

# Search for $\mu$ -e Conversion : COMET at J-PARC

- Staging approach -

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International Workshop on Neutrino Factories, Super Beams and Beta Beams: NuFact2012  
July 23-28, 2012, Williamsburg, VA USA

25+5 min



# Outline

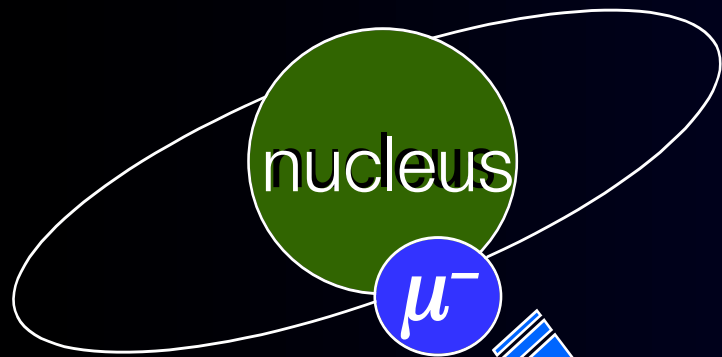
- Overview of  $\mu$ -e conversion
- COMET staging approach
- COMET Phase-I
- R&D progress
  - Results of extinction measurement
- Summary



# $\mu$ -e Conversion Search

- Two experiments are going to start to search for the  $\mu$ -e conversion process: COMET@J-PARC and Mu2e@FNAL.
- These are stopped muon experiments. When a  $\mu^-$  is stopped in a material, ...

1s state in a muonic atom



**Fates of the  $\mu^-$  within the SM**

muon decay in orbit

$$\mu^- \rightarrow e^- \nu \bar{\nu}$$

nuclear muon capture

$$\mu^- + (A, Z) \rightarrow \nu_\mu + (A, Z - 1)$$

## Beyond the SM

$$\mu^- + (A, Z) \rightarrow e^- + (A, Z)$$

**$\mu$ -e  
conversion**

Forbidden by the SM, because the lepton flavor is changed to  $\mu$ -flavor to e-flavor.

**Event signature :**

a single mono-energetic electron of 100MeV

## in the SM + $\nu$ masses

$\mu$ -e conversion can occur via  $\nu$ -mixing, but expected rate is well below the experimentally accessible range. Rate  $\sim O(10^{-54})$

**Discovery of the  $\mu$ -e conversion is a clear evidence of new physics beyond the SM.**

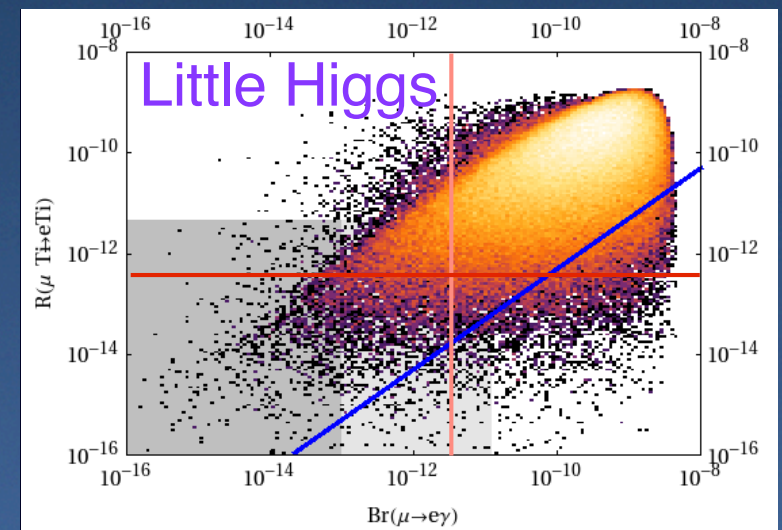
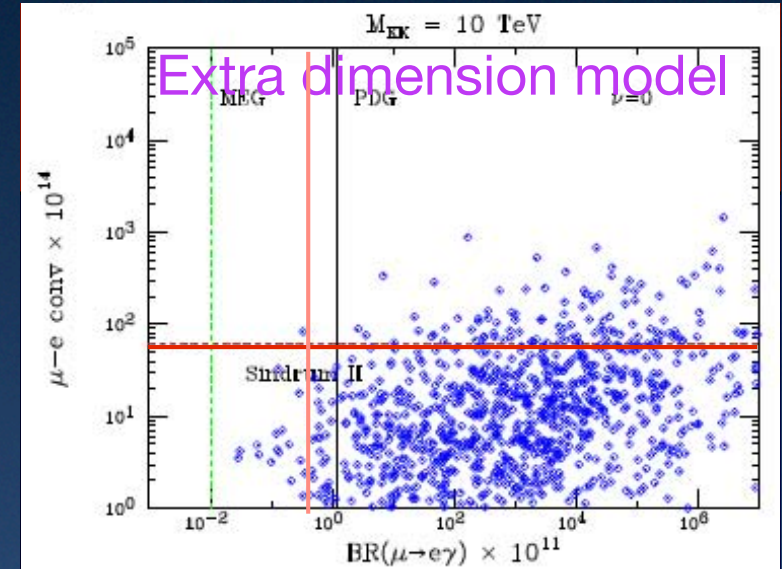
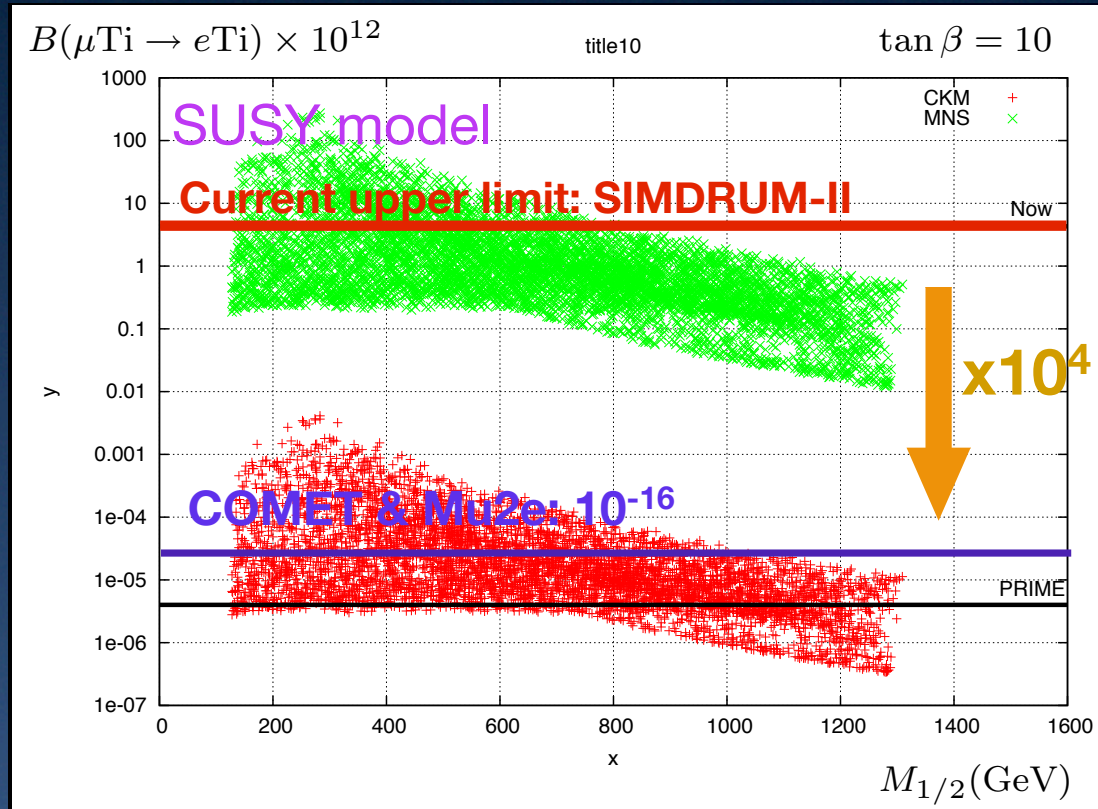
## in the SM + new physics

A wide variety of proposed extensions to the SM predict observable  $\mu$ -e conversion rate.



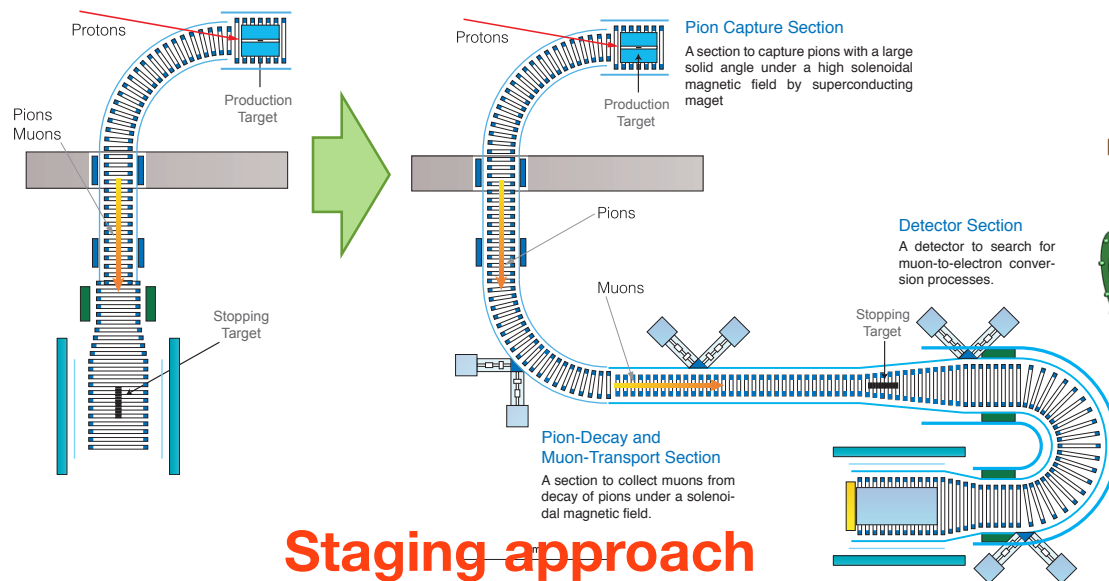
# $\mu$ -e Conversion Predictions

- Various beyond the SM models predict sizable  $\mu$ -e conversion.





# COMET @J-PARC



## Staging approach

### COMET Phase-I :

physics run 2017-

$BR(\mu+Al \rightarrow e+Al) < 7 \times 10^{-15} @ 90\%CL$

\*8GeV-3.2kW proton beam, 12 days

\*90deg. bend solenoid, cylindrical detector

\*Background study for the phase2

### COMET Phase-II :

physics run 2019-

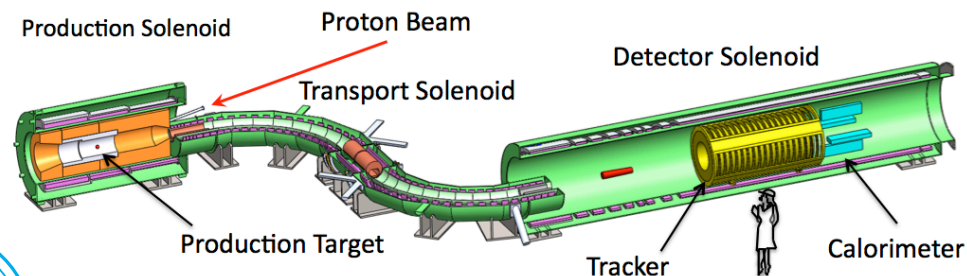
$BR(\mu+Al \rightarrow e+Al) < 6 \times 10^{-17} @ 90\%CL$

\*8GeV-56kW proton beam, 2 years

\*180deg. bend solenoid, bend spectrometer,

transverse tracker+calorimeter

# Mu2e @FNAL



### Mu2e :

physics run 2019-

$BR(\mu+Al \rightarrow e+Al) < 6 \times 10^{-17} @ 90\%CL$

\*8GeV-8kW proton beam, 3 years

\*2x90deg. S-shape bend solenoid,

straw tracker+calorimeter

a factor of 10,000 better sensitivity than the current upper limit (SINDRUM II)

### COMET Phase-I

#### has a strong endorsement from J-PARC

- "COMET is a high priority component for the J-PARC program." (KEK/J-PARC-PAC March/2012)
  - The IPNS proposed, as the first priority item in the next 5-year plan, to construct a proton beam line and the 1<sup>st</sup> half of solenoid magnets for COMET Phase-I. The PAC endorsed the laboratory plan.
- Proposal has been submitted to J-PARC PAC (July 2012)
- Construction will be started from 2013.

### COMET Phase-II

#### Stage-1 approved by J-PARC PAC in 2009.



# Status of COMET project

- We have submitted a LOI of a staging plan and a proposal of Phase-I to the J-PARC PAC.
  - **COMET Phase-I: A proposal has been submitted (July 2012)**
    - $B(\mu+Al \rightarrow e+Al) < 7 \times 10^{-15}$  @ 90%CL
      - 8GeV-3.2kW proton beam, 12 days
      - 90deg. bend solenoid, cylindrical detector
    - Background study for the phase2
  - **COMET Phase-II: Stage-1 approved (2009)**
    - $B(\mu+Al \rightarrow e+Al) < 6 \times 10^{-17}$  @ 90%CL
      - 8GeV-56kW proton beam, 2 years
      - 180deg. bend solenoid, bend spectrometer, transverse tracker+calorimeter
- After a discussion in the last PAC meeting (16-17, March, 2012), We got a strong recommendation from the J-PARC-PAC.
  - "COMET is a **high priority component for the J-PARC program.**" (KEK/J-PARC-PAC March/2012)
  - The IPNS proposed, as **the first priority item in the next 5-year plan**, to **construct** a proton beam line and the **1st half of solenoid magnets for COMET Phase-I**. The PAC endorsed the laboratory plan.
- **J-PARC plans to submit a budget request to the Ministry of Education, Culture, Sports, Science and Technology, the budget includes 20M-USD(1USD=100JPY) for the COMET-phase1.**
- **The construction will be started from 2013.**



# COMET Collaboration

## The COMET Collaboration

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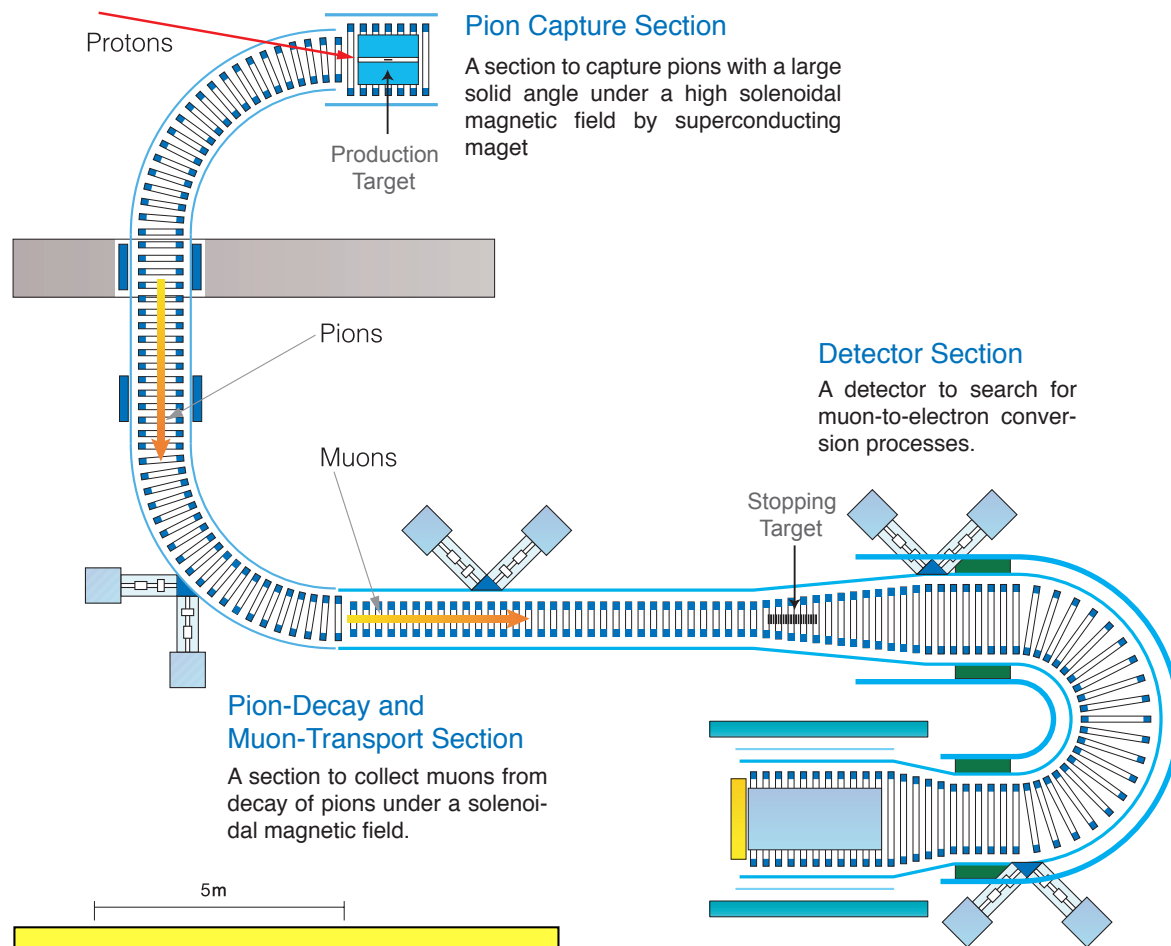
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109 collaborators  
25 institutes  
11 countries



# Key Points of COMET(S.E.S $10^{-17}$ )



## COMET Phase-II :

physics run 2019-

$BR(\mu + Al \rightarrow e + Al) < 6 \times 10^{-17}$  @ 90%CL

\*8GeV-56kW proton beam, 2 years

\*180deg. bend solenoid, bend spectrometer,  
transverse tracker+calorimeter

Details in  
a NuFact09 talk by A. Sato

## Intense Pulsed Proton Beam

8GeV-56kW ( $2 \times 10^7$  sec)

width~100ns, separation>1 $\mu$ s

Extinction level <  $10^9$  **reduce beam related BG**

## Pion Capture Solenoid

5T superconducting  **$10^{11}$   $\mu$ /sec**

## Long Transport Solenoid

L >10m

Curved 180deg Solenoid **eliminate energetic  $\mu$  (>75 MeV/c) and pions**

## Thin Stopping Target

Al 200 $\mu$ m x 17

**improve  $e^-$  energy resolution**

## Electron Spectrometer

Curved Solenoid

**reduce detector hit rate**

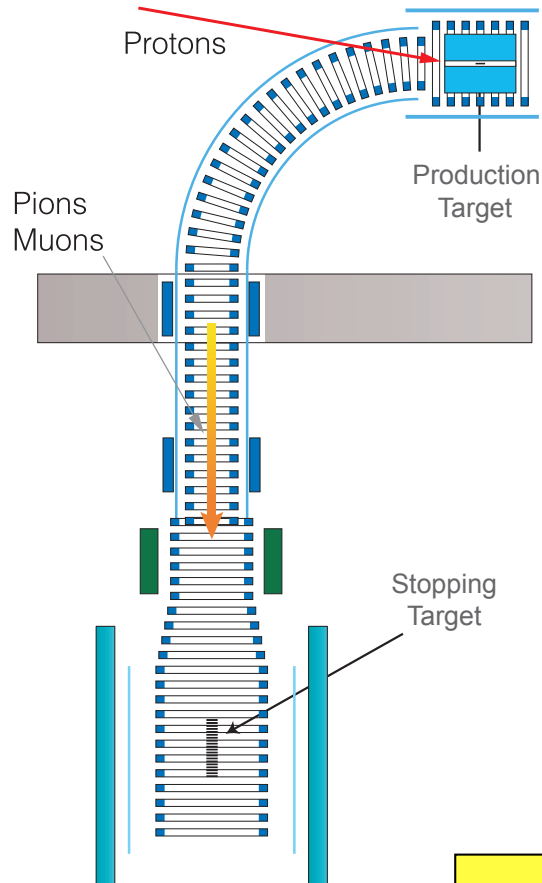
## Low-mass Tracker

Straw chamber  
in Vacuum

**improve  $e^-$  energy resolution**



# Key Points of COMET(S.E.S $10^{-17}$ )



## COMET Phase-I :

physics run 2017-

$BR(\mu + Al \rightarrow e + Al) < 7 \times 10^{-15}$  @ 90%CL

\*8GeV-3.2kW proton beam, 12 days

\*90deg. bend solenoid, cylindrical detector

\*Background study for the phase2

## Intense Pulsed Proton Beam

8GeV-3.2kW (12 days)

width~100ns, separation>1 $\mu$ s

Extinction level <  $10^9$  **reduce beam related BG**

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## Electron Spectrometer

Curved Solenoid

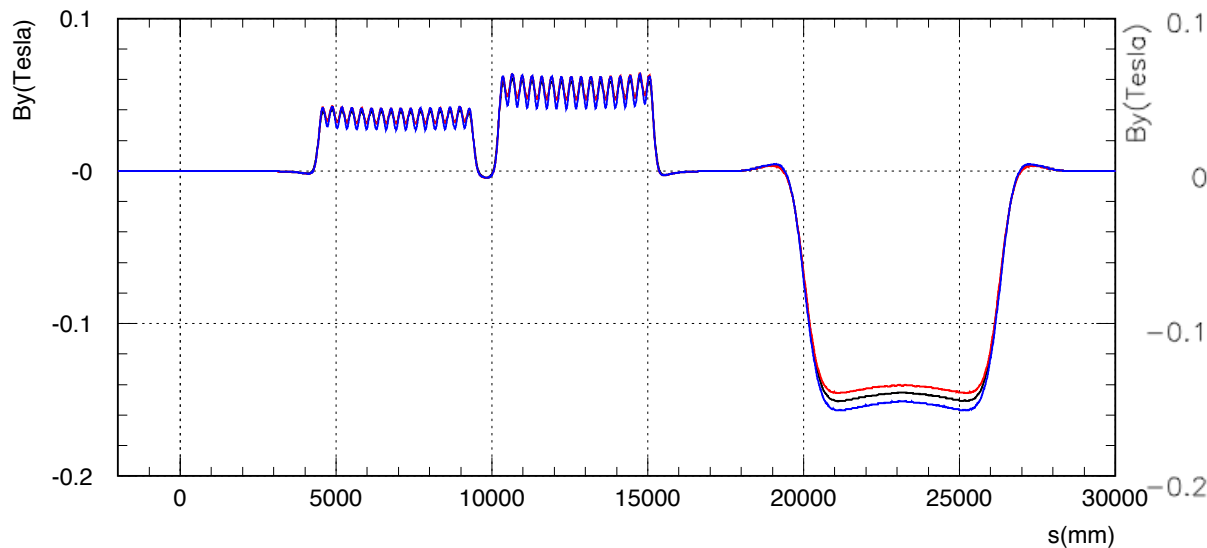
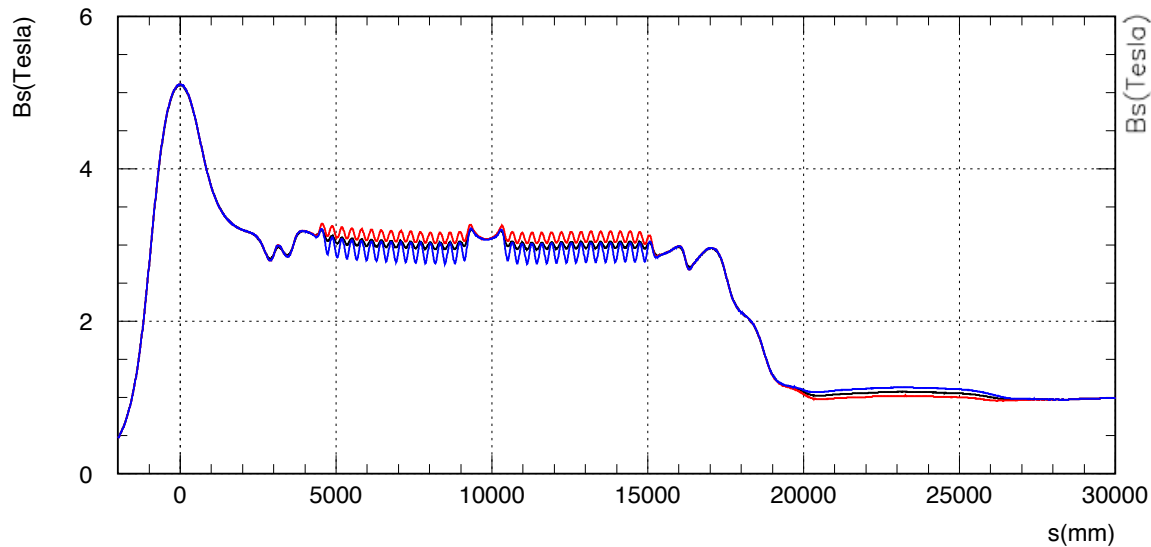
## Low-mass Tracker

Cylindrical drift chamber

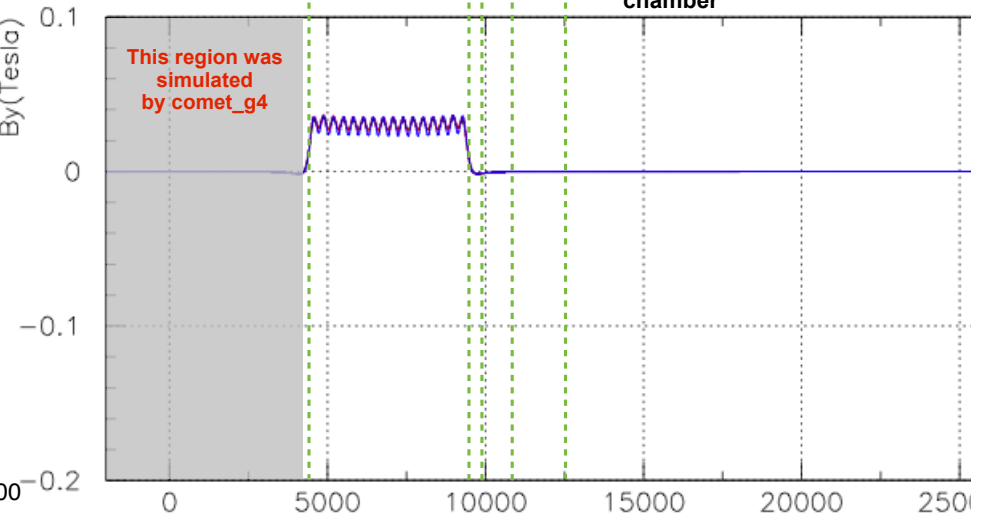
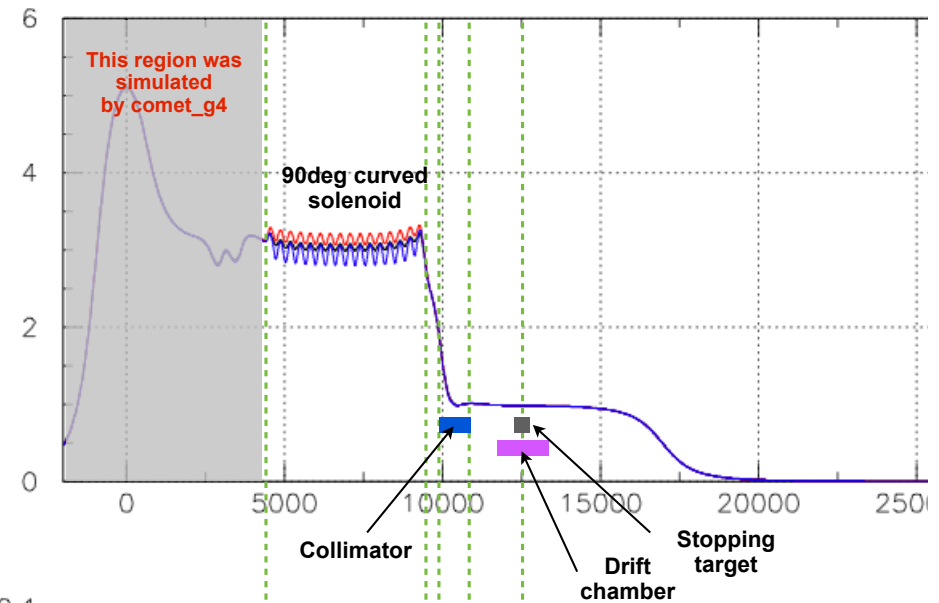


# Magnetic Fields

## COMET Phase-II



## COMET Phase-I





# COMET Phase-I Overview

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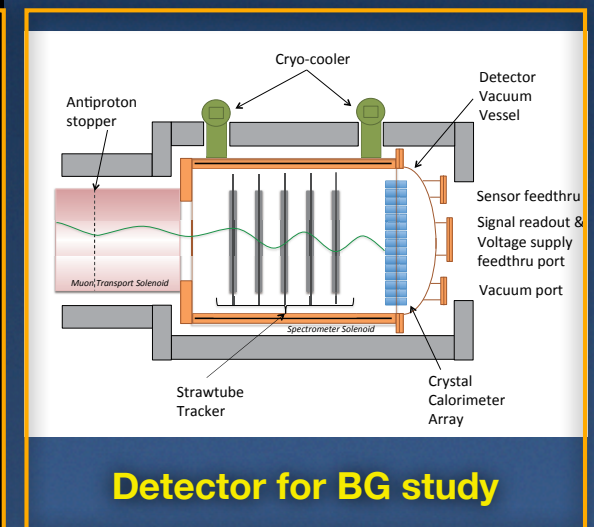
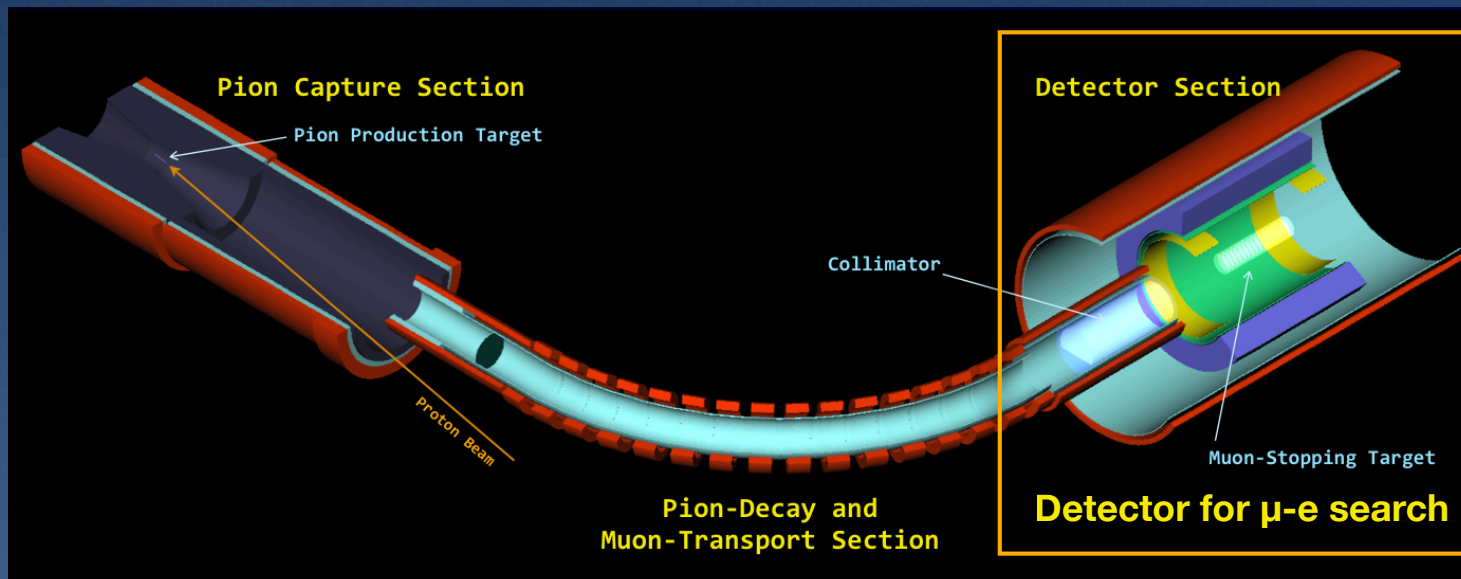
# Goal of COMET Phase-I

- **Background Study for COMET Phase-II**

- direct measurement of potential background sources for the full COMET experiment by using the actual COMET beamline constructed at Phase-I

- **Search for  $\mu$ -e conversion**

- a search for  $\mu^- - e^-$  conversion at intermediate sensitivity which would be more than 100 times better than the SINDRUM-II limit

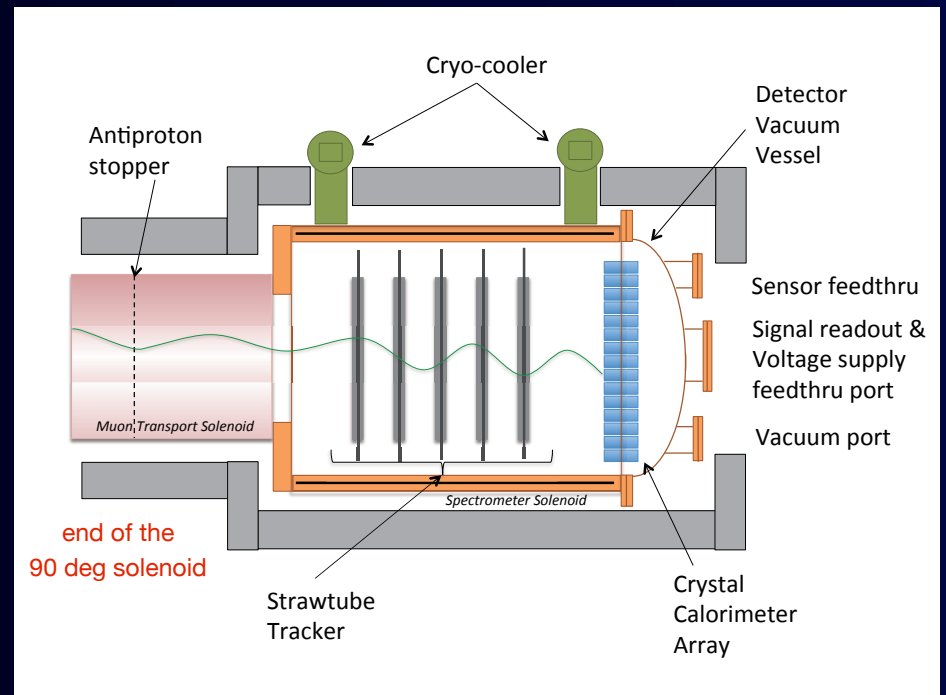




# Background Study

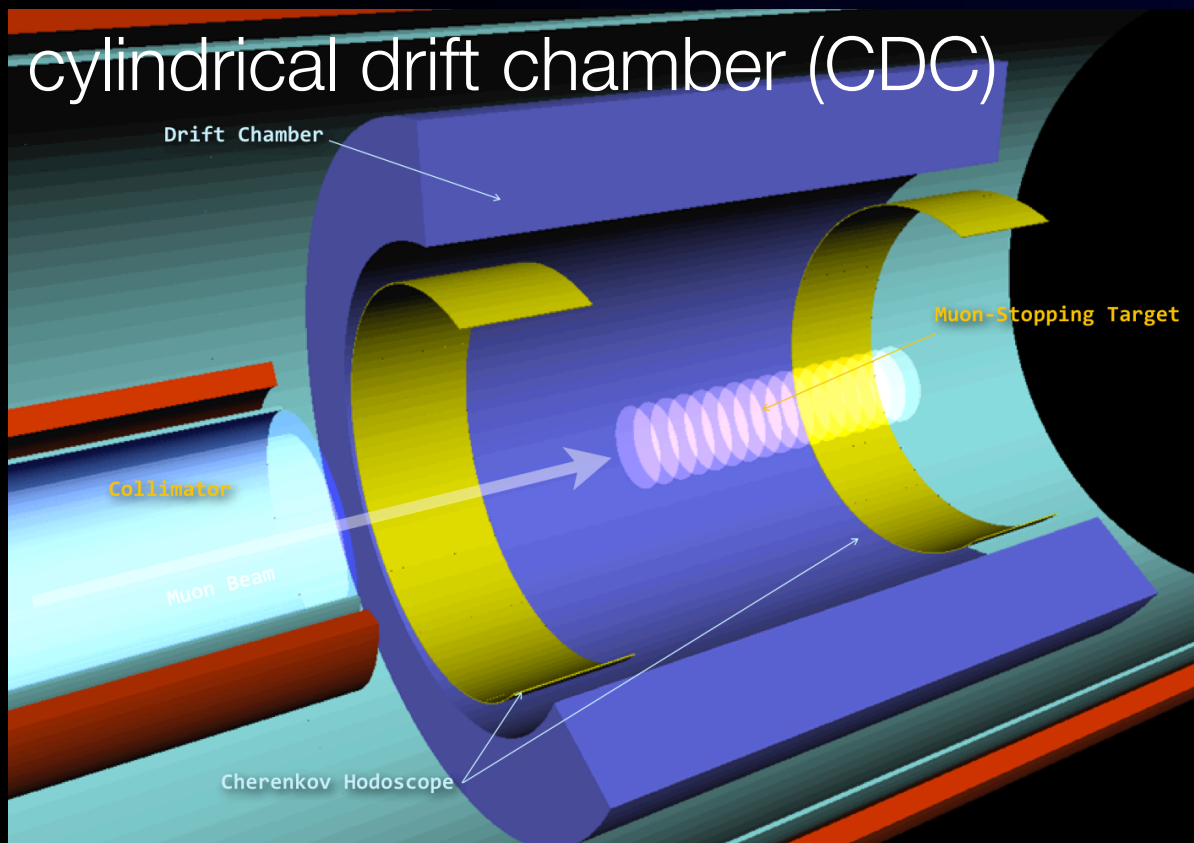
- measure almost all background schematic layout
- sources
  - muons, pions, electrons, neutrons, antiprotons, photons
- same detector technology used in COMET Phase-II
  - SC spectrometer solenoid
  - straw tube transverse tracker
  - crystal calorimeter
- particle ID with  $dE/dX$  and  $E/P$

## schematic layout



aim to know the known BG &  
aim to know the unknown BG

# Search for $\mu$ -e conversion at Intermediate Sensitivity (CDC case)



## Design Philosophy

by keeping an open end in a solenoid geometry, beam particles continue downstream and escape the detector.

- CDC design is based on Belle II CDC (small cell part)
- **Design difference (from LOI)**
  - He:C<sub>2</sub>H<sub>6</sub> (=50:50) gas
  - trigger counters at the both ends (smaller acceptance)
  - no proton absorber
- **CDC hit rates**
  - 40 kHz/wire at the innermost layer by proton emission from muon capture (0.15 per capture)
- **CDC trigger rate**
  - 270 Hz from DIO



# S.E.S. for COMET Phase-I

- Single event sensitivity

$$B(\mu^- + Al \rightarrow e^- + Al) \sim \frac{1}{N_\mu \cdot f_{cap} \cdot A_e},$$

- $N_\mu$  is a number of stopping muons in the muon stopping target. It is  $8.7 \times 10^{15}$  muons.
- $5.8 \times 10^9$  stopped  $\mu$ /s with 3 kW proton beam power, with  $1.5 \times 10^6$  sec running.
- $f_{cap}$  is a fraction of muon capture, which is 0.6 for aluminum.
- $A_e$  is the detector acceptance, which is 0.06.

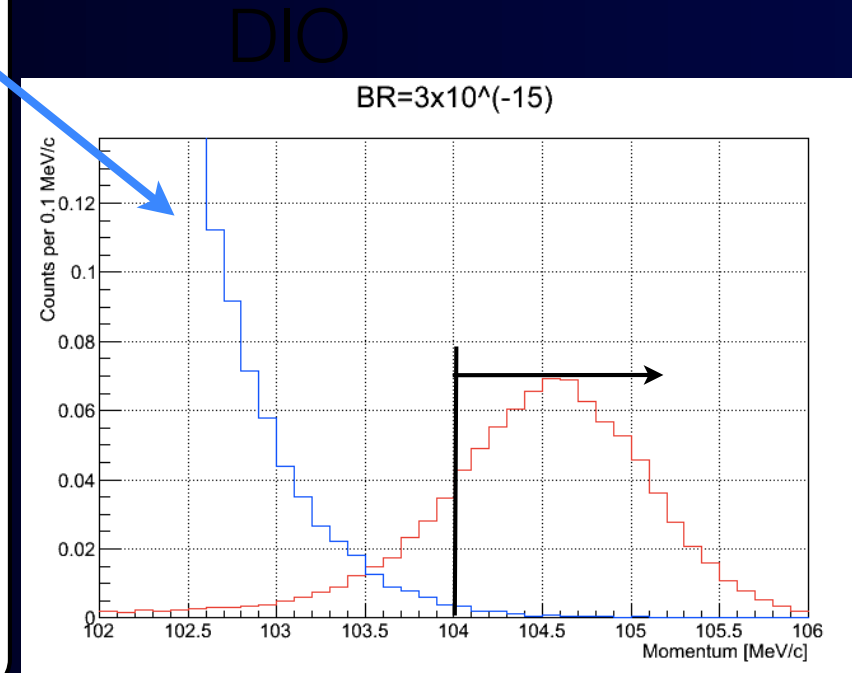
Event selection	Value	Comments
Geometrical acceptance	0.24	tracking efficiency included
Momentum selection	0.74	$104.1 \text{ MeV}/c < P_e < 106 \text{ MeV}/c$
Timing selection	0.39	same as COMET
Trigger and DAQ	0.9	same as COMET
Total	0.06	

$$B(\mu^- + Al \rightarrow e^- + Al) = 3.1 \times 10^{-15}$$

$$B(\mu^- + Al \rightarrow e^- + Al) < 7 \times 10^{-15} \quad (90\% C.L.)$$

# Backgrounds for COMET Phase-I

Background	estimated events
Muon decay in orbit	0.01
Radiative muon capture	< 0.001
Neutron emission after muon capture	< 0.001
Charged particle emission after muon capture	< 0.001
Radiative pion capture	0.0096*
Beam electrons	< 0.00048*
Muon decay in flight	
Pion decay in flight	
Neutron induced background	$\sim 0^*$
Delayed radiative pion capture	0.002
Anti-proton induced backgrounds	0.007
Electrons from cosmic ray muons	< 0.0002
Total	0.03



with proton extinction factor of  $3 \times 10^{-11}$

Expected BG events are about 0.03 at S.E.S. of  $3 \times 10^{-15}$ .



# R&D for COMET

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# R&Ds

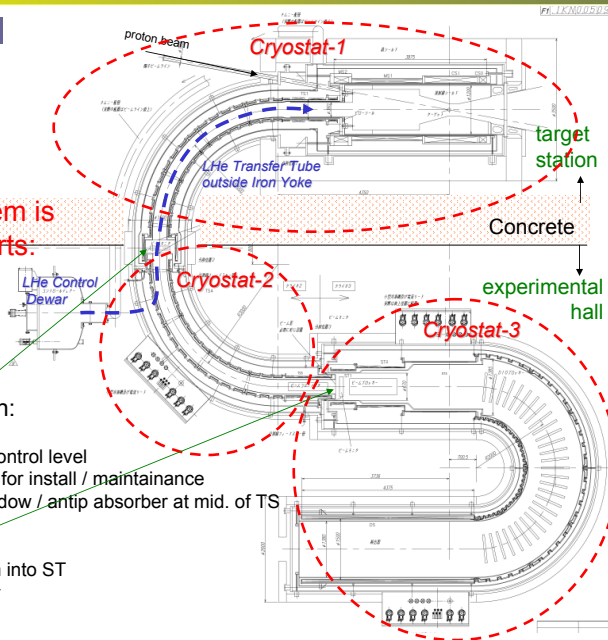
## COMET Magnet Design

The magnet system is separated in 3 parts:

- Cryostat-1: CS+UpstreamTS
- Cryostat-2: DownstreamTS
- Cryostat-3: ST+SS+DS

Purpose of separation:

- At concrete wall
  - Different radiation control level
  - Movable Cryostat-2 for install / maintenance
  - Vac. separation window / antip absorber at mid. of TS
  - Beam monitors
- At stopping target
  - inject electron beam into ST
  - Muon beam monitor



## ROESTI Prototype I

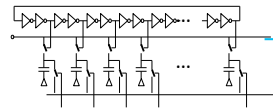
### Specifications

Front-end: ASD  
(Developed for Belle)

- 1pC  $\rightarrow$  1V
- 8ch/1chip

Analog Memory (Wave Form Sampling): DRS4

- 1024 Switching capacitor array
- 0.7-5 GSPS
- 8ch/1chip



Signal from Straw

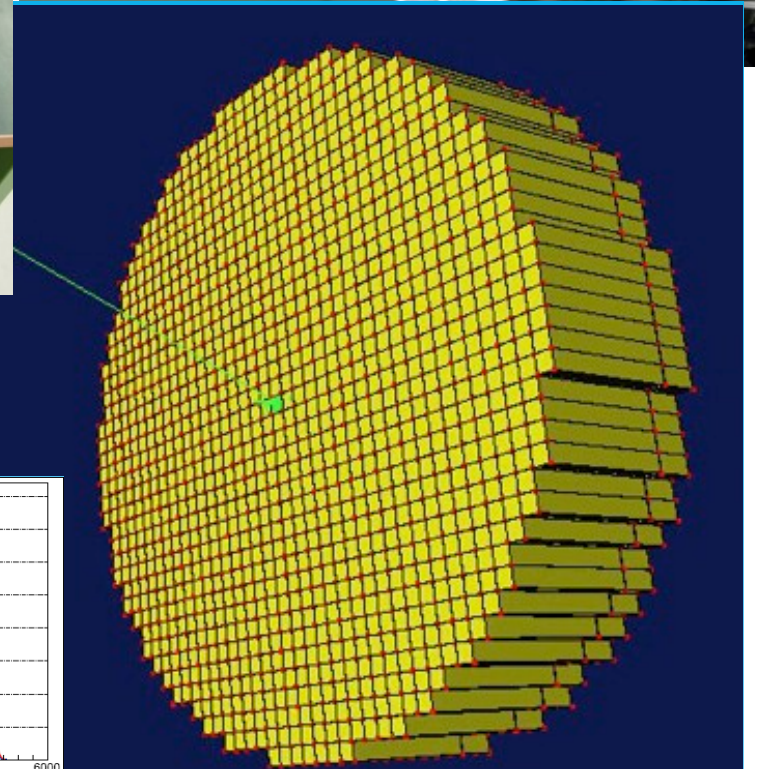
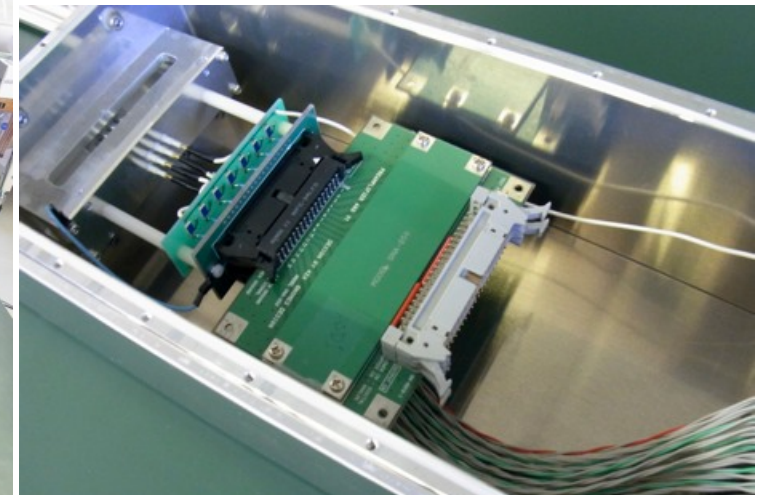
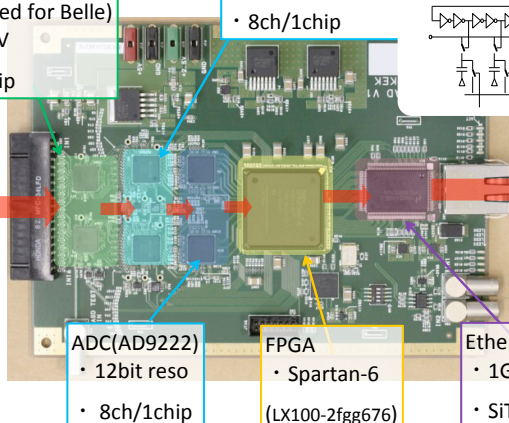
Ethernet

16ch/board

ADC(AD9222)  
• 12bit reso  
• 8ch/1chip

FPGA  
• Spartan-6  
(LX100-2fgg676)

Ether Net  
• 1G bit/sec  
• SiTCP





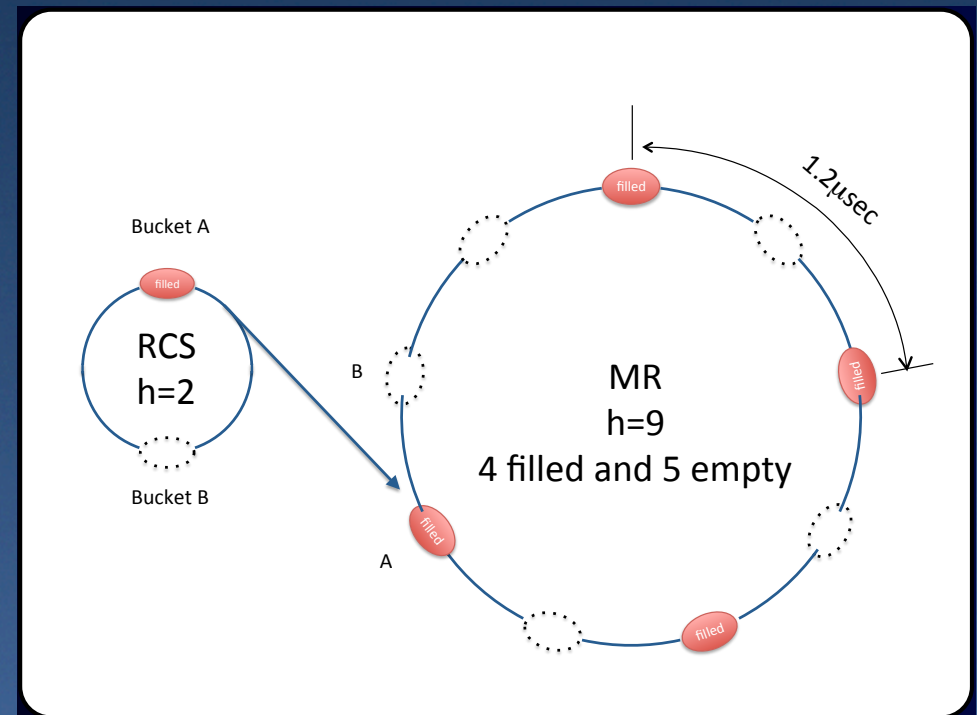
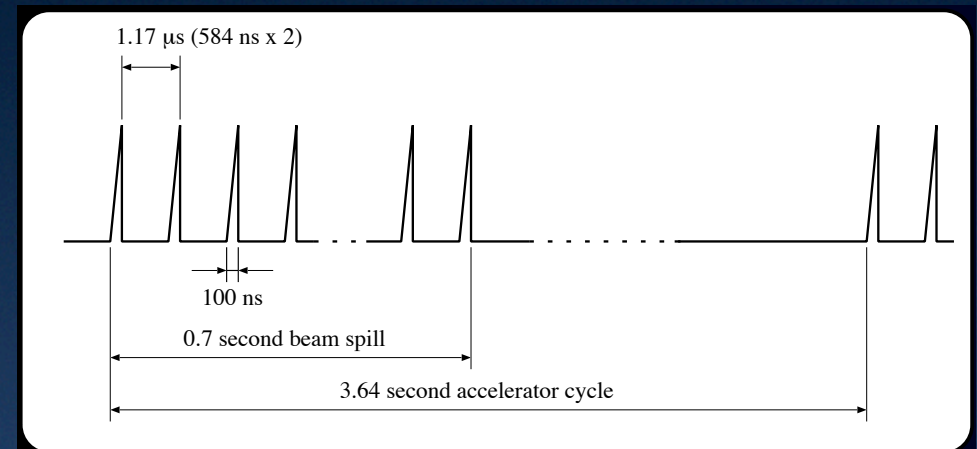
# **Extinction Measurements at J-PARC MR**

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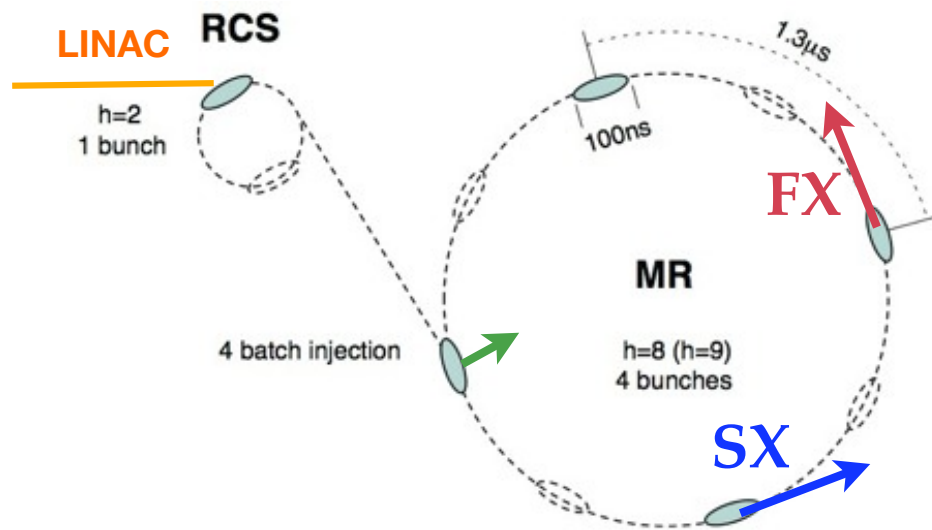
# Pulsed Proton Beam at J-PARC

- A pulsed proton beam is needed to reject beam-related prompt background.
- Time structure required for proton beams:
  - Pulse separation is  $\sim 1\mu\text{sec}$  or more (muon lifetime).
  - Narrow pulse width ( $<100\text{ nsec}$ )
- Pulsed beam from slow extraction.
  - fill every other RF buckets with protons and make slow extraction applying the RF.
  - spill length (flat top)  $\sim 0.7$
- Extinction level is very important!

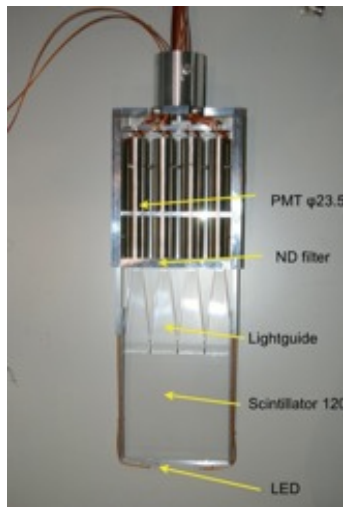




# Available Two Measurements

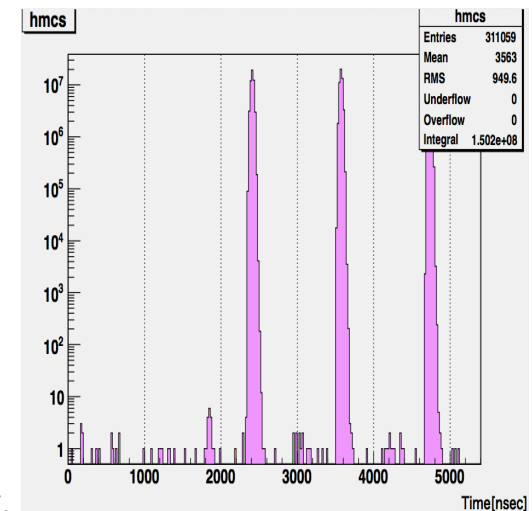


- ❖ FX : Fast Extraction for Neutrino beam
- ❖ Abort monitor is installed in front of the beam dump to measure extinction
- ❖ SX : Slow Extraction for Hadron hall
- ❖ By measuring the secondary beam, extinction at hadron hall is measured



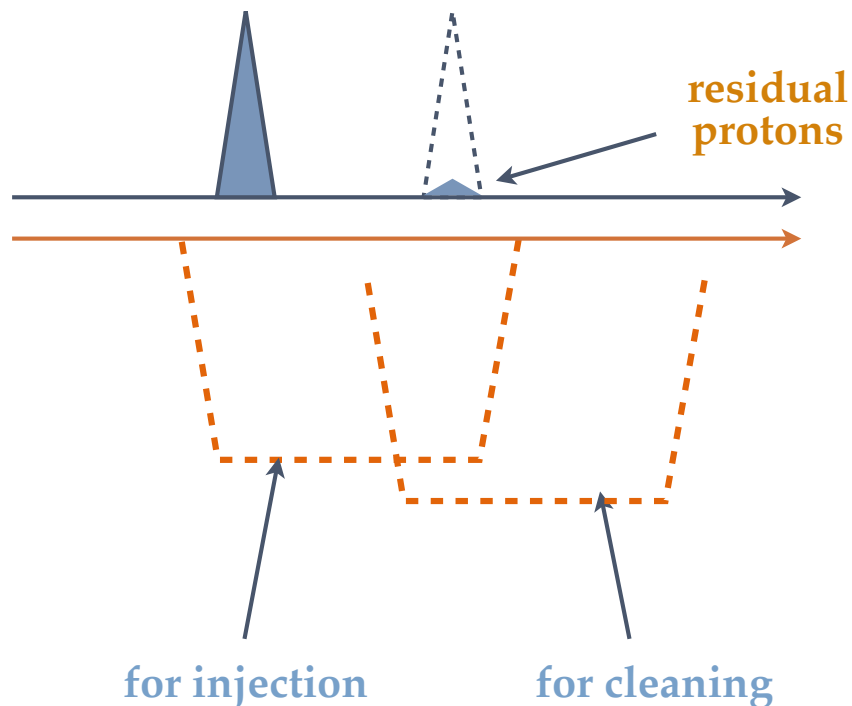
- Last measurement
  - 2010-Dec., @ FX abort line
  - Result:
    - Ext.  $< \sim O(-7)$
- In addition, **double kick injection** method was demonstrated to achieve the required extinction level.

- Last measurement
  - 2010-Oct., @ SX
  - Result:
    - Ext.  $< 5.4 \times 10^{-7}$
- w/o any treatment to improve extinction
- Consistent with measurement at abort.



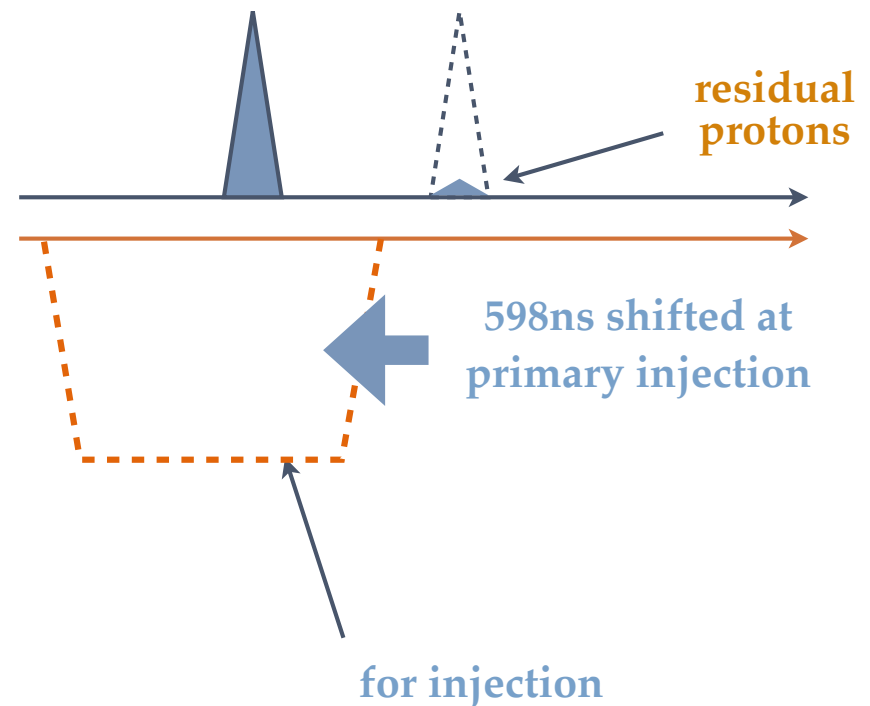
# Injection from RCS to the MR

## \* Double kick injection



- \* Residual protons are swept away by the secondary kicking which is shifted by  $1/2$  phase (598ns).
- \* Not realistic, Need big modification on accelerator (RCS kicker, Injector for MR)

## \* Single bunch kick injection **New**



- \* By shifting the kicker timing 598ns forward/backward, residual protons are originally not injected into MR.
- \* Completely empty bucket should be realized !



# Results

chopper

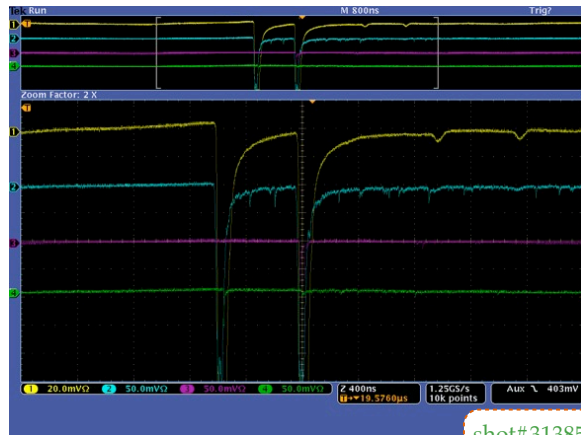
kicker

All beam chopped at LINAC

with filled buckets

## Double bunch kick

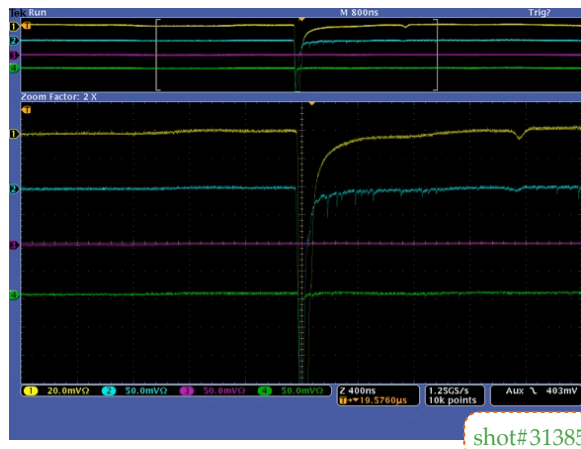
\* "all chop", w/o kicker-timing shift



(!) macro pulse width is 0.5ms, thus number of residual protons are 5 times more than before.

## Single bunch kick

\* all chop, kicker shifted by 1/2 backward



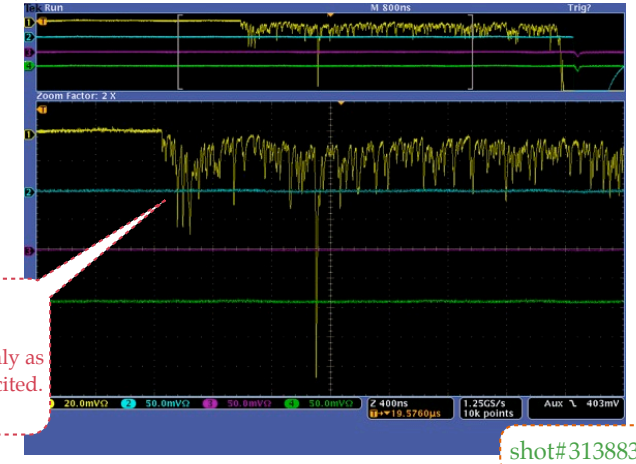
proton leakage after acceleration

$1.7 \times 10^{10}$  proton, Kicker timing is shifted by 1.8μsec (≈1.5 phase)

RF=16kV

many proton leakage

Residuals are distributed uniformly as long as kicker is excited.

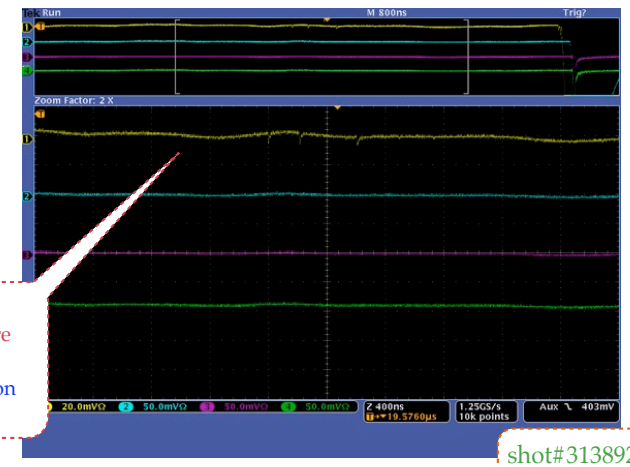


Kicker timing is shifted by 1.8μsec (≈1.5 phase)

RF=260kV

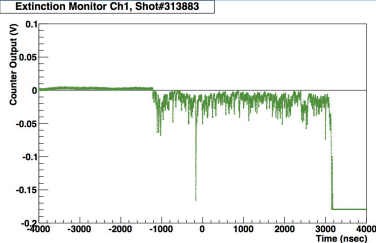
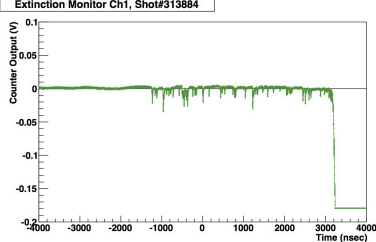
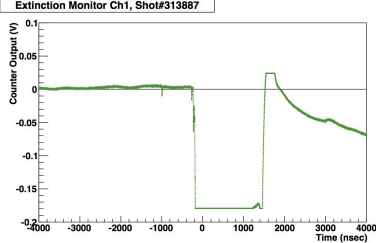
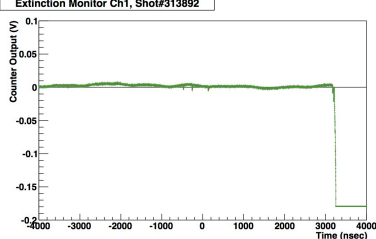
only 3 protons observed

Three protons are remained.  
Limit of Extinction



Single bunch kick

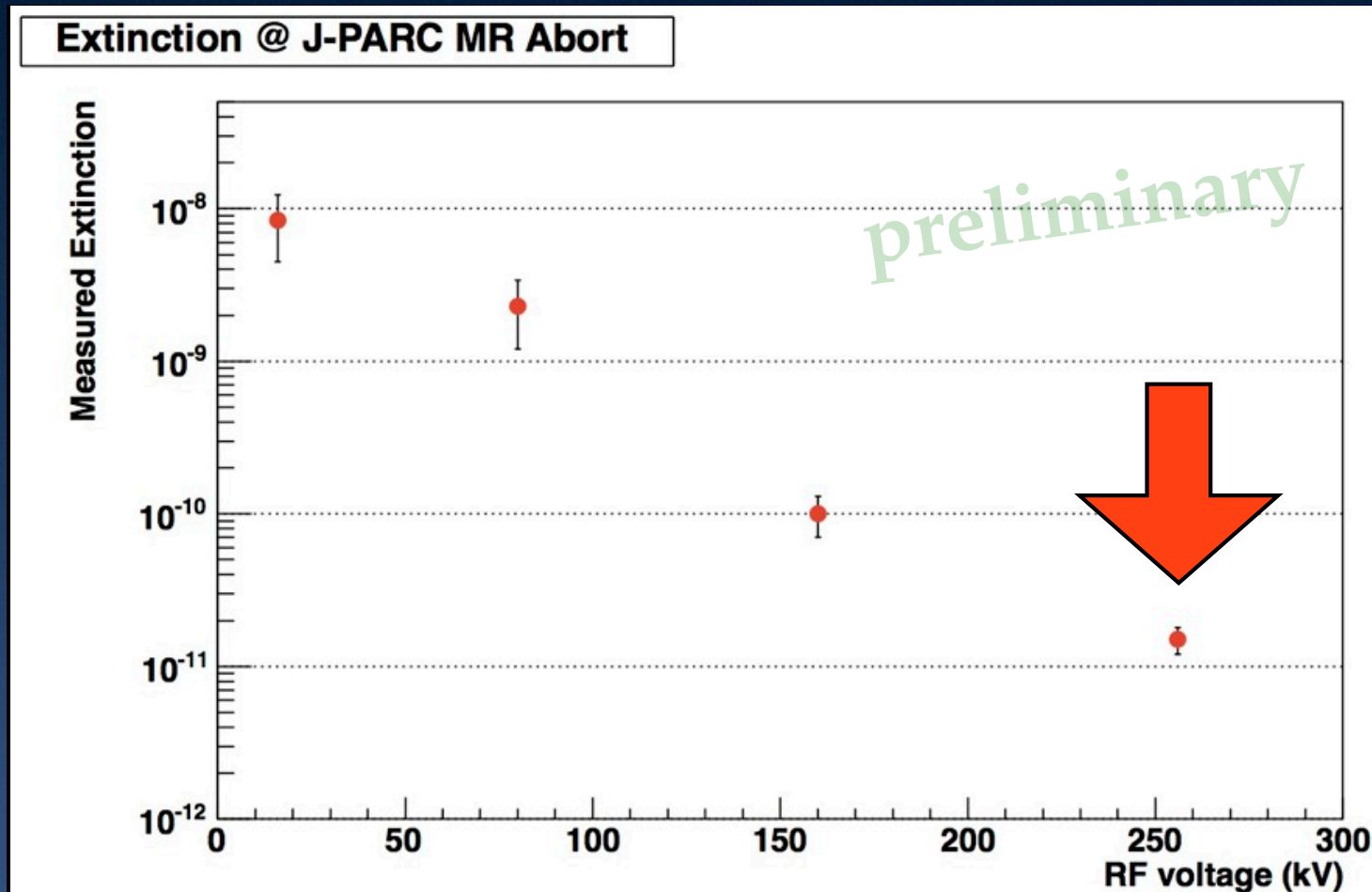
# Results of Extinction Measurement

Beam Condition	Tuned Intensity	Abort Monitor Output	# of Residual Protons (between bunches)	Extinction
<b>shot# 313883</b> macro pulse <b>0.1ms</b> , chop width <b>25ns</b> , thinner <b>3/32</b> , kicker delayed <b>1.8μs</b> , RF <b>16kV</b>	$1.7 \times 10^{10}$ protons		$142.3 \pm 19$	$8.4 \times 10^{-9}$
<b>shot# 313884</b> macro pulse <b>0.1ms</b> , chop width <b>25ns</b> , thinner <b>3/32</b> , kicker delayed <b>1.8μs</b> , RF <b>80kV</b>	$1.7 \times 10^{10}$ protons		$38.8 \pm 21$	$2.3 \times 10^{-9}$
<b>shot# 313887</b> macro pulse <b>0.1ms</b> , chop width <b>25ns</b> , thinner <b>32/32</b> , kicker delayed <b>0.6μs</b> , RF <b>160kV</b>	$1.0 \times 10^{11}$ protons		$10 \pm 0.3$	$1.0 \times 10^{-10}$
<b>shot# 313892</b> macro pulse <b>0.1ms</b> , chop width <b>25ns</b> , thinner <b>32/32</b> , kicker delayed <b>1.8μs</b> , RF <b>256kV</b>	$1.0 \times 10^{11}$ protons		$1.5 \pm 0.3$	$1.5 \times 10^{-11}$

(Estimated error is **very preliminary**, need DCCT calibration and systematics estimation)



# Results of Extinction Measurement (June, 2012)

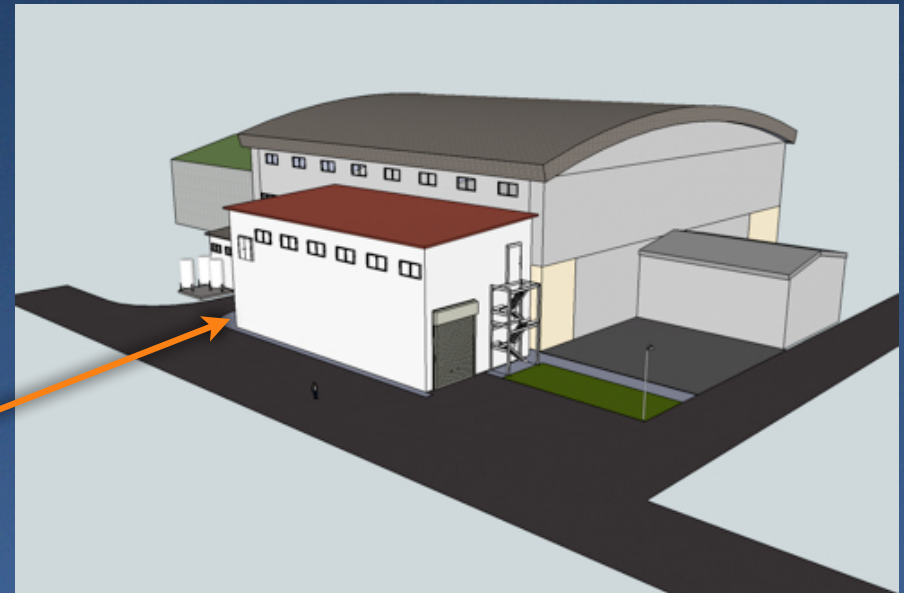
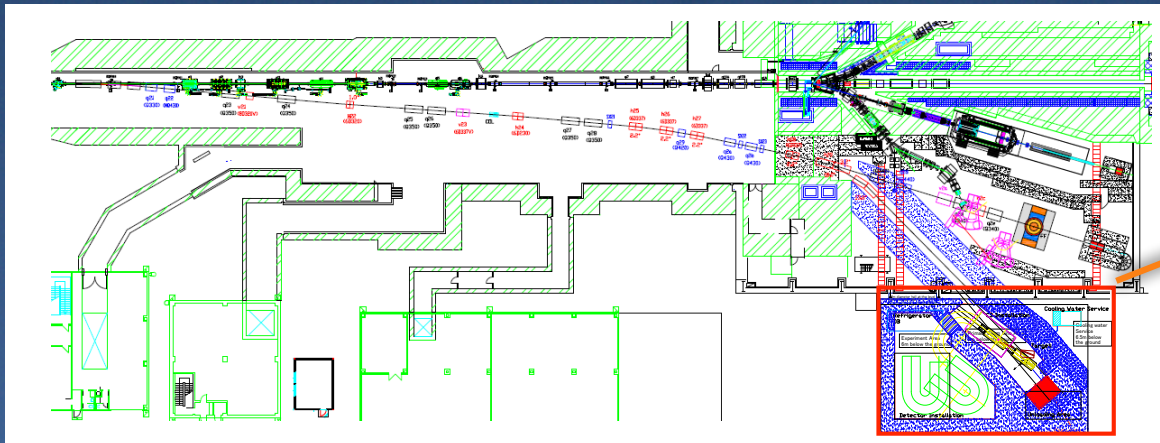
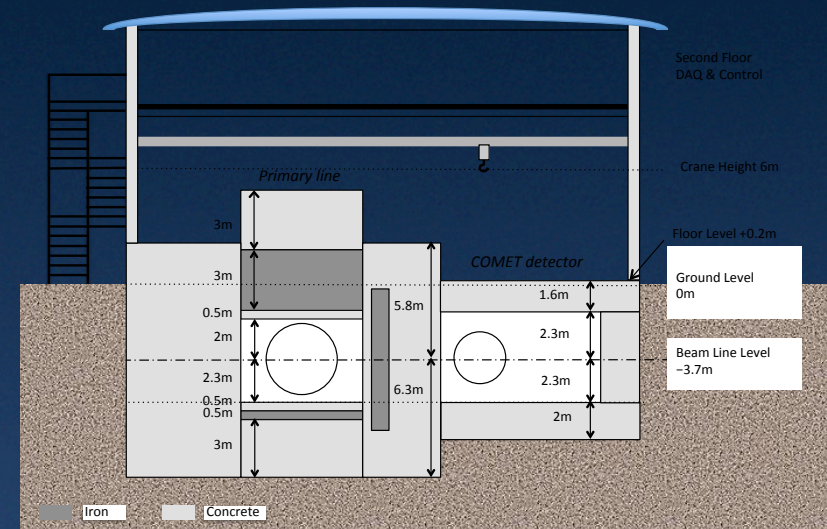


- proton extinction factor of  $1.5 \times 10^{-11}$  has been achieved.
  - at MR abort line after acceleration up to 30GeV.
- Next step: measurements at SX line.



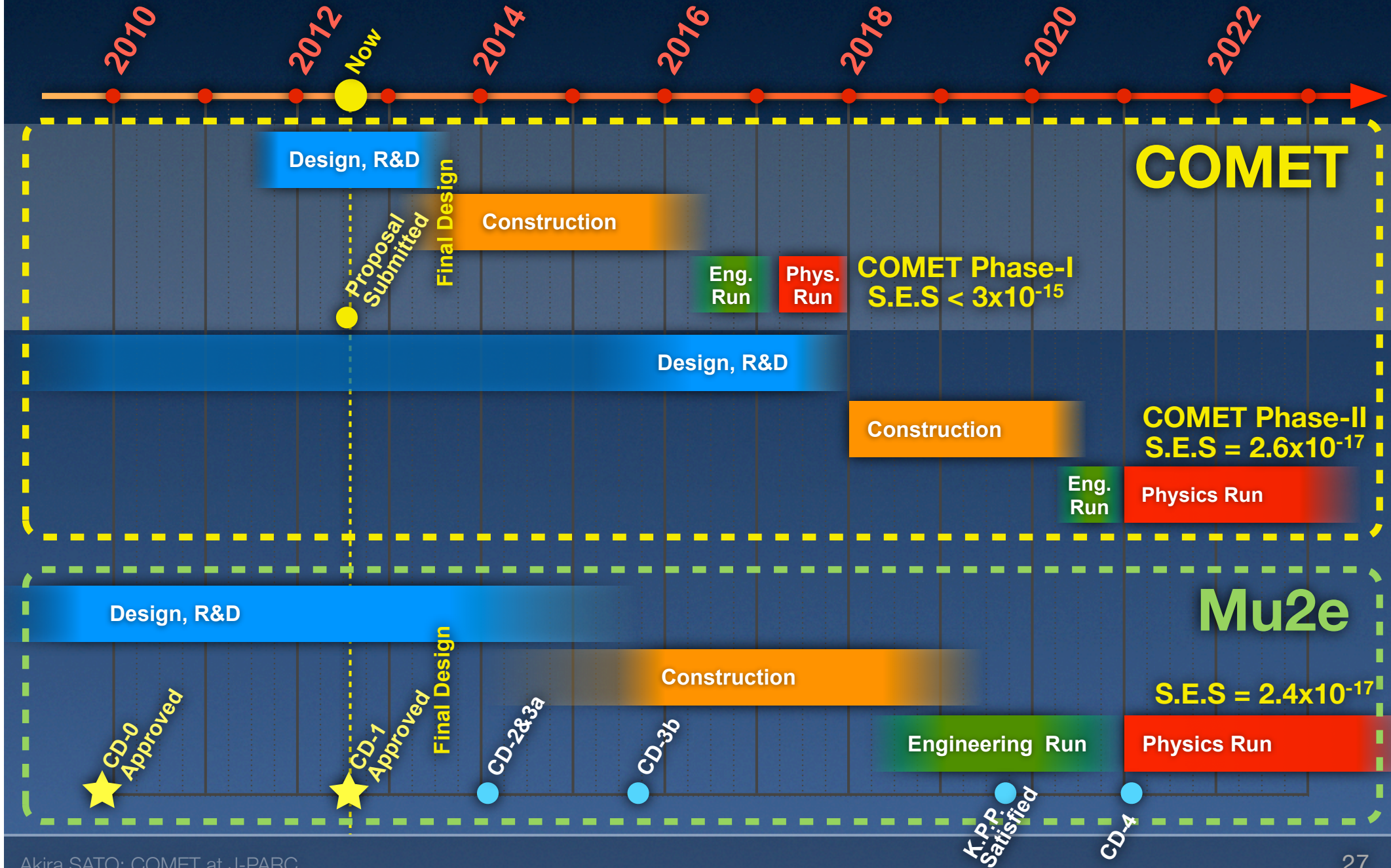
# Facility Construction

- Design work is in progress
  - Primary proton beam area, and beam line
  - Experimental area
- Ground floor for service/power supply/refrigerator
- Compressor will be installed in a separate building





# Schedule of COMET and Mu2e





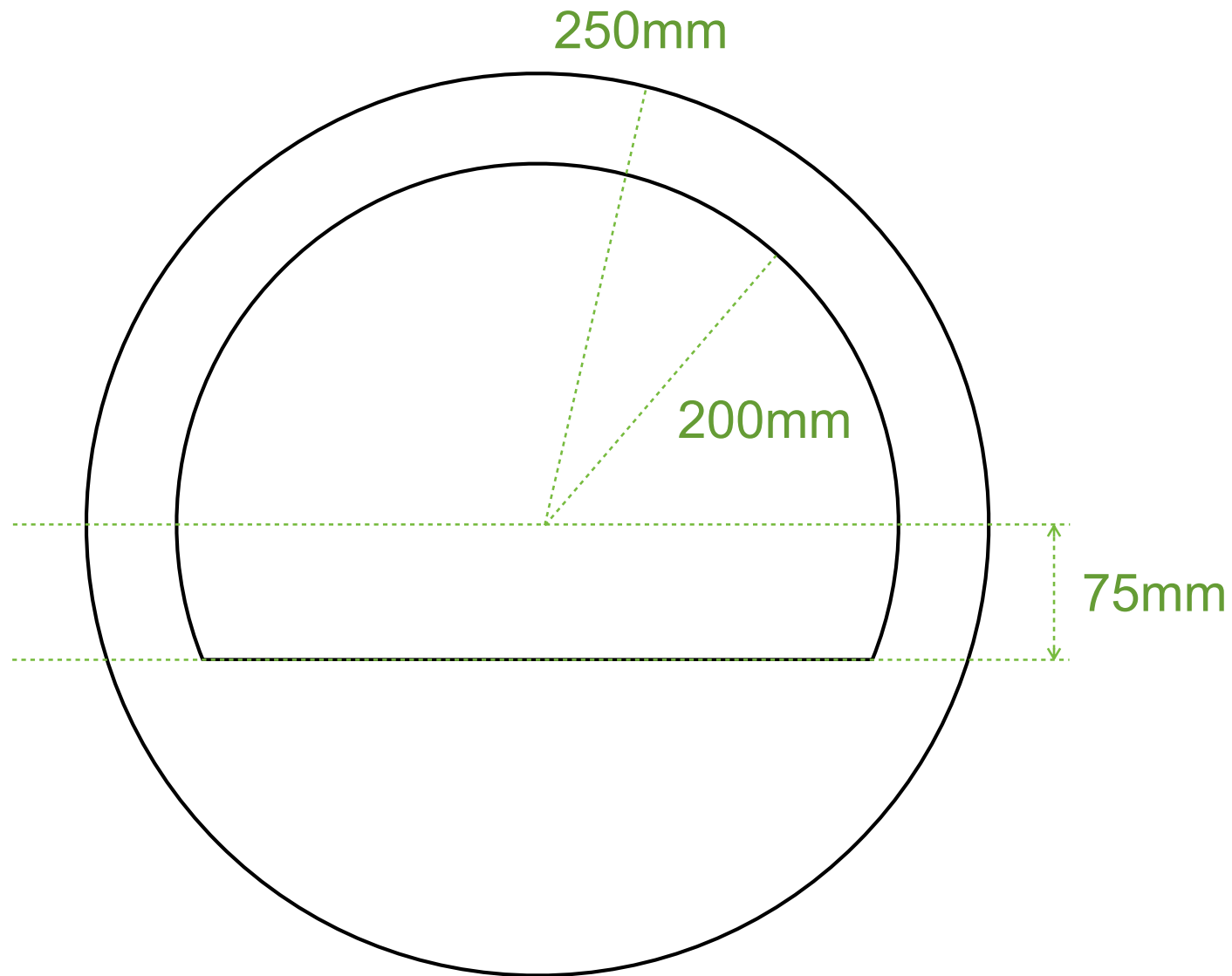
# Summary

- COMET is preparing the staging approach for the  $\mu$ -e conversion search at J-PARC with strong endorsements and supports from KEK/J-PARC.
- COMET Phase-I: Construction start from 2013
  - $B(\mu + \text{Al} \rightarrow e + \text{Al}) < 7 \times 10^{-15}$  @ 90%CL
    - 8GeV-3.2kW proton beam, 12 days
    - 90deg. bend solenoid, cylindrical detector
  - Background study for the phase2
    - transverse tracker+calorimeter
- COMET Phase-II: Stage-1 approved (2009)
  - $B(\mu + \text{Al} \rightarrow e + \text{Al}) < 6 \times 10^{-17}$  @ 90%CL
    - 8GeV-56kW proton beam, 2 years
    - 180deg. bend solenoid, bend spectrometer, transverse tracker+calorimeter



# Backup Slides

# Collimator



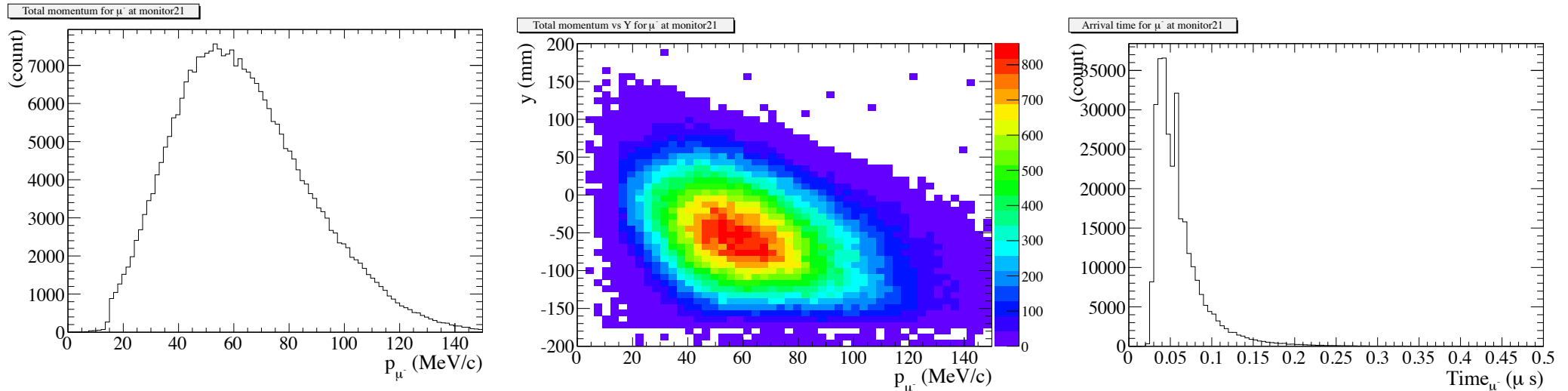
Material : Tungsten

Length = 1000mm

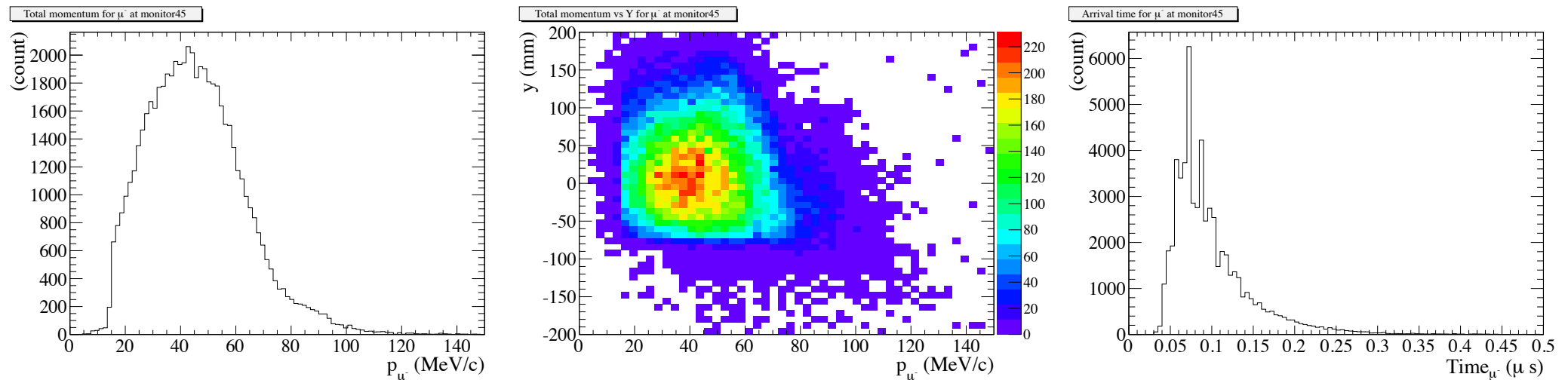


# Muons before/after the collimeter

## monitor21: before the collimator

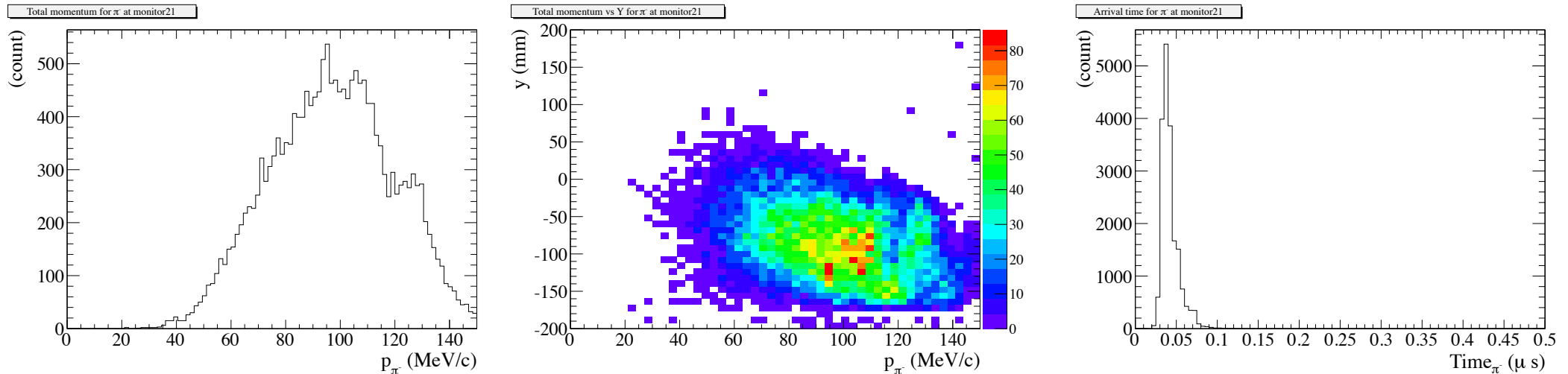


## monitor45: after the collimator (before the stopping target)

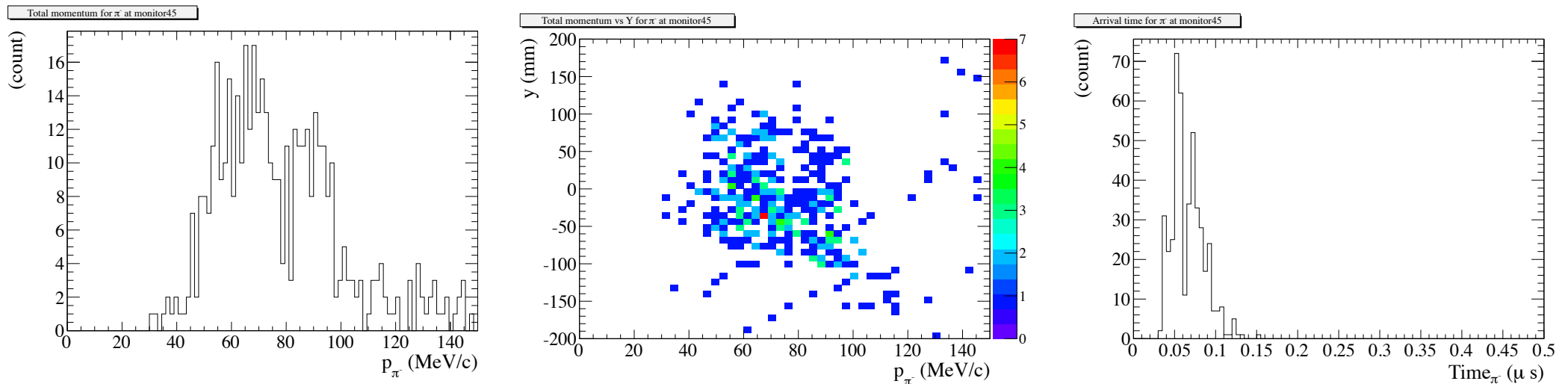


# Pions before/after the collimeter

## monitor21: before the collimator



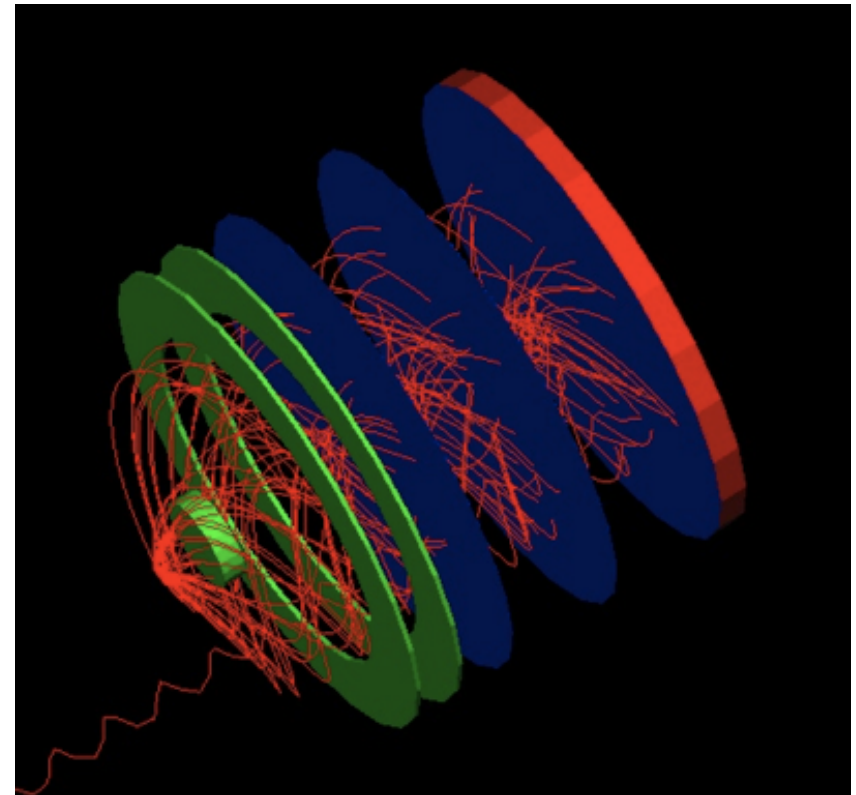
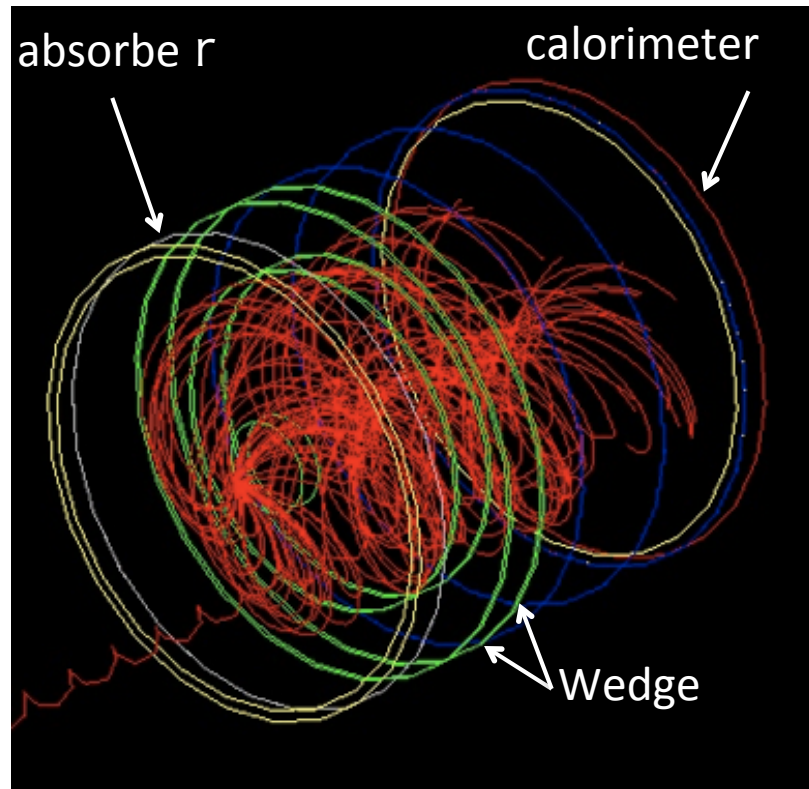
## monitor45: after the collimator (before the stopping target)





# Configuration

- Muon stopping target : 11 points along the beam
- Proton degrader; 500  $\mu\text{m}$ , polystyrene
- Cu Beam Blocker; 200 mm radius, 100mm length
- Two Proton stopping wedges made of Cu, 20 mm thick
- 3 planes of virtual detectors and calorimeter



# Key Points of COMET



# COMET Phase-I / Phase-II and Mu2e

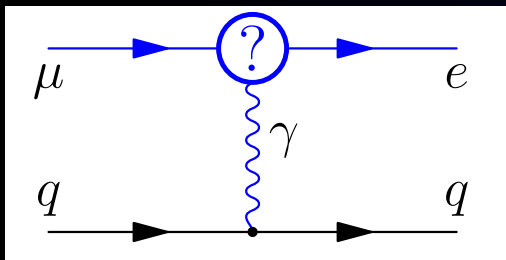
	S.E. sensitivity	BG events at aimed sensitivity	running time (sec)	Year	Comments
COMET Phase-I	$3 \times 10^{-15}$	0.03	$1.5 \times 10^6$	~2016	Proposal (2012)
COMET Phase-II	$3 \times 10^{-17}$	0.34	$2 \times 10^7$	~2019	CDR (2009)
Mu2e	$3 \times 10^{-17}$	0.4	$3 \times (2 \times 10^7)$	~2019	J. Miller's talk at SSP2012

constructive

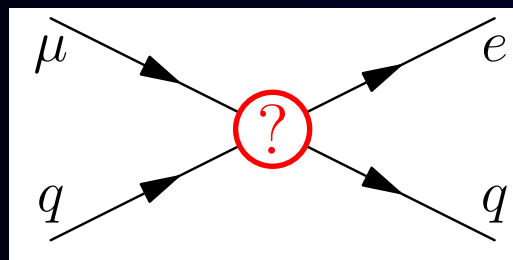
# Physics Sensitivity: $\mu \rightarrow e\gamma$ vs. $\mu$ -e conversion

$$L_{\text{CLFV}} = \frac{1}{1 + \kappa} \frac{m_\mu}{\Lambda^2} \bar{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} + \frac{\kappa}{1 + \kappa} \frac{1}{\Lambda^2} (\bar{\mu}_L \gamma^\mu e_L) (\bar{q}_L \gamma_\mu q_L)$$

Photonic (dipole) interaction



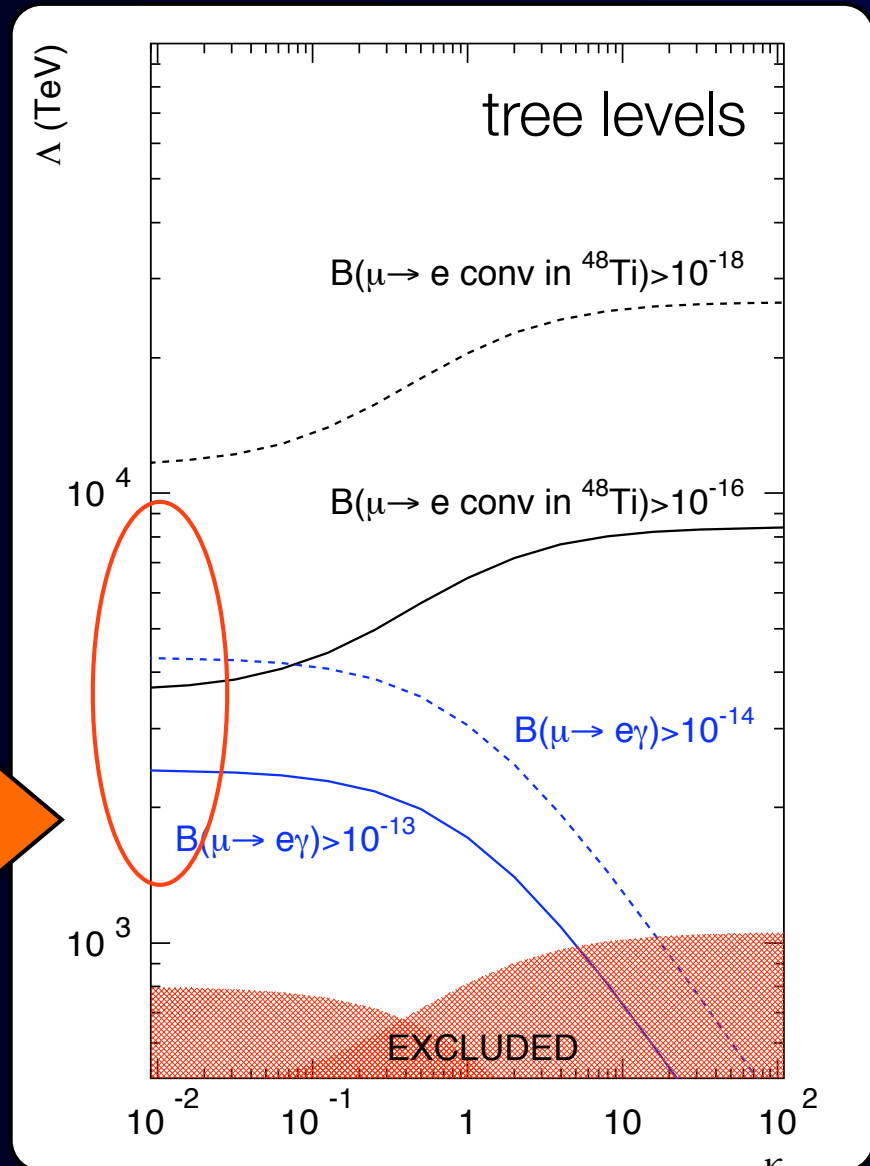
Contact interaction



if photonic contribution dominates,

$$\frac{B(\mu N \rightarrow eN)}{B(\mu \rightarrow e\gamma)} = \frac{G_F^2 m_\mu^4}{96\pi^3 \alpha} \times 3 \times 10^{12} B(A, Z) \sim \frac{B(A, Z)}{428}$$

- for aluminum, about  $1/390 \sim 0.003$
- for titanium, about  $1/230$



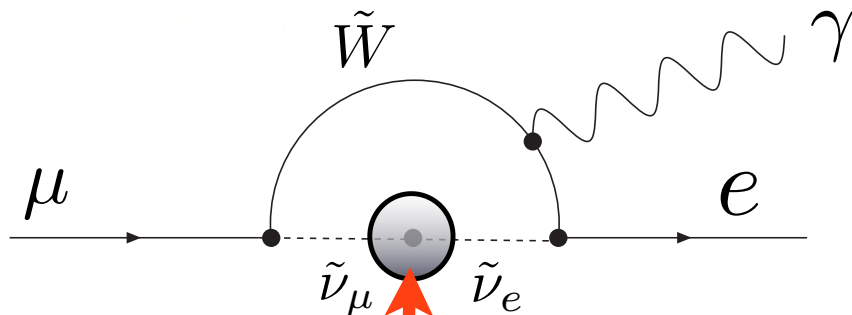


# Example: Sensitivity to Energy Scale of NP Loop contribution in SUSY models

For loop diagrams,

$$\text{BR}(\mu \rightarrow e\gamma) = 1 \times 10^{-11} \times \left( \frac{2\text{TeV}}{\Lambda} \right)^4 \left( \frac{\theta_{\mu e}}{10^{-2}} \right)^2 \quad y = \frac{g^2}{16\pi^2} \theta_{\mu e}$$

> sensitive to TeV energy scale with reasonable mixing



example diagram for SUSY (~TeV)

Physics at about  $10^{16}$  GeV

SUSY-GUT model

SUSY neutrino  
seesaw model

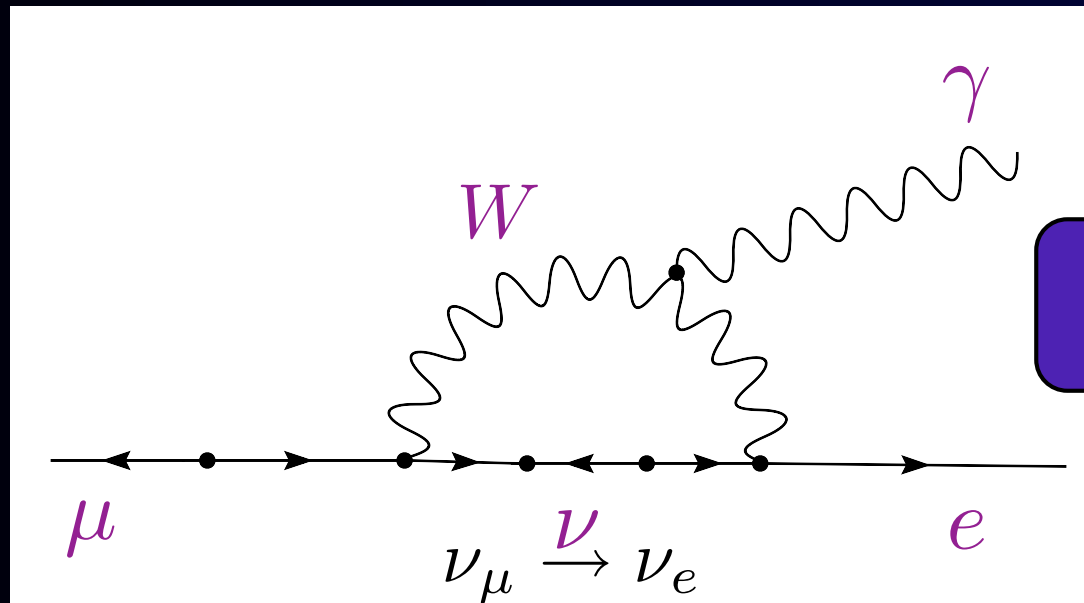
slepton mixing  
(from RGE)

$$(m_{\tilde{L}}^2)_{21} \sim \frac{3m_0^2 + A_0^2}{8\pi^2} h_t^2 V_{td} V_{ts} \ln \frac{M_{GUT}}{M_{R_s}}$$

$$(m_L^2)_{21} \sim \frac{3m_0^2 + A_0^2}{8\pi^2} h_\tau^2 U_{31} U_{32} \ln \frac{M_{GUT}}{M_R}$$

# CLFV in the SM with Massive $\nu$

$$B(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_l (V_{MNS})_{\mu l}^* (V_{MNS})_{el} \frac{m_{\nu_l}^2}{M_W^2} \right|^2$$



$$\text{BR} \sim \mathcal{O}(10^{-54})$$