

# Proposal PR12-12-011:

Measurements of  $A_{\parallel}$  and  $A_{\perp}$  to Extract  $G_E^n$  and  $G_M^n$  at  
 $Q^2 = 1 - 2.6 \text{ (GeV/c)}^2$  from the Inclusive  
 $\vec{^3\text{He}}(\vec{e}, e')$  Reaction

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for the PR12-12-011 Collaboration

PAC 39 Meeting

June 21<sup>st</sup>, 2012

# Motivation

- **Neutron** not understood to the same accuracy as the proton
  - No pure neutron target
  - **Indirect measurements** using appropriate targets: deuteron and/or  $^3\text{He}$
- **High precision** measurement will help pin down **theoretical treatments** on the extraction of the the neutron electromagnetic form factors from different nuclei (**deuteron** and  $^3\text{He}$ ) and different reaction channels  **$A(e,e')$**  and  **$A(e,e'n)$**
- Theoretical models and parameterizations begin to diverge for  $Q^2 > 1 \text{ (GeV/c)}^2$
- Compared to the other form factors the precision on  $G_E^n$  is poorly constrained over the measured  $Q^2$  range (**only three data points have a precision better than 10%**)

# Extraction of $G_E^n$ at $Q^2 = 0.98 \text{ (GeV/c)}^2$ by Measurements of $^3\text{He}(\vec{e}, e')$

- $G_E^n$  was extracted for the first time by inclusive polarized measurements from  $^3\text{He}$  at  $Q^2 = 0.98 \text{ (GeV/c)}^2$
- Form the ratio of asymmetries for longitudinal and transverse target polarization; use the well known proton electromagnetic and the neutron magnetic form factors
- **Proton and neutron contributions calculated in PWIA**
- This technique agrees with previous measurements; uncertainty  $\sim 19\%$  (limited by statistics in only a few shifts of data)
- **Note: M. Sargsian and G. Salme` are ready to support full model extractions of precision data**

# <sup>3</sup>He Inclusive Response Functions near the Quasi-elastic Peak in PWIA

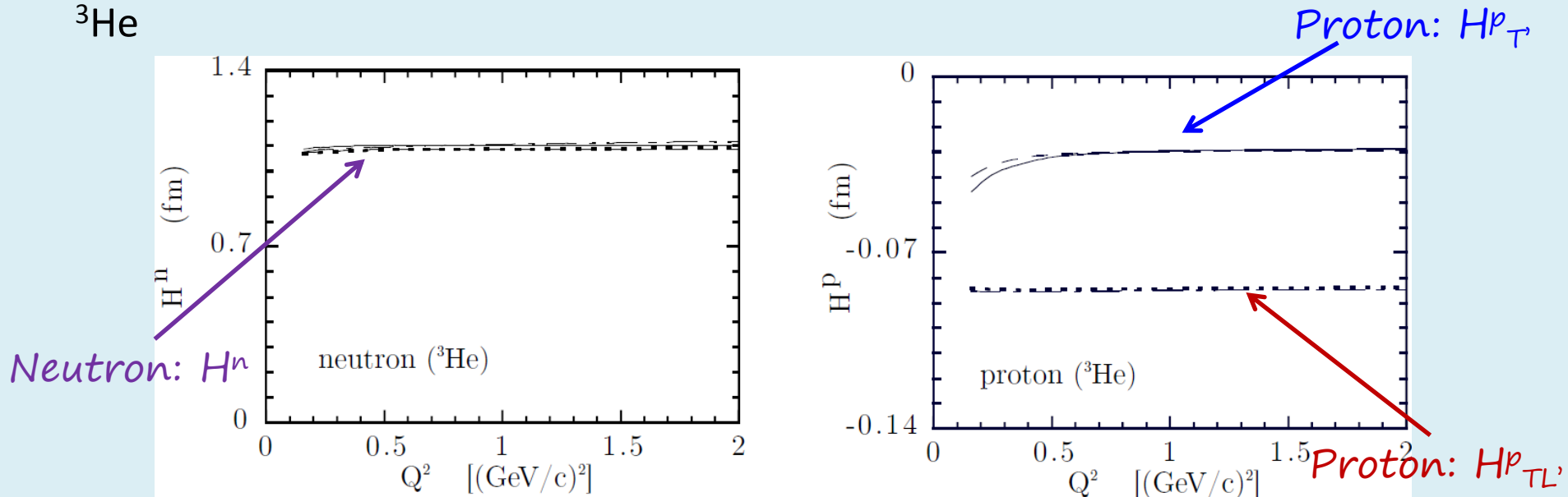
Transverse-  
longitudinal:

$$R^{^3\text{He}}_{TL'} = -\sqrt{2}[2G_E^p G_M^p H^p_{TL'} + G_E^n G_M^n H^n_{TL'}]$$

Transverse:

$$R^{^3\text{He}}_{T'} = \frac{Q^2}{2qM} [2(G_M^p)^2 H^p_{T'} + (G_M^n)^2 H^n_{T'}]$$

where  $H$ 's are calculated by momentum distribution and nucleon polarization in <sup>3</sup>He



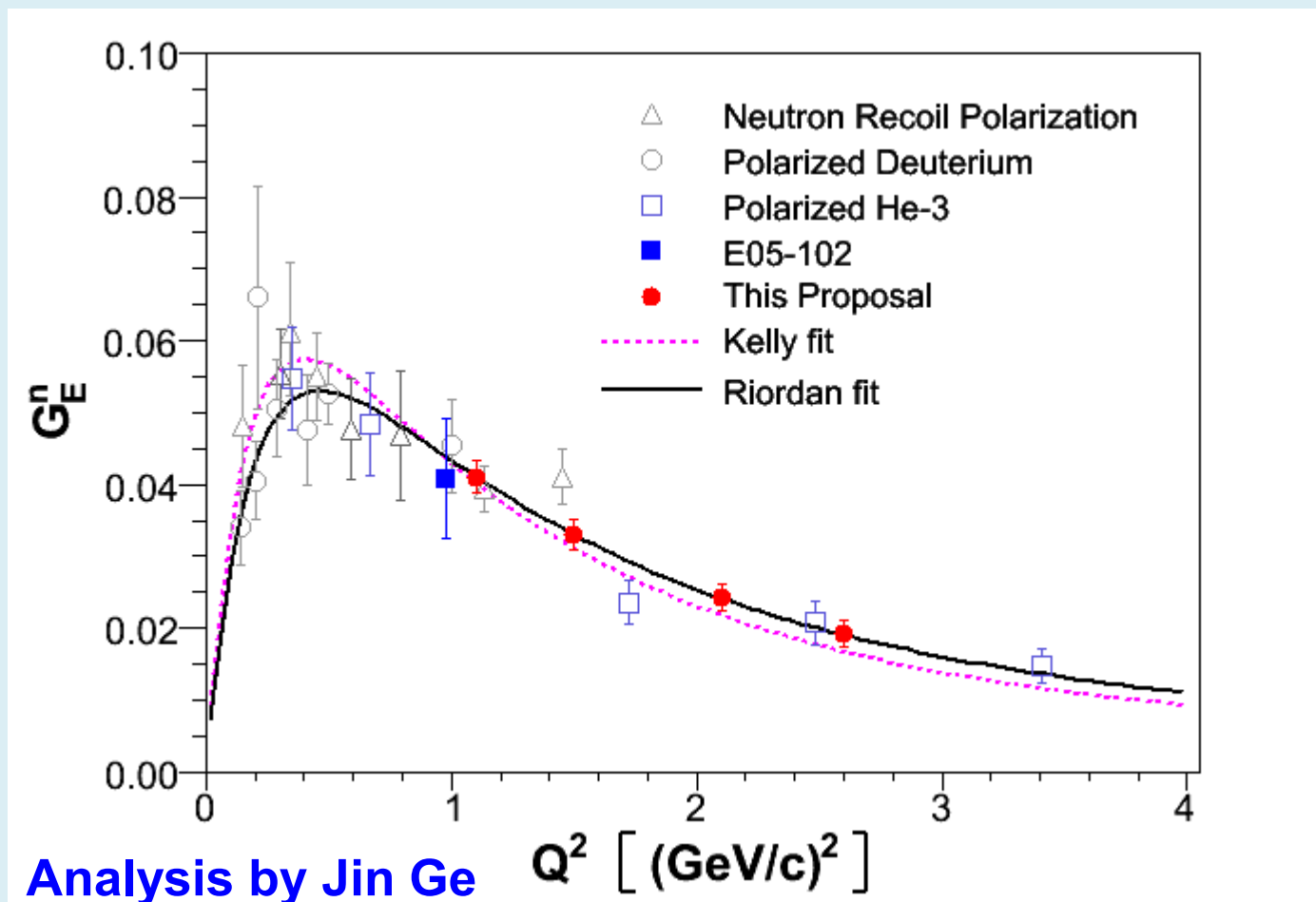
A. Kievsky, E. Pace, G. Salme' and M. Viviani, PRC 56 (1997) 64

# Ratio of Asymmetries as a Function of Form Factors

$$\frac{A_{TL'}}{A_{T'}} = \frac{v_{TL'}(-\sqrt{2}[2G_E^p G_M^p H^p_{TL'} + G_E^n G_M^n H^n_{TL'}])}{v_{T'}(\frac{Q^2}{2qM}[2(G_M^p)^2 H^p_{T'} + (G_M^n)^2 H^n_{T'}])}$$

- By measuring  $A_{TL'}/A_{T'}$  and using  $G_E^p$ ,  $G_M^n$ , and  $G_M^p$  as known parameters can one extract  $G_E^n$

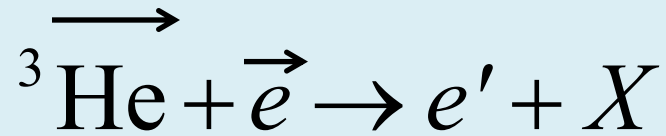
# $G_E^n$ from $^3\text{He}(e,e')$ at $Q^2=0.98 \text{ (GeV/c)}^2$ with a few shifts of data



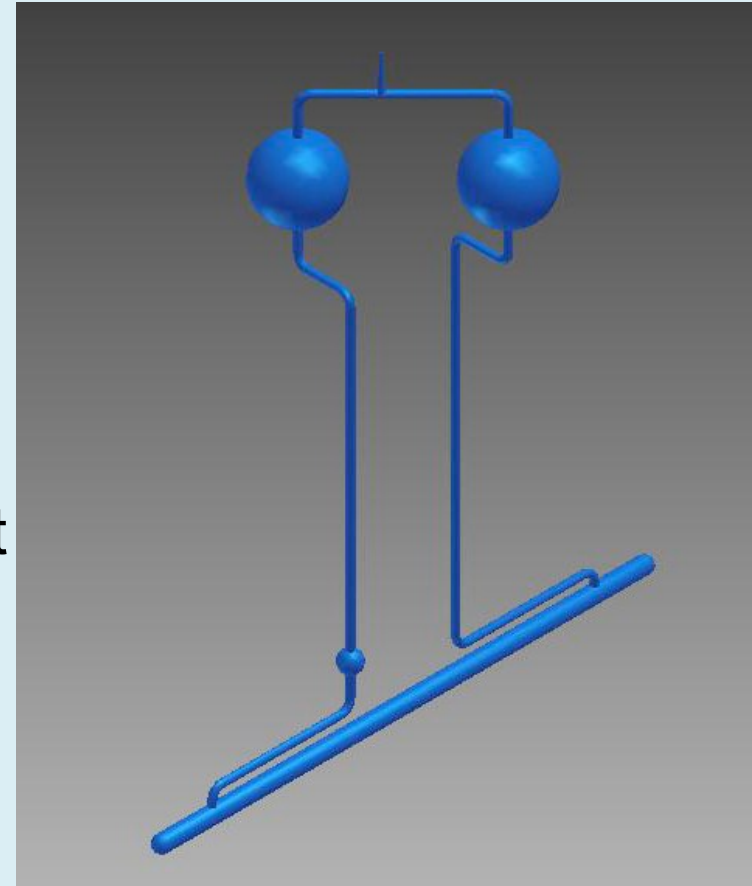
$$G_E^n/G_D = 0.234 \pm 0.044 \text{ (stat)} \pm 0.011 \text{ (syst)}$$

$$G_E^n = 0.0414 \pm 0.0077 \text{ (stat)} \pm 0.0019 \text{ (syst)}$$

# Overview of Experiment

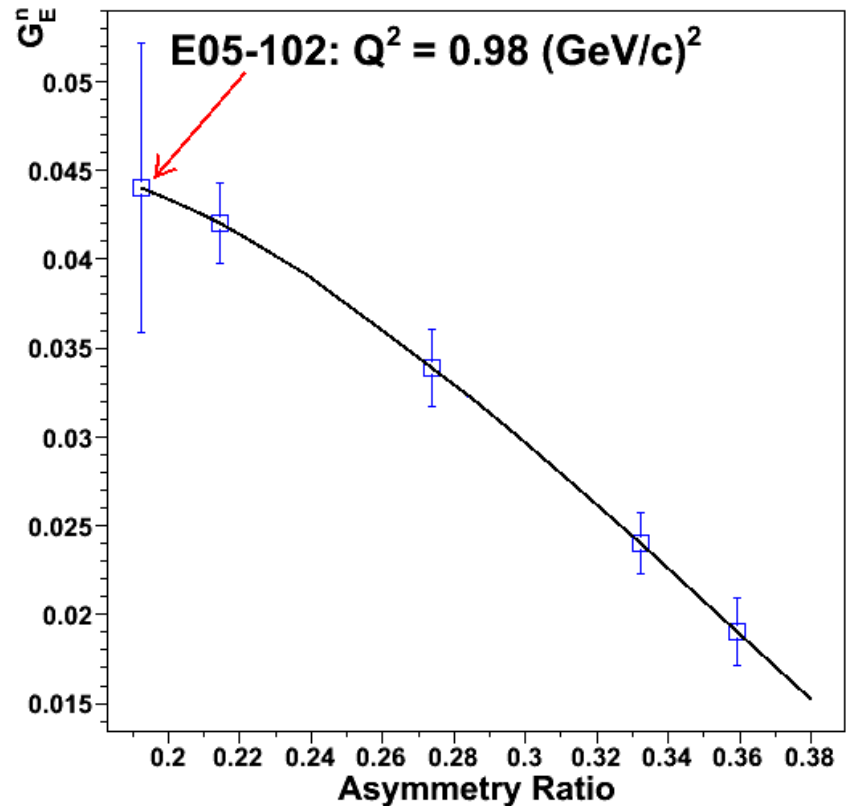
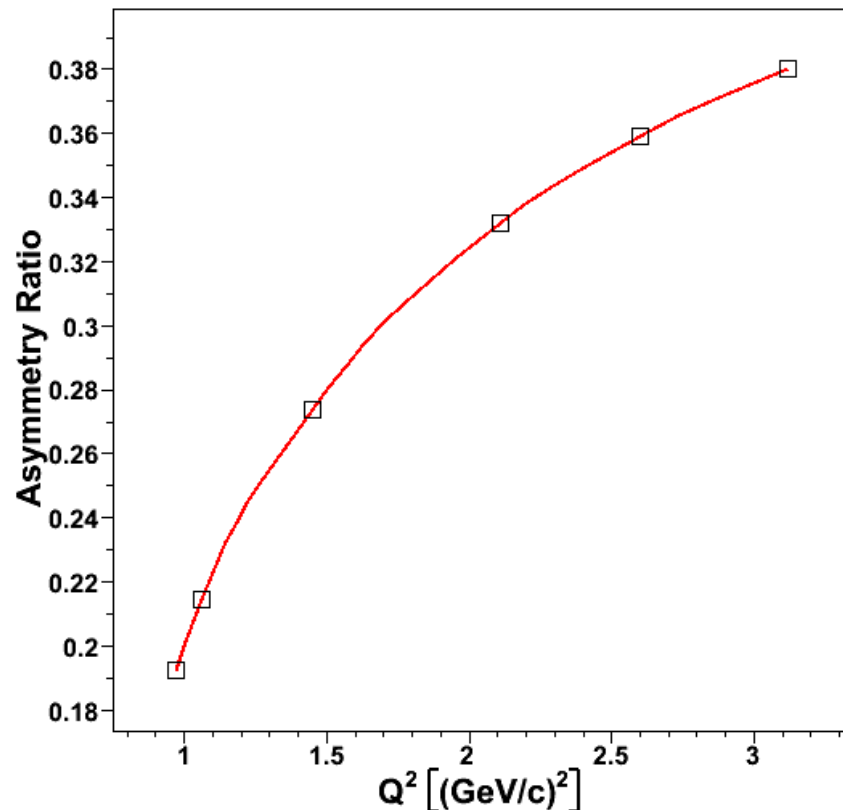


- Measure inclusive double-polarized  ${}^3\text{He}$  asymmetries
- Use the Hall C Super High Momentum Spectrometer (SHMS) to detect the scattered electrons at 6 and 8.5 degrees with 11 GeV beam
- Use the upgraded polarized  ${}^3\text{He}$  target planned for the  $A_1^n$  (E12-06-110) and  $d_2^n$  (E12-06-121) experiments
- Considering to detect the knock-out proton in the High Momentum Spectrometer (HMS)



# Form Factor Sensitivity to Asymmetry Ratio

$$A_{ratio} = \frac{A_{TL'}}{A_{T'}}$$



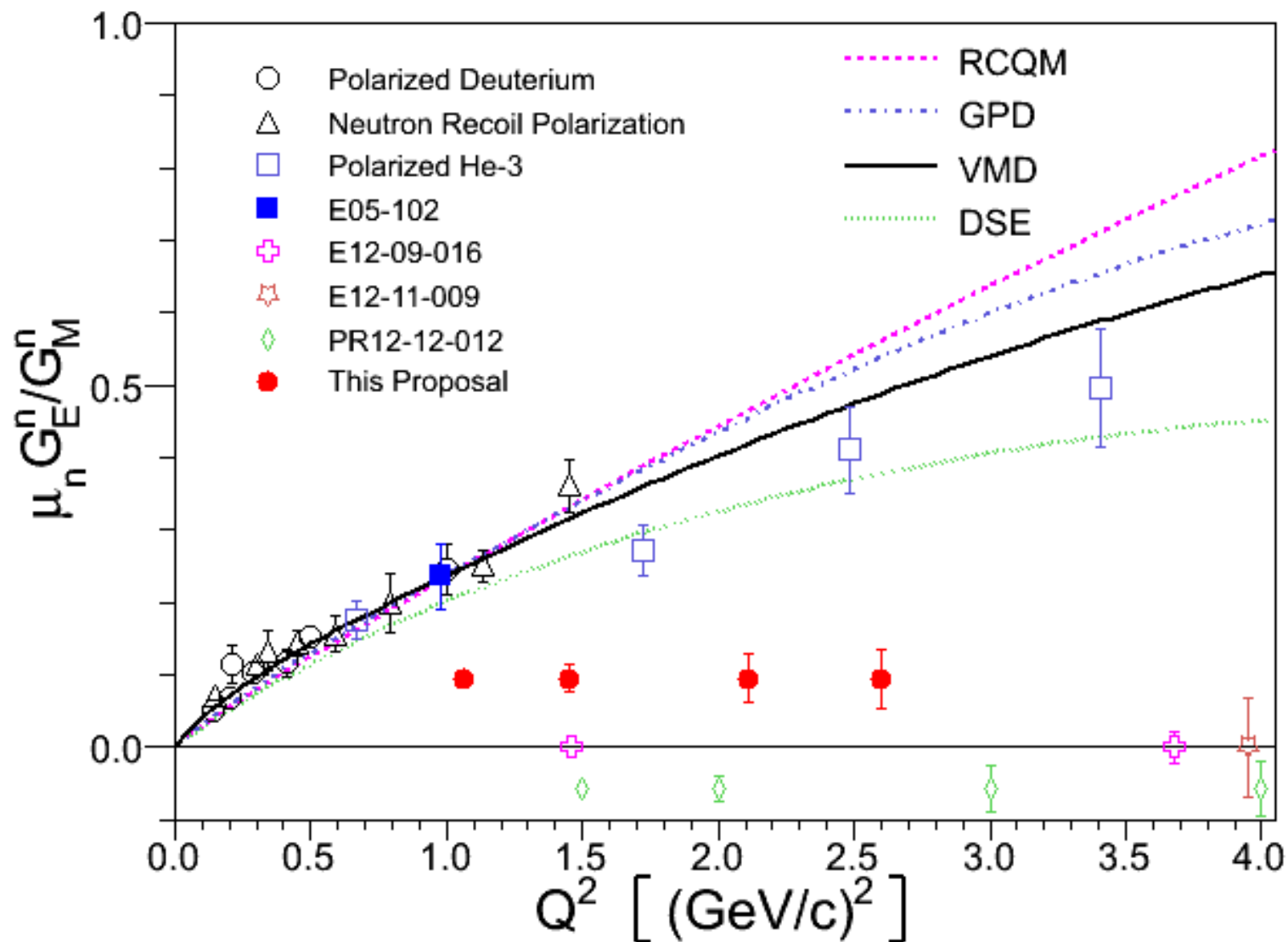


# Kinematics and Rates

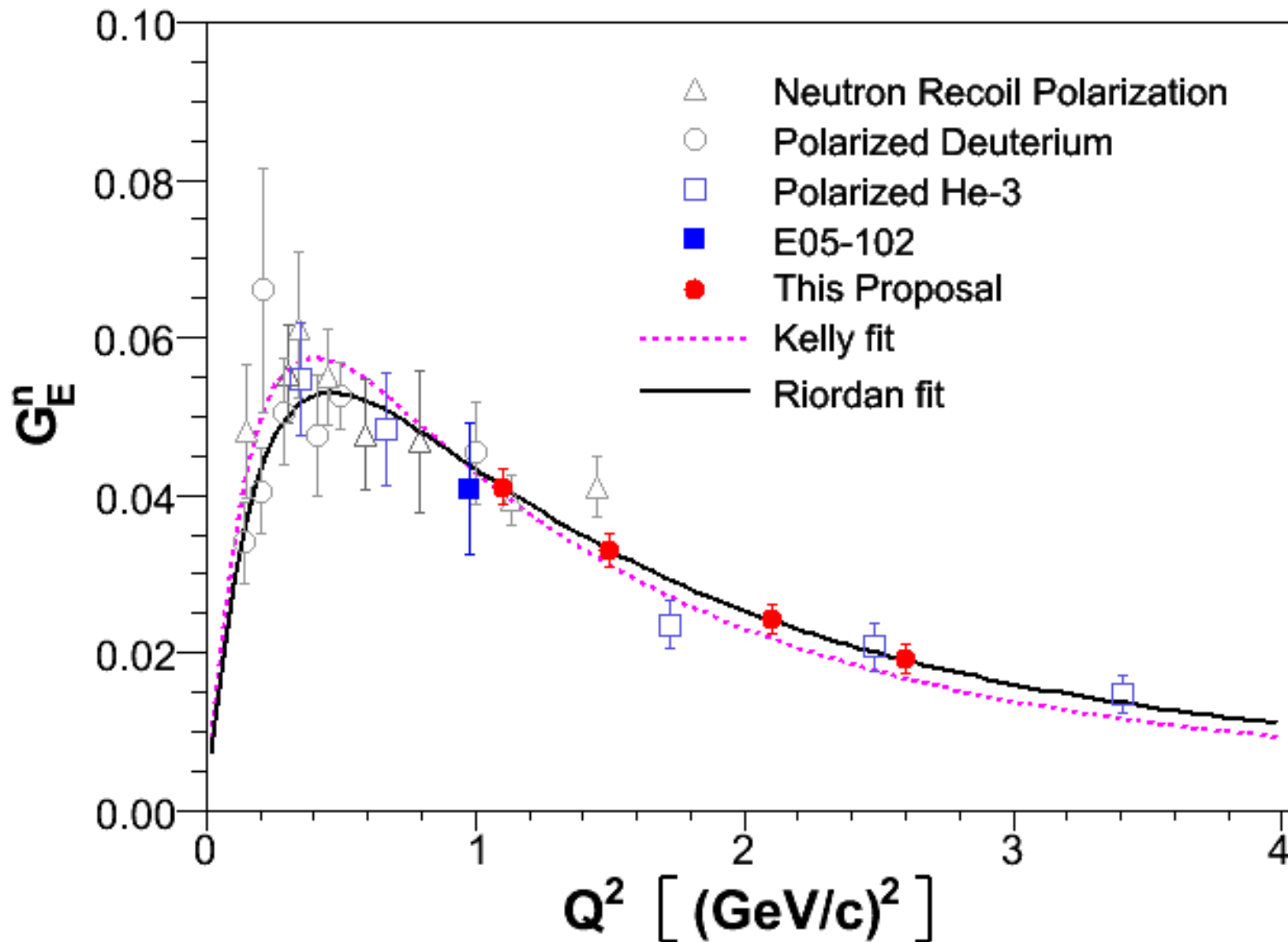
$E_0$ [GeV]	$E'$ [GeV]	$\theta_{\text{SHMS}}$ [deg]	Range of $\theta_{\text{lab}}$ [deg]	$Q^2$ (GeV/c) <sup>2</sup>	$e^-$ rate [kHz]	$t_{\parallel}$ [hrs]	$t_{\perp}$ [hrs]	$\Delta A_{\parallel}$ [ $\cdot 10^{-4}$ ]	$\Delta A_{\perp}$ [ $\cdot 10^{-4}$ ]
11.0	10.437	6	5 – 6	1.057					
11.0	10.229	6	6 – 7	1.446	7.70	48	6	0.8	2.2
11.0	9.874	8.5	7.5 – 8.5	2.114					
11.0	9.612	8.5	8.5 – 9.5	2.604	0.37	240	36	1.6	4.1

- Utilize full capabilities of SHMS (**11 GeV forward angle**)
  - Take advantage of the **rate boost from  $\sigma_{\text{Mott}}$**
  - Helps **minimize inelastic backgrounds**
- Estimated quasi-elastic counting rates for a 42-cm long target with 60% target polarization, 80% beam polarization at 60  $\mu\text{A}$
- Based on J. Arrington parameterization for  $G_E^p$  and  $G_M^p$  and CLAS data for  $G_M^n$

# Expected Results



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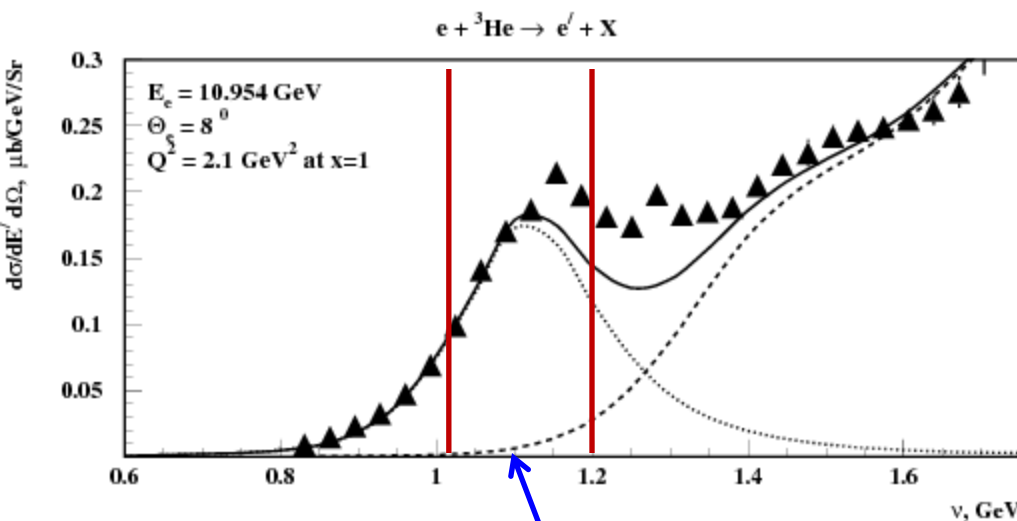


# Concerns Raised by PAC 39 and TAC

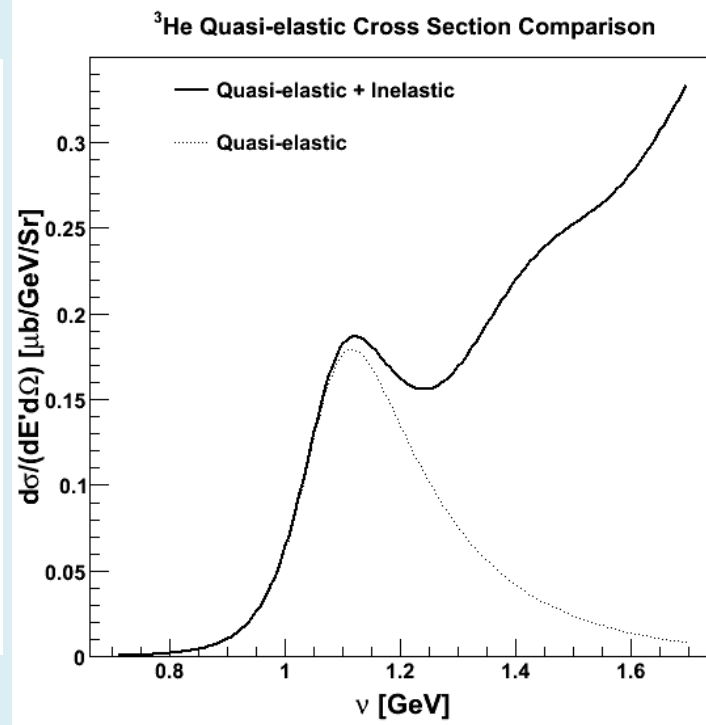
- Polarized Inelastic background contamination
- Final State Interactions (FSI) and Meson Exchange Currents (MEC)
- Relativistic Effects

# Inelastic Contamination

- Used the cross section models from Misak Sargsian and Peter Bosted (<http://arxiv.org/abs/1203.2262>)
- The two models agree well with each other at the top of the quasi-elastic peak with less than a 0.5% absolute difference



$\delta = 2\%$



# Inelastic Contamination

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- By varying the momentum cut, the effect of the contamination can be studied with the data

$Q^2$ (GeV/c) <sup>2</sup>	Contamination $x = 1$ [%]	Contamination (dp = 2%) [%]	Contamination (dp = 1.5%) [%]
1.06	0.3	0.7	0.4
1.45	1.5	3.0	1.7
2.11	4.6	8.8	4.9
2.60	7.8	11.9	6.8

# Inelastic Contamination on Asymmetry

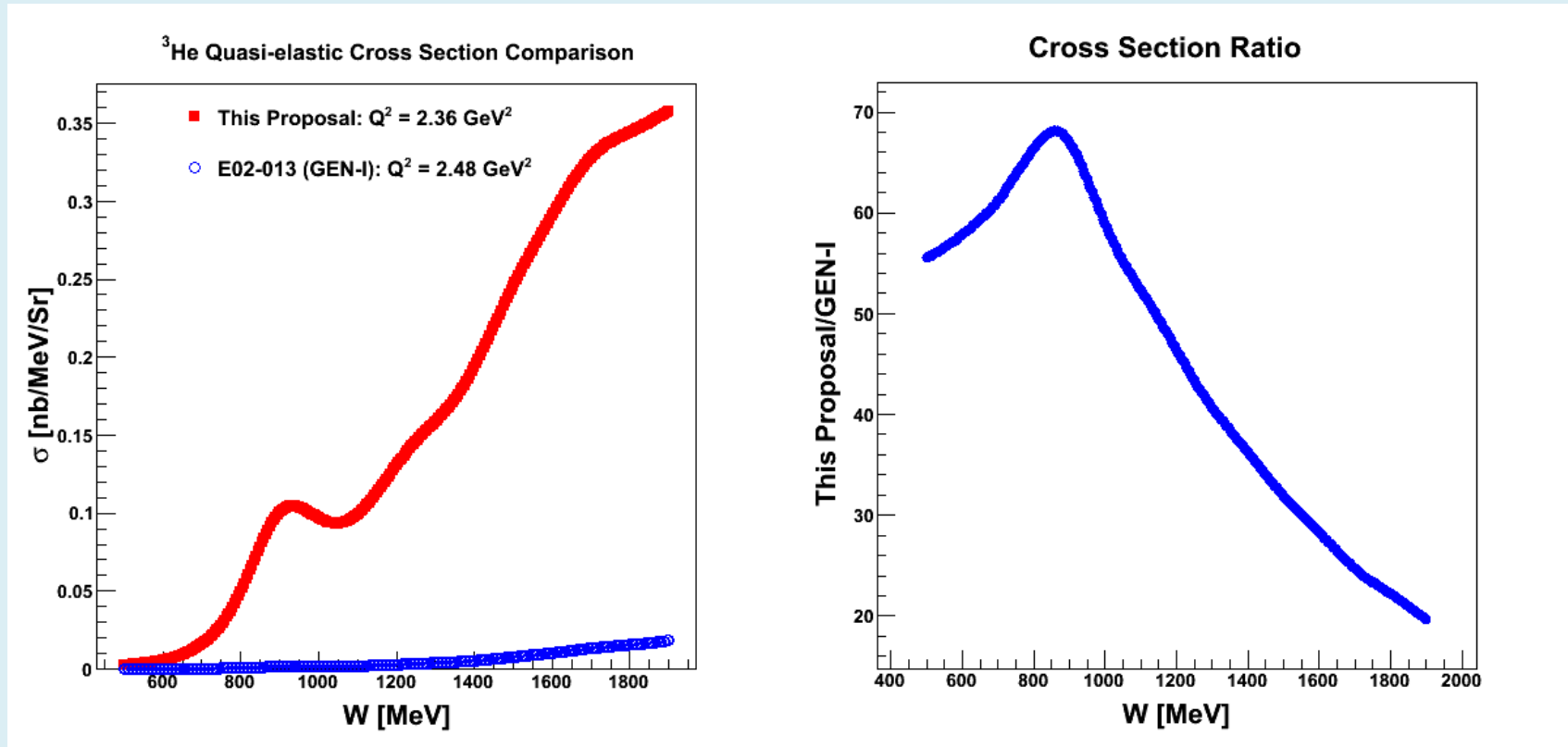
$$A_{QE} = \frac{(A_{raw} - f_c \cdot A_{in})}{1 - f_c}$$

- $f_c$  is the amount of contamination under the quasi-elastic peak
- $A_{QE}$ ,  $A_{raw}$  and  $A_{in}$  are the quasi-elastic, measured and inelastic asymmetries
- Using the determined contamination numbers from the models and the measured asymmetries from experiments E01-012 and E05-102 with the assumption that  $A_{in} = A_{\Delta}$ , the effect on the asymmetry was calculated

$Q^2$ (GeV/c) <sup>2</sup>	$A_{raw}$	$A_{QE}$	Difference [%]
1.0	-0.1656	-0.1699	2.5
2.6	-0.2325	-0.2258	3.0

# Comparison of Cross Sections at $Q^2 \sim 2.5 \text{ GeV}^2$

The quasi-elastic cross section is about a factor of 70x larger at forward angle compared to the GEN-1 data point.



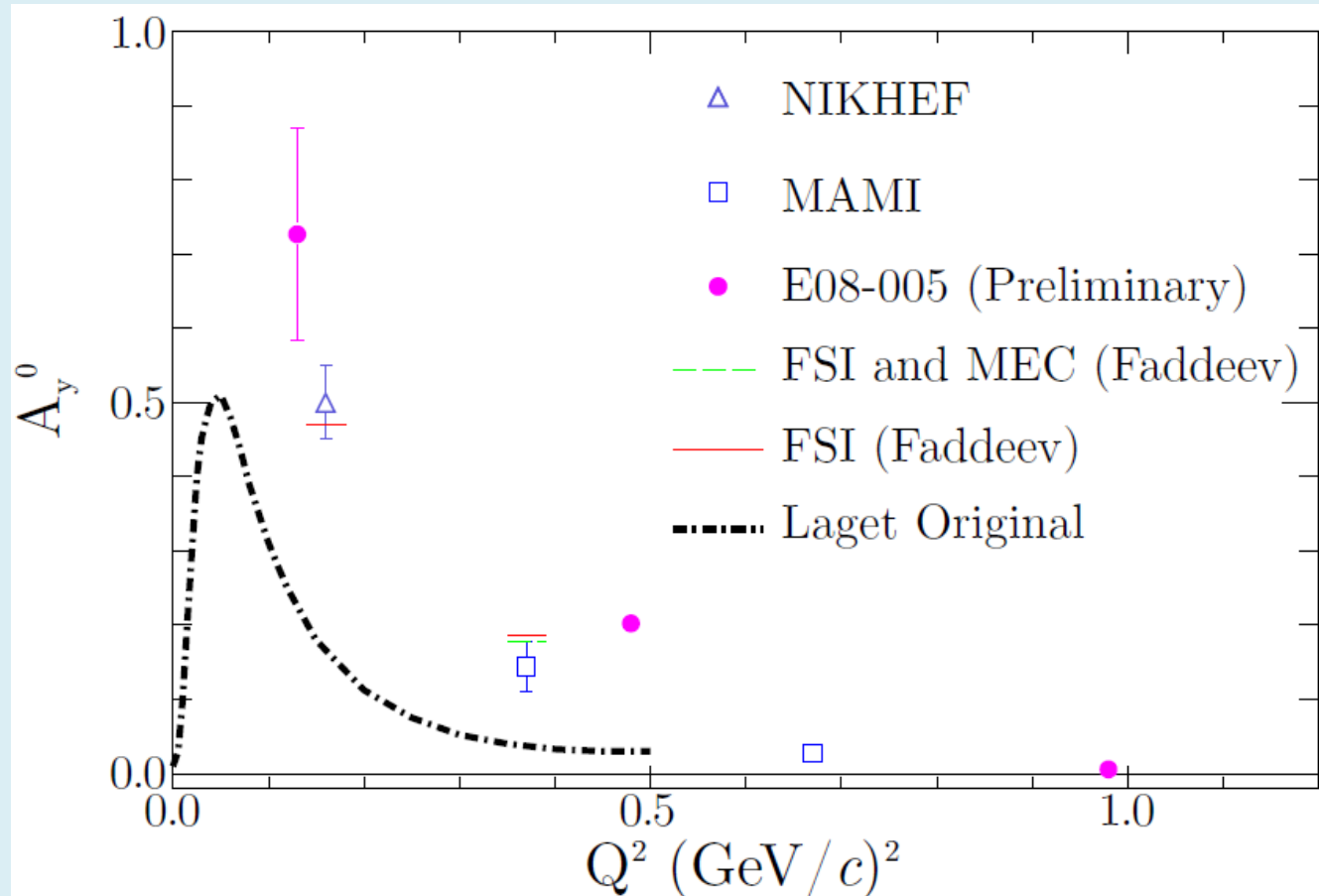
## Cross section model from P. Bosted

- The proposed measurement benefits from the SHMS resolutions compared to BigBite
- We will also measure the inelastic contribution within the SHMS momentum acceptance, allowing us to **carefully choose our cuts for each  $Q^2$  point**



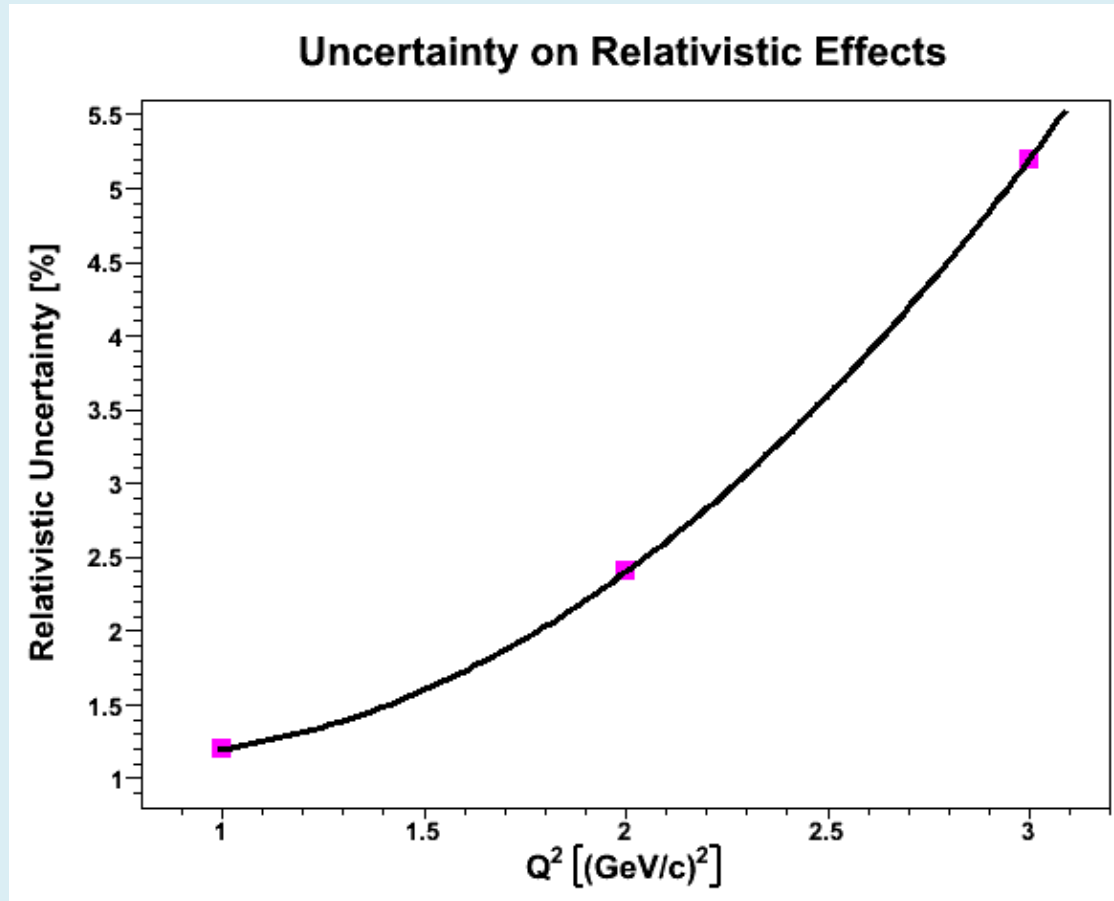
# FSI and MEC vs. $Q^2$

- Experiment E08-005: recent  $^3\text{He}^\uparrow(e,e'n)$  single spin asymmetry ( $A_y$ ) measurements, **target polarized normal to scattering plane**
- $A_y$  vanishes in PWIA, and measurements of this asymmetry are a good check of **FSI and MEC contributions**
- Small asymmetry near 1 (GeV/c) $^2$  is indicative that these mechanisms have become negligible
- Analysis by E. Long



# Relativistic Effects

- Misak Sargsian compared his model calculation using the Virtual Nucleon and Light Cone approximations
- He provided the difference in these two methods as the uncertainty due to relativistic effects
- Giovanni Salme` is constructing a Poincare` invariant approach for the relativistic treatment in his calculation



# Relativistic Effects

- Misak Sargsian compared his model calculation using the Virtual Nucleon and Light Cone approximations
- He provided the difference in these two methods as the uncertainty due to relativistic effects
- Giovanni Salme` is constructing a Poincare` invariant approach for the relativistic treatment in his calculation

$Q^2$ (GeV/c) <sup>2</sup>	Total Model Uncertainty (2012) [%]
1.06	2.2
1.45	2.4
2.11	3.2
2.60	4.3

# Estimated Systematic Uncertainties

$Q^2$ (GeV/c) <sup>2</sup>	$G_E^p$ [%]	$G_M^p$ [%]	$G_M^n$ [%]	Model [%]	Experimental [%]	Inelastics [%]	( $\sigma_{\text{syst}}$ ) [%]	( $\sigma_{\text{stat}}$ ) [%]	( $\sigma_{\text{total}}$ ) [%]
1.057	1.4	1	0.1	2.2	2.3	2.0	4.1	3.5	5.4
1.446	1.4	0.8	0.5	2.4	2.3	2.0	4.2	4.5	6.4
2.114	1.4	0.6	0.9	3.2	2.3	3.0	5.2	5.0	7.2
2.604	1.4	0.5	1.3	4.3	2.3	3.0	6.0	8.0	10.0

- Relative systematic uncertainties from nucleon form factors, model (updated numbers from M. Sargsian), experimental (beam pol. 1.5%, target pol. 1%, radiative corrections 1%), and the inelastic contamination
- GEp: 1% at  $Q^2 = 1$  (GeV/c)<sup>2</sup> with a linear increase up to 3% at 3 (GeV/c)<sup>2</sup>
- GMp: 1% over the planned  $Q^2$  range
- GMn: 2% to 2.4% from the high precision Hall B data (J. Lachniet *et al.*)

# Beam Time Request

	Time (Hours)	Time (Days)
Long. Pol. $^3\text{He}$ at 11 GeV, 6 degs	48	2
Trans. Pol. $^3\text{He}$ at 11 GeV, 6 degs	6	0.25
Long. Pol. $^3\text{He}$ at 11 GeV, 8.5 degs	240	10
Trans. Pol. $^3\text{He}$ at 11 GeV, 8.5 degs	36	1.5
Dilution, calibrations	24	1
Total Time Requested	336 + 24	14 + 1

**We request a total of 15 days of beam time**

# Summary

- Experiment is a straight forward  $\overrightarrow{{}^3\text{He}}(\vec{e}, e')$  measurement at  $Q^2$  from 1 to 2.6 (GeV/c) $^2$
- Already have theoretical support from G. Salme` and M. Sargsian to make  $G_E^n$  extractions from the data
- Makes use of the Hall C investments for the  $A_1^n$  and  $d_2^n$  **experiments without requiring additional equipment**
- We request 15 days of beam





**Thank You!** 04.22.2009 16:20

# PR12-12-011 Collaboration

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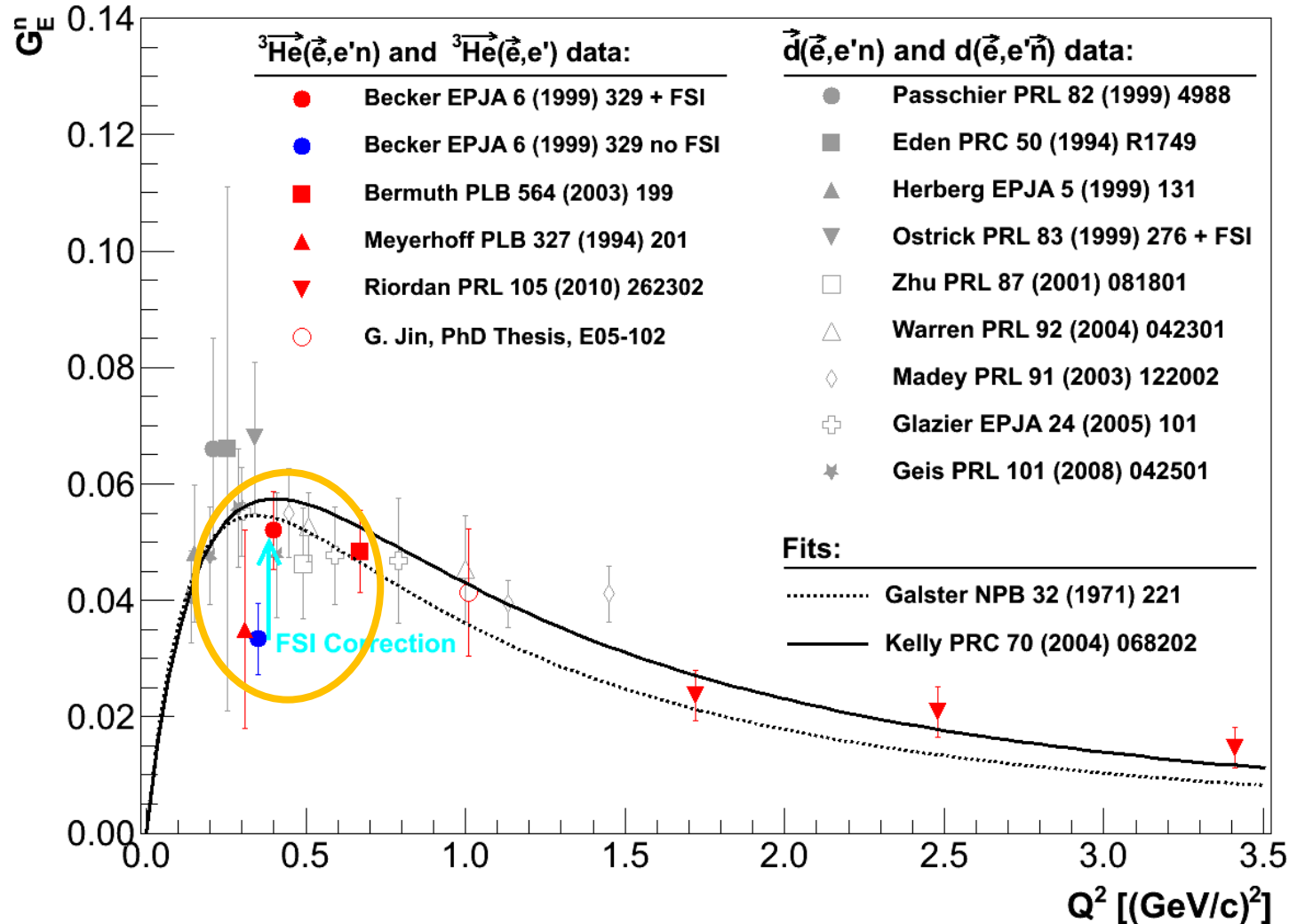
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T. Holmstrom **(Longwood University)**

K. Aniol **(University of California)**



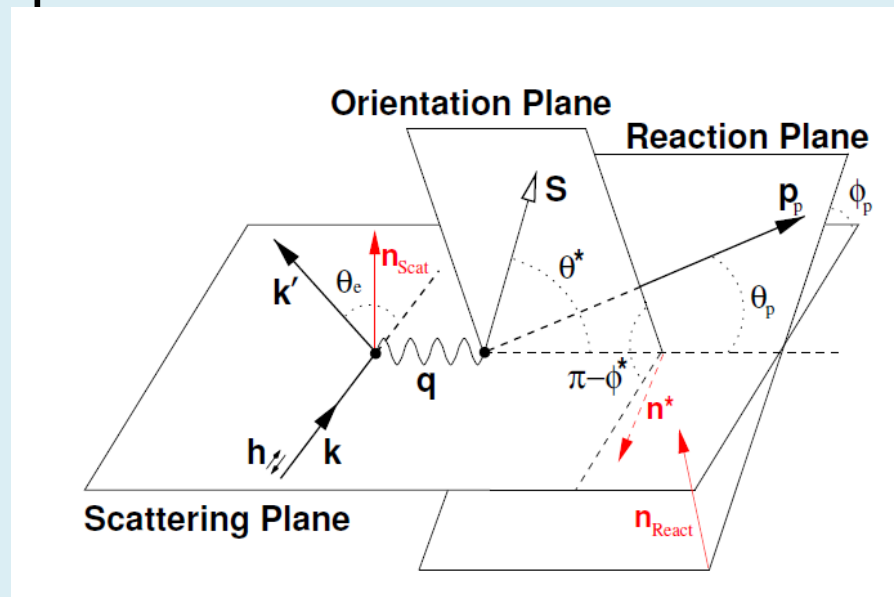
# Motivation



# Helicity Asymmetry in Electron Scattering

$$A = - \frac{\sin \theta^* \cos \phi^* v_{TL'} R^{^3He}_{TL'} + \cos \theta^* v_{T'} R^{^3He}_{T'}}{v_L R^{^3He}_L + v_T R^{^3He}_T}$$

where  $R$ 's are response functions and  $v$ 's are kinematics factors



T. D. Donnelly and A. S. Raskin, Ann. Phys 169, 247 (1986)

# Ratio of Asymmetries

when  $\theta^* = 0$ , transverse asymmetry  $A_{T'} = -\frac{v_{T'} R^{^3He}_{T'}}{v_L R^{^3He}_L + v_T R^{^3He}_T}$

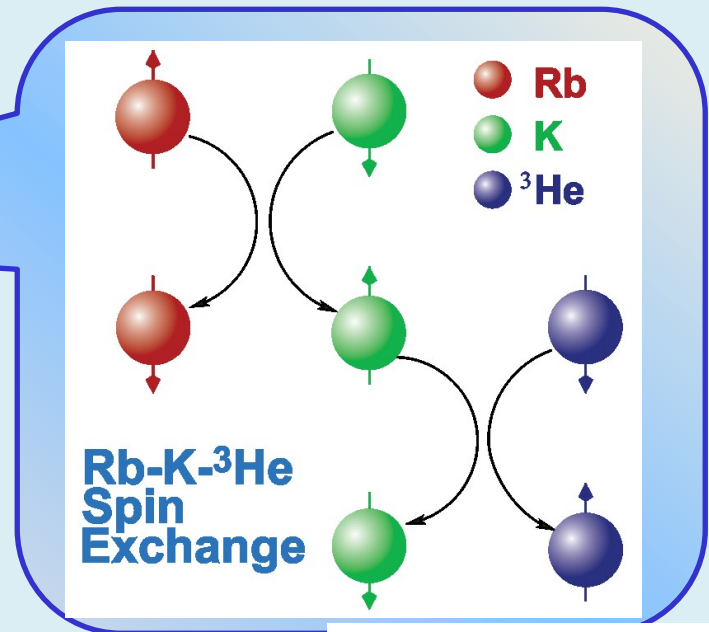
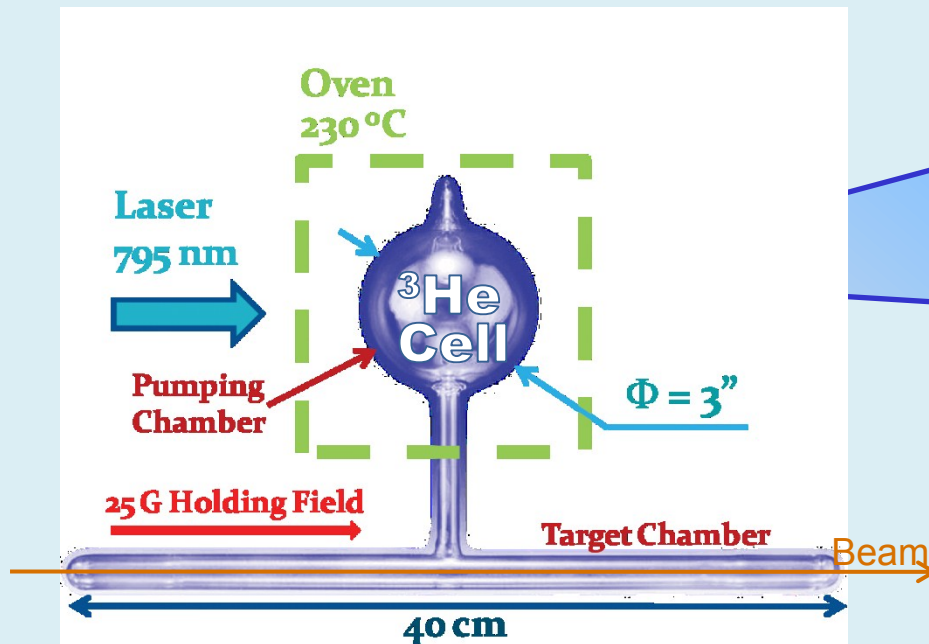
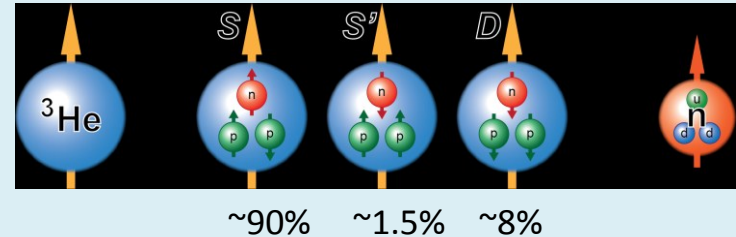
when  $\theta^* = \pi / 2$  and  $\phi^* = 0$ , transverse - longitudinal asymmetry

$$A_{TL'} = -\frac{v_{TL'} R^{^3He}_{TL'}}{v_L R^{^3He}_L + v_T R^{^3He}_T}$$

$$\Rightarrow \frac{A_{TL'}}{A_{T'}} = \frac{v_{TL'} R^{^3He}_{TL'}}{v_{T'} R^{^3He}_{T'}}$$

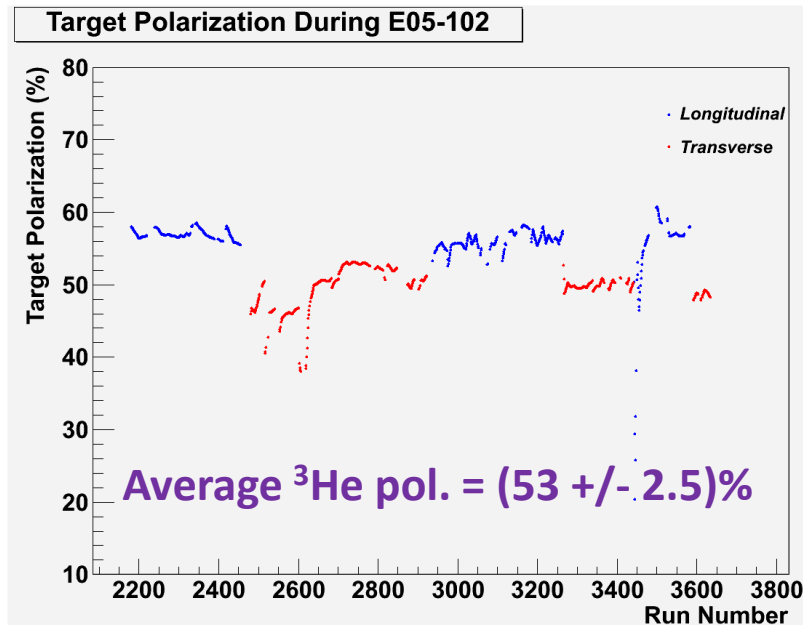
# Polarized $^3\text{He}$ Target

- Improved figure of merit
  - Rb+K hybrid mixture cell
  - Narrow bandwidth lasers
- Compact size: No cryogenic support needed

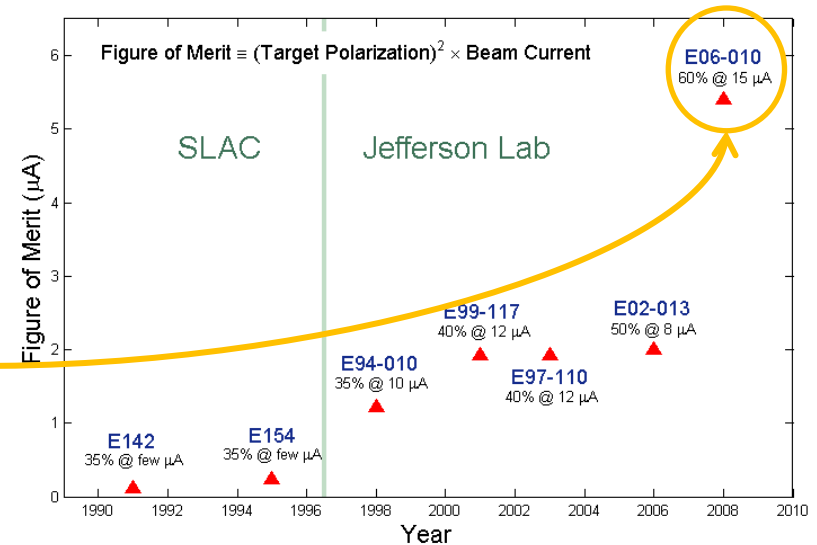


# 6-GeV Performance of $^3\text{He}$ Target

- Luminosity:  $L(n) = 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$
- Achieved record high steady  $\sim 60\%$  polarization with a beam current up to  $15 \mu\text{A}$



History of Figure of Merit of Polarized  $^3\text{He}$  Target

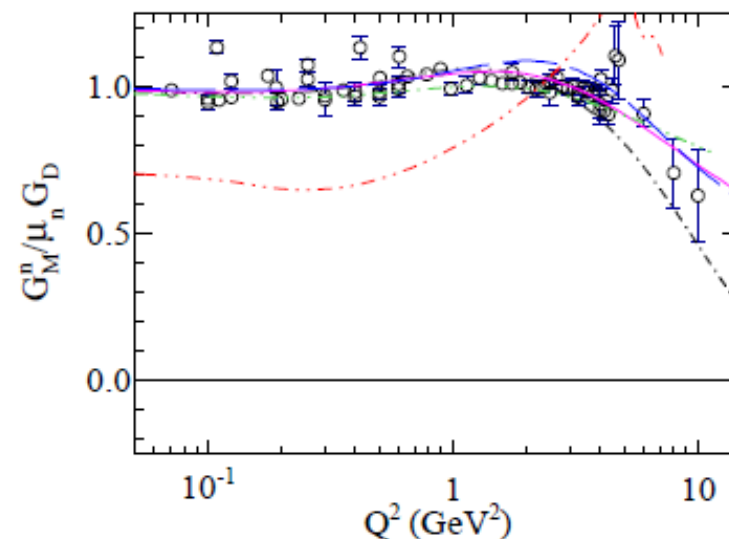
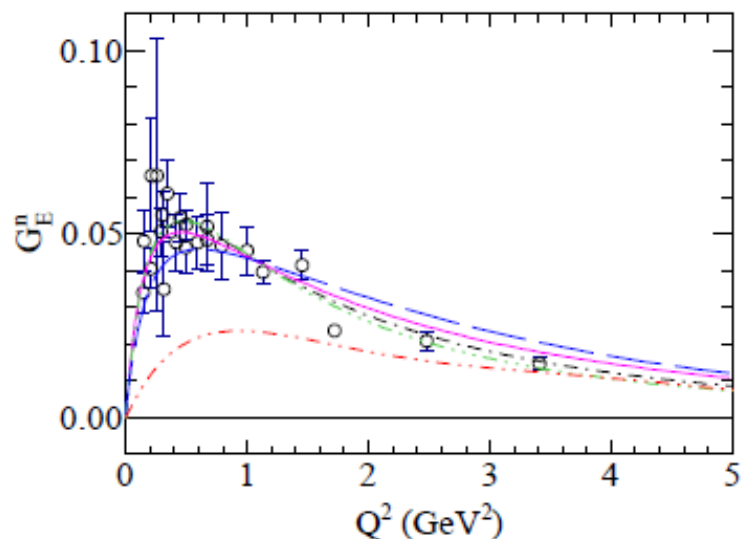
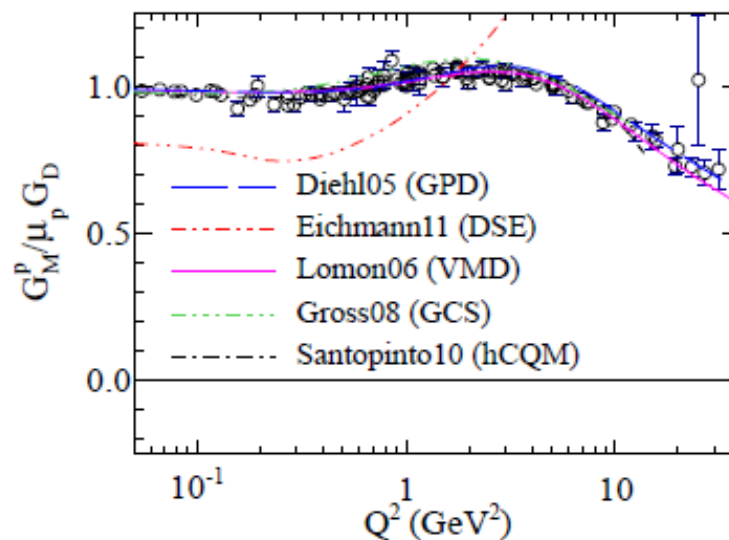
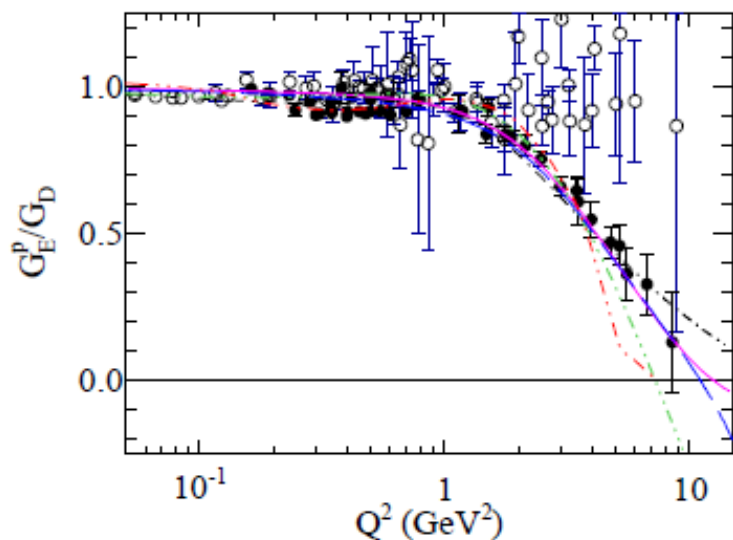


# Planned $^3\text{He}$ Target for 12-GeV Experiments

- Upgrade takes advantage improvements of hybrid spin exchange optical pumping and spectrally narrowed lasers
- This proposal takes advantage of the already planned factor of 8 improvement in polarized luminosity discussed in the and the Hall C approved  $A_1^n$  experiment
  - “Dual transfer tube” design for convection mixing of polarized gas
  - Additional diagnostics for direct measurement of  $^3\text{He}$  and alkali-vapor polarizations
- **Goal: 60% target polarization with a beam current of 60  $\mu\text{A}$  on a 60-cm long target**



# Current Status of EM Form Factors

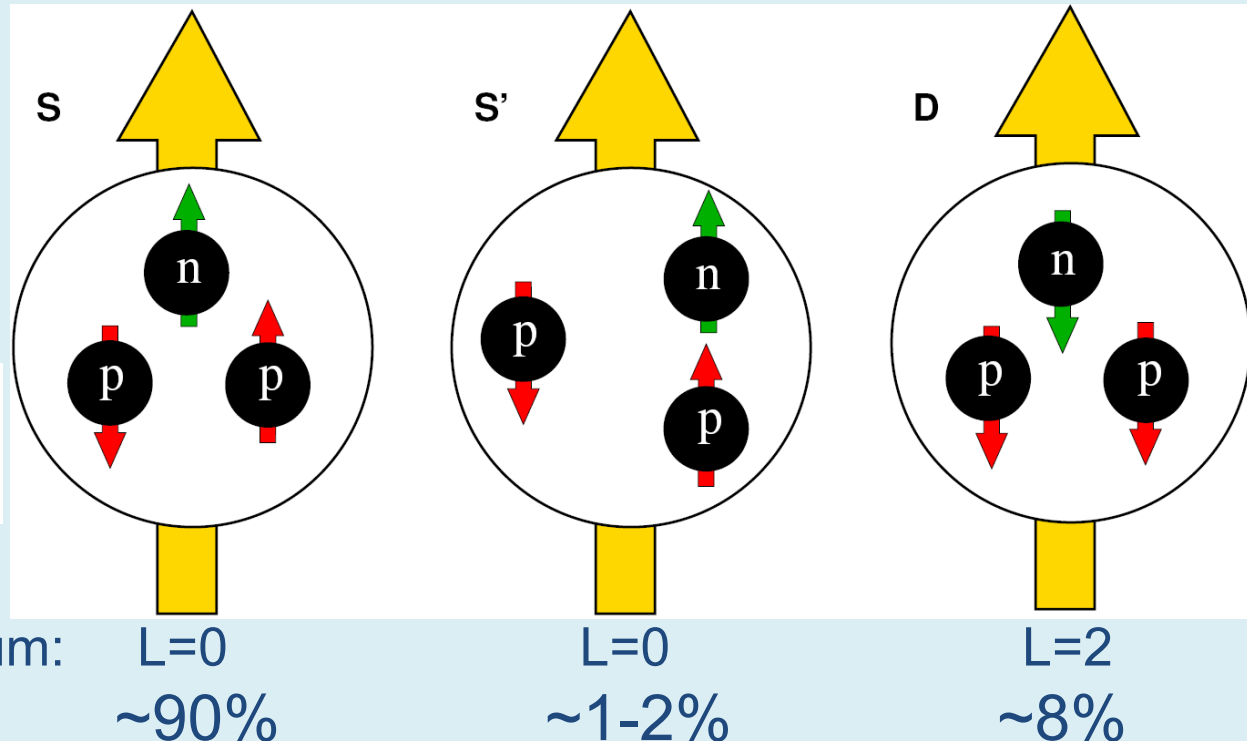


# <sup>3</sup>He spin structure

- Spin-1/2 Particle, 3 spin-1/2 Nucleons (Proton and Neutron)
- Protons are in spin-singlet state. <sup>3</sup>He spin is dominated by spin of **n**. Therefore <sup>3</sup>He can be used as an effective **n** target
- S' mixed symmetry, (spin-isospin)-space correlations

*Effective  
Polarized  
Neutron  
Target*

$$\frac{\mu_{^3\text{He}}}{\mu_n} = \frac{-2.131}{-1.913} \approx 1$$



Angular Momentum:

L=0  
~90%

L=0  
~1-2%

L=2  
~8%