

# On measuring two-body current contribution to neutrino inclusive cross section

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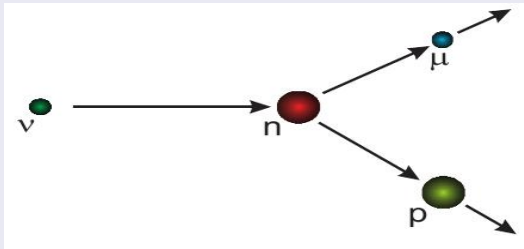
## Outline

- Motivation
  - What is charge current quasi-elastic (CCQE) interaction?
  - Experimentalist definition of CCQE.
  - Axial mass puzzle; MiniBooNE 2D data.
  - Energy reconstruction (back-up slides).
- Two-body current - theoretical models.
- Multinucleon knock-out model.
- Two-body current - experimental aspects:
  - Two reconstructed knock-out protons.
  - Integrated knock-out proton kinetic energy.
  - Other approaches.
- Outlook.

## Quasielastic reaction on a free nucleon target

$$\nu_l + n \rightarrow l^- + p,$$

$$\bar{\nu}_l + p \rightarrow l^+ + n.$$



Everything is clear. There are a muon and a proton in the final state.

## Nuclear target reaction

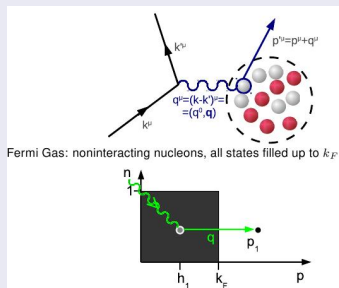
We would like to use the same definition in neutrino-nucleus reactions.

Complications:

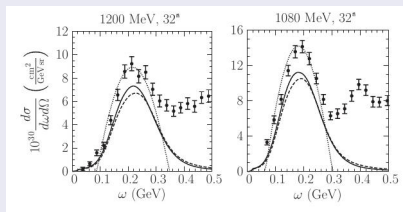
- Can we assume that neutrino sees nucleus as composed of quasi-free nucleons (validity of impulse approximation (IA))?...
- What is an experimental *definition* of CCQE? A muon and a proton in the final state, as before (impact of final state interaction (FSI) effects)?...

## Impulse approximation – Fermi gas model

In the IA we assume that nucleons are quasi-free like in Fermi gas model. Correct?...



from Jakub Zmuda



from A. Ankowski, JTS, Phys. Rev C77 (2008)

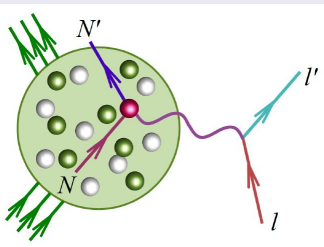
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Electron scattering: In wide kinematical region IA works quite well.

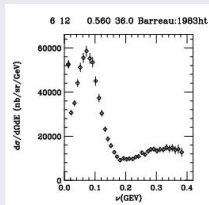
Electron energy and scattering angle are fixed.



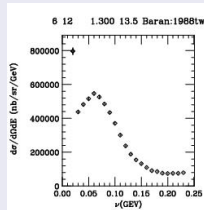
## Impulse Approximation (IA) - limitations



from Artur Ankowski



Electron carbon  
data

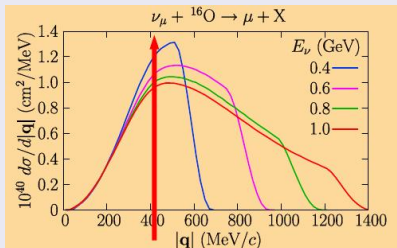


Think about de Broglie wave and remember  $1 \text{ fm} \sim (200 \text{ MeV})^{-1}$ . If momentum transfer is 200 MeV spatial resolution is 1 fm. If momentum transfer is smaller than  $\sim 300 \text{ MeV}$  IA becomes problematic. In fact, for small energy transfers one can see giant resonances.

## Impulse approximation (IA) - limitations

In electron scattering one can select a kinematical region in which IA is reliable.

In neutrino experiments beams are always rather wide-band and above is impossible. How much of the cross section come from the low momentum transfer region?



from Artur Ankowski

Remedy: include RPA, or better CRPA, corrections.

Usually  $Q^2$  is used, where  $Q^2 = q^2 - \omega^2 \geq 0$ . Low  $|\vec{q}|$  translates to low  $Q^2$ .

There are always many “CCQE” events with small  $q$  (or  $Q^2$ ).



## How do experimentalists define CCQE?

### MiniBooNE

- Only 2 *subevents* (Cherenkov light from muon and then from electron).
- No assumptions about proton.
- Most of CC events with pions give rise to 3 subevents.

### NOMAD

- 1- and 2-track events (muons and protons with  $p > 300 \text{ MeV}/c$ ).
- Several cuts are imposed to eliminate the (pion) background.

**Do MiniBooNE and NOMAD measure the same?!...**



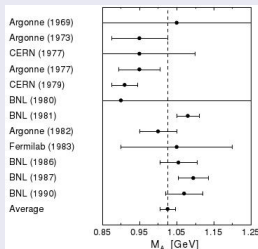


## CCQE axial mass puzzle

In a basic theory of CCQE the only unknown quantity is  $M_A$ , axial mass,

Until a few years ago it seemed that  $M_A$  measurements converge to a value  $M_A \sim 1.03$  GeV.

There is a tension between old, mainly deuterium (left), and recent heavier target (right)  $M_A$  measurements.



Experiment	Target	Cut in $Q^2$ [GeV <sup>2</sup> ]	$M_A$ [GeV]
K2K <sup>g</sup>	oxygen	$Q^2 > 0.2$	$1.2 \pm 0.12$
K2K <sup>g</sup>	carbon	$Q^2 > 0.2$	$1.14 \pm 0.11$
MINOS <sup>g</sup>	iron	no cut	$1.19 \pm 0.17$
MINOS <sup>g</sup>	iron	$Q^2 > 0.2$	$1.26 \pm 0.17$
MiniBooNE <sup>h</sup>	carbon	no cut	$1.35 \pm 0.17$
MiniBooNE <sup>h</sup>	carbon	$Q^2 > 0.25$	$1.27 \pm 0.14$
NOMAD <sup>g</sup>	carbon	no cut	$1.07 \pm 0.07$

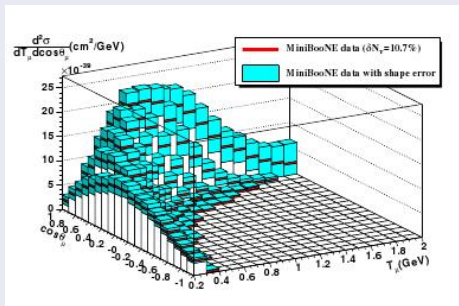
[from Bernard, Elouadrhiri, Meissner]



## MiniBooNE double differential cross section data

The most interesting recent CCQE data comes from the MiniBooNE experiment.

The data is available in a form of double differential cross section in muon: kinetic energy and production angle:



A.A. Aguilar-Arevalo et

al., [MiniBooNE collaboration]

Phys. Rev. D81, 092005 (2010)

The best fit value is

$$M_A^{eff} = 1.35 \pm 0.17 \text{ GeV},$$

$\kappa = 1.007 \pm 0.012$  (to cure low  $Q^2$  problem).

Similar values of  $M_A^{eff}$  were obtained from shape only and normalized cross section analysis.



## Effective axial mass?!...

It is a fit in a particular experimental situation (flux, detector, selection of events,...).

We need more universal description of the data, **we need a theory.**

## What is there in the MB signal?

Background events come mostly from pion absorption. This background is subtracted from the CCQE-like sample of events.

NUANCE (Monte Carlo (MC) event generator used by MiniBooNE) assumes certain fraction of pionless  $\Delta$  decays and such (MC) events are also subtracted (a very confusing point).

Hypothesis: there is a large two-body current multinucleon knock-out contribution to the inclusive CC cross section.



## Two-body current – basic intuition

One-body hadronic current operator:

$$J^\alpha = \cos \theta_C (V^\alpha - A^\alpha) = \cos \theta_C \bar{\psi}(p') \Gamma_V^\alpha \psi(p)$$

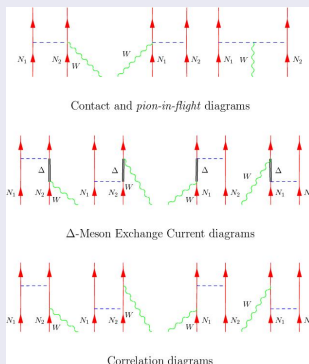
In the second quantization language  $J^\alpha$  is the operator which annihilates (removes from the Fermi sea, producing a hole) a nucleon with momentum  $p$ , and creates (above the Fermi level) a nucleon with momentum  $p'$ :

$$J_{1body}^\alpha \sim a^\dagger(p') a(p)$$



## Two-body current – basic intuition

Think about more complicated Feynman diagrams:



$$J_{2\text{body}}^\alpha \sim a^\dagger(p'_1) a^\dagger(p'_2) a(p_1) a(p_2)$$

can create two particles and two holes (2p-2h).

## Microscopic models

- M. Martini, M. Ericson, G. Chanfray, J. Marteau (MEChM – based on Marteau PhD thesis  $\sim$  2000)
- J. Nieves, I. Ruiz-Simo, M.J. Vicente-Vacas
- J.E. Amaro, M.B. Barbaro, J.A. Cabbalero, T.W. Donnelly, C.F. Williamson, J.M. Udias

The models provide muon inclusive 2D cross section and a separate problem is to get predictions for final state nucleons.

## Effective models

- Bodek, et al
- Lalakulich, Mosel, et al model
- Steve Dytman model in GENIE.



## Some comments

- There are large differences between the theoretical models predictions, by a factor of 2.
- There a controversy how large is two-body contribution in antineutrino scattering.
- Nieves et al stress a role of RPA effects: they must be included in order to reproduce the MiniBooNE data.
- There is an intriguing result of Carlson et al: for light nuclei in order to get observed (in the electron scattering) two-body current contribution one must use more realistic ground state than Fermi gas model (used in all the neutrino microscopic models...).

## Terminology

Meson exchange current (MEC)



two-body current



$n$  particles  $n$  holes ( $np - nh$ )

However, sometimes the term *MEC* refers only to a smaller subset of *two-body current* Feynman diagrams which lead to *np-nh* final states.



## How to distinguish CCQE and two-body current events?

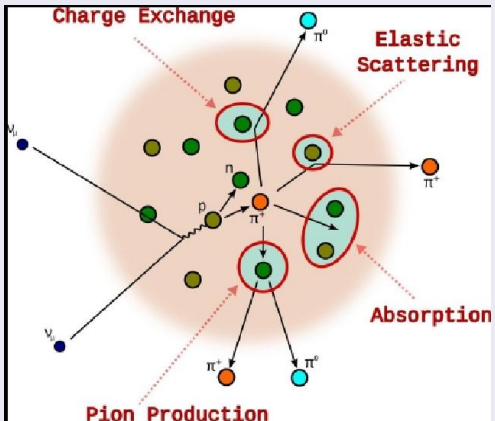
It is not enough to study muons.

One must analyze nucleons in the final state.

For that one needs theoretical predictions.

FSI effects are very important and a model giving predictions for nucleons after MEC events must be combined with a MC event generator (or hadronic transport code like GiBUU).

## Relevance of Final State Interactions



from Tomasz Golan.

The cartoon is for pions, but analogous effects are experienced by nucleons.



## The model

Based on JTS, arXiv:1201.3673[hep-ph]; to be published in Phys. Rev C.

A main idea: use as an input any model which gives predictions for the two-body contribution to the muon inclusive cross section and make predictions for the final state nucleons.

Two such muon scattering models will be used in numerical computations:

- Bodek et al TE model
- Marteau inspired model, not exactly the MEChM model, but similar in many respects

Both models are implemented in NuWro MC event generator.

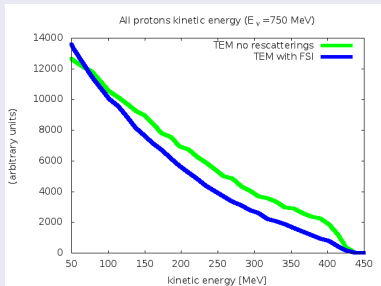
## The model of the nucleon knock-out

We use only muon information.

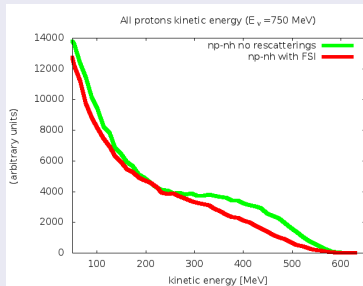
- We know muon's kinetic energy and production angle.
- Equivalently, we know momentum and energy transfer.
- We select 2(3) nucleons from the Fermi sea.
- We add the energy and momentum transferred to the hadronic system.
- We perform a boost to the hadronic center-of-mass frame (CMF).
- In the CMF we select isotropically 2(3) nucleons in the final state.
- We perform boost back to the laboratory frame.
- Energy balance must be consistent with FSI model.
- Event's weight is given by muon differential cross section.



## Predictions – relevance of FSI effects (1)



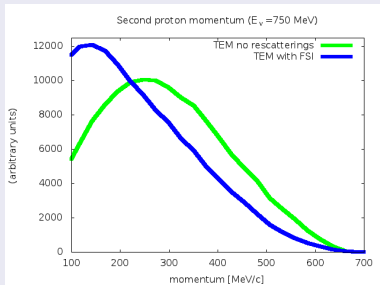
Effective transverse enhancement model.



Microscopic model.

Predictions from two models implemented in NuWro are compared.  
Due to FSI effects protons become less energetic.

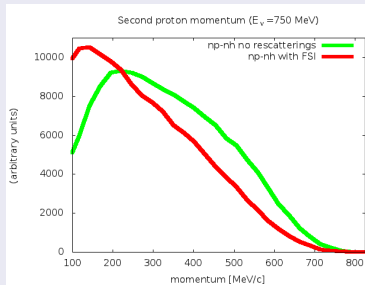
## Predictions – relevance of FSI effects (2)



Effective transverse enhancement model.

If the second proton is energetic enough we can see a pair of protons in one event.

The second energetic proton can have quite large momentum!



Microscopic model.

## How to measure the two-body current contribution?

- Of interest are CCQE-like events, with no pions in the final state; one needs a strong veto on pions.
- One can use the information contained in reconstructed proton tracks and also in the *vertex activity*.
- It is better to have a low threshold for reconstruction proton tracks.
- The quality of FSI model is very important, real pion absorption seems to be the most important background.
- Observables like integrated kinetic energy seem to be less affected by FSI.



## IDEA 1: Pairs of reconstructed knocked-out protons

TE model. Predicted number of proton pairs with both momenta above various threshold values and two threshold values of the  $\pi^\pm$  momentum. Simulations done for the 750MeV muon neutrinos. The number of generated events is  $2.5 \cdot 10^5$ .

$\pi^\pm$ cut [ $\frac{MeV}{c}$ ] $\downarrow$	proton cut [ $\frac{MeV}{c}$ ] $\rightarrow$	300	400	500
0	signal	5457	2271	651
	background	13780	7961	2267
200	signal	5465	2271	651
	background	16112	8691	2349





## IDEA 1: Pairs of reconstructed knocked-out protons

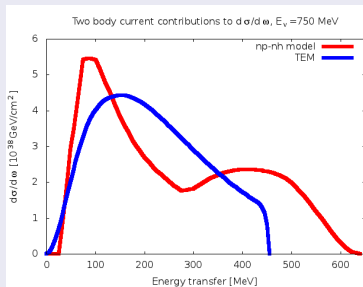
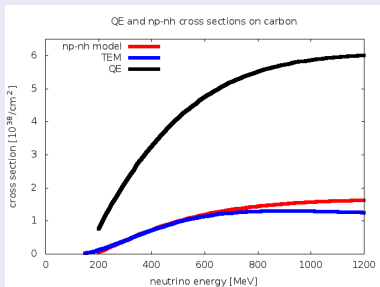
Microscopic model. Predicted number of proton pairs with both momenta above various threshold values and two threshold values of the  $\pi^\pm$  momentum. Simulations done for the 750MeV muon neutrinos. The number of generated events is  $2.5 \cdot 10^5$ .

$\pi^\pm$ cut [ $\frac{MeV}{c}$ ] $\downarrow$	proton cut [ $\frac{MeV}{c}$ ] $\rightarrow$	300	400	500
0	signal	7185	4201	1805
	background	13774	7928	2311
200	signal	7231	4201	1805
	background	16158	8577	2388



## IDEA 1: Pairs of reconstructed knocked-out protons

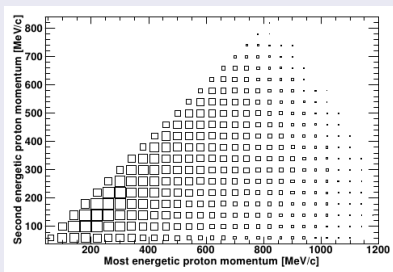
Model predictions for the proton pairs above 500 MeV/c signal differ by a factor of 3. Why?



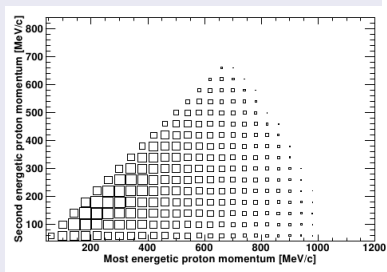
In the microscopic model typical energy transfers are larger which translates into more energetic protons.

## IDEA 1: Pairs of reconstructed knocked-out protons

Of interest can be also 2D distributions of two most energetic protons:



Microscopic model.



TE model.



## IDEA 1: Pairs of reconstructed knocked-out protons; resumé

A probability to have an event with two protons above 500 MeV/c is 0.26...0.72%. For a 400 MeV/c threshold a probability is 0.9...1.7%,

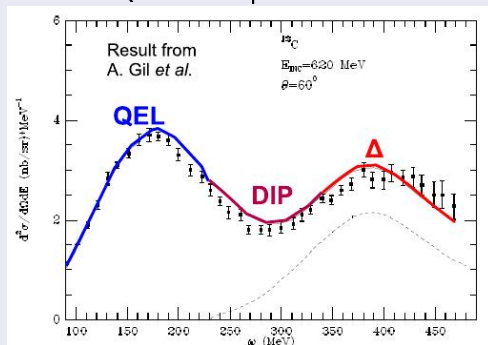
For the 500 MeV/c threshold signal/background ratio is 0.28 ... 0.75.

Which is an uncertainty in NuWro background estimation? For  $E=1$  GeV a comparison with GENIE: an agreement is within 30-50% (GENIE predicts the background to be smaller)

I thank Steve Dytman for providing me results of GENIE simulations.

## IDEA 2: Integrated knocked-out protons kinetic energy

Two-body current events are believed to populate a DIP region between QE and  $\Delta$  peaks:



A. Gil, J. Nieves and E. Oset, Nucl. Phys. A 627 (1997) 543;

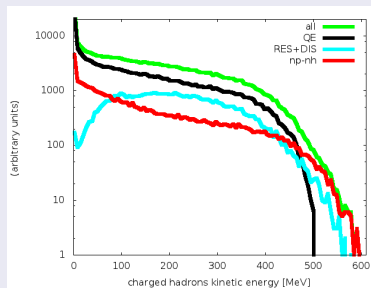
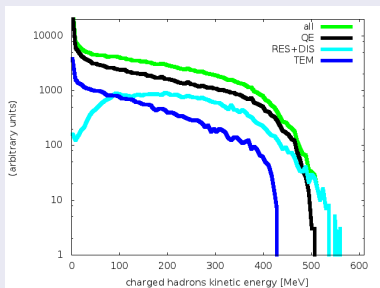


## IDEA 2: Integrated knocked-out protons kinetic energy

Define two observables:  $\sum_j T_j$  and  $\frac{\sum_j T_j}{E_\mu}$ , where  $T_j$  is the kinetic energy of charged hadron. We include all the kinetic energy: both reconstructed hadrons and blobs.

Assume, all  $\pi^0$  and  $\pi^\pm$  with momenta above 200 MeV/c are detected. Events with detected pions are not included in the analysis.

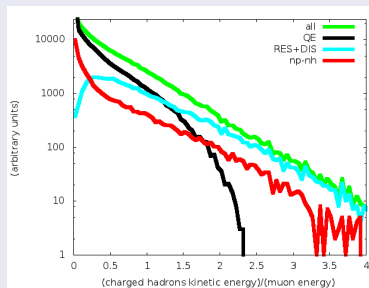
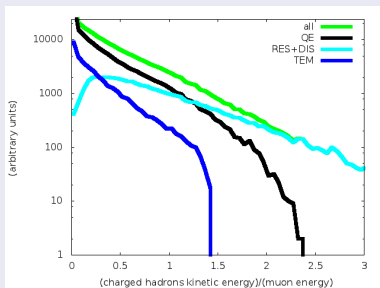
## IDEA 2: Integrated knocked-out protons kinetic energy



Various dynamical mechanisms contribute with different shapes. From the measured shape one can try to deduce existence of the MEC contribution.



## IDEA 2: Integrated knocked-out protons kinetic energy



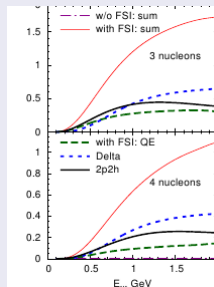
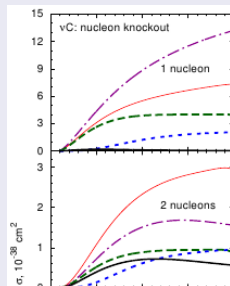
Muon energy sets energy scale of an event. From the measured shape one can try to deduce existence of the MEC contribution.





## Other approaches (1)

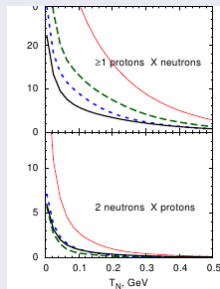
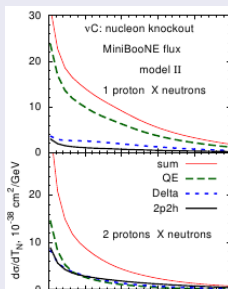
Until now, we discussed a model described in arXiv:1201.3673.  
The same problem is discussed by Lalakulich, Gallmeister, Mosel, arXiv:1203.2935.



2p2h contributes to 2,3,4 nucleon knock-out, but there are also large contributions from QE (due to FSI) and  $\Delta$ .

## Other approaches (2)

Which are energies of knocked-out nucleons?



For 2 protons probably a sum of kinetic energies of protons/nucleons is shown. It is very difficult to compare models predictions because results are given in different formats.



## Outlook

- During last three years (since NuInt09 in Sitges) there has been a lot of discussions about two-body current contribution to muon inclusive cross section.
- Theorists proposed various models.
- It is time to try to measure the effect by looking at final state nucleons.
  - In some models (Martini et al) the contribution is really large.
  - The task is not easy and requires reliable simulation tools to describe nucleon propagation in nuclear matter.

But still...

- ... hopefully, there is a chance to see the effect or at least to put constraints on theoretical models.

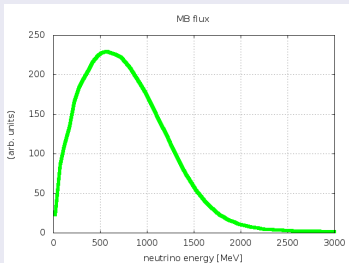
Thank you for your attention!

## Energy reconstruction (1)

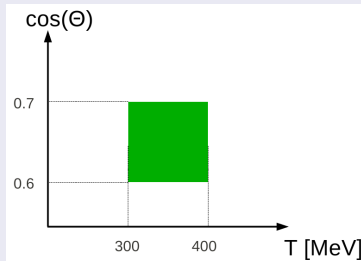
If one infers about neutrino energy based on an detected muon only, MEC events introduce a bias.

A case study. Consider only CCQE and MEC events.

Consider MiniBooNE  
neutrino flux...



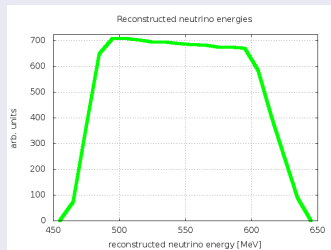
... and a particular 2D muon  
bin



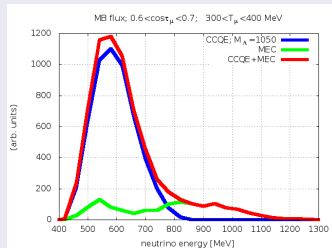
## Energy reconstruction (2)

Then...

... neutrino energies calculated using a standard reconstruction formula are:



... while true neutrino energies are:



Notice a large true neutrino energy tail coming from the two-body current contribution.

From J. Morfin, JTS, poster presented at NEUTRINO 2012.

## Energy reconstruction

The problem of neutrino energy reconstruction is studied in detail in:

M. Martini, M. Ericson, G. Chanfray, *Phys.Rev.* **D85** (2012) 093012.

O. Lalakulich, K. Gallmeister, U. Mosel, *Many-Body Interactions of Neutrinos with Nuclei - Observables*, arXiv:1203.2935 [nucl-th].

D. Meloni, M. Martini, *Revisiting the T2K data using different models for the neutrino-nucleus cross sections*, arXiv:1203.3335 [hep-ph].

J. Nieves, F. Sanchez, I. Ruiz Simo, M.J. Vicente Vacas, *Neutrino Energy Reconstruction and the Shape of the CCQE-like Total Cross Section*, arXiv:1204.5404.

