

# Precision at future long baseline oscillation facilities

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Work in collaboration with

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arXiv: 1203.5651 [hep-ph]

NuFact12, July 24<sup>th</sup> 2012

W&M, Williamsburg, VA

# Outline

- Present status of the  $U_{\text{PMNS}}$  matrix and  $\theta_{13}$
- Why precision?
- General landscape: discovery vs precision
- Simulation details
- Analytical approach and phenomenology
- Results:
  - for  $\theta_{13}$
  - for delta
- Summary and conclusions

# Present status on $\theta_{13}$

- Global analyses, 2008: 0808.2016 [hep-ph]  
0806.2649 [hep-ph]  
$$\sin^2 2\theta_{13} = 0.06 \pm 0.04$$
- T2K, 2011: 1106.2822 [hep-ex]  
$$\sin^2 2\theta_{13} = 0.11_{-0.08}^{+0.17} (90\%)$$
  
$$\sin^2 2\theta_{13} = 0.104_{-0.045}^{+0.060}$$
  
Nakaya's talk at  
Neutrino 2012
- MINOS, 2011: 1108.0015 [hep-ex]  
$$\sin^2 2\theta_{13} = 0.041_{-0.031}^{+0.047} (90\%)$$
- Global analyses, 2011: 1106.6028 [hep-ex]  
1108.1376 [hep-ph]  
$$\sin^2 2\theta_{13} = 0.098 \pm 0.027$$

# Present status on $\theta_{13}$

- D-Chooz, 2011:

$$\sin^2 2\theta_{13} = 0.109 \pm 0.030 \pm 0.025$$

Ishitsuka's talk at Neutrino 2012

- Daya Bay, 2012:

$$\sin^2 2\theta_{13} = 0.089 \pm 0.010 \pm 0.005$$

Dwyer's talk at Neutrino 2012

- RENO, 2012:

$$\sin^2 2\theta_{13} = 0.113 \pm 0.013 \pm 0.019$$

1204.0626 [hep-ex]

# The leptonic mixing matrix

Pontecorvo, 1957

Maki, Nakagawa, Sakata, 1962

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{Atmospheric}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\text{Interference}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{Solar}}$$

$$\Delta m_{31}^2 = 2.47 \times 10^{-3} \text{eV}^2$$

$$\sin^2 \theta_{23} = 0.386 \quad (\text{for NH})$$

$$\sin^2 \theta_{13} = 0.0241 \quad (\text{for NH})$$

$$\Delta m_{21}^2 = 7.54 \times 10^{-5} \text{eV}^2$$

$$\sin^2 \theta_{12} = 0.307$$

Fogli et al., 1205.5254 [hep-ph]  
(see also Forero et al, 1205.4018 [hep-ph])

# Why precision?

$$V_{CKM} \sim \begin{pmatrix} \color{red}\blacksquare & \color{yellow}\blacksquare & \color{white}\blacksquare \\ \color{yellow}\blacksquare & \color{red}\blacksquare & \color{yellow}\blacksquare \\ \color{white}\blacksquare & \color{yellow}\blacksquare & \color{red}\blacksquare \end{pmatrix}$$

$$U_{PMNS} \sim \begin{pmatrix} \color{red}\blacksquare & \color{yellow}\blacksquare & \color{white}\blacksquare \\ \color{yellow}\blacksquare & \color{yellow}\blacksquare & \color{red}\blacksquare \\ \color{yellow}\blacksquare & \color{yellow}\blacksquare & \color{red}\blacksquare \end{pmatrix}$$



*flavour symmetries?*

Parameter	Value (neutrino PMNS matrix)	Value (quark CKM matrix)
$\theta_{12}$	$34 \pm 1^\circ$	$13.04 \pm 0.05^\circ$
$\theta_{23}$	$43 \pm 4^\circ$	$2.38 \pm 0.06^\circ$
$\theta_{13}$	$9 \pm 1^\circ$	$0.201 \pm 0.011^\circ$
$\Delta m_{21}^2$	$+(7.58 \pm 0.22) \times 10^{-5} \text{ eV}^2$	
$ \Delta m_{32}^2 $	$(2.35 \pm 0.12) \times 10^{-3} \text{ eV}^2$	$m_3 \gg m_2$
$\delta_{CP}$	unknown	$67 \pm 5^\circ$

Table from Bishai's talk at PXPS

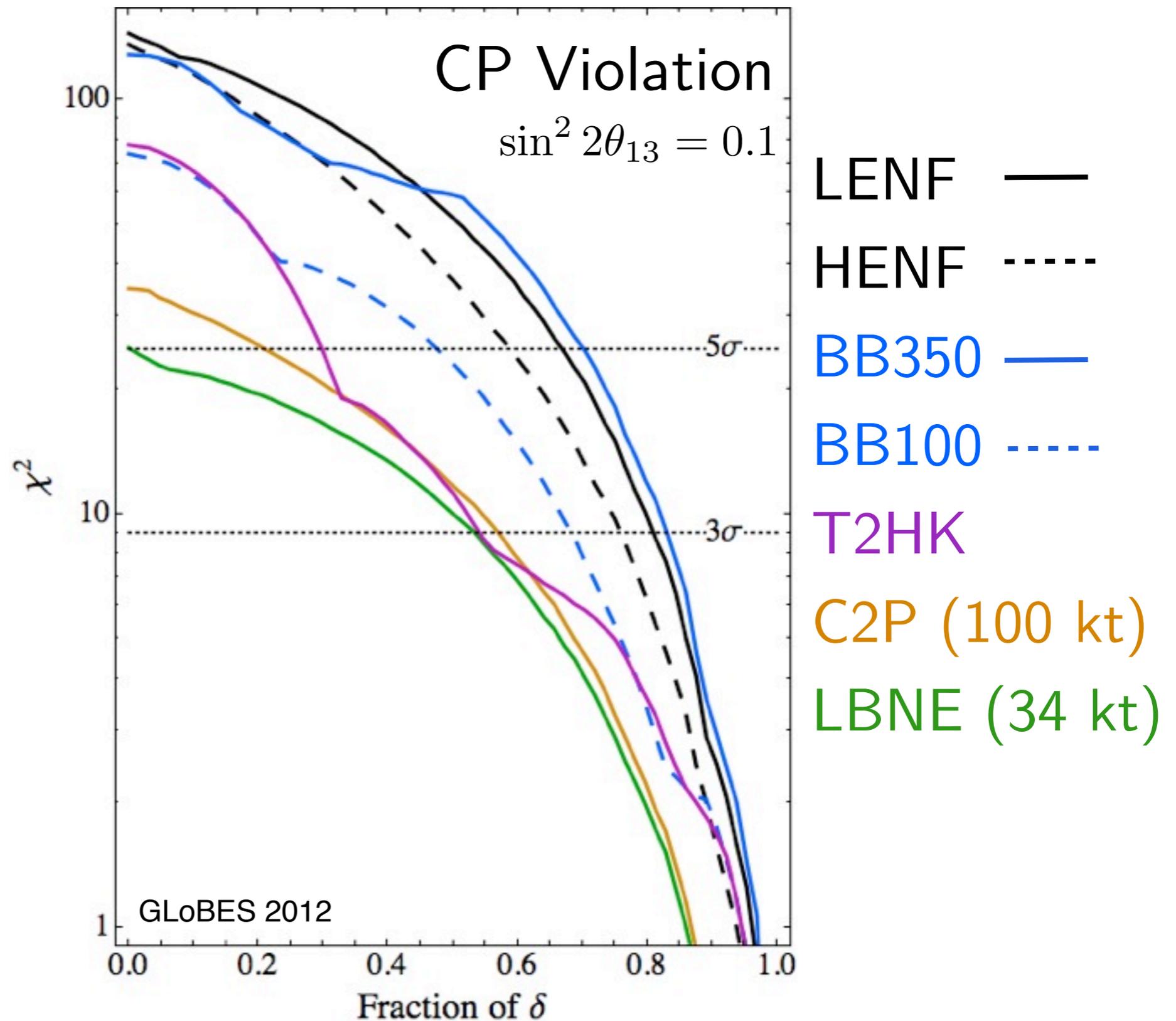
# The setups

- **T2HK** (1109.3262 [hep-ex]): 4 MW, 8 years (4+4), 500 kton WC simulated as in hep-ph/0204352,  $L=295$  km
- **C2P** (1001.0077 [physics.ins-det]): 800 kW, fluxes from PoS ICHEP2010 (2010) 325, 10 years (5+5), 100 kton LAr,  $L=2300$  km
- **LBNE** (1110.6249 [hep-ex]): 700 kW, 10 years (5+5), 34 kton LAr,  $L=1290$  km
- **SPL** (detector as in hep-ph/0603172, fluxes from 1106.1096 [physics-acc.ph]): 4 MW, 10 years (2+8), 500 kton WC,  $L=130$  km

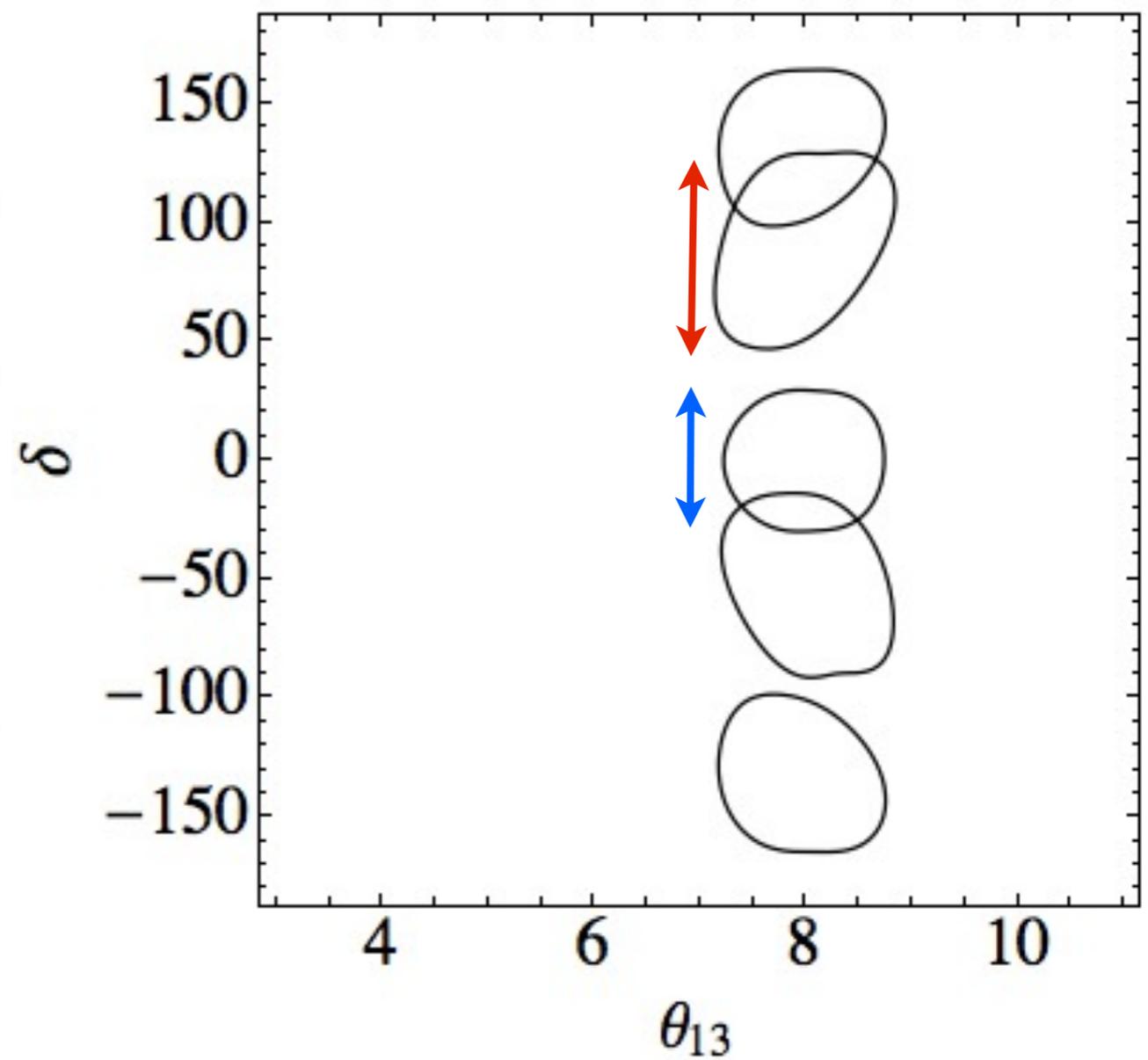
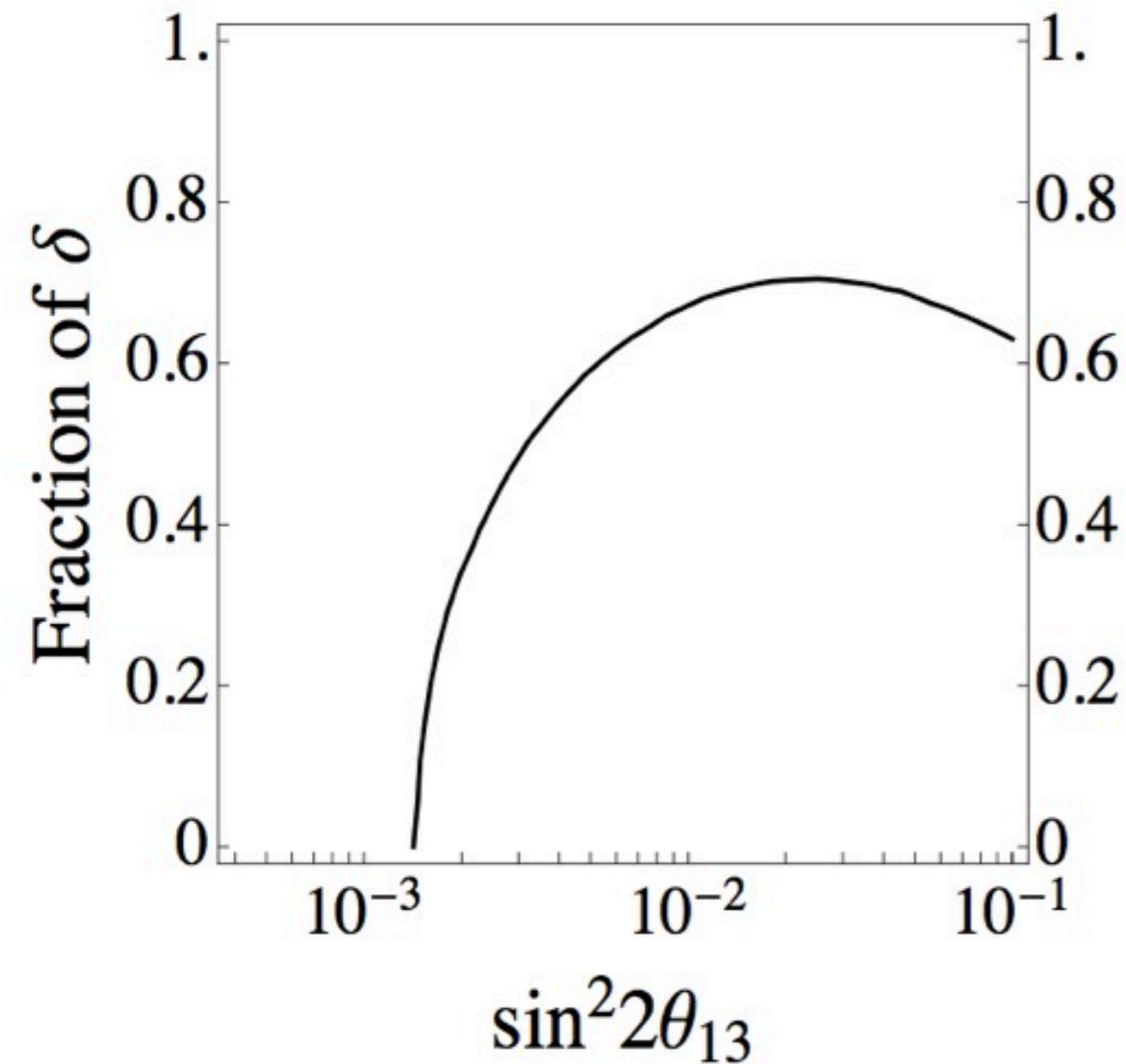
# The setups

- **BB350/100** (hep-ph/0312068, hep-ph/0503021):  $\gamma=350$ ,  $1.1(2.8)e18$  useful  $^{18}\text{Ne}(^6\text{He})$  ion decays per year, 10 years (5+5), 500 kton WC,  $L=650/130$  km
- **LENF/IDS1B** (1012.1872 [hep-ph],): 10/25 GeV muons,  $1.4e21$  useful muon decays per year, 10 years (5+5), 100 kton MIND,  $L=2000/4000$  km

# General landscape

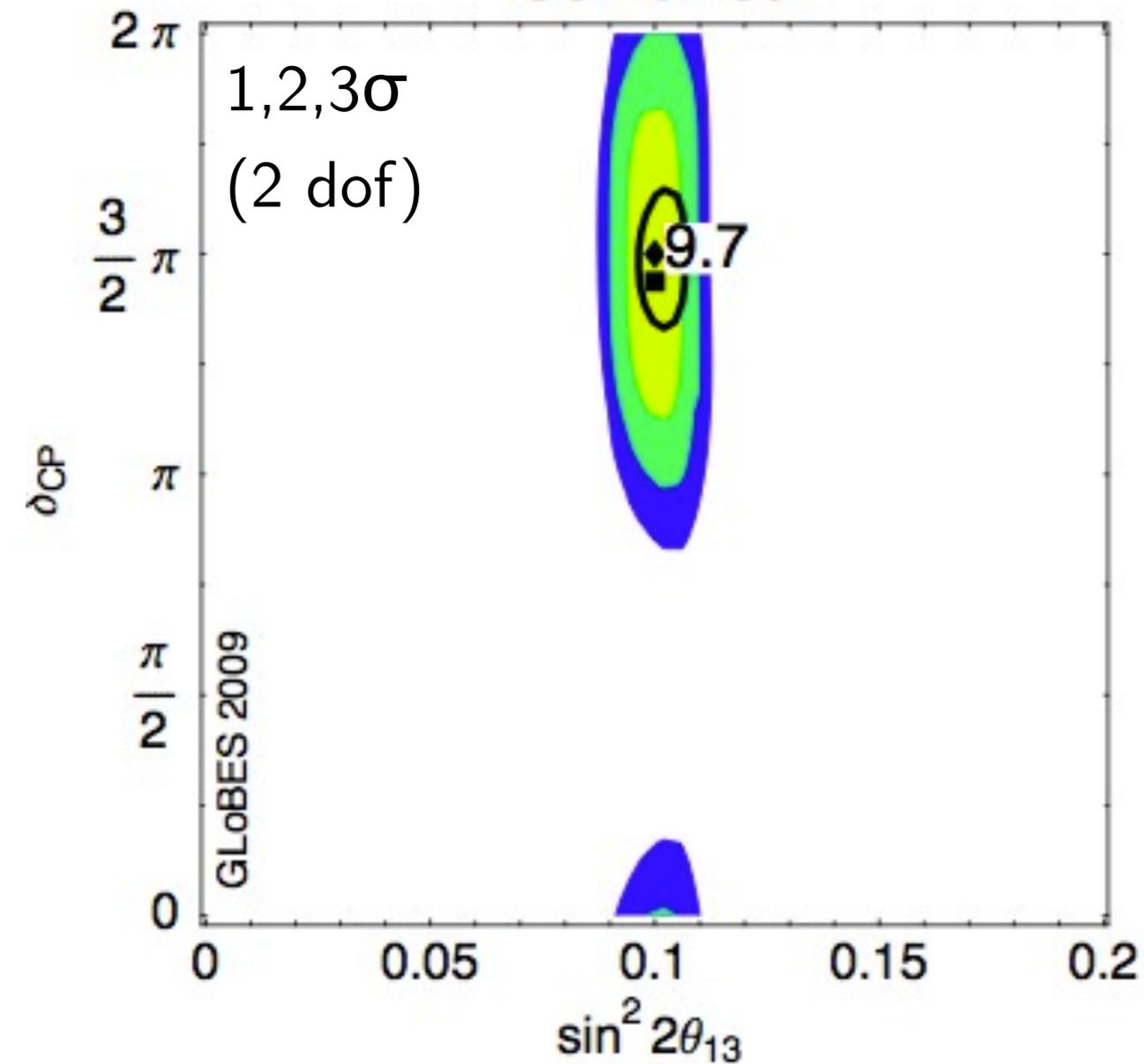


# Discovery vs precision

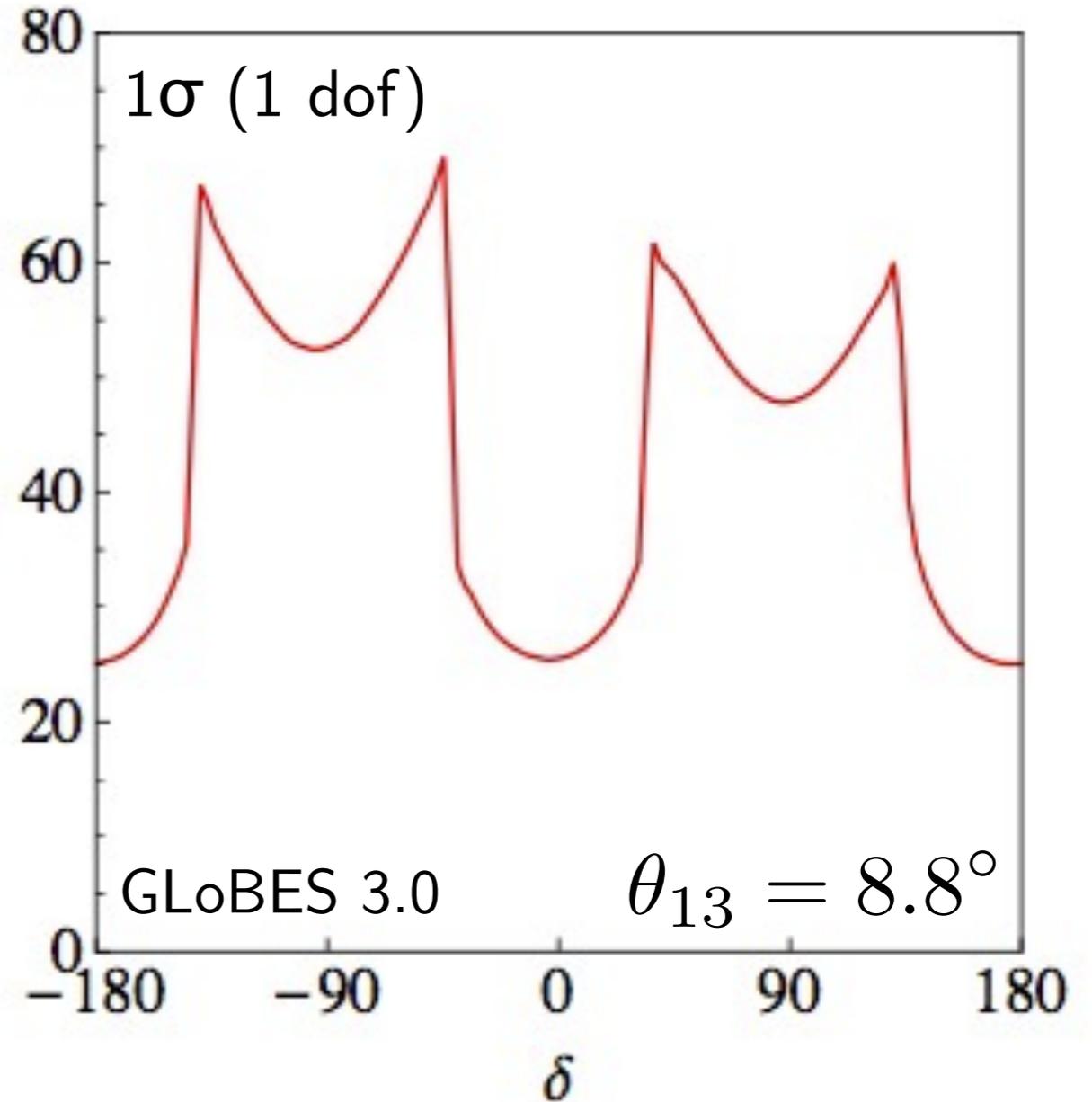


# The starting point

NO $\nu$ A+T2K+Daya Bay



Huber, Lindner, Schwetz, Winter,  
0907.1896 [hep-ph]



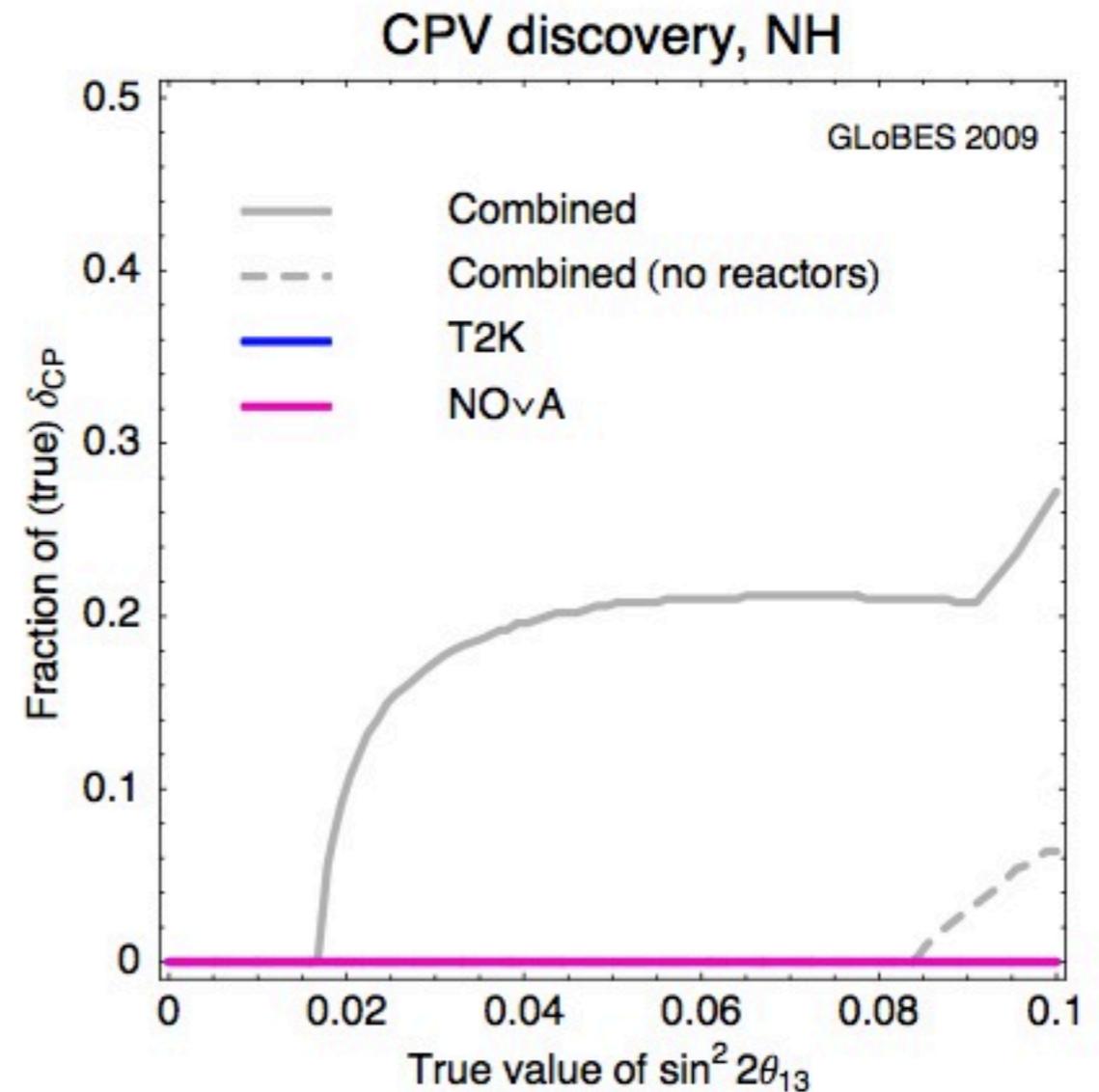
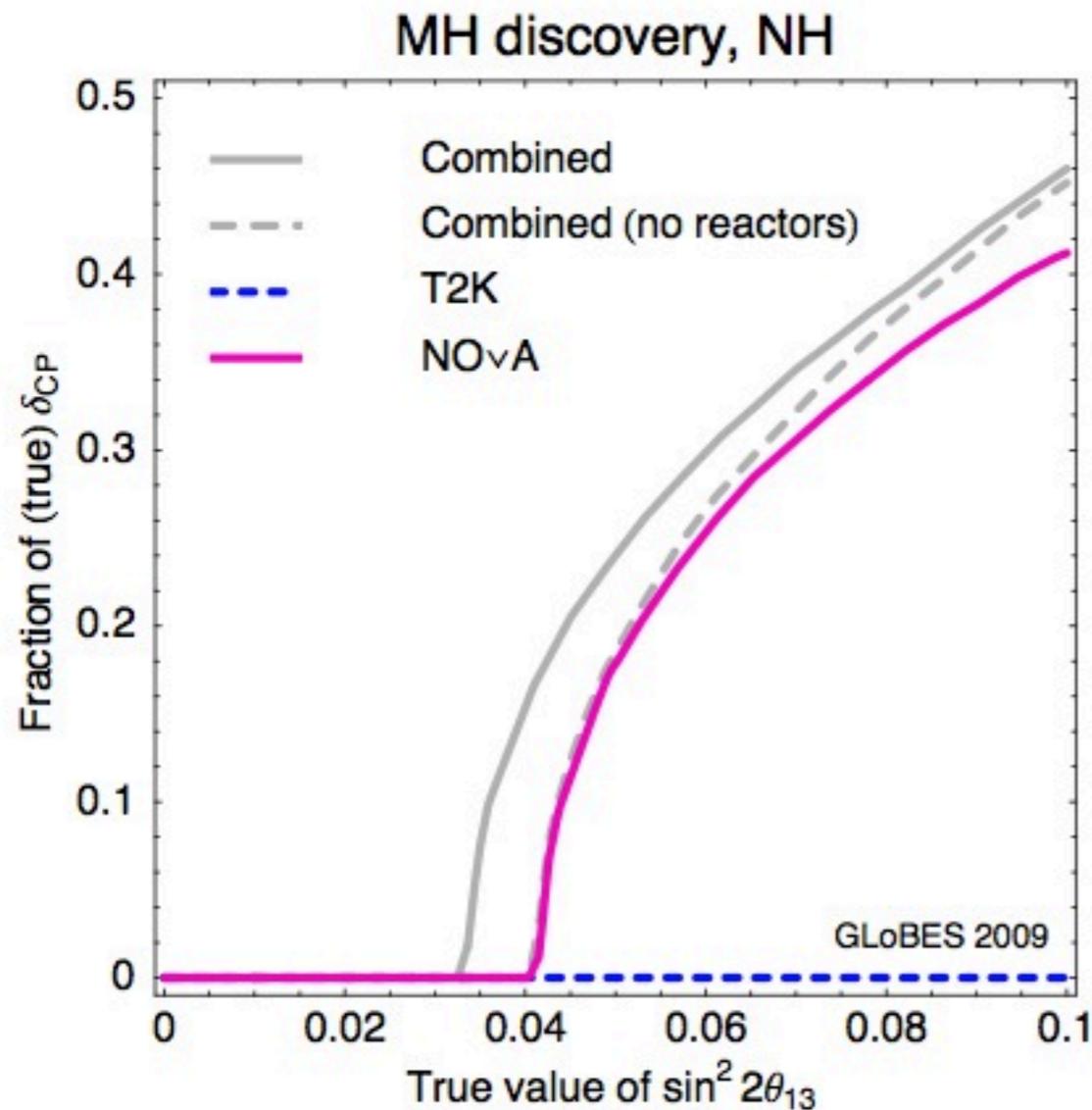
Coloma, Donini, Fernández-Martínez,  
Hernández, 1203.5651 [hep-ph]

# Simulation details

- GLoBES software used hep-ph/0407333  
hep-ph/0701187
- Input values in agreement with best fits 1205.5254 [hep-ph]  
1205.4018 [hep-ph]
- Marginalization over solar and atmospheric params performed assuming  $1\sigma$  gaussian priors 1108.1376 [hep-ph]
- $\theta_{13}$  varied in the  $3\sigma$  range allowed by Daya Bay, around their best fit in March 2012 1203.1669 [hep-ex]
- $1\sigma$  (1 dof) unless stated otherwise
- No degeneracies have been accounted for: atmospheric angle set to maximal, normal hierarchy

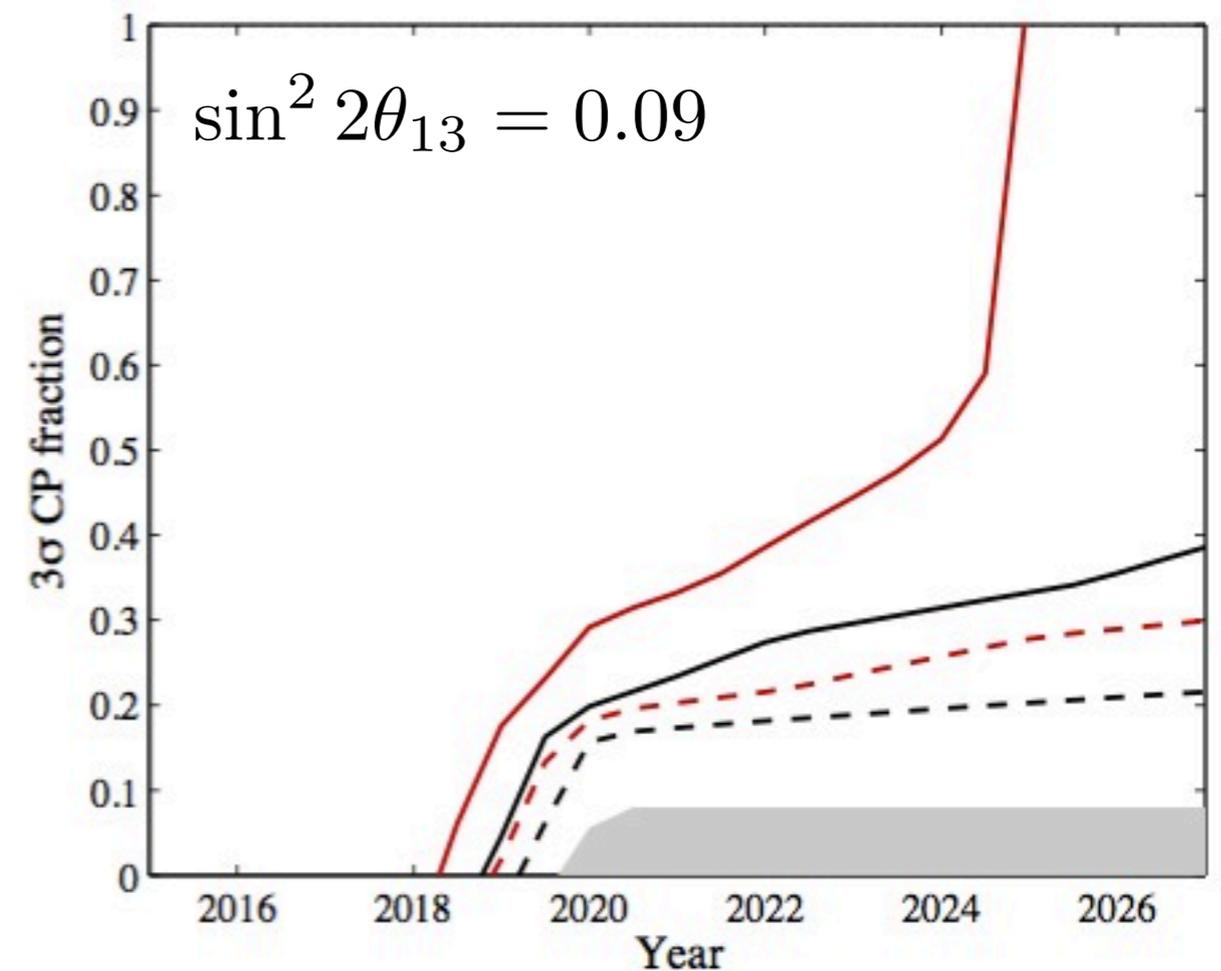
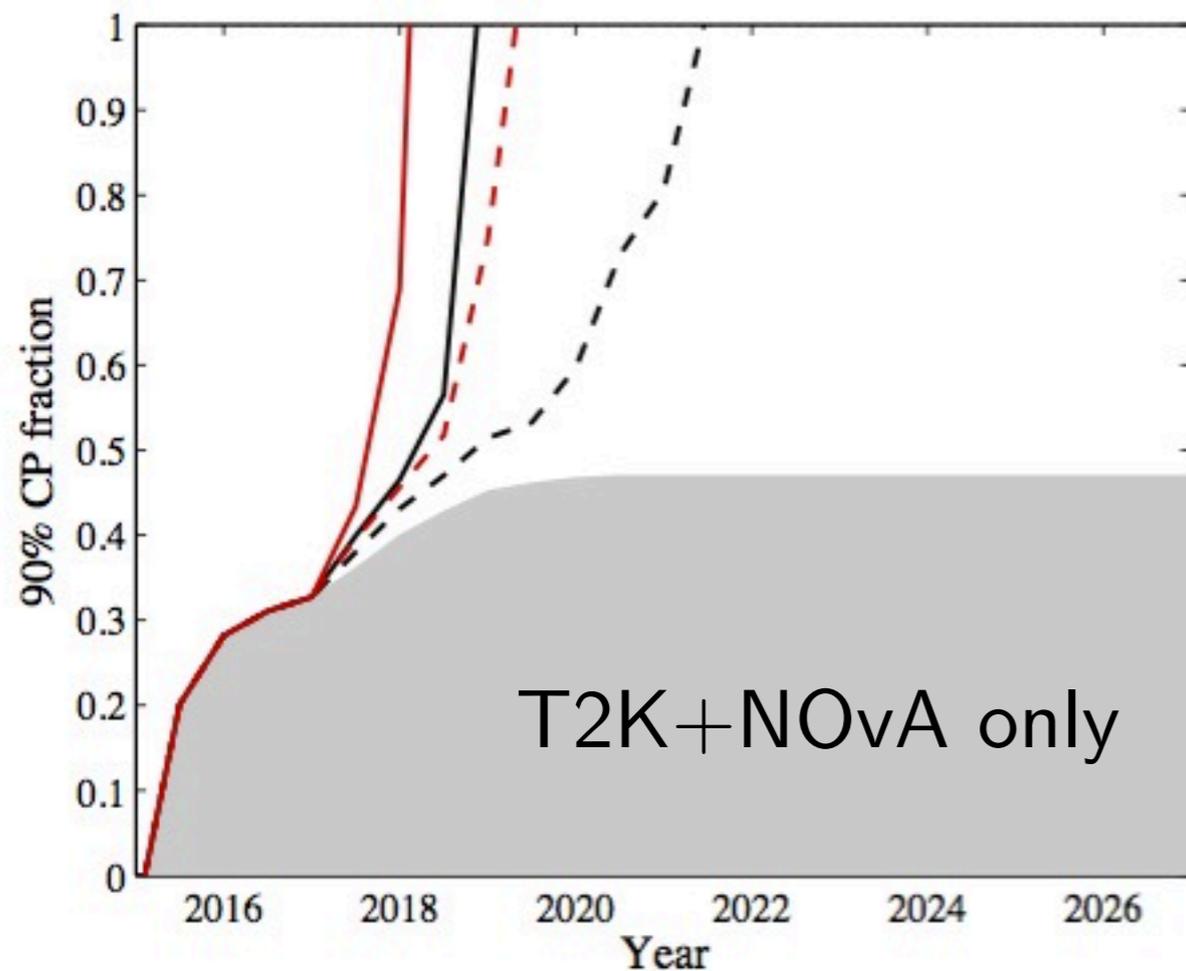
# Mass hierarchy

Discovery potential at the 90% CL



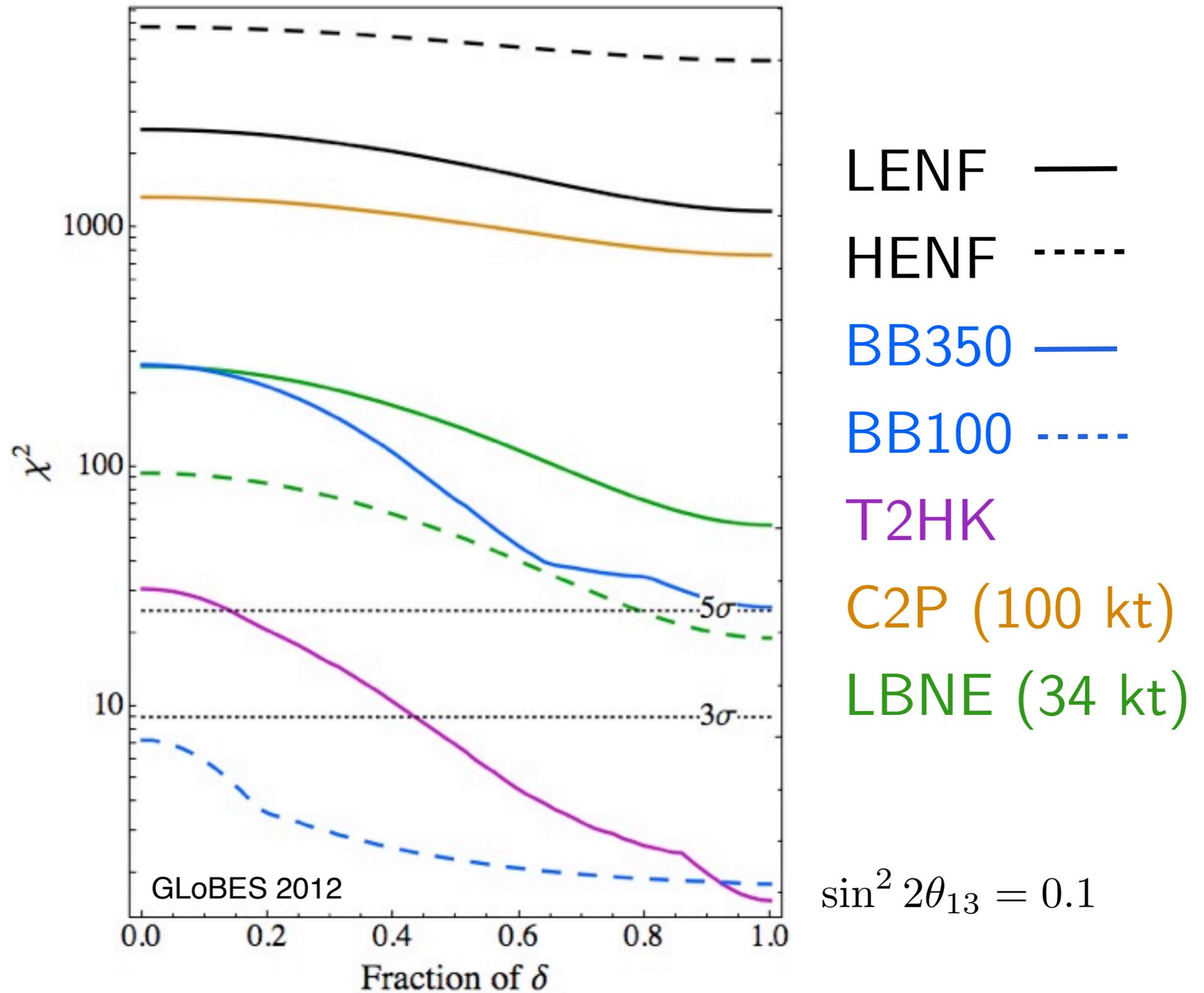
# Mass Hierarchy

T2K+NOvA+INO  
(50kt/100kt; low/high res)

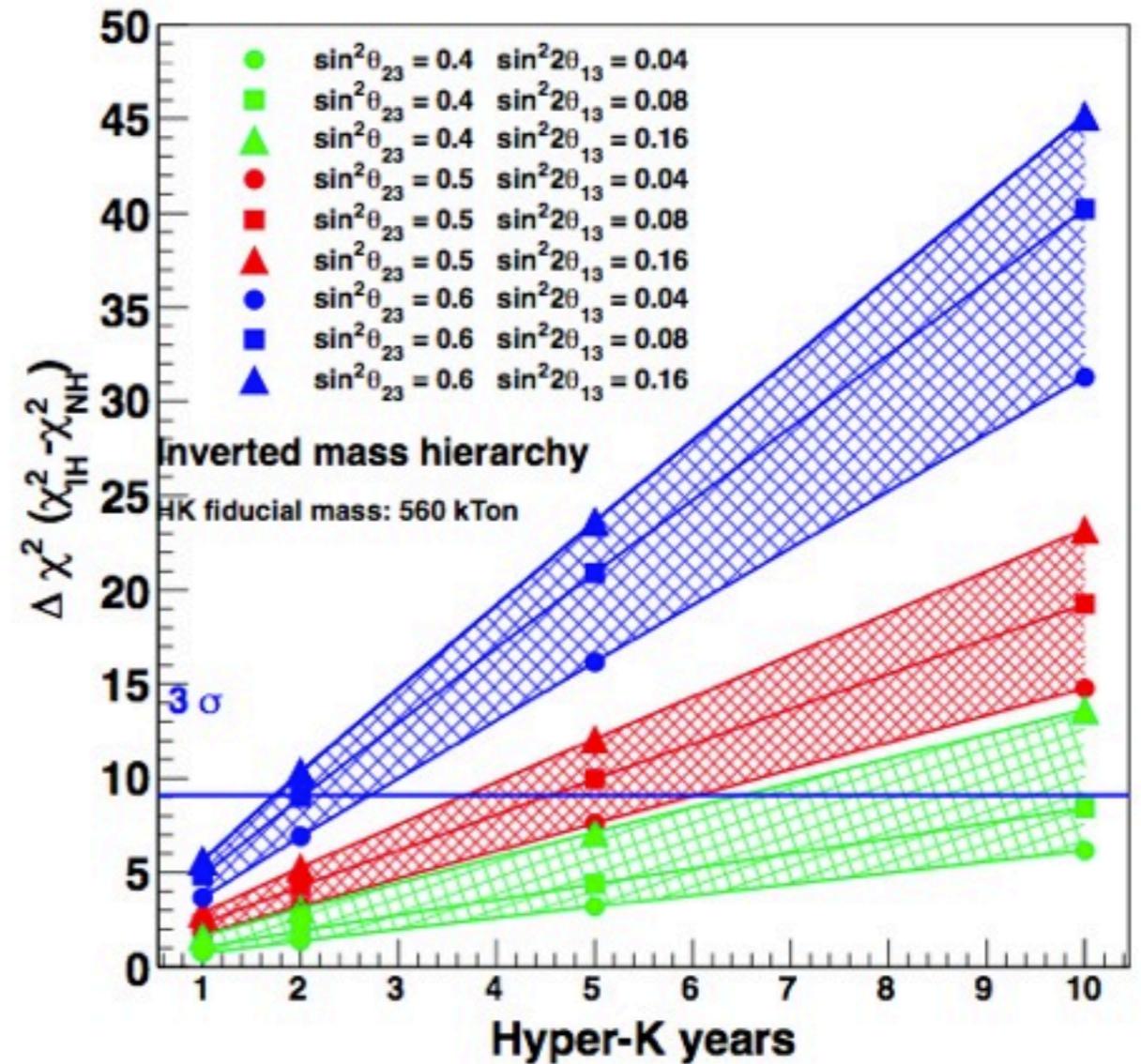
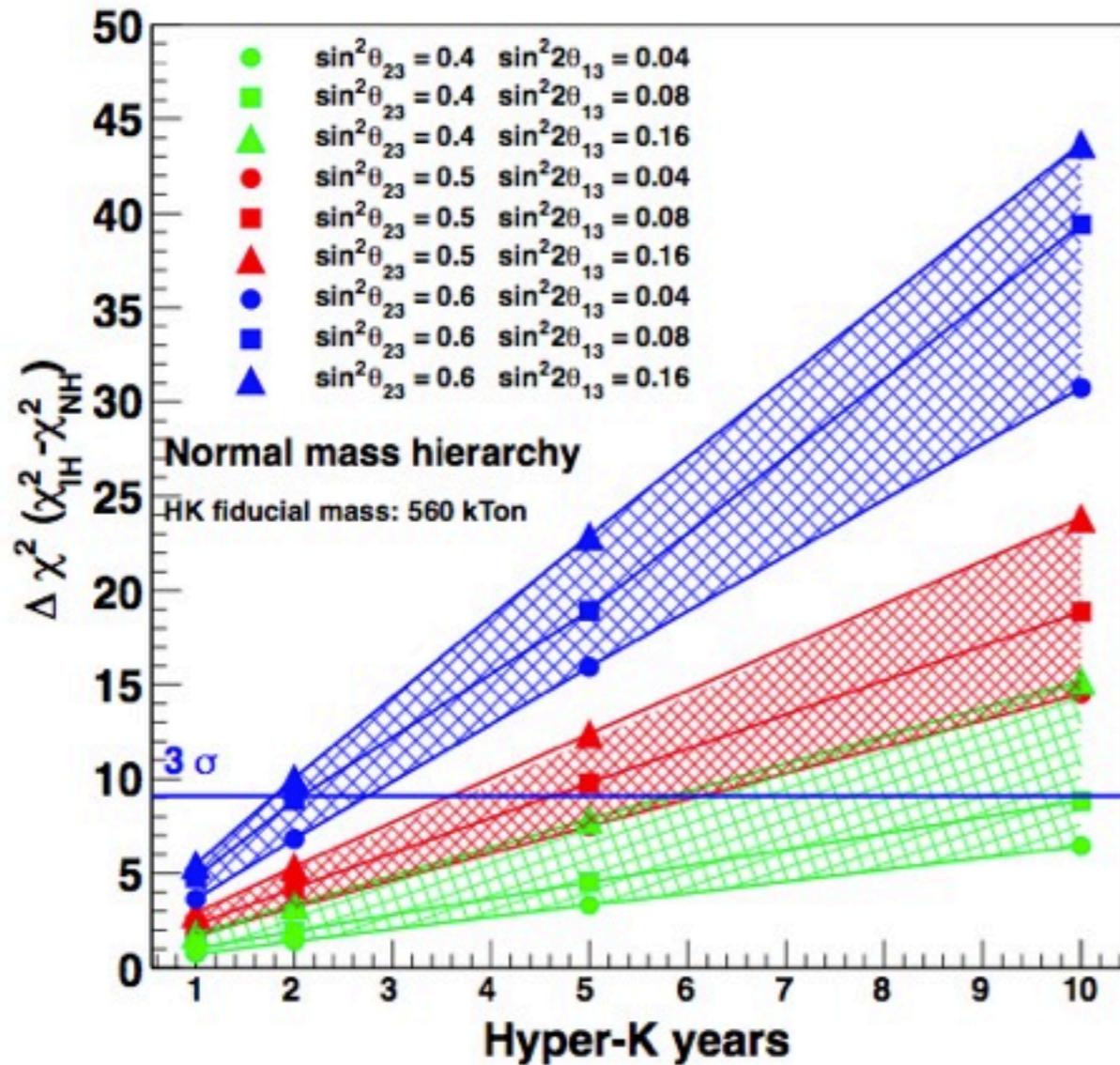


Blennow, Schwetz, 1203.3388 [hep-ph]

# Mass hierarchy



# Mass Hierarchy



HK Lol, 1109.3262 [hep-ex]

Precisión in theta13

# Error propagation

$$\Delta N_{\pm} = \left| \frac{\partial N_{\pm}}{\partial \theta_{13}} \right| (\Delta \theta_{13})_{\pm}$$

*neutrino/antineutrino*



# Error propagation

$$\Delta N_{\pm} = \left| \frac{\partial N_{\pm}}{\partial \theta_{13}} \right| (\Delta \theta_{13})_{\pm} \propto \theta_{13} \frac{\sin^2((1 \mp \hat{A})\Delta)}{(1 \mp \hat{A})^2} (\Delta \theta_{13})_{\pm} + \dots$$

$$\hat{A} \equiv \frac{\sqrt{2}G_F n_e L}{2\Delta}; \Delta \equiv \frac{\Delta m_{13}^2 L}{4E}$$

The final error would be:

$$(\Delta \theta_{13}) \simeq \left( \sqrt{\frac{1}{(\Delta \theta_{13})_+^2} + \frac{1}{(\Delta \theta_{13})_-^2}} \right)^{-1}$$

# Error propagation

$$(\Delta\theta_{13})_{\pm} \propto \left[ \frac{(1 \mp \hat{A})^2}{\sin^2((1 \mp \hat{A})\Delta)} \right] \frac{1}{\theta_{13}} \Delta N_{\pm}$$

Statistical limit:

$$\Delta N_{\pm} \propto \sqrt{N_{\pm}} \propto \theta_{13} \longrightarrow (\Delta\theta_{13})_{\pm} \propto \text{const}$$

Systematics on the signal:

$$\Delta N_{\pm} \propto N_{\pm} \propto \theta_{13}^2 \longrightarrow (\Delta\theta_{13})_{\pm} \propto \theta_{13}$$

Background error:

$$\Delta N_{\pm} \propto \text{const} \longrightarrow (\Delta\theta_{13})_{\pm} \propto 1/\theta_{13}$$

# Precision in $\theta_{13}$

Statistical limit:

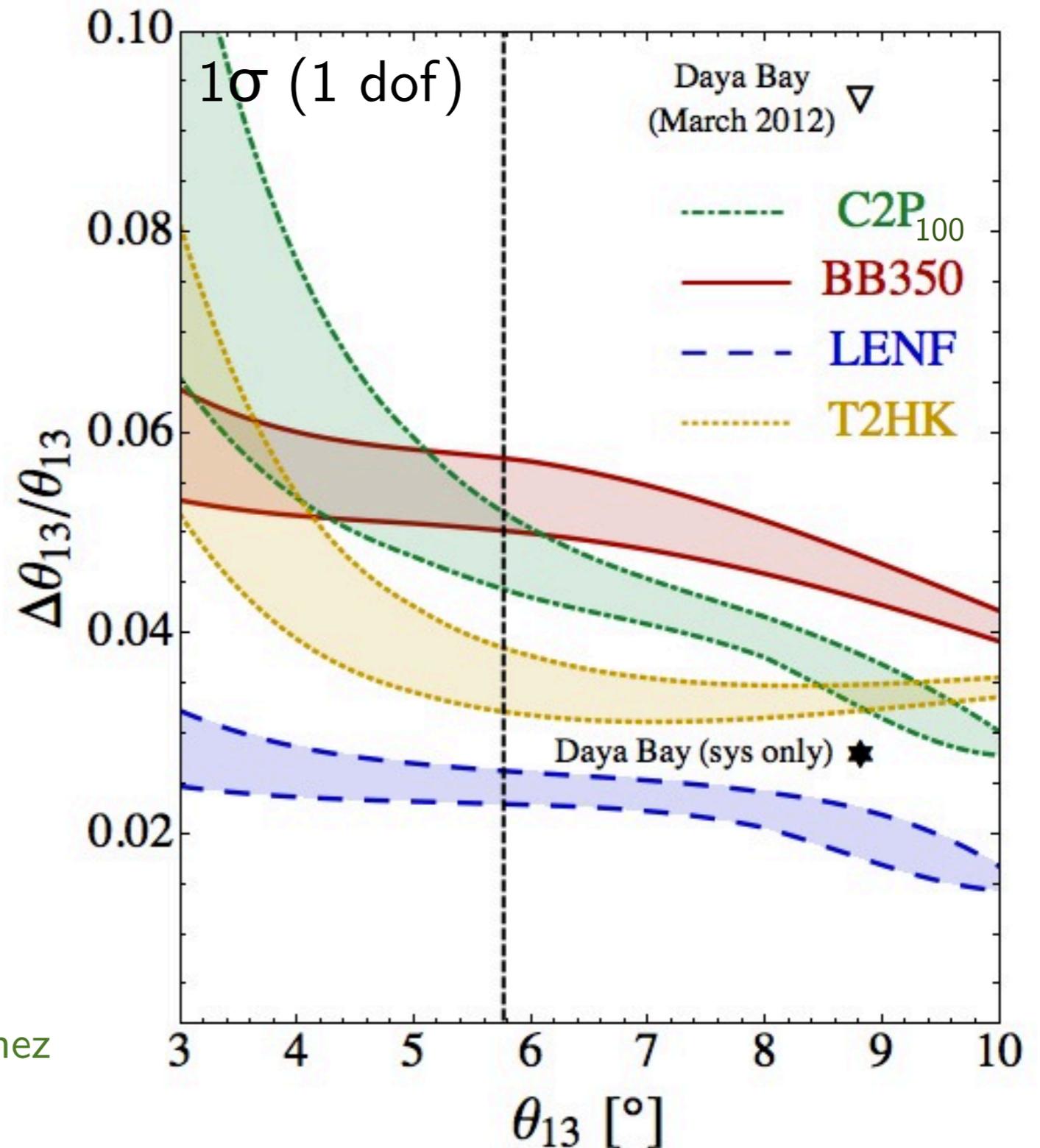
$$\frac{\Delta\theta_{13}}{\theta_{13}} \propto \frac{1}{\theta_{13}}$$

Systematics on the signal:

$$\frac{\Delta\theta_{13}}{\theta_{13}} \propto \text{const}$$

Background error:

$$\frac{\Delta\theta_{13}}{\theta_{13}} \propto \frac{1}{\theta_{13}^2}$$



Precisión  $\delta$

# Precision in $\delta$

Error propagation:

$$(\Delta\delta)_{\pm} \propto \left| \frac{\hat{A}\Delta}{\sin \hat{A}\Delta \sin(\Delta \mp \delta)} \right|$$

*position of maxima depend both on delta and the matter effects*

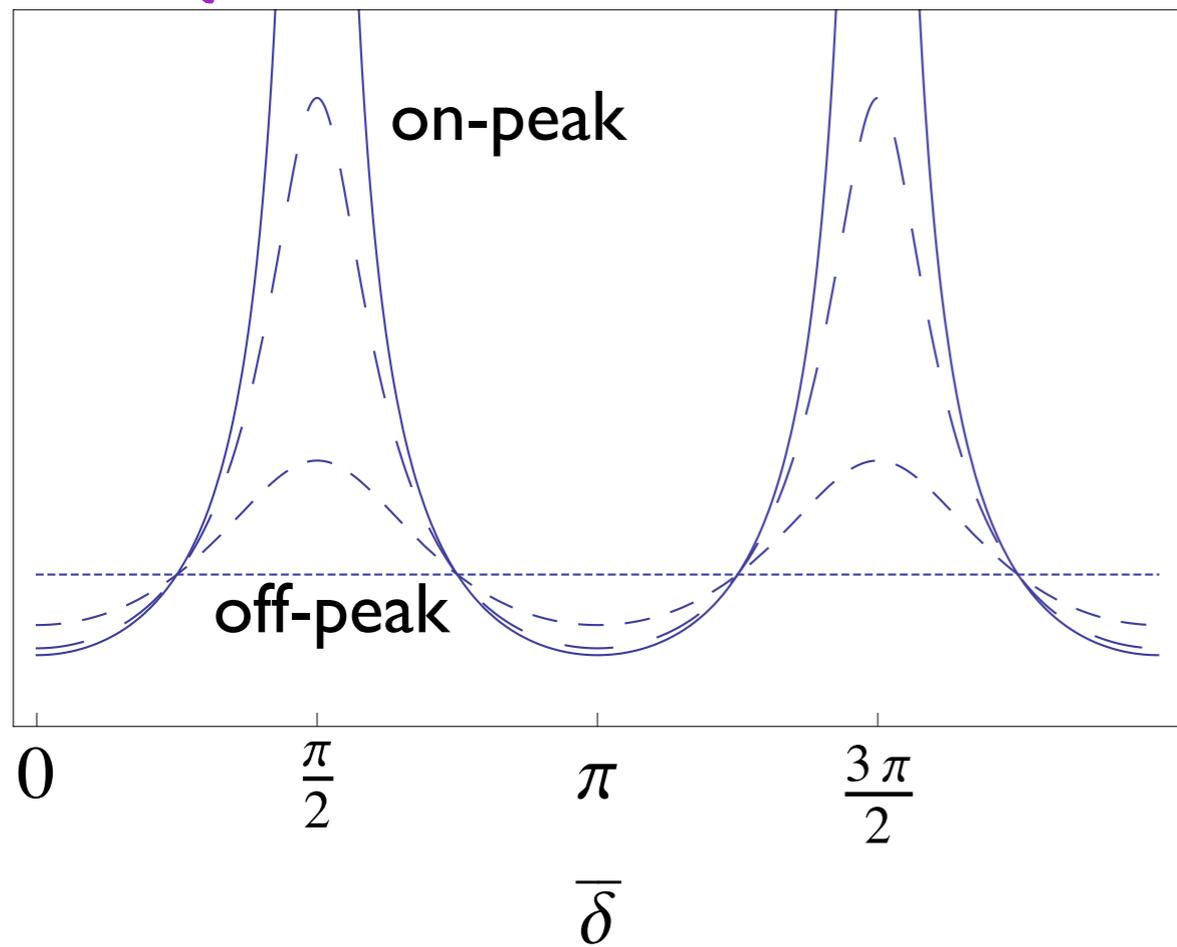
$$(\Delta\delta) \simeq \left( \sqrt{\frac{1}{(\Delta\delta)_+^2} + \frac{1}{(\Delta\delta)_-^2}} \right)^{-1}$$

# Precision in $\delta$

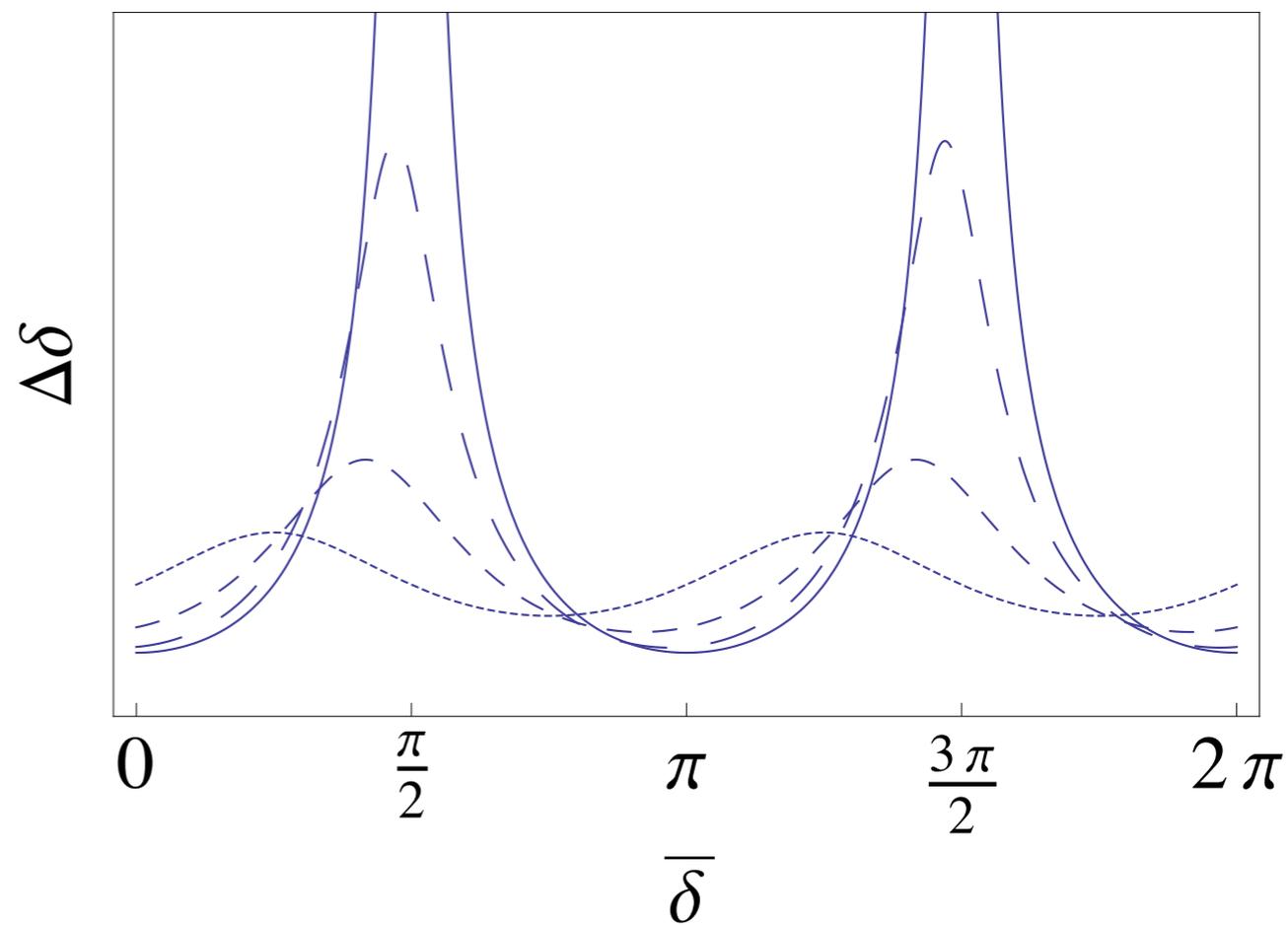
VACUUM

$$(\Delta\delta)_{\pm} \propto f[\Delta] \frac{1}{\sin\left(\frac{\pi}{2} \mp \delta\right)}$$

equal  $\nu$  and  $\bar{\nu}$  events



less  $\bar{\nu}$  than  $\nu$  events



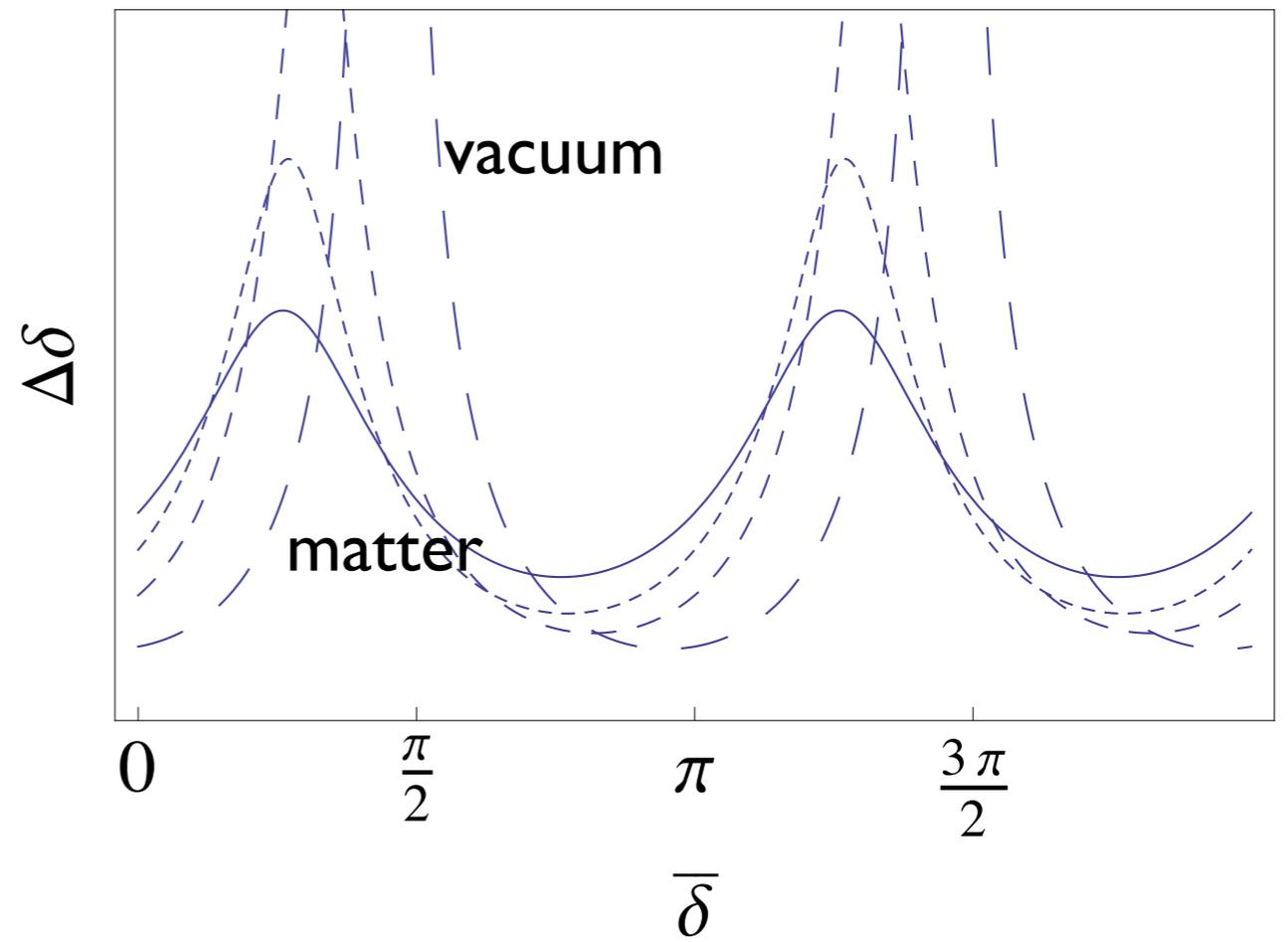
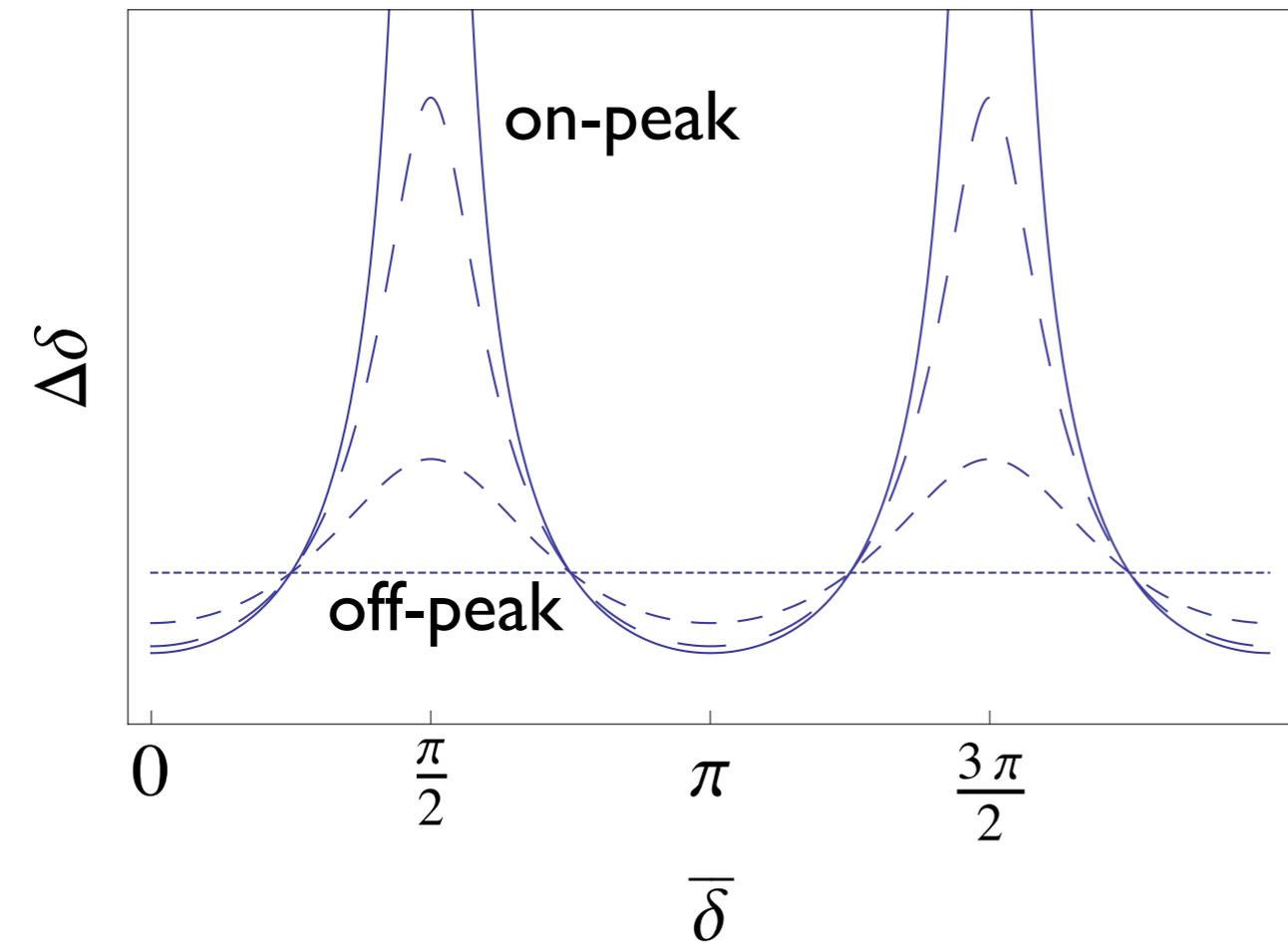
# Precision in $\delta$

**VACUUM**

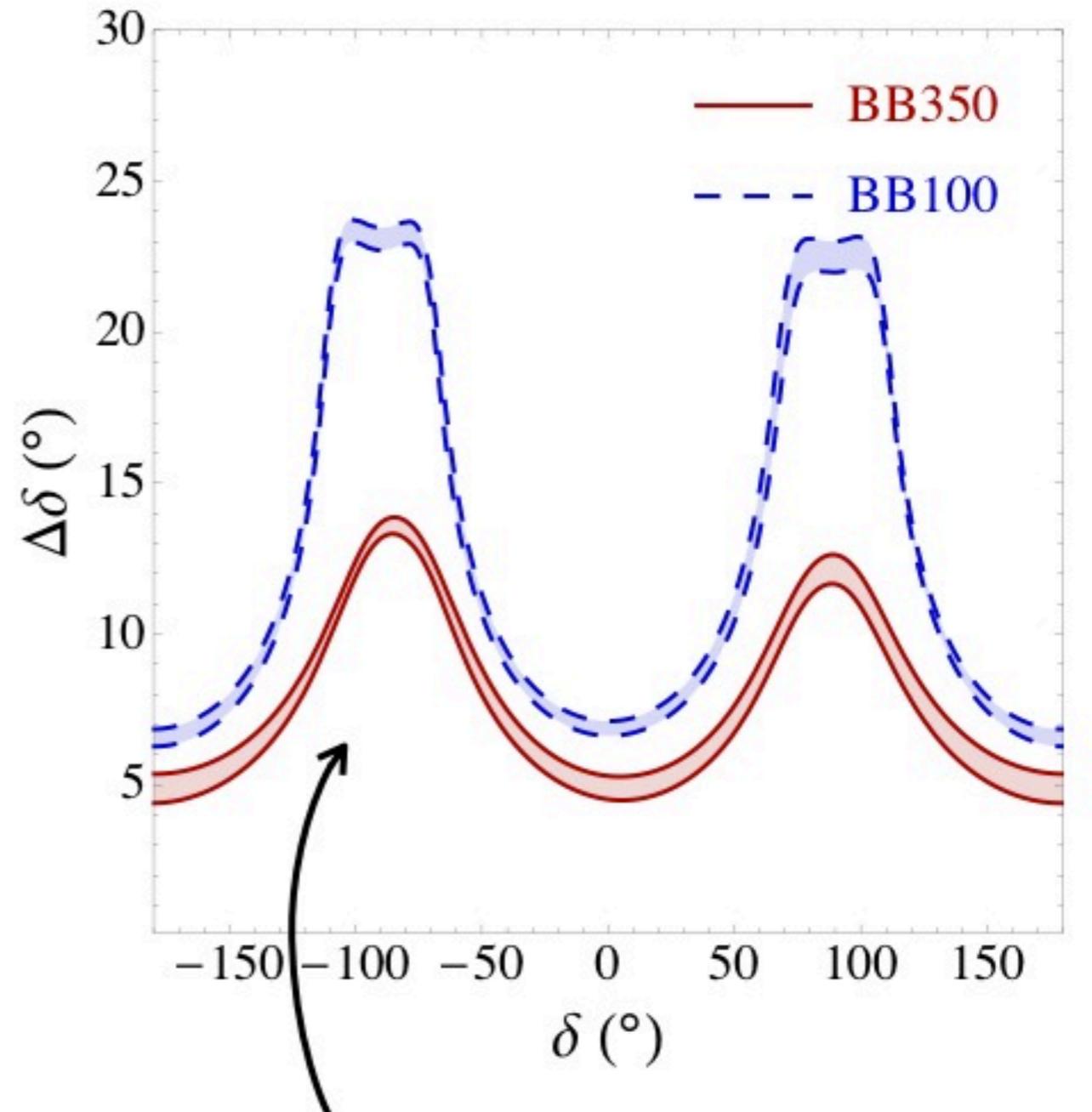
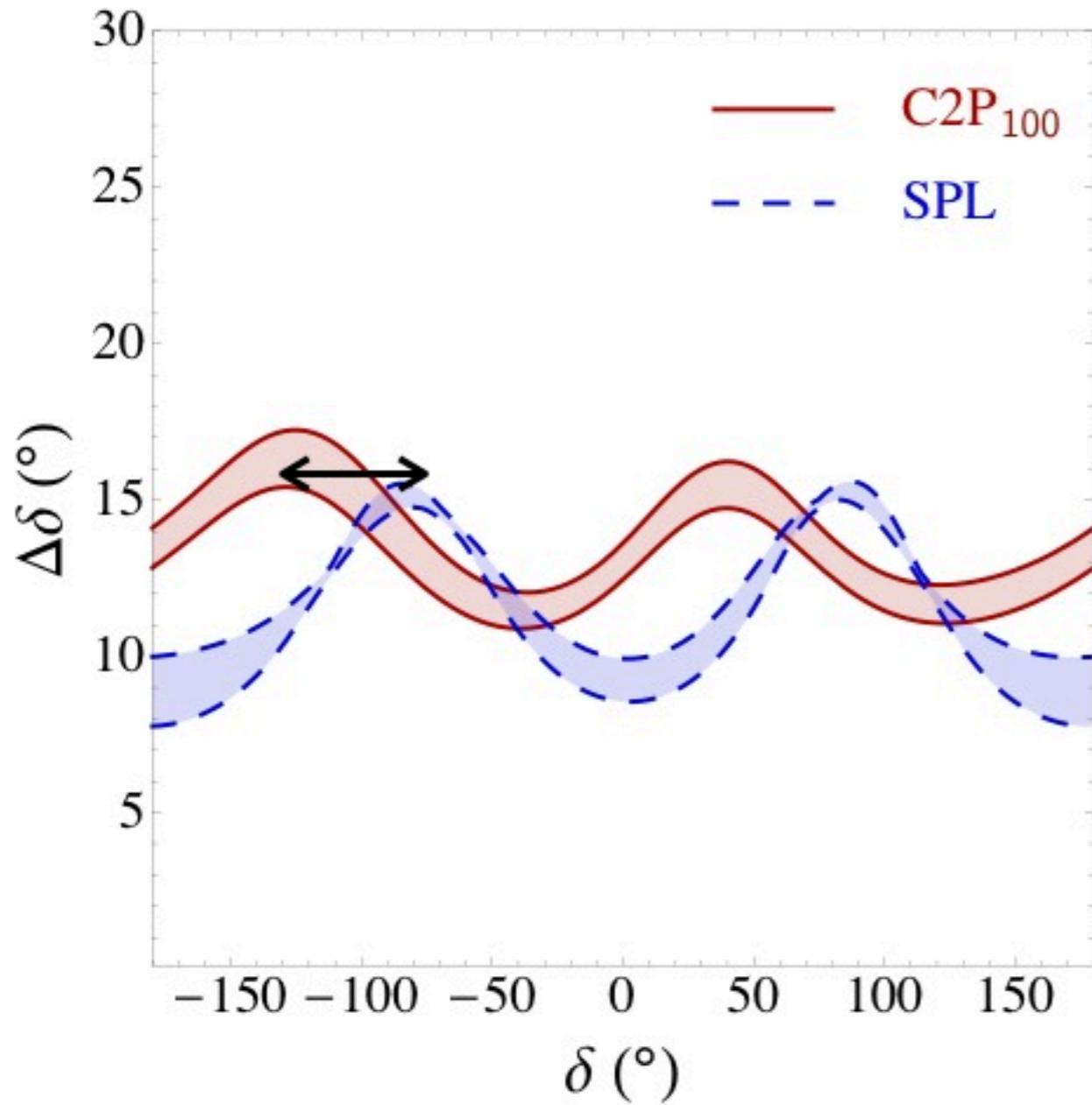
$$(\Delta\delta)_{\pm} \propto f[\Delta] \frac{1}{\sin\left(\frac{\pi}{2} \mp \delta\right)}$$

**MATTER**

$$(\Delta\delta)_{\pm} \propto \tilde{f}[\Delta, \hat{A}] \frac{1}{\sin\left(\frac{\pi}{2} \frac{\hat{A}}{(1 \mp \hat{A})} \mp \delta\right)}$$



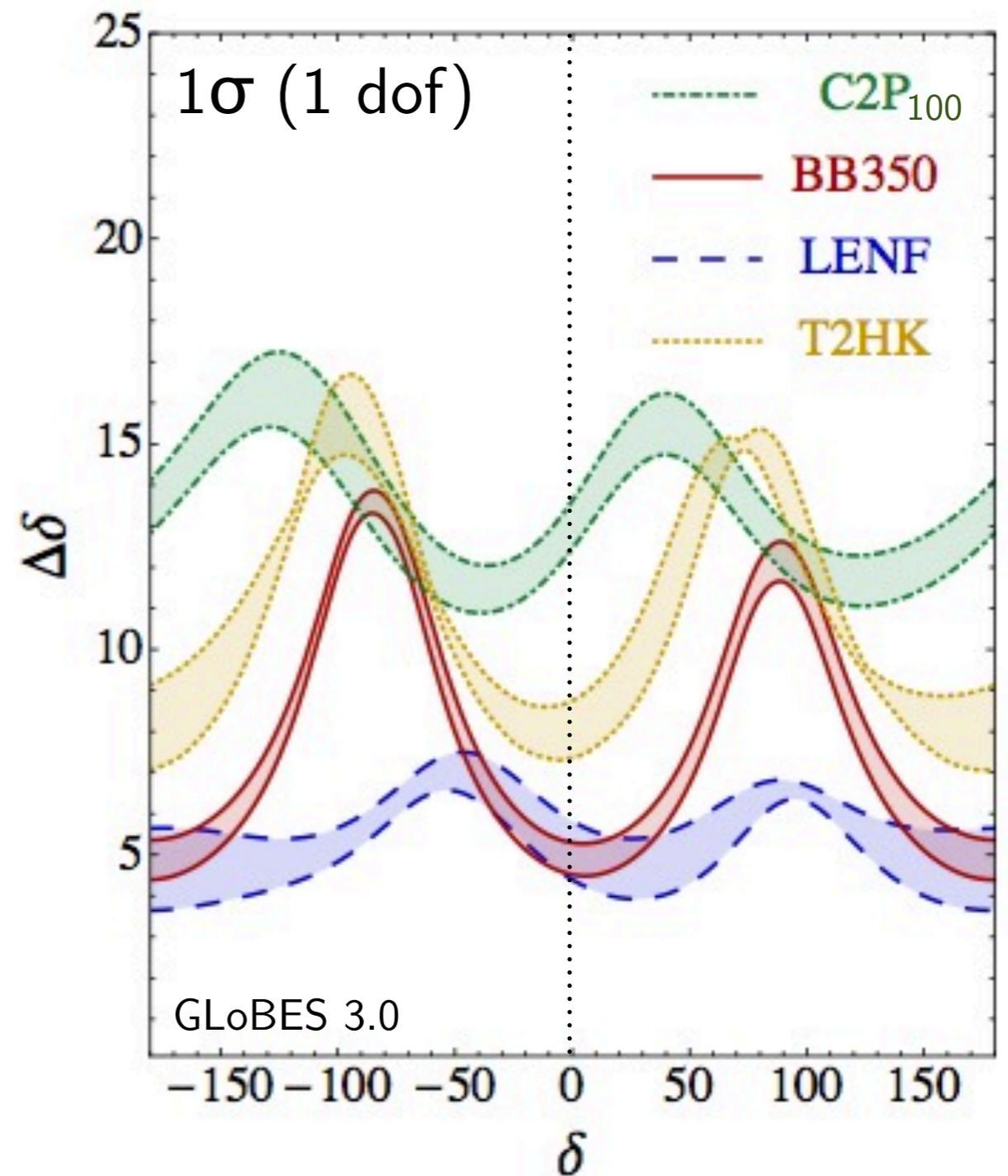
# Precision in $\delta$



BB in combination with T2K

# Precision in $\delta$

- 1) Mild  $\theta_{13}$  dependence
- 2) Strong delta dependence for BB350 due to no disappearance data
- 3) CPV discovery potential related to precision around  $0, \pi$ : more favorable for setups in vacuum and with similar number of nu/nubar events



# Conclusions

- Precision in  $\theta_{13}$ :
  - reactors can only be beaten by a NuFact
- Precision in delta:
  - beta-beams suffer from lack of disappearance data (need to be combined with T2K)
  - BB100 suffers from intrinsic degeneracies: this could be alleviated from a refined analysis or from its combination with SPL
  - Facilities in vacuum have very good precision around  $0, \pi$  but a strong delta dependence
  - Matter effects help to smooth this dependence out

Backup

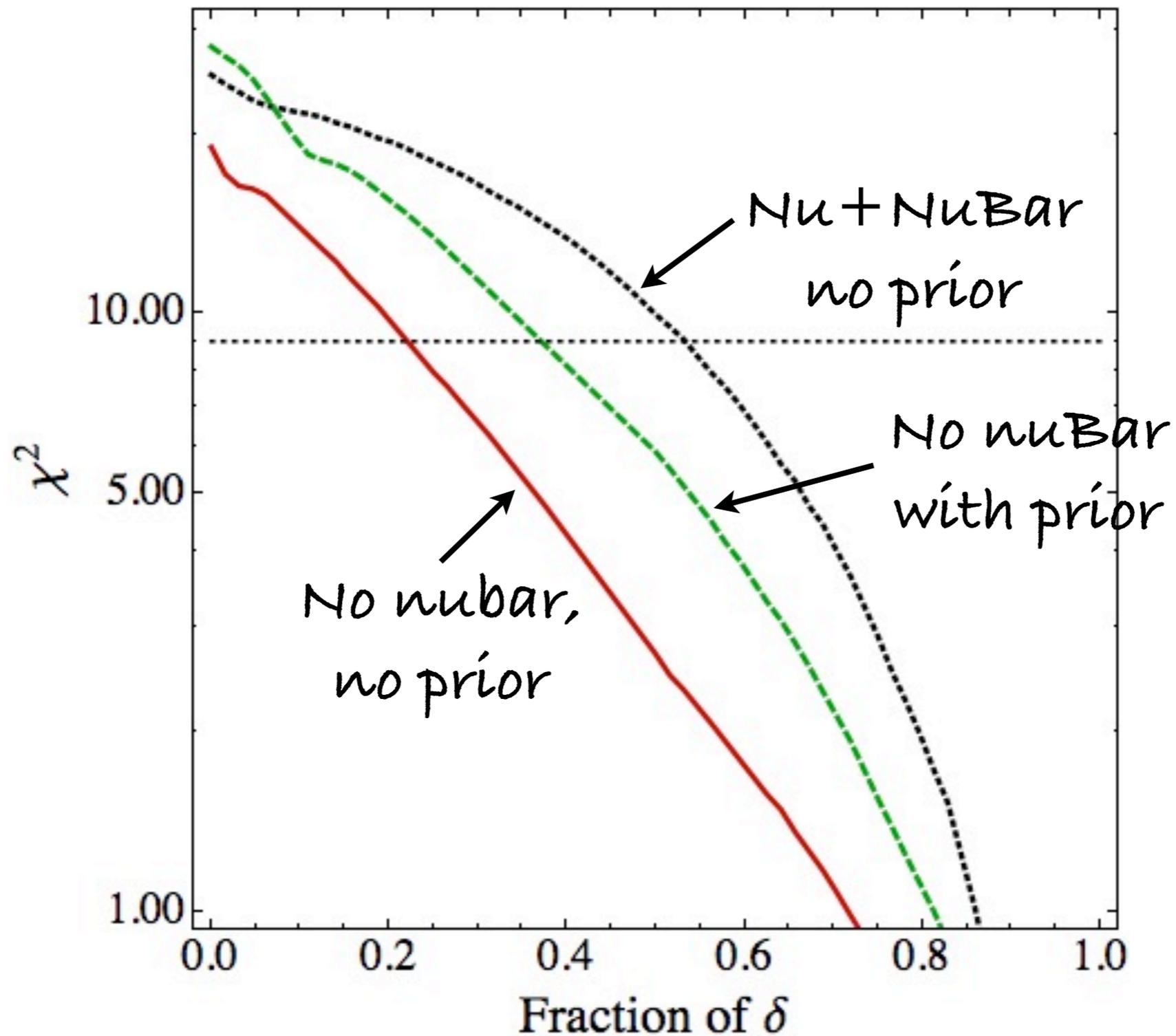
	$L$	$N_\nu/N_{\bar{\nu}}$	$B_\nu/B_{\bar{\nu}}$	$\langle E_\nu \rangle / \langle E_{\bar{\nu}} \rangle$	$\delta E_\nu / \delta E_{\bar{\nu}}$	$\hat{A}$
T2K	295	$2.6/0 \times 10^3$	46/0	0.72/-	0.27/-	0.02
NO $\nu$ A	810	$1.1/0.7 \times 10^3$	10/11	2.02/2.04	0.43/0.42	0.14
T2HK	295	$4.3/1.3 \times 10^5$	$4.3/1.5 \times 10^3$	0.79/0.80	0.18/0.18	0.022
LBNE	1290	$2.3/0.9 \times 10^4$	302/201	3.55/3.50	1.38/1.33	0.30
SPL	130	$2.5/1.6 \times 10^5$	$1.1/1.2 \times 10^3$	0.59/0.57	0.20/0.21	0.017
C2P	2300	$2.4/1.1 \times 10^4$	210/129	5.04/5.15	1.65/1.59	0.48
BB100	130	$2.9/4.4 \times 10^4$	$0.6/1.2 \times 10^3$	0.47/0.45	0.18/0.18	0.013
BB350	650	$5.0/9.2 \times 10^4$	372/432	1.53/1.61	0.45/0.45	0.11
LENF	2000	$8.1/5.3 \times 10^5$	48/81	6.75/6.78	1.81/1.79	0.63
IDS1b	4000	$1.9/1.2 \times 10^6$	154/196	16.85/16.86	4.57/4.55	1.65

# Setup details

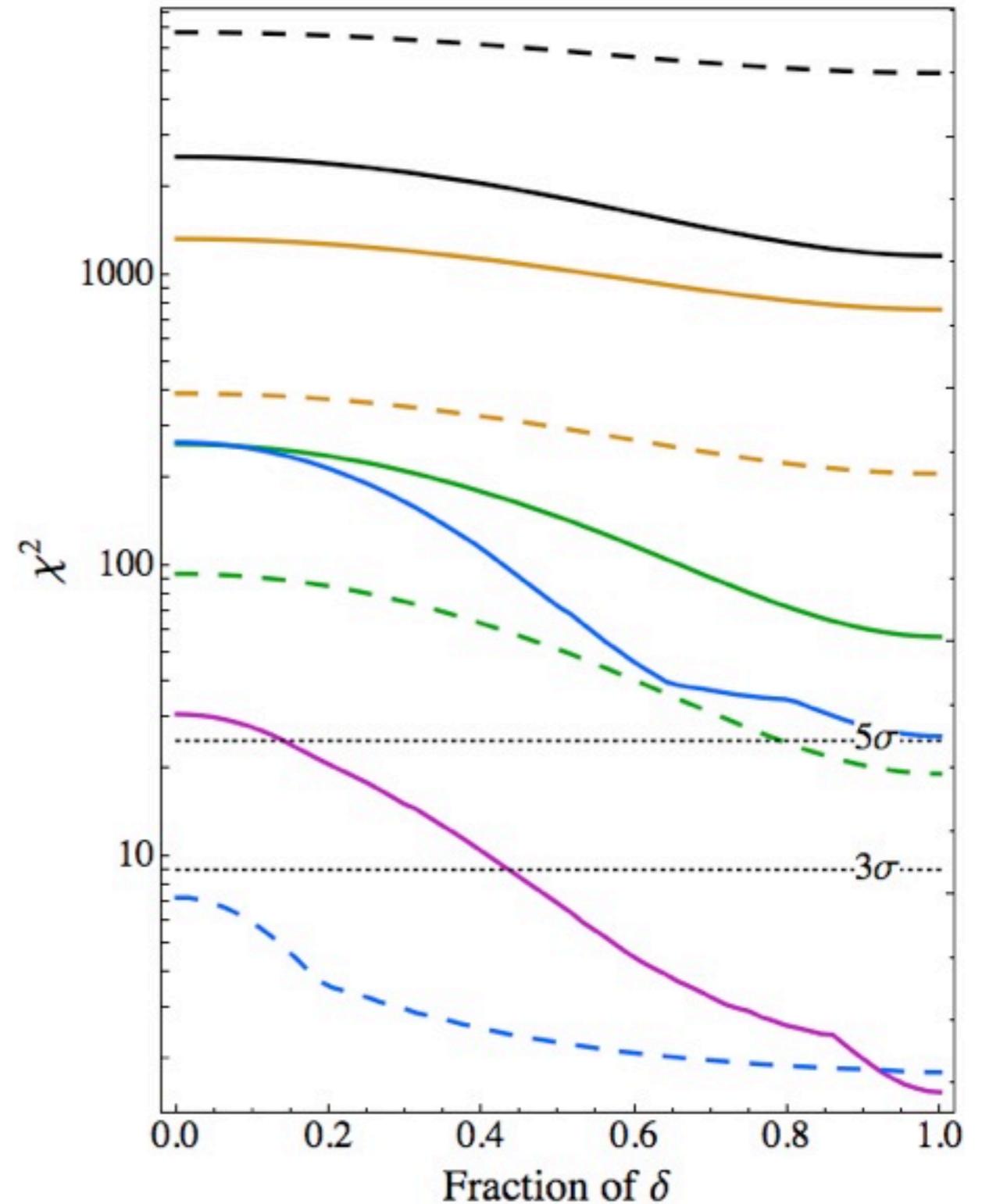
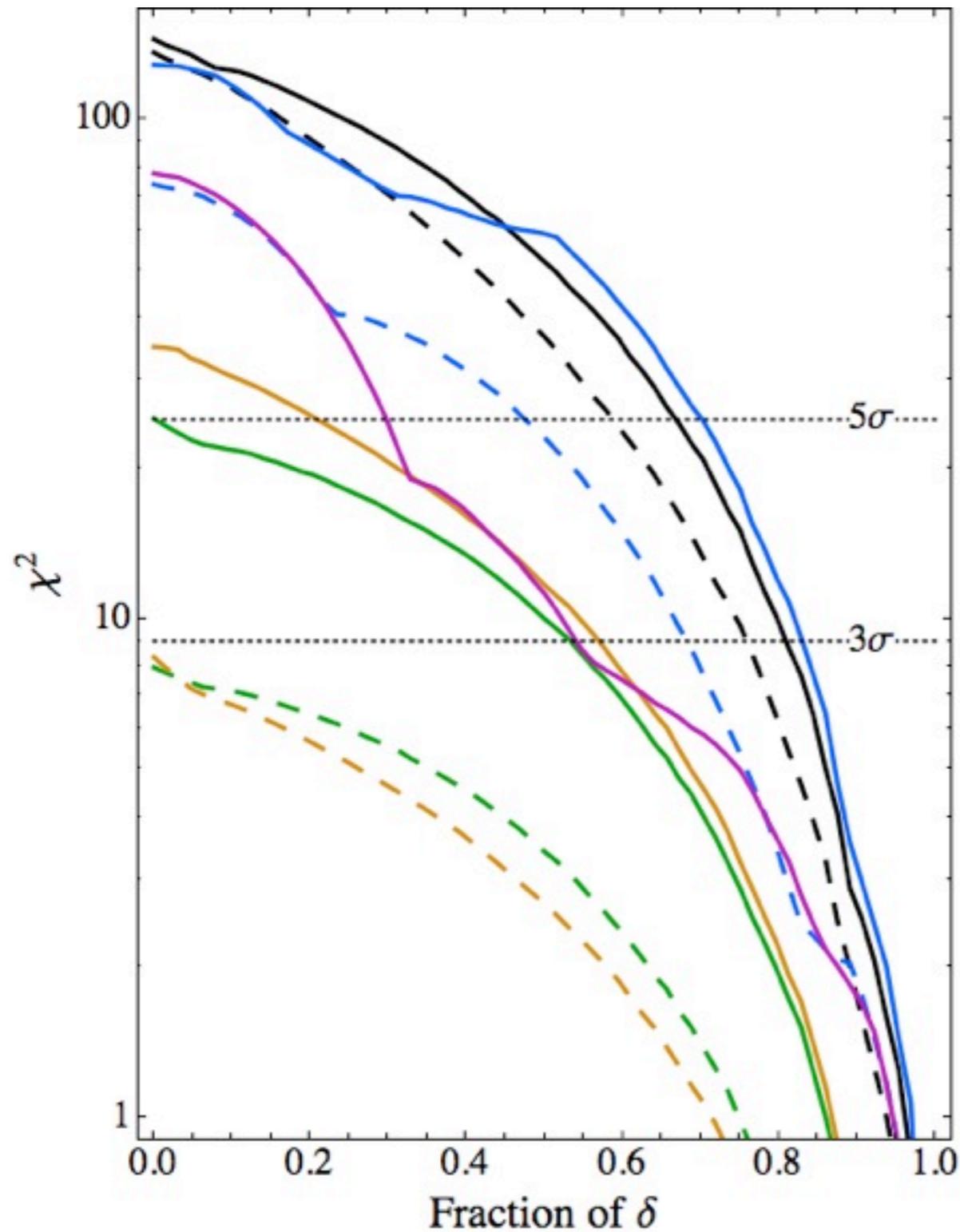
	$L$ (km)	Det. (kton)	MW	$(t_\nu, t_{\bar{\nu}})$	Refs.
T2K	295	WC (22.5)	0.75	(5,0)	[79–83]
NO $\nu$ A	810	TASD (15)	0.7	(3,3)	
T2HK	295	WC (500)	4.0	(4,4)	[38, 84, 85]
LBNE	1290	LAr (33.4)	0.7	(5,5)	[33, 86, 87]
SPL	130	WC (440)	4.0	(2,8)	[16, 36]
C2P	2300	LAr (100)	0.8	(5,5)	[33, 88, 89]

**Table 2:** Summary of the main details for the conventional beam and super-beam setups that have been presented in the comparison. From left to right, each column indicates the baseline, the detector technology (Water Čerenkov, Totally Active Scintillator Detector, or Liquid Argon) and its fiducial mass, the beam power, the number of years that the experiment would be running in  $\nu$  and  $\bar{\nu}$  modes, and the references which have been followed in order to simulate each setup. It should be noted that the numbers quoted in this table correspond to the values stated in the cited references, where the beam power in each case has been computed according to a certain number of useful seconds per year (which in general do not coincide): T2K and T2HK assume 130 useful days per year ( $1.12 \times 10^7$  secs, approx.); NO $\nu$ A assumes  $1.7 \times 10^7$  sec $\times$ yr $^{-1}$ ; LBNE assumes  $2 \times 10^7$  sec $\times$ yr $^{-1}$ ; and SPL and C2P assume  $10^7$  sec $\times$ yr $^{-1}$ .

# Effect of th13 prior on CPV

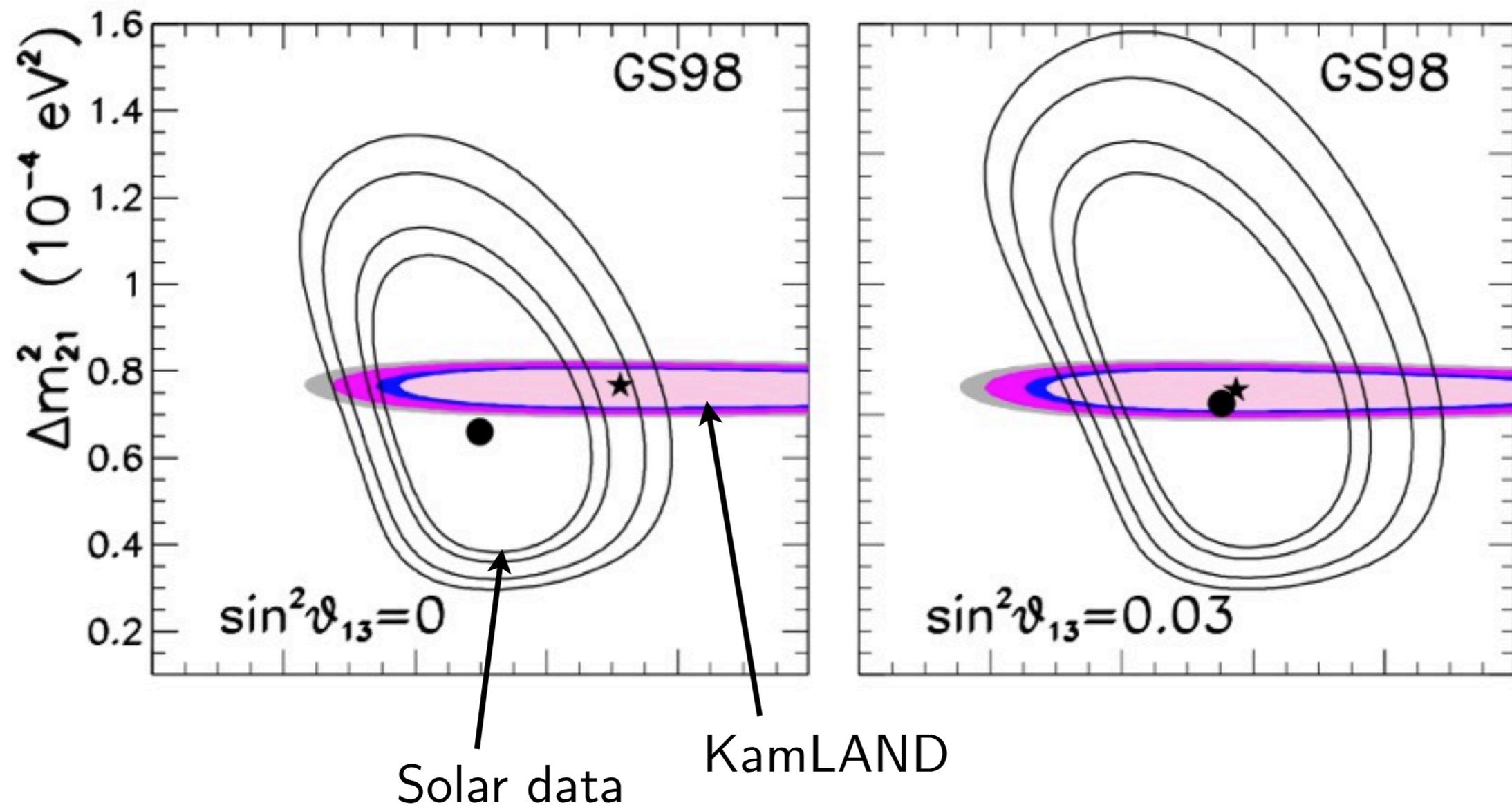


# Mass hierarchy and CPV

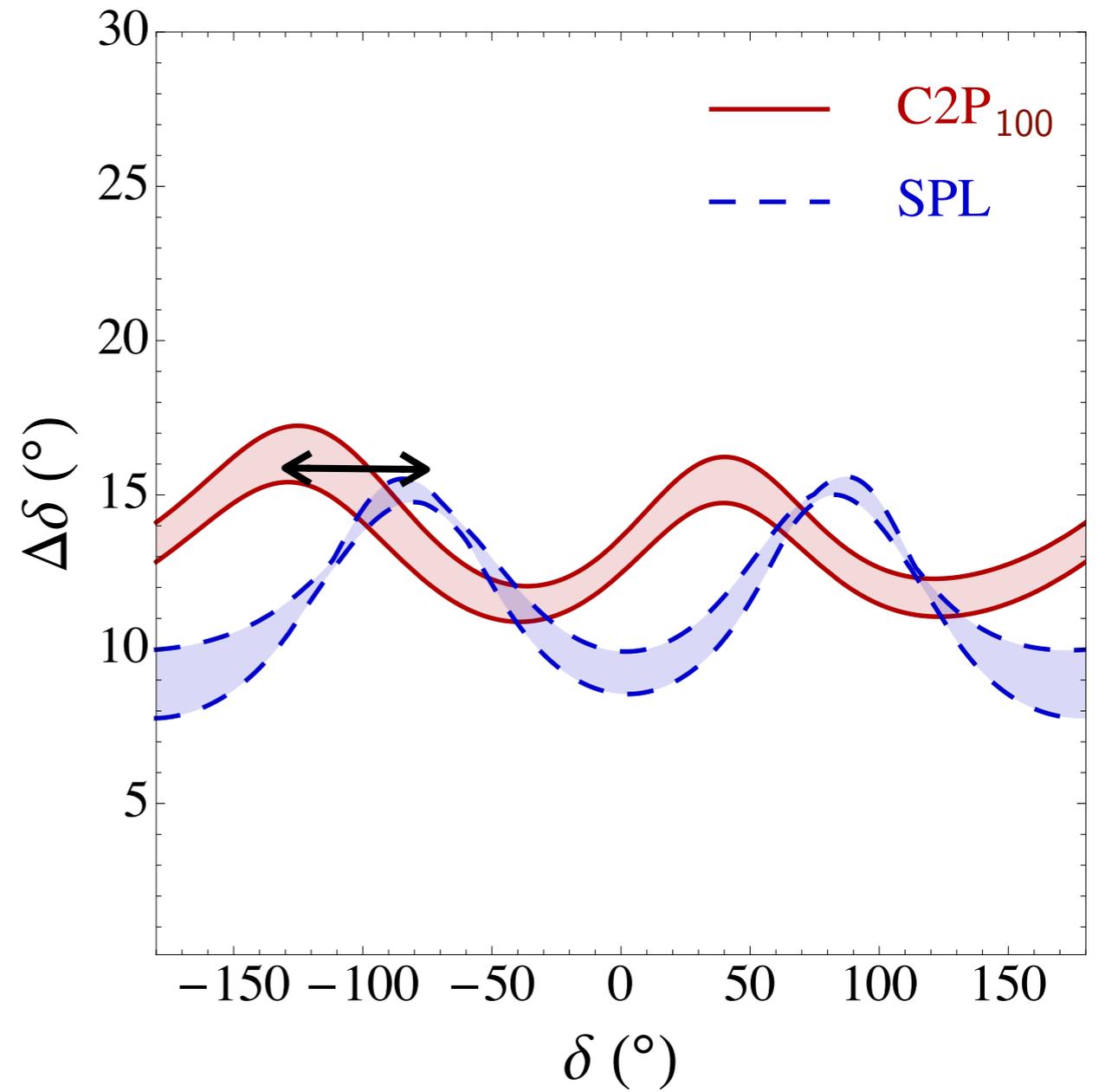
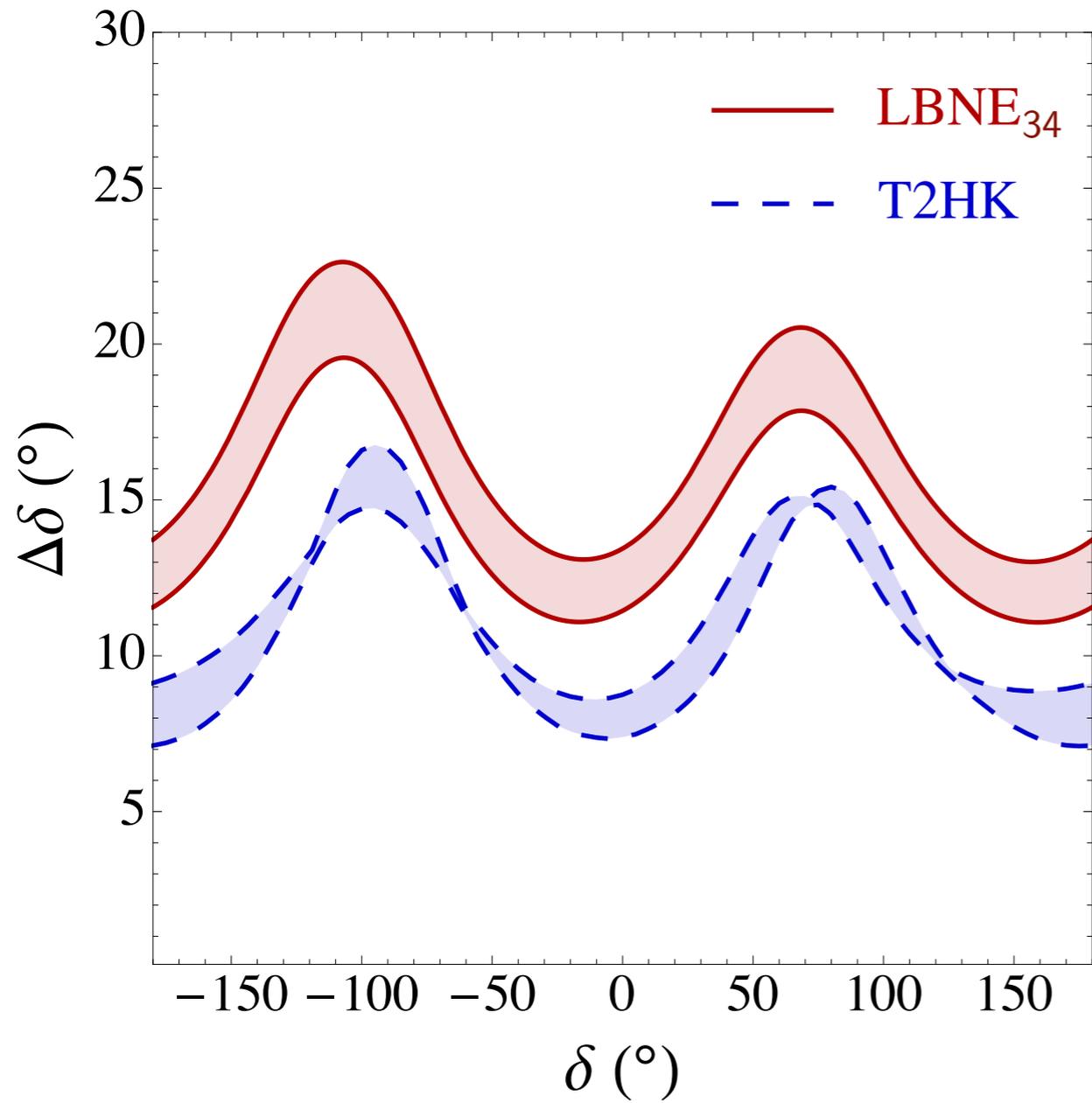


# Previous hints on $\theta_{13}$

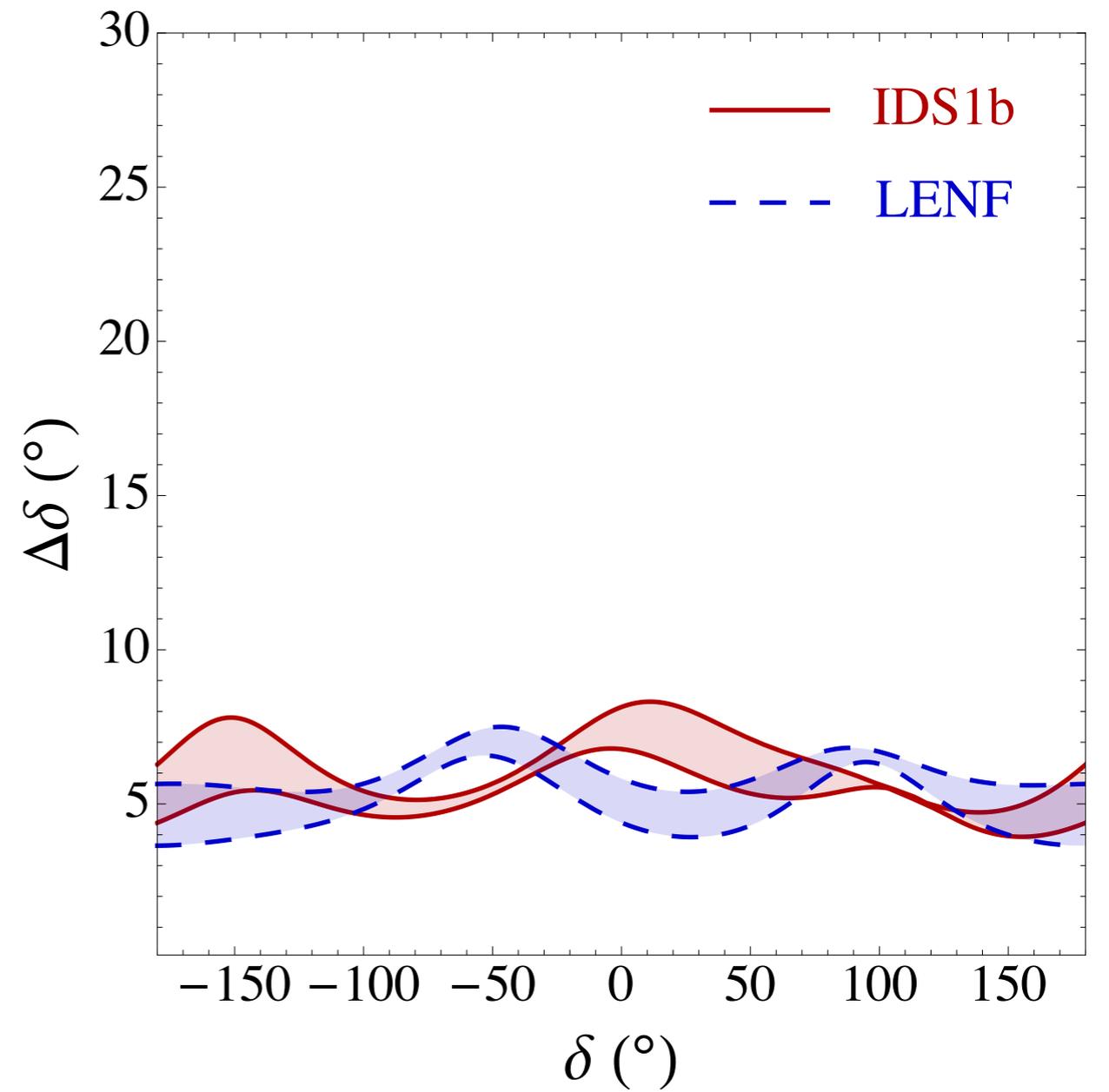
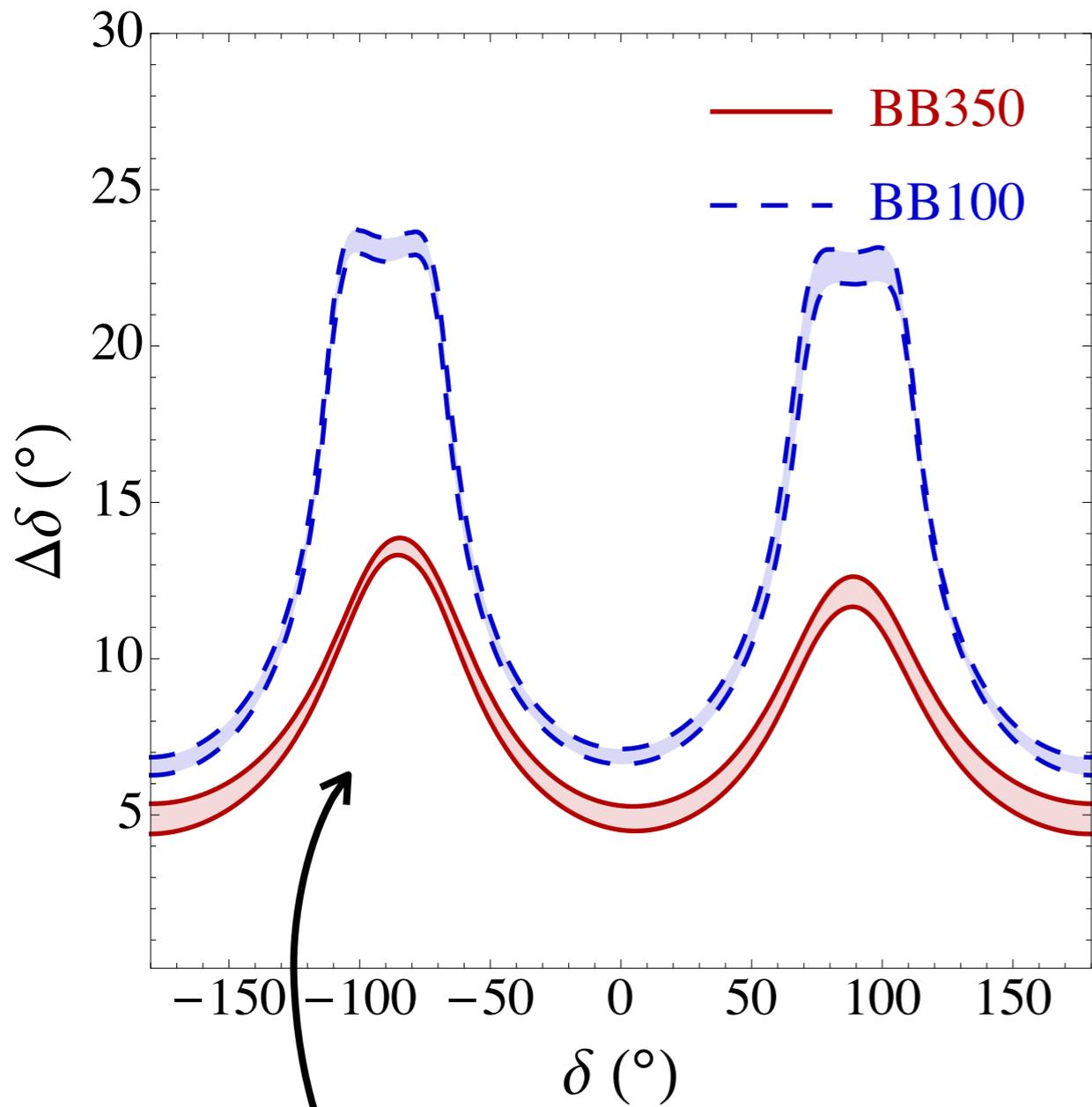
Previous hints from global fits pointed to nonzero  $\theta_{13}$ ...



# Precision in $\delta$



# Precision in $\delta$



BB in combination with T2K data

# The leptonic mixing matrix

Pontecorvo, 1957

Maki, Nakagawa, Sakata, 1962

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{Atmospheric}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}}_{\text{Interference}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{Solar}}$$

$$\Delta m_{31}^2 = 2.47 \times 10^{-3} \text{eV}^2$$

$$\sin^2 \theta_{23} = 0.386 \quad (\text{for NH})$$

$$\sin^2 \theta_{13} = 0.0241 \quad (\text{for NH})$$

$$\delta = 1.08\pi$$

$$\Delta m_{21}^2 = 7.54 \times 10^{-5} \text{eV}^2$$

$$\sin^2 \theta_{12} = 0.307$$

Fogli et al., 1205.5254 [hep-ph]  
(see also Forero et al, 1205.4018 [hep-ph])

# Precision at 2nd peak

