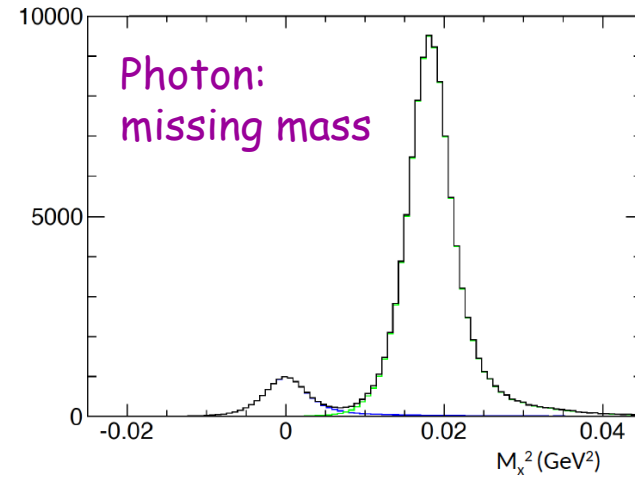
Sensitivity to the GPs grows with the photon energy

# Experimental Setup



Hall C: SHMS, HMS  
 4.4 GeV  
 45-85  $\mu$ A  
 Liquid hydrogen 15 cm

e & p detection in coincidence



cross sections

in-plane azimuthal asymmetries

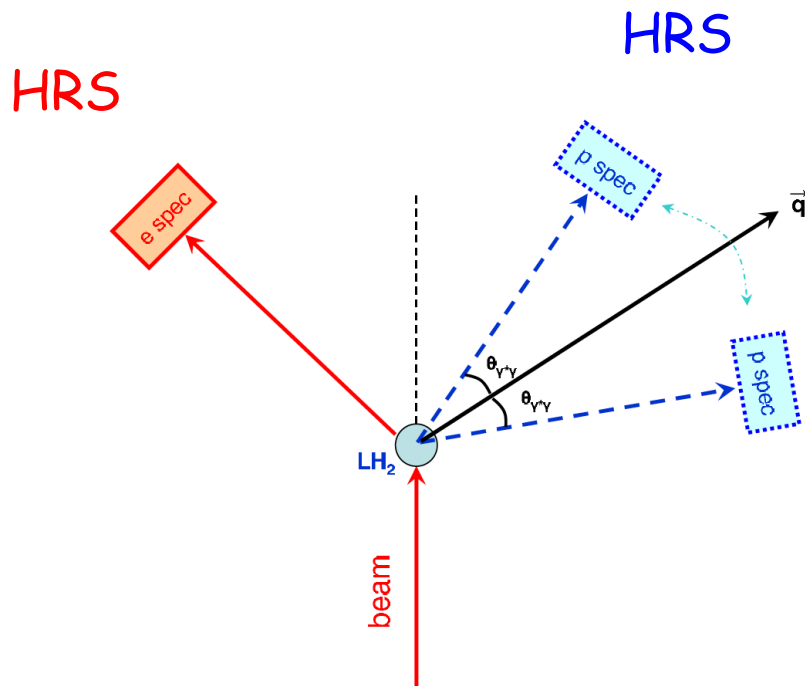
$$A_{(\phi_{\gamma^*\gamma}=0,\pi)} = \frac{\sigma_{\phi_{\gamma^*\gamma}=0} - \sigma_{\phi_{\gamma^*\gamma}=180}}{\sigma_{\phi_{\gamma^*\gamma}=0} + \sigma_{\phi_{\gamma^*\gamma}=180}}$$

sensitivity to GPs

suppression of systematic asymmetries



# Experimental Setup



## Hall A (?)

HRS min. angle = 12.5 deg

Can not run Part I with 4.4 GeV

Run Part I with a lower beam energy

Part I with 3.3 GeV:

- Reduced sensitivity to GPs
- Smaller cross section

→  $\delta\alpha_E$  increased by 16.5%

(still very competitive measurement)

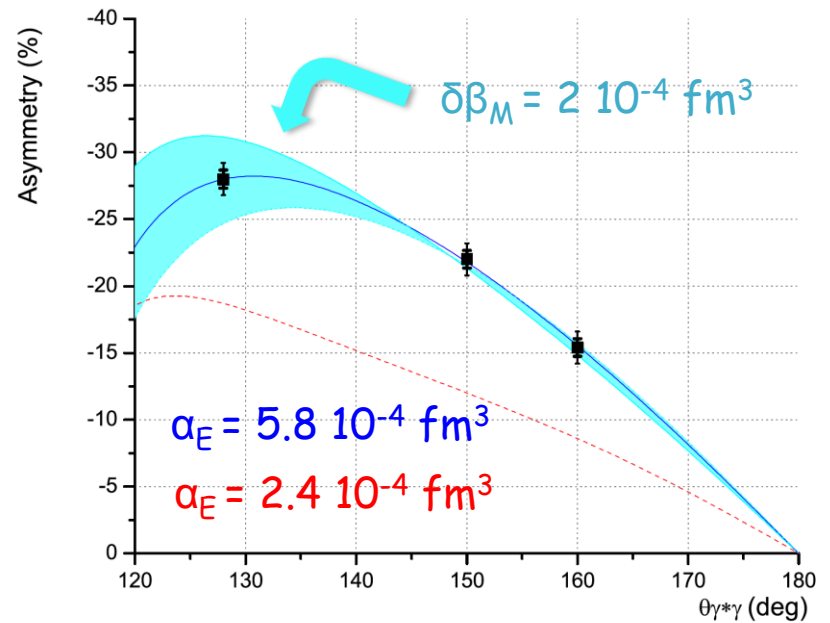
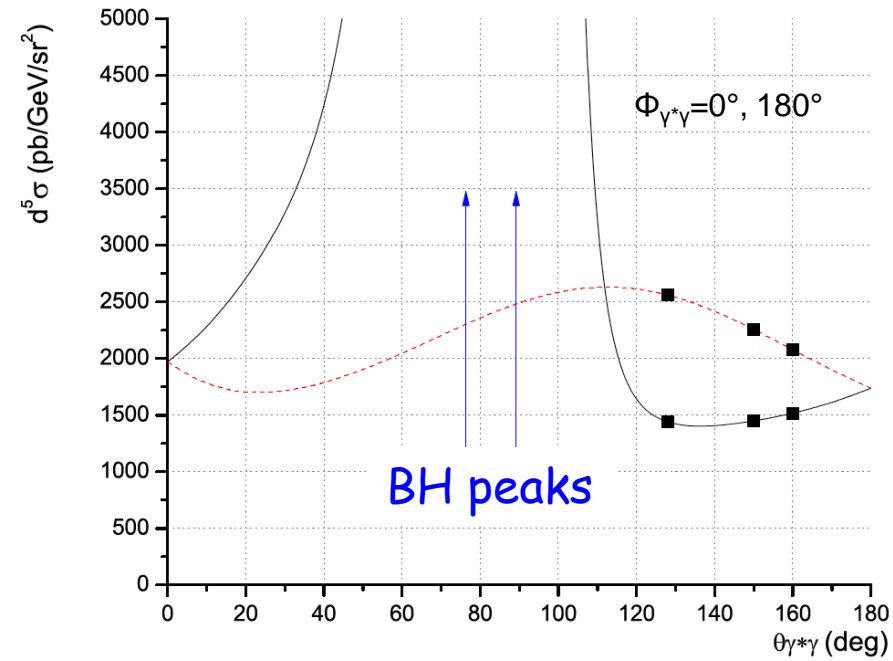
Hall A: HRS(e), HRS(p)  
3.3 GeV 3.5 days  
4.4 GeV 10.5 days

Will not be able to allow for the maximum beam energy to another Hall during Part I (3.5 days)

The high  $Q^2$  Jlab measurements (E93-050) were done in Hall A with the two HRSs, a 15 cm LH2 target, and a 4 GeV beam

# Measurements

$$Q^2 = 0.43 \text{ (GeV/c)}^2$$



avoid BH peaks  
stay at  $\theta_{V^*\gamma} > 120^\circ$

# Measurements

	Kinematical Setting	$\theta_{\gamma^*\gamma}^\circ$	$\theta_e^\circ$	$P'_e(\text{MeV}/c)$	$\theta_p^\circ$	$P'_p(\text{MeV}/c)$	S/N	beam time (days)
Part I	Kin Ia	165	9.39	3820.5	40.85	1010.40	1.3	0.5
	Kin Ib	165	9.39	3820.5	48.45	1010.40	2.4	0.5
	Kin IIa	155	9.39	3820.5	38.34	995.20	1	0.5
	Kin IIb	155	9.39	3820.5	50.96	995.20	3.2	0.5
	Kin IIIa	128	9.39	3820.5	31.84	919.43	0.7	0.95
	Kin IIIb	128	9.39	3820.5	57.46	919.43	7.8	0.55
Part II	Kin IVa	165	11.54	3708.6	40.81	1175.25	2.6	1.5
	Kin IVb	165	11.54	3708.6	47.35	1175.25	5	2
	Kin Va	160	11.54	3708.6	39.73	1167.72	2.2	1.5
	Kin Vb	160	11.54	3708.6	48.43	1167.72	6.3	2
	Kin VIa	140	11.54	3708.6	35.52	1117.38	1.2	1.5
	Kin VIb	140	11.54	3708.6	52.64	1117.38	8	2

Part I 3.5 days

Part II 10.5 days

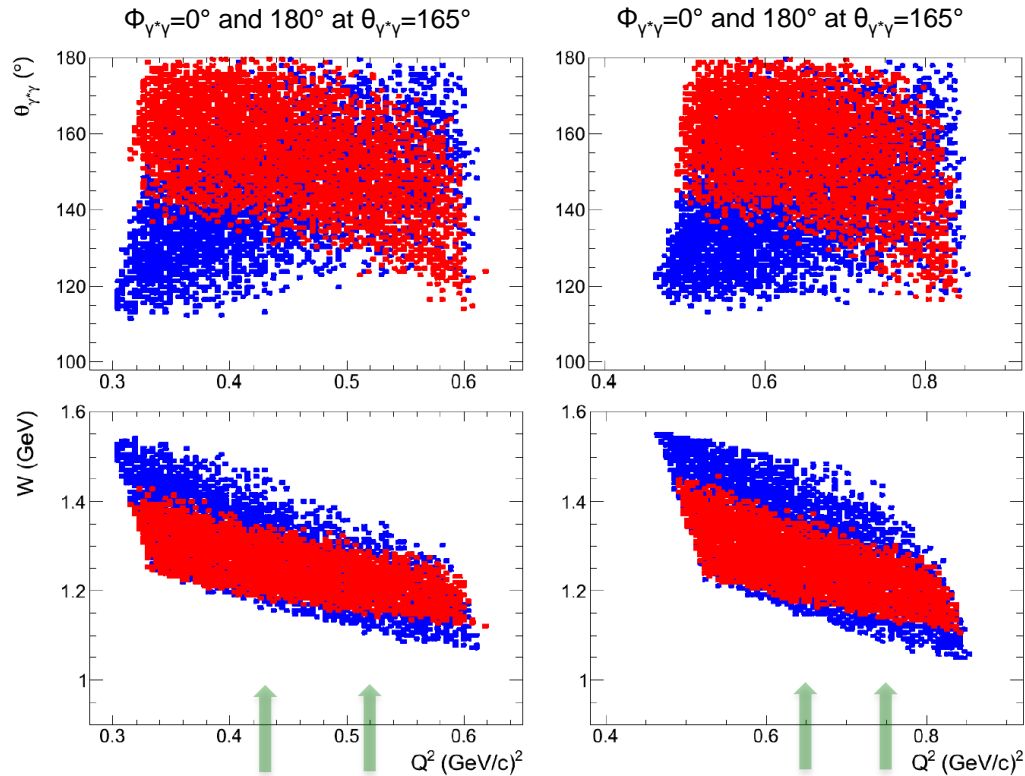
SHMS keeps same position & momentum through out Part I (Part II)

Part	I	I	II	II
$Q^2$	0.43 (GeV/c) <sup>2</sup>	0.52 (GeV/c) <sup>2</sup>	0.65 (GeV/c) <sup>2</sup>	0.75 (GeV/c) <sup>2</sup>

# Measurements

## Part I

## Part II



Phase space binned  
in  $Q^2$ ,  $W$ ,  $\theta_{\gamma^*\gamma}$ ,  $\Phi_{\gamma^*\gamma}$

Cross section:  
DR calculation,  
B. Pasquini

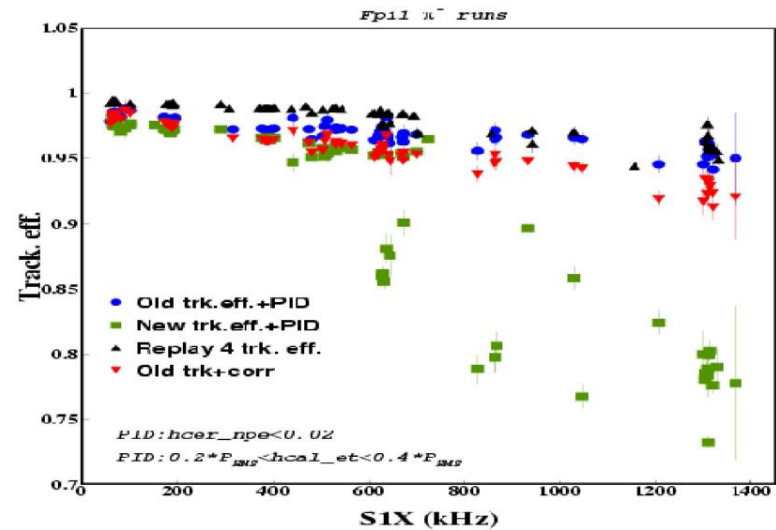
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$Q^2$	0.43 ( $\text{GeV}/c^2$ )	0.52 ( $\text{GeV}/c^2$ )	0.65 ( $\text{GeV}/c^2$ )	0.75 ( $\text{GeV}/c^2$ )

# Measurements

## HMS singles rates

	Kinematical Setting	HMS singles rates (kHz)
Part I	Kin Ia	213
	Kin Ib	91
	Kin IIa	290
	Kin IIb	68
	Kin IIIa	300
	Kin IIIb	34
Part II	Kin IVa	102
	Kin IVb	37
	Kin Va	122
	Kin Vb	31
	Kin VIa	244
	Kin VIb	16

## HMS Tracking Efficiency



HMS singles rates kept below 300 kHz

Kin IIIa → 45  $\mu$ A

All other settings → 85  $\mu$ A

# Measurements

Plus for systematics:

- Electron momentum & angle stays fixed through out Part I
- Electron momentum & angle stays fixed through out Part II
- Proton momentum stays fixed for the asymmetry pair ( $\Phi_{\gamma^* \gamma} = 0^\circ, 180^\circ$ ) measurements
- No beam energy changes

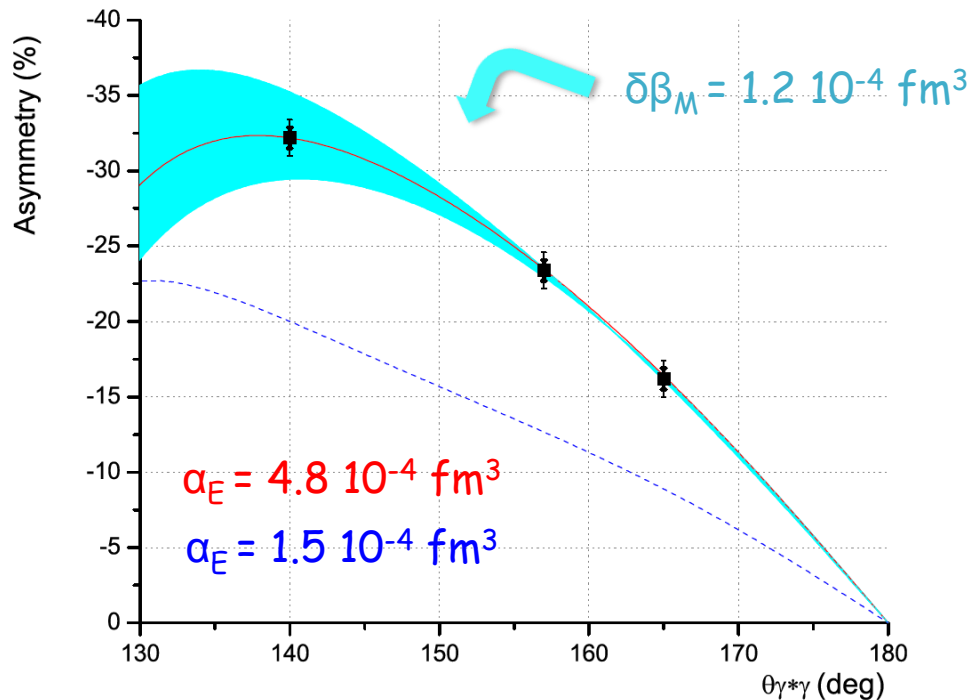
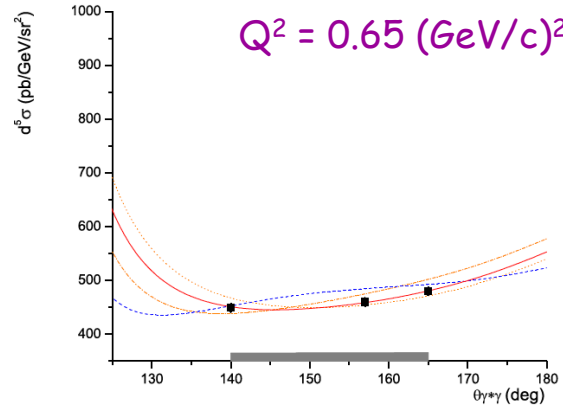
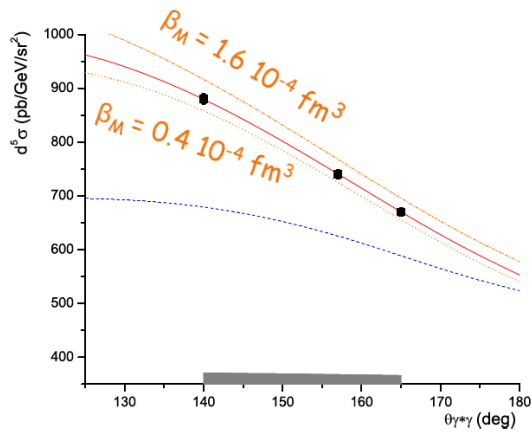
One day for normalization studies / system check out

Time could be shared if running with group of other experiments

$p(e, e'p)\pi^0$  measured for free

- High statistics
- Cross section very well known in this region
- Additional normalization per setting

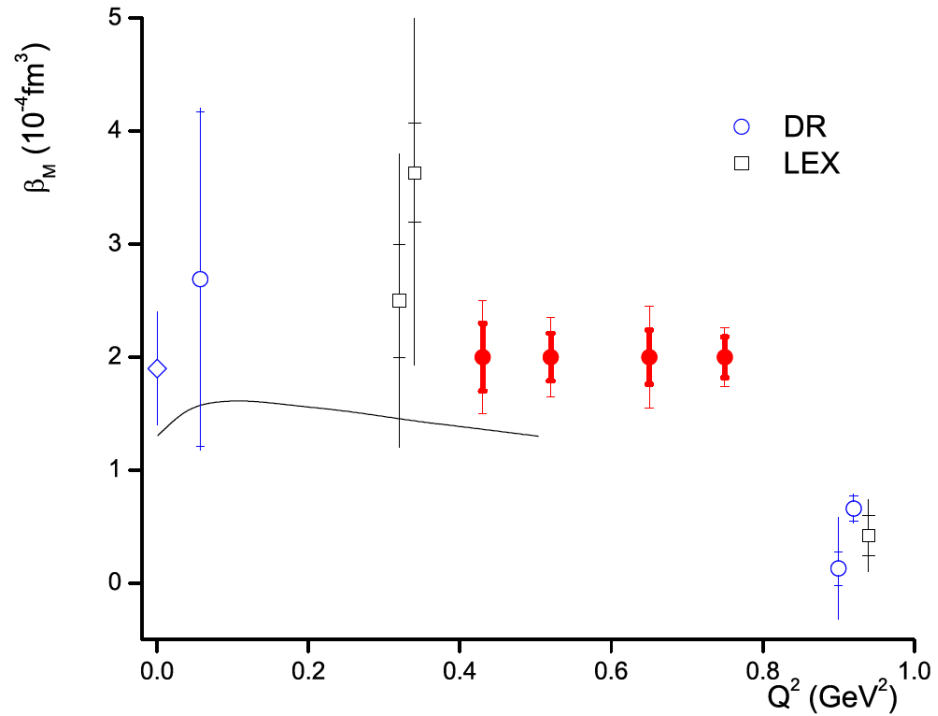
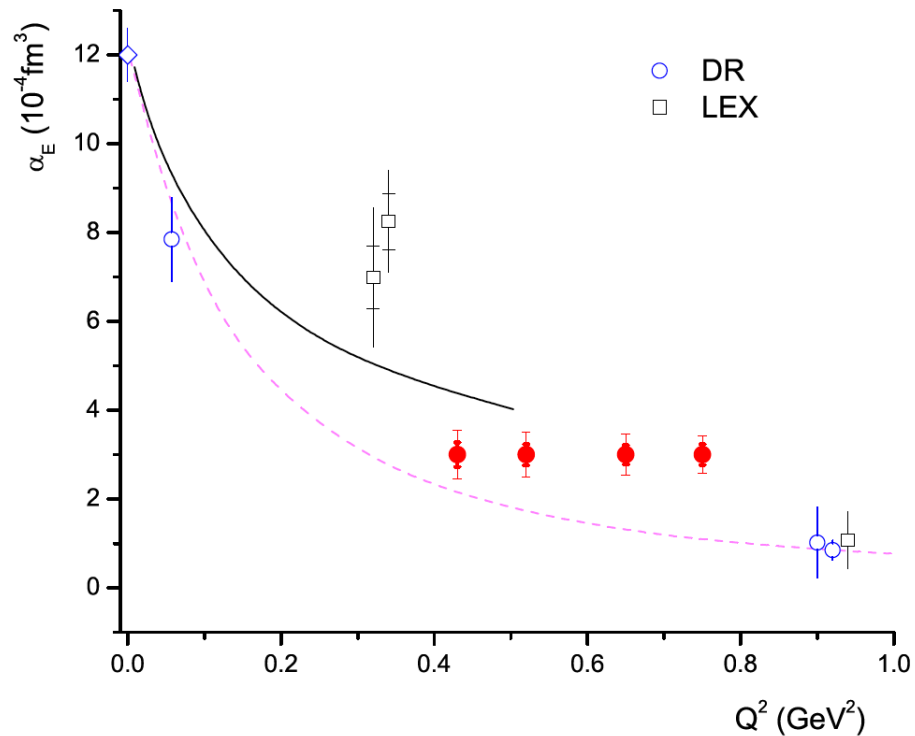
# Measurements



Statistical	< ±1.3%
Beam energy / scat. Angle	±1-2.5%
Target density	±0.5%
Detector efficiency	±0.5%
Acceptance	±0.5%
Target cell backgr.	±0.5%
Target length	±0.3%
Beam charge	±0.3%
Dead time	±0.3%
Pion contamination in MM	±0.3%
Rad. Corr.	±1.5%
Other	±0.5%

$\sigma$	< ±1.3% (stat)	< ±3.3% (syst)
$A$	≈ ±0.7% (stat)	≈ ±1.1% (syst)

# Projected Results



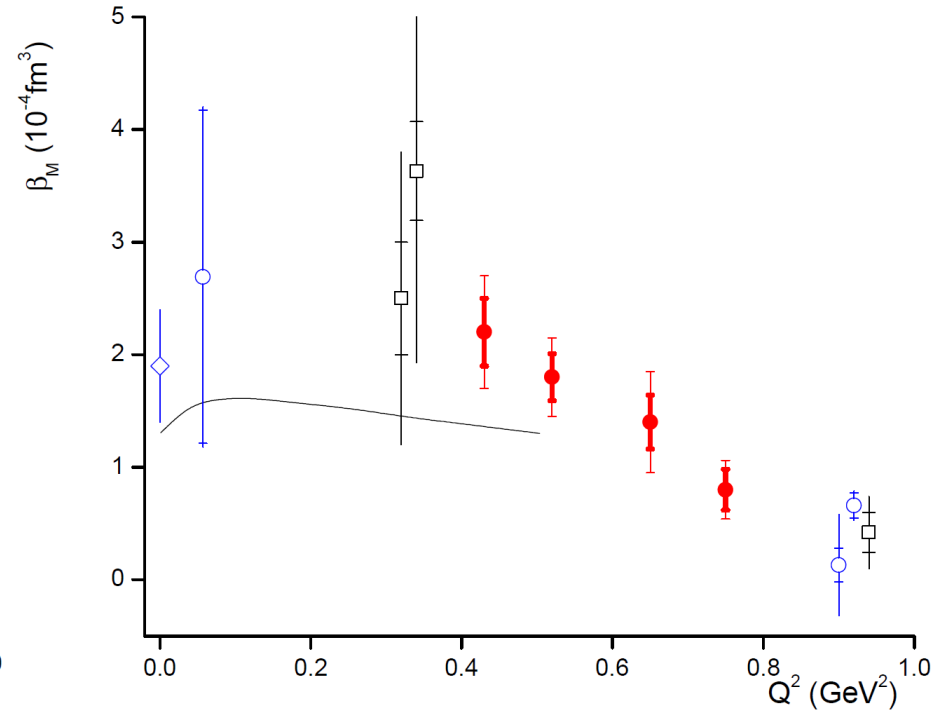
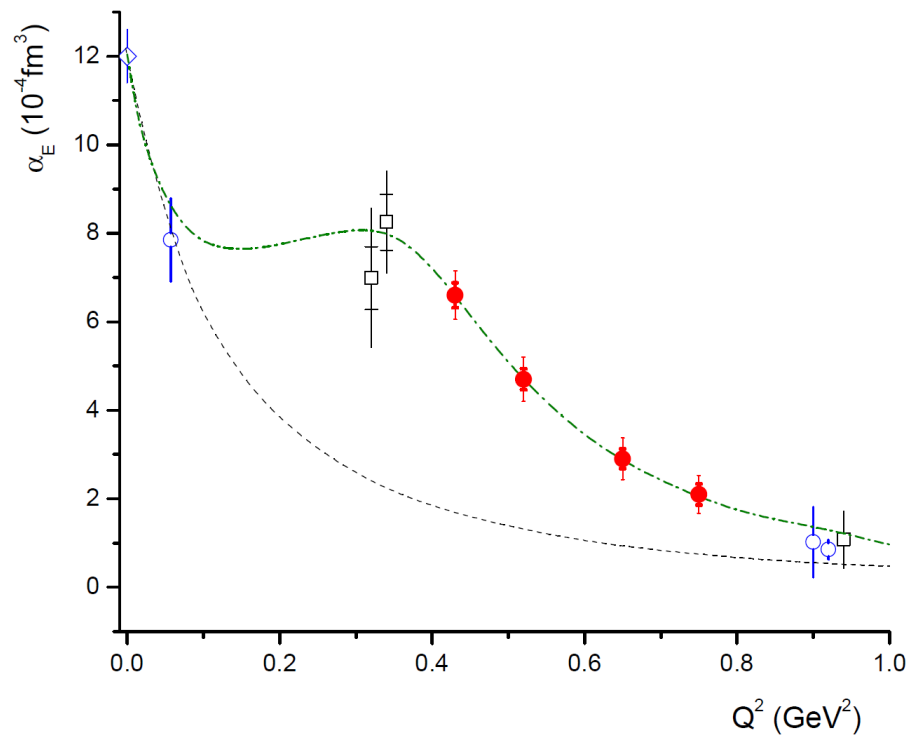
$$\delta_{\text{GPs}(\text{stat})} \approx 0.7 \delta_{\text{GPs}(\text{syst})}$$

$$\delta_{\text{GPs}(\text{syst})} \approx \delta_{\text{GPs}(\text{FFs/DRmult})}$$



# Beam time request

measurements arbitrarily projected

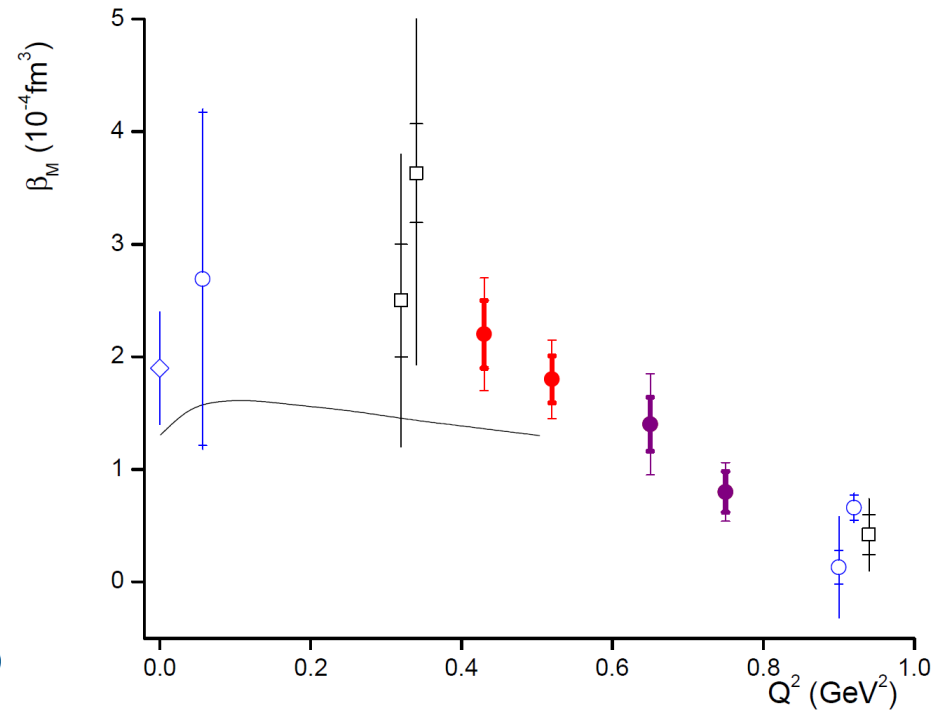
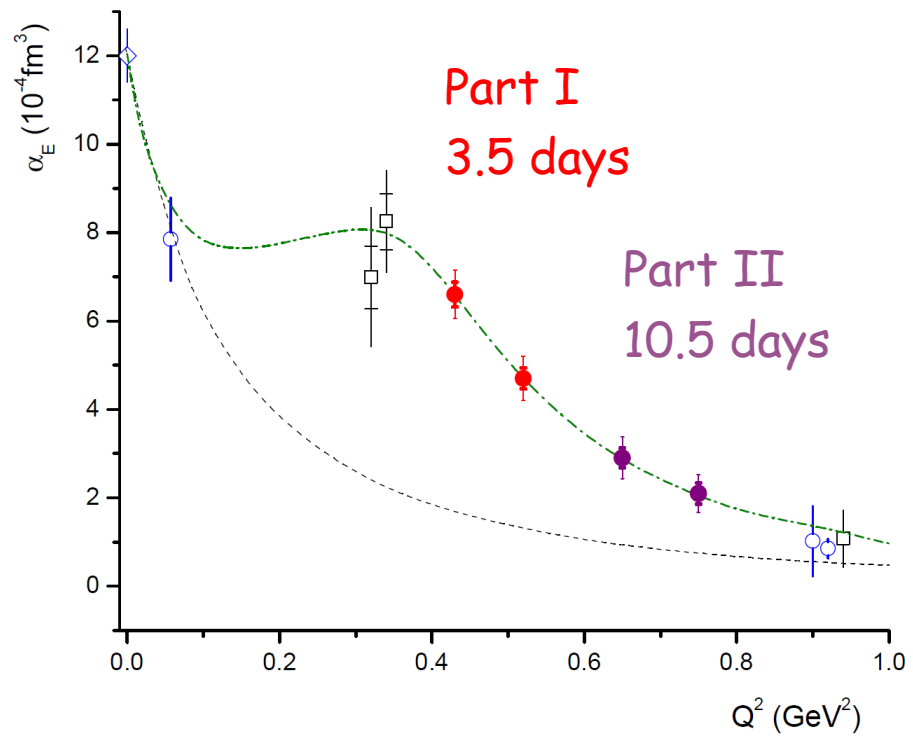


Beam time request: 15 days 4.4 GeV 85  $\mu\text{A}$  Hall C

Could also run in Hall A with the HRS's and two different beam energies (3.3 GeV and 4.4 GeV)

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# Summary

High precision measurements of the electric and magnetic GPs

- fundamental structure constants
- internal structure and dynamics of the nucleon
- complementary to elastic & transition FFs, GPDs, TMDs, ...

New measurements in a region very sensitive to the nucleon dynamics

- will improve the precision of  $a_E$  and  $\beta_M$  by a factor of 2
- map vs  $Q^2$  - bridge low  $Q^2$  measurements - cross check measurements of other labs
- explore non trivial  $Q^2$  dependence of  $a_E$  (mesonic cloud, something else ... ?)
- quantify the balance between paramagnetism and diamagnetism through  $\beta_M$
- will provide with high precision the spatial deformation of charge & magnetization densities under an applied e.m. field (currently a profound structure is suggested in the region 0.5 fm - 1 fm)
- Lattice QCD results will be emerging in the next few years - very important to cross check these calculations
- the new measurements are expected to trigger more theoretical activity

Beam time request:

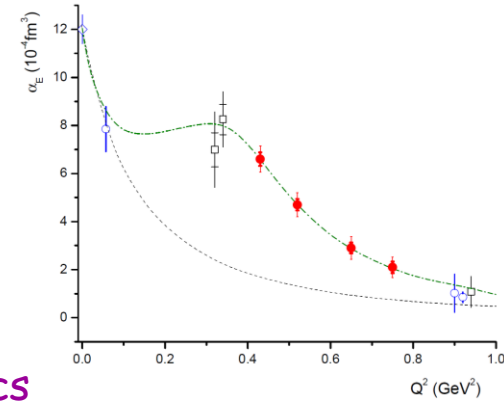
- 15 days with 4.4 GeV in Hall C (standard setup)
- 3.5 days (Part I) advances greatly our current knowledge of  $a_E$ ,  $\beta_M$
- possible also in Hall A

Thank you!

# Summary

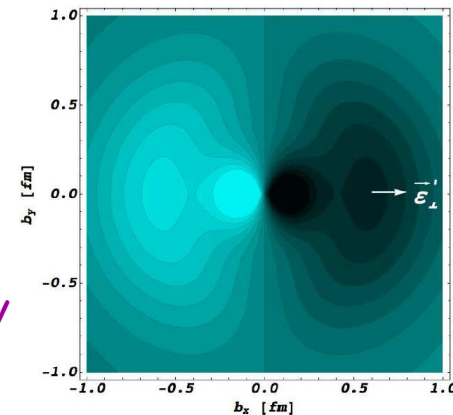
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