



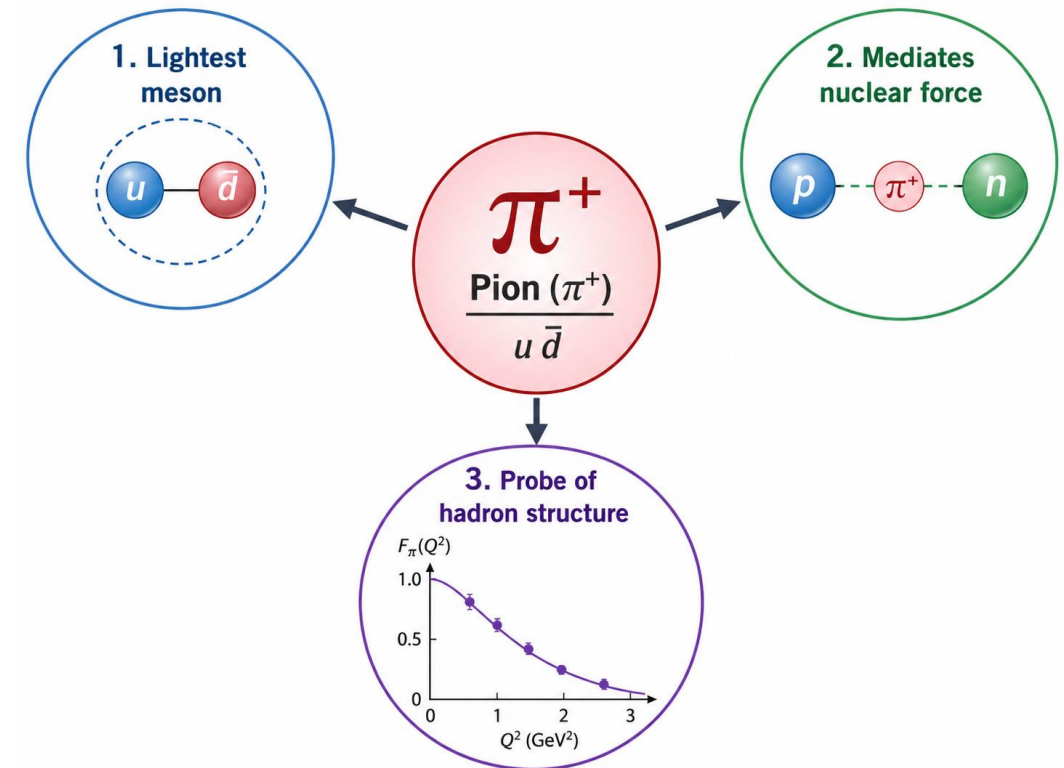
# Probing Pion Structure with L/T-Separated Cross Sections in Hall C at Jefferson Lab

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# Scientific Motivation

- ❑ The interaction of quarks and gluons is successfully described by **Quantum Chromodynamics (QCD)**.
- ❑ **But unable to construct the quantitative description of hadrons in terms of the underlying constituents, quarks and gluons.**
- ❑ **Pion** is the lightest meson and provides an ideal testing ground for our understanding of the bound  $q\bar{q}$  hadronic system.
- ❑ **Pions mediate the residual strong force that helps bind nucleons inside the nucleus.**
- ❑ **Form factor ( $F(Q^2)$ )** is an important observable that can be studied to understand the internal structure of hadrons.
- ❑ **Measuring the pion form factor at various  $Q^2$  (up to  $8.5\text{GeV}^2$ ) checks the validity of QCD-based theories, including the transition region between perturbative and non-perturbative approaches.**



# The Pion in perturbative QCD

□ **Form Factor** describes transverse spatial position of partons within hadrons.

□ At very large  $Q^2$ , pion form factor ( $F_\pi$ ) can be calculated using pQCD;

$$F_\pi(Q^2) = \frac{4}{3} \pi \alpha_s \int_0^1 dx dy \frac{2}{3} \frac{1}{xy Q^2} \phi(x) \phi(y)$$

□ At asymptotically high  $Q^2$ , the pion distribution amplitude becomes;

$$\phi_\pi(x) \rightarrow \frac{3f_\pi}{\sqrt{n_c}} x(1-x)$$

□ And  $F_\pi$  takes the very simple form;

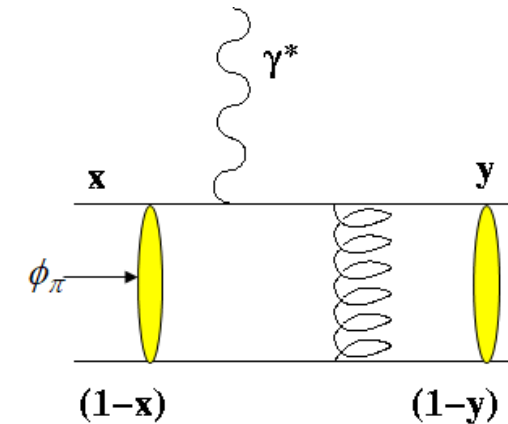
$$Q^2 F_\pi(Q^2) \rightarrow 16\pi \alpha_s(Q^2) f_\pi^2 \quad (Q^2 \rightarrow \infty)$$

[G.P. Lepage, S.J. Brodsky, Phys.Lett. 87B(1979)359].

□  $Q^2 F_\pi$  should behave like  $\alpha_s(Q^2)$  even for moderately large  $Q^2$

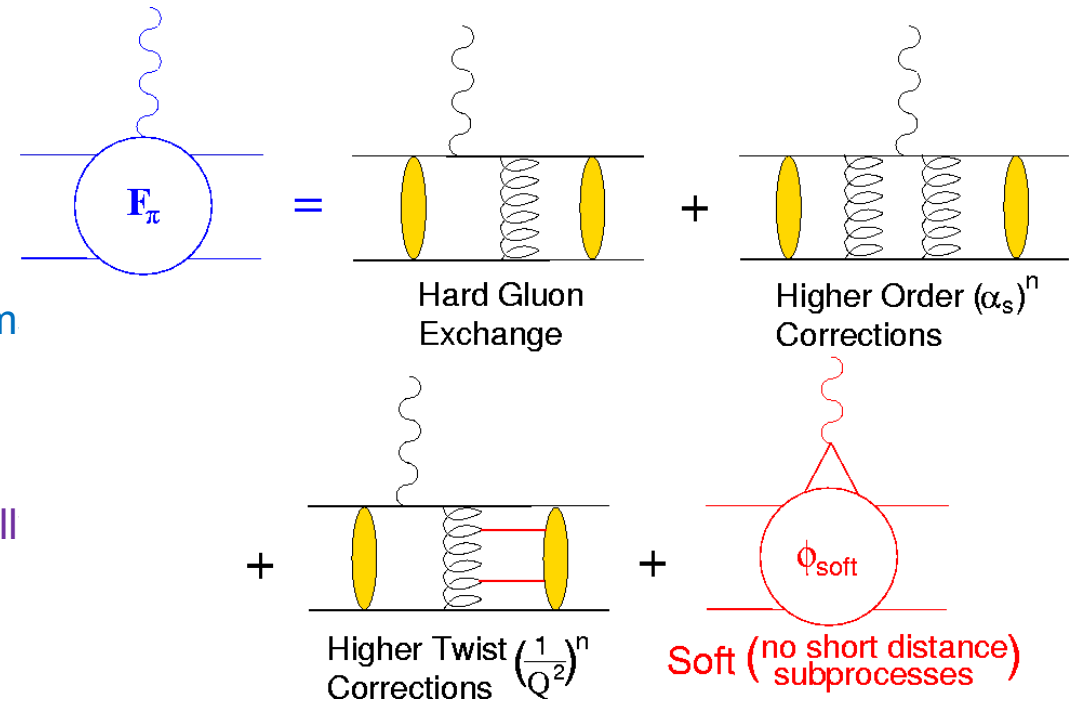
□ Pion form factor seems to be best tool for experimental study of nature of the quark-gluon coupling constant renormalization

[A.V. Radyushkin, JINR 1977, arXiv:hep-ph/0410276]



# Pion in Accessible $Q^2$ Region

- At experimentally accessible  $Q^2$ , both the "hard" and "soft" components (e.g., transverse momentum effects) contribute.
- The interplay of hard and soft contributions is poorly understood
- Different theoretical viewpoints on whether higher-twist mechanism dominate until very large momentum transfer or not.
- The pion elastic and transition form factors are experimentally accessible over a wide kinematic range.
- Hall C at Jefferson Lab is only facility in the world with the capacity to perform  $F_\pi$  measurement.

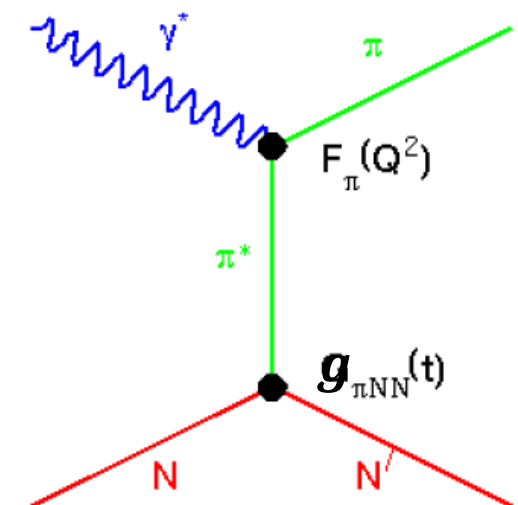
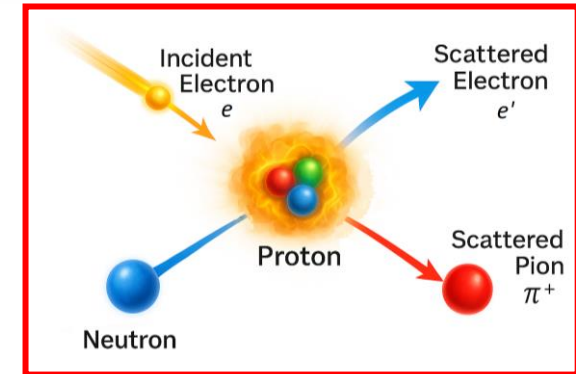


# Pion Form Factor Measurement

- Above  $Q^2 > 0.3\text{GeV}^2$ ,  $F_\pi$  is measured indirectly using the “pion cloud” of the proton via pion electroproduction  $p(e, e'\pi^+)n$
- Indirect measurement – Form factor extraction requires a model.
- Need to extract  $\sigma_L$  from the total cross-section.
- As an illustration of how  $\sigma_L$  connects to  $F_\pi^2(Q^2, t)$ , we consider a simple **Born Term Model**;

$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_\pi^2)} g_{\pi NN}^2(t) F_\pi^2(Q^2, t)$$

- In reality, we use other available models such as VGL, CKY and PKT for  $F_\pi^2(Q^2, t)$  extraction.



# Rosenbluth Separation Technique

- Rosenbluth separation required to isolate  $\sigma_L$  for L/T separation.

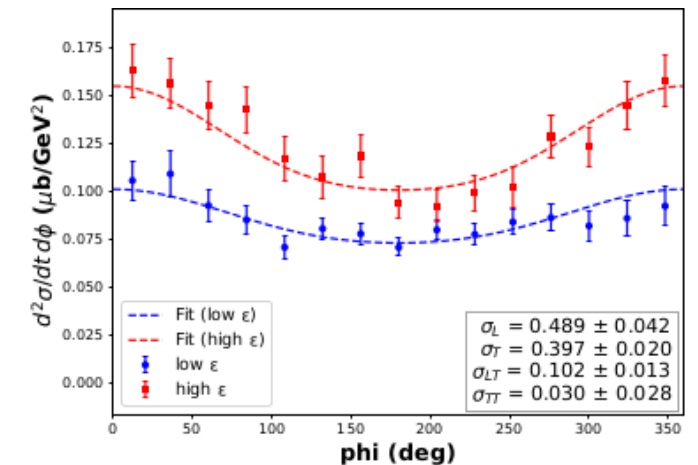
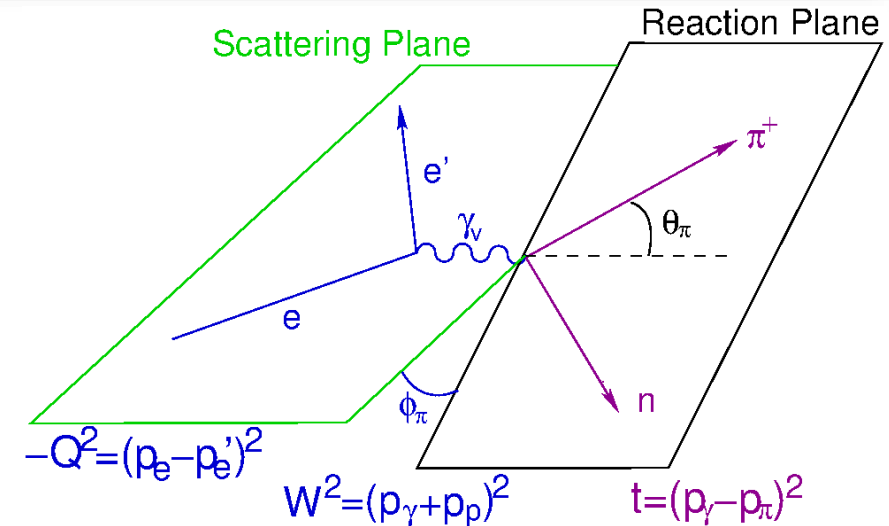
- The physical cross-section for the electroproduction process is given by;

$$2\pi \frac{d^2\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\epsilon(\epsilon + 1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

- Here “ $\epsilon$ ” is polarization of virtual photon.

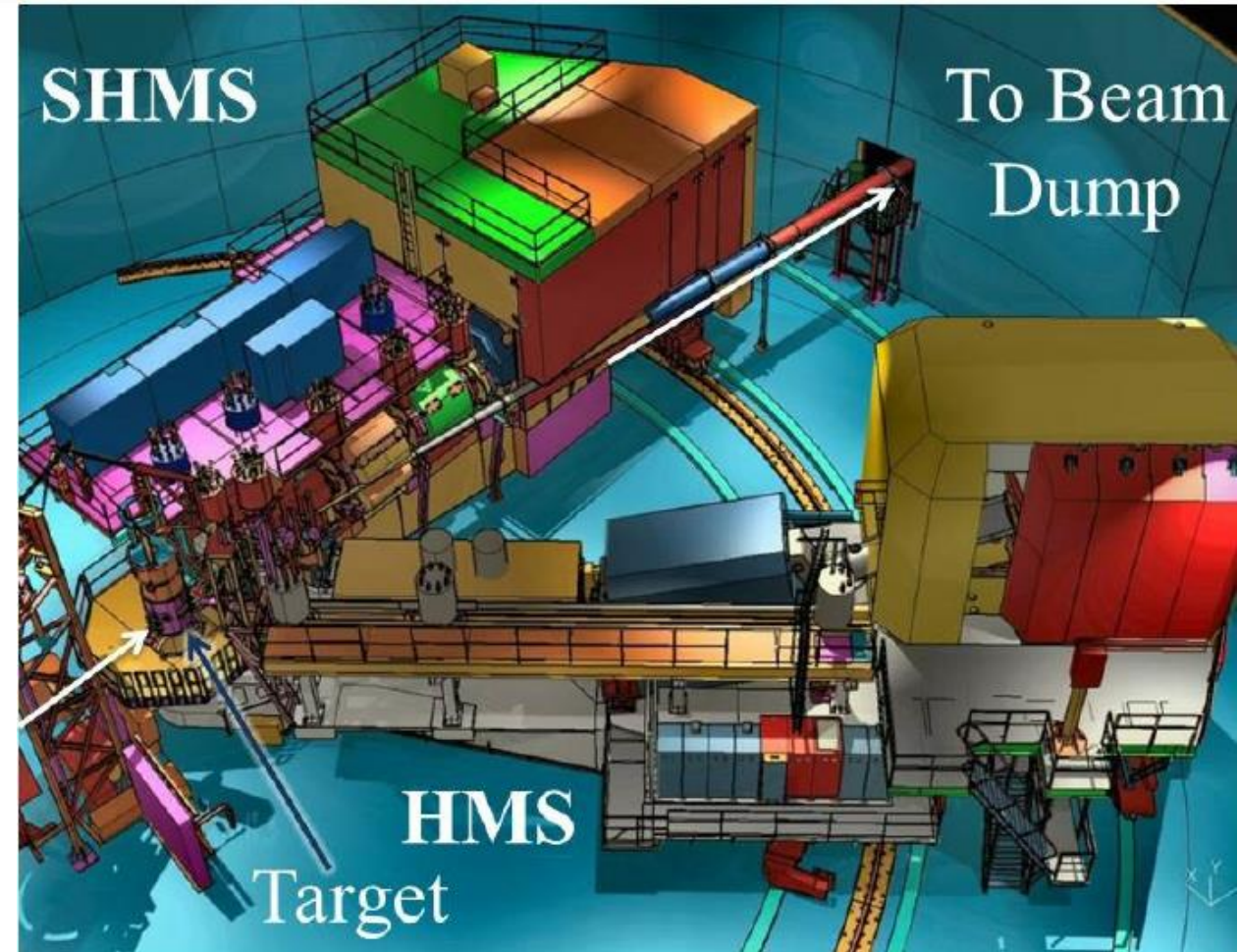
$$\epsilon = \left[ 1 + 2 \frac{(E_e - E_{e'})^2 + Q^2}{Q^2} \cdot \tan^2 \frac{\theta_{e'}}{2} \right]^{-1}$$

- Perform two scattering measurements with different beam energies “ $E_e$ ” to vary “ $\epsilon$ ” and separate different cross-section terms.
- Careful attention must be paid to systematic studies such as spectrometer acceptance, kinematics, efficiencies, etc.



# Pion-LT Experiment at JLab

- Specially designed to measure precise cross-sections and form factors for mesons.
- Experimental setup contains a target and two detector arms.
- Target can be Liquid  $H_2$ , Liquid  $D_2$  or solid targets.
- Two detectors are;
  - High Momentum Spectrometer (HMS)
  - Super High Momentum Spectrometer (SHMS)

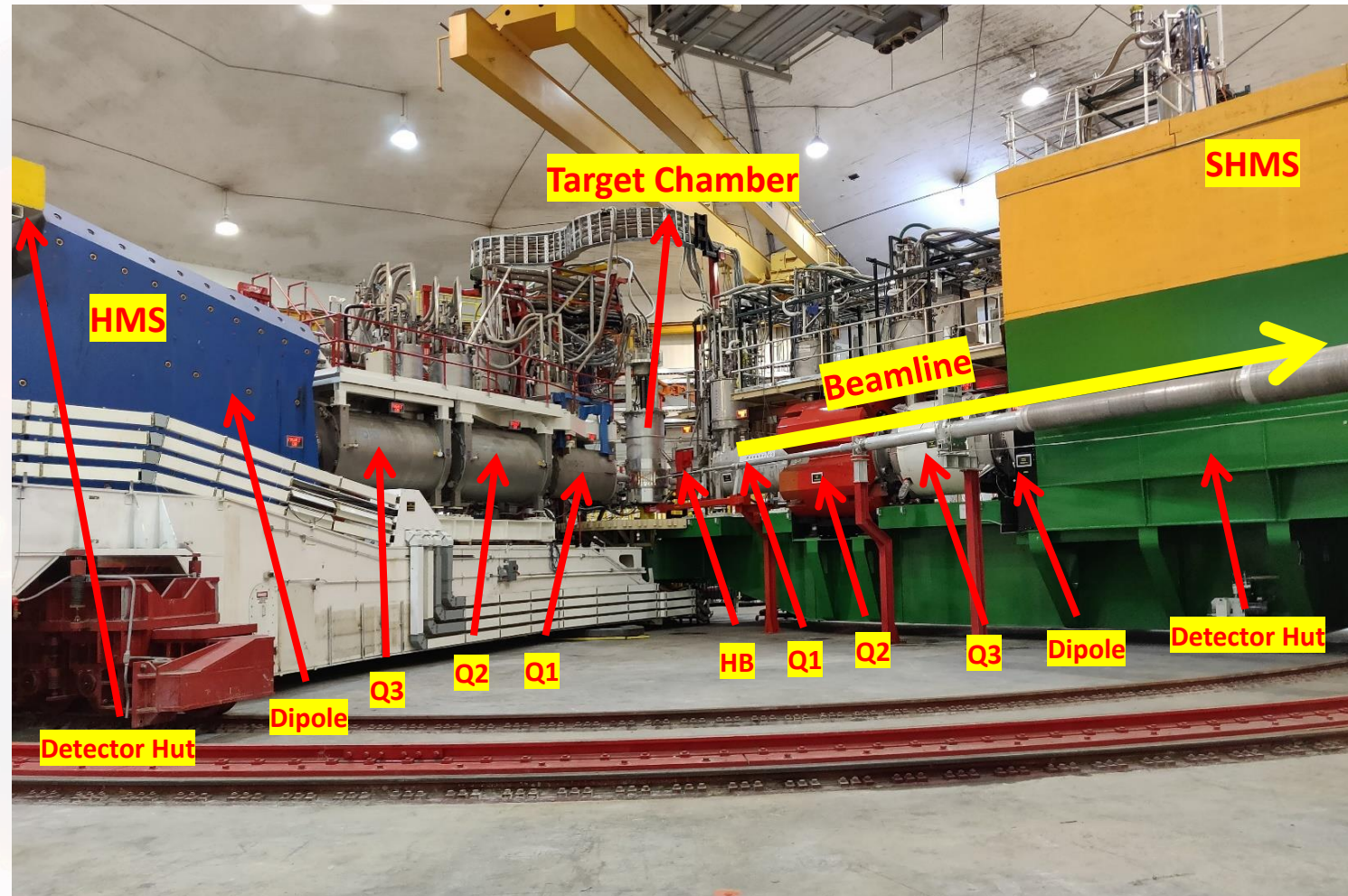


# Hall C Spectrometers

- Both spectrometers are movable and have sets of quadrupole (Q), dipole (D) superconducting magnets and a Detector Hut.
- Both spectrometers are rotatable and contain similar detector packages.

Spec	Angle range (deg)	Momentum range
HMS	10.5 – 90	0.5 – 7 GeV
SHMS	5.5 – 40	0.5 – 11 GeV

- Took coincidence data; simultaneously detected **electrons in HMS** and **pions in the SHMS**

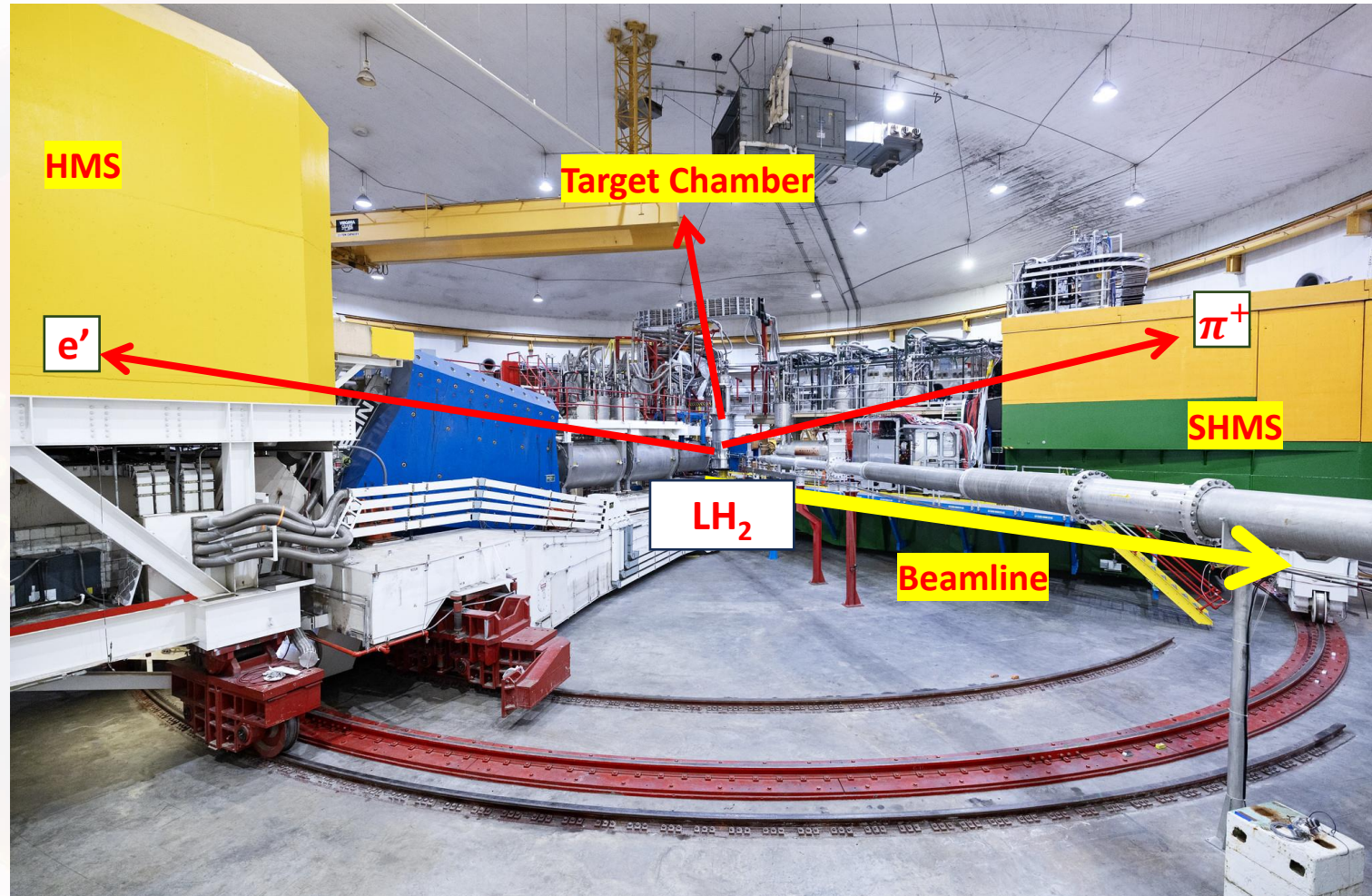


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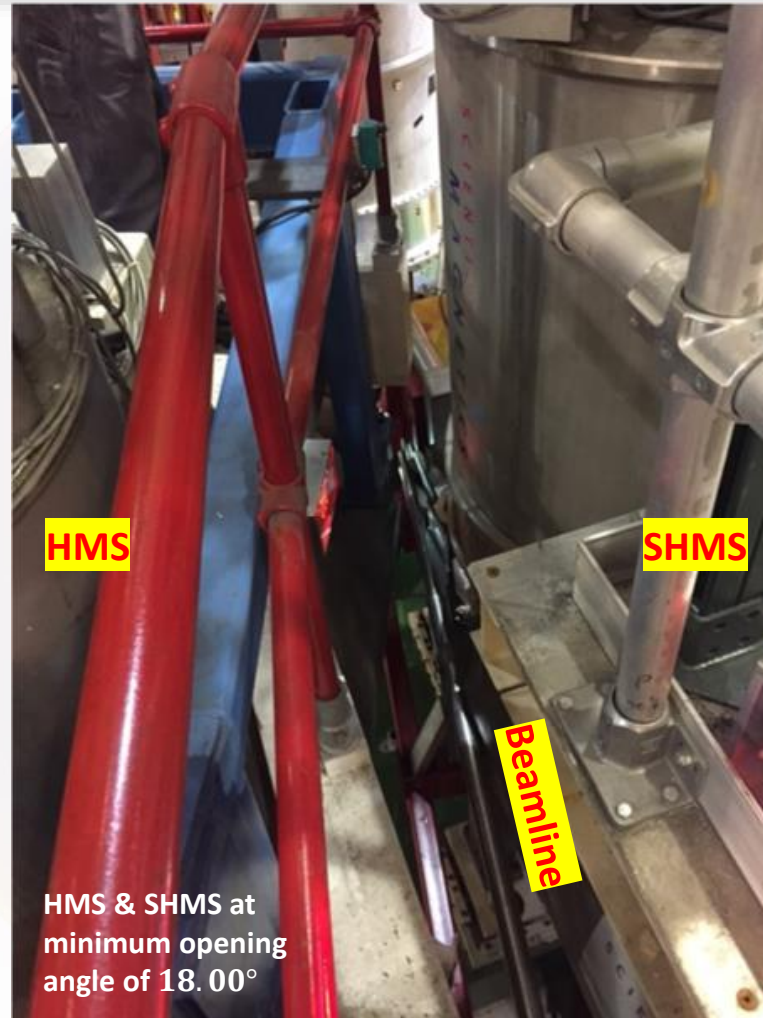
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# Hall C Spectrometers

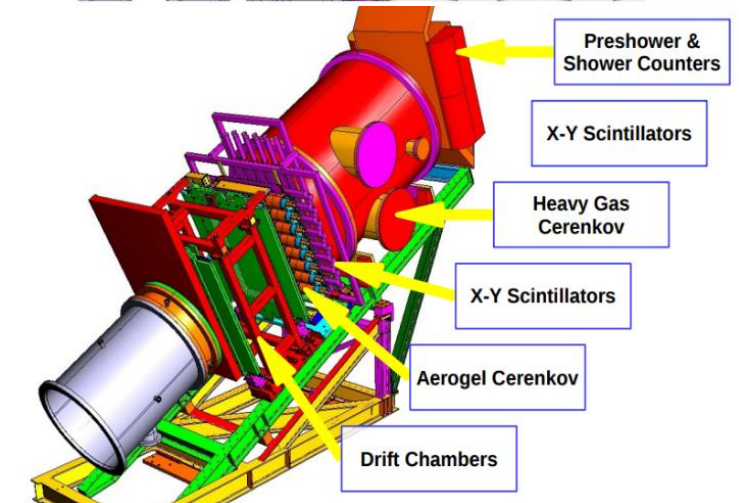
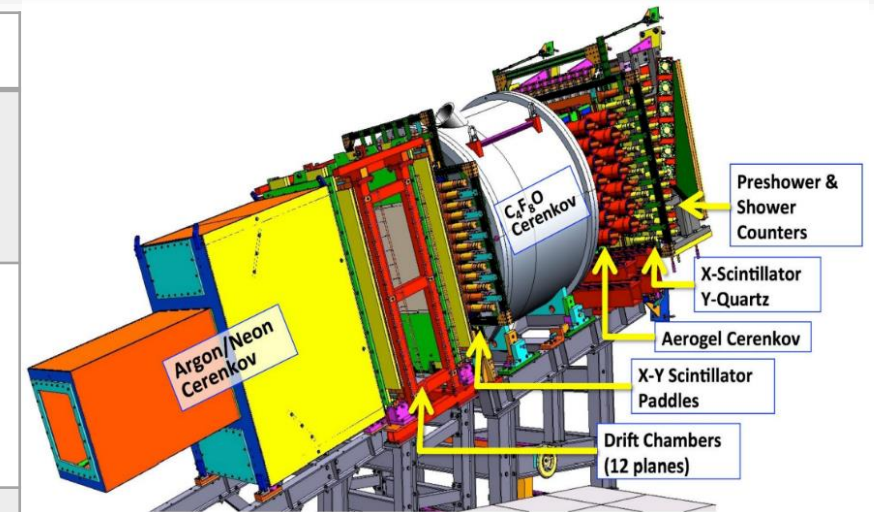
- This experiment has in large part driven the forward angle requirements of SHMS and HMS
- The **minimum opening angle** between SHMS and HMS was, **18.00°**, reached for this experiment.
  - HMS moved to **11.01°** deg and SHMS moved **18.00°** away at **6.99°**
- In this experiment, we pushed **SHMS to 5.50°**.
  - Several kinematic settings used the SHMS at its minimum angle of **5.50°**

**Thank you to the Hall C scientific and technical staff members who made all of this possible**



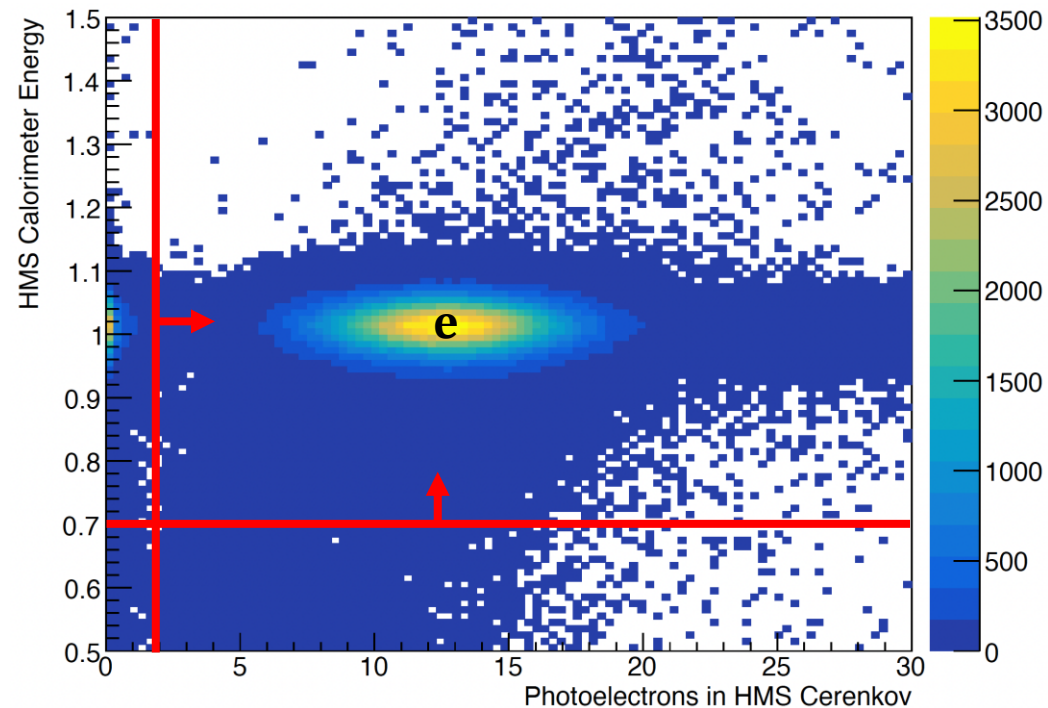
# Detectors

Detectors	Purpose	Notes
Noble Gas Cerenkov (NGC)	Particle ID Trigger 'e <sup>±</sup> /π <sup>±</sup> ' at high momentum	Vary Ar/Ne mixture to set index at 'π <sup>±</sup> ' threshold. Only used in SHMS.
Heavy Gas Cerenkov (HGC)	Particle ID Trigger 'π <sup>±</sup> /K <sup>±</sup> ' discrimination	C <sub>4</sub> F <sub>8</sub> O - Vary pressure to set n at π <sup>±</sup> threshold (here n = 1.011 – 1.030 at 1 atm)
Aerogel Cerenkov	Particle ID Trigger 'K <sup>+</sup> /p' discrimination	n = 1.011, 1.015, 1.03, 1.05
Drift Chambers	Momentum measurement, Tracking	5mm max. Drift, 300 micron resolution
Hodoscopes	Trigger, Time reference, Measure β	X-Y Scintillators
Calorimeters (EM-Preshower and Shower Counters)	Particle ID, Trigger, e <sup>±</sup> Tagging	



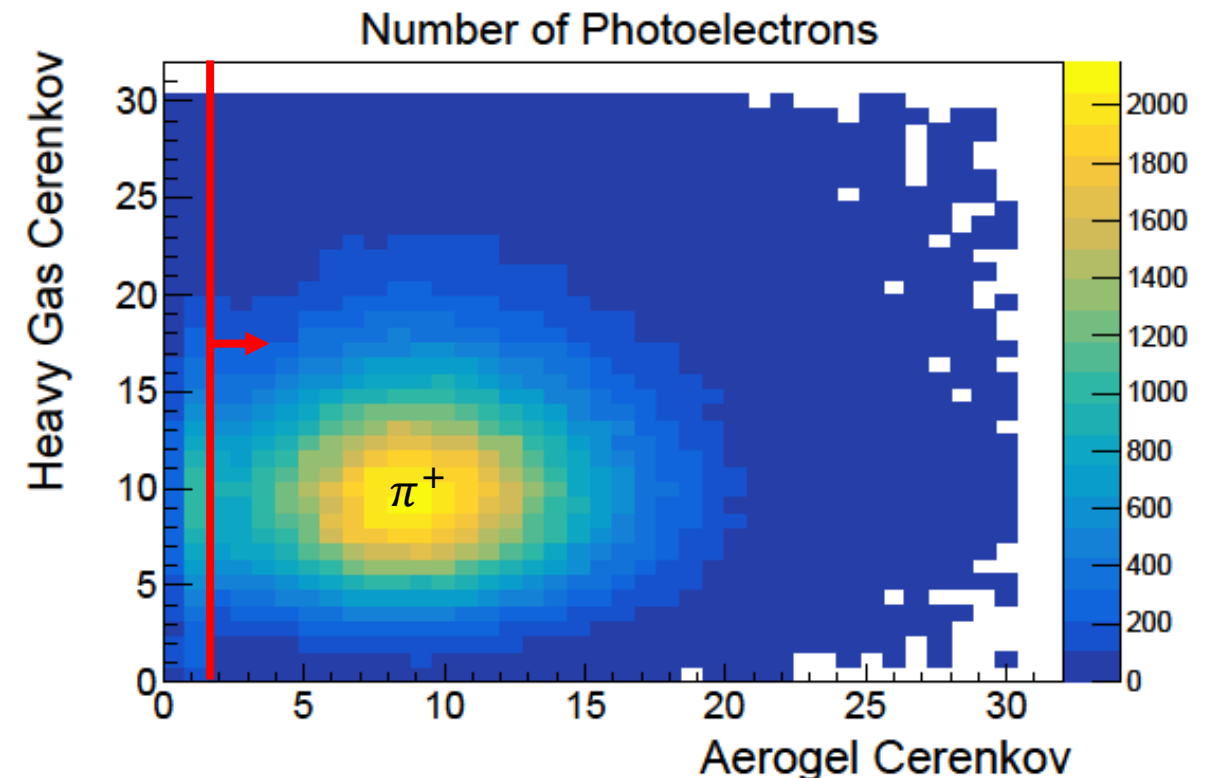
# Event Selection Criteria

- Purpose is to select the clean pion events sample in coincidence with the electrons to measure the cross-sections.
- Cuts must be tight, but not so close as to sacrifice efficiency across the acceptance.
- Overall, detector efficiencies are greater than ~98%.



HMS PID

Q2 = 3.85, W = 2.62, t = 0.21 (2 epsilons)



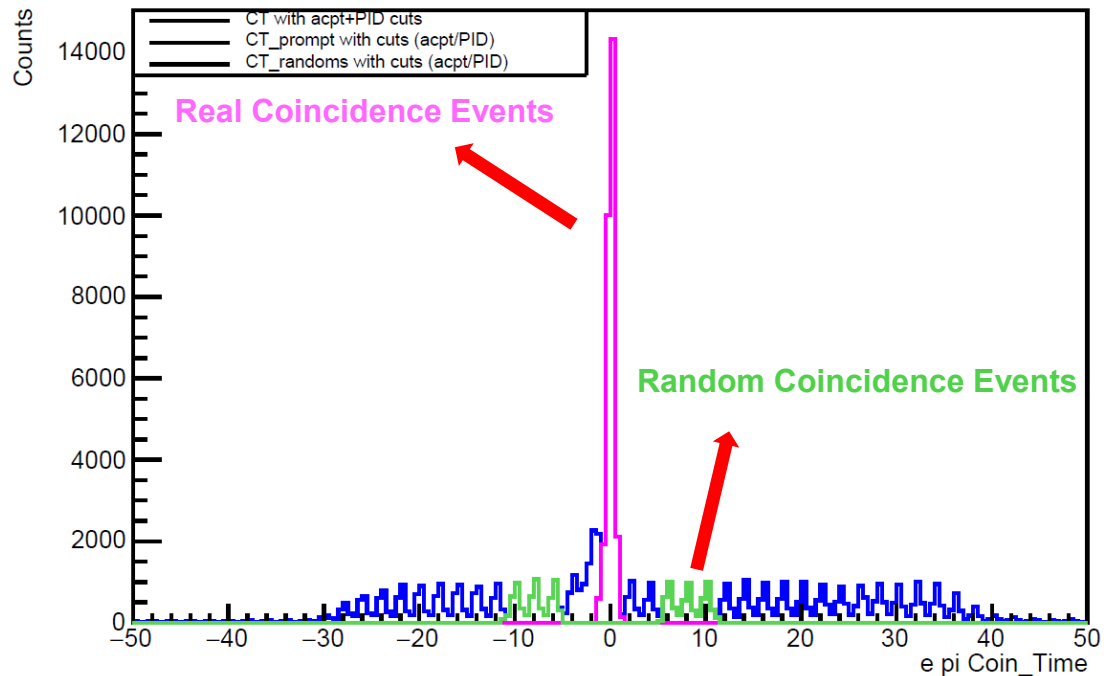
SHMS PID

# Event Selection Criteria

- ❑ CoinTime (CT) is given as:

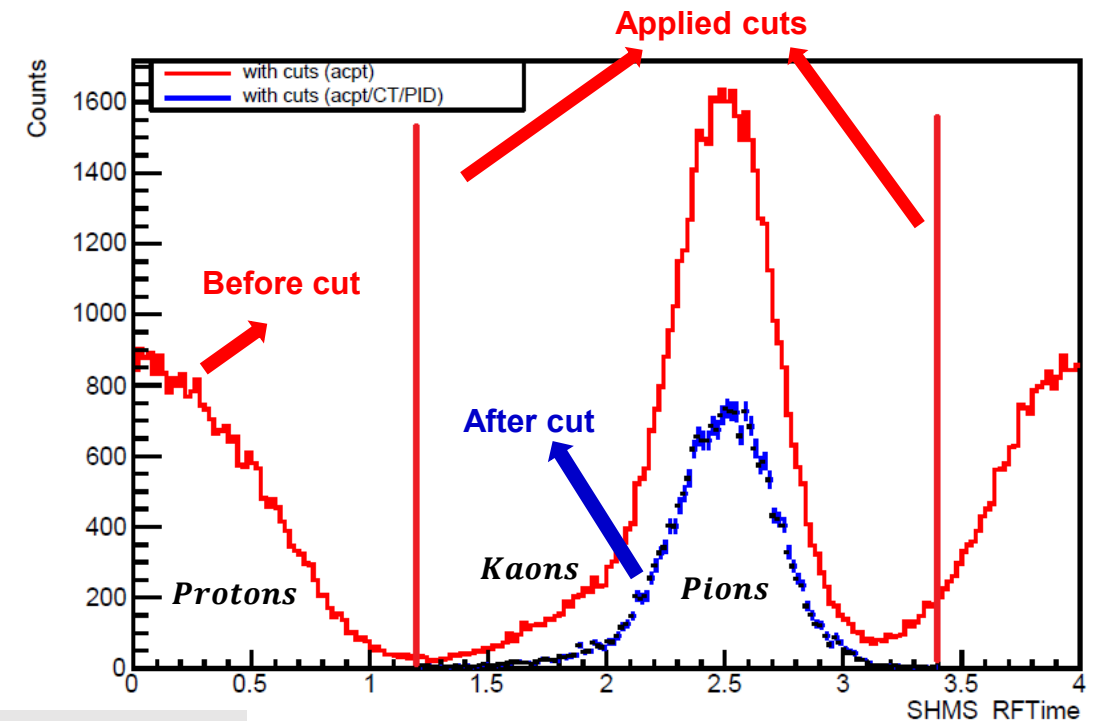
$$t_{coin} = t_{HMS} - t_{SHMS}$$

- ❑ Used to eliminate random background caused by random coincidences.



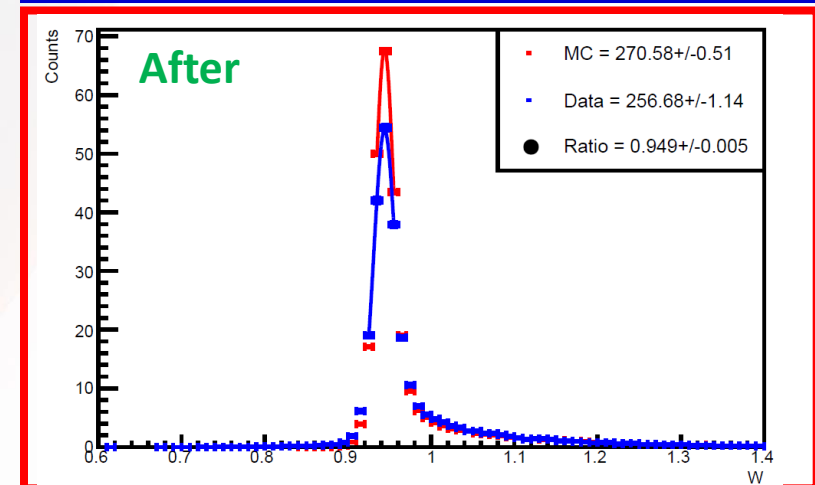
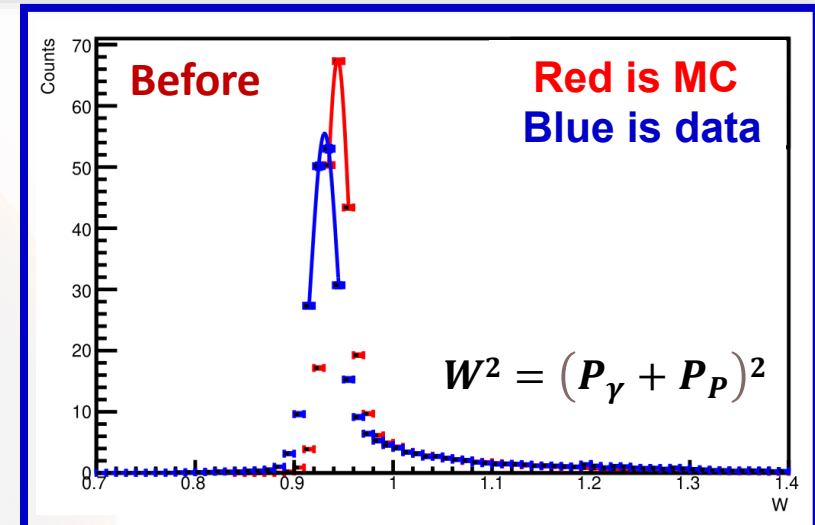
Q2 = 3.85, W = 2.62, t = 0.21 (2 epsilons)

- ❑ RF time refers to the time difference between a detected event and the nearest preceding RF signal of the electron linac.
- ❑ Enables the differentiation between pions, kaons, and protons due to their distinct velocities.



# Elastic $ep$ Reaction Study

- ❑ Collected elastic  $ep$  data to identify possible kinematic offsets by comparing measured quantities with the well-known elastic reaction expectations.
- ❑ Purpose of the kinematic offset study is to quantify and correct small shifts in reconstructed kinematics and to help manage systematic uncertainties.
- ❑ looked at distributions of the missing variables ( $E_M, \vec{P}_M, W$ ) to find deviations from expected values based on kinematics.
- ❑ The  $E_M$ , the components of  $\vec{P}_M$ , and  $W$  are correlated to different spectrometer quantities (momentum, angle, beam energy), and thus offsets can be extrapolated from them.
- ❑ By adjusting the beam energy, momentum and angles, missing variables ( $E_M, \vec{P}_M, W$ ) can be moved to better agree between data and SIMC.
- ❑ Offsets are doing a good job and peaks are in agreement with each other.
- ❑ Applied the determined kinematic offsets to the physics data for cross-section measurement.



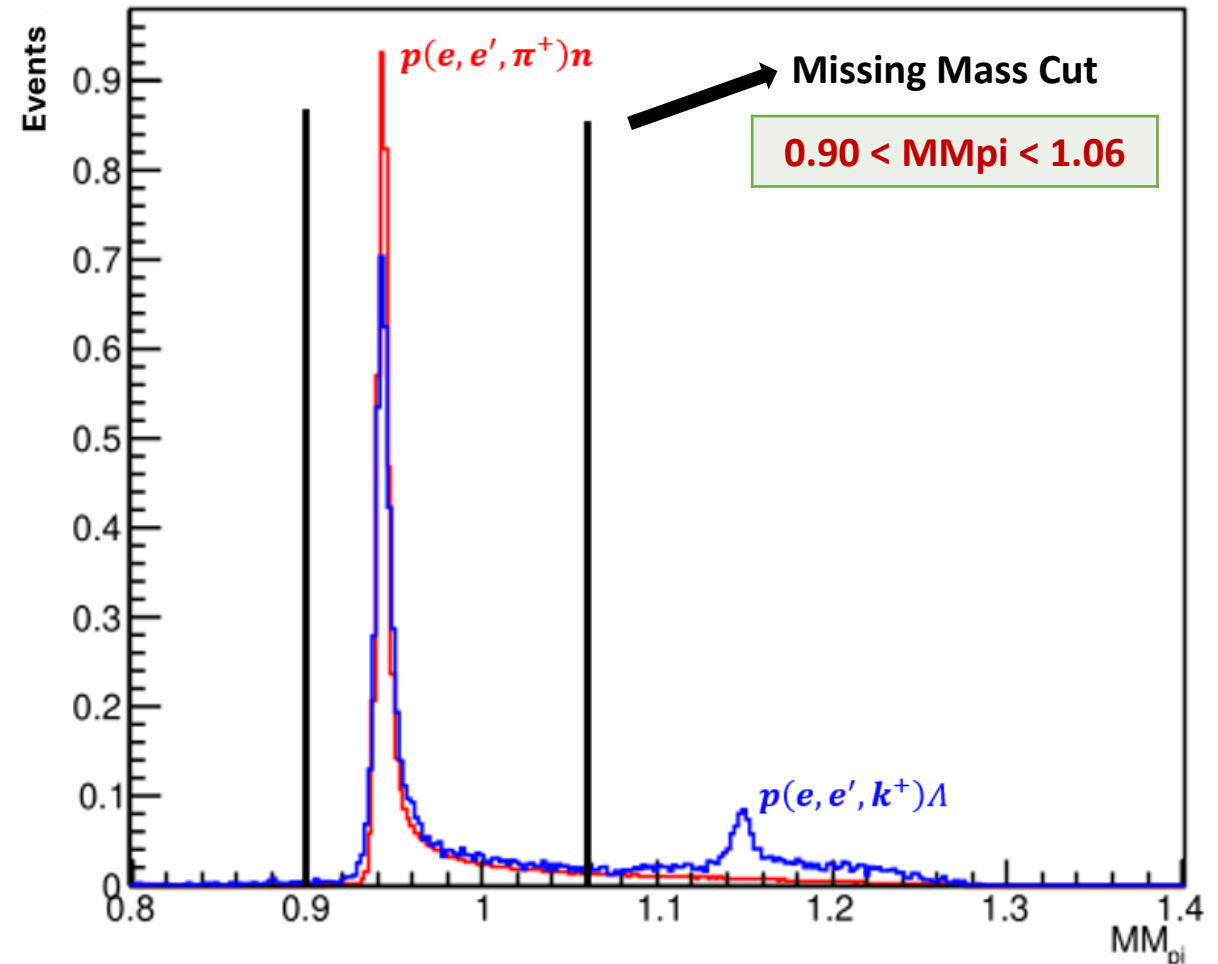
# Selection of Event Sample

- Selected electrons in HMS in coincidence with pions in the SHMS.

- Missing particle reconstruction (neutron).

$$M_m = \sqrt{(E_e + m_p - E_{e'} - E_{\pi^+})^2 - (\mathbf{p}_e - \mathbf{p}_{e'} - \mathbf{p}_{\pi^+})^2}$$

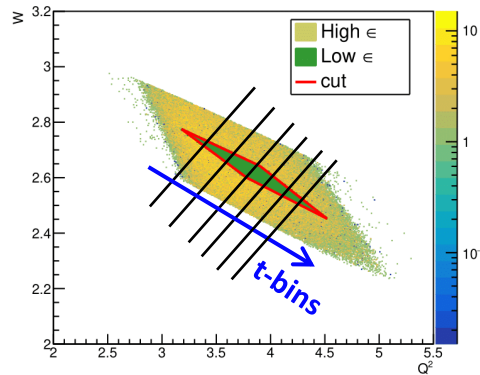
- Blue represents the experimental data missing mass plot.
- Red represents the Monte Carlo missing mass plot.
- To eliminate the remaining background, a missing-mass cut was applied to both the Monte Carlo and experimental data.



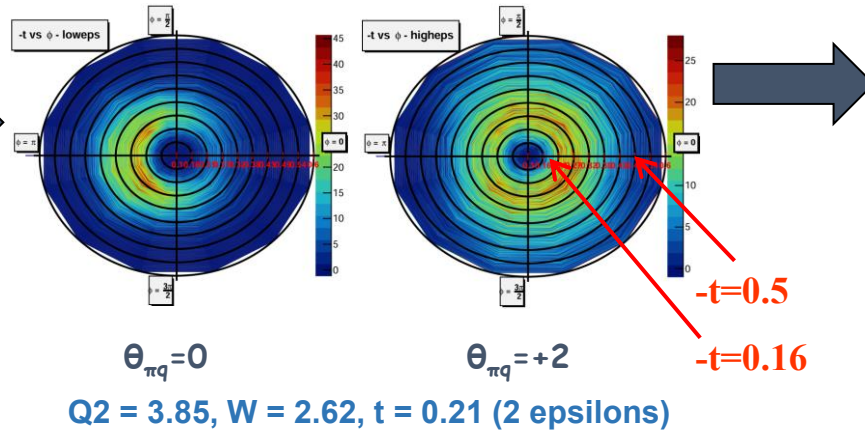
$Q^2 = 3.85 \text{ GeV}^2, W = 2.62 \text{ GeV}$  (2 epsilons)

# L/T Separation Iteration Procedure

Diamond cut



Improve  $\phi$  coverage by taking data at multiple  $\pi$  (HMS) angles,  $-2^\circ < \theta_{\pi q} < 2^\circ$ .



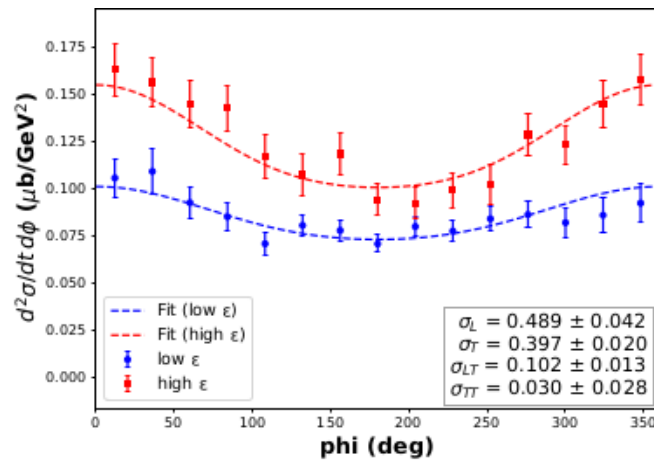
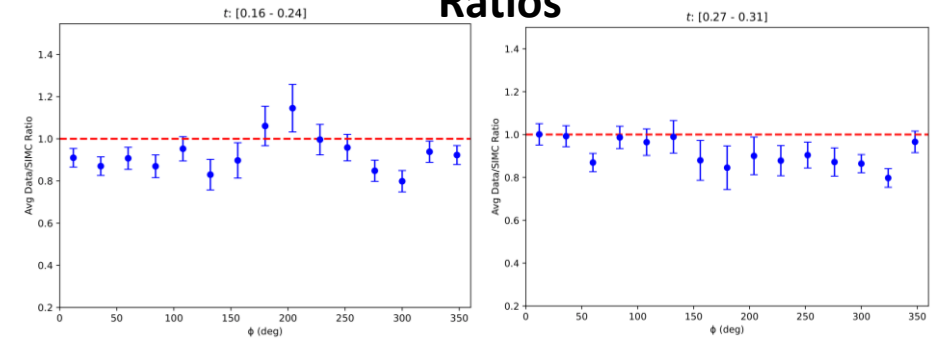
$Q_2 = 3.85, W = 2.62, t = 0.21$  (2 epsilons)

For each  $\pi$  HMS setting, form ratio:

$$R = \frac{Y_{EXP}}{Y_{SIMC}}$$

Combine ratios for  $\pi$  settings together, propagating errors accordingly.

Ratios



$\sigma_L = 0.489 \pm 0.042$   
 $\sigma_T = 0.397 \pm 0.020$   
 $\sigma_{LT} = 0.102 \pm 0.013$   
 $\sigma_{TT} = 0.030 \pm 0.028$

Extract via simultaneous fit of L, T, LT, TT

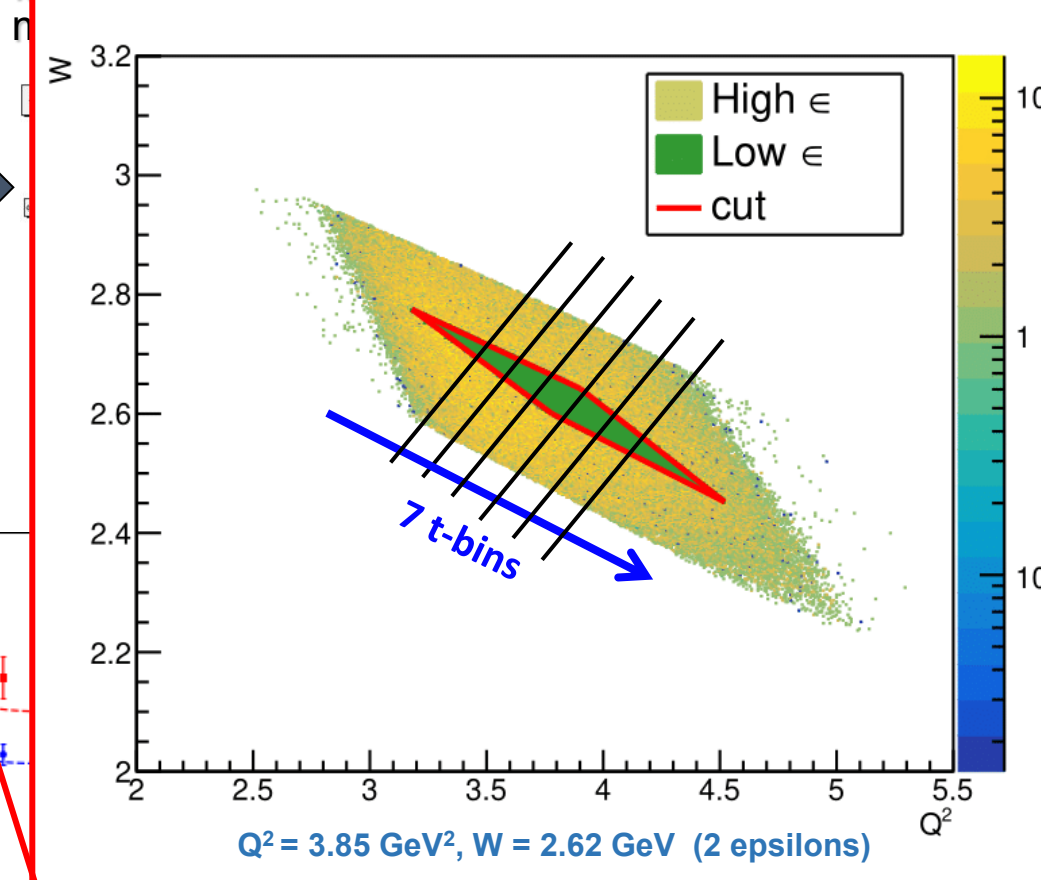
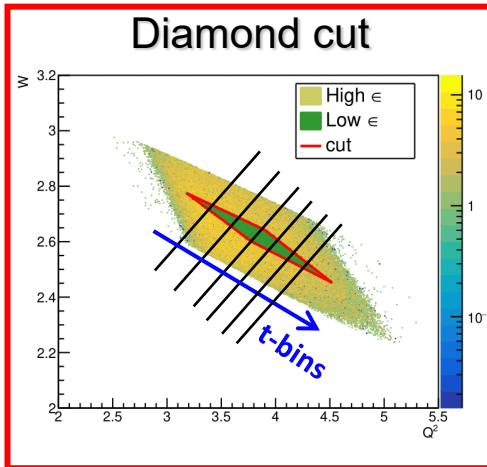
$$2\pi \frac{d\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

$$\frac{d^2\sigma}{dt d\phi}_{EXP} = \left( \frac{Y_{EXP}}{Y_{SIMC}} \right) \frac{d^2\sigma}{dt d\phi}_{SIMC}$$

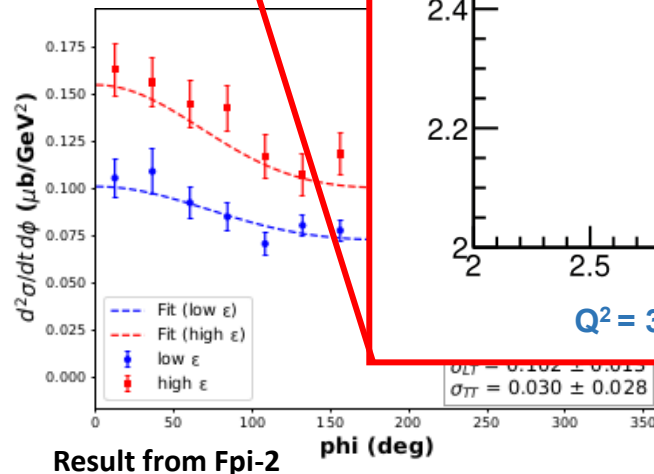
# Importance of Diamond Region

Improve  $\phi$  coverage by taking data at

For each  $\pi$  HMS setting, form ratio:



- Electron spectrometer acceptance is larger for high  $\epsilon$ .
- Selected an overlapped phase-space region.
- Divided data into 7 t-bins based on data statistics.
- Purpose is to ensure consistency across different kinematic settings and measure the t-dependence

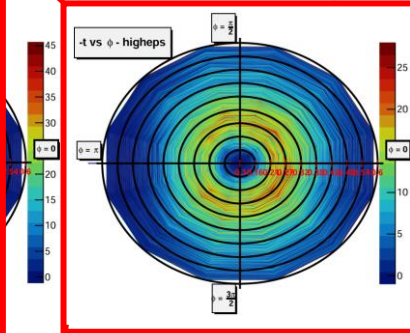
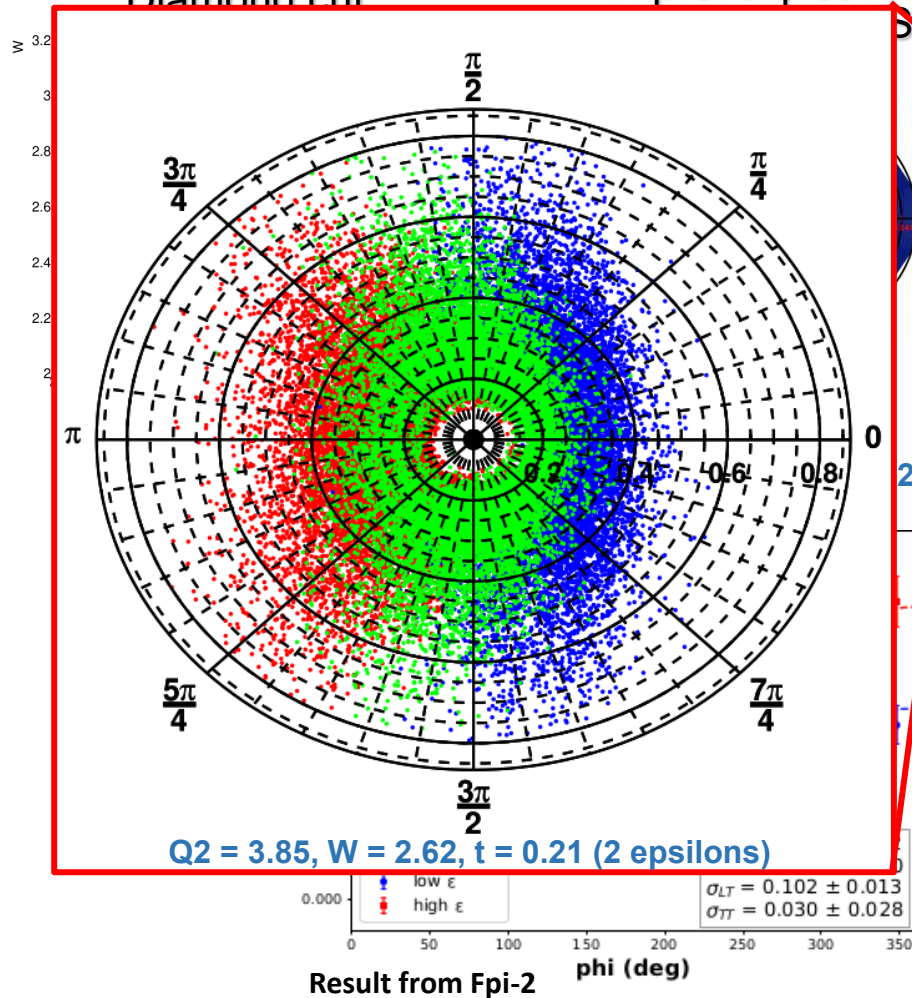


$$2\pi \frac{d^2\sigma}{dt d\phi} = \epsilon \frac{d\sigma}{dt} + \frac{d\sigma}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma}{dt} \cos\phi + \epsilon \frac{d\sigma}{dt} \cos 2\phi$$

# Full $\phi$ -Coverage

Diamond cut

Improve  $\phi$  coverage by taking data at  $\phi$  angles,  $-2^\circ < \theta_{\pi q} < 2^\circ$ .



- To get full- $\phi$  coverage, data is taken on two degrees on the right and left of the central angle by rotating the pion arm.
- **Red** corresponds to the **right angle pion arm setting**
- **Green** corresponds to the **central angle pion arm setting**
- **Blue** corresponds to the **left angle pion arm setting**
- Divided data into 15  $\phi$ -bins to measure the  $\phi$  dependence.

$$2\pi \frac{d\sigma}{dt d\phi}$$

# Normalized Yield Calculation

- The goal is to calculate the experimental cross-sections using the ratio method.

$$\frac{d^2\sigma}{dtd\phi}_{EXP} = \left(\frac{Y_{EXP}}{Y_{SIMC}}\right) \frac{d^2\sigma}{dtd\phi}_{SIMC}$$

- Calculated normalized bin-by-bin data yield.

$$Y_{EXP} = \frac{N}{Q_{eff}}$$

where,

$Q_{eff}$   
= *Charge* × *Tracking Eff* × *Detector Eff* × *EDTM Live Time* × *Boiling Corr*  
× *other normalization factors* ... ..

- Same cuts, binning, and kinematic selections criteria is applied to Monte Carlo (SIMC) to calculate the normalized bin-by-bin SIMC yields.

Normalization Factors	Comments
Charge	Calculated run-by-run
HMS & SHMS Tracking Efficiencies	> 98%
Live Time Correction	>98%
HMS Cerenkov Efficiency	>99%
HMS Calorimeter Efficiency	>99%
SHMS Aerogel Efficiency	>98%
HMS & SHMS Hodoscope Efficiency	>98%
RF Efficiency	>99%
Boiling Correction Factor	Calculated run-by-run
Coin Blocking Correction	Calculated run-by-run
Pion Absorption Correction	~97%

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× *other normalization factors* ... ..

- Same cuts, binning, and kinematic selections criteria is applied to Monte Carlo (SIMC) to calculate the normalized bin-by-bin SIMC yields.
- Calculated ratios (DATA/SIMC) for each t & phi-bin setting-by-setting, separately.

$$R(t, \phi) = \frac{Y_{EXP}}{Y_{SIMC}}$$

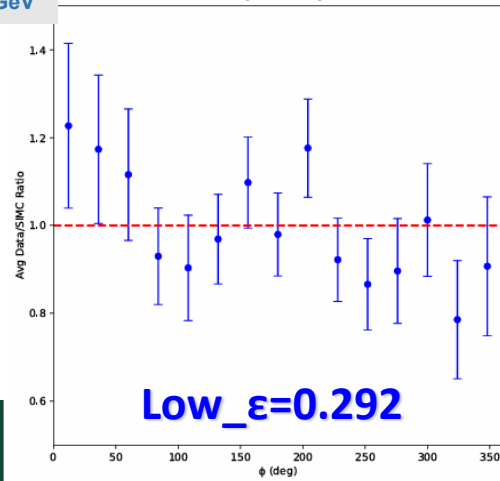
- Combined data from each pion arm angle setting per  $\epsilon$  by calculating their error-weighted average.

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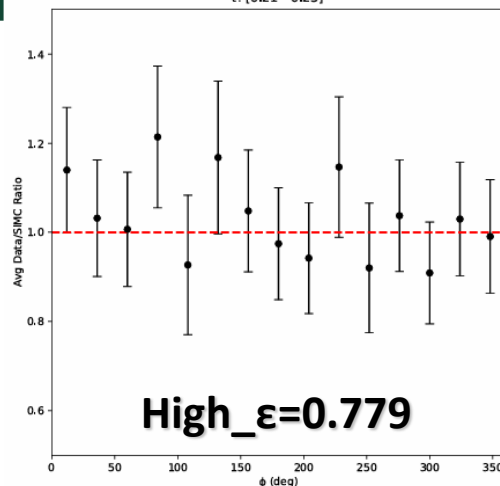
# High & Low-epsilon Data/MC Ratios

$Q^2 = 3.85 \text{ GeV}^2, W = 2.62 \text{ GeV}$

$t: [0.21 - 0.23]$



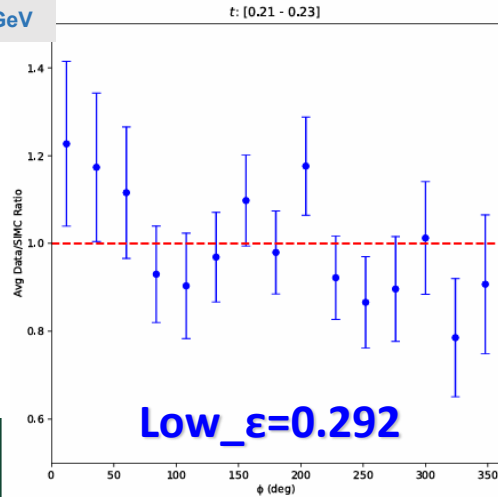
$t: [0.21 - 0.23]$



$$R(t, \varphi) = \frac{Y_{\text{EXP}}}{Y_{\text{SIMC}}}$$

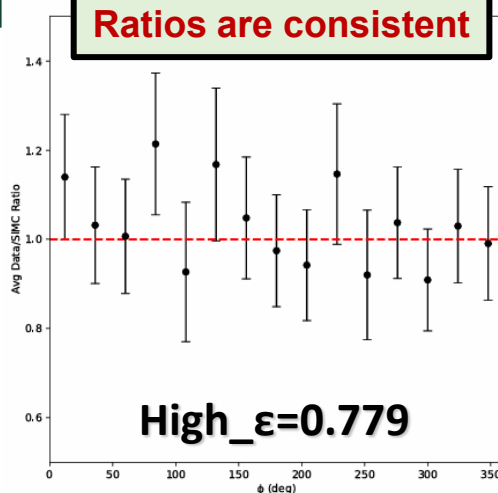
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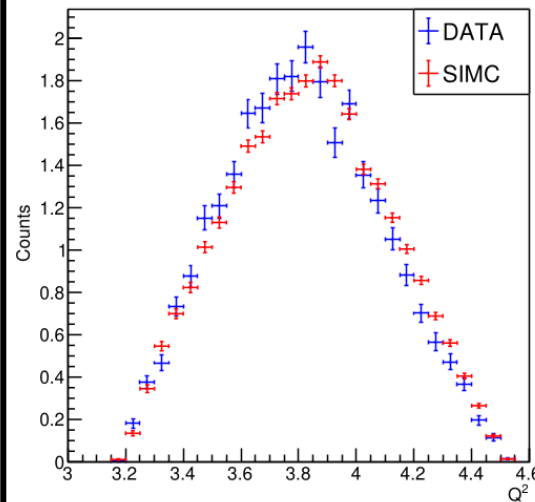
$$R(t, \phi) = \frac{Y_{\text{EXP}}}{Y_{\text{SIMC}}}$$

**Ratios are consistent**



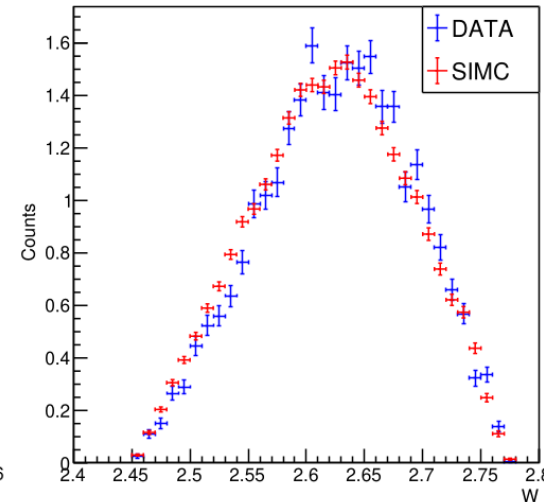
Compared kinematic and spectrometer variables between data and SIMC to verify that the SIMC model reliably reproduces the measured distributions.

Q2 Distribution



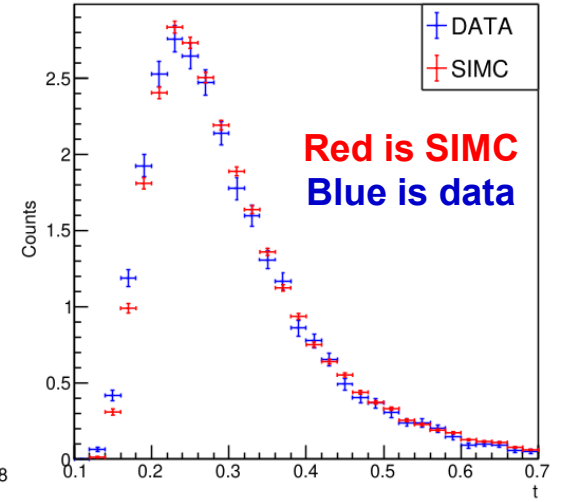
$$Q^2 = -(P_e - P_{e'})^2$$

W Distribution



$$W^2 = (P_\gamma + P_p)^2$$

t Distribution

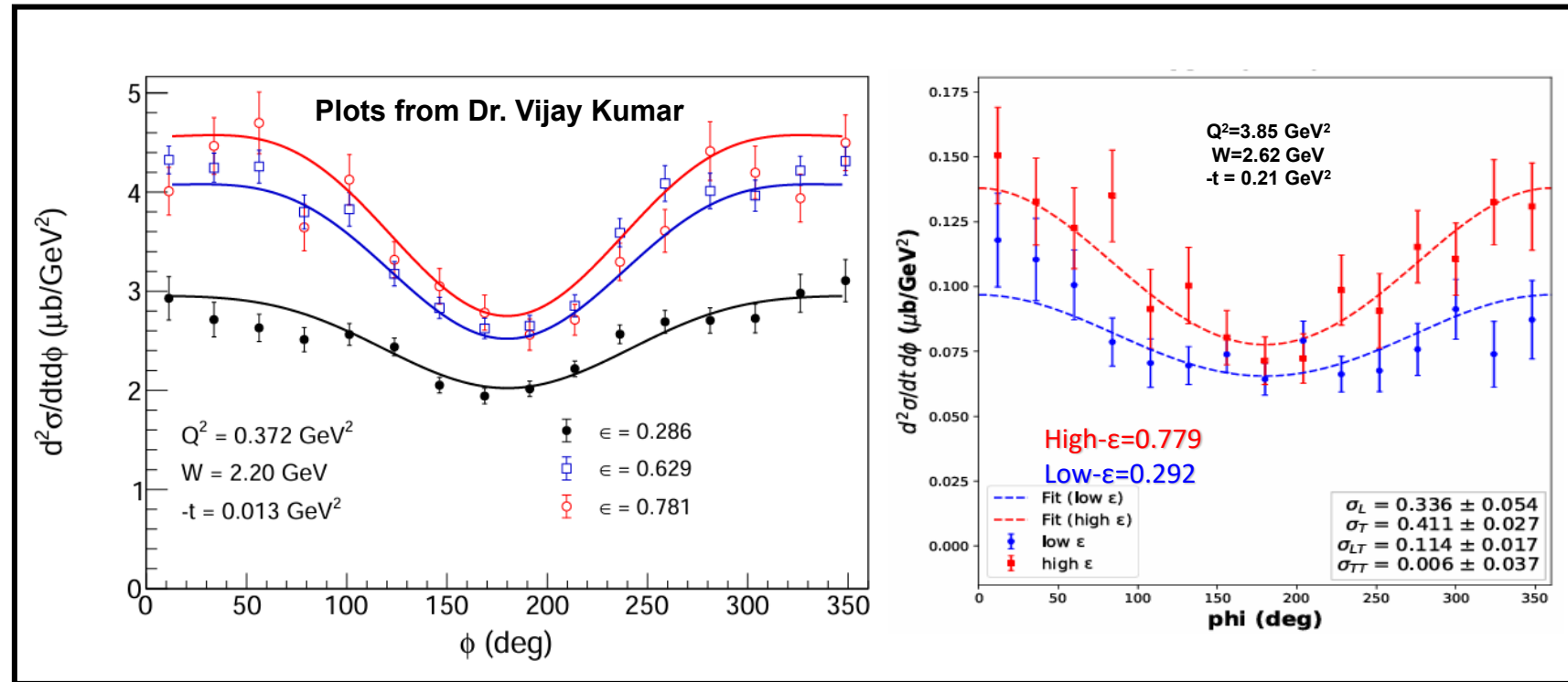


$$t = (P_\gamma - P_\pi)^2$$

$Q^2 = 3.85 \text{ GeV}^2, W = 2.62 \text{ GeV}$  (low-epsilons)

# L/T Separated Cross-section Measurements

- ❑ This L/T Separation technique is model-dependent.
- ❑ Requires the SIMC empirical model to reproduce data.
- ❑ Only reliable if SIMC reproduces the data well in both shape and normalization.
- ❑ Fit the Rosenbluth equation to extract the cross-section components.
- ❑ Need to iteratively tune L/T/LT/TT empirical model until MC reproduces experimental data.



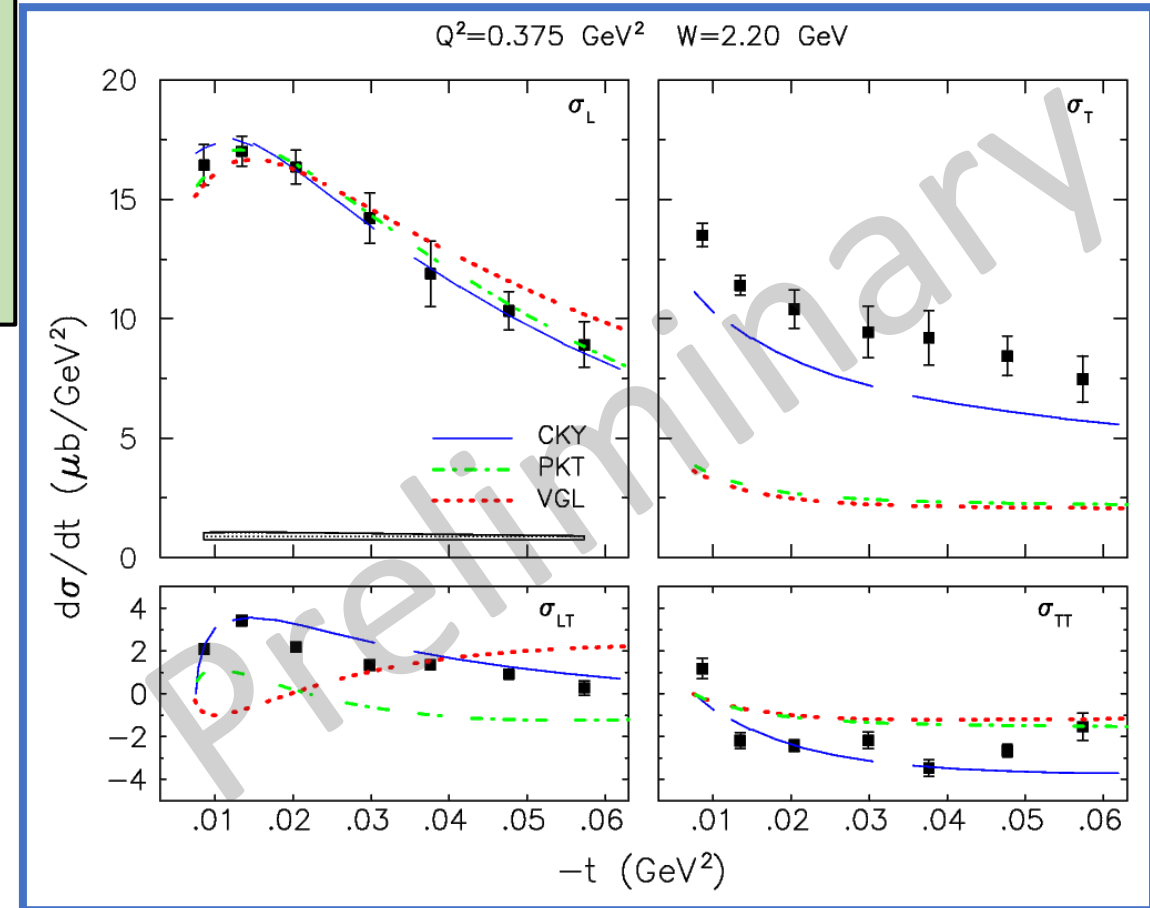
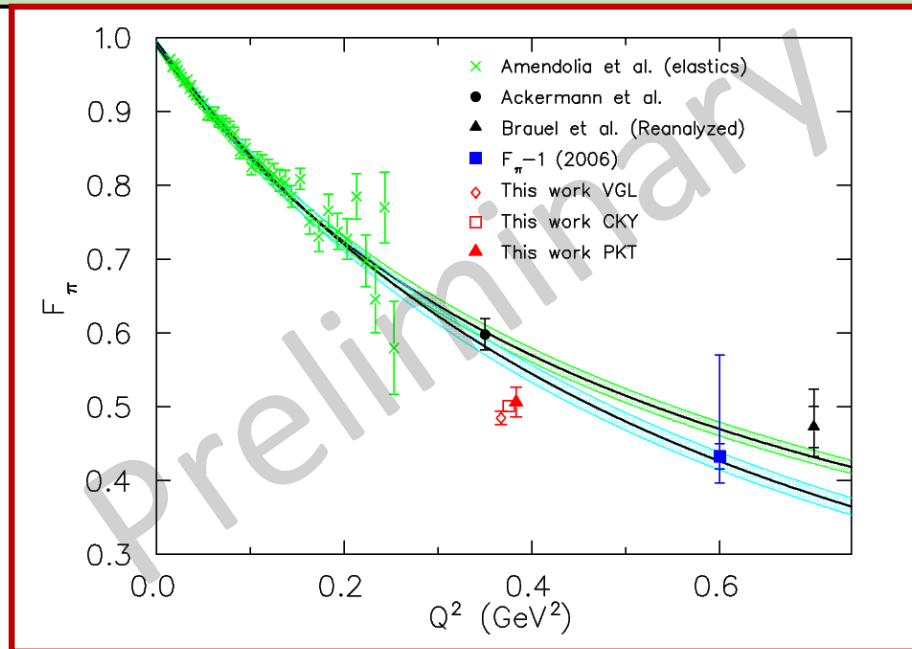
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# Model Dependence & Future Extraction of $F_\pi$

- ❑ Our philosophy is to publish our experimentally measured  $\frac{d\sigma_L}{dt}$ , so that updated values of  $F_\pi(Q^2)$  can be extracted as improved theoretical models become available.
- ❑ Jefferson Lab  $F_\pi$  experiments have primarily used three models for form-factor extraction:
  - **VGL Regge Model** — Vanderhaeghen, Guidal, Laget, PRC 57, 1454 (1998)
    - VGL model has proven to give a **reliable description of  $\sigma_L$**  over a across a wide kinematic domain.
    - However, VGL **significantly underestimates  $\sigma_T$** , indicating the need for improved models to fully describe the separated cross-section data.
  - **CKY Regge Model** — Choi, Kong, Yu, JKPS 67, L1089 (2015)
    - **This motivated the development of the CKY model**, aimed at improving the description of  $\sigma_T$  without degrading the successful description of  $\sigma_L$ .
  - **PKT Model** — Perry, Kizilersu, Thomas, PLB 807, 135581 (2020)
    - A **modern pion electroproduction model** was developed to improve theoretical consistency and study model dependence in the extracted  $F_\pi(Q^2)$ .
    - The PKT model provides an alternative framework for comparing how different reaction models affect the form-factor extraction.
- ❑ **More theoretical models are welcome**, especially those capable of describing both  $\sigma_L$  and  $\sigma_T$  consistently.

# Results from Low- $Q^2$ Pion-LT Experiment

- **CKY model describes the  $t$ -dependence of  $\sigma_L$  very well.**
- **The VGL and PKT models dramatically underestimate the  $\sigma_T$**
- **CKY model provides much better T/L ratio, as expected.**
- **CKY model is also doing good job for  $\sigma_{LT}$  and  $\sigma_{TT}$ .**
- **The results are consistent with the elastic fits of Amendolia et al. - ~one standard deviation below**

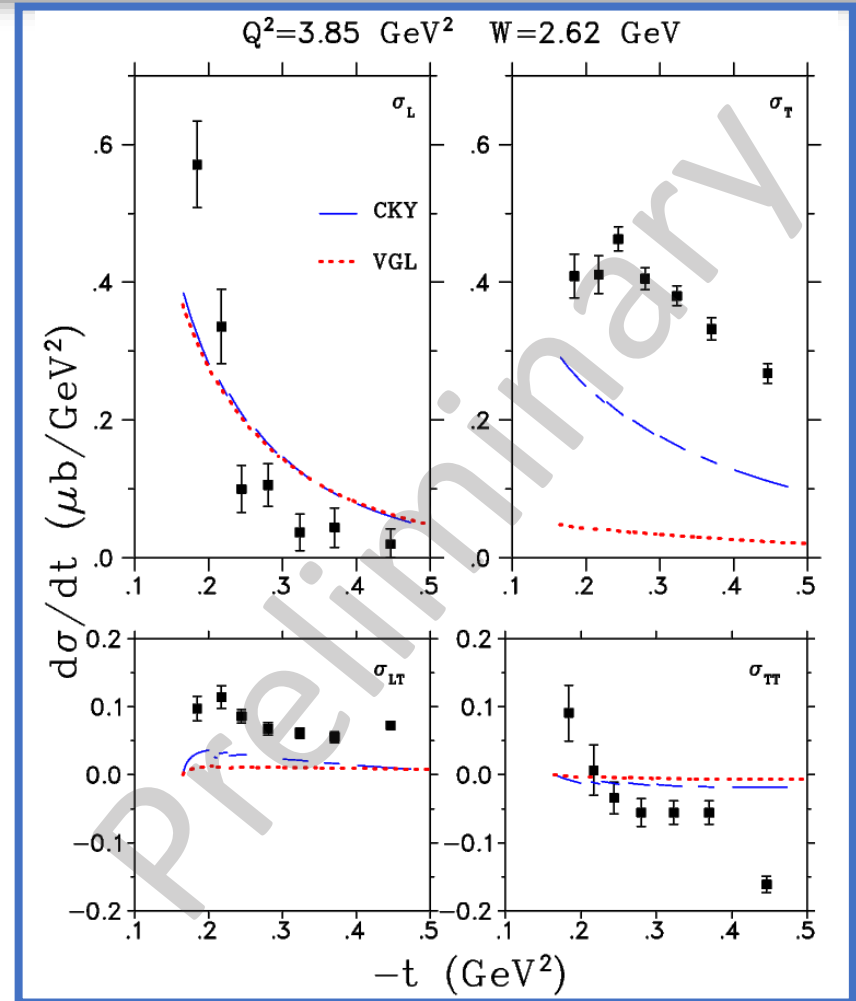
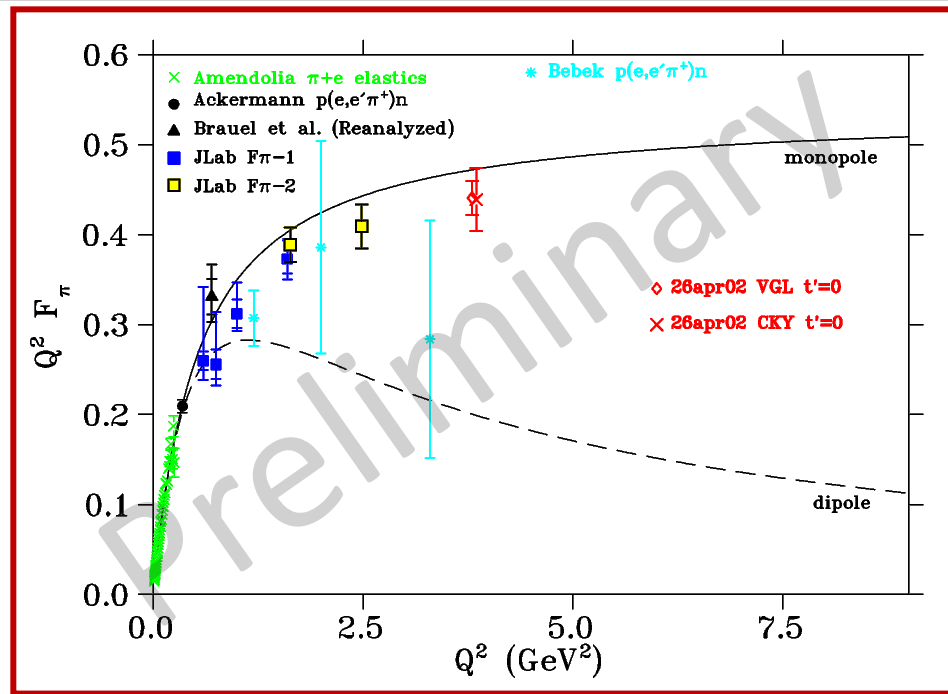


Plots from Dr. Vijay Kumar

Model is evaluated at precise kinematics of data. Discontinuities indicate change in  $(Q^2, W)$  for each  $t$ -bin.

# Results from Moderate- $Q^2$ Pion-LT Experiment

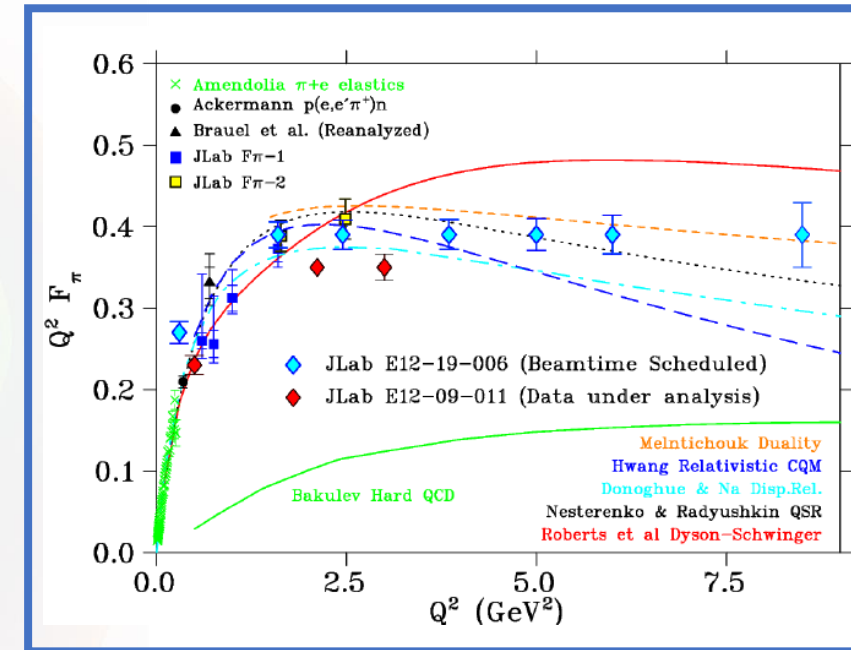
- The VGL model struggles to describe the  $t$ -dependence of  $\sigma_L$  well, and dramatically underestimates T/L ratio.
- The CKY model also struggles to describe the  $t$ -dependence of  $\sigma_L$  well, but has a better T/L ratio.
- Comparison with PKT Model is in progress.



Model is evaluated at precise kinematics of data. Discontinuities indicate change in  $(Q^2, W)$  for each  $t$ -bin.

# Summary and Future Plans

- ❑ **E12-19-006 (12 GeV Flagship Experiment) is expected to provide the definitive  $p(e, e'\pi^+)n$  L/T-separation data set and will remain important for decades to come.**
- ❑ **Preliminary L/T separation is completed for  $Q^2=0.37$  GeV<sup>2</sup> and  $Q^2=3.85$  GeV<sup>2</sup> physics settings.**
- ❑ **Systematic uncertainty studies still need to be done for  $Q^2=3.85$  GeV<sup>2</sup>.**
- ❑ **Will analyze the other two  $Q^2=3.85$  physics settings to calculate the L/T separated cross-sections using the Rosenbluth technique and extract the pion form factor.**
- ❑ **Will do a detailed comparison with existing VGL, CKY, and PKT theoretical models.**
- ❑ **Results will help to understand the dependence of the Form factor and in validating theoretical models.**
- ❑ **Expected to be graduated in fall 2026. Publications are expected soon.**



Projected Results

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