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Lepton Flavor Violation vs. θ_{13}

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Why LFV?

- Neutrinos oscillate \rightarrow Lepton family numbers are not conserved!
- Can we observe LFV in charged leptons decays?



Suppression due to small neutrino masses Cheng Li '77, '80; Petcov '77

In presence of NP at the TeV we can expect large effects!



Flavour violation induced by misalignment between leptons and sleptons

LFV vs θ_{13}



LFV vs θ_{13}

Why LFV?

- Unambigous signal of New Physics
- Stringent test of NP models
- It probes scales far beyond the LHC reach:

Process	Relevant operators	Pres. Bound on Λ $(c = 1)$	Fut. Bound on Λ $(c = 1)$
$\mu \to e \gamma$	$\frac{c}{\Lambda^2} \frac{m_\mu}{16\pi^2} \overline{\mu}_L \sigma^{\mu\nu} e_R F_{\mu\nu}$	48 TeV	107 TeV
$\mu \rightarrow eee$	$\frac{c}{16\pi^2\Lambda^2} (\overline{\mu}_L \gamma^\mu e_L) (\overline{e}_L \gamma^\mu e_L)$	17 TeV	166 TeV
	$\frac{c}{16\pi^2\Lambda^2}(\overline{\mu}_L e_R)(\overline{e}_R e_L)$	$10 { m TeV}$	$98 { m TeV}$
$\mu \rightarrow e$ in Ti	$\frac{c}{16\pi^2\Lambda^2} (\overline{\mu}_L \gamma^\mu e_L) (\overline{d}_L \gamma^\mu d_L)$	33 TeV	577 TeV
	$\frac{c}{16\pi^2\Lambda^2}(\overline{\mu}_L e_R)(\overline{d}_R d_L)$	$59 { m TeV}$	$1000 { m TeV}$

LC Lalak Pokorski Ziegler '12

LFV vs θ_{13}

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LC Lalak Pokorski Ziegler '12 $BR(\mu \to eee) < 10^{-16} CR(\mu \to e \text{ in Ti}) < 5 \times 10^{-17}$				

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	$\frac{c}{\Lambda^2}(\overline{\mu}_L e_R)(\overline{e}_R e_L)$	124 TeV	1230 TeV	
$\mu \rightarrow e \text{ in Ti}$	$\frac{c}{\Lambda^2} (\overline{\mu}_L \gamma^\mu e_L) (\overline{d}_L \gamma^\mu d_L)$	419 TeV	7254 TeV	
	$\frac{c}{\Lambda^2}(\overline{\mu}_L e_R)(\overline{d}_R d_L)$	745 TeV	$12600 { m TeV}$	
LC Lalak Pokorski Ziegler '12		$BR(\mu \to eee) < 10^{-16}$	$\operatorname{CR}(\mu \to e \text{ in Ti}) < 5 \times 10^{-17}$	

LFV vs θ_{13}

(SUSY) Seesaw Mechanism



(SUSY) Seesaw Mechanism



Mismatch between low and high-energy params.

Casas Ibarra '01

LFV vs θ_{13}

(SUSY) Seesaw Mechanism



Direct link to the light neutrino mass matrix! In principle all parameters known

LFV vs θ_{13}

In SUSY, new fields interacting with the MSSM fields enter the radiative corrections of the sfermion masses Hall Kostelecky Raby '86

This applies to the new seesaw interactions: Borzumati Masiero '86 generically induce LFV in the slepton mass matrix!

Type I
$$(\tilde{m}_L^2)_{ij} \propto m_0^2 \sum_k (\mathbf{Y}_N^*)_{ki} (\mathbf{Y}_N)_{kj} \ln \left(\frac{M_X}{M_{R_K}}\right)$$
Borzumati Masiero '86Type II $(\tilde{m}_L^2)_{ij} \propto m_0^2 (\mathbf{Y}_\Delta^{\dagger} \mathbf{Y}_\Delta)_{ij} \ln \left(\frac{M_X}{M_\Delta}\right) \propto m_0^2 (\mathbf{m}_\nu^{\dagger} \mathbf{m}_\nu)_{ij} \ln \left(\frac{M_X}{M_\Delta}\right)$ A. Rossi '02; Rossi Joaquim '06Type IIISimilar to type IBiggio LC '10; Esteves et al. '10

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$$\begin{array}{c} \hline \text{Type I} & (\tilde{m}_{L}^{2})_{ij} \propto m_{0}^{2} \sum_{k} (\mathbf{Y}_{N}^{*})_{ki} (\mathbf{Y}_{N})_{kj} \ln \left(\frac{M_{X}}{M_{R_{K}}}\right) & \text{Borzumati Masiero '86} \\ \hline \text{Type II} & (\tilde{m}_{L}^{2})_{ij} \propto m_{0}^{2} (\mathbf{Y}_{\Delta}^{\dagger} \mathbf{Y}_{\Delta})_{ij} \ln \left(\frac{M_{X}}{M_{\Delta}}\right) \propto m_{0}^{2} (\mathbf{m}_{\nu}^{\dagger} \mathbf{m}_{\nu})_{ij} \ln \left(\frac{M_{X}}{M_{\Delta}}\right) \\ \hline & & \mathbf{M}_{\nu}^{2} U^{\dagger} & \text{A. Rossi '02; Rossi Joaquim '06} \\ \hline & & & \\ m_{\ell}^{2} = \begin{pmatrix} (\tilde{m}_{L}^{2})_{ij} + (m_{\ell}^{2})_{ij} - m_{Z}^{2} (\frac{1}{2} - \sin^{2} \theta_{W}) \delta_{ij} & A_{ji}^{\ell*} v_{d} - (m_{\ell})_{ji} \mu \tan \beta \\ & A_{ij}^{\ell} v_{d} - (m_{\ell})_{ij} \mu^{*} \tan \beta & (\tilde{m}_{E}^{2})_{ij} + (m_{\ell}^{2})_{ij} - m_{Z}^{2} \sin^{2} \theta_{W} \delta_{ij} \end{pmatrix} \end{array}$$

LFV vs θ_{13}

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LFV vs θ_{13}

Type II : direct connection between seesaw couplings and the PMNS. Hierarchical neutrinos normal ordering (IO similar):

 $BR(\mu \to e\gamma) \propto \left| \Delta m_{31}^2 \, s_{\theta_{13}} c_{\theta_{13}} s_{\theta_{23}} + \Delta m_{21}^2 \, s_{\theta_{12}} c_{\theta_{13}} (c_{\theta_{12}} c_{\theta_{23}} - s_{\theta_{12}} s_{\theta_{13}} s_{\theta_{23}}) \right|^2$

$$\operatorname{BR}(\tau \to \mu \gamma) \propto \left| \Delta m_{31}^2 c_{\theta_{13}}^2 c_{\theta_{23}} s_{\theta_{23}} + \mathcal{O}(\Delta m_{12}^2) \right|^2$$



LFV vs θ_{13}

However, theoretically motivated examples where the correlation is there:

• Trivial mixing from RHv (i.e. *R*~1) :

 θ_{13} (°) Antusch et al. '06

However, theoretically motivated examples where the correlation is there:

• SO(10) GUT ('PMNS mixing' case):

Chang Masiero Murayama '02; Masiero Vives Vempati '02



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LC Faccia Masiero Vempati '06

LFV vs θ_{13}

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LC Chowdhury Masiero Patel Vempati, to appear

$$m_0 \in [0, 5] \; ext{TeV}$$

 $\Delta m_H \in \begin{cases} 0 & ext{for mSUGRA} \bullet \\ [0, 5] & ext{for NUHM1} \bullet \\ m_{1/2} \in [0.1, 2] \; ext{TeV} \\ A_0 \in [-3m_0, +3m_0] \\ ext{sgn}(\mu) \in \{-, +\} \end{cases}$

 $BR(\mu \to e\gamma) \propto \left| y_t^2 U_{\mu 3} U_{e3}^* \right|^2$

$$|U_{e3}| = 0.11$$

 $124.5 \text{ GeV} \lesssim m_h \lesssim 126.5 \text{ GeV}$

LFV vs θ_{13}

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Such scenarios (hierarchical RHv and $\theta_{13} << 1$) could 'naturally' suppress $\mu \rightarrow e$ transitions relative to $\tau \rightarrow \mu$

This cannot be realized with $\theta_{13} \sim O(0.1)$

Random variation of matrix R and neutrino parameters:

$$\frac{\mathrm{BR}(\tau \to \mu \gamma)}{\mathrm{BR}(\mu \to e \gamma)} \lesssim \mathcal{O}(1000) \implies \mathrm{BR}(\tau \to \mu \gamma) \lesssim \mathcal{O}(10^{-9})$$

DayaBay/Reno measurements imply that SUSY seesaw(s) can be preferably tested through $\mu \rightarrow e$ transitions

LFV vs θ_{13}

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Possible exception: 1st and 2nd generation sleptons much heavier than 3rd generation

LFV vs θ_{13}

Correlations in the μ -*e* sector

In SUSY (with R_P) $\mu \rightarrow eee$ and $\mu \rightarrow e$ conversion dominated by the dipole $\mu \rightarrow e\gamma^*$ Strong correlations:



$$BR(\mu \to eee) \sim \alpha_{em} \times BR(\mu \to e\gamma)$$

$$\operatorname{CR}(\mu \to \text{ in N}) \sim \alpha_{\text{em}} \times \operatorname{BR}(\mu \to e\gamma)$$

• Sensitivities < 10⁻¹⁵ would go beyond MEG

• Crucial model discriminators



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LFV vs θ_{13}

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not only seesaw models!

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$$\operatorname{CR}(\mu \to \text{ in N}) \sim \alpha_{\text{em}} \times \operatorname{BR}(\mu \to e\gamma)$$

• Sensitivities < 10^{-15} would go beyond MEG

• Crucial model discriminators

In fact, there are models where $\mu \rightarrow eee$ and/or $\mu \rightarrow e$ conv. arise at tree-level.



- SUSY with R-parity violation
- Low-energy type III seesaw
- Low-energy flavor models with Higgs-like messengers LC Lalak Pokorski Ziegler '12

Rates enhanced wrt. $\mu \rightarrow e_Y$!

e.g. Dreiner Kramer O'Leary '06

Abada et al '07

TeV scale seesaw fields with large Yukawa couplings are possible (cancellations, flavor symmetry, inverse seesaw...)

Potentially large LFV coupling to gauge bosons are induced (e.g. lepton-W-RHv)

Type I
NH :
$$BR(\mu \to e\gamma) \cong$$

 $\frac{3\alpha_{em}}{32\pi} \left(\frac{y^2 v^2}{M_1^2} \frac{m_3}{m_2 + m_3}\right)^2 \left| U_{\mu 3} + i\sqrt{\frac{m_2}{m_3}} U_{\mu 2} \right|^2 \left| U_{e3} + i\sqrt{\frac{m_2}{m_3}} U_{e2} \right|^2 [G(X) - G(0)]^2$
IH : $BR(\mu \to e\gamma) \cong$
 $\frac{3\alpha_{em}}{32\pi} \left(\frac{y^2 v^2}{M_1^2} \frac{1}{2}\right)^2 |U_{\mu 2} + iU_{\mu 1}|^2 |U_{e2} + iU_{e1}|^2 [G(X) - G(0)]^2$. Dinh Ibarra Molinaro Petcov '12

• Possibly suppressed rates



de Dinnie Dennet Correle Henstern

Dinh et al. '12

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LFV vs θ_{13}

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$$NH: BR(\mu \to e\gamma) \cong Abada Biggio Bonnet Gavela Hambye 07$$

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$$IH: BR(\mu \to e\gamma) \cong \frac{3\alpha_{em}}{32\pi} \left(\frac{y^2 v^2}{M_1^2} \frac{1}{2}\right)^2 |U_{\mu 2} + iU_{\mu 1}|^2 |U_{e2} + iU_{e1}|^2 [G(X) - G(0)]^2.$$
Dinh Ibarra Molinaro Petcov '12

- Possibly suppressed rates
- $\mu \rightarrow e$ conversion strongest constraint (loop function enhancement)
- Correlations: parameters can be determined through diff. channels

Dinh et al. '12



• SU(3)	LC Jones-Perez Vives '07; LC Jones-Perez Masiero Park Vives '09; LC Hodgkinson Jones-Perez Masiero Vives '09
• $U(2)_l x U(2)_e$	Blankenburg Isidori Jones-Perez '12
• A ₄	Feruglio Hagedorn Lin Merlo '08, '09; Altarelli Feruglio Merlo Stamou '09
 Model independent discussion 	LC Lalak Pokorski Ziegler '12

Structure of slepton mass matrices determined by the flavor symmetry Same dynamics explain fermion masses and mixing and controls LFV

LFV in SUSY flavor models

LC Jones-Perez Vives '07; LC Jones-Perez Masiero Park Vives '09; LC Hodgkinson Jones-Perez Masiero Vives '09

Blankenburg Isidori Jones-Perez '12

Feruglio Hagedorn Lin Merlo '08, '09; Altarelli Feruglio Merlo Stamou '09

• Model independent discussion

LC Lalak Pokorski Ziegler '12

SU(3) with light SUSY spectrum:



• SU(3)

• A₄

• $U(2)_l x U(2)_e$

LFV vs θ_{13}

LFV in SUSY flavor models

• SU(3)



- A₄
- Model independent discussion

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LC Lalak Pokorski Ziegler '12

 $U(2)_l x U(2)_e$ with heavy first generations sleptons

Stau masses < 1 TeV



Blankenburg Isidori Jones-Perez '12

Lorenzo Calibbi (MPP)

LFV vs θ_{13}

LFV in SUSY flavor models

• SU(3)

• $U(2)_l x U(2)_e$

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LFV vs θ_{13}

- LFV processes among the stringest constraints/tests of new physics
- In (SUSY) seesaw, $\theta_{13} \sim O(0.1)$ favours $\mu \rightarrow e$ transitions
- MEG already constrain some SUSY seesaw/GUT models far beyond LHC
- Searches for $\mu \rightarrow e\gamma$, $\tau \rightarrow \mu\gamma$, $\mu \rightarrow eee$ and $\mu \rightarrow e$ conv. (in different nuclei) would give complementar information crucial for model discrimination

Thanks for your attention!