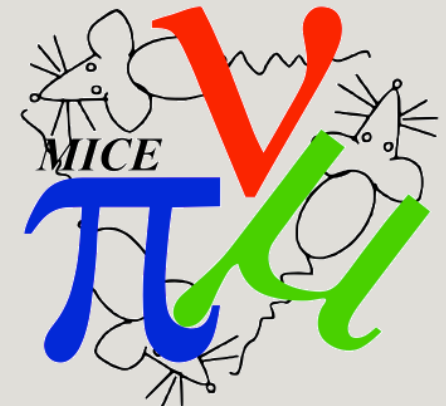


MICE STEP I: FIRST MEASUREMENT OF EMITTANCE WITH PARTICLE PHYSICS DETECTORS

V. Blackmore, University of Oxford,
on behalf of the MICE Collaboration

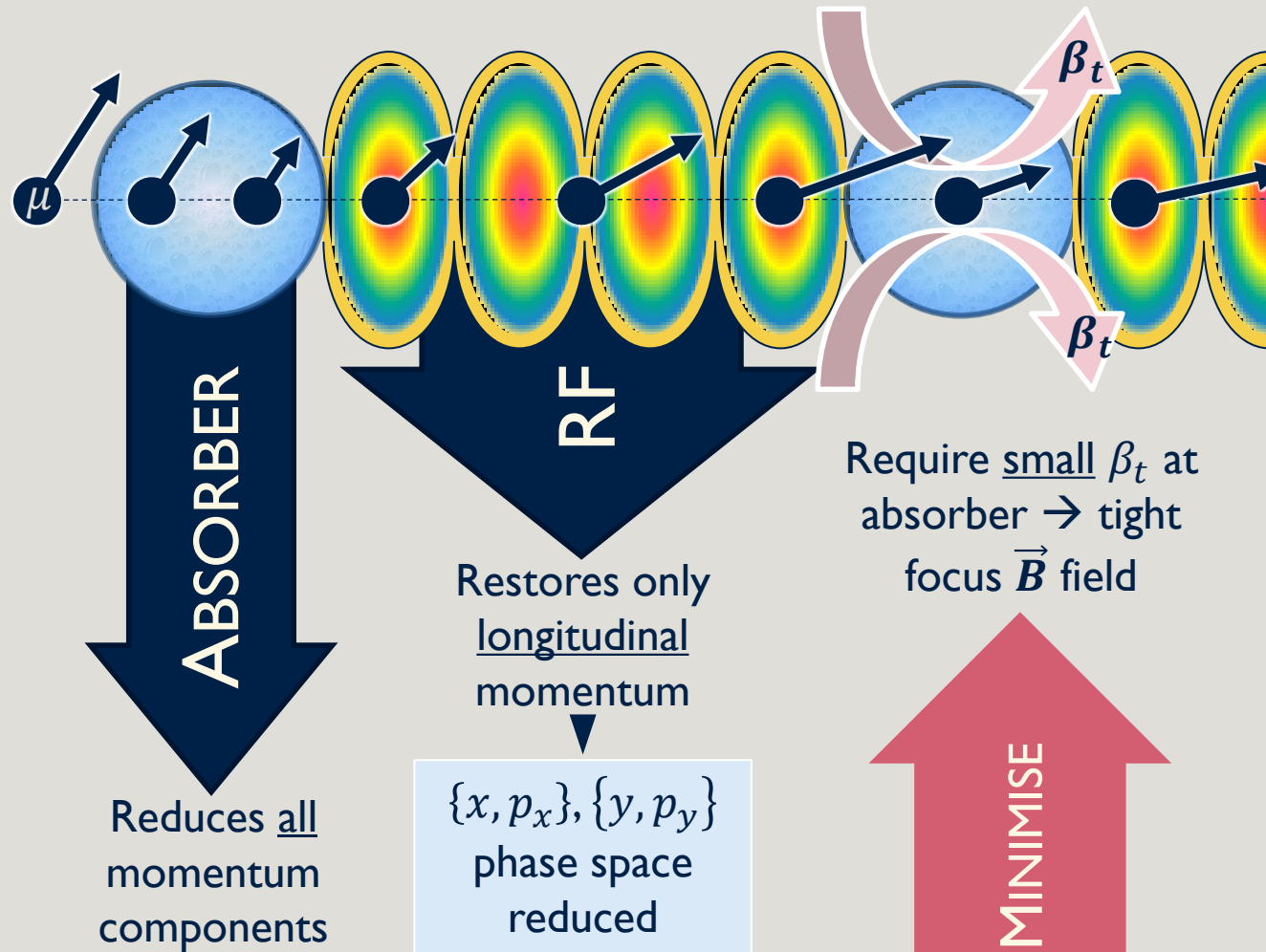


ABOUT MICE

- Ionisation cooling
- The Muon Ionisation Cooling Experiment (MICE)
- The beam line

Ionisation Cooling

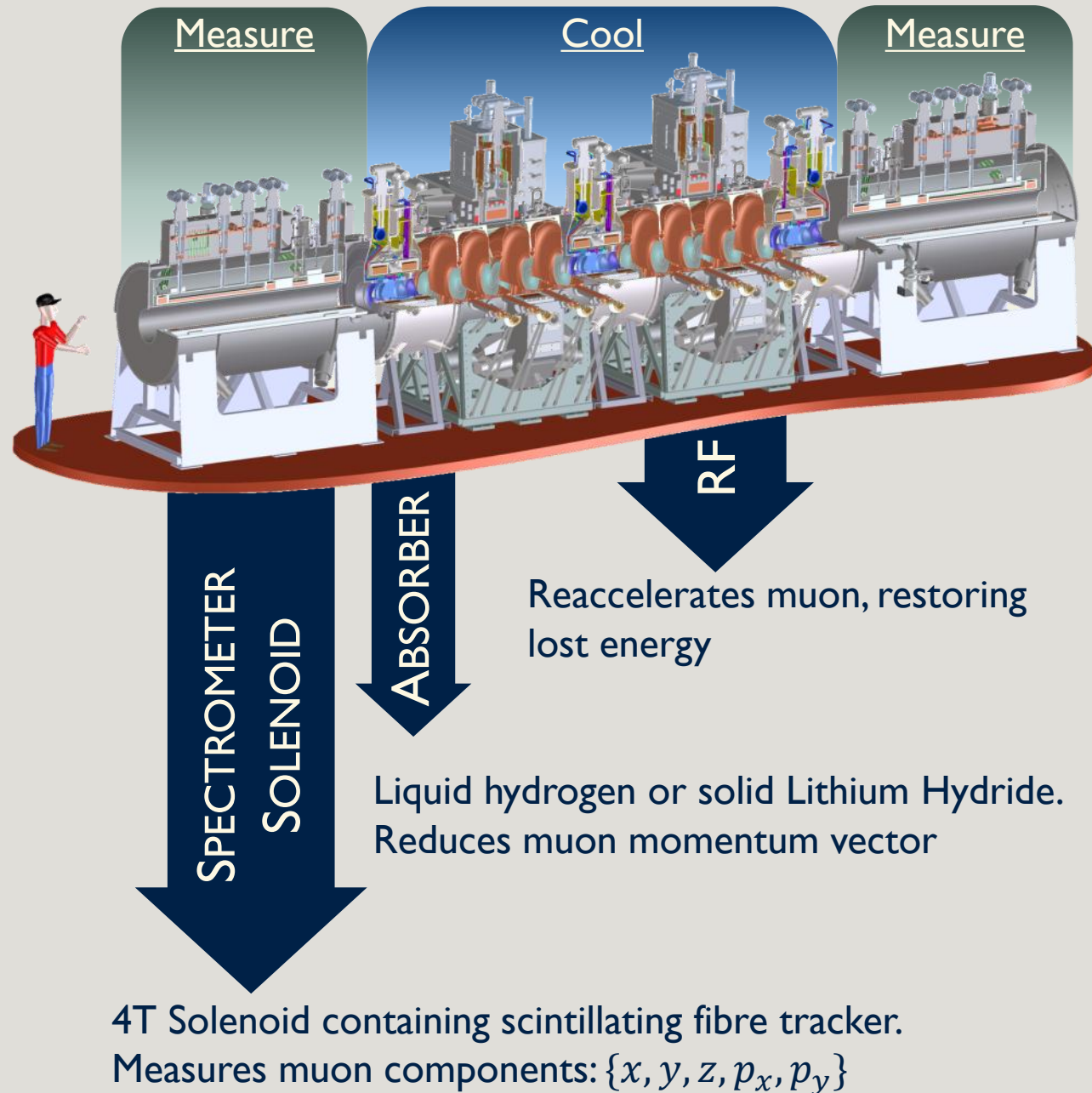
- **Cooling:** reduction of the beam volume in 2, 4, or 6 dimensional phase space.
 - Light-to-moderate 4D cooling required for Neutrino Factory.
 - **Intense** 6D cooling required for Muon Collider.
 - Begin with ionisation cooling.



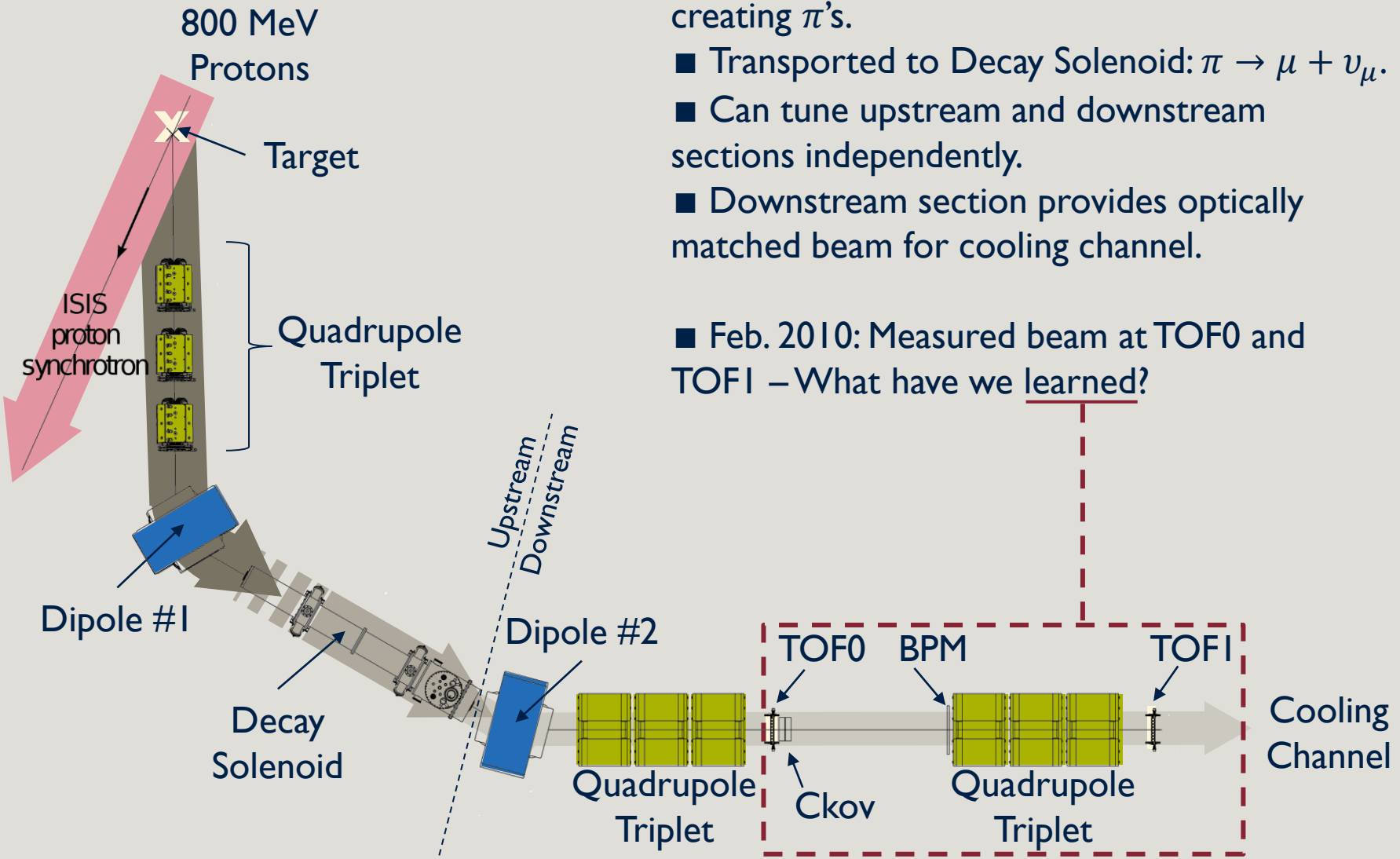
$$\frac{d\varepsilon_n}{dX} \approx \underbrace{\frac{-\varepsilon_n}{\beta^2 E} \left\langle \frac{dE}{dX} \right\rangle}_{\text{Cooling}} + \underbrace{\frac{\beta_t (0.014 \text{ GeV})^2}{2\beta^3 E m_\mu X_0}}_{\text{Heating (Mult. Scat)}}$$

The Muon Ionisation Cooling Experiment (MICE)

- In construction at Rutherford Appleton Laboratory, UK.
- Full cell of ionisation cooling lattice.
- Test performance in different operational modes.
- Require relative precision of $\frac{\Delta \varepsilon_n}{\varepsilon_n} \sim 1\%$ → use particle physics detectors.
- Muon-by-muon measurement.



The Beam Line



- Target samples 600 – 800 MeV protons, creating π 's.
- Transported to Decay Solenoid: $\pi \rightarrow \mu + \nu_\mu$.
- Can tune upstream and downstream sections independently.
- Downstream section provides optically matched beam for cooling channel.
- Feb. 2010: Measured beam at TOF0 and TOF1 – What have we learned?

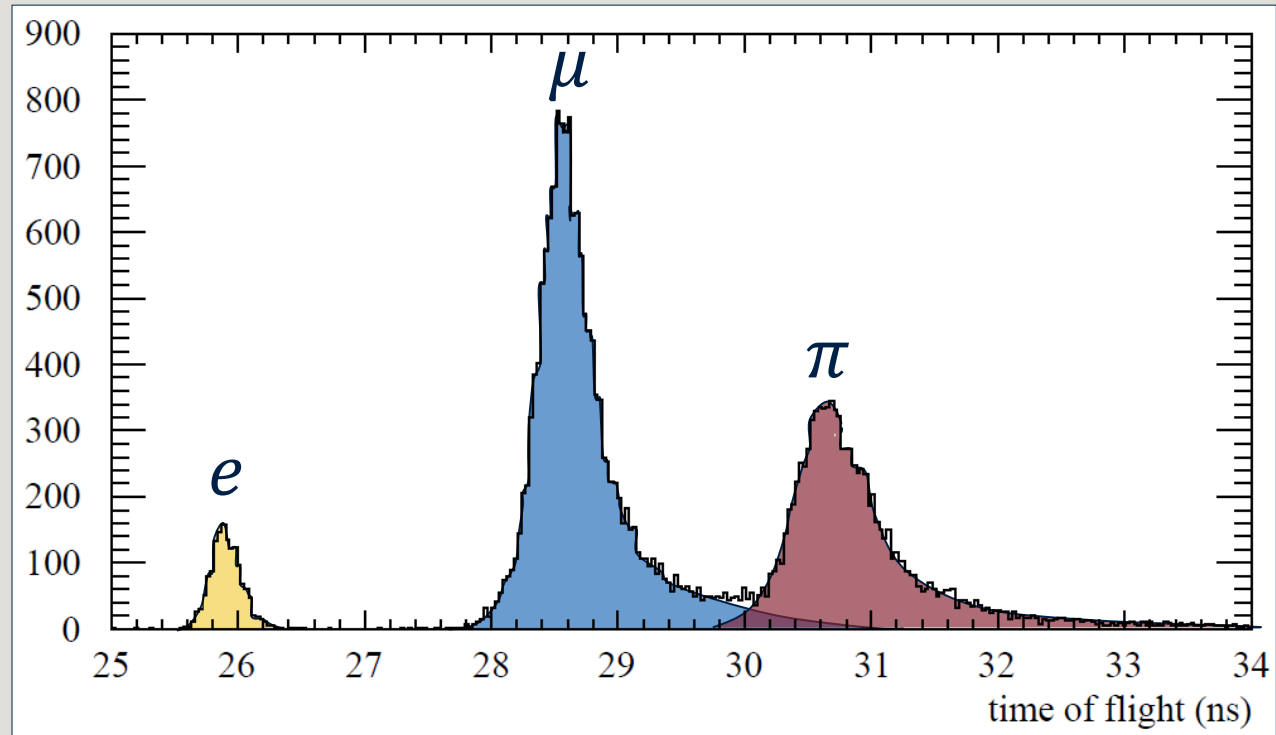
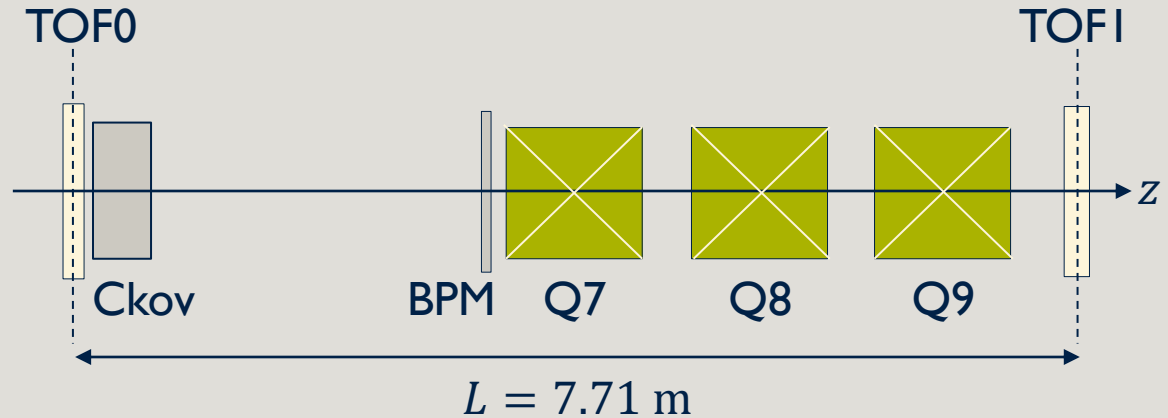
EMITTANCE & MOMENTUM RECONSTRUCTION

- The Time Of Flight (TOF) system
- Measuring position components
- Reconstruction of muon paths
- Accuracy of the reconstruction technique

The Time Of Flight (TOF) System

- Two detectors, each with two orthogonal planes of scintillator slabs.
- Measure particle crossing time to 50 ps
- Dipole selects mean momentum of beam.
- Time-of-flight depends on particle mass – PID possible.

$$t = \left(\frac{L}{c}\right) \sqrt{1 + \frac{(mc)^2}{p^2}}$$



Measuring Position Components

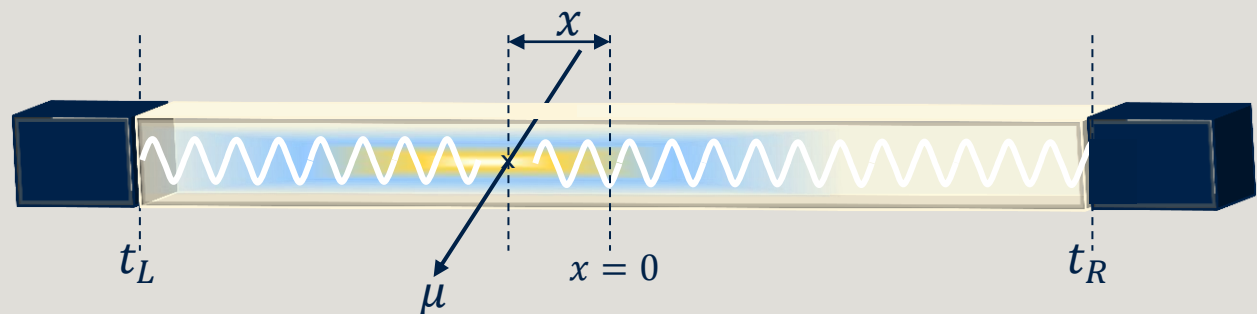
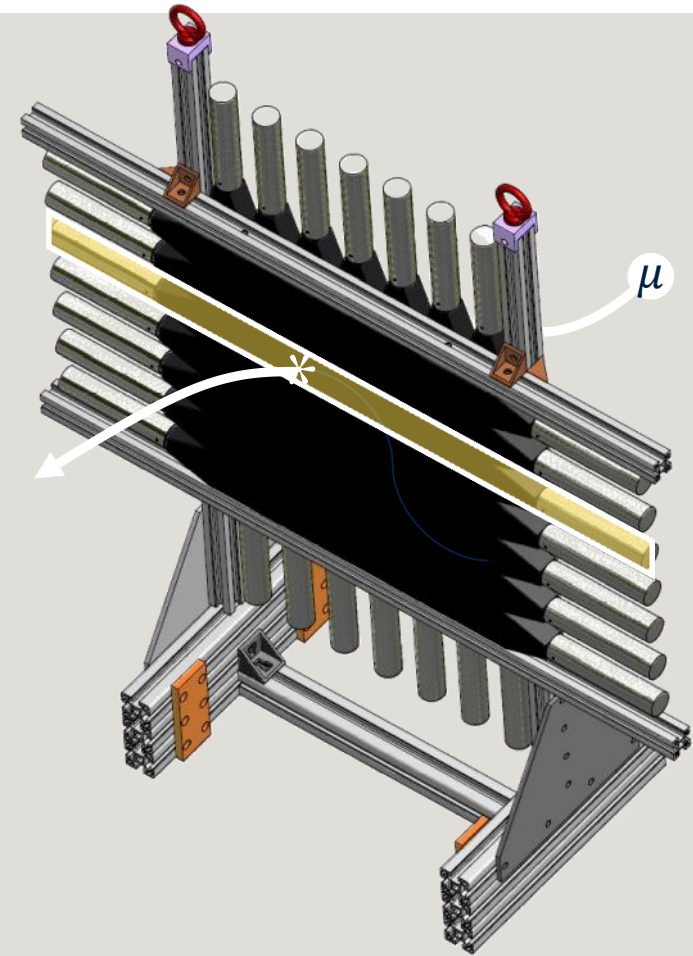
■ Two independent methods of measuring position:

- 1) Measure pixel position,
- 2) Measure position according to signal arrival time at PMTs.

$$x = \frac{c_{\text{eff}}(t_L - t_R + \Delta)}{2}$$

- Position resolution,
TOF0: 9.8 mm
TOF1: 11.4 mm

- For each particle crossing the TOF stations, we know $\{x, y, t\}$
- To learn more about the beam line we must also know $\{x', y', p_z\}$, where $x' = \frac{p_x}{p_z}$ etc.
- Reconstruct particle trajectories.

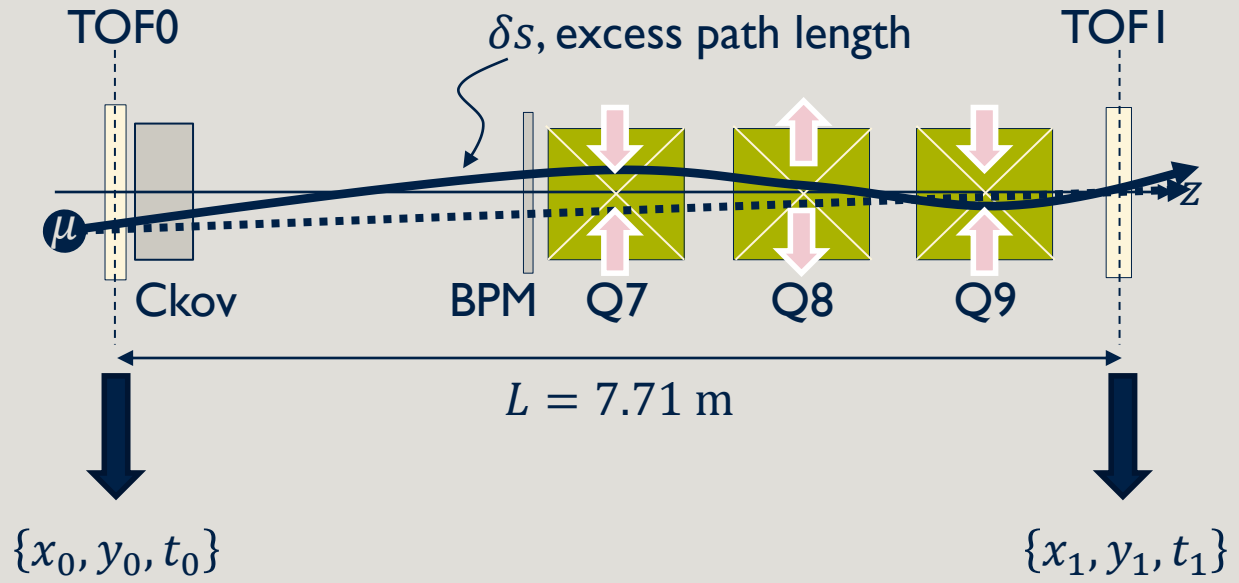


Reconstructing Muon Paths

■ Begin with position measurements of muon at TOF0 and TOF1.

■ \underline{M}_x and \underline{M}_y vary quickly at low p_z .

■ Correct for energy lost between TOF0 and TOF1



REPEAT

1) Calculate p_z from time of flight.

2) Assume linear beam transport*:

* \underline{M} depends on p_z

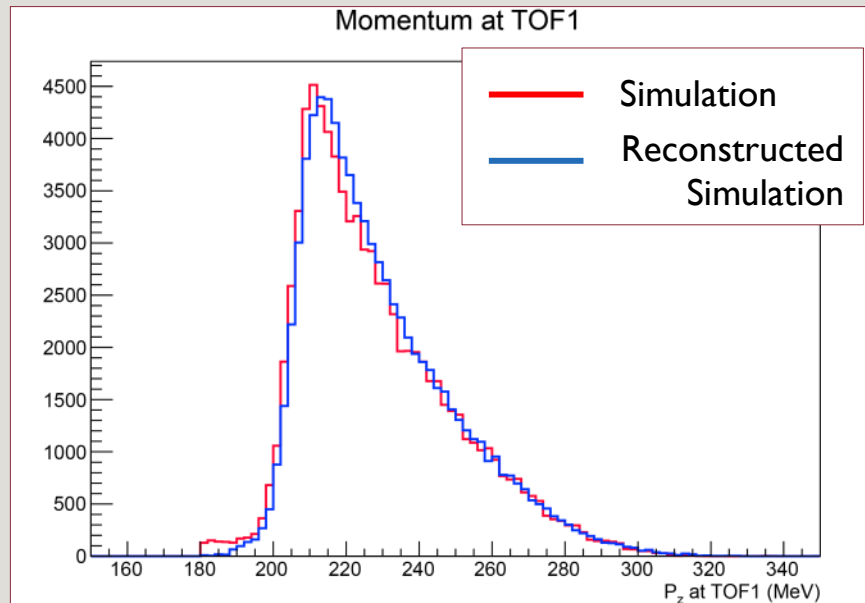
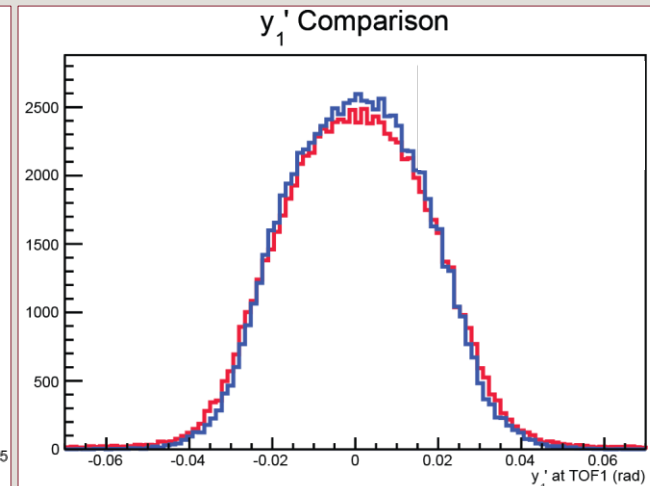
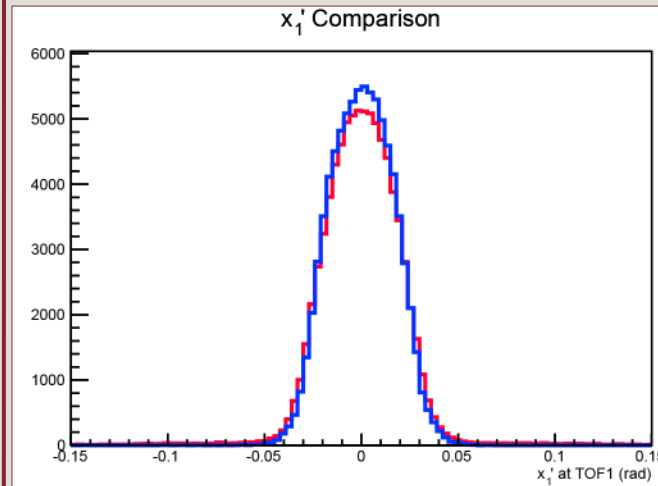
$$\begin{pmatrix} x_1 \\ x_1' \end{pmatrix} = \begin{pmatrix} M_{11} & M_{12} \\ M_{12} & M_{22} \end{pmatrix} \begin{pmatrix} x_0 \\ x_0' \end{pmatrix} \Rightarrow \begin{pmatrix} x_0' \\ x_1' \end{pmatrix} = \frac{1}{M_{12}} \begin{pmatrix} -M_{11} & 1 \\ -1 & M_{22} \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \end{pmatrix}$$

3) Track through quadrupoles to calculate δs ,

$$\underline{M}_x = \underline{O}_{Q9 \rightarrow TOF1} \underline{F}_{Q9} \underline{O}_{Q8 \rightarrow Q9} \underline{D}_{Q8} \underline{O}_{Q7 \rightarrow Q8} \underline{F}_{Q7} \underline{O}_{TOF0 \rightarrow Q7}$$

Accuracy of Reconstruction Technique

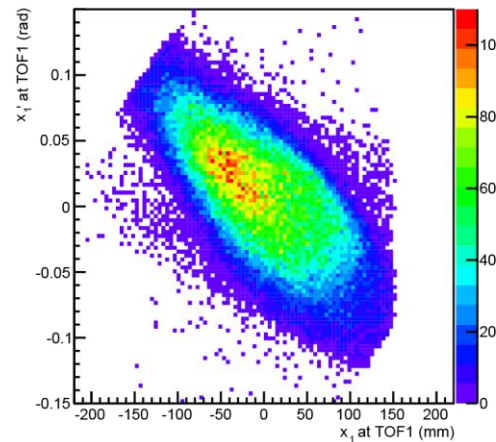
- (x, y, t) from Monte Carlo (G4beamline, G4MICE) simulation are smeared by the TOF resolution.
- Trace-space components and momentum reconstructed.



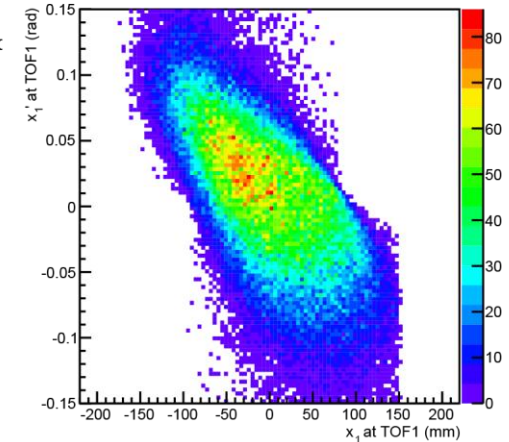
Accuracy of Reconstruction Technique

- (x, y, t) from Monte Carlo (G4beamline, G4MICE) simulation are smeared by the TOF resolution.
- Trace-space components and momentum reconstructed.
- Good qualitative agreement:
 - Core reproduced well.
 - Good reproduction of high amplitude particles.

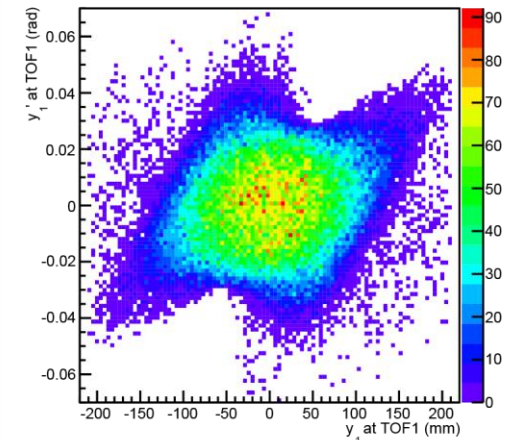
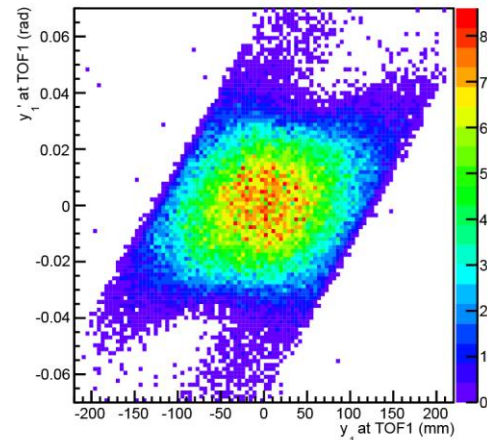
Horizontal trace space



Reconstructed Simulation



Vertical trace space



STEP I DATA

- Step I data sets
- Expectations versus reality

Step I Data Sets

■ MICE investigates cooling potential of lattice cell for different beam settings.

■ Categorise beam settings by their values at the **centre of an absorber**.

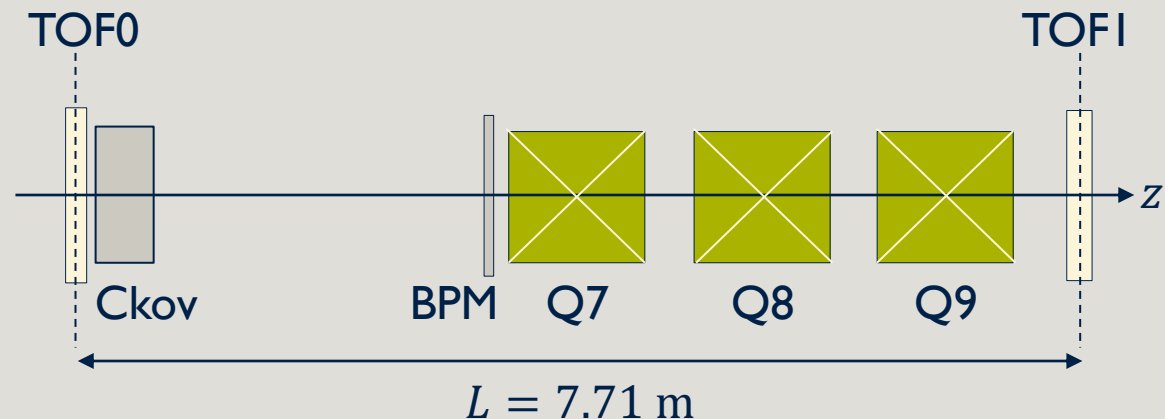
■ Nominal test beams given in an “emittance-momentum” matrix.

■ 9 beam settings \times 2 muon polarities = 18 beams [17 measured].

	$p_z = 140\text{MeV}$	$p_z = 200\text{MeV}$	$p_z = 240\text{MeV}$
$\varepsilon_N = 3 \text{ mm}$	$D = 0 \text{ mm}$	$D = 0 \text{ mm}$	$D = 0 \text{ mm}$
$\varepsilon_N = 6 \text{ mm}$	$D = 5.0 \text{ mm}$	$D = 7.5 \text{ mm}$	$D = 7.5 \text{ mm}$
$\varepsilon_N = 10 \text{ mm}$	$D = 10 \text{ mm}$	$D = 15.5 \text{ mm}$	$D = 15.5 \text{ mm}$

Thickness of Pb required to achieve this emittance and momentum upstream of cooling channel (“diffuser”)

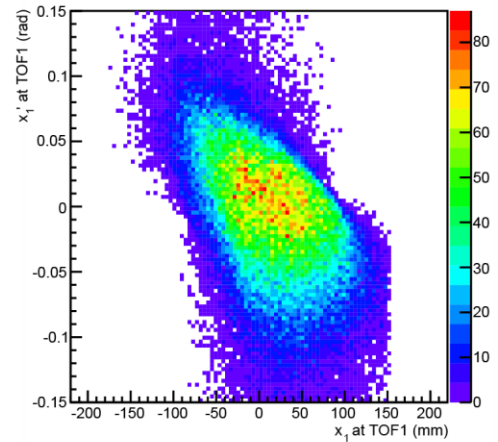
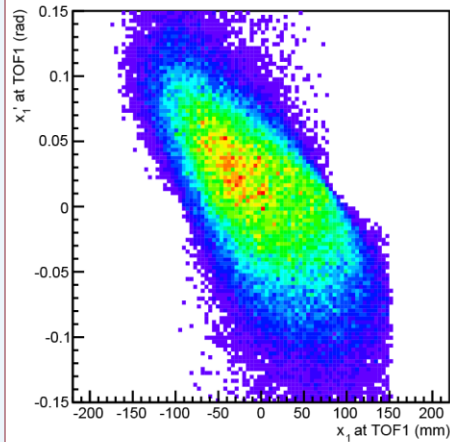
Complication: Our beam line measurements exist upstream of the diffuser: higher momentum and lower emittance.



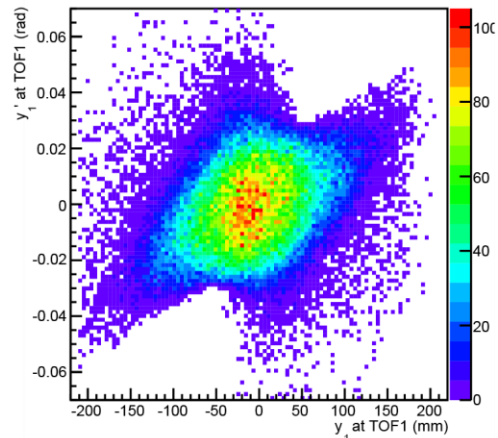
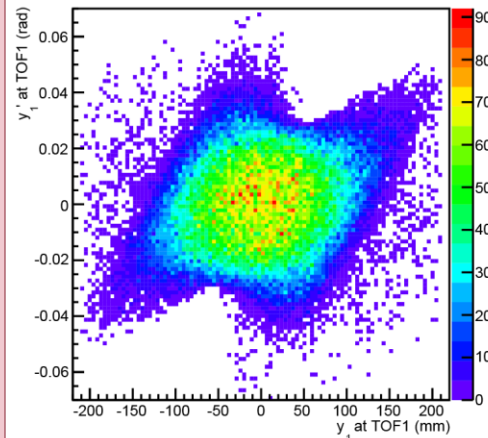
Expectation versus Reality

- Compare data to reconstructed simulation.
- Overall good qualitative agreement.

Horizontal trace space

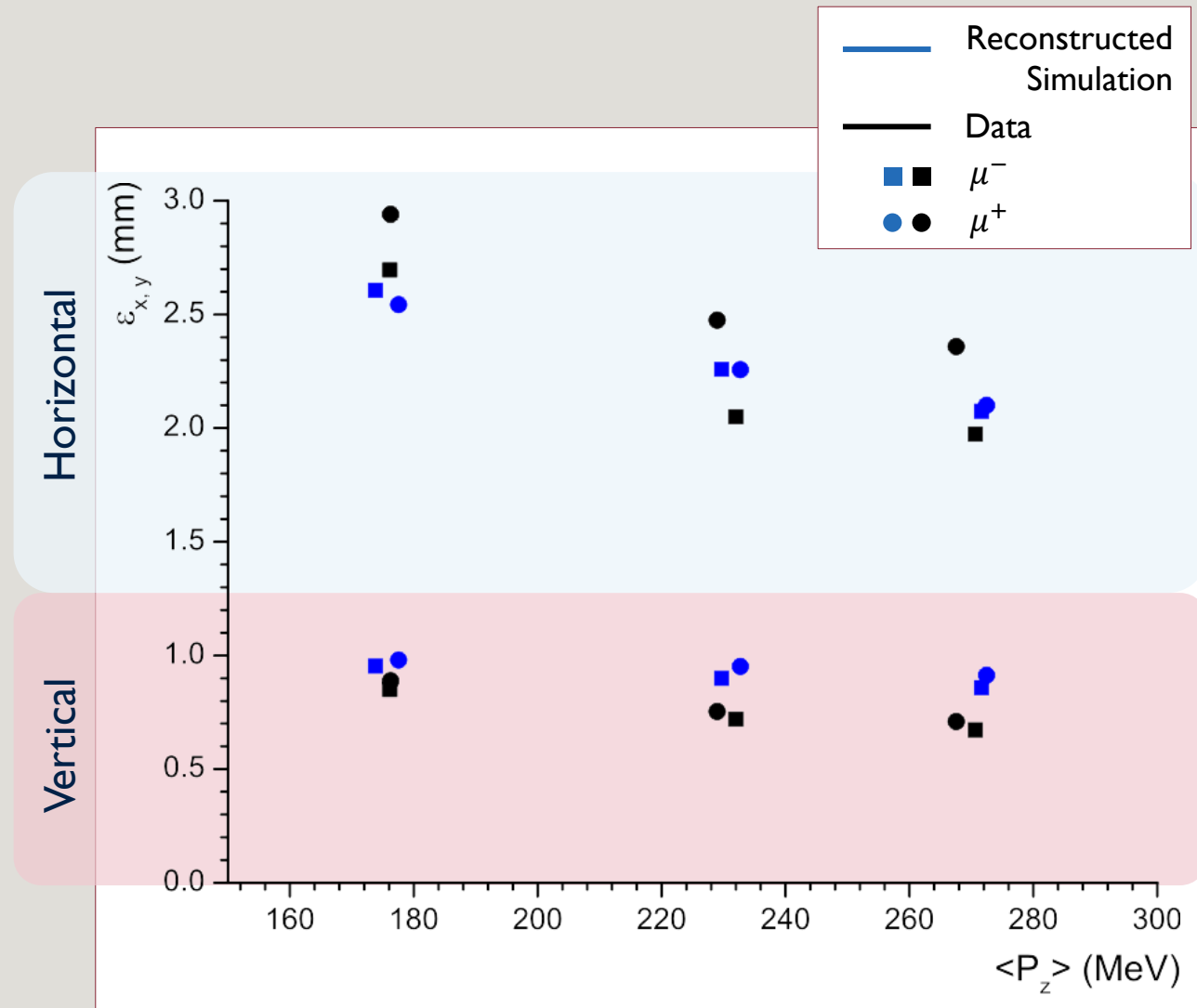


Vertical trace space



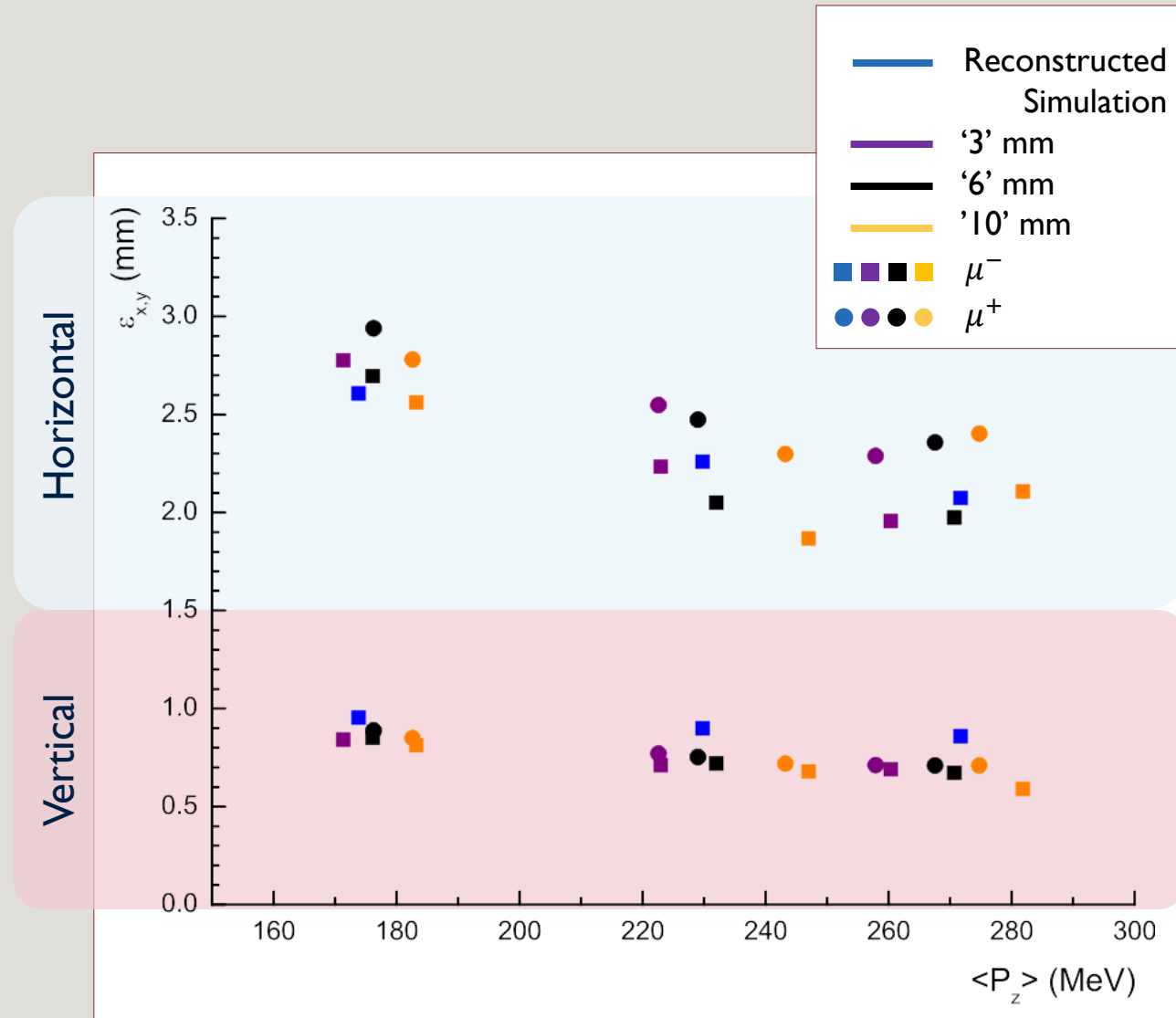
Expectation versus Reality

- Compare data to reconstructed simulation.
- Overall good qualitative agreement.
- Larger difference in horizontal plane



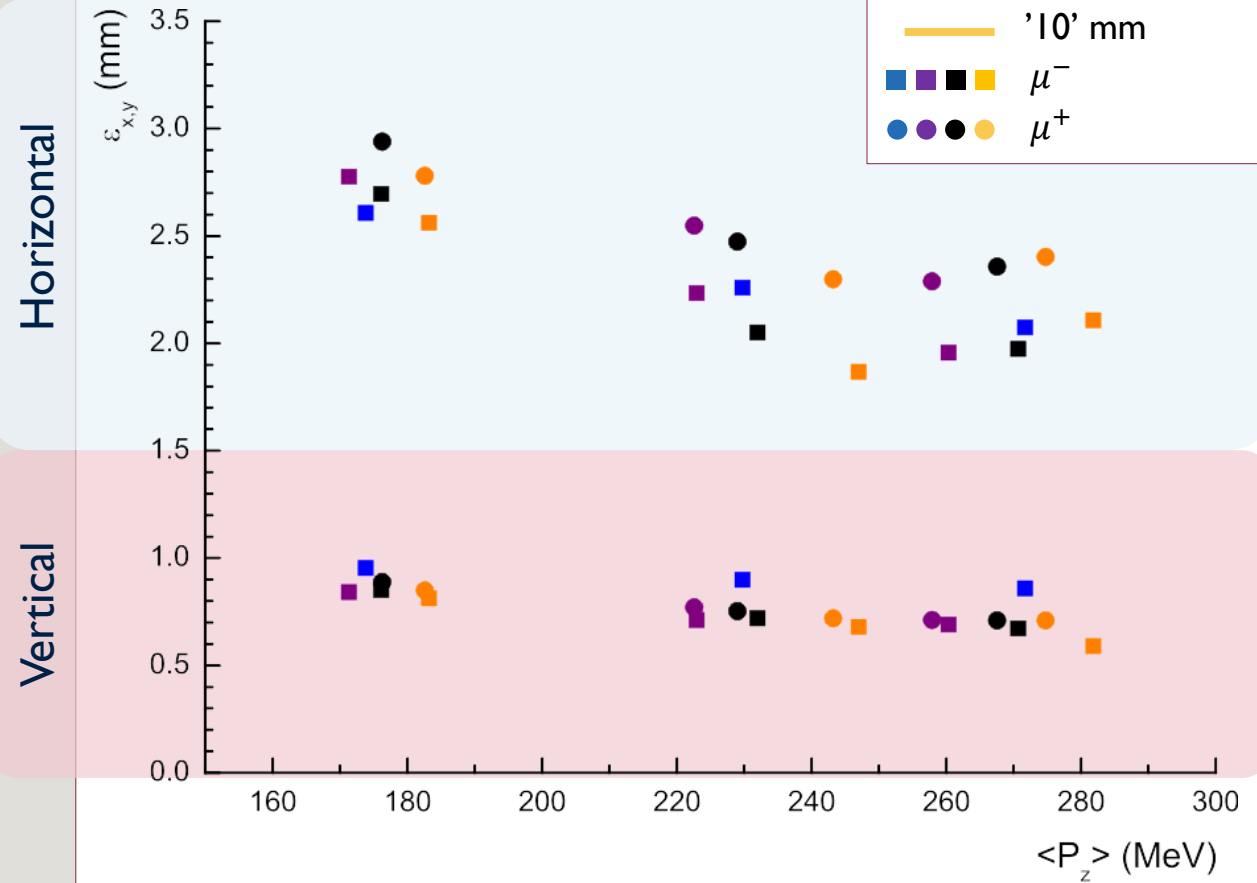
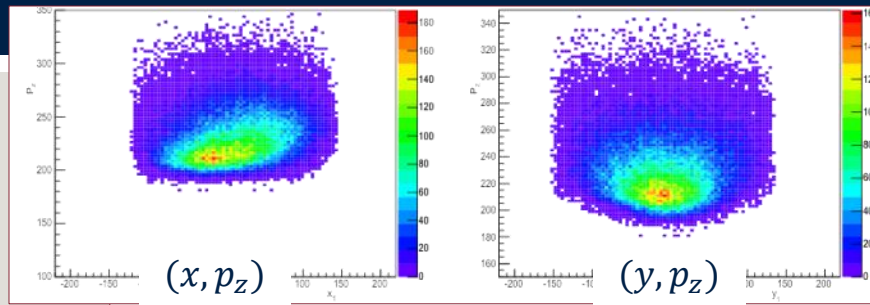
The Full Data Set

- Measured, and reconstructed emittances of 17 of the beam line settings.
- Note: The nominal '3', '6' and '10' mm emittance is after the diffuser.
- Good agreement with simulation.



Summary

- Constant vertical emittance of 0.8 mm.
- Horizontal emittance varies depending on dispersion from D2, ~ 2.5 mm.
- Resolution of reconstruction method has not been removed.
- Beam is asymmetric in x and y .
- Limited by quadrupole apertures.



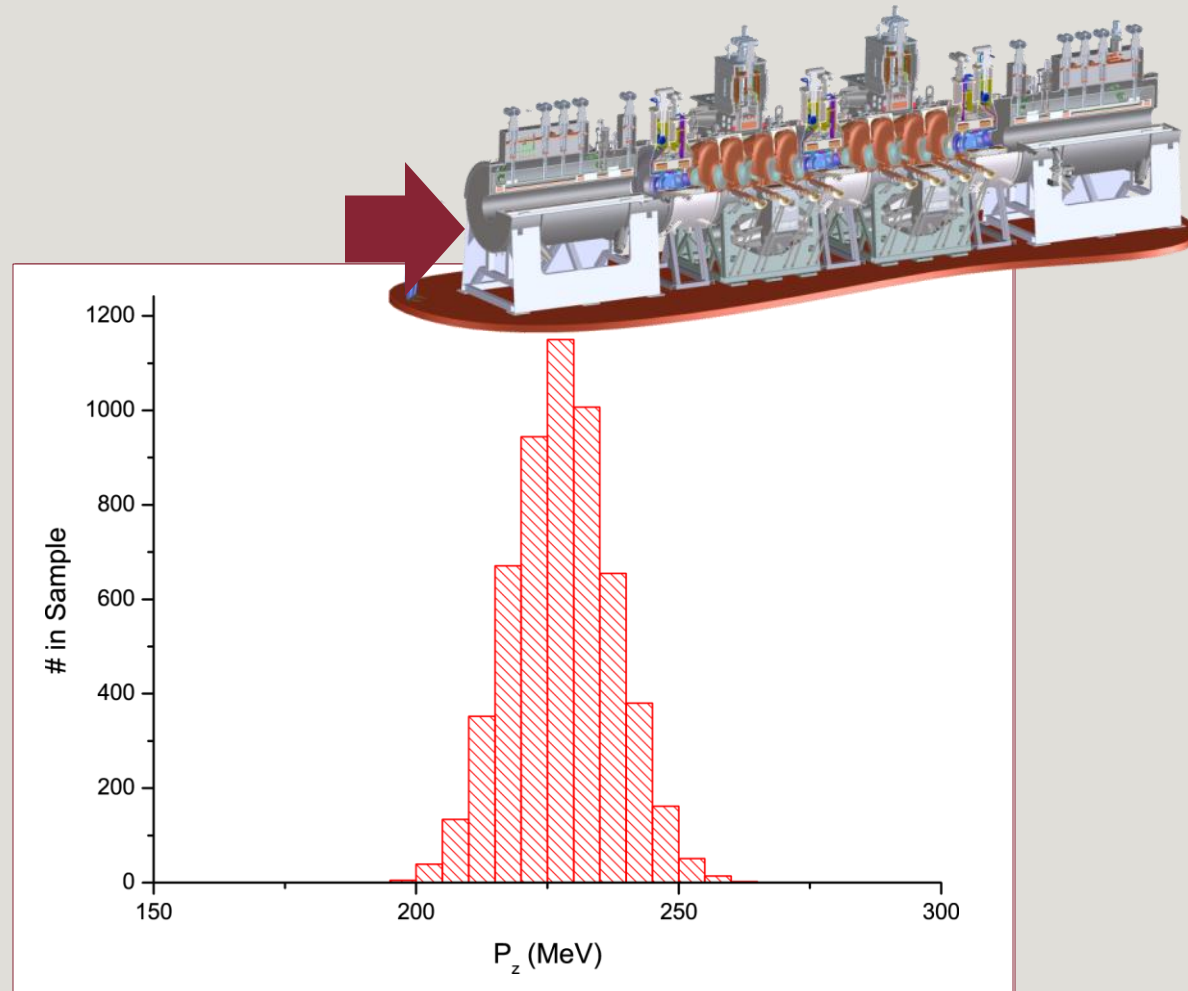
What would happen if we put our measured muons through a simulation of the full cooling channel?

EVOLUTION THROUGH STEP VI

- Expected performance of the cooling channel
- Conclusions

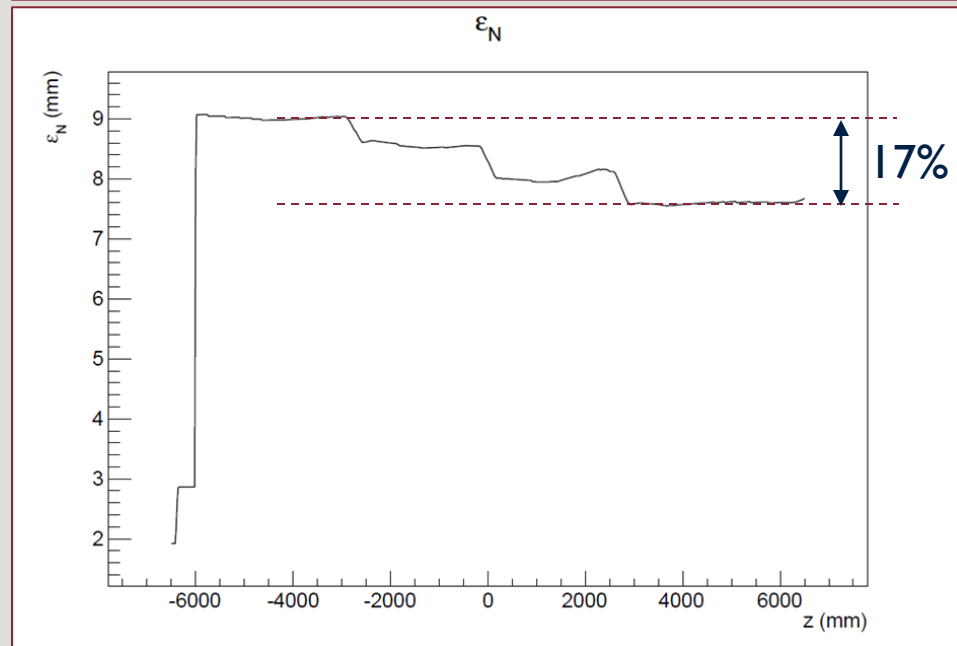
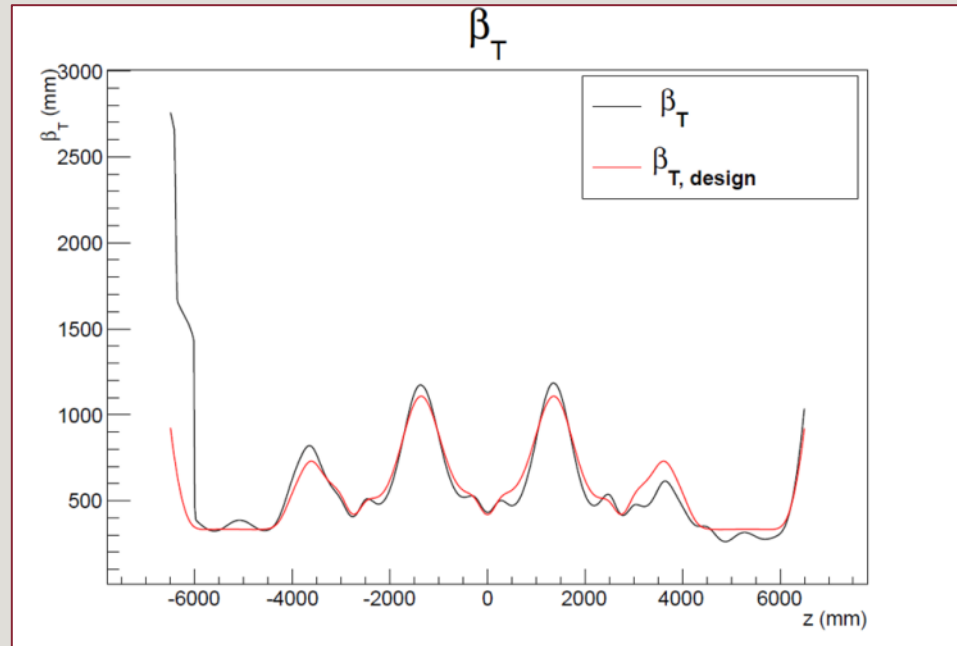
Expected Performance of the Cooling Channel

- Propagate measured beams forward through full cooling channel simulation
- Select a 'NF-like' Gaussian p_z distribution of muons to send down the channel.



Expected Performance of the Cooling Channel

- Propagate measured beams forward through full simulated cooling channel.
- Select a 'NF-like' Gaussian p_z distribution of muons to send down the channel.
- Track matching through channel.
- Track emittance reduction across the channel.



Conclusions

- First single-particle emittance measurements of the MICE beam line.
- Good agreement with simulations.
- Propagating a sub-selection of real measured muons through cooling channel demonstrates excellent beam matching and cooling performance.
- MICE Step VI promises to be very exciting!