Neutrino Interactions with Nuclei

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Motivation and Contents

- Determination of neutrino oscillation parameters requires neutrino energy
- Nuclear effects affect neutrino energy reconstruction
- Neutrino interactions in the ,shallow inelastic regime' (Minerva, NOvA): determination of cross sections

Neutrino Oscillations

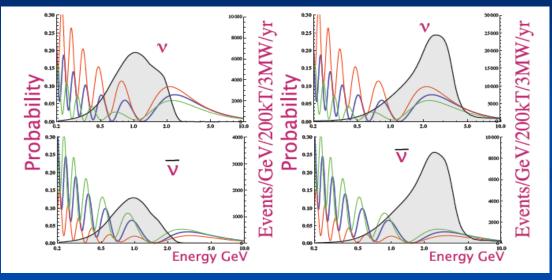
2-Flavor Oscillation:

$$P(
u_{\mu}
ightarrow
u_{e}) = \sin^{2} 2\theta \sin^{2} \left(\frac{\Delta m^{2} L}{4E_{\nu}} \right)$$

Know: L, need E_{ν} to determine Δm^2 , θ



Project X, δ_{CP} sensitivity



From: Bishai et al arXiv:1203.409

$$\delta_{CP} = 0$$

$$\delta_{CP} = \pi/2$$

8 GeV

proton energy

60 GeV

Need energy to distinguish between different δ_{CP}



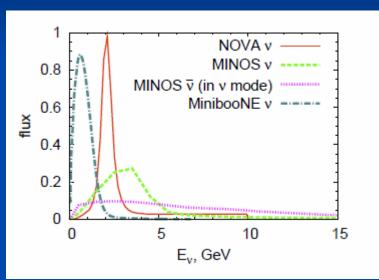


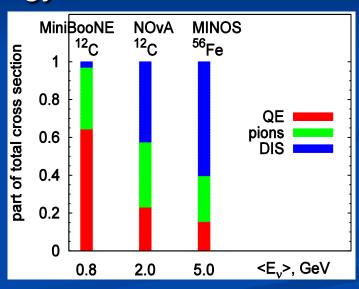
Now to ongoing experiments



Neutrino Beams

Neutrinos do not have fixed energy:



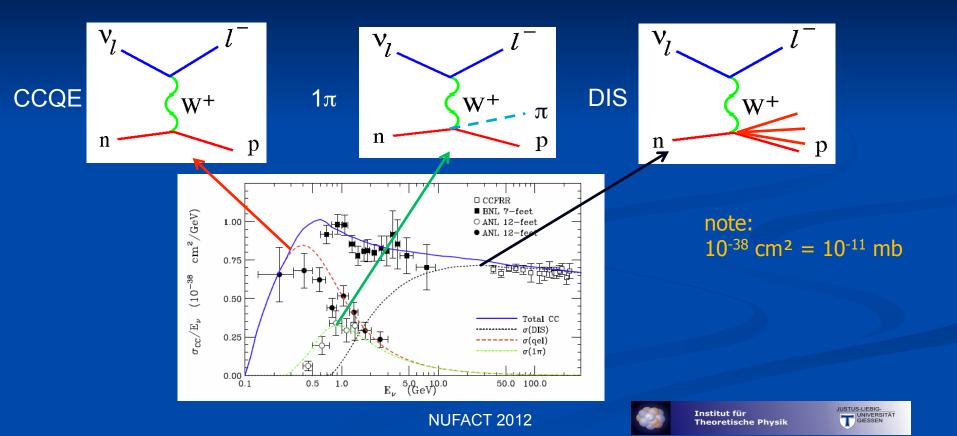


Have to reconstruct energy from final state of reaction



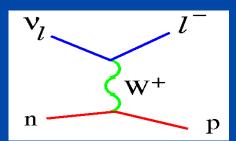


Neutrino-nucleon cross section



Energy Reconstruction by QE

In pure QE scattering on nucleon at rest outgoing lepton determines neutrino energy:



$$E_{\nu} = \frac{2M_{N}E_{\mu} - m_{\mu}^{2}}{2(M_{N} - E_{\mu} + p_{\mu}\cos\theta_{\mu})}$$

- BUT: all modern experiments contain nuclei as targets →
 1. Problem to identify QE
 - 2.effects of binding energy, Fermi motion, Pauli principle

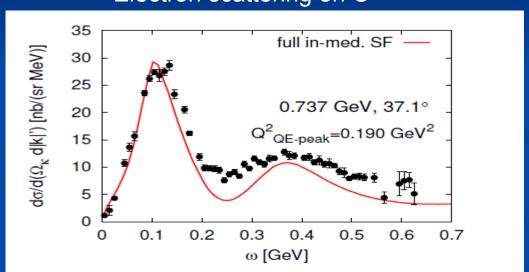




Two Complications to identify QE

Identification of QE Scattering

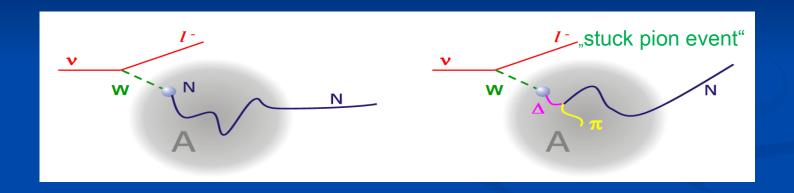
Electron scattering on C



Difficulty to separate processes if neutrino energy is not known



Final State Interactions in Nuclear Targets



Complication to identify QE

Nuclear Targets (K2K, MiniBooNE, T2K, MINOS, Minerva,)

- GiBUU: Theory and Event Generator
 based on an approx. solution of Kadanoff-Baym equations
- Physics content (and code available): Phys. Rept. 512 (2012) 1 http://theorie.physik.uni-giessen.de/GiBUU/
- Gibuu describes (within the same unified theory and code)
 - heavy ion reactions, particle production and flow
 - pion and proton induced reactions
 - low and high energy photon and electron induced reactions
 - neutrino induced reactions

......using the same physics input! And the same code!



Theoretical Basis of GiBUU

- Kadanoff-Baym equation (1960s)
 - full equation can not be solved yet
 - not (yet) feasible for real world problems
 - Boltzmann-Uehling-Uhlenbeck (BUU) models
 - Boltzmann equation as gradient expansion of Kadanoff-Baym equations, in Botermans-Malfliet representation (1990s): GiBUU
 - Cascade models (typical event generators, NUANCE, GENIE, NEUT,..)
 - no mean-fields, primary interacts and FSI not consistent



Theoretical Basis: GiBUU

Time evolution of spectral phase space density (for $i = N, \Delta, \pi, \rho, ...$) given by KB equation in Botermans-Malfliet form:

$$\left[\left(1 - \frac{\partial H}{\partial p_0} \right) \frac{\partial}{\partial t} + \frac{\partial H}{\partial p} \frac{\partial}{\partial x} - \frac{\partial H}{\partial x} \frac{\partial}{\partial p} + \frac{\partial H}{\partial t} \frac{\partial}{\partial p_0} \right] F_i(x, p) = C[F_i(x, p), F_j(x, p)]$$

Hamiltonian *H* includes off-shell propagation correction

8D-Spectral phase space density

Collision term

Off shell transport of collision-broadened hadrons included with proper asymptotic free spectral functions



Practical Basis: GiBUU

- one transport equation for each particle species (61 baryons, 21 mesons)
- coupled through the potential in H and the collision integral C
- W < 2.5 GeV: Cross sections from resonance model (PDG and MAID couplings), consistent with electronuclear physics
- W > 2.5 GeV: particle production through string fragmentation (PYTHIA)
- GiBUU: Only `Neutrino Event Generator' that has widely been tested with various hadronic and em reactions, NO TUNING





GiBUU Ingredients: ISI

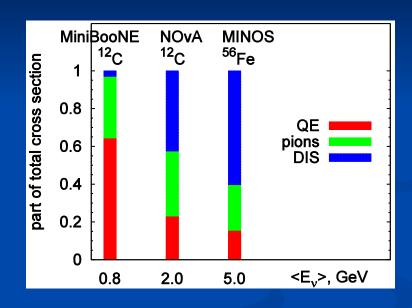
- In-medium corrected primary interaction cross sections, boosted to restframe of moving bound nucleon in local Fermigas
- Includes spectral functions for baryons and mesons (binding + collision broadening)
- Hadronic couplings for FSI taken from PDG
- Vector couplings taken from electro-production (MAID)
- Axial couplings modeled with PCAC





GiBUU Ingredients

- Processes included:
 - CC + NC QE scattering
 - Resonance excitation
 - DIS
- CC FSI for all produced particles



A complete model has to describe all of them

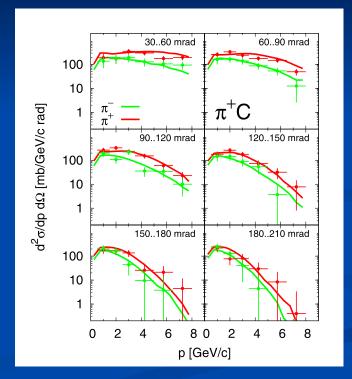


Check: pions in HARP

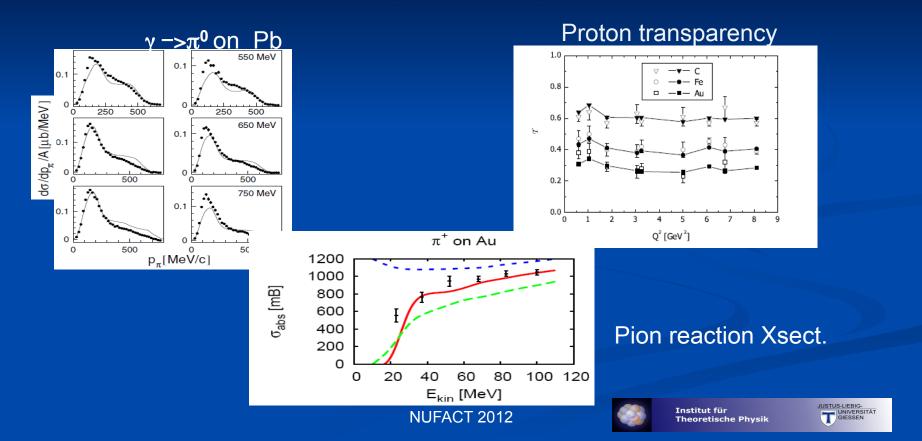
HARP small angle analysis
12 GeV protons

Curves: GiBUU

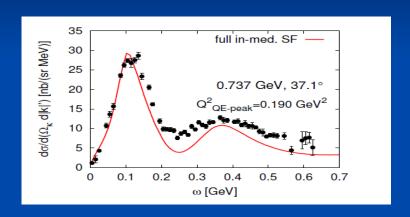
K. Gallmeister et al, NP A826 (2009)

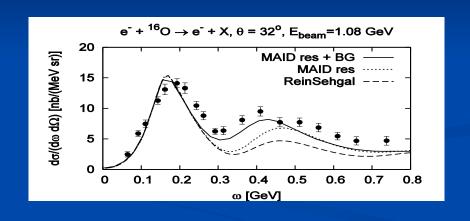


Check: pions, protons



Electrons as Benchmark for GiBUU



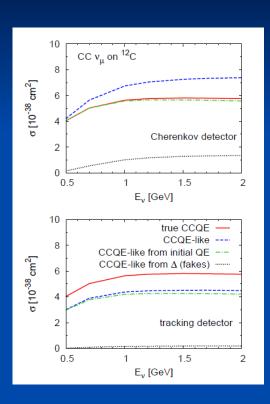


No free parameters!

Rein-Sehgal does not work for electrons! Why should it work for neutrinos?



Event Identification



 Cerenkov detector (MiniBooNE, K2K 1kt, T2K) defines QE by:

```
CCQE: 1\mu^- \ 0\pi^+ \ 0\pi^- \ 0\pi^0 \ xp \ xn
CC1\pi^+: 1\mu^- \ 1\pi^+ \ 0\pi^- \ 0\pi^0 \ xp \ xn
```

Too high QE: misidentifies about 20%, pion-induced fakes

 Tracking detector (Sci-BooNE, K2K, SciFi, T2K) defines QE by

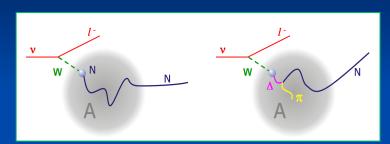
CCQE:
$$1\mu^- \ 0\pi^+ \ 0\pi^- \ 0\pi^0 \ 1p \ xn$$

CC1 π^+ : $1\mu^- \ 1\pi^+ \ 0\pi^- \ 0\pi^0 \ xp \ xn$

QE identification is clean, but 30% of total QE cross section is missed



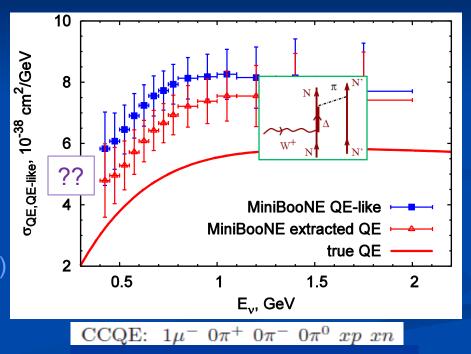
MiniBooNE QE puzzle



QE with FSI

QE-like bgr

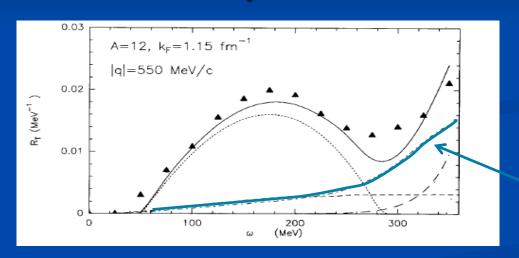
Event generator is used to remove QE-like bgr from QE-like Xsect (blue) and to extract QE Xsect (red)
→ model dependence of QE data



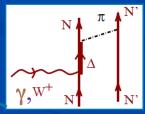


The MiniBooNE QE Puzzle Hint from Electrons: 2p-2h interacts.

Dekker, Brussaard, Tjon (1991): influence of two-body currents



2p-2h events:





2p-2h in GiBUU

arXiv: 1203.2935, PR C (2012)

Model for $v + p_1 + p_2 \rightarrow p_3 + p_4 + \mu$ (no recoil)

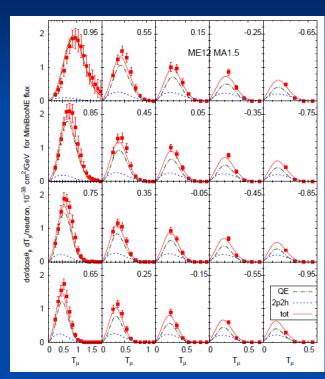
$$\frac{d^2\sigma}{dE'_l d(\cos\theta')} \propto \frac{k'}{k} \int_{NV} d^3r \int \prod_{j=1}^4 \frac{d^3p_j}{(2\pi)^3 2E_j} f_1 f_2 \overline{|M|^2} (1 - f_3) (1 - f_4) \delta^4(p)$$

with flux averaged matrixelement

$$\overline{|M|^2} = \int \Phi(E_{\nu}) L_{\mu\nu} W^{\mu\nu} dE_{\nu}$$

Flux smears out details in W
Constraint from e-scattering:
W contributes to transverse scattering

2p-2h in GiBUU



MB flux averaged

Data corrected for stuck-pion events!

Dotted: 2p-2h contribs, Relatively most important at backward angles (transverse!).

Inclusive double-differential X-sections fairly insensitive to details of 2p-2h interaction



The MiniBooNE QE Puzzle Various, contradictory Explanations

- Change of axial FF only
 - Larger axial mass M_A ≈ 1.3 GeV (exp)
 - Change of axial FF shape (Hill)
- Change of vector FF only (Bodek)
- 2p-2h (Ericsson, Martini, Nieves, Amaro et al)



The MiniBooNE QE Puzzle Explanations

How to decide which one is correct?

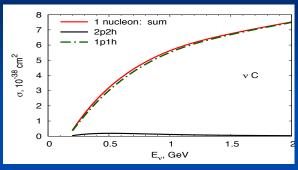
Must not only consider inclusive X-sections, but also exclusive ones:

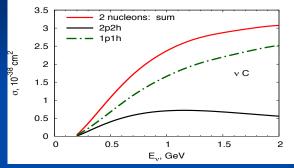
Nucleon Knock-out, numbers and spectra



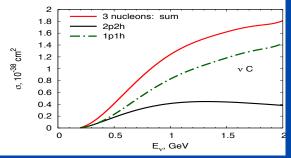


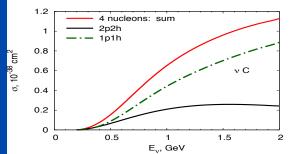
The MiniBooNE QE Puzzle Nucleon Knock-Out











FSI smear out characteristics of primary event





Energy Reconstruction by QE

- All modern experiments use heavy nuclei as target material: C, O, Fe → nuclear complications
- Quasifree kinematics used for QE on bound nucleons:
 Fermi-smearing of reconstructed energy expected
- For nuclear targets QE reaction must be identified to use the reconstruction formula for E_{ν}
- But: exp. definition of QE cannot distinguish between true QE (1p-1h), N* and 2p-2h interactions

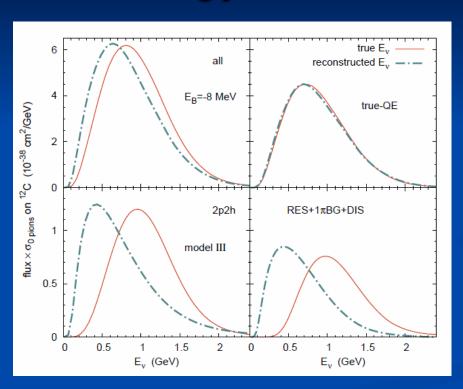
Energy reconstruction

 Entanglement of pion production and QE scattering leads to bias towards lower neutrino energies

- Existence of 2p-2h component divides incoming energy transfer among two nuclei: slower nuclei are interpreted as lower neutrino energy!
 - -> more bias to lower energies



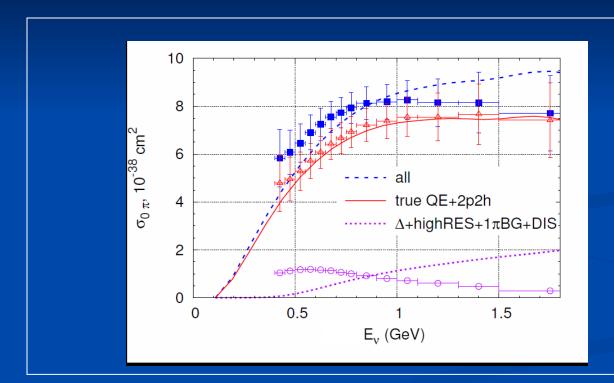
Energy reconstruction in MB



Reconstructed energy shifted to lower energies for all processes beyond QE



Energy reconstruction in MB



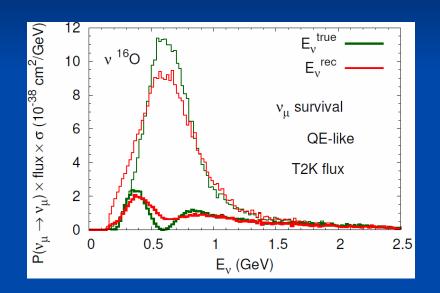
Data: plotted vs
Reconstructed energy

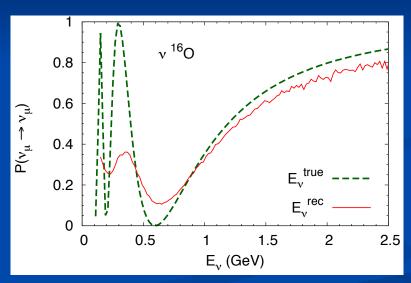
Curves: plotted vs. True energy

Explains strange energy-dependence of stuck pion events



Oscillation signal in T2K v_µ disappearance

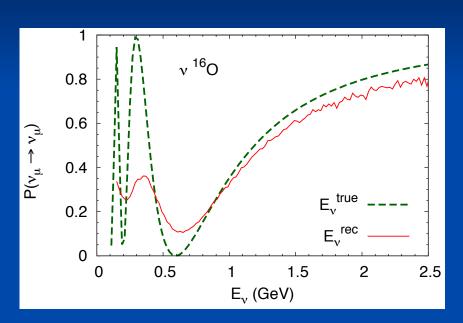


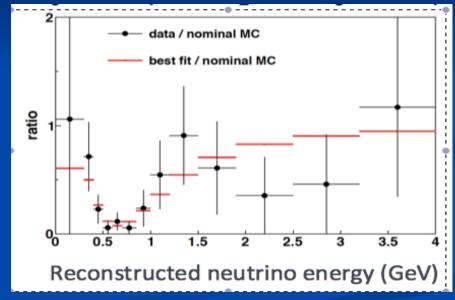


Ratio = oscillation probability

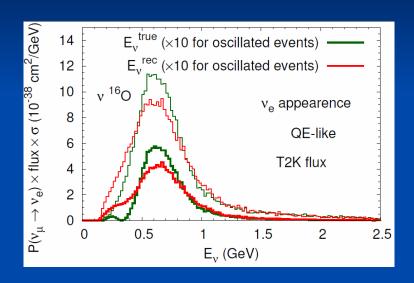


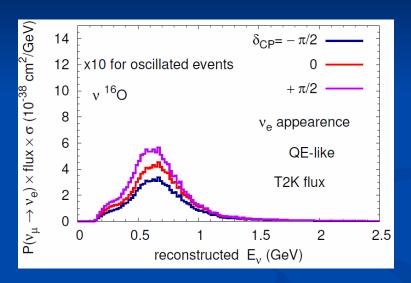
Oscillation signal in T2K ν_μ disappearance





Oscillation signal in T2K δ_{CP} sensitivity

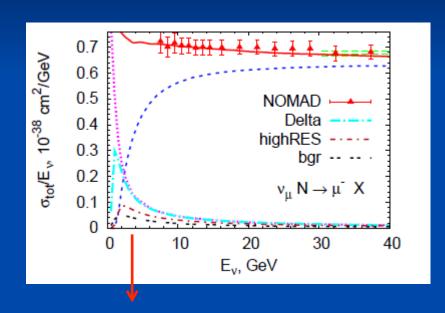


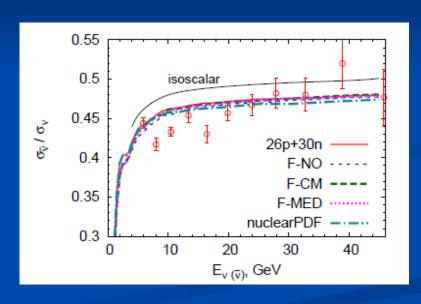


Uncertainties due to energy reconstruction as large as δ_{CP} dependence



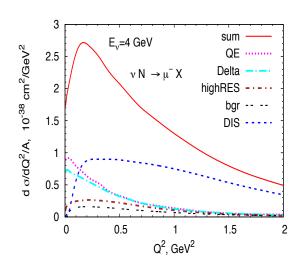
Phys. Rev. C86 (2012) 014607

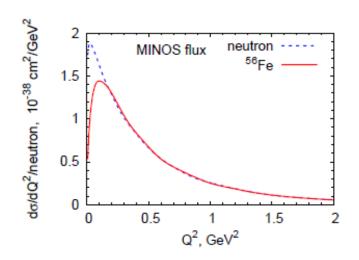




Shallow Inelastic Region

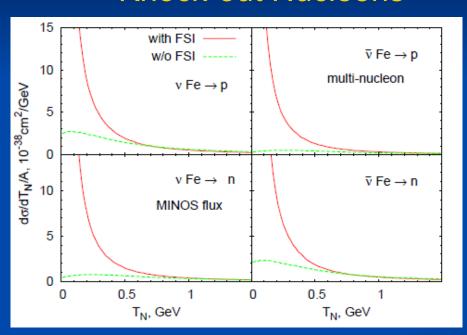




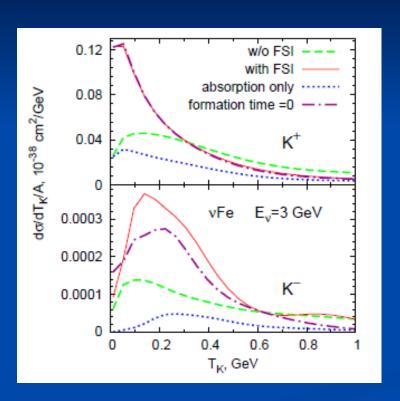


Q² dependence similar to lower-energy MB experiment

Knock-out Nucleons



Strong rise below 300 MeV, dominated by FSI



Lesson for Minerva:

The particles you measure are not those that the neutrino produced. Secondary production is important

Summary

- Event generators for neutrino-nucleus interactions have to describe QE, π produktion and DIS simultaneously
- Due to flux average reaction types are closely entangled
- MB puzzle of high axial mass explained: contains 2p-2h
- Energy reconstruction based on QE leads in Cerenkov detectors to downward shift of reconstructed distribution
- FSI are extremely important, may make the extraction of elementary neutrino-particle production rates impossible



Importance of Generators

- Two points of view:
 - A good generator does not have to fit the data, provided it is right
 - A good generator does not have to be right, provided it fits the data
- Let us strive for a generator that is ,right' and as much state-of-the-art as the experimental equipment is!



Need for solid nuclear physics theory suport in Neutrino Physics



"What we especially like about these theoretical types is that they don't tie up thousands of dollars worth of equipment."

